### HANDBUCH; DER ASTROPHYSIK

#### HERAUSGEGEBEN VON

#### G EBERHARD · A KOHLSCHUTTER H LUDENDORFF

BAND V / ZWEITE HALFTE
DAS STERNSYSTEM

ERSTER TEIL



BERLIN VERLAG VON JULIUS SPRINGER 1933

### DAS STERNSYSTEM

ERSTER TEIL

II

BEARBEITET VON

HEBER D. CURTIS · B. LINDBLAD K. LUNDMARK · H. SHAPLEY

> MIT 118 ABBILDUNGEN UND 2 TAPELN





BERLIN VERLAG VON JULIUS SPRINGER 1933



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		into four groups according to bolometric magnitude, while von Zeifel and
		LINDGREN had divided them into four colour-groups, called g-giants, b- and
		a-type stars, f-dwarfs, and g-dwarfs Their results are given in the second part
		of the table together with the mean absolute bolometric magnitudes computed
		by Wallenguist for the different colour-groups used. In both cases the mass
		of the stars in the second group has been selected as unity
		The state of the s

#### Chapter 4.

# Luminosities, Colours, Diameters, Densities, Masses of the Stars.

By

#### Knut Lundmark-Lund

(Continued.)

With 12 Illustrations.

#### d) The Dlameters of the Stars.

190. The Diameters of the Stars. Earlier Conceptions. Pioneer Work. The underestimation of the distance and the dimensions of the Sun that was a dominating feature of Greek astronomy, was adopted by the astronomers of the Occident and believed until the end of the 17th century Practically nothing was known about the physical nature of the stars until that time. The distances of the stars also were underestimated and that fact may explain why many observors thought that the stars displayed measurable diameters. It is clear that it was the irradiation and diffraction that deceived the pioneers. In order to illustrate the kind of rôle these phenomena sometimes play we quote some measurements of the "diameters" of different magnitudes

Apparent magnitude	Саврамия	TYCHO PRABE	MAGIFUE <sup>2</sup>	LANDS- BERGIUS	VAN DEN HOVA	HISCHOLI <sup>®</sup>	Hewst, and
1**	480" 360	120"	600" 330	60" 40	6"	13",7-16",7	
3	240	90 65	240	30	5	7 .9-12 .3	3,8
\$	180 120	45 30	180 120	10	3	6,2 5,3	3,2 2,5
6	60	20	60	5	2	4,4	2,0

KEPLER<sup>8</sup> who must have had a poor eyesight, although not so poor as MAGINUS and CARDANUS, thought at first that the brightest stars displayed diameters of 240" (Sirius), but, after the invention of the telescope, he states that when a larger magnification is used the diameters become smaller. He was con-

Novas coolestium orbium theoricae. Moguntiael (1608)

Uranometria, Middalburgi (1631).

Almagestum novum I, p. 424, 716 (1651).
 Mercurius in Solo visus, p. 92. Godani (1662)

<sup>1</sup> Libelli duo, unus de supplemento almenceh etc Norimbergeo (1543)

S Opera omnia 2, p 429 (1925); Astronomiae instauratae progymnasmata. Pragae (1602)

HORTENSIUS, Landsbergii commentationes in motum terrae Middelburgi (1630)

Opera II, p 676, 689 (1859) Opera VI, p 335 (1866)

vinced that the stars had no appreciable diameters, but were "puncta mera" I Horrocks also was of the same opinion A little later A Kirchi R<sup>2</sup> called attention to the optical phenomena tending to increase the size of small discs (e g diffraction) and concluded that the estimates of stellar diameters are ıllusoi y.

The thought that the stars displayed such appreciable diameters and the fact that no parallaxes could be derived from his observations convinced Tycho Brahl that the heliocentric system was not tenable and seem to have made

him start his short-lived compromise-system

The experiences of the telescope made it gradually clear that the diameters of the stars must be very small Ilooke4 concluded that the dimensions of the stars were below 1" and later E HALLEY reached the same conclusion

It was clear to J Michiell that even in the case of Shius the apparent angular diameter must be less than 0",01 He pointed out that if the "native brightness" was in accordance with colour the white stars would have the largest

The different conceptions regarding the diameter of Sixus since the middle ages are illustrated from the following summary

Authority	Diameter of Sirius	Authority	Diameter of Sirins
ALBATEGNIUS KEPLER GALILFI VAN DLN HOVE RICCIOLI	45"	Hewelke	6",57
	(240)	J Cassini	5
	5,3	Michell	0 ,01
	10	W Herschel	<0 ,01
	18	Actual value	0 ,0053

W. Herschel' examined a number of bright stars and used extremely high magnifying power in order to determine whether the stars have sensible dimensions He found that the telescopic discs appeared smaller with increasing telescopic power and accordingly he considered spurious the discs of light seen in telescopes He also used this phenomenon as a ready criterion for determining whether a small bright body has an appreciable size or only impresses the sense of sight by virtue of its intrinsic brightness

In 1835, F M Schwerd suggested a method for determining the diameters of the stars which is based on measurements with two different telescopes in order to eliminate the influence of the diffraction and concluded that the

diameter of Altair is 0",104

The method applied by S STAMPFER<sup>9</sup> in 1852 is of much interest. The image of the Sun observed through a telescope was reduced through a globe of Mercury until it matched the image of a star seen in the same telescope Stampfer concluded that the diameter of the first magnitude stars is 0",00491, which is a little to low, but of the right order of magnitude (0",0085)

<sup>2</sup> Ars magna lucis et umbrae, p 119 Romae (1646) Opera omnia 2, p 429 (1925), Astronomiae instauratae progymnasmata Pragae

(1602) An Attempt to prove the Motion of the Earth, p 26 London (1674)

<sup>8</sup> London Phil Trans p 853 (1718), p 3 (1720)

Wien Denkschr Akad Wiss II Cl 5, p 91 (1852)

6 London Phil Trans p 234 (1767) 7 Collected Works II, p 297 (1912)

<sup>&</sup>lt;sup>1</sup> Venus in Sole visa anno 1639, p 139, edited by HFVELIUS, see Note 7, p 575, De magnitudine fixarum Opera, p 61 (1672-78), ed by Wallis, London

<sup>&</sup>lt;sup>8</sup> Die Beugungserscheinungen aus der Undulationstheorie analytisch entwickelt Mannheim (1835)

In 1868 FIZEAU1 suggested a method for the direct measurement of the stellar diameters When interference is produced by the appearatus of Thomas YOUNG<sup>2</sup>, the mirrors of FRESNEL<sup>8</sup>, or a biprism the apparent diameter of the light source must be very small, if the fringes are to be pure. If the diameter of the light source is varied, the sharpness of the fringes decreases as the diameter increases, and for a certain value of the diameter the fringes disappear Proportionality exists between the separation of the fringes and the limiting diameter of the source. The complete theory of this phenomenon has been given by A MICHELSON In 1890-924 He derived the condition that the fringes become invisible when the angular diameter D of the source is a little greater than the interval l that separates one fringe from the next Thus:

$$D = 1.22 l$$

The reason why the fringes disappear if the source has an extension is the following. Each separate point gives a system of pure fringes. The systems corresponding to different points will trespass upon each other's ground and mutually blend together. The condition for disappearance of the franges is that a uniform intensity should be produced, which happens when the law of Michel-BON is fulfilled.

The method of Fizeau was applied by Stephan at the Observatory of Marseilles in 1873 The objective of the 80 cm telescope was covered with an opaque screen that had two apertures placed symmetrically with regard to the centro. The two pencils converged at the focal plane and the image was examined under high magnification. The apparatus could not distinguish angular diameters less than 0",2. Since all the stars investigated gave very clear-cut fringes, it was possible to conclude that none of them had a diameter of 0",2, but that probably even the largest were far beneath this value.

The interferometer method was later independently applied by Michelson\*

and HAMY for the measurement of the satellites of Jupiter

In a paper of 1880 E. C Pickering gave a masterly treatment of the problem of determining the diameters of stars. He first derived the expression:

$$\log d_{\bullet} = \log d_{\odot} + 0.2 \, m_{\odot} - 0.2 \, m_{\bullet} - 0.5 \, \log_1.$$

d being the diameters expressed in seconds of arc and the intrinsic brightness of the star (or in other words the ratio borne by the quantity of light emitted by the star to that emitted by the Sun from the same superficial area), me and mo the magnitude of the star and the Sun respectively

Substituting the numerical values then at his disposal the formula read:

$$\log d_* = 8.184 - 0.2 m_* - 0.5 \log_1.$$

Pickering suggested the following way of determining the approximate value of f. An electric current heats a platinum-iridium wire to incandescence and the brightness of a short portion of it is compared with an artificial star, while the current is varied by a known amount. As the current increases the colour changes. The ratio of the blue light to red light may be determined by

<sup>1</sup> CR 66, p 932 (1868) Fixeau also pointed out the possibility of using the phenomona of scintiliation for the determination of stallar diameters,

London Phil Trans (1802), A Course of Lectures on Natural Philosophy. London (1807)

Ann Chim Phys I (1816); XI (1819), Paris Mam de l'Acad V (1826) 4 Phil Mag (5) 30, p 1 (1890), (5) 31, p 338 (1891); (5) 34, p 280 (1892); Amer J of Science (3) 39, p 115 (1890).

5 C R 78, p 1008 (1874)

6 Publ A S P 3, p 274 (1891)

<sup>7</sup> BA 16, P 257 (1899) Proc Amor Academy of Arts and Sciences 16, p 1 (1880)

inserting a double-image prism in the collimator of a spectroscope, and viewing the wire through it. The relative brightness of the two images is varied by a Nicol in the eye-piece, which can be turned a known amount.

Pickering also pointed out that only an approximate value of the comparative light emitted by equal areas of the two bodies can be obtained. The effect of absorption is not allowed for, and thus a difference of temperature is assumed to be the only cause of the observed difference in colour

As far as the author is aware this scheme was not put into practice before

it was applied in the Potsdam determination of stellar temperatures.

The term equivalent diameter, the diameter of the stars if they all had the same temperature as the Sun, was introduced by E.C Pickering by taking The following table gives this diameter for different magnitudes and represents very closely the means of the modern determinations where the temperature has been taken into account

		Equivalent	Apparent	Equivalent	Apparent	Equivalent
		diameter	magnitude	diameter	magnitude	diameter
	0 <sup>th</sup> 1 2 3 4	0",0153 0 ,0096 0 ,0061 0 ,0038 0 ,0024	5 <sup>m</sup> 6 7 8	0",0015 0 ,0010 0 ,0006 0 ,0004 0 ,0002	10 <sup>m</sup> 11 12 13 14	0",00015 0",00010 0 ,00006 0 ,00004 0 ,00002

NORDMANN<sup>1</sup> has claimed that he should have priority for being the first who derived a formula how to compute the diameter of a star. In 1911 he derived the formula

$$\log \frac{R_*}{R_{\odot}} = \log \frac{\pi_{\text{O}}}{\pi_*} - \left\{ 0.2 \left( m_* - m_{\text{O}} \right) + \frac{1}{2} \log \frac{E_*}{E_{\odot}} \right\},\,$$

where R are the diameters and E the "éclats intrinsèques effectives" or the surface brightnesses. The quantities  $\frac{R_*}{R_{\odot}}$  were computed for 10 stars from their effective temperatures

This attempt is certainly one of the first, but NORDMANN cannot be given the priority, because Herrzsprung had already in 1906 advised essentially the same method2

Somewhat earlies than Nordmann wrote his paper also B v Harkanys had investigated the effective temperatures T of the stars and had derived formulae for computing the diameter of a star from T and  $m_{vis}$  or  $m_{ph}$ .

191. Wilsing's Investigations4. When estimating stellar colours several observers have remarked that the stars do not exhibit any other colours than those represented in the radiation from cooling metals. The spectral-photometric work at Potsdam confirmed this view. It was found that the energy distribution in stellar spectra corresponded to that of a black-body radiator. If such is the case the colour or rather the effective temperature will be determined by a comparison with the energy distribution at the same temperature as the celestial body But the temperatures of terrestrial sources cannot be raised above 3000° It will then be necessary to transform the stellar radiation into radiation of a lower temperature This can be done by using mirrors that selectively reflect the incident light or by using absorbing media

<sup>&</sup>lt;sup>1</sup> CR 152, p 73 (1911)

<sup>&</sup>lt;sup>2</sup> Z f wiss Photogr 4, p 43 (1906)

<sup>&</sup>lt;sup>3</sup> A N 185, p 33 (1910), 186, p 161 (1910) <sup>4</sup> Potsd Publ No 76 (1920)

If a mirror is used with a reflection coefficient of  $as^{-b/2}$ , then the reflected radiation is:

 $E = c_1 a \int_{\lambda^{-1}} \lambda^{-1} e^{-(a/T+b)\lambda^{-1}} d\lambda$ ,

and thus the reflected radiation corresponds to the temperature  $T_1$  which is determined by the formula  $c_1/T_1 = c_1/T + b$  The only mirrors suitable for the purpose are those of gold. It was found by the aid of two parallel mirrors that after five reflections the effective temperature of the B and A stars could be brought to equality with that of an electric lamp. It was also confirmed that the spectral distribution did not change appreciably by the repeated reflexions. During the course of the work it was found that the use of a red-filter yields still better results than the reflection-method, and thus a red-wedge from Schott in Jenu was taken into use which has the property that its transmission is closely represented by means of the expression  $-(\beta_0 + \beta_1/\lambda)d\log s$ , where d is the thickness of the wedge. The red filter has been used in connection with a ZOLLNER photometer.

The intensity of radiation of wave length & outside our atmosphere is expressed

by means of  $e_1 \lambda^{-3} e^{-\gamma_0 - \left(\frac{e_1}{T} + \gamma_1\right)^{1-1}}$ , where  $\gamma_0$  and  $\gamma_1$  are defined by the expression:  $\gamma_0 \log e = \log \left(1 - e^{-s_0/\lambda T}\right) - \frac{\gamma_1 \log e}{\lambda}$ ,  $\gamma_1 \log e = 0.0075 \cdot 10^{-3} (T - 3000)$ .

$$\gamma_0 \log a = \log (1 - e^{-a/\lambda T}) - \frac{71 \log a}{\lambda}, \quad \gamma_1 \log a = 0.0075 \cdot 10^{-a} (T - 3000).$$

When the radiation has passed the atmosphere, its intensity is equal to

$$c_1\lambda^{-1} \sigma^{-\gamma_0-\alpha_0 l} \sigma^{-\frac{1}{\lambda} \left(\frac{\alpha_1}{T}+\gamma_1+\alpha_1 l\right)}$$

where I is the relative path through the atmosphere at a certain distance from the zenth. This expression has further to be multiplied by the factor o- (A+A/A)\*, corresponding to the scale reading  $d = d' - \delta$ , where  $\delta$  is the scale-reading for the zero-point. The values for the photometer-lamp corresponding to T and of are T and ci. By integrating the energy between \$4500 and \$6800 it is found that the equation can be divided into the two expressions:

$$c_1/T + \gamma_1 + \alpha_1 l + \beta_1 d' = c_1/T',$$

$$c_1 e^{-\gamma_1 - \alpha_1 l - \beta_1 d'} = c_1' \sin^2 \varphi.$$

The reading of the intensity-circle gives the value  $\varphi$ . The first of the expressions gives the effective temperature in terms of T', d'; the constants are  $\alpha_1 = +0.938$ ;  $\beta_1 = +0.214$ . The ratio of the energy of two stars within the defined interval is given by the equation:

$$\log \frac{s_1}{s_1} = -2.5(m_1 - m_1) = 2(\log \sin \varphi_1 - \log \sin \varphi_1) - 0.138(l_1 - l_1) - 0.1420(l_1 - l_1) + \log \varphi(s_1) - \log \varphi(s_1).$$

 $\varphi(s)$  is the definite integral of the modified equation of Planck, viz.:

$$E = c_1 \int_{1-s}^{2-s} \frac{1-s}{\sqrt{2}} d\lambda = c_1' \sin^2 \varphi s^{\alpha_s l} + \beta_s s' \int_{1-s}^{2-s} \frac{1}{\sqrt{2}} (\frac{c_s}{2} + h) d\lambda$$

$$= c_1' \sin^2 \varphi s^{\alpha_s l} + \beta_s s' \int_{1-s}^{2-s} \lambda^{-s} s^{-s/\lambda} dt = c_1' \sin^2 \varphi s^{\alpha_s l} + \beta_s s' \varphi(s),$$
or 
$$\varphi(s) = \left[ \frac{s^{-\frac{s}{2}}}{s^{\frac{2}{3}}} \left( 1 + 3 \frac{\lambda}{s} + 6 \left( \frac{\lambda}{s} \right)^2 + 6 \left( \frac{\lambda}{s} \right)^2 \right) \right]_{1+soo}^{1-s},$$
where  $s = \frac{c_s}{2} + \gamma_1$ .

A comparison between colorimetrically measured  $c_2/T$  and those derived from spectral-photometric values at Potsdam showed good agreement mean error for a three-day determination was in the former case in the mean  $\pm 0.11$ , whereas the second method gave  $\pm 0.12$ .

Next a companison was made between the colonmetrical magnitudes and the visual magnitudes in the Potsdam Durchmusterung. A somewhat unexpected result was found, namely that there was good agreement between the two different magnitudes. This agreement involves not only the possibility of the radiation in the whole spectral interval under consideration being represented by means of the radiation law, but it also involves proportionality between the radiated energy and the relative sensibility of the observer's eye to light of the different colours

The results of H E IVES1, H BENDER2, P G. NUITING8, and W. W COB-LENTZ' concerning the visibility of radiation of the normal curve of the sensibility of the eye for different colours were collected and discussed. The physiological intensity

$$\varphi_{\gamma}(\varepsilon) = \int_{\lambda 4500}^{\lambda 6800} s_{\lambda} \lambda^{-5} e^{-\varepsilon/\lambda} d\lambda$$

was determined by Wilsing, and it was found that  $\log[\varphi(t)/\varphi_*(t)]$  was inmarkably constant. The limits for the wave lengths in the photographic region are 3600 A and 4850 A. The energy of this spectral region is then  $c_1 e^{-\gamma_0} \varphi_n(\varepsilon_0)$ . where

$$\varphi_{p}\left(\varepsilon_{p}\right) = \int_{\lambda 3600}^{\lambda 1850} \lambda^{-5} e^{-\frac{\varepsilon_{p}}{\lambda}} d\lambda.$$

The following small table gives the values of this integral.

8	$\log \varphi \left( \varepsilon_{p} \right)$	8	$\log q (e_p)$
0,9	0,06	3,0	7,88
1,0	9,95	4,0	6,86
2,0	8,91	4,5	6,36

The difference  $\log \varphi_p(\varepsilon_p + 1) - \log \varphi_p(\varepsilon_p)$  is of sufficient constancy and thus

$$\varphi_{ps}(e_p) = \int_{\lambda 3600}^{\lambda 1850} s_p e^{-\frac{s_p}{\lambda}} d\lambda = a_p e^{-b_p s_p},$$

if  $s_n(\lambda)$  is the curve of sensibility of the plate

It is found that the proportionality between the radiation and the physiclogical intensity is not dependent on a symmetrical form for  $\varphi_s(\varepsilon)$  Nor are the limits selected for the integration of much importance. In the case of the natrium cell the deviations from proportionality between the radiation and the intensity curve of the cell are considerable on account of the wider range in wave length ( $\lambda$  3650 to  $\lambda$  5780)

The equations given above permit the establishment of a relation between the constants of the selective atmospheric extinction  $\alpha_0$  and the mean coefficient of transmission p The result of G MULLER that the influence of a selective absorption is negligible in the magnitude determinations of the stars was confirmed by WILSING

Phil Mag 24, p 352 (1912).
 Dissert Breslau (1913)
 Phil Mag 29, p 301 (1915), Amer Illum Engin Soc Trans 9, p. 633 (1915).
 Scientific Pap Bureau Stand No 303 (1917)

With regard to the question of the physical meaning of the effective temperatures the measurements of the intensity in the solar spectrum are of much importance. It was found that the measured intensities could be very satisfactorily represented by means of the law of Planck, if the temperature was taken at 6070° abs. By applying the radiation law of Wien certain systematic deviations were found. It was concluded that the solar radiation has the same properties as the black-body radiation if the deviations are neglected that are produced from the mixture of different temperatures that give rise to the solar spectrum.

The presence of the absorption-bands in the K and M stars 19 found to

influence the temperature to an amount of some 200°

It can thus be concluded that the effective and the real temperature of a star do not differ considerably. The diameters of the stars can then be approximated from the radiation law. The radiation in the visual and the photographic part of the stellar spectra can be represented by.

$$-0.4m_p = \log g \left(\frac{d}{d}\right)^2 e^{-\gamma_{n} y} \int_{\lambda = 500}^{\lambda = 500} d\lambda + h_0$$

$$-0.4m_p = \log g \left(\frac{d}{d}\right)^2 e^{-\gamma_{n} y} \int_{\lambda = 500}^{\lambda = 500} d\lambda + h_0$$

where d and  $\Delta$  are the diameter and distance of a star and g depends on the constant  $\sigma$  in the STEFAN radiation law and the radiation constant  $\sigma_2$ . Further

$$\frac{1}{d} = 2 \frac{\pi}{\varrho_{\odot}} \sin \frac{1}{2} \varrho_{\odot}'$$

is introduced, where n is the parallex,  $\varrho_{\odot}$  the linear diameter, and  $\varrho_{\odot}$  the apparent diameter of the Sun; then the equation is obtained

$$\log\left(\frac{\varrho}{\varrho_{\odot}}\right)^{n} = -0.4 \, m_{p} + 0.4 \, m_{\odot} + \gamma_{op}(\varepsilon_{p}) \log s - \gamma_{op}(\varepsilon_{\odot p}) \log s + \log m_{p}(\varepsilon_{\odot p}) - \log m_{p}(\varepsilon_{p}) - \log m_{p}^{n}$$

which is simplified to

$$\log\left(\frac{\varrho}{\varrho_{\mathbf{Q}}}\right)^{2} = -0.4 \, m_{p} + \gamma_{e,p}(\varepsilon_{p}) \log e - \log \varphi_{p}(\varepsilon_{p}) - 2 \log \pi - 1.35 \,,$$

putting  $m_0 = -25^{m}.93$  and expressing n in seconds of arc.

The diameters corresponding to the visual magnitudes in P D are computed according to the formula:

$$\log\left(\frac{q}{q_{\odot}}\right)^{2} = -0.4 m_{\pi} + \gamma_{0\pi}(r_{0}) \log s - \log \varphi_{0}(s_{0}) - 2 \log \pi - 1.16.$$

The first formula was applied to 104 bright stars that had been measured for photographic magnitude by E. S. King¹ using the out of focus method.

The following moun diameters for different spectral classes were found.

e/I	Spectral class	Diameter	n	<b>₩</b> T	Spectral class	Diameter	
0,5-1,0 1,0-1,5 1,5-2,0 2,0-2,5 2,5-3,0	B B, A A, F F, G F, G	8,6 <sub>©</sub> 5,9 2,1 5,0 8,9	12 4 8 12 14	3,0-3,5 3,5-4,0 4,0-4,5 4,5-5,0	G, K G, K K K, M	16,7⊙ 32,1 50,6 61,0	21 12 10 9

<sup>1</sup> Harv Ann 59, Nr 6 (1912).

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WILSING computed a diameter value of  $\alpha$  Orionis of 0",0395 which is of a certain interest as being very close to the value 0",045, actually measured a year after Wilsing's prediction

It would certainly be of much interest to apply Wilsing's formula to the material in PD and Göttinger Aktinometrie, New Draper Catalogue, and other sources, and to derive the diameters from a consideration of existing values of

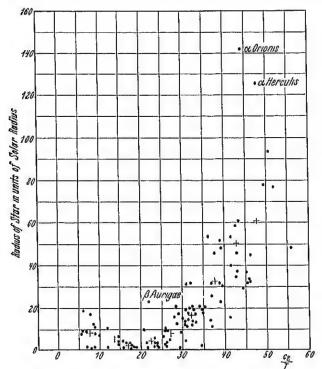


Fig 148 The radii of stars as a function of the inverse value of their effective temperature according to Wilsing's investigations. Dots denote individual values and crosses mean values. The minimum value of the radii around  $c_0/T = 20$ , corresponding to A stars, is no doubt caused by the selection in data because the main bulk of the investigated stars are giants. Compare the following figure

parallaxes or substitutes of parallaxes. In this way some 10000 star diameters of tolerable accuracy could be derived

J. Hopmann<sup>1</sup> has used the red-wedge coloumeter according to the construction of WIL-SING for measuring stars of spectral type N and red variable stars IIIs observations of twenty objects, mainly N stars, give for the temperature of the Na stars 2440° and for the Nb stars 2370°. HOPMANN has derived the diameter of 19 Piscium as 0",017 PETTIT and NICHOLSON® have computed the value 0".018 Thus the star might be measurable with the aid of the interferometer

thod. H. N Russell's Method. H. N Russell's discussed in 1920 the determination of the diameters of the stars. If d is the apparent diameter, m the visual

magnitude and J the surface brightness of a star, it follows from elementary considerations that:

$$d = \text{const} \cdot 10^{-0.2m} J^{-\frac{1}{4}}$$

By inserting the data for the Sun the constant is found to be 0",0087, provided that the Sun's surface brightness is taken as unity. Further  $\eta = -2.5 \log J$  is introduced. The above equation may then be written

$$d = 0.0087(0.631)^{m-j}$$
.

The following method for a determination of 1 was used. The difference

<sup>&</sup>lt;sup>1</sup> A N 222, p 237, 226, p 1 (1925); 226, p 225 (1926), <sup>2</sup> Mt Wilson Contr No 369 (1928), Ap J 68, p 279

<sup>8</sup> Publ ASP 32, p 307 (1920)

in surface brightness of two stars expressed in magnitudes is proportional to the difference in colour indices C. Thus for two stars

$$j_1 - j_1 = k(C_1 - C_1)$$

The constant k depends on the wave lengths used in measuring the surface brightness and colour index, but is the same for all stars. As long as Wirn's formula can be applied,  $k = \lambda_{\rm phot}/(\lambda_{\rm vis} - \lambda_{\rm phot})$ , and at higher temperatures, when Planck's formula has to be used, the value of k gradually increases, since for an infinite temperature this formula gives infinite surface brightness, but finite colour index

The Sun permits a direct observational test of this law. The work of SCHWARZ-SCHLD, ABOTT, and LINDBLAD makes it very probable that different parts of the Sun's disc differ in colour and brightness, because at the centre we see down further and into hotter layers than near the limb where the line of vision is more oblique. It can therefore be assumed that on passing from the centre to the limb of the Sun we meet successively with conditions very similar to those met with in the photospheres of cooler stars. Abbot's observations of 1913 have been used for a determination of k. In some cases the values closely agree with those predicted, but in others the discordances are considerable, probably on account of a departure from black-body conditions.

The different scales of C have to be standardized on account of the fact that some of the scales are more open than the others. The standardization is made by deriving the ratios  $C/C_{K \text{stars}}$  in one and the same system. The colour index  $(C_{K \text{stars}})$  for K stars is then called the colour equation of the given system. A system for which  $C_{K \text{stars}}$  is exactly 1,00 was suggested by Pichering as a standard. Let K be the value of h, referred to such a system. For any other system of C, with a colour equation E, we have k = K/E. This new constant K is equal to  $f_{A \text{stars}} - f_{K \text{stars}}$ . In the case of Parkhurst's colour indices  $\lambda_{F \text{is}}$  is 5410 and  $\lambda_{P \text{is}} = 4280$  and thus k = 3.8. In order to correct for the systematic difference between his spectra and those of Harvard Russell takes E = 1.27 and hence K = 4.8 An independent system of colour indices has been derived by Rosenberg from photographic spectra and gives the intensity at  $\lambda$  4000 relative to that at  $\lambda$  5000. Arranging his data according to the Harvard spectral classification Russell finds  $C_E - C_A = 1.83 - 0.10$  and K = 6.7 for  $\lambda$  5200 A

Then the stellar temperatures determined by Wilsing and Schriner were used. By applying Planck's formula Russell has found K = 4.0 for 1 5200 A. Also other astronomical data could be used, e.g. eclipsing binaries, or a comparison of densities of eclipsing binaries with the relation between density and surface brightness derived from visual double stars. Russell derived in his address of 1914 the relation.

Special class	C	1	Spectral class	С	1
B A F	-0,3 0,0 +0,3	-1,2 0,0 +0,9	G M	+0,7 +1,6	+2,0 >4,5

Also the concomitant variations in magnitude and colour index of the Cephelds can be used, provided that the observed variation is due to changes of temperature in a radiating surface of constant area. This assumption is very dubious, as has been pointed out by Russell

<sup>1</sup> Pop Astr 22, p. 339 (1914).

Method	K
PARKHURST, colour indices	4,8
ROSENBERG, colour indices	6,7
WILSING and SCHEINER, temperatures	4,0
U Cephei (direct observations)	3,2
Eclipsing variables (colour indices)	3,1
Comparison of eclipsing variables and binary stars	3,5
Colour change of Cepheids	2,3
	Mean 3,9 -1- 0.4
	Adopted 4,0

Then the colour indices of King, Schwarzschild, Parkhurst, and Haivard are expressed in units of  $C_R - C_A$  so that they all have C = 1,00 for K0 stars. The values of j are derived. The small table given here will facilitate considerably the computation of d. When the parallax is known the linear diameter D is found by  $D = 9,22 (0.631)^{M-j}$ , the Sun's absolute magnitude being 4,83

Spectral class	-1	Spectral class	1	<i>m−₁</i> <i>M−₁</i>	đ	D
B0 B2 B5 B8 A0 A2 A5 F0	+3 <sup>m</sup> ,2 +3,0 +2,7 +2,5 +2,1 +1,7 +1,3 +1,0 +0,6	F8 G0 G5 K0 K2 K5 Ma Mb N	+0 <sup>th</sup> ,1 0,0 -0,9 -1,9 -2,9 -3,3 -3,7 -4,0 -6,3	0, <sup>m</sup> 0 0, 5 1, 0 1, 5 2, 0 2, 5 3, 0 3, 5 4, 0 4, 5 5, 0	0",0087 69 55 43 34 27 22 17 14 11 0",0009	9,2 O 7,3 5,8 4,6 3,7 2,9 2,3 1,8 1,5 1,2 0,9

A number of diameter-values were computed by Russell, and among these were values of  $\beta$  Andromedae, Betelgeuze, and Antares Betelgeuze was measured about a year later with the interferometer, it was found then a very good agreement between the diameters actually measured and those computed by Russell, Wilsing, and others

193 Diameters from  $c_2/T$ . As has been described in the chapter on stellar colours, E Hertzsprung has reduced the principal determinations of colours or colour equivalents of the brighter stars to a homogeneous system from which  $c_2/T$  is derived. These values have been used for a derivation of the angular diameter d of 734 stars according to the formula

$$5 \log \sin \frac{d}{2} = -43,44 + 2,3 (c_2/T)^{0,93} - m$$

All the available trigonometric parallaxes of these stars as well as all available spectrographic data have been collected by me and the values of the linear diameters computed in terms of that of the Sun Also  $\pi_{s\mu}$  has been used. It is evident that in many cases already a knowledge of the colour and proper motion will give the linear diameter of a star with fair accuracy

K F Bottlinger2 has derived the following linear diameter formula:

$$\log D/2 = 0.2(m_{\text{O}} - m_*) - \log \pi + (\log c_2/T_* - \log c_2/T_{\text{O}}) + 5.3144$$

where D is the linear diameter in units of the diameter of the Sun; the magnitudes are reduced to the bolometric scale. The diameters were first computed

Leiden Ann XIV 1 (1922)
Berlin-Babelsberg Veröff 3, H. 4 (1923)

for 104 stars for which the colour index had been measured photo-electrically In a subsequent paper the diameters have been computed for some 400 stars. The diagram connecting diameter and spectral class shows a certain resemblance with the Russell diagram. The dispersion in diameter on the giant branch is considerable and it does not seem quite impossible that we have, in fact, two branches, a giant and a supergiant branch. The fact that the diameter values computed on the basis of data of echasing binaries do not deviate systematically from the values computed from the temperatures is of a certain importance

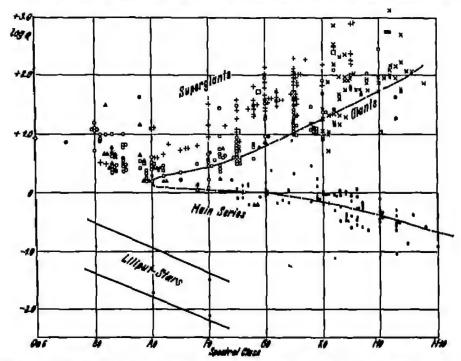


Fig. 449 Distribution of the logarithms of the diameters of stars within different spectral classes according to Bottleman. The triangles denote colleging binaries, dots trigonometric paralleless or dynamical paralleless of high weight, open circles theoretical paralleless (moving clusters, companions) Further denote  $\times$  spectrographic paralleless and + paralleless of Cophekis. The two squares give the mean values of log  $\varrho$  for the  $\circ$  stars

BOTTLINGER suggests the name liliputian stars for the white dwarfs. The spectra should according to his proposal be denoted e.g. I B9

194. Diameters from Radiometric Measurements, PRITIT and NICHOLSONS have derived the following expression.

$$\log T = 2.638 - 0.1 (m_r - \Delta m_r) - 0.5 \log d$$

where d is the apparent diameter of the star in seconds of arc and T is the temperature,  $m_r$  the apparent radiometric magnitude of a star, and  $\Delta m_r$  the correction to no atmosphere including atmospheric absorption and losses in the telescope. The following table contains the diameters measured directly by Phase, and the diameters computed from the above formula with temperatures

<sup>&</sup>lt;sup>2</sup> Sceliger-Festschr p 338 (1924).

Mt Wilson Contr No 369, Ap J 68, p. 279 (1928).

derived from water-cell absorptions and from heat indices, it further contains the temperatures computed from measured d, water-cell absorptions, and heat indices (comp ciph 187)

		Diameter		Absolute temperature				
Object		Mensured by interfero mater	Computed from m <sub>to</sub>	Computed from C <sub>II</sub>	From measured d and mr	From m <sub>t0</sub>	$\begin{array}{c} 1 \text{ rom} \\ C_H \end{array}$	
Arcturus Aldebaran Betelgeuze Antares β Pogasi α ITerculis Λ ο Ceti A (max)		0",020 0 ,020 0 ,047 0 ,040 0 ,021 0 ,030 0 ,056	0",031 0 ,033 0 ,071 0 ,062 0 ,029 0 ,065 0 ,038	0",028 0 ,031 0, 076 0 ,065 0 ,028 0 ,090 0 ,073	4300° 3890 3270 3270 3140 3320 2210	3440° 3080 2700 2680 2730 2340 2610	3580° 3170 2600 2620 2730 2030 1970	

195 Kalmar's Investigation 1 The author starts from the following formula which is easily derived

$$\log \varrho = 0.5 \log J_{\rm O}/J_{*} - 2.6243$$

where  $I_*$  is determined from the equation of Planck

$$J_* = C \int_{J_1}^{\lambda_1} \lambda^{-5} \left( e^{\frac{c_2}{\lambda T}} - 1 \right)^{-1} d\lambda.$$

C is equal to  $590 \mu^2 \, \mathrm{erg \, sec^{-1}}$ ,  $c_2 = 14600 \, ^{\circ} \mu \, \mathrm{degree}$  Celsius. As limits for the integral  $\lambda_1 = 0.40 \,\mu$ ,  $\lambda_2 = 0.76 \,\mu$  have been taken. The following substitution is made

$$a = \frac{c_2}{\lambda_1 T}$$
,  $b = \frac{c_2}{\lambda_2 T}$ ,  $x = \frac{\frac{c_2}{\lambda T} - a}{b - a}$ ,

$$J_* = C(a-b) \left(\frac{c_2}{T}\right)^{-4} \int_0^1 \frac{[a-x(a-b)]^3}{[e^{a-x(a-b)}-1]} dx$$

The integral is then evaluated by means of mechanical quadrature. If r and Rare the radius and distance of the star and  $\rho$  the apparent radius

$$r = R t g \rho$$

Introducing the parallax  $\pi$  and measuring R in light-years we have

$$\log \pi_0 = \log \pi + 0.2 m$$
, and  $R = \frac{3.228}{\pi}$ 

where  $\log \pi_0$  is the parallax reduced to apparent magnitude m=0.

From the derivation of stellar temperatures by BRILL<sup>2</sup> the following values have been taken

Spectral class	В	A	I,	G	K	М
$c_2/T$	1,22	1,51	2,06	2,81	3,74	4,17
For t	he Sun $c_2$	T = 2,35	$J_{\rm C}$	= 52,75	ergsec-1	$u^{-2}$ .

A number of the existing parallaxes had to be excluded on account of uncertainty The author has selected 260 parallaxes, from which the following values of  $\pi_0$  have resulted

A N 233, p 93 (1928) Also thesis in Budapest (Hungarian),
 A N 219, p 21 (1923).

			В	A	٨	•	F	•	G	*	K		М	•
Giants			04,170	21	0",138	13	0",140	7	0",132 1 ,263	14	0",128	15	0",122	7
Dwerts .			_	_	0,284	26	0 ,796	45	1 ,263	56	4 ,031	54	6 ,158	2

From the data at hand the following results have been found by KALMAR.

Spect class		Abuninte temperature	Horisco brightness J	Mean app.	Mosp red	J.hear redim
	K	3 500° 3 900	2,38 4,53	0",0198	26,5 26,0	34,8 ⊙ 24,8
Glants	G	5200 7100	23,46 87,00	0 ,0063	24,6 23,0	10,3 4,7
	AB	9700	266,73 475,23	0 ,0019	20,9 18,1	1,8
	A	9700 7100	266,73 87,00	0 ,0019	10,3	1,3
Dwarfs	GK	5200 3900	23,46 4,53	0 ,0063	2,2 0,8	0,9
	ĹΜ	3 500	2,38	8910, 0	0,6	0,7

196. Interferometer Measurements at Mount Wilson. The reason why the interferometer method was not applied earlier to diameter measurements of stars must have been because astronomers have thought that atmospheric disturbances are a too serious source of arror. As a matter of fact observations have proved to be feasible even when visibility is poor. According to A. MICHELSON and F. G. PEASE<sup>1</sup> the explanation is that the atmospheric disturbances, being uregularly distributed over the surfaces, simply blurr the diffraction pattern. In the case of two isolated pencils, too small to be affected by such an integrated disturbance, the resulting interference fringes, though in motion, are quite distinct unless the period of the disturbances is too rapid for the eye to follow them.

As the diameter of the 100 inch reflector was not sufficiently large for the fringes to vanish, an interferometer with movable outer mirrors was constructed. The maximum separation was 20 feet.

Four mirrors,  $M_1$ ,  $\tilde{M}_2$ ,  $M_2$ , and  $M_4$ , about 150 mm in diameter, inclined at 45° to the base, are modeled on slides.  $M_2$  and  $M_3$  are adjusted by three scrows at the back, and  $M_1$  and  $M_4$  can be adjusted about two horizontal axes by means of fine scrows at the ends of lever arms. The mirrors  $M_2$  and  $M_3$  are kept fixed at a constant separation of 114,2 cm, except that  $M_3$  has a motion of several millimetres along its slide and parallel to the beam.

The fringe pattern has a spacing equal to 0,02 mm and is easily visible with a magnification of 1600.

The observations are made at the CASSEGRAIN focus, corresponding to an equivalent focal length of 40,84 m. Two pencils from the star are reflected from the outer mirrors,  $M_1$  and  $M_4$ , to  $M_2$  and  $M_3$ , and from there along the ordinary optical way to the large mirror, the convex mirror, the Coudé flat, and finally to the focus. The coincidence of the pencils at the focus is obtained by adjusting

<sup>1</sup> Mt Wilson Contr No 184, 185 (1920) and No. 203 (1921), Ap J 51, p. 257, 2031

<sup>53,</sup> p 249

Recent work by W. A. Calder at Harvard College Observatory [Harv Bull 885 (1931)] using the Harvard 15 inch refractor and a stellar interferementar in front of the objective, emphasizes the importance of good seeing at interferementar measures. Calder concludes: "... that the statements frequently found to the effect that, in contrast to what might be expected, the interferementar does not require excellent seeing conditions, are unduly optimistic. Atmospheric conditions appear to be the controlling factor, and seriously restrict the possibilities of the interference method."

the outer mutors  $M_1$  and  $M_4$  and then tilting a plane parallel glass plate of 15 mm thickness in the path of one of the pencils. The equality of the paths of the pencils is obtained by setting the outer mirrors as nearly symmetrically as possible on the beam, and then by adjusting a double wedge of glass in the path of one of the pencils, the relative motion of the wedges alters the paths slowly and continuously.

In order to obtain "zero" fringes for purposes of reference the end of the telescope tube is entirely covered, except for two apertures in the beam 152 mm in diameter. The pencils entering these apertures pass through the wedges and the compensating plate, and produce an image of the star in the field of vision; when they have been adjusted for coincidence and equality of path, these pencils interfere and produce the zero fringes which cross the reference images

The interferometer images are next brought into the field of the eyepiece and made to coincide at a short distance from the zero star, thus forming a second star in the field. The parallel plate compensator is used only for differential deflection of the steel beam. When the wedge is moved in order to equalize the difference in the path of the interferometer pencils, the zero fringes disappear, and the number of turns of the rod are determined which are required to bring the first fringes into view. The mirror  $M_3$  is then moved a small amount in order to compensate for this difference. After several trials both sets of fringes are seen in the field of vision crossing their respective images.

The distribution of light in the disc to be measured is represented by the formula:  $I = I_0 (R^2 - r^2)^n$ 

where r is the distance from the centie, R the radius of the star, and n the exponent expressing the amount of darkening at the limb. The visibility V of the interference bands is defined by

$$V = \frac{1}{P} \sqrt{C^2 + S^2}$$

$$C = \int F(x) \cos kx \, dx, \quad S = \int F(x) \sin kx \, dx,$$

$$P = \int F(x) \, dx, \quad k = \frac{2\pi_c b}{l_{eff} d},$$

where C

in which b is the distance between the two pencils entering the interferometer,  $\lambda_{\rm eff}$  the mean effective wave length of the light-source, d its distance, and F(x) dx is the total intensity of a strip of the source having a width of dx in a coordinate system where x, y are the coordinates of a luminous point in the disc of the star. The star disc must be symmetrical and thus.

$$V = \frac{C}{P}$$

Assuming the illumination to be a function of the distance from the centre in the way indicated above we have, when substituting  $r^2 = r^2 + v^2$ 

$$F(x) = \int_{0}^{\sqrt{R^{2}-x^{2}}} (R^{2}-x^{2}-y^{2})^{n} dy$$

Expanding in series and substituting in V Michelson and Pease<sup>1</sup> find:

$$V = \frac{\int\limits_{0}^{R} (R^{2} - v^{2})^{\frac{2n+1}{2}} \cos kx \, dx}{\int\limits_{0}^{R} (R^{2} - x^{2})^{\frac{2n+1}{2}} dx}$$

<sup>&</sup>lt;sup>1</sup> Mt Wilson Contr No 203, Ap J 53, p 249 (1921)

The following table computed under the direction of F R. MOULTON gives the values of the integral.

 $F(k,n) = \int_{0}^{1} (1-x^{2})^{\frac{2n+1}{2}} \cos hx \, dx.$ 

	s=0		n=0,5		g = 1		A-2
70 0 0 100 130 160 200 230 240 280 320 360 400 520 600	F (h, n) +0.785 +0.507 +0.378 +0.243 +0.065 -0.024 -0.050 -0.100 -0.095 -0.053 -0.007 +0.036 +0.042 -0.011	30 60 90 120 150 180 210 240 257,45 270 300 330 330 360 390 420 450 480 510 540 570 600 630	F (h, si) +0,785 +0,765 +0,702 +0,607 +0,490 +0,363 +0,127 +0,038 +0,024 -0,057 -0,068 -0,059 -0,040 -0,016 +0,005 +0,019 +0,028 +0,026 +0,019 +0,029 -0,009	40 80 120 160 200 240 280 320 360 400 440 480 520 600 640 680	F (h, #) +0.785 +0.746 +0.663 +0.536 +0.383 +0.237 +0.112 +0.024 -0.029 -0.045 -0.039 -0.020 -0.020 +0.012 +0.013 +0.005 -0.004	40 80 120 160 240 280 320 360 400 440 480 520 600 640 680 720	F (A, n) +0,785 +0,761 +0,694 +0,590 +0,468 +0,342 +0,123 +0,054 +0,003 -0,019 -0,024 -0,018 -0,006 +0,005 +0,005

The authors point out the theoretical possibility of deriving the actual distribution of light in the source from observations of the visibility curve itself. Even if the present means are not able to give such a result, it does not seem impossible that future observations will do so.

If  $b_1$  and  $b_2$  are the distances for which the fringes vanish the first and second times, the following formula gives a fair approximation to the value of n:

$$n = -1 + 75 \left( \frac{b_1}{b_2} - \frac{1}{2} \right)^2.$$

Denoting the visibility of the first negative maximum by Vmax we have:

$$n = 0.22 \left(\frac{1}{V_{\text{max}}} - 7.8\right)^{0.7}$$

The value sought by the measurements is F(h, \*) = 0 or the separation between the outer minors  $M_1$  and  $M_2$  for which the fringes vanish P. Merrill, when using the Anderson interferometer used for the investigation of the orbit of Capella, found that the visibility of the fringes of  $\alpha$  Orionis decreased, for the maximum separation of 100 inches, in that apparatus. As the decrease was independent of the position angle of the interferometer the star was certainly not a binary.

On December 19, 1920, after the adjustment of the instrument had been checked by means of settings on other stars,  $\alpha$  Orionis was investigated. A separation of 121 inches did not give any fringes for that star, although the zero fringes were quite visible. The disappearance of the interferometer fringes evidently could not be caused by any disturbances of an instrumental nature. The instrument was not provided at that time with means for continuously altering the distance between the movable mirrors

The effective wave length was assumed to be  $\lambda$  5750 for  $\alpha$  Onoms, and the angular diameter was thus found to be

$$d = 0''.047$$

Somewhat later J A Anderson made an investigation of the effective wave length and found the value  $\lambda_{eff}$  5520, from which it follows that:

$$d = 0''.045 + 0''.0045$$
.

The stars for which a value of the diameter has been found by direct measurements are the following:

			Par	rallax		Diameter	
Star	Diameter	Trigo nometric	Spectro graphic	Spectral proper motion	Concluded value	in linear measure	
α Orionis	0",047	0",011	0",010	0",012	0",011	460 🕥	
& Bootis	0 ,022	0 ,085	0 ,131	0 ,158	0,090	26	
α Scorpn	0 ,040	0 ,026	0 ,013	0,010	0 ,020	160	
o Ceti,	0,056	0 ,011	_	0 ,020	0 ,010	600	
a Herculis	0 ,021	0 ,030	0 ,002?	800, 0	0 ,007	320	
α Taurı	0 020	0 ,057	0 ,083	0 ,096	0 ,060	36	
β Pegasi .	0 ,021	0 ,019	0 ,023	0 ,028	0 ,020	110	
y Andromedae	(0,014)	0 ,010	0 ,007	0 ,024	0,010	(150)	
a Arietis	(0,011)	0 ,037	0,053	0,046	0,040	(30)	

The values within parentheses depend on extrapolation of the visibilitycurves and on a correction for seeing, and are hence uncertain and subject to changes when a larger separation can be used, so that the actual disappearance of the fringes will be estimated

The value for  $\alpha$  Orionis is given above as 0",045 and the mean value of 8 determinations is 0",042. I have preferred to use the original value from 1920. The value for  $\alpha$  Scorpii has been checked at different epochs

The linear diameter D is found from the formula  $D = 107.5 \ d^{1/2}/\pi''$  On account of the importance of knowing the linear dimensions the existing values of the parallaxes have been discussed with great care, as an example, we give in some detail the discussion for  $\alpha$  Orionis.

 $\alpha$  Orionis Six trigonometric values of the parallax are known  $+0'',031 \pm 0'',024$  (Yale),  $+0'',018 \pm 0'',007$  (Schlesinger),  $+0'',022 \pm 0'',007$  (Lee);  $+0'',013 \pm 0'',006$  (Mitchell),  $+0'',011 \pm 0'',006$  (van Maanen), and  $-0'',005 \pm 0'',007$  (Alden) Spectrographic determinations are 0'',012 (Mount Wilson), 0'',014 (Norman Lockyei Observatory), 0'',009 (Victoria). The spectral proper motion method gives  $\pi_{8\mu} = 0'',012$ .

A weighted mean of the trigonometric values gives 0",014 and of the spectrographic values 0",010. The high luminosity of  $\alpha$  Orionis makes it probable that its mass is high. Thus a systematic difference ought to be present between  $\pi_{\rm tr}$  and  $\pi_{\rm s}$ . But if a mass factor is present the luminosity would be too small in the second case and the parallax too large. It thus seems that either the parallaxes available do not suggest such an effect or the mass is small

Anyhow it seems that the best parallax value to be derived from the material is 0",011.

197. Varying Stellar Diameters. The most sensational discovery concerning the diameters of the stars is without doubt that of PEASE<sup>2</sup> that the dimensions of  $\alpha$  Orionis vary between certain limits. Numerous tests have shown that the

Mt Wilson Contr No 222 (1922), Ap J 55, p 48

<sup>&</sup>lt;sup>2</sup> Publ ASP 34, p 346 (1922), Mt Wilson Reports 1920-1928

variation must be real. Thus it is proved that pulsations occur among the stars. The data are too few to admit the establishment of correlations between the apparent magnitude, the radial velocity, and the diameter. There seems to be some relation, but the observations are too few. Besides, the estimates of magnitudes are liable to considerable uncertainty on account of the lack of comparison stars and the rather exceptional colour of the star. The following determinations have been obtained by Pease:

Epoch	Apparent changes	Rpoch	Apparent disension
December 1920	0",047	December 1924 December 1925 December 1926 Pebruary 1928	0",044
September-November 1921	0 ,054		0 ,034
October 1922	0 ,034		0 ,041
December 1923	0 ,041		0 ,037

Adopting the parallax above the following values of the linear diameter are found:  $460 \odot$ ,  $540 \odot$ ,  $330 \odot$ ,  $400 \odot$ ,  $430 \odot$ ,  $330 \odot$ ,  $400 \odot$ , and  $360 \odot$  respectively. This gives a mean value of  $400 \odot$  and a dispersion of  $\pm 71 \odot$  around the mean.

It is possible that the dimension of Mira Ceti also varies, but the observations

available cannot decide this question.

The new interferometer with a maximum base of 50 feet was taken into use at the end of 1930, with this magnificent instrument the number of measurable stars will be increased to forty or more. In the Mt Wilson Report for 1931 it is stated that the adjustment and operation of the 50 feet interferometer have been continued by PEASE, who has observed fringes with mirror-separations up to 44 feet. Measurements of  $\alpha$  Orionis give an angular diameter of about 0",040 and of  $\beta$  Andromedae 0",046.

198. The Theoretical Investigations of M. Hamy. M Hamy' has proved that the light E of a point in a circular star can be expressed by the convergent

series.

$$E = A_0 + A_1 (1 - \rho^2)^{\frac{1}{2}} + A_2 (1 - \rho^2) + A_3 (1 - \rho^2)^{\frac{1}{2}} + \cdots$$

where q is the ratio between the angular distance of the point considered from the contre and the angular diameter, and  $A_0$ ,  $A_1$ ,  $A_2$ ,... are constants depending on the constitution of the stellar atmosphere

For the San and Latt = 5062 A we have

e	Keibe	Remail	o	Echa	Rome
0,00	1,0000	1,0000	0,825	0,7196	0,7195
.20	0,9891	0,9882	0,875	0,6605	0,6607
.40	0,9510	0,9505	0,92	0,5909	0,5911
,55	0,8998	0,9003	0,95	0,5289	0,5285
,65	0.8516	0.8521	0,97	0,4719	0,4721
.75	0.7871	0,7865			.,,,,

The values  $E_{\text{comp}}$  are formed from the following values of the constants derived by the aid of a least square solution:

$$A_0 = 0.257379$$
  $A_1 = 0.941025$   $A_2 = -0.255333$   $A_4 = -0.019945$ 

The formula for E has an interesting application to the measurements of the diameters of the stars,

<sup>&</sup>lt;sup>1</sup> CR 174, p 342 (1922); Journal de Mathématiques pures et appliquées 1917 and 1920; B A Mém et Var I, p. 198 (1920).

When two apertures are used the fringes of Young will disappear as soon as the well-known relation  $\varepsilon = 1.22 \frac{\gamma_{\rm eff}}{T}$ 

is fulfilled,  $\epsilon$  is the angular diameter of the star and l the distance between the apertures. The relation presumes the star disc to be uniform

It is also possible to determine the value of  $\varepsilon$  and the variation in the surface brightness of the star in cases where an absorbing atmosphere gives a non-uniform distribution of light over the disc, if the ratios of the intensities of the maxima and minima of the fringes have been observed

If l is the value for which the fringes disappear,  $K_i$  the ratio of the intensities when the distance is  $l_i$ , and  $\alpha_i = l_i/l$ , and if further  $m = \pi_0 \frac{ls}{l_{eff}}$  and  $m_i = \pi_0 \frac{l_i s}{l_{eff}}$  and thus  $m_i = m\alpha_i$ , we obtain, by using the expression above for E, the following equation

$$A_0[f_0(m_i) - K_i F_0(m_i)] + A_1[f_1(m_i) - K_i F_1(m_i)] + = 0$$

The value of the n constants is determined from n equations, that is, from n determinations of the  $K_i$ . The functions / and F are known and depend on the evaluation of an integral of the form

$$\int_0^1 (1-x^2)^{p+\frac{1}{2}} \cos qx \, dv,$$

where p is a whole positive number or zero and q has not a high value. In a subsequent note HAMY makes use of the following designations:

$$\begin{split} U_0 &= \sum_{n=0}^{n=\infty} (-1)^n \frac{m^{2n}}{(1\cdot 2-n)^2} \frac{1}{n+1} = \frac{4}{\pi} \int_0^1 (1-u^2)^{\frac{1}{2}} \cos 2mu \, du, \\ U_1 &= \sum_{n=0}^{n=\infty} (-1)^n \frac{m^{2n}}{(1-2-n)^2} \frac{1}{(n+1)(n+2)} = \frac{8}{3\pi} \int_0^1 (1-u^2)^{\frac{3}{2}} \cos 2mu \, du, \\ B &= \frac{A_0}{2} + \frac{A_1}{2} + \frac{A_2}{4} + \frac{A_3}{5} + \frac{A_1}{6}, \\ C &= A_0 \frac{U_0}{2} + A_1 \frac{1}{4m^2} \left( \frac{\sin 2m}{2m} - \cos 2m \right) + A_2 \frac{U_1}{2} \\ &\quad + A_3 \frac{9}{4m^2} \left[ \frac{1}{4m^2} \left( \frac{\sin 2m}{2m} - \cos 2m \right) - \frac{1}{3} \frac{\sin 2m}{2m} \right] \\ &\quad + A_4 \frac{1}{4m^2} \left( 2U_1 - U_0 \right) \end{split}$$

The coefficients  $A_0$ ,  $A_1$ ,  $A_2$ ,  $A_3$ ,  $A_4$  in the expression for C are tabulated in the table on p 593

HAMY shows that the maxima of intensity are proportional to B+C and the minima to B-C.

If  $l_0$  is used as a designation for the value for which the fringes disappear, the ratio K then equals unity If  $\alpha_1 = l_0/l$  and  $\mu = m_0/\alpha_1$  we have the following system

<sup>1</sup> CR 174, p 904 (1922)

$\mu$ , $\frac{A_1}{A_0}$ The found
<i>l</i> In
Sun ti simplo of districtensity diametric value or and s'vin interthe foll found.
In per-gia giants certain account atmosp pld fall aity to

These equations de- termine the quantities	м	10	A1	A,	As	AL
	0,0	+0,5000	+0,3333	+0,2500	+0.2000	+0,1667
$\mu, \frac{A_1}{A_0}, \frac{A_0}{A_0}, \frac{A_0}{A_0}, \frac{A_3}{A_0}$	0,1	,4975	3320	,2492	,1994	1663
A, A, A, A, A	0,2	,4901	,3280	,2467	,1977	,1650
	0,3	14779	,3215	,2426	,1949	,1630
The diameter s is	0,4	,4611	,3125	,2369	,1910	,1601
found from	0.5	,4401	,3012	,2298	,1861	,1565
l-e	0,6	,4153	,2877	,2213	,1802	,1522
$\mu = \pi_0 \frac{l_0 t}{L_{ct}}$ .	0,7	,3871	,2724	,2116	.1735	,1472
Aeti	0,8	,3562	,2554	,2008	,1659	,1417
In the case of the	0,9	,3231	,2371	,1890	,1577	1355
Sun the application is	1,0	,2884	,2177	,1764	,1489	,1290
simple because the law	1,1	,2527	,1975	,1632	,1395	,1220
	1,2	,2168	1769	,1496	,1298	,1147
of distribution of the in-	1,3	,1811	,1561	,1308	,1198	11071
tensity is known. If the	1,4 1,5	,1464	,1354	,1219	,1097	,0993
diameter is a whon con-	1,6	,1131	,1152	0944	,0895	,0916
sideration is taken of	1,7	,0527	,0771	,0813	,0796	,0760
the variation in inten-	1,8	,0265	0597	0686	,0699	0684
	1,9	+0,0034	.0436	,0567	,0606	.0610
sity on the solar disc,	2,0	-0.0165	,0290	,0455	,0518	,0538
and s' when no variation	2,1	,0330	,0160	0352	,0435	,0469
in intensity is supposed,	2,2	,0461	+0,0047	,0258	.0357	,0404
the following relation is	2,3	.0558	-0.0049	,0174	,0285	0343
found.	2,4	,0622	,0128	,0104	,022()	,0286
	2,5	,0655	,0490	+0,(X)37	,0162	,0233
$\epsilon' = 0.91 \epsilon$ .	2,6	,0660	,0236	~0,0016	,0110	,0186
In the case of su-	2.7	,0640	,0267	,0059	,0065	,0143
	2,6	,0597	,0283	,0094	十0,0027	,0105
per-giants and ordinary	2,9	.0537	,0287	,0119	-0,0005	.0071
giants the correction is	3,0	,0461	,0280	,0135	,0031	10043
certainly much larger on	3,1	,0376	,0263	,0144	,0051	1 0,0018
account of the extended	3,2	,0284	,0238	,0147	,0066	-0,0002
atmosphere and the ra-	3.3	,0190	,0207	,0143	,0075	,0018
pld falling off in inten-	3,4	,0096	,0172	,0135	,0081	,0030
	3.5	-0,0007	,0135	,0123	,0082	,0039
aity towards the limbs	3,6	+0,0076	,0096	,0109	,0080	10045
Later on HAMY1	3.7 3,8	,0210	,0058  -0,0021	,0091	,0076	,0048
considered the case	3,0	,0218	+0.0012	,0073	,0061	,0049
where the dimension of	4,0	+0,0294		-0,0034 -0,0035		-0,0046
the exertures sould not	4,0	I COMPT	1 010042	נביאינט	0,000	- Olonia

the apertures could not be considered as negligible in comparison with the distance between them. In his earlier work he had reached an approximative solution.

If we denote the common width of the apertures by a, the distance between them by l, by O the angular distance from the centre of a point in the focal image of the star taken parallel with the line joining the centres of the aportures, by w another angle in the same direction as O, then the intensity I in the direction \( \theta \) is proportional to the integral:

$$\int_{-\frac{1}{4}}^{\frac{\pi}{4}} - w^{\frac{1}{2}} \Big|^{\frac{1}{2}} \left[ \frac{\sin \frac{\pi_{\sigma} a}{\lambda_{\rm eff}} (w - \Theta)}{\frac{\pi_{\sigma} a}{\lambda_{\rm eff}} (w - \Theta)} \right]^{\frac{1}{2}} \cos^{\frac{\pi}{4}} \pi_{\sigma} \frac{I}{\lambda_{\rm eff}} (w - \Theta) dw.$$

Putting .

$$\theta = \frac{\epsilon}{2} t$$
;  $\theta = \frac{\epsilon}{2} \tau$ ;  $\frac{\epsilon}{l} = \alpha$ ;  $m = \frac{\alpha_l l \epsilon}{2 \lambda_{ml}}$ 

<sup>1</sup> CR 175, p. 1123 (1922).

BA 16, p 257 (1899)

one can write

$$I = 2 \int_{-1}^{+1} (1 - u^2)^{\frac{1}{2}} \left[ \frac{\sin m \alpha (u - \tau)}{m \alpha (u - \tau)} \right]^2 \cos^2 m (u - \tau) d\tau$$

Further we put

$$2m\tau = x$$

$$S(m) = \frac{4}{\tau_0} \int_{0}^{1} (1 - u^2)^{\frac{1}{2}} \cos 2mu \, du,$$

$$T(m) = \frac{4}{3\pi_c} \int_0^1 (1 - u^2)^{\frac{1}{2}} \cos 2m \, u \, du$$

Then one can easily derive.

$$\frac{4}{\pi_0} \int_0^1 u^3 (1 - u^3)^{\frac{1}{2}} \cos 2mu du = S(m) - 3 \Gamma(m),$$

$$\frac{4}{\pi_0} \int_0^1 u (1 - u^3)^{\frac{1}{2}} \sin 2mu du = 2mT(m)$$

The numerical values of S(m) and T(m) have been computed by Hamy as follows:

111	S(m)	$\Gamma(m)$	218	S(m)	$\Gamma(m)$
0,0	1,0000	0,2500	1,0	0,5767	0,1764
0,1	0,9950	0,2492	1,1	0,5054	0,1632
0,2	0,9801	0,2467	1,2	0,4335	0,1496
0,3	0,9557	0,2426	1,3	0,3622	0.1308
0,4	0,9221	0,2369	1,4	0,2927	0,1219
0,5	0,8801	0,2298	1,5	0,2261	0.1080
0,6	0,8305	0,2213	1,6	0,1633	0,0944
0,7	0,7742	0,2116	1,7	0,1054	0,0813
0,8	0,7124	0,2008	1,8	0,0530	0,0686
0,9	0.6461	0,1890	1,9	0,0067	0,0567
1,0	0,5767	0,1764	2,0	-0,0330	0,0455
•	,=,-,		2,1	-0,0660	0,0352

Supposing  $\alpha$  to be small and including terms of the third order we can derive the following formula, taking  $2m\tau = x$ .

$$\frac{2}{\pi_{e}}I = 1 + S(m)\cos x - \frac{\alpha^{2}}{6}\left\{\frac{x^{2}}{2} + \frac{m^{2}}{2} + \left[\frac{S(m)}{2}x^{2} + 2m^{2}S(m) - 6m^{2}T(m)\right]\cos x - 4m^{2}T(m)v\sin v\right\}$$

S(m) is zero for  $m=m_1=1.916$  The intensity has maxima when  $v=2K\pi_0$  and minima when  $x=(2K+1)\pi_0$ , where K is an integral number. The fringes disappear when

 $m_1 = \frac{\pi_o l \varepsilon}{2 \lambda_{\text{off}}} = 1,916,$ 

or

$$\varepsilon = 1,22 \frac{\gamma_{\rm eff}}{l}$$

This is the formula derived by MICHELSON

When a is small, but not zero, we get from the above formula

$$\frac{2}{\pi_0} \frac{\partial I}{\partial x} = -S(m) \sin x - \frac{\alpha^2}{6} \left[ x + [S(m) - 4m^2 T(m)] x \cos x - \left\{ \frac{S(m)}{2} x^2 + [S(m) - T(m)] 2m^2 \right\} \sin x \right]$$

It is known that if m is smaller than  $m_1$ , the equation  $\frac{\partial I}{\partial x} = 0$  has real roots near  $x = K m_0$ . Only the root x = 0 remains fixed when  $\alpha$  and m vary. In the neighbourhood of x = 0 we have

$$\frac{2}{\pi_*} \frac{\partial I}{\partial \pi} = -\pi \left\{ S(m) + \frac{\alpha^2}{6} \left[ 1 + (1 - 2m^2) S(m) - 2m^2 T(m) \right] \right\} + \frac{\pi^2}{6} \left\{ S(m) - \frac{\alpha^2}{3} \left[ (m^2 - 3) S(m) + 5m^2 T(m) \right] \right\} + \pi^2 (...) + \text{higher terms.}$$

When m=0 the coefficient of x is negative. It remains negative as long as m is below the smallest positive value  $\mu$  that makes the coefficient disappear. The root x=0 then corresponds to a maximum of I

The coefficient of x cannot disappear more than for a value of m that makes S(m) of the same order of magnitude as  $x^n$ 

The equation

$$S(\mu) + \frac{\alpha^2}{6}[1 - 2m_1^2T(m_1)] = 0$$

determines  $\mu$ . Developing  $S(\mu)$  in terms following powers of  $\mu - m_1$  and dropping  $(\mu - m_1)^n$ , which is of the order  $\alpha^n$ , one finds the equation:

$$\mu = \frac{\kappa_e l s}{2 \lambda_{eff}} = 1,916 + 0,236 \, \alpha^2$$

or:

$$s = \frac{\lambda_{eff}}{I} (1,22 + 0,15 \alpha^{0}).$$

This formula is not strictly applicable when  $\alpha$  is not very small. When  $\alpha$  is a considerable fraction of the unit,  $\mu$  cannot be derived without a laborious numerical discussion.

HAMY has derived the values of  $\mu$  for the following cases:

In another paper<sup>1</sup> HAMY has made further studies of the problem. The study of variation in the intensity of the central maximum does not permit any conclusion concerning the value of the diameter of the light source.

The disappearance of the two minima encompassing the central maximum ought, on the other hand, to be able to give a value of s if the relation is known between s and l when such a disappearance occurs.

а	μ	411 4	
+	1,992	1,268	
4	1,960	1,248	
Ŧ	1,945	1,238	
Į.	1,932	1,230	
Į.	1,922	1,224	
le l	1,918	1,221	
Ö	1,916	1,220	

One can write the expression for the intensity:

$$I = \int_{-1}^{+1} (1-u^{2})^{\frac{1}{2}} \frac{2-\cos 2\pi (\alpha+1)(u-\tau)-\cos 2\pi (\alpha-1)(u-\tau)+2\cos 2\pi (u-\tau)-2\cos 2\pi \alpha (u-\tau)}{m^{2}\alpha^{2}(u-\tau)^{2}} du.$$

From this can be deduced:

$$\frac{I}{\tau} = 0 = \sum_{p=0}^{p=\infty} (-1)^p \frac{2 - (\alpha + 1)^{2p+4} - (\alpha - 1)^{2p+4} - 2\alpha^{2p+4}}{(2p+3)(2p+4)\alpha^2} m^{2p} \sum_{q=1}^{q=p+1} \frac{(2\tau)^{2q-2}}{I'(2q)I'(p+q+2)I'(p-q+3)},$$

$$\frac{r_I}{r^2} = 0 = \sum_{p=0}^{p=\infty} (-1)^p \frac{2 - (\alpha + 1)^{2p+4} - (\alpha - 1)^{2p+4} - 2\alpha^{2p+4}}{(2p+3)(2p+4)\alpha^2} m^{2p} \sum_{q=1}^{p=+1} \frac{(2r)^{2q-2}}{\Gamma(2q-1)\Gamma(p-q+2)\Gamma(p-q+3)}$$

<sup>1</sup> CR 176, p 1849 (1923).

The problem to be solved is to find the smallest positive value of m and the smallest value of  $\tau$  that simultaneously satisfy the equations. When  $\alpha$  is very small the following solution is found.

$$m = \mu_1 = 1,916 - 1,15\alpha^2,$$
  
 $2\tau = 2,911$ 

By taking "small" values of  $\alpha$ , for instance  $\alpha = \frac{1}{10}$ , and substituting neighbouring values, the unknowns are found by a process of interpolation

199. Danjon's Interferometer-Method 1. The apparatus used in applying this method is of the same type as the interferometer of Jamin, where the interference is caused by a system of thick glass plates. When observing through this instrument, the star to be measured is seen moving upon a field of bright and dark fringes. If the star has no sensible dimension it disappears completely when its light passes through the centre of the dark fringes. But if the star has an appreciable disc, not all the points of this disc will disappear extinction will only be complete along a chord coinciding with the centre of the dark fringe On each side of this chord there are illuminated parts. When the star is circular and has its light uniformly distributed over the disc, the ratio y between the maximum and minimum brightness is defined by

$$\gamma = \frac{1 - J}{1 + J},$$

$$J = 1 - \frac{1}{2} \frac{n}{2^2} + \frac{1}{3} \frac{n^2}{(2 \cdot 4)^2} - \frac{1}{$$

where

and n is equal to  $\pi_{\sigma}\varrho$ , where  $\varrho$  is the ratio between the angular diameter of the star and the distance between the fringes The determination of the apparent radius is thus dependent on actual photometric measurements of the quantity y No results of the experiments at Strassburg have been published as yet.

200. The Companion of Sirius (Sirius B). In his paper on the relation between the masses and luminosities of stars Eddington2 pointed out the possibility that Sirius B had a density of 53000 that of the water, on account of the elections being in the capture zone of two or more nuclei simultaneously. The question whether such density really exists could be settled if the Einstein shift  $+0.62 \frac{m}{R}$  km/sec, amounting to 20 km/sec, could be measured The possibility of testing the general theory of relativity as well as the theory of extremely dense matter was independently pointed out by Bottlinger and by Webi RJ

In 1925 W. S Adams4 communicated the results of measuring spectrograms of Sirius B Direct measurements are difficult on account of the diffuse character of the lines, and the large registering photometer was accordingly used Several observers have checked the measurements. The difference in velocity between Sirius A and Sirius B varies between 2 and 37 km for different spectial lines, but outstanding features of the results are the definite character of the positive displacement and its change with the amount of the wave length. The greater relative intensity of the spectrum of scattered light of Sirius A towards violet and the increasing influence of the superposition of the lines in its spectrum upon those of Sirius B will tend to reduce the amount of measured displacement. An approximate correction was derived from photometric measurements

<sup>&</sup>lt;sup>1</sup> C R 174, p 1408 (1022) 
<sup>2</sup> M N 84, p 308 (1924)
<sup>3</sup> Berlin-Babelsberg Veroff 3, No 4 (1923), A N 220, p 189 (1924) 4 Wash Nat Acad Proc 11, p 382 (1925)

of the relative intensities of the continuous spectrum of Sirius A and Sirius AB The correction factor d is found from.

$$d=1+\frac{k_A}{k_B}$$

where  $h_A$  is the density of the spectrum of scattered light of Sirius A, and  $h_B$  that of the companion. By applying the correction factors the mean values were found

Hg . . . +26 km/sec H<sub>7</sub> . . . +21 ., Additional lines . . +22 ...

The relative orbital velocity at the epoch is +1,7 km/sec. The remaining displacement of 21 km is interpreted as a relativity displacement. The following elements for Sirius B were derived by using Seares's values for surface brightness, on the alternatives of F0 or A5 for the spectral class.

	Yo	AJ
Surface brightness Radius	-0=,88 24000 km	-1 <sup>m</sup> ,45 18000 km
Donalty (Water = 1) Relativity displacement .	30000 +0,23 Å	64 000 0,32 A

The radial velocity of Sirius B also was determined at the Lick Observatory in 1928. J. H Moore found the following values on the basis of 4 spectrograms:

The result of ADAMS is thus confirmed

Although the idea that Sirius B is an enormously dense body seems to be accepted generally, it seems fair to consider some other explanation. And and others suggested that the light of the companion is reflected from a dark body. The fact that the spectrum is not identically the same as that of the primary does not make this theory impossible. Because of its general importance for stellar photometry we give a short review of Anding's paper.

A luminous surface element d/ with intensity I emits light at an angle of emanation s to an element df' at the distance r, and at an angle of incidence s'.

The light received by df is:

$$dL = I d/\cos \frac{df' \cos t'}{dt}.$$

The element d' not emitting light itself reflects the light dL' at an angle of emanation s' to another element d':

$$dL' = I d/\cos \epsilon \frac{1}{A} \frac{A}{\kappa} df' \cos \theta' \cos \theta' \frac{1}{A} df'' \cos \theta'',$$

where A is the albedo according to the definition of LAMBERT, " the angle of incidence of this element and / its distance.

Applying this to Sirius we have the integral J (extended over an hemisphere).

$$J = \int I \, d/\cos \epsilon,$$

<sup>1</sup> Publ A S P 40, p. 229 (1928).

AN 229, p. 69 (1926).

as the expression for the luminosity of the star. If  $D_{\epsilon}$  is the distance of Silius A from the Earth, the density of its light rays as observed by us is

$$H_s = \frac{J}{D_s^2}$$
.

Further we introduce

$$df' = R_c^2 d\sigma'$$

where  $d\sigma'$  is the surface element of a sphere of unit radius and  $R_a$  the radius of Sirius B The angle between the radius vector Sirius-Companion and the radius vector Earth-Sirius is called  $\pi_0 - \alpha$  Then we have

$$\int \cos i' \cos \varepsilon' \, d\sigma' = \frac{2}{3} \left[ (\pi_0 - \alpha) \cos \alpha + \sin \alpha \right]$$

Further in the formula for dL' above r' stands for  $D_{\mathfrak{o}}$  (the distance of the compamon from the Earth), and the value of the light He from the companion is.

$$H_o = J \frac{R_e^2}{r^2} A \frac{2}{3\pi_e} \{ (\pi_e - \alpha) \cos \alpha + \sin \alpha \} \cdot \frac{1}{D_e^2}.$$

The distance of Sirius A is equal to that of Sirius B, or  $D_o = D_a$  We then get the expression for the ratio of the light of the two objects

$$\frac{H_o}{H_s} = A \frac{R_o^2}{r^2} \frac{2}{3\pi_o} \{ (\pi_o - \alpha) \cos \alpha + \sin \alpha \}$$

For simplifying purposes we assume A = 1, r equal to the mean distance a between Sirius A and B, and  $\alpha = \frac{\pi_0}{2}$ 

Then

$$\frac{II_e}{H_e} = \frac{2}{3\pi_e} \left(\frac{R_e}{a}\right)^2$$

or expressed in magnitudes

$$m_c = m_s + 1.7 - 5\log\frac{R_c}{a}$$

The value of a is 20 astronomical units and the mass of the companion equals the mass of the Sun If  $R_o$  is supposed to be equal to the Sun the following value is found

$$m_0 = 18^{\rm m} 5$$
.

Thus Sirius B should be ten magnitudes fainter than is the actual case. If  $R_{
m e}$ is computed from the value  $m_0 = 8.5$  it is found that  $R_0 = 100$  0 and the density would be 1/955000 of that of the Sun! The observations show the contrary to be the case, but it might be possible to explain the facts in favour of the reflection theory if the companion is surrounded by a swarm of dark bodies having the character of a dust-cloud

A detailed investigation does not make the existence of such a dust-cloud very probable Another hypothesis is that the companion of Sirius is a close binary system where one of the components is dark and has the same mass as the Sun. If the distance between the dark companion and Sirius B is equal to one planetary unit, the magnitude of the dark companion will be 21m,8 on account of the light reflected from Sirius B, if the same distance is 0,1, the magnitude of the dark companion will be 16m,8.

In order to test the theory it will be necessary to observe the radial velocity of Sirius B at different epochs, because in the case of an orbital motion the radial velocity of Sirus B will show corresponding variations

201. Diameters from Scintillation-Observations. G. Ticnov<sup>1</sup> has used the colour changes caused by the scintillation of the stars for computing the apparent diameters. From 77 stars he finds the simple relation.

$$d = \frac{5.5036}{S} - 0.0607$$

where d is the diameter in seconds of arc, and S the number of changes in the colour in a second of time

The theory of scintillation shows that the blinking is related in a simple way to the apparent diameter of the stars Durour has found that the red stars do not undergo such rapid changes as the white stars. Montigny has published a series of papers concerning the scintillation and he has given, in a catalogue, observations of the number of colour changes for 120 stars. I have used his data and tried to establish a relation analogous to that of Tichov, but so far without success. It seems that so many variables enter into the determination of the number of changes that the diameter is a very complicated function of S. Anyhow, it is clear that the diameters cannot be determined from the material of MONTIGNY with such an accuracy as when they are derived from observations of colour and magnitude The details of Tichov's investigation have not been necessible to me and it is possible that his data are more accurate than those of MONTIGNY.

202. The Fallacy in S. Pozzewsky's Method. This method was based on the use of elliptically polarised light and was published at first in the year 1912. and later on in 1915. As plans have been made to apply the method in practice, EDDINGTON® took up the "ungrateful and ungracious" task of showing the breakdown of the method The essential principle is the bringing into superposition of two widely separated beams that have been previously polarised in perpendicular planes. If the phase-difference is zero or 12, plane polarized light is obtained, and circularly polarized light for phase differences of \$\frac{1}{4}\text{ or \$\frac{1}{4}\text{.}} For intermediate values elliptically polarised light is obtained, which cannot be completely extinguished by a Nicol prism as is the case with plane polarised light. With point-source light the phase difference can be made zero and the image completely extinguished, but with a finite disc the difference will not be zero for all points of the disc simultaneously and the image will not wholly disappear. The angular diameter should result from the intensity of the realdual image. The fallacy in the method arises according to Eddington from the fact that the intensity that is calculated by Pokrowaky is not that of the whole starimage, but the intensity at a certain point in the focal plane. If the star is slowly displaced with regard to the instrumental axis, its image does not pop in and out, but bright and dark interference bands pass across the point considered.

The inadequacy of the treatment in the paper of Pokrowsky arises on account of the assumption that for a point-source plane waves emerge from the two apertures and travel in a particular direction. Owing to the diffraction, the waves travel in various directions inclined at angles that are not small compared to the angles, such as 0",003, occurring in the investigation.

Mittellungen Leshafts Inst Loningrad (Russian) 2, p 126 (1921).
 Recoull inaugural de l'Université de Lausanne (1892). La scintillation des étolics.

Bull de l'Acad Roy Belg Ser. II, 25, p 631 (1868); 29, p. 80 (1870), 29, p. 455 (1870); 37, p. 165 (1874); 38, p. 300 (1874) (Catalogue', 42, p. 255 (1876); 44, p. 694 (1877); 43, p. 391 (1878); 46, p 17 (1878), 46, p 328 (1878), 46, p. 596 (1878), 47, p. 755 (1879); 48, p. 22 (1879) Ser. III, 1, p 231 (1881), 6, p 426 (1883), 9, p. 85 (1885); 16, p 160, 553 (1888); Ann de l'Obs Bruxelles 1878, p 245.

Ap J 36, p. 156 (1912); AN 192, p. 21 (1912); BA 29, p 305 (1912), Ap J 41, p 147 (1915).

MN 87, p. 34 (1926).

#### e) The Densities of the Stars.

203. Densities of the Stars. Pioneer Work. The densities of the stars can. of course, be derived as soon as their masses and dimensions have been computed. A determination of the density itself is only possible in cases of visual binaria's

and echosing variables and involves a knowledge of the mass ratio

E C, Pickering and later on W H S Monck have separately derived at equation for binary stars with known orbital elements which renders it possible to determine the relation between brightness and mass of these stars quite independently of their distance. It is easy to show that the formula don't not distinguish between the extent of the surface and the temperature difference in mass-brightness may be due to variety in mean density (diameter) or to variety in surface brilliancy or temperature. The effects observed will be quite the same Pickering realized that if the temperatures were considered as not varying from star to star the mean densities of binary stars could be easily derived

In a paper of 1891 E. W MAUNDER<sup>8</sup> drew attention to several cucumstances that indicate that the spectral class marks a difference in constitution inthi: than a difference in the stage of development. In this paper the author computed the densities of 51 double stars assuming that the intrinsic brightness per unit of surface is the same for all the stars, which is far from truth. He found for the Sirian stars the mean density  $\bar{\rho} = 0.0211$  O and for the solar stars  $\bar{\rho} = 0.102611$ He also determined the ratio of the absolute brightness of the two groups of stars as 45,6/70,5, corresponding to a difference in absolute magnitude of  $10^{11}$ , 15. whereas it should be  $-3^{M}$ , 3 The author also points out the possibility of name the double stars for studying the differences in absolute magnitude of different spectral groups

204. Densities of Visual Binary Stars The densities of visual binary stars have recently been computed by E OPIK, who derived a relation giving the mean densities e, expressed in terms of the elements of the orbit and of the masses  $\mathfrak{M}_A$  and  $\mathfrak{M}_B$  (Solar mass is taken as unit ) If R is the radius of the primary star in linear measure and  $I_A$  the surface brightness of the primary expressed in that of the Sun as unit,  $v_A$  the apparent brightness, and  $\pi$  the parallely,

the relation.

$$\frac{I_A}{I_A} = R^2 \pi^2 \sin^2 4''$$

is immediately derived Further we have the well-known equation'

 $\mathfrak{M}_A + \mathfrak{M}_R = a^3 \pi^{-3} P^{-2}$ 

Further

$$\mathfrak{M}_A = \varrho_A R^3$$
,  $\mathfrak{M}_A + \mathfrak{M}_B = \varrho_A R^3 \left(1 + \frac{\mathfrak{M}_B}{\mathfrak{M}_A}\right)$ 

And

$$\log \varrho_A = \log \frac{a^3}{P^2} + \frac{3}{2} (\log I_A - \log \iota_A) - \log \left(1 + \frac{\mathfrak{M}_B}{\widehat{\mathfrak{M}}_A}\right) - 3 \log 206265$$

Taking the stellar magnitude of the Sun to be -26m,60, we have:

$$m_A + 26,60 = -2,5 \log i_A$$

Expressing the surface brightness in stellar magnitudes and taking the Sun as unit: '  $I_A = -2.5 \log I_A$ 

<sup>8</sup> JBAA 2, p 35 (1891); Astronomy and Astrophysics 11, p 145 (1892), Ap J 44, p 293 (1916).

<sup>&</sup>lt;sup>1</sup> Proc Amer Acad of Arts and Sciences 16, p 1 (1880) <sup>2</sup> Obs 10, p. 96 (1887)

and after substitution, the following formulae

$$\log \varrho_A = \log \frac{a^3}{P^4} + 0.6(m_A - j_A) + 0.02 - \log \left(1 + \frac{\Re j}{\Re l}\right),$$

$$\log \varrho_B = \log \frac{a^3}{P^4} + 0.6(m_B - j_B) + 0.02 - \log \left(1 + \frac{\Re l_A}{\Re l_B}\right),$$

give the densities of the two components.

The surface temperature depends on the absolute temperature and thus, also, on the spectral type. This dependence can be derived from the colour index, but OPIK preferred to use the effective temperatures of 109 stars, as determined by Wilsing and Schringer If  $\lambda_{\bullet}$  and  $\lambda_{\odot}$  denote the wave lengths of maximum spectral energy of the two sources, Planck's formula gives for the spectral region  $\lambda$ :

$$\frac{I_{\bullet}}{I_{\odot}} = \frac{e^{\frac{4,9652_{\odot}}{2}}}{\frac{4,9652_{\bullet}}{2}}.$$

For visual light we have  $\lambda = 0.56 \,\mu$ ,  $\frac{4.965}{\lambda} = 8.87 = c$ , and the difference (in magnitudes) of the visual surface brightnesses of a star and the Sun becomes

$$j = 2.5 \log \frac{e^{\lambda_1 - 1}}{e^{\lambda_2 - 1}}$$
.

From Wien's formula,  $\lambda_{\bullet} T = 2940$ ,  $\lambda_{\bullet}$  can be computed if T is known

The effective temperatures determined by Wilsing and Scheiner are probably systematically too low. The temperature of the Sun, 5130°, corresponds to a value, 1,16 cal/cm $^{-1}$  of the solar constant, which is much smaller than the value observed, 1,6-1,7 cal/cm $^{-1}$ . The value for  $T_{\odot}$ , 6250°, as derived by Abbot and Fowle, was therefore assumed as a zero-point, and the Potsdam temperatures were differentially corrected.

OPIR finds from the table giving the means of T for various spectral subdivisions and the mean reduced wave length of the spectral energy-maximum that the temperature varies somewhat irregularly with spectral class. The fact that the spectral scale is qualitative makes it possible that the abrupt changes in T

between some stellar classes may be real

The mass-ratio must also be known for a computation of the densities. There are few cases where such a determination has been possible, and it is necessary to assume that the relation between  $M_B - M_A$  and  $\mathfrak{M}_B/\mathfrak{M}_A$  is known. Eleven cases were available, and from them the following table was derived.

The results as to the densities are not reviewed here because the following investigation by BERNEWITZ contained a more extensive material than that at disposal in 1916.

In 1921 E. Bernewitz published an investigation concorning the densities of

Ma-Ma	TRA/BIA	Maria	SE PLANT
0 ,8 0 ,8 1 ,0 2 ,0	1,00 1,00 0,95 0,88	3 <sup>11</sup> ,0 5 ,0 10 ,0	0,76 0,60 0,30

binary stars. The formula giving  $q_4$  was adopted in the form:

$$\log q_{\perp} = \log \frac{e^{\theta}}{2^{n}} + 0.6(m_{\perp} - j_{\perp}) - \log(1 + \frac{\Re p}{\Re n}) + 0.089.$$

<sup>1</sup> AN 213, p 1 (1921).

The determination of the surface magnitude 1 is based on the equation of Planck'

$$\frac{I_*}{I_{\odot}} = \frac{\left(e^{\frac{c_*}{\lambda}}I_{\odot} - 1\right)}{\left(e^{\frac{c_*}{\lambda}}I_{\odot} - 1\right)} = 2.512^{-j}$$

The quantity  $\eta_{A}$  has to be defined in the same way as the apparent magnitude m and thus account must be taken of the visibility curve  $g(\lambda)$  of the human eye. We can assume

$$-0.4\log\int_{0}^{\infty} \left[\frac{c_{1}\lambda^{-5}}{e^{\frac{c_{1}}{2T_{4}}}-1}\right] g(\lambda) d\lambda = m$$

The function  $g(\lambda)$  is taken in accordance with Henning's icsult<sup>1</sup> as

$$g(\lambda) = \left[\frac{5520}{\lambda} e^{1-\frac{5520}{\lambda}}\right]^{140} + 0.1 \left[\frac{4600}{\lambda} e^{1-\frac{4600}{\lambda}}\right]^{1000} - 0.07 \left[\frac{6600}{\lambda} e^{1-\frac{6600}{\lambda}}\right]^{1000}$$

The values of the integral are computed by means of numerical integration. The following corrections have to be applied to the visual magnitudes

Spectral class	Correction of m	Autt	Spectral class	Correction Am	Jeft
A0	+0 <sup>10</sup> ,049	5420	Ko	-0 <sup>m</sup> ,035	5580
G0	0,000	5490	K5	-0 ,041	5630
G5	-0,022	5540	Me	-0 ,039	5680

The effective temperatures were used as determined by Wilsing The following values of j were found

Spectral class (ADAMS)	$\frac{c_1}{T}$	1	Spectral class (Adams)	$\frac{c_s}{T}$	1
B0 B5 B8 A0 A2 A5 A8 F0 F3 F5 F8	1,45 1,45 1,48 1,53 1,62 1,72 1,87 1,99 2,16 2,29 2,50	- L <sup>13</sup> , 93 -1, 93 -1, 87 -1, 76 -1, 58 -1, 37 -4, 07 -0, 83 -0, 49 -0, 24 +0, 18	G0 G3 G5 G8 K0 K3 K5 K8 Ma Mb	2,64 2,85 3,00 3,28 3,52 3,92 4,18 4,48 4,62 4,76 4,87	+0 <sup>m</sup> ,45 +0 ,86 +1 ,15 +1 ,70 +2 ,16 +2 ,94 +3 ,45 +4 ,03 +4 ,51 +4 ,78

For the determination of the mass-ratio 10 pairs were used and the following relation resulted:

d ##	Ma Ma	d m	90t <u>H</u>	d m	$\frac{\mathfrak{M}_A}{\mathfrak{M}_B}$
0 <sup>M</sup> ,0	1,00	2 <sup>M</sup> ,0	0,81	4 <sup>M</sup> ,0	0,68
1 ,0		3 ,0	0,74	5,0	0,62

For 31 out of 63 pairs, only the mean density of both components could be computed. An attempt was made to find a relation between absolute magnitude and density. The results are given in the following table.

<sup>1</sup> Jahrb d Radioakt u Elektronik 1919, H 1.

The data under the heading II refer to the remaining material when 5 spectroscopic pairs and α Centauri were excluded By forming the part I of the table o Eridani, Sirius B and ε Hydrae were excluded We see from the table

that there is a steady

λī	I		п	Limits of	
AI .	ē	,	<u> </u>		apentral class
o™,8	0,08 ①	4	0,080	4	AO-F3
1 .5	0,20	6	0,14	4	A0-F2 (F1)
2 ,6	0,26	10	0,23	9	A0 (A2) - G
3 ,5	0,24	9	0,24	9	A2-K2
4 ,6	0,58	12	0,45	11	F1 (14)-G;
5 ,6	0,43	12	0,40	11	F5-K0
6 ,2	0,45		0,50	8	1'2-K5
7 ,9	0,47	5 2	0,47	5	K2-K5
10 ,8	2,81	2	2,81	2	Mb

increase in the mean density from  $0.08 \odot$  to about  $0.5 \odot$  Between  $5^{M}$  and  $40^{M}$   $\bar{\varrho}$  is sensibly constant, but seems to increase for  $M > 40^{M}$ . There also seems to be a certain increase in  $\bar{\varrho}$  with spectral class from A2 to Mb, but the evidence

is rather uncertain

A. R. Thompson 1 has recently derived the formulae for computing the density of binary stars, evidently without any knowledge of earlier work. In several cases the agreement with earlier results is not very good. The principal cause of such deviations is to be sought in different assumptions concerning the temperature. The uncertainties arising from uncertain mass-ratios and uncertain orbital elements are not of nearly such importance as those arising from differences in the scale of effective temperatures.

I have derived the absolute magnitudes of most of the objects in Thompson's

list and have found the following dependence between M and  $\bar{\varrho}$ :

М	ē		И	I	,
Brighest-0",0	0,33 ①	2	6×,0- 7×,9	2,430	16
0×,0-0 9	0,14	3	8 ,0-10 ,9	3,50	3
1 ,0-1 ,9	0,36	16	Kra 60 A	62	1
2 ,0-2 ,9	0,94	17	of Krid C	48	1
3 ,0-3 ,9	0,54	17	Kr0, 60 B	9,6	1
4 ,0-4 ,9	1,40	15	o* Erid. B	16600	1
5 ,0-5 ,9	0,99	15	Sidus B	46000	1

There seems to be a general relation between the absolute magnitude and the density, but the dispersion is considerable. In spite of all the uncertainty that is undoubtedly connected with the derivation of  $\bar{\varrho}$ , it is difficult to avoid the impression obtained from a close scrutiny of the material that the actual relation between M and  $\varrho$  is not a one to one correspondence. This question has undoubtedly some bearing on the question of the character of the mass-luminosity law.

205. The Ratio of Densities in Double Stars. From the formula quoted earlier it follows immediately that

$$\log Q_A - \log Q_B = 0.6 (m_A - m_B) - 0.6 (j_A - j_B) + \log \frac{m_A}{m_B}$$

If both the spectra are known and the mass-ratio can be approximated, the ratio of the densities can thus be computed without any knowledge of the elements of the orbit. The mass-ratio can be computed from the formula:  $\frac{m_s}{m_s} = -0.61 + 0.36 (M_B - M_A)$  derived from a least square solution using existing material.

If both spectra have been observed the above formula will give us the change in logarithm of density  $\Delta \log q$  for different groups. We can also form the

<sup>1</sup> JBAA 39, p. 247, 253 (1929).

mean values of  $d \log \varrho / dS$ , where dS gives the change in spectral index. Putting

$$\frac{\Delta \log \varrho}{\Delta S} = \varphi(S)$$

it will be possible, by applying a process of graphical integration, to find the curve

$$\log \varrho = \psi(S)$$

which gives the relation between density and spectral class. An attempt has been made to derive this curve but it seems that the present material is rather scanty and that we should wait for a more extensive material. A practical difficulty arises on account of the selection in the material which favours small  $\Delta S$  (equal spectra). This part of the material can be used for a derivation of the dispersion in  $\log\varrho$  for the different spectral classes. The following small table gives the results hitherto obtained

Spectral class	$\Delta \log \varrho$	σ⊿ log ϱ	Mean spectral index (B=1,0, M=5,0) and its dispersion	11
B	0,68	士0,50	0,4 ± 0,3	19
A	0,47	士0,38	1,4 ± 0,3	11
F	0,23	士0,35	2,5 ± 0,2	11
G	-0,07	士0,41	3,3 ± 0,2	7
K	+0 13	士0,11	4,7 ± 0,4	5

206 Densities of Echpsing Binaries. Methodical. The possibility of deriving the mean density of an echpsing binary system was first pointed out by Meriau<sup>1</sup> in 1896. We have

$$P^{2} = \frac{k a^{3}}{\mathfrak{M}_{A} + \mathfrak{M}_{B}} = \frac{3 k a^{3}}{4 \pi_{c} (r_{A}^{3} \varrho_{A} + r_{B}^{3} \varrho_{B})}$$

where k is a constant, P the period, a the semi-axis major of the orbit,  $\varrho_A$  and  $\varrho_B$  the densities of the two components,  $r_A$  and  $r_B$  then radii Putting  $r_A = an_A$ ,  $r_B = an_B$ , and  $3k/n_o = k_1$ , we have

$$P^{2} = \frac{h_{1}}{4 \left( n_{A}^{3} \varrho_{A} + n_{B}^{3} \varrho_{B} \right)},$$

$$\bar{\varrho} = \frac{n_{A}^{3} \varrho_{A} + n_{B}^{3} \varrho_{B}}{n_{A}^{3} + n_{B}^{3}},$$

when  $\bar{\varrho}$  is the mean density of the two components

In the case of a circular orbit the duration of the eclipse is  $2\pi_0 t/P$  where t is the duration of the light variation. Further let i be the inclination of the orbital plane. Then

$$n_A + n_B = \left(1 - \cos^2\frac{\pi_a t}{P} \cos^2 t\right)^{\frac{1}{2}}$$

and thus

$$\bar{\varrho} = \frac{(n_A + n_B)^3}{4 (n_A^3 + n_B^3)} \frac{h_1}{P^2 \left(1 - \cos^2 \frac{\pi_e t}{P} \cos^2 t\right)^{\frac{11}{2}}}.$$

The term  $(n_A + n_B)^8$  is  $\leq 4(n_A^3 + n_B^8)$ . If  $r_A = r_B$ , the limiting value of the first factor of the expression for  $\bar{\varrho}$  is 1, and if  $r_B = 0$  (no eclipse then takes place), the same factor has the value  $\frac{1}{4}$   $n_A$ ,  $n_B$ , P, t, and t can be derived from the light-curve and the value of  $k_1$  is taken from solar data:

Thus  $\bar{\varrho}$  can be computed

$$k_1 = 5.56 \sin^3 46' 2''$$

<sup>1</sup> CR 122, p 1254 (1896).

In the case of an elliptical orbit the formulae become very complicated.

A. W ROBERTS discussed in 1899 the densities of four Algol stars and derived the following expressions for the densities

$$\begin{split} \varrho_A &= \frac{(0,0092)^3}{p^3 P^4} \left( \frac{\mathfrak{M}_A}{\mathfrak{M}_A + \mathfrak{M}_B} \right), \\ \varrho_B &\coloneqq \frac{(0,0092)^3}{q^3 P^4} \left( \frac{\mathfrak{M}_B}{\mathfrak{M}_A + \mathfrak{M}_B} \right), \end{split}$$

where P is the period (in years), p and q the diameters of the components, expressed in terms of the semi-axis major of the system.

As the two mass terms must always be less than unity or rather as only one of them can ever approach unity, a limit is given in one direction by the expressions

 $\lim \varrho_A = \frac{(0,0092)^4}{p^3 P^4}, \quad \lim \varrho_B = \frac{(0,0092)^4}{q^4 P^4}.$ 

The following results were obtained:

	llm e₄	lbn e z
X Carinao , , ,	0,25	0,25
S Volorum	0,61	0,03
RR Centauri	0,27	0,27
RS Sagittarii	0,16	0,21

At the same time H. N. Russell's made a derivation of a limiting value for the mean density of 17 variable stars of the Algel type and found.

$$\frac{Q_{AB}}{3} < \frac{W_A + W_B}{3} \cdot \frac{1}{3} \cdot \frac$$

Now

$$r_A^3 + r_B^3 \ge \frac{1}{2} (r_A + r_B)^3$$

the sign of equality only holding good when  $r_A = r_B$ 

At the first and fourth contacts we have the projection of the distance between the centres of the two stars upon a plane perpendicular to the line of sight  $= r_A + r_B$ . The arc described during the time from the beginning to the middle of the eclipse is  $n_a t/P$ , where t is the duration of the light variation, and the projected displacement is  $a \sin n_a t/P$ , where a is the radius of the orbit. Then we have the condition:

$$r_A + r_B \ge a \sin \frac{\pi_a t}{D}$$
.

The sign of equality only holds good when the transit is central. Besides there is the relation

 $\mathfrak{M}_A+\mathfrak{M}_B=h\frac{a^*}{2^*}$ 

and thus:

$$Q_{AB} \leq \frac{3h}{z_{a}P^{a}\sin^{a}\frac{\pi_{a}t}{P}}$$

Taking the Earth density as 5,53 Russell found  $3k/n_e = 44,1$  (the unit of the time being  $1^{\rm h}$  and the unit of density that of water), and derived the densities for 17 stars.

207. Shapley's Work. In 1915 H Shapley published his extensive research concerning the orbital elements of 90 eclipsing binaries based on nearly 10000 magnitudes obtained with the polarizing photometer of the observatory at

<sup>&</sup>lt;sup>1</sup> Ap J 10, p. 308 (1899)

Ap J 10, p. 315 (1899)

PRINCETON¹ The memori discusses the theory of the orbital determination, and then all existing observational data were used for deriving the elements. The total number of observations used is 27094. A general experience in the discussion of this extensive material is that the light curves of eclipsing binaries are, in general, symmetrical, smooth, and regular. The inegularities and anomalies that are often reported in the older literature do not gain any support from accurate photometric work. The investigations of Shapley also disposed of the supposition so prominent in earlier days that one component of the ordinary Algol star is non-luminous. The disparity in brightness of the eclipsing binaries is even smaller than in the case of visual binaries. In all cases except for five or six eclipsing binaries there is positive evidence that the fainter star is itself luminous.

The existence of a darkening toward the limb of the same order of magnitude as in the Sun seems to be well established. It was also found that there is general agreement between the actual gravitational elongation of eclipsing binary stars and the theoretical ellipticity of homogeneous fluid bodies according to G. II. Darwin's investigations

By assuming that the components of each binary are equal to the Sun in mass the "equal mass densities" were computed according to the formulas

$$\varrho_A = (5.29 P^{\frac{9}{3}} r_A)^{-3}, \quad \varrho_B = (5.29 P^{\frac{9}{3}} r_B)^{-3},$$

where P is the period in days,  $r_A$  and  $r_B$  the radii, the radius of the relative orbit being taken as unit, and  $\varrho_A$  and  $\varrho_B$  the densities. These were corrected for polar flattening and for the mass-ratio. The mean density is independent of the total mass of the system relative to the Sun, but a knowledge of the mass-ratio is essential for a derivation of the mean densities of the components. At that time the spectroscopic data for eclipsing binaries were very scanty

The corrected densities for "darkened" solutions were compared with the spectral classes and the following distribution, which is still of interest, was found:

Spectral class	В	A	F	G	К	Spectral class	13	A	ŀ	G	К
+0,5 to 0,0 0,0 ,, -0,5 -0,5 ,, -1,0 -1,0 ,, -1,5 -1,5 ,, -2,0	8 5 3	11 24 13 6	7 3	1 1		-2,0 to -3,0 -3,0 ,, -4,0 -4,0 ,, -5,0 -5,0 ,, -6,0	1		i	2	1

208. Parallaxes and Absolute Magnitudes of Eclipsing Binaries. The parallaxes of eclipsing binaries have been derived by H N Russell and H Shapley on basis of the following considerations. If the radius and the surface brightness of a certain star are R and J, expressed in units of the solar radius and surface brightness, respectively, we have

$$M = 4.75 - 5 \log R - 2.5 \log J$$

The elements of the eclipsing systems give us the value of r, that is the radius of the brighter component expressed in units of the mean distance a of the components. The mass is assumed to be  $2\mathfrak{M}$  times the Sun's mass. Taking the radius of the Sun as unit and expressing the period, P, in days the mean distance will be

$$a = 5.29 P! \mathfrak{M}!$$

<sup>&</sup>lt;sup>1</sup> Princeton Obs Contr. No 3 (1915)

Hence

Setting for brevity  $5,297P^1 = A$ 

we find.

$$M = 4.75 - 5 \log A - 4 \log \mathfrak{M} - 4 \log J$$

A may be derived from the known elements of the eclipsing system. The parallax  $\pi$  is then found from the formula:

$$M = m + 5 + 5 \log \pi$$

For computing M and  $\pi$  two assumptions have thus to be made, viz. the value of  $\mathbb{R}$  and of J When the spectral class is known, both the quantities can be fairly approximated and thus also a tolerable value of M or  $\pi$  computed. In this way the parallaxes of some 100 eclipsing binaries have been computed. In the cases where the masses are known the individual densities of eclipsing binaries can be derived with a considerable degree of accuracy.

209. Recent Statistics of the Eclipsing Binaries. These stars give valuable contributions to our knowledge of several of the physical properties of the stars. Also in those cases where no orbits have been calculated but the eclipsing nature of the pair is known, the maximum possible mean density can be derived.

DEAN McLaughlin has discussed the data of eclipsing binaries Altogether photometric orbits have been derived for 116 stars. The densities of the brighter components of each binary are tabulated against spectra as follows.

Relation between spectrum and density.

Density Spentral class	O-Di	DS-AS	A5-F5	14-G5	X-M	800
<0,001		1	1	2		4
0,0010,01	2	2		2		6
0,01 -0,05	6	7	1	1		15
0,05 -0,10	4	15	4			20 38
0,10 -0,30	3	31	4			38
0,30 -0,70		16	7	1		24
0,70 -1,0		2	1			3
>1,0				3	1	4
Sum	15	74	15	9	4	114

Mean values of the radii  $r_A$  were derived for certain period intervals as is shown in the next table.

11-4-4-	Mesn period	Radius of	Radios of b	dighter ster	_
- Perioda	(1)	orbit is km.	in parts of a	is km	
< 14,0	04,6	4,2-10	0,37	1,6 - 10	16
14,0 - 2,2	1,6	8,0	0,30	2,4	24
2,2-3,2	2 .7	11,4	0,23	2.6	21
3,2 - 4,25	3 .7	14.0	0,21	3,0	17
4,25- 5,3	4 .7	16,4	0,19	3,2	13
5,3 - 7,0	6,0	19,3	0,19	3.5	9
7,0 - 10,0	8 ,5	24,3	0,10	2,4	4
10 -100	25	50	0,14	7,1	9

The radii of the orbits have been calculated from the formula  $80 = \frac{4}{10^{20}} \cdot \frac{a^2}{10^{20}}$ . The average mass of eclipsing binaries is, in fact lower than that value but

RUSSELL and SHAFLEY, Ap J 40, p. 417 (1914) and subsequent papers by numerous workers within this field.

A J 38, p. 45 (1927).

scopic eclipsing binaries, the computed radii will be diminished by only 16 percent.

The radii of the stars are more nearly constant than the radii of their orbits.

The stars of the period group <1<sup>d</sup>,0 days are probably smaller than has been calculated, since they are dwarfs which are less massive than has been assumed

It seems likely that the discovery-chance has resulted in an unduly large radius for stars of periods 1<sup>d</sup>,0-10<sup>d</sup>,0 since the greater radii will mean longe duration of eclipse. Then it is quite possible that the average radius will be nearly constant.

## f) The Masses of the Stars.

210. Methods of Deriving Stellar Masses. The laws of gravitation furnish a method of deriving the masses of heavenly bodies. As soon as a gravitational effect exercised by one body on another can be measured the mass is easily determined. Inasmuch as the motions of the stars are not known to such an extent and accuracy that we can determine any curvature of the orbits it is no possible to derive any masses. The only cases for which it has been possible to determine individual masses is when the absolute orbit of a visual double star has been derived with accuracy or when the Doppler displacements in both spectra of an eclipsing binary star have been measured. When both spectra is an ordinary spectroscopic binary are exhibited and their displacements measure the mass-ratio can be accurately determined. When the relative orbit of one component of a visual binary is known the sum of the masses of the component can be determined. In the case of spectroscopic binaries showing one spectrum a rather complicated function of the mass can be derived, which treated statistically can yield results of value concerning the mean mass of groups of stars.

For groups of visual binaries for which the orbital motion has been observed but the orbital elements are unknown, the mean value of the masses can be derived

if the distances are accurately known.

Finally there seems to be some gravitational effect in the upper layers of the atmosphere of the stars affecting the intensity of certain lines in spectra. The problem cannot be said to be solved as yet, but some mass-effect seem to be present in the spectrographic parallaxes, which fact will probably lead of methods of determining the stellar mass from certain spectral characteristic

In the case of clusters or agglomerations of stars of cluster structure it possible to determine the mass-ratios of such groups of members as have a different spatial distribution and hence a different distribution when projected a photographic plate. The differences in the space densities are effects of the gravitation (e. g. heavy bodies will be more concentrated towards the centre the agglomeration than less massive ones) and when the distribution in space of the separate groups is known the mass-ratios can be derived. This, of cours involves accurate determinations of the distance of the agglomeration.

The cases mentioned are the only ones where a direct determination of the masses or the mean masses of groups can be performed. In order to extend our knowledge to ordinary stars we have to search for simple relations between the

masses and other characteristics of the stars.

Such a relation is known to exist between mass and spectral class; there also a relation between mass and luminosity, which was first found empiricall but later on derived from the theory of radiative equilibrium. The establishmen of the mass-luminosity relation is of fundamental importance and too many effor can scarcely be made with regard to the accurate derivation of this relation fro empirical data and theoretical deductions. It is possible that the mass-luminosi

relation only represents a first approximation and that the actual relation should include a second variable, the effective temperature.

The mass can also be related to the reduced proper motion, which is sometimes of advantage. There probably exists a relation between the density and the mass, but it cannot at present be established with any accuracy. There seems to be a relation between the mean mass of a group of stars and the mean squared space- (or radial) velocities of the same group (equipartition of energy).

The sum of the masses of the two components in a binary system is found

applying the third law of KEPLER ("the harmonic law"). We have:

$$\mathfrak{M}_A+\mathfrak{M}_B=\frac{\sigma^4}{\pi^4\,P^4},$$

if we select as units the year and the solar mass. The major axis a is taken in seconds of arc as well as the parallax  $\pi$ .

In the case of spectroscopic binaries this equation can be written:

$$\mathfrak{M}_A + \mathfrak{M}_B = \frac{4\pi!}{h^4} \frac{(a_A + a_B)^2}{P^4}$$

(h is the Gaussian constant,  $\log k = 8,23558 - 10$ ) or:

$$\mathfrak{M}_A+\mathfrak{M}_B=k'\frac{a^2}{D^2}$$

where P is the period expressed in days, a the major axis expressed in km, and k' a numerical constant. We do not know a or  $a_A + a_B$  but only its projection a sin; and thence we have to multiply both members with  $\sin^2 k$  where k is the inclination of the orbit.

Thus: 
$$(\mathfrak{M}_A + \mathfrak{M}_B) \sin^2 i = k' (a_A \sin i + a_B \sin i)^2 P^{-2}$$
.

From the theory of the determination of orbits of spectroscopic binaries we have:

$$a_A \sin i + a_B \sin i = K'(K_A + K_B) P \sqrt{1 - 6^a}$$

where  $K_A$  and  $K_B$  are the semi-amplitudes of the radial velocities of the two components, expressed in km/sec, and k'' is a constant, hence.

$$(\mathfrak{M}_A + \mathfrak{M}_B) \sin^6 i = k_1 (K_A + K_B)^5 P (1 - 6^3)^{\frac{1}{2}}$$
.

The numerical value of  $\log h_1$  is 3,01642 - 10.

If both spectra have been measured we have:

$$\mathfrak{M}_{A} \sin^{3} i = h_{1} (K_{A} + K_{B})^{3} K_{B} P (1 - \epsilon^{3})^{\frac{1}{3}},$$
  

$$\mathfrak{M}_{B} \sin^{3} i = h_{1} (K_{A} + K_{B})^{3} K_{A} P (1 - \epsilon^{3})^{\frac{1}{3}}$$

In fact.

$$\frac{\mathfrak{M}_{A}}{\mathfrak{M}_{A}} = \frac{K_{A}}{K_{A}}.$$

When only one spectrum (of component A) is visible another formula has to be used:

$$\frac{\mathfrak{M}_{A}^{n} \sin^{n} t}{(\mathfrak{M}_{A} + \mathfrak{M}_{A})^{n}} = h_{1} K_{A}^{n} P (1 - e)^{\frac{1}{2}}.$$

At any rate it is necessary to assume a mean value for sin i. We have.

$$\overline{\sin^2 i} = \frac{\int_0^{\pi_0/2} \sin^4 i \, di}{\int_0^{\pi_0/2} \sin i \, di} = \frac{3}{16} \pi_0 = 0.59.$$

Because of the preference for high values of  $\iota$ , it is better to adopt a somewhat higher value for  $\sin^8 \iota$  than 0,59, for instance 0,66 Sometimes even as high a

value as 0.93 has been adopted 1,

We have seen above how the mass-ratio can be determined in case of spectroscopic binaries. If such a system also is observed as an eclipsing binary the value of i can be found when deriving the orbit and thus the masses of the pair can also be computed. In case of visual binaries the mass-ratio can be determined in the following way.

Let A and B denote the two components of a binary and C be a star that does not take part in the motion of the system AB, or in other words does not

belong to the system

Let

 $\varrho_{AC}$  = the angular distance between A and C  $\theta_{CA}$  = position angle of C with respect to A

 $v_A, v_A$  = the rectangular coordinates of A with C as origin, the v-axis being directed toward the North Pole

 $x_0, y_0$  = the rectangular coordinates of the centre of gravity O of the system AB with C as origin

 $\xi_0$ ,  $\eta_0$  = the coordinates of O with A as origin

 $\varrho_{AB}$  = the distance between A and B

 $\hat{\theta}_{BA}$  = the position angle of B with respect to A.

 $k = \frac{\mathfrak{M}_A}{\mathfrak{M}_A + \mathfrak{M}_B}$ 

The coordinates of the centre of gravity of AB are

$$x_0 = x_A + \xi_0,$$
  
$$y_0 = y_A + \eta_0,$$

which may be written in the form

$$\begin{aligned} x_0 &= +k \, \varrho_{AB} \cos \theta_{BA} - \varrho_{AO} \cos \theta_{CA}, \\ y_0 &= +k \, \varrho_{AB} \sin \theta_{BA} - \varrho_{AC} \sin \theta_{CA}. \end{aligned}$$

The motion of the centre of gravity O with respect to C is rectilinear and thus we can write

$$x_0 = a + b (t - t_0),$$
  
 $y_0 = a' + b' (t - t_0),$ 

where a, a', b, and b' are constants, t a certain epoch of observation, and  $t_0$  an initial epoch

Thus  $a + b (t - t_0) - k \varrho_{AB} \cos \theta_{BA} = -\varrho_{AC} \cos \theta_{CA},$   $a' + b' (t - t_0) - k \varrho_{AB} \sin \theta_{Bi} = -\varrho_{AC} \sin \theta_{CA}.$ 

The problem is, in fact, nearly identical with the problem of determining the trigonometric parallax of a star, only that the period is much longer than a year, and the same methods can be applied with advantage in practice. It seems that observers have not always appreciated the great advantage of connecting visual doubles with a sufficient number of stars being independent of the system. The student is adviced to consult the two observing lists for the determinations of mass-ratios as given by AITKEN [Lick Bull 7, p 3 (1912)] and by VAN BIESBROBCK [A J 29, p 173 (1916)]

211 Are Derived Mass-Values Representative? It will certainly be asked whether we have any right to extend our knowledge concerning the masses of the densities of the double stars to ordinary stars. The following facts may be

<sup>1</sup> KREIKEN, MN 89, p 589 (1929)

mentioned which show that the double stars do not form an exceptional group

among the stars of the stellar system

The distribution of double stars on the sky is the same as the distribution of ordinary stars. Our knowledge concerning the special distribution of the former is scanty, but the evidence so far shows the general agreement in the distribution in space of the two groups (Liwis1, Kreiken1).

The motions of the double stars do not differ from the motions of the single stars in any known respect. The present writer has investigated the proper motions and radial velocities of some 150 binaries without finding any pecu-

liar behaviour, C LUPLAU-JANESEN® has determined the apex of double stars and found the values  $A = 265^{\circ}$ ,  $D = +26^{\circ}, V = 17.1 \text{ km/sec}$ J. OORT has found the adjoined mean residual radial velocities of binary stars.

Spectral class	Spectroscopio binaries		Single stars (Campusta)	
B0-B9	6,6 km/sec	43	6,5 km/see	225
VO-VO	12,0	30	11,0	177
FO—F9	12,4	20	14,1	184
G0—K9	16,0	18	13,6	492

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He derives the ratio  $V_{\text{single stars}}/V_{\text{binaries}} = 1,03 \pm 0,05$  and concludes that the average mass of the brighter component of a visual binary is about equal to that of a single star of the same spectrum and absolute brightness.

The double stars exhibit typical stellar spectra (Miss Cannon, Leonard, and others). No such spectral peculiarities are found among double stars as to place them among the special groups of stars. The RUSSELL diagram of the binary stars as first constructed by F. C. LEONARD, has the same form as that of single stars. Applying a different method the present writer and W. J LUYTEN later on derived a typical Russell diagram on the basis of some 300 double stars

As far as all the evidence goes it is only the fact that two or more bodies are moving within the activity-spheres of each other's gravitation that places the double or multiple stars in a certain class. With regard to motion, space distribution, physical properties, absolute magnitudes, temperatures, densities, general chemical and physical constitution the double stars are typical citizens of the stellar realm.

Thus it seems justifiable to conclude that the masses or densities of binaries should not differ systematically from the masses or densities of the ordinary stars.

212. Historical Notes. Observational Evidences. The first star for which it was possible to obtain accurate knowledge of its dimonsions, mass, and density was our Sun. When the first trigonometric parallaxes of stars had been secured, and orbital elements of double stars had been computed, the third law of KEPLER ("the harmonic law") was applied and it was evident that the masses of neighbouring stars did not differ systematically from that of the Sun Already in Madras about 1850 Jacob found the mass of the a Centauri system. to be 10 and interpreted this result as showing that the mass of the system is of the same order of magnitude as the mass of the Sun. On account of the alow progress of the determinations of stellar parallax our knowledge of the masses of the stars also advanced slowly. A table in AGNES M CLERKE's well-known work "The System of the Stars" (1905) is, I think, representative of the knowledge possessed of the stellar masses at that time. The sums of the masses

<sup>-</sup> mom R A B 56 (1906).

M N 89, p. 647 (1929).

A N 203, p 9 (1916); Ksbenhavn R Acad Forhandl Oversigt 1916, No. 1.

A J 35, p. 141 (1924)

Lick Bull 6, p. 125 (1911).

Harv Ann 56, No. 7 (1912).

Lick Bull 10. p. 460 (4002) A J 35, p. 93 (1923). MN 10, p 170 (1850).

in twelve binary systems are given in that table. The values range between 0.670 and 12.66 O. It is of a certain interest that Capella is included with a minimum value of 2.140 derived on the strength of the observations at Greenwich in 1905, when the separation was estimated as 0".05 These observations could not be confirmed at Lick and the Greenwich results were not generally accepted. A comparison by I. HAAS of the positions derived on basis of the orbital elements from the Mount Wilson interferometer measurements with the Greenwich estimates in 1905 has made it very probable that Capella actually was seen as oblong by the Greenwich observers-a very icmarkable observation!

The astronomers of the 19th century certainly took a keen interest in the development of methods to determine physical characteristics of the stars. In 1844 Bessel noticed that the proper motions of Sirius and of Piocyon were vallable This led him to investigate in a masterly written paper the possible causes of changes in proper motions of the stars2 He found it most probable that the changes in Silius and in Procyon were caused by the gravitation of a possible dark companion to the bulliant star It is well known how after many disappointments on account of presumed, but not confirmed, discoveries this theoretical investigation finally led to ALVAN CLARK's discovery of the companion of Silius in 1862. It is also well known how the investigations of Bessli and the later work of AUWERS3 led to the discovery by J M Schaeblele of the companion of Procyon in 1896 The point that concerns us here is that these investigations have developed the methods of determining the mass-ratio in double stars in such a definite way that at present we have no leason to change of modify the classical formulae.

This method depends on accurate determinations of periodic changes of small amplitude in the proper motions. It is very difficult to obtain reliable results. When T Lewis published in 1906 his large catalogue of the  $\Sigma$  double stars, he collected the results then existing concerning the value of  $\mathfrak{M}_A/\mathfrak{M}_H$ On the basis of the material he arrived at the wrong conclusion that the fainter component in a binary system is generally the more massive one. The evidence accumulated later shows that this conclusion is not tenable. The mass-ratios known hitherto are still affected by considerable uncertainty in the case of visual binaries but their general accuracy has much increased since 1905. We also have nowadays the possibility of deriving accurate mass-ratios from spectroscopic binaries giving impressions of both spectra on photographic plates

Of the different computations of the mean masses of the binary stars we mention here only a few In 1910 R G AITKEN® used the material in the parallax catalogue of KAPTEYN and WEERSMA? and found the masses to vary between 0,002 o and 371 O, most of the variation being attributable to the uncertainty of the parallax measurements. It could be assumed that the real variation in the size of stellar masses is very small

In the following table the results of some computations of the total mass of stellar systems, generally not specially mentioned or reviewed in the text, are collected. No completeness is aimed at The sole purpose is to illustrate the general development during the last decades of our knowledge of stellar masses

<sup>1</sup> Obs 47, p 376 (1924).

<sup>&</sup>lt;sup>2</sup> AN 22, p 145 (1844), Abhandlungen von Friedrich Wilhelm Bessel, herausg von R Engelmann II, p 306 (1875)

<sup>3</sup> AN 58, p 33 (1862) 4 Mem R A S 56 (1906) Exwis did not care to derive  $\mathfrak{M}_A + \mathfrak{M}_B$  from his material, but pointed out the possi bility of doing so [Mem RAS 56, p. XXI (1906)]

7 Groningen Publ, No 24 (1910).

Authority	Mean value	Range		Rpoch	Вошта
Auwers	1,60	1,04 - 2,200	2	1892	AN 129, p 232.
Young .	1,6	0,33 - 3,1	4	1899	General Astronomy.
GOES	5	1,9 -15	5	1907	AstronomicalEssays
DOBERCE	11/0		few cares	1908	A N 178, p. 381
<b>Newcomb-Engelmann</b>	1,4	0,1 - 3,5	7	1911	Popularo Astrono- mio, IV. Aufi
	1,4	0,3 - 3,2	9	1921	Populare Astrono- mio, VI Aufl
Donerck	2,46	0,43 -372	11	1912	A N 191, p. 425
ATTKEN	2,5-3,0	0,002-371	24	1910	Pop Astr 18, p 483
CAMPBELL	1,9	1,0 - 5,0	6	1913	Stellar Motions
Foucut	2,0	0,3 - 7,8	13	1916	BSAF 30, p 90.
AITKEN	1,76	0,45 - 3,3	14	1918	The Binary Stars.
VAN MAAHEH.	4,2	0,18 - 45,7	39	1919	Publ ASP31, p.231
MITCHELL	10	0,38 - 71,3	19	1920	McCormick Publ
MILLER and PITMAN .	5,44	0,11 -134,5	68	1922	AJ 34, p 127.
LUNDMARK	1.7	0,2 -150	250	1929	Card Catalogue.

In 1916 R. T. A INNES! discussed the size of the stellar masses. For 50 stars fairly reliable orbits had been computed Bocause of the lack of data concerning the parellaxes of these stars the author assumed that the absolute magnitudes were constant and equal to the absolute magnitude of the Sun. INNES prefers the term "gravitative power" instead of mass, as the last term suggests a body of matter and it is an assumption to consider mass as equivalent to gravitative power. Among the many interesting conclusions in INNES's paper we quote the one that few of the double stars have a gravitative power equal to that of the Sun In general the mass must be considerably smaller than the solar mass. It seems probable that the spectrum varies with the mass. On account of his assumption the masses of the B stars in INNES's list came out too low and the masses of red dwarfs too high. Some of the conclusions are naturally influenced by this fact. Only a few years later the situation with regard to our knowledge of stellar parallaxes had changed in such a favourable way that the order of magnitude of the mean masses of different spectral classes could be determined with fair accuracy.

In 1919 A. VAN MAANEN<sup>a</sup> derived the masses of 55 blastics, of which the parallaxes of 39 could be accepted as fairly well determined. The dispersion in the values is very small; indeed, it only amounts to 2,1 ©. Two stars which had a mass larger than 10 © wore excluded and the lowest of the values was 0,18 © When the masses were plotted against the absolute magnitudes a quite definite relation was found, which was in good agreement with later theoretical derivations of the mass-luminosity relation. Also a relation between mass and velocity was sought for, but no definite result was found.

In 1922 B MEYERMANN<sup>8</sup> computed the masses of the components of 59 pairs. The mean values are  $\mathfrak{M}_A = 1,4 \odot$  and  $\mathfrak{M}_B = 1,2 \odot$ , and the dispersion is very small indeed. In a subsequent paper<sup>4</sup> the relation between mass and proper motion (reduced to km/sec by means of the known parallexes) was investigated and gave as a main result:

No.	ν	п
3.7 O 1,2 O	19,8 km/900 25,4	19

South African Journal of Science. 1916 June.
 Publ A S P 31, p. 231 (1919).
 A N 216, p. 301 (1922).
 A N 216, p. 385 (1922).

Mass-latios Visual Binaries.

System	a 1900	ð 1900	dM (visual)	Mn/M 1	Authority	Ma/MA (adopt )	Period (years)
Σ 3062 13 Ceti	0 <sup>h</sup> 1 <sup>m</sup> ,0 0 30,1	+57°53' - 4 9	1,0	1,0 1,32	Boss PARASKEVOPOU-	1,0	106 6,88
7 Cassiopeiae	0 43,0	+57 17	3,6	0,92	ros Pogo		
, cassepones	0 43,0	1.37 17	3,0	0,92	STRUVE	1	1
				0,5	LEWIS	)	[
				0,76	Boss Mitchell		
		ì	Ì	0,34	VAN BIESBROLCK	0,38	346
o <sup>2</sup> Eridani BC	4 10,7	- 7 49	2,0	1.08	LEWIS	.,,,,,,,	}
		}	}	1,0	MITCHILL		]
		1		0,47	VAN DEN BOS		
			-	0.64	ABETTI	0,45	248
80 Tauri	4 24,4	+15 25	3,3	0,39	VAN DEN BOS	0,39	150,2
α Aurigae Sirius	5 9,3	-+45 54	0,5	0,79	MERRILL	0.79	0,28
Dirius	6 40,7	-16 35	10,0	0,47	Auwlrs Sec		
				0,39	Boss	0,44	50,2
Castor	7 28,2	+32 6	0,86	1	FURNER		
				0,81	MITCHFLL RABE		
			ì	0,60	RABE	0,80	306
Procyon	7 34,1	+ 5 29	13,0	0,2	SEE	0,00	
				0.33	Boss		
		1		0,31	Boss Jonus	0,31	40,3
9 Argus	7 47.1	-13 38	0,6	0 37	MITCHELL	0,31	40,5
Cancri				0,4	O STRUVE	0,30	23,3
Cancri Ilydrae	8 6,5 8 41,5	+ 17 57	0,24	1,0	SECLIGER LEWIS	1,0	57,89
,,	0 41,5	1 40 47	1,3	0,9	SEEI IGER		
5 TV . 54				1,0	MITCHELL	0,95	15.3
E Urs Majoris	11 12,9	+32 6	0,5	1,5	BOWYER	į	
			1	0,72	Boss Abetri		1
		ţ	(	1,0	HER12SPRUNG	0,9	59,8
y Virginis .	12 36,6	- 0 54	0,0	1,0	LEWIS		
25 Can Venati				1,0	Boss	1,0	178
corum	13 33,0	+36 48	1,9	2,0	FURNER	2,0	220
or Centauri ,	14 32,8	-60 25	1,37	1,0	ELKIN	1	1
				1,05	GILL		1
	)		}	0,96	ROBERTS Boss	0,97	80,09
§ Bootis .	14 46,8	1-19 31	2,0	1,2	BOWYER	0,07	00,03
ξ Scorpπ	14 50 0			0,87	Boss	0,87	151,4
§ Scorpn σ Cor Borealis	15 58,9 16 10,9	-11 6 +34 7	0,3	1,3	S HORR LEWIS	1,0	14,7
1000000	10 10,9	( 1757 /	( 0,9	1,1	HADLEY		
	ļ			0,47	Boss		
A Ophiuchi	16 25,9	1 2 10	2.	2,6	ABETTI	1,5	500
ζ Hetculis	16 25,9	+ 2 12 +31 47	2,1	4,3	Lewis Lewis	4,3	110
	}	13. 17	3,3	0,43	Boss	1	1
70 Onhurst	10 0			0,88	CHANG	0,7	34,40
70 Ophiuchi	18 0,4	+ 2 31	1,70		PREY		
	1		1	0,79	Comstock Lau	1	}
	l			0,82	Boss		1

Bystom	a 1900	ð 1900	AM (visual)	DHR.	Anthority	(myody) Marinia	(years)
70 Ophluchl	18 <sup>b</sup> 0 <sup>m</sup> ,4	+ 2°31'		0,79		- 0	
β Deiphini .	20 32,9	+14 15	1,0		VAN BIESBROECE CHANG HADLEY	0,8	87,7 26,8
т Судоц.,	21 10,8	+37 37	4,2	0,89	HADLEY VAN BIESDROECK	•	
и Pegani	21 40,1	+25 11	0,5		ABETTI HEMROTEAU	0,9 0,40	49,2 11,6
Krueger 60	22 24,5	+57 12	1,5	1,14 0,83 0,45 0,91 0,83	RUGAELL ALDEN		
85 Pegani	23 56,9	+26 33	5,15	4 3 1,0	BERNEWITZ FURNER LEWIS BOSS COMETOCK	0,8	44,27
				1,7		1,7	25,42

Computing the total space motions on the basis of data for 15 objects

Vien	V	
4,0 ① 1,4 ①	23,5 km/soo 33,7 ,,	8 7

The masses that are derived on the basis of double star data are dependent on the amount of the gravitation between the components. Thus the total mass of the binary system is obtained, i.e. not only the mass of the two suns, but also of planets and other dark bodies that may be present. There are 10 typical Sun stars for which the mass has been determined with a fair degree of accuracy. The mean value of the masses is  $1,05 \odot \pm 0.11 \odot$  and the mean value of the absolute magnitudes M = 4,76. It seems that these systems cannot be of a structure radically different from that of our solar system.

A remarkable event was the discovery of J S PLASKETT in 1922 that the O star BD + 6° 1309 was a very massive system. The two components had the mass values.

 $\mathfrak{M}_A = \frac{75.6}{\sin^3 i} \odot, \quad \mathfrak{M}_B = \frac{63.3}{\sin^3 i} \odot.$ 

The system has later been carefully watched for changes in the magnitudes, but so far without positive results. Plaskett's star does not seem to be an eclipsing binary system and therefore it is justifiable to conclude that the sum of the masses is at least 160 O.

In Eddington's first theory of stellar evolution 40 © was determined as the upper limit for the mass of a star H von Zeipel has pointed out several times in his lectures that this was not a necessary consequence; if there is an upper limit it has a very high value. In the final theory of Eddington there seems to be no low limit for the possible size of stellar masses; on the other hand it seems that a limit exists, and it must be a quite exceptional case if a stellar mass is much above 100 ©.

The tables on p. 614 to 616 summarize the results hitherto found for the massratios in visual binaries and colleging variables. There exist also some 100 well

<sup>1</sup> MN 82, p. 447 (1922).

determined mass-ratios of spectroscopic binaries where both spectra have been observed. These have been excluded because of the lack of data for the magnitude of the components. The student interested in these stars should consult the catalogues by J. H. Moore [Lick Bull 11, p. 141 (1924)] and A. Beer [Beelin-Babelsberg Veroff 5, H. 6 (1927)]

Eclipsing Binaries,

			poing	Radius	Density	. 1		
Object	a 1900	AM	$\mathfrak{M}_B/\mathfrak{M}_A$	of bright		Purdiax	M	5ր
HD1337 .	0 <sup>h</sup> 12 <sup>m</sup> ,5	1,2	0,93	23,8 🔾	0,00270	0",002	6,0 4,8	O8,5n O8,5n
TV Cassiopeiae .	0 13 ,9	1,82	0,59	2,54	0,112	0 ,0047	+0,8	A0n A0
7 Tauri	3 55 ,1	1,49	0,33	5,35	0,024	0 ,0095	-1,1 -1-0,4	133
# Aurigae .	5 52 ,2	00,0	0,98	2,83	0,11	0 ,030	+0,6	Aon Aon
WW Aurigae .	6 25 ,9		0,86	1,9	0,32	0 ,010	+2,2	A.7
Castor C	7 28 ,2	0,21	0,90	0,76	1,4	0 ,074	+9,6 +9,8	Mie
V Puppis	7 55 ,4	0,45	0,77	7.5	0,050	0 ,004	-2,0	Bin
S Anthae	9 27 ,9	0,74	0,56	1,34	0,31	0 ,007	1,5 -+-2,9	133n   A8n
			}	1	}		+3.6	A8n
W Ursae Majoris	9 36 ,7	0,04	0,72	0,72	1,92	0 ,013	+5,4 +5,4	F8n F8n
RS Can Venati-								
corum	13 6 ,0	0,92	1,00	7,1	0,004	0 ,0022	-0,0 +0,9	F3n Ko
i Bootis .	15 0 ,5	0,0	1,00	0,6	2,2	0 ,152(?)	-1 6,3	G2
U Cor Borealis		4.06	0.10	0.04	0.10	0.0025	+6,3	B3n
	15 14 ,1	2,96	0,38	2,94	0,19	0 ,0037	+0,4	B3n
U Ophiuchi	17 11 ,5	0,18	0,88	3,23	0,18	0 ,0059	+0.2	B3n
u Herculis	17 13 ,6	0,88	0,40	4,64	0,094	0 ,0071	+0,4 -0,8	B5n B3n
TX Herculis	17 15 ,4	0,68	0,87	1,57	0,53	0 ,0053	+0,1 +2,3	B3n A28
							+3,0	A28
Z Herculis	17 53 ,6	0,35	0,87	1,77	0,28	0 ,013	+3,3	F2s F2
RXHerculis .	18 26 ,0	0,12	0,95	1,95	0,280	0 ,0064	+3,6	B9n
β Lyrae	18 46 ,4	_	0,41	13,6	0,0012	0 ,005	+1,9	Bon Beep
RSVulpeculae	19 13 ,4	2,35	0,31	4,22	0,06	0 ,0045	-2,6	cB8 B8n
Z Vulpeculae .							+2,0	B9
Z Vulpeculae .	19 17 ,5	1,45	0,45	4,54	0,052	0 ,0018	-0,7 +0,7	B3n B3
σ Aquilae .	19 34 ,3	0,36	0,82	3,48	0,15	0 ,0060	-0,2	B8n
Y Cygnı ,	20 48 ,1	0,38	0,92	4,60	0,17	0 ,0022	1-0,2	B8n   B2n
- 0,6	20 40 ,1	0,30	0,92	4,00	0,17	0 ,0022	-0,8	B2n

I think that the first table will show how imperfect our knowledge of the mass-ratios of visual binaries still is. The length of the periods makes it difficult in most cases to cover even one period by observations. The values in the second table are by far more accurate than those in the first table.

The mass-ratios when plotted against differences in magnitudes show certain deviations from the curve computed in accordance with the mass-luminosity relation. There seems to be some systematic difference between the mass-ratios

of visual and eclipsing binaries. The considerable dispersion in the mass-ratios does not seem to be dependent on the errors in the individual determinations alone

213. Equipartition of Stellar Energy. J. Halm' was one of the first to apply the law of equipartition of the energy to the derivation of the average mass of the stars. According to the Maxwellian law the number of molecules of mass  $\mathfrak{M}$  with velocities between u, v, w and u + du, v + dv, w + dw is.

where A and k are constants.

The kinetic energy of a single molecule of mass IR is:

Hence the total energy of all the molecules.

$$E = \frac{1}{2} A \Re \int \int_{-\infty}^{+\infty} \int e^{-M^2 \Re (u^2 + v^2 + w^2)} (u^2 + v^2 + w^2) du dv dw,$$

or:

$$E = \frac{1}{8} \frac{A}{k^3} \sqrt{\frac{\kappa_s}{k^3 300}} \times$$

$$\left[\int\limits_{-\infty}^{+\infty} e^{-\frac{1}{h^2} \frac{\partial R}{\partial x^2} (x^2+x^2)} \, dv \, dw + \int\limits_{-\infty}^{+\infty} e^{-\frac{1}{h^2} \frac{\partial R}{\partial x^2} (x^2+x^2)} \, du \, dv + \int\limits_{-\infty}^{+\infty} e^{-\frac{1}{h^2} \frac{\partial R}{\partial x^2} (x^2+x^2)} \, du \, dv \right],$$

or, the three integrals in the brackets being identical,

$$E = \frac{3}{8} \frac{A}{h^2} \sqrt{\frac{\kappa_0}{h^2 W}} \int_{-\infty}^{+\infty} e^{-h^2 W (r^2 + r^2)} dr dw.$$

The total number of molecules is:

$$N = A \int \int \int \int e^{-M \cdot \mathbf{R} \left( \mathbf{s}^2 + \mathbf{s}^2 + \mathbf{s}^2 + \mathbf{s}^2 \right)} du \, dv \, dw = \frac{1}{2} A \sqrt{\frac{\pi_e}{k^2 \cdot \mathbf{R}}} \int \int \int e^{-M \cdot \mathbf{R} \left( \mathbf{s}^2 + \mathbf{s}^2 \right)} \, dv \, dw.$$

Hence.

$$\overline{E} = \frac{E}{N} = \frac{3}{4M}$$

i. e. the average kinetic energy is independent of the mass. If  $\Omega$  denotes the average speed we thus find:

IR Q = const...

i. e. the average speed is inversely proportional to the square root of the mass. Halm says that it is certainly not illogical to associate the rate of development from earlier to later types with the mass of a star. If stars of different masses started their development at the same time, it would be expected a priori that the lighter stars would cool down more quickly, and hence arrive at the more advanced spectral stages sooner than the heavy stars. The average mass of the "earlier" spectral classes will be larger than that of the more "advanced" spectral classes. In this way the lesser average speed of the earlier stars could be explained,

<sup>1</sup> MN 71, p. 610 (1911).

Spectral class	Mcan radial velocity	11	Spectral class	Mean radial velocity	31
B-B9	6,0 km/sec	64	G-G5	12,6 km/sec	26
A-A5	11,2 ,,	18	K-K5	15,4	55
F-F8	14,5 ,,	17	Ma	19,3	6

HALM points out that the ratio  $\mathfrak{M}_n/\mathfrak{M}_n$  is probably independent of spectral class and quotes the following results

$\mathfrak{M}_B/\mathfrak{M}_A$	i	
10,77	"Orion	type"
	Other	classes
	$\begin{cases} 0.77 \\ 0.83 \end{cases}$	M <sub>B</sub> /M <sub>A</sub> {0,77 "Orion 0,83 Other 0.81

Thus it is admissible to assume that the ratios of the average values of the mass-function Ma sina 2

for different types are practically identical with the ratio of their combined masses From spectroscopic binaries showing both the spectra HALM derived.

(M + M p)2

Orion type 
$$(\mathfrak{M}_A + \mathfrak{M}_B) \sin^3 i = 16.4 \pm 3.4 \bigcirc$$
  
Classes A-G  $1.9 \pm 0.3 \bigcirc$ 

Ratio of average mass Orion stars/other classes = 8,6

Using the binaries where only one component was seen, i.e where only the mass-function is determined, it was found.

Period	Mass ratio Orion stars/other classes	#
< 5 <sup>d</sup>	8,60	29
54-30	4,6	24
>30	6,2	20
All	6,50	'

The square roots of the two values of the mean ratio of Orion stars/other classes are 2,9 and 2,5 Thus it is justifiable to assume that the Onon stars are on the average more massive than the stars of more advanced type.

From the above table of KAPILYN

the ratio of average speed of Orion stars/average speed of other classes is 0,42, whereas the inverse square root of the mass-ratio of the two groups is 0,34 or 0,40 Thus the agreement is good, a fact that seems to support the equipartition of energy

HALM has used the average parallaxes according to KAPPEYN's formula and found (see close by) H N RUSSELL1 had

Apparent Group ū M magnitude Orion stars 0",0066 -0.105,0 A stais . 5,0 8,0098 0,0 F-K stars 5,0 0 ,0224 +1 ,8

found (see close by)

Combining his results with the preceding conclusion concerning the heavier mass of the earlier stars, HALM makes the remarkable statement that, "we may also say that intrinsic brightness and mass are in direct relationship"

Spectral class	Apparent magnitude		М
F8 G-G2 G5 K K5 M	7,0 7,8 8,6 7,4 8,2 8,3	0",044 0 ,029 0 ,064 0 ,119 0 ,254 0 ,221	5 <sup>11</sup> ,2 5 ,1 7 ,6 7 ,8 10 ,2

This is the first time, as far as the present writer knows, that a massluminosity relation has been thought to exist among the stars

<sup>&</sup>lt;sup>1</sup> A J 26, p 147 (1910)

HALM's investigation does not tell us anything concerning the size of the dispersion in stellar mass. It is not possible to determine this element without making complicated investigations. The method is of much value in any case, because of its possibilities for determining the average mass of the stars that do not belong to such selected groups as double stars or stellar clusters.

The relation between the mean speed and M is perhaps not applicable to all classes of stars. The O stars and the planetary nebulae are undoubtedly heavy bodies, but do not move as slowly as the B stars. When reviewing Seares's results we will see who the law of equipartition in general fits modern

data concerning the space motion of the stars

214. Schlesmeer's and Baker's Study on Spectroscopic Binaries. An early contribution to this subject was made by Schlesinger and Baker', who analysed data derived from spectroscopic binaries. Considering first the systems in which spectra of both components have been observed they found without exception that the brighter component of a spectroscopic binary is always the more mussive of the two. The close correspondence between mass and relative brightness (one could also say absolute brightness) is shown from the following summary where I stands for the (absolute) intensity

ma/ma	$I_{M}I_{A}$		<b>明</b> 斯默』	Inlla	п
0,99	1,00 0,73	2	0,74 0,66	0,53	3

The authors assumed that the discovery-chance of spectroscopic binaries is  $\infty$  sin; Thus  $\sin^2 s$  will be equal to 0,68, a value which is considered somewhat too low newadays. They concluded that in fifteen pairs showing both spectra the average mass was between 40 and 50. They also concluded that this statement could not be extended to other spectroscopic binaries. The difficulties arising from the use of the mass-function were pointed out. From 44 pairs showing only one of the spectra it was concluded that the masses of spectroscopic binaries are of very different orders, some being much greater than that of our sun, while others are doubtless insignificant in comparison.

The peculiar law of distribution of the values  $(M_A + M_B)^{-1}$  for Copheid variables was also commented upon Reasons were also given for the considerable uncertainty affecting several of the data for  $M_B/M_A$  collected or derived by Lewis, which were not in agreement with the conclusions of the authors

215. Ludermore's Researches on the Masses of Spectroscopic Binaries. As a rule only the "mass-function", /, is determinable for a spectroscopic binary, vis

 $f = \frac{\Re \{\sin^2 i - 0.03993 - (a \sin i)^2 - P^4\}}{(\Re A + \Re A)^3} = +0.03993 - (a \sin i)^3$ 

LUDENDORFF puts  $\mathfrak{M}_B/\mathfrak{M}_A = \alpha$ .

There is a wide disparity in the values of f. The numbers do not give much guidance for forming conclusions concerning the size of stellar mass. The situation turns out more favourably when the dependence between  $a \sin i$  and P is used. If the spectroscopic binaries are divided into groups according to the size of the pariod, and means are formed, a regular increase with  $\overline{P}$  is found in  $\overline{a \sin i}$ , in such a way that f or 0,03993  $\overline{(a \sin i)}$  is rather constant.

ì

<sup>&</sup>lt;sup>1</sup> Publ Alleghony Obs 1, No. 21 (1910)

AN 189, p. 145 (1911).

The stars were divided into two groups containing the stars of the spectral classes Oe5-B8 and A-K The mean numbers are given below, being still of interest.

When  $\overline{P}$  is plotted against  $a\sin i$  the points of the two groups define a smooth curve. The smoothed values are given under the heading Asin J The constant C is defined from the equation.

$\overline{P}$	a sin 1	11	$A \sin J$	a sin i — 1 sin J
0 <sup>d</sup> ,22	0,040	2	0,74	-0,70
2,58	3,30	5	3,84	-0.54
4,16	5.37	4	5,28	+0,09
6,23	5,17	4	6,92	-1,75
9.75	6,82	3	9,32	-2,50
28 ,15	26,47	3 2 2	18,90	+7.57
121,62	54,10	2	50,13	+3,97
137 ,64	51,46	3	54,44	-2,98
	Λ	-K s	tars	

14,35 1,04 -0.671,42 2,60 2,65 -1,234 4 4 3 2 +0,113.87 3.76 4,39 -0.9811,38 6,11 7,09 18,89 8,51 9,94 -1,4339 ,34 16,43 +0,2224,22 +0,9071,80 25,12

30,72

102,56

31,51

$$A\sin J = \left(\frac{C\bar{P}^2}{0.03993}\right)^{\frac{1}{3}},$$

and has the following values.

 $C = 0.34 \odot$  for the B stars

C = 0.110 for the A-K stars.

For 8 stars of such a period that they could not be included in the graphs the agreement with the A-K curve was still good

Next Ludendorff inquies concerning the significance of the relations.

B stars 
$$\frac{\alpha^3}{(1+\alpha)^2} \mathfrak{M}_A \sin^3 i = 0.340$$
,  
A-K stars.  $\frac{\alpha^3}{(1+\alpha)^2} \mathfrak{M}_A \sin^3 i = 0.110$ 

+0.79

The difference in C can be explained in different ways. The inclination for B stars might be systematically higher than for other stars on account of a preference of the former to move in orbits parallel with the galactic plane This explanation does not seem very likely, because no dependence can be found between asini and the galactic latitude, but the material available was meagre

Another explanation is that the mass-ratio should be systematically larger for the helium stars than for other systems. As soon as α deviates from unity small changes in a give rise to considerable changes in / A means of testing the possibility of the hypothesis is found in the cases where both spectra have been observed LUDENDORFF finds

(M 1+MB) sin3 ;	ã	1)	Group
8,5 ⊙	0,70	9	B stars
2,6 ⊙	0,80		A-K stars

The scanty material rather suggests that the differences in mass-ratio work in the opposite direction, as regards the values of C, to that found above. Luden-DORFF therefore thinks that the difference in C is best explained by an actual difference in mass, as is also indicated from the numbers given above for (Ma + Mn) sing 2

LUDENDORFF pointed out that the results concerning the higher mass of the B stars in comparison with the other stars are preliminary, and that the difference may be explained partly by other causes. On account of the higher accuracy attainable when measuring spectra of later types, smaller changes will be more easily discovered than in the case of B stars Thus small amplitude B stars will not, as a rule, be discovered, which makes the mean value of the masses for the later types apparently too low A closer study of the material available showed that no such dangerous effect had crept in among the numbers used.

The stars with the c and ac character in their spectra were not used, because of their peculiar position as regards the value of / This constant which is on an average 0,0034, suggests that  $\alpha$  is of the order 0,1 for these stars.

In general no conclusions can be made from the value of f concerning the size of the sum of the masses. If we have an infinite number of stars,  $\sin^2 s$  is 0,59 Because of the preference of high values of t, the value will be higher. Ludrandorff assumes the value to be 0,75. Thus the mean masses are

$$\mathfrak{M}_A = 0.45 \frac{(1+\alpha)^2}{\alpha^2} \odot \quad (B \text{ stars}), \qquad \mathfrak{M}_A = 0.15 \frac{(1+\alpha)^2}{\alpha^2} \odot \quad (\Lambda - K \text{ stars}).$$

For different values of  $\alpha$  the following table gives the values of  $\mathbf{R}_{\lambda}$  and  $\mathbf{R}_{n}$ .

			B stars			A-E stars	
railo a	(1+a)2 a2	R.	R,	数4十数3	D4	Si a	数4+数3
0,1	1210	544 O	54 O	598 O	181 ①	18 @	199 0
0,2	180	81	16	97	27	5	32
0.3	63	28	8	36	9	3	12
0,4	31	14	6	20	4,6	1,8	6,4
0,5	18	8	4	12	2,7	1,4	4,1
0,6	11,8	5.3	3,2	8,5	1,8	1,1	2,9
0,7	8,4	3,8	2,7	6,5	1,3	0,9	2,2
0,8	6,3	2,8	2,2	5,0	0,9	0,7	1,6
0,9	5,0	2,3	2,1	4,4	0,8	0,7	1.5
1,0	4,0	1,8	1,8	3,6	0,6	0,6	1,2

LUDENDORFF<sup>1</sup> returned to the subject in a later paper. A considerably increased material was at his disposal owing to the energy of the American astronomers who went in for the determination of orbits of spectroscopic binaries.

The following groups were excluded as before: the c and ac stars, some stars whose orbits were dependent on the displacements of the H and K lines, some stars where the orbital motion is not very well established (e. g.  $\alpha$  Orionis), v Sagittarii, stars with variable amplitude such as 12 Lacertae and  $\beta$  Cephel, Boss 1275, where the period used is probably much too large, and, lastly, five stars with periods  $>1000^4$ . The following mean values were found, the f being computed from f=0.03993  $\frac{a\sin t^2}{B^4}$ :

P	e shi è		7		Þ	o who	M	ſ
	Os	_Qo5					Á	
154,66	21,60	3	1,6		1 4,49	1,57	4	0,07)
	-				2 .57	1,60	5	0,02
	190	—B5			3 ,62	2,43	4	0,04
1 ,18	1,55	4 1	0,11		4,02	4,09	4	0,17
2,54	3,12	5 5	0,19		6 ,82	4,72		0,09 0,10
3 ,81	4,94	5	0,33		10 ,21	5,92	5	0,08
5 ,12	6,02	4	0,33	0,25	17 .37	9,67	5 5	0,12
7 ,60	6,92	5	0,23		47 47	23,50	4	0,23
20 ,24	11,18	4	0,14		114 ,79	31,71	1	0,10
123 ,54	53,36	5	0,40		[ ''' "' '	3-,, -	F	0,10,
	138	and Bo			1 ,38	0,51	1 .	0.002)
4 99	2,68						1 2	0,003
1 ,82		1 1	0,23	0.15	4 ,52	2,97	5	0,05
4 ,41	3.75	4	0,11	0,15	10 ,87	6,88	5	0,11
47 ,54	17,13	3	0,09		49 ,89	16,94	3	0,08
1 4 1	211, p	105 (192	10)					

If  $\alpha$  and vare on an average the same for the different spectral classes, then  $\mathfrak{M}_B/\mathfrak{M}_{B8}=1.7$ ,  $\mathfrak{M}_B/\mathfrak{M}_A=2.5$ ,  $\mathfrak{M}_B/\mathfrak{M}_1=4$ , where  $\mathfrak{M}_B$ ,  $\mathfrak{M}_{B8}$ ,  $\mathfrak{M}_A$ ,  $\mathfrak{M}_1$  are the mean masses of stars of the spectral classes B0-B5, B8-B9, A, and b respectively. The stars of the Oe class seem to have a very large mass

There are only few binaries with known orbits in the G and K class, and there is a lack of short periods among the former stars. Four K stars give /= 0.02, which suggests even a lower mass for these stars than for the F stars.

LUDENDORFF then made investigations as to whether the stars of the same class give a constant value for  $\overline{f}$ . He remarks that this quantity seems to increase with increasing period. At first it might, therefore seem natural to think that systems of long period also have large masses, but a closer inquiry will show that this is not the case.

216 Frequency of Stellar Masses for Different Spectral Classes. The important problem concerning the frequency of stars of different mass has been investigated by E von der Pahlen<sup>1</sup> For that purpose he makes use of the number of stars of different spectral classes and the relation between stellar mass and spectrum. Besides this the relation between spectral class and mean velocity is also used as an indicator of the mean mass for different classes, or in other words the equipartition of energy is supposed to hold also within the stellar system.

It is not enough to use these two series of data. It is also necessary to possess knowledge of the cosmogonic time scale or the time for each stage of development from the stage when a star starts more or less as a giant until it becomes more and more dwarfish. Before the theory of Eddington was worked out there was no possibility whatever of overcoming the difficulty. By the aid of a hypothetical assumption explained later on, yide particles computed the frequency. Other assumptions involved in his investigation are that the visible stellar system is in a stationary stage, in such a way that the number of visible stars in each spectral subdivision is constant with respect to the time. Putting the assumption in another form it means that for each interval of time just as many stars of each mass enter as giants as there are stars of the same mass developing into dwarfs through cooling, and thus becoming invisible.

The following notation is used

 $N_B$ ,  $N_A$ , ,  $N_M$ , Number of stars within each spectial class  $V_B$ ,  $V_A$ , ,  $V_M$ , Mean radial velocities for each spectial class  $\mathfrak{M}_B$ ,  $\mathfrak{M}_A$ , ,  $\mathfrak{M}_M$ , Masses of the stars which at the top of their evolution reach the spectral classes given as subscripts  $n_B$ ,  $n_A$ , ,  $n_M$ , Frequency of stars of masses  $\mathfrak{M}_B$ ,  $\mathfrak{M}_A$ , etc  $v_B$ ,  $v_A$ , ,  $v_M$ , Mean radial velocities of stars of masses  $\mathfrak{M}_B$ ,  $\mathfrak{M}_A$ , etc.  $T^{(B)}$ ,  $T^{(A)}$ , ,  $T^{(M)}$ , The lengths of time or periods during which stars of masses  $\mathfrak{M}_B$ ,  $\mathfrak{M}_A$ , etc are visible,  $t^{(B)}_B$ ,  $t^{(B)}_A$ , ,  $t^{(B)}_M$ , The periods for a star of mass  $\mathfrak{M}_B$  to pass the spectral classes B, A, , M

 $t_A^{(A)}, t_F^{(A)}, , t_M^{(A)},$  The same quantities for a star of mass  $\mathfrak{M}_A$ .  $t_F^{(F)}, , t_M^{(F)},$  The same quantities for a star of mass  $\mathfrak{M}_F$ .  $t_M^{(M)},$  The same quantity for a star of mass  $\mathfrak{M}_M$ .

<sup>1</sup> AN 216, p 309 (1922)

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Instead of the absolute periods t and T of time the following ratios are used

$$\begin{aligned} \tau_{A}^{(p)} &= \frac{f_{A}^{(p)}}{T^{(p)}}; \quad \tau_{A}^{(p)} &= \frac{f_{A}^{(p)}}{T^{(p)}}, \quad \tau_{B}^{(p)} &= \frac{f_{A}^{(p)}}{T^{(p)}}, \quad \tau_{A}^{(p)} &= \frac{f_{A}^{(p)}}{T^{(p)}}, \quad \tau_{A}^{(p)} &= \frac{f_{A}^{(p)}}{T^{(p)}}; \\ \tau_{A}^{(A)} &= \frac{f_{A}^{(p)}}{T^{(A)}}, \quad \tau_{B}^{(p)} &= \frac{f_{B}^{(p)}}{T^{(p)}}, \quad \tau_{B}^{(p)} &= \frac{f_{A}^{(p)}}{T^{(p)}}; \quad \tau_{A}^{(p)} &= \frac{f_{A}^{(p)}}{T^{(p)}}; \quad \tau_{B}^{(p)} &= \frac{f_{A}^{(p)}}{T^{(p)}}; \quad \tau_{A}^{(p)} &= \frac{f_{A}^{(p)}}{T^{(p)}}; \quad \tau_{A}^{(p)} &= \frac{f_{A}^{(p)}}{T^{(p)}}; \\ \tau_{A}^{(p)} &= \frac{f_{A}^{(p)}}{T^{(p)}}; \quad \tau_{B}^{(p)} &= \frac{f_{A}^{(p)}}{T^{(p)}}; \quad \tau_{A}^{(p)} &= \frac{f_{A}^{(p)}}{T^{(p)}}; \\ \tau_{A}^{(p)} &= \frac{f_{A}^{(p)}}{T^{(p)}}; \quad \tau_{A}^{(p)} &= \frac{f_{A}^{(p)}}{T^{(p)}}; \quad \tau_{A}^{(p)} &= \frac{f_{A}^{(p)}}{T^{(p)}}; \\ \tau_{A}^{(p)} &= \frac{f_{A}^{(p$$

Of these 21 quantities the last one is known and has a value = 1 because a star, having the mass  $\Re_M$ , belongs during all the time it is visible to spectral class M.

Then we have the equations:

$$N_B = n_B \tau_A^{(b)}$$
 $N_A = n_B \tau_A^{(b)} + n_A \tau_A^{(d)}$ 
 $N_A = n_B \tau_A^{(b)} + n_A \tau_A^{(d)} + n_B \tau_A^{($ 

and:

clph 216.

$$V_{B} = v_{B}$$

$$V_{A} = \frac{v_{B} n_{B} \tau_{A}^{(A)} + v_{A} n_{A} \tau_{A}^{(A)}}{n_{B} \tau_{A}^{(A)} + n_{A} \tau_{A}^{(A)}}$$

$$V_{M} = \frac{v_{B} s_{B} \tau_{B}^{(0)} + v_{A} s_{A} \tau_{B}^{(0)} + v_{P} s_{P} \tau_{B}^{(0)} + v_{G} s_{G} \tau_{B}^{(0)} + v_{E} s_{E} \tau_{B}^{(0)} + v_{M} s_{M} \tau_{B}^{(0)}}{s_{B} \tau_{B}^{(0)} + s_{A} \tau_{B}^{(0)} + s_{B} \tau_{B}^{(0)} + s_{B} \tau_{B}^{(0)} + s_{B} \tau_{B}^{(0)} + s_{B} \tau_{B}^{(0)}}.$$

The unknown v's can be eliminated by using the equipartition of energy in the following form:

The second equation then becomes:

$$n_B \tau_A^{(B)} (V_A - V_B) + n_A \tau_A^{(A)} \left\{ V_A - \left( \frac{\Omega V_B}{\Omega V_A} \right)^{\frac{1}{2}} V_B \right\} = 0.$$

Further notation introduced is as follows:

$$n_B \tau_B^{(p)} = p_B;$$
  $n_A \tau_A^{(q)} = p_A;$   $n_B \tau_B^{(p)} = p_B;$   $n_C \tau_B^{(p)} = p_C;$   $n_C \tau_B^{(p)} = p_E,$   $n_H \tau_B^{(q)} = p_H;$   $V_A = V_B = C_A^B,$   $V_A = \left(\frac{\Re s}{\Re s}\right)^{(q)} V_B = C_A^A;$  ... and in general:

$$C_A^R = V_B - \left(\frac{\Omega R_B}{2R_B}\right)^{\frac{1}{2}} V_B.$$

(pg is the number of stars of spectral class S).

The equations then take the form

$$N_{B} = p_{B}$$

$$N_{A} = p_{B} \frac{\tau_{I}^{(B)}}{\tau_{B}^{(B)}} + p_{A}$$

$$N_{F} = p_{B} \frac{\tau_{F}^{(B)}}{\tau_{B}^{(B)}} + p_{A} \frac{\tau_{F}^{(A)}}{\tau_{A}^{(A)}} + p_{F}$$

$$. . .$$

$$C_{A}^{B} p_{B} \frac{\tau_{A}^{(B)}}{\tau_{B}^{(D)}} + C_{A}^{A} p_{A} = 0$$

$$C_{F}^{B} p_{B} \frac{\tau_{F}^{(B)}}{\tau_{F}^{(B)}} + C_{F}^{A} p_{A} \frac{\tau_{F}^{(A)}}{\tau_{A}^{(A)}} + C_{I}^{I} p_{F} = 0$$

The system of equations is indeterminate on account of the appearance of the quantities  $\tau_S^{(p)}$ , of which we do not know much, if anything at all. If we represent the development of a star passing through the spectral classes by means of a curve that is some function of the time, then the mass is the parameter that will determine the form of this curve. It seems plausible that a continuous change in mass corresponds to a continuous change in this curve, and that when the masses do not vary within too wide limits, the different curves show some general resemblance. This will be the same as if the ratios of the periods expressing the times it takes for a star to pass through the spectral classes, will oscillate around some values valid for a star of mean mass. Approximately the ratios of periods for corresponding spectral stages (counting from the highest stage attainable for a star of given mass) will be equal for all stars

In this way we reach the necessary number of conditions to enable us to solve the above system v. d. Pahlen is aware that the assumption is lather bold. According to the theory of Eddingson the difference between two stars of which one can reach the B stage and the other the A stage is some 3  $\odot$ . On the other hand the same difference for two stars of classes K and M is only some  $\frac{1}{100}$  O. If the idea of v. d. Pahlen were to be worked out strictly it would be necessary to make a new spectral division fulfilling the condition that the masses increase in arithmetical proportion from class to class

According to the assumption made above we have:

$$\begin{split} \frac{\tau_{A}^{(B)}}{\tau_{B}^{(B)}} &= \frac{\tau_{G}^{(A)}}{\tau_{A}^{(A)}} = \frac{\tau_{G}^{(F)}}{\tau_{F}^{(B)}} = \frac{\tau_{K}^{(G)}}{\tau_{G}^{(B)}} = \frac{\tau_{K}^{(B)}}{\tau_{K}^{(B)}} = \sigma_{A} \\ &\frac{\tau_{F}^{(B)}}{\tau_{B}^{(B)}} = \frac{\tau_{G}^{(A)}}{\tau_{A}^{(A)}} = \frac{\tau_{K}^{(F)}}{\tau_{G}^{(B)}} = \frac{\tau_{K}^{(B)}}{\tau_{G}^{(B)}} = \frac{\tau_{K}^{(B)}}{\tau_{G}^{(B)}} = \sigma_{F} \\ &\frac{\tau_{G}^{(B)}}{\tau_{B}^{(B)}} = \frac{\tau_{K}^{(A)}}{\tau_{A}^{(A)}} = \frac{\tau_{K}^{(B)}}{\tau_{A}^{(B)}} = \sigma_{G} \\ &\frac{\tau_{K}^{(B)}}{\tau_{B}^{(B)}} = \frac{\tau_{K}^{(A)}}{\tau_{A}^{(B)}} = \sigma_{K} \\ &\frac{\tau_{K}^{(B)}}{\tau_{B}^{(B)}} = \sigma_{M}. \end{split}$$

Hence'

$$\begin{split} N_B &= \rho_B \\ N_A &= \rho_B \sigma_A + \rho_A \\ N_F &= \rho_B \sigma_F + \rho_A \sigma_A + \rho_F \\ N_G &= \rho_B \sigma_G + \rho_A \sigma_F + \rho_F \sigma_A + \rho_G \\ N_K &= \rho_B \sigma_K + \rho_A \sigma_G + \rho_F \sigma_F + \rho_G \sigma_A + \rho_K \\ N_H &= \rho_B \sigma_K + \rho_A \sigma_K + \rho_F \sigma_G + \rho_G \sigma_F + \rho_K \sigma_A + \rho_M \end{split}$$

and:

$$\begin{split} C_A^B \rho_B \sigma_A + C_A^4 \rho_A &= 0 \\ C_F^B \rho_B \sigma_F + C_F^4 \rho_A \sigma_A + C_F^B \rho_F &= 0 \\ C_G^B \rho_B \sigma_G + C_G^4 \rho_A \sigma_F + C_F^6 \rho_F \sigma_A + C_G^6 \rho_G &= 0 \\ C_B^B \rho_B \sigma_E + C_A^4 \rho_A \sigma_G + C_F^6 \rho_F \sigma_F + C_F^6 \rho_G \sigma_A + C_F^6 \rho_K &= 0 \\ C_B^6 \rho_B \sigma_M + C_A^4 \rho_A \sigma_K + C_M^6 \rho_F \sigma_G + C_M^6 \rho_G \sigma_F + C_M^6 \rho_K \sigma_A + C_M^6 \rho_M &= 0 \end{split}$$

From these all p's and o's can be determined.

The following data were used:

Spectral ciase	М	y	Tomperature	n
В	3196	6,8 km/sec	17000°	4,27 @
A	8852	11.5 ,,	10000	1,23
F	7950	14,5 ,,	6750	0,59
G.	7400	15,4 ,,	4750	0,32
K	9090	16,4	3700	0.20
M	684	17,2 ,,	3100	0,15

The numbers in the second vertical row give the numbers of stars brighter than 8<sup>m</sup>,0 per 10000 square degrees according to Tab. 11 in Groningen Publ No. 30.

In the computations it was necessary to include the M stars in the K group.

The results are:

	TO DESCRIPT	
ng - 1582	4.3	$t_{2}^{(B)} = 0.337$
$n_0 = 2802$	7.5	FA - 0,177
mp - 6033	16,3	rp = 0,080
m_ = 17266	46,5	$\tau_q^{(B)} = 0.217$
$n_{B} = 9486$	25,5	$r_{x}^{(B)} = 0.189$

According to the author these numbers are to be taken only as a first rough

approximation.

It is also of importance to know the frequency function of masses for stars in a certain volume of space. This problem can be solved by reducing the number of stars  $n_B, n_A \dots$  in the above equations to equal volumes. Because of the lack of parallaxes Eddington's theory is used in such a way that the absolute (belometric) magnitudes, M, are used which are computed from the supposition of constant space-density

The space unit is a sphere with such a radius that the stars of mass  $\mathfrak{M}_s$  in stage B which are situated on its surface are of apparent magnitude  $+8^{m}$ ,0.

Thus:

$$M_B+C_B=8^{\rm m},0,$$

where  $M_B$  is the bolometric magnitude of a star of mass  $\mathbb{R}_B$  and  $C_B$  the reduction to be applied to  $M_B$  to give it the absolute visual magnitude of spectral

class B. The ratio of the distances  $r_1$  and  $r_2$  of two stars of equal apparent magnitude having the absolute magnitudes  $M_1$  and  $M_2$  is

$$r_1/r_2 = 10^{-0.2(M_1 - M_2)}$$

and the ratio of the two volumes  $v_1$  and  $v_2$  with radii  $r_1$  and  $r_2$  is.

$$v_1/v_2 = 10^{-0.6(M_1-M_1)}$$
.

A star of mass  $\mathfrak{M}_B$  in spectral stage A has a visual magnitude  $M_B+C_A$  and thus  $n_B$  in the equations related to stage A has to be multiplied by the factor

In the equations corresponding to stages F, G, etc  $n_B$  appears multiplied by the factors  $10^{-0.6(C_F-C_B)}$ ,  $10^{-0.6(C_B-C_B)}$  etc

In the same way we find for  $n_A$  in the equation for the A stage the factor  $40^{-0.6(M_A+O_A-M_B-O_B)} = 40^{-0.6(M_A-M_B)} \cdot 10^{-0.6(O_A-O_B)}$ 

We introduce

$$\overline{n_A} = \eta_A \, 10^{-0.6(M_A - M_B)} \\
\overline{n_T} = n_F \, 10^{-0.6(M_F - M_B)} \\
\vdots \\
\overline{n_L} = n_F \, 10^{-0.6(M_A - M_B)}$$

The following values were used in the calculation

$$M_B = -2^{m},3$$
  $C_B = +1^{m},8$   $M_1 = +0,2$   $C_A = +0,3$   $M_h = +2,2$   $C_h = 0,0$   $M_0 = +4,0$   $C_0 = +0,2$   $M_h = +5,0$   $C_h = 0,8$ 

from which it was found that

$$\overline{n_A} = 850$$
  $n_A = 20389000$   $88,92$   $\tau_B^{(R)} = 0,589$   $\overline{n_B} = 376$   $n_B = 2268000$   $9,89$   $\tau_A^{(R)} = 0,039$   $\overline{n_F} = 464$   $n_F = 232000$   $1,01$   $\tau_A^{(R)} = 0,035$   $\overline{n_A} = 1123$   $n_A = 35500$   $0,15$   $\tau_B^{(R)} = 0,070$   $\overline{n_B} = 5424$   $n_B = 5500$   $0,02$   $\tau_A^{(R)} = 0,267$ 

Another computation was undertaken of the frequency function of the masses of stars bughter than 8<sup>m</sup>,0, in which attention was paid to the change in the visual magnitude with the colour. The following results were found

Spectral class	$\mathfrak{m}_B$	Ma	Mr.	We .	$\mathfrak{M}_K$	Sum	Mean masses
В	3196	0	0	0	0	3196	$\mathfrak{M}_{B}=4.27\odot$
A	1679	7176	0	0	0	8855	$\mathfrak{M}_{1} = 1.81$
F	2008	1248	4698	О	0	7954	$\mathfrak{M}_{1} = 1.62$
G	3210	748	410	3028	0	7396	$M_0 = 2,14$
IC	5 5 2 5	680	141	152_	3267	9773	$\overline{\mathfrak{M}}_{K}=2,56$
Sum	15618	9860	5249	3180	3267	37174	

217. Sproul Determinations of Masses In 1922 J A MILLER and J II. PITMAN<sup>I</sup> made use of the material available for computing the masses of the visual binary stars. The original parallax programme of the Sproul Observatory was outlined with a view to determine the masses of these stars. All the visual binaries

<sup>1</sup> A J 34, p 127 (1922)

with well-determined orbits have been included, together with objects for which tolerable elements will be known in the near future. Most of these objects have also been included in the other parallax observatories, so in most cases determinations of several modern parallax values are available.

Most of the pairs in question are so close together that the combined images on the plates at Sproul are sensibly round. The question then arises whether the orbital motion will not change the shape of the photographic image and vitiate the determination of the parallaxes. PITMAN and Miss POWELL have made an investigation with regard to this question using the equation

$$C + t\mu + /\pi + \frac{\theta}{2} \sin \theta = d,$$

in which d is the total displacement, and the fourth term on the left side takes into account the apparent orbital motion, q and  $\theta$  being the radius vector and the position angle of the star in its orbit. For the stars with dm smaller than  $2^m$  it was found that there were the following changes in the parallaxes:

According to the opinion of the present writer the errors in the trigonometric purallaxes, other things being equal, are slightly larger in the case of double than in the case of single stars. As the orbital motion contributes so little to the error, the discrepancy is cortainly caused by other factors, which are mainly dependent on the nearness of the images

Am	
0",000-0",001 0 ,002 0 ,004 0 ,009	11 1

The average sums of the masses within the different spectral classes are as follows according to MILLER and PITMAN:

Openiral aless	В	A	It	G	K	N
W. + W.	(14,91 ①) B	3,490	3,92 © 11	1,77 ① 6	1,57 @	0,650

The mass of the B stars was taken from other sources

218. Pitman's Investigation. An extensive presentation of the existing material for deriving the masses of the binary stars was given by J. H. PITMAN in 1929<sup>1</sup>. The orbits of the binaries are generally those given by VAN DEN BOS<sup>2</sup> together with a few orbits, new or revised, published since the latter's paper appeared. The parallaxes are taken from the manuscript catalogue of the Sproul Observatory. In general only modern determinations are used. These are corrected for systematic errors and weighted according to the method given in Pop Astr 31, p. 244. The corrections reduced the determinations of trigonometric parallaxes to the same system as ADAMS's spectroscopic results; in this sense the parallaxes tabulated are absolute.

The objects are divided into three groups, which are given in separate tables. Table I contains 33 stars for which the probable error of the parallax does not exceed fifteen per cent of the parallax itself. Table II contains 20 stars for which the probable error lies between fifteen and thirty per cent of the parallax, while Table III contains 54 cases in which the probable error exceeds thirty per cent and those for which only one trigonometric determination has been made. In each case the trigonometric parallax has been made the basis of classification.

The results are summarized in the following table, where the absolute magnitudes are visual values. The second lines in the table give the average masses and absolute magnitudes for the single components. The numbers #

<sup>&</sup>lt;sup>1</sup> A J 39, p. 57 (1929). <sup>8</sup> B A N 3, p. 149 (1926).

Spectrographic σ distances         Spectrographic σ distances         Trigonometro τ         Trigonometro τ         Spectrographic σ distances         Trigonometro τ         Trigonometro τ				Visual	ual binanes	n					Echpsu	Echpsing binaries	, A		-		Spec	trosco	Spectroscopic binaries	**		028
Meanmass         M.         M.         Meanmass         M.	Spectral	Trigit	pometr	2 31	S	pectrog	raphic a		Ing	nometric	7		pectrogra	phic m		Trigon	отеры т		Spec	trograph	۲	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		Mean mas			N	328	Ж	u	Mean mass	M	2	Meanm		, n		ean mass	Jζ		Mean mass	M		
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0 -B0											70,10		x,26	CI	17,40	~	4	85,00	-4 4 J	9	<u> </u>
$\begin{array}{cccccccccccccccccccccccccccccccccccc$												35,0		89,	4	8,7	3 96	4	42,5	13,		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	B1-B3			-	12,90		1 M, 14	₹	20 870	7 ×0	_	15,24	_	,54	1	15,5	99, 0	C)	9,91	11 7		_
$\begin{array}{cccccccccccccccccccccccccccccccccccc$					6,4		0 ,27	7	10 44	9, 01	-	7,6		81	14	7 75	1 29	4	5 22	0	4	
265O         2 <sup>8</sup> 80         6         269         2,23         9         4,71         -1,47         1         4,61         0,51         4         1,58         0,79         3,50         2         5,37         0,25         7           676         1         5         1         2         4         7         1,47         1         4,61         0,51         4         2,60         0,56         15         7         0,56         1         2         3         3         1         2         9         4,71         -1,47         1         4,61         0,51         4         1,50         2         3         0         0         3         3         0         3         3         0         3         3         2         2         4,72         0         3         3         0         0         3         3         0         3         3         0         3         3         1         4         5         0         0         3         4         4         4         4         4         4         4         4         4         4         4         4         4         4         4         4         4         4 <td>B4-B8</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>787</td> <td></td> <td></td> <td>7,18</td> <td>_</td> <td>2</td> <td>4</td> <td>1,58</td> <td>2 ,72</td> <td>41</td> <td>11,21</td> <td></td> <td>0</td> <td></td>	B4-B8								787			7,18	_	2	4	1,58	2 ,72	41	11,21		0	
2650         2 <sup>8</sup> 80         6         269         2,23         9         4,71         1         4,61         0         51         4         1,88         0         61         4         2,60         0         56         15           152         3         25         1         54         1         1,51         2         33         1         1,52         7         0,94         1,66         8         1,30         1         92         30           6 76         1         54         4         5,47         1,16         9         2,37         -0         72         2         2,36         1         30         0         12         3         2         2         1,42         1         30         0         1         2         1         4         3         3         1         3         3         1         3         3         1         3         3         1         1         2         3         4						•••			3.94		-	3.55		2,	00	0,79	3,50	61	5,37	0		
152         3,25         10         1,51         2,94         15         2,37         -0,72         2,36         1,52         7         0,94         1,66         8         1,30         1         92         30           676         1         54         4         5,47         1,16         9         1,30         2         320         0         12         3         2         35         1,48         4         1,48         1,48         4         1,48         4         1,47         0         1,30         2         3,43         1         2,48         3         8         1,48         4         1,48         4         1,48         4         1,48         4         1,48         4         1,48         1,48         4         1,48         4         1,48         4         1,48         4         1,48         4         1,48         4         1,48         4         1,48         4         1,48         4         1,48         4         1,48         4         1,48         4         1,48         4         1,48         4         1,48         4         1,48         4         1,48         4         1,48         4         1,48         4	B9-A1	2 65O	3 M 5	30,	2 69	_	2 ,23	6	4,71		-	4,6	-	,51	4	1,88	0,61	4	2,60	0		
6 76         1 54         4 5,47         1 ,16         9         4,29         1 ,30         2 320         0 12         3 252         1 ,42           3 15         2 41         8 2,74         2 ,07         18         10         2,15         2 ,23         4 1,60         1 18         6 1,26         2 ,43           3,57         2 ,25         4 5,17         1 ,88         10         2,15         1 1         2,90         4 ,82         1 2,76         2 ,23         4 ,57         2 0,86         2 ,43           2,44         3 ,26         9 2,12         3 ,70         4 ,82         1 2,76         2 ,21         2 ,67         2 ,90         2 ,93         2 ,10         4 ,57         2 ,90           2,44         3 ,26         18         2,22         3 ,70         2 ,81         2 ,91         2 ,91         2 ,91         3 ,91         1 ,126         2 ,90           2,11         3 ,76         18         2,22         3 ,70         4 ,82         1 ,26         5 ,43         2 ,13         4 ,57         2 ,20         2 ,67         2 ,56         2 ,23           2,11         3 ,76         18         4 ,75         45         65         65         67         1 ,78         <		1 52	47	15 10	1,51		2 ,94	15	2,37			2,36	_	,52	7	0,94	1 ,66	œ	1,30	4		
315         2 41         8         2,74         2 ,07         18           3,57         2 ,25         4         5,17         1,88         10         1,17         0 ,53         1         1,26         1,45         2 ,43         26           2,44         3,57         2,25         4         5,17         1,88         10         1,17         0 ,53         1         2,95         3 ,89         1         1,73         1,26         2 ,93         3 ,98         1         1,17         0 ,53         1         2,95         3 ,93         1         1,73         1         2,96         3 ,98         1         1,73         1         2,96         3 ,98         1         1,73         1         2,96         2         2,12         3 ,48         1         1,173         1         2,56         2         2,21         2         2,57         2         2,57         2         2,57         2         2,56         2         2,21         3 ,76         4         4         1         1         2,25         2         2,37         4         4         1         2         2,51         1         1         2         2,51         1         1         2         2 </td <td>A2-A6</td> <td>929</td> <td>-</td> <td>4</td> <td>5,47</td> <td></td> <td>1 ,16</td> <td>6</td> <td></td> <td></td> <td>-</td> <td>4,25</td> <td></td> <td>,30</td> <td>CI</td> <td>3 20</td> <td>0 12</td> <td>(1)</td> <td>2 52</td> <td>4,</td> <td></td> <td></td>	A2-A6	929	-	4	5,47		1 ,16	6			-	4,25		,30	CI	3 20	0 12	(1)	2 52	4,		
3,57         2,25         4         5,17         1,88         10           4,59         4,15         10         2,41         3,32         22         1,17         0,58         1         2,17         0,58         1         1,17         0,58         1         1,17         0,58         1         1,17         0,58         1         1,17         0,58         1         1,17         0,58         1         1,17         0,58         1         1,17         0,58         1         1,17         0,58         1         1,17         0,58         1         1,17         0,58         1         1,17         0,58         1         1,17         0,58         1         1,17         0,58         1         1,17         0,58         1         1,17         0,58         1         1,17         0,58         1         1,17         0,58         1         1,17         0 <t< td=""><td></td><td>3.15</td><td></td><td>3</td><td>2,74</td><td></td><td>2,07</td><td>18</td><td></td><td></td><td>-</td><td>2,15</td><td></td><td>,23</td><td>4</td><td>1,60</td><td>1 18</td><td>9</td><td>1,26</td><td>2 4</td><td>~ -</td><td></td></t<>		3.15		3	2,74		2,07	18			-	2,15		,23	4	1,60	1 18	9	1,26	2 4	~ -	
1,59         4,15         10         2,41         3,32         22         2,41         3,32         22         2,44         3,32         22         2,45         3,15         11         2,90         4,82         1         2,76         2,21         2         2,02         2,67         5         2,56         2,23         11           2,44         3,26         9         2,12         3,15         11         2,90         4,82         1         2,76         2         20         2         20         2         20         2         20         2         20         2         20         2         3         1,01         3,64         10         1,28         3,02         22         2         2,20         2         2,21         2         2,07         2         1,26         5         6         2         1         2,64         10         1,28         3         10         1         1,28         3         1,01         3         4         1         2,12         2         2,26         2         2,21         2         2,26         2         2,31         3         4         4         4         4         4         4         4 <th< td=""><td>A7-F2</td><td>3.57</td><td></td><td>5</td><td>5,17</td><td></td><td>1,88</td><td>10</td><td></td><td></td><td></td><td>1,17</td><td>_</td><td>55</td><td>7</td><td>2 95</td><td>3,89</td><td>~</td><td>1,73</td><td>e.</td><td></td><td></td></th<>	A7-F2	3.57		5	5,17		1,88	10				1,17	_	55	7	2 95	3,89	~	1,73	e.		
2,44         3,26         9         2,12         3,45         11         2,90         4,82         1         2,76         2,21         2,01         3,64         10         3,64         10         1,28         3,02         22           2,11         3,76         18         134         4         54         28         1,45         5         88         2         159         2         83         3         1,01         3,64         10         1,28         3,02         22           2,11         3,76         18         2,22         3,70         24         1,26         5,60         2         126         5,13         2         2,01         4,34         1         2,12         2,37         2           4,75         4,94         33         11         4         92         11         6         3,14         1         2,12         2         3,14         4		1.59				_	3 ,32	23			_	0,58		30	61			(1	0,86		-	
131     4,50     18     134     4 54     28     1,45     5 58     2     159     2 83     3     1,01     3,04     10     1,26     3,02     22       2,11     3,76     18     2,22     3,70     24     1,26     5,60     2     126     5,13     2     2,01     4,34     1     2,12     2,37     2       4,75     4,94     33     113     4     75     45     0.63     5     8     4     100     5     16     2     106     5     16     2     106     5     11     138     4     50     2     138     4     50     2       2,22     4,94     35     11     4     10     6     5     8     2     136     5     10     5     10     5     10     5     10     5     10     5     11     4     10     6     5     11     4     10     6     10     6     10     6     10     6     10     6     10     10     10     10     10     10     10     10     10     10     10     10     10     10     10     10     10     10	F3-F7	2,44			_	-	3 ,15	11	2,90		2 1	2,76		12,	7	-		ru i	2,56			
2,11     3,76     18     2,22     3,70     24     1,26     5,60     2     126     5,13     2     2,01     4,34     1     2,12     2,37     2     3,14     4     75     45     0 63     5     8     4     108     5     9     5     100     5     16     2,12     2,37     2     1,38     4     5     138     4     5     1     138     4     5     1     138     4     5     1 <td< td=""><td></td><td>131</td><td></td><td></td><td></td><td>_</td><td>4 54</td><td>28</td><td>1,45</td><td></td><td></td><td>1 59</td><td></td><td>83</td><td>3</td><td></td><td></td><td>٦</td><td>3,5</td><td></td><td>-</td><td></td></td<>		131				_	4 54	28	1,45			1 59		83	3			٦	3,5		-	
106     4,94     33     113     4 75     45     063     5 83     4     108     5 09     5 100     5 10     2 100     5 10     2 100     5 10     2 100     5 10     2 100     5 10     2 100     5 10     2 100     5 10     2 100     5 10     2 100     5 10     2 10     4 50     2 10     4 50     2 10     4 50     2 10     4 50     2 10     4 50     2 10     4 50     2 10     4 50     2 10     4 50     2 10     4 50     2 10     4 50     2 10     4 50     2 10     4 50     2 10     4 50     2 10     4 50     2 10     4 50     2 10     4 50     2 10     4 50     3 10     4 50     <	G0-G2	2,11				<b>6</b> 3	3 ,70	24	1,26		-	1 26		133	C1 1			(	2,17			
4,75     4,91     6     2,71     4     92     11       2,28     6     11     11     1,35     5     ,84     22       1,54     6     2,1     11     10     6     5     61     4     0,69     5     61     4     0,69     5     61     4     0,69     5     61     4     0,69     5     41     4       0,78     10     43     2     1,16     9     97     2     1,20     8     320     1       0,31     11     ,40     5     0,51     11     02     5     060     9     02     2     060     8     90     2		1 06		-			4 75	45	0 63			1 08		6	'n		10	7	9 6			
2,28         6         11         11         1,35         5,84         22           1,54         6,21         6         4,39         5,38         7           0,78         17         43         2         1,120         8,32         1         1,20         8,20         1           0,64         10,48         5         0,51         11,02         5         060         9,02         2         060         8         90         2	G3-G9	4,75					4 92	11			_		_			200	20 4	N *	1 50		_	
1,54     6 ,21     6 4,39     5 ,38     7       0,78     7 43     13     2,01     6 ,38     16       0,64     10 ,43     2 1,16     9 97     2 1,20     8 ,32     1     1,20     8 ,20     1       0,31     11 ,40     5 0,51     11 ,02     5 060     9 ,02     2 060     8 90     2		2,28					5 ,84	22	-					_	_	600	5 01	4	0,00	J.		
0 78   7 43   13 2,01 6 ,38   16	М	1,54			_	_	5 ,38	7							,			****				<b>D1</b>
0,64 10 ,43 2 1,16 9 97 2 1,20 8 ,32 1 1,20 8 ,20 1 0,31 11 ,40 5 0,51 11 ,02 5 060 9 ,02 2 060 8 90 2		0 78	7 4				5,38	16			_	1,74		4	<b>4-1</b> ·							C 1
11,40 5 0,51 11,02 5 060 9,02 2 060 8 90 2	M	0,64						ч	1,20			1,20	_	,20	-1		-					ıcı
		0,31		0, 5	0,51			īŪ	09 0			090	_	8	01	-		-			_	.61

represent the numbers of stars, only in the case of the trigonometric parallaxes of visual binaties the n represent the weights given to the mass-values

PITMAN has reduced the M's to belometric values and has made detailed comparisons between his results and the mass-luminosity diagram of Eddington. A change of  $+0.15\pi$  in the parallax will increase M by 0,3 and decrease log M by 0,18, while a change of  $-0.15\pi$  in the parallax will increase log M by 0,21 and decrease M by 0,35 Seventy-five per cent of the first-class determinations fall within these limits of the curve There are, however, a few cases that would require changes of  $0.50 \pi$  or more in the parallax With regard to the values denived from the spectrographic parallaxes there is a marked concentration of stars of approxmately the same mass and absolute magnitude as the Sun There is also a very large scattering, which may or may not be due to errors in the observed data

The spectroscopic binaries that show both spectra were also investigated From the "Third Catalogue of Spectroscopic Binaries" and various other sources Priman collected

<sup>&</sup>lt;sup>1</sup> Lick Bull 11, p 141 (1924)

75 such systems and compared the minimum values of M with the mass-luminosity law. The comparisons of PITMAN show that there is a correlation between M and log M. The value of the coefficient of correlation can be estimated as having a value of about 0,7. Another question is whether such a correlation has a physical meaning such as that expressed in the mass-luminosity law. For the present it hardly seems possible to answer this question even if the material available seems to suggest a revision of the constants in Eddington's formula.

819. Statistics of accurately Determined Stellar Masses. E B. Wilson and W. J Luyten<sup>1</sup> made an investigation with a view to discuss the material concerning stellar masses as a set of precise astronomical measurements.

To begin with they quote the 8 cases of stellar mass determinations given by Eddington in his well-known book, "Stellar Movements" The figures expressed in terms of the mass of our Sun are in order of size 0,7, 1,0, 1,0, 1,3, 1,8, 1,9, 2,5, 3,4, from which  $2R = 1.7 \pm 0.2$ . As no masses may be negative and there is no restriction, except through disintegration by internal light-pressure or dynamical fission upon the upper side, it is natural to discuss the distribution, not of the mass itself, but of its logarithm The 8 results are -0,155, 0,000, 0,000, 0,114, 0,255, 0,279, 0,398, 0,532, from which  $\log \mathfrak{M} = 0,178 \pm 0.05$ . The dispersion  $\sigma$  is 0,21  $\pm$  0,035 and the probable error  $\varrho = 1 \sigma = 0.14$ . The geometric mean mass is 1,5 and coincides with the median. If the distribution is normal a departure of 9  $\rho = 1,26$  in the logarithm from its mean 0,18 could not occur; because there is only one chance in a billion and a half that log IR should exceed 1.44 and an equal chance that it should be less than 8,92-10, and there are probably less than one billion stars nearer than 2000 parsecs, which makes it certain that no such numbers could possibly be registered on the best photographic plate. There are at least three known binaries the mass of which exceeds 10124 - 27,5 0. It is clear, therefore, that a normal distribution as determined from these data has no correspondence in the stellar world.

Then the authors use the following 15 systems as having reasonably well-determined masses:

```
a Aurigne
                                   η Casadopeiso 1,13 () = 0,89 () + 0,24 ()
          7.50 0 - 4,18 0 + 3,32 0
B Aurigue
                                   & Bootis
                                                     = 0.58 + 0.51
          4.72 = 2.38 + 2.34
                                               1,09
                 - 2,45 + 0,96
a Can Ma 3.41
                                    Sun
                                               1.00
80 Tanri
           2,57
               -1,85 + 0,72
                                   85 Pegnal
                                               0,93
                                                     = 0.60
                                                             + 0,33
a Centauri 2,11 - 1,14 + 0,97
                                   "Horoulis BC 0.88
                                                     -0.44
                                                             + 0,44
70 Ophluchl 1,82 = 0,96 + 0,86
                                   Krueger 60 0;43
                                                     = 0.30
                                                             + 0.13
¿ Hercolls
           1,60 = 1,12 + 0,48
                                   e Bridani BC 0.41
                                                     ~ 0,21
                                                             + 0,20
a Can. Min. 1,50 - 1,13 + 0,37
```

The mean  $\overline{\mathbb{R}} = 1.97 \pm 0.28$ , the median is still 1.50,  $\overline{\log \mathbb{R}}$  is 0.18  $\pm$  0.06, and  $\sigma_{\log \mathbb{R}} = 0.34 \pm 0.04$ . The mean deviation  $\vartheta$  is 0.27 and the test  $\sigma_{\mathbb{R}} = 1.25 \vartheta$  for normality is perfect. A study of the distribution of the log  $\mathbb{R}'$ s with regard to the size of the probable error,  $\varrho = 0.23$ , also gives evidence of the satisfactory normality of the frequency function. The  $\mathbb{R}$  is 1.50. The larger material in this second case has increased the size of the error by a fifth. The authors say that even considering the small size of samples 8 and 15 it is difficult to reconcile the relative magnitudes of the standard deviation and their probable errors; the difficulty would have been even greater if the additional 7 had been treated as a second sample. The fact is that the two sets probably do not belong to the same statistical universe—one at least of the samples is not fair.

Wash Nat Ac Proc 10, p. 394 (1924)

From HERTEPRUNG's paper in BAN 2, p. 15 (1923).

If charmed with the excellence of the normal distribution of the 15 cases one would derive the probability of a binary with  $\log \mathfrak{M}$  as great as 0.18  $\vdash 9\varrho$  = 2.21 it is found that the chance will be one in a billion and a half for a star of mass 1620. The authors points out that we have Plaskeri's star with such a mass, and that 27 Canis Majoris probably has a still larger mass.

Of course, considerable uncertainty is involved on account of imperfect parallax data. The figures may be inaccurate by 30 percent, which means a variation of some 0,12 in the individual logarithms. If there is nothing systematic in such errors the error in the mean will be about 0,03. As far as the accidental errors go, the mean will be reasonably well-established although the error is liable to increase when a more extensive material is at hand

A similar discussion is given for the 29 stars of Herizsprung's list when each component of a binary is counted separately. The  $\mathfrak{M}$  is then 1,07  $\pm$  0,12 and the median mass 0,86 and the distribution is skew. The log  $\mathfrak{M}$  is 9,984  $\pm$  10  $\pm$  0,044, the median 9,934  $\pm$  40, and  $\mathfrak{M}$  = 0,965. The dispersion is 0,357  $\pm$  0,030, and checks perfectly with  $\sigma$ . Its value is not greater to 29 stars than for 15 systems. The mean is better determined statistically in the first sample than could be expected before when one remembers that the scanty material has only been doubled.

220. Real and Apparent Masses If the mass of a star undergoes a steady decrease from spectral class B to M, as is indicated by the work of Shares, various suggestions present themselves as an explanation of this phenomenon B. A Kostitzin<sup>2</sup> has applied the results of Majorana<sup>3</sup> with regard to a possible absorption of the gravitation. The real mass of a star is designated by  $\mathfrak{M}_r$  and the apparent mass by  $\mathfrak{M}_a$ . Let further r be the radius,  $\bar{\varrho}$  the mean density, and  $\alpha$  the coefficient of absorption = 7.59  $\cdot$  10<sup>-12</sup> for the Sun. Then the attractive force will be diminished in accordance with the "law of progressive absorption" and in the case of a homogeneous liquid mass, where  $\bar{\varrho}$  is equal to the true density, the following equations hold good

$$\mathfrak{M}_{n} = \frac{\pi_{o} \gamma^{2}}{\alpha} \left[ 1 + \frac{e^{-2\alpha \overline{\varrho} r}}{\alpha \overline{\varrho} r} + \frac{e^{-2\alpha \overline{\varrho} r}}{2\alpha^{2} \overline{\varrho}^{2} r^{2}} - \frac{1}{2\alpha^{2} \overline{\varrho}^{2} r^{2}} \right], \qquad \mathfrak{M}_{r} = \frac{4}{3} \pi_{o} \overline{\varrho} r^{3}.$$

Introducing a new variable  $2\alpha \tilde{\varrho}r = v$  and putting

$$\varphi(v) = [(1+v)e^{-v} + 0.5v^2 - 1]3v^{-3}$$

Kosticzin finds the relation;

$$\mathfrak{M}_{a}=\mathfrak{M}_{r}\varphi\left( v\right)$$

Accordingly  $\varphi(v)$  is the ratio between the apparent density and the true density. If the above value of  $\alpha$  and  $\mathfrak{M}_r = 5.3$  times the apparent mass of the Sun are accepted for the Sun, it is found that for a stai with the same real mass as the Sun and  $r = 9 \, r_{\rm O}$  the apparent mass  $\mathfrak{M}_a$  is nearly equal to its real mass, viz 5.3 times the apparent mass of the Sun. If  $r = 3 \, r_{\rm O}$  the apparent mass is four times the apparent mass of the Sun. The diameters thus derived for different spectral classes are of the same order of magnitude as the computed ones.

H N Russell has pointed out that if the absorption of gravitation is accepted there are a number of important astronomical consequences. The true masses of the planets have been computed according to this theory and it is found that the inertial masses cannot be equal to the true masses. If they are assumed

<sup>&</sup>lt;sup>1</sup> Mt Wilson Contr 226 (1922)

<sup>&</sup>lt;sup>2</sup> Publ Obs Astrophys Centr Russ Moscou 2, p 289, 303 (1923)

<sup>&</sup>lt;sup>3</sup> Phil Mag 39, p 488 (1920) Ap J 54, p 334 (1921), Mt Wilson Contr 216.

to be equal to the apparent gravitational masses we are led to such discrepancies in the case of the tides that the conclusion is unavoidable that the coefficient of absorption cannot exceed 1/8000 of the value assigned to it by MAJORANA.

221. Seares's Researches. In an extensive paper of 1921 F. II. Seares¹ has made an interesting study of the masses and densities of the stars partly along new lines. The salient point in his method is a comparison between the absolute magnitude  $M_d$  as derived from the dynamical parallax  $\pi_d$  and the spectrographic magnitude M as derived from  $\pi$ . The well-known relation

$$\mathfrak{M} = \mathfrak{M}_A + \mathfrak{M}_B = \frac{a^3}{\pi^3 P^4}$$

gives.

$$\log \mathfrak{M} = k - 0.6 M,$$

where

$$M = m + 5 + 5 \log \pi$$

and

$$h = 3\log a - 2\log P + 0.6m + 3.$$

The assumption used in the computation of  $\pi_2$  is  $\mathfrak{M}=20$ . Thus if the orbital elements are known:

$$0.30 = k - 0.6 M_{d}$$

and:

$$\log \mathfrak{M} = 0.30 - 0.6 (M - M_d) = 0.30 - 0.6 \Delta M$$

and for a group of stars

$$\log M = \log R = 0.30 - 0.6 (M - M_{\bullet}) = 0.30 - 0.6 AM$$

The next last equation only holds good for individual stars in the case of binaries where the elements are known, because the mean inclination of the orbital planes is involved in the dynamical parallaxes. The last equation holds good for any group of stars.

At that time, in the case of the binaries investigated, only  $M_d$  was known, and thus an indirect process was necessary. Shakes used  $M_d$  from single stars of known parallax, whose selection with respect to the stars as a whole presented the same characteristics as those of the binaries themselves.

If  $\overline{M_s}$  represents the mean absolute magnitude of a certain spectral type of single stars of known parallax, and  $\overline{M_b}$  the corresponding value for binaries of the same type, we have:

$$\widetilde{M_*} = \widetilde{M_*} + \delta M_*$$

Thus oM expresses the influence of difference in selection. We may write:

$$M_1 - M_2 = \overline{AM} = M_1 - M_2 + \delta M = \overline{AM_1} + \delta M$$
.

Shares has derived  $\partial M$  from the some hundred binaries of measured parallax and calculated  $\overline{\partial M}$ , for each spectral type by comparing the 550 stars in the lists of Jackson and Fuener with the homogeneously selected single stars of known parallax. Then  $\overline{\partial M}$  was formed and M computed. The underlying assumption is that the mass-luminosity relation is the same for both binaries and ordinary stars.

The binaries and single stars of known parallax were grouped according to apparent magnitude and spectral class. The comparison between 505 binaries and 1152 parallax stars from Adams's catalogue in Mt Wilson Contr 199 and from

Mt Wilson Contr, No. 226 (1922), Ap J 55, p. 165 (1922).

Kapteyn's investigation of the parallaxes of the helium stars gave the following table

Median		В			A			Γ		G5-	-K5	(1	K
apparent magnitudo	B	J&P Pi	K&A Pi	BS	J&r Pl	K & A	B	J&b Pi	K&A	B	J&F Pi	K&A Pi	k & A 14
3,5	0,1			0,1			0,4			1			
4,5	0,2	7	34	0,2	3	17	0,3	3	12	3	3	3	0,4
5, 5	0,2	2	13	0,6	2	4	0,3	2	6	0,8	2	4	1,5
6,5	1,0	1,0	1,0	1,0	1,0	1,0	1,0	1,0	1,0	1,0	1,0	1,0	1,0
7,5	$\infty$	0,52	0,00	1,6	0,29	0,18	1,5	0,38	0,25	2,2	0,80	0,33	0,46
8,5	000	0,08	0,00	1,5	0,04	0,03	1,8	0,10	0.05	3,5	0,54	0,08	0,34
9,5	-	0,00	0,00	0,2	0,00	0,02	0,7	0,01	0,01	0,5	0,02	0,02	0,12
B	bınaı		; <u>J&amp;</u>		6/	SON &		ER	K & A	K	Adminis 60	n & Ai	

If the selection for the two lists were the same, the ratios of the corresponding numbers would not vary with magnitude, and if the selection were homogeneous the ratios for the different classes would show the same change

The number of A stars in the spectrographic list then available was small, and in order to obtain a test Seares used the star counts of W II Picki RING<sup>2</sup>.

The degree of homogeneity is satisfactory and the only deviations of a school-nature are those of the faint G5—K5 stars and the faint B stars. The absence of pronounced irregularities in the curve  $M_d = f$  (Sp Class) shows that the error in the corresponding  $\overline{AM_d}$  must be small. The limitation in this value for called B stars, on account of the fact that Kapteyn's investigations do not include stars fainter than  $6^m$ ,0, will not be of much consequence

The increment  $\delta M$  determines the zero-point, which can easily be proved. Seares has used the spectrographic parallaxes alone, since they are based on a homogeneous system.

a homogeneous system

<sup>2</sup> Publ ASP 33, p 140 (1921)

A diagram given in fig 450 was constructed giving  $\overline{M}_s$  and  $\overline{M}_d$  as functions of the spectral class. The table shows the value of the zero-point for different spectral classes, the two lists of Jackson and Furner being treated separately:

Spectral class	$M_b-M_d$	d Me	δM	78	Spectral class	$\overline{M_b-M_d}$	AMa	anr	n
A7 F2 F5 G0 G4 K2 K8	-0 <sup>31</sup> .7 -0,6 -0,1 0,0 +0,4 +0,4 +0,5	-0 <sup>1</sup> ,5 -0,2 0,0 +0,4 +0,6 +0,7 +0,8	-0 <sup>1</sup> ,2 -0,4 -0,1 -0,4 -0,2 -0,3	3 14 13 18 10 7	A9 F5 G0 K3	-0 <sup>1</sup> / <sub>8</sub> 0 0 +0 3 +0 3	-0 <sup>11</sup> ,4 0,0 +0,4 +0,8	-0 <sup>M</sup> ,4 0 ,0 -0 ,1 -0 ,5	11 7 9 9
Mean			-0 ,29	69				-0 ,27	36

From 69 and 36 stars respectively mean values of  $\delta M = -0^{\rm M}$ ,29 and  $-0^{\rm M}$ ,27 were found, thus as a mean  $\overline{\Delta M} = \overline{\Delta M}_s - 0^{\rm M}$ ,3

was adopted The fact that there is no marked progression in the values of  $\delta MI$  with spectral class confirms the conclusion concerning the homogeneity of the selection.

In the determination of the zero-point a certain systematic difference was found between the results of Jackson and Furner with regard to  $\pi_d$  as determined

<sup>&</sup>lt;sup>1</sup> Mt Wilson Contr., No. 82, 147, Ap J 40, p 43 (1914), 47, p 146, 255 (1918)

from known elements or from arcs of relative motion. In the former case the agreement between  $\overline{n_s}$  and  $\overline{n_s}$  was excellent. In the second case the following systematic difference was found

$$\bar{\pi}_{s} = \bar{\pi}_{s} - 0^{\circ}.010$$

The stars occurring in both lists give  $\overline{\pi}_1 = \overline{\pi}_2 - 0''.007$ .

The value  $\overline{AM}$ , determines the rate AM/AS, where AS is the change in spectral index S, while the constant  $\partial M$  determines the zero-point. For the determination of  $\partial M$  only spectrographic parallaxes have been used In computing  $M_s - M_d$  it has to be borne in mind that the  $M_s$  correspond to the most probable values of the parallaxes and thus are not the most probable values of the magnitudes themselves. Thus a small correction of  $+0^M$ ,08 to the M tabular values was adopted.

The following geometrical mean masses were derived:

Spectral class	H,	Μe	Vimal binaries ut	Single Mars M
Bo	-1,60	(-0,25)	18 ①	10 0
B5	-0,20	+1,00	14	8,3
AO	+0,70	1,65	10,5	6,0
A5	1,50	2,15	6,9	4,0
FO	2,40	2,70	4,4	2,5
F5	3,32	3,27	2,7	1,5
Go	4,35	3,95	1,7	1,0
G5	5,20	4,60	1,3	0,76
Ko	5,90	5,20	1,2	0,68
<b>K</b> 5	7,10	6,30	1,1	0,62
Ma	十9,80	8,95	1,0	0,59

In order to test the influence of selection on the values of M on account of the lack of more distant stars the following comparison was made:

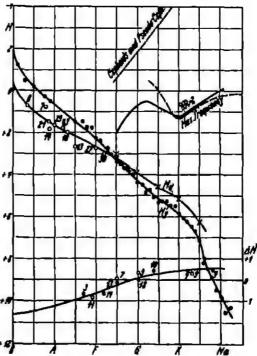


Fig. 150. SEARER'S determination of the masses of the stars from the different slants of the stars in the Russell diagram. The curve M, is the line of maximum frequency of M for the B stars of Kapieyn and the dwarfs from the list of spectroscopic parallexes. M, is the similar curve for the absolute magnitudes as based upon the dynamical parallexes derived by Jackson and Fuener. The differences in the ordinates, corrected for zero point, are shown by the curve below (AM). The straight line "Copheids and Pacudo-Coph." is the absolute magnitude spectral relation according to Russellus magnitude spectral relation according to Russellus maximum frequency for giants and the full drawn curve the mass line R = 2.

Ì	Šþ	d log 18		π	57	d log til	•
0",018 0 ,026 0 ,032 0 ,046	F2 F6 G1 F7	-0,08 -0,12 -0,08 +0,03	10 10 10	0",061 0 ,102 0 ,270	G3 G1 G8	-0,04 +0,04 +0,12	10 10 9

The slight systematization of the numbers shows that the mean masses of more distant stars have been computed too large. This suggests that the variation of  $\mathbb R$  with spectral class has been influenced by selection, and in order to make the data fully representative a constant correction to the log  $\mathbb R$  of -0.08 has to be applied. The values given above contain this correction.

In deriving the geometrical mean masses  $\mathcal{M}$  of single stars a constant value of  $\mathfrak{M}_B/\mathfrak{M}_A = 0.75$  was assumed.

The probable dispersion in the mass for dwarfs of F0 to M was determined as:

$$\sigma_{\log M} = \pm 0.22$$
.

This is not the true dispersion, but includes the errors in M and  $M_d$  as well. The dispersion in M is not well known and thus only the following dependence can be indicated:

αN	a log 201	Limits for probable error	σμ	a logm?	Limits for probable error
±0 <sup>M</sup> .35 0 .30 0 .25	±0,07 0,13 0,16	(0,85-1,18) <u>M</u> (0,74-1,35) <u>M</u> (0,69-1,45) <u>M</u>	±0 <sup>M</sup> ,20 0 ,15	士0,18 0,20	(0,66-1,51) M (0,63-1,58) W

If the kinetic theory of gases can be applied to the stars, this implies the equipartition of energy of translation so that:

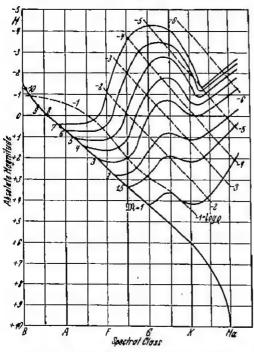


Fig. 151. Nomogram showing distribution of mass (full curves) and mean density (broken curves) of stars derived by Seares from the principle of equipartition. The full-drawn curve running downward to the right is the line of the maximum frequency of the dwarfs or the main series.

$$\mathfrak{M}_n \overline{V_n^3} = \text{const.}$$

The theory for a collection of stars is much simpler than for a gas, because encounters and collisions occur so seldom that they may be neglected. The effective agency for the transfer of energy is only that which arises from the attraction of the bulk of stars upon individual members of the system. The effect of this simplification is an enormous increase in the time of relaxation and for that reason several theorists have rejected the analogy between the stellar system and a collection of gases. On the other hand, JEANS concurs with the application of the theory of gases to the stellar universe.

Several objections are considered by Seares, who finds that equipartition has not been obtained within the stellar system, but that there may be an approach to that state.

The distribution of the logarithms of the space velocities can be represented by means of a normal (Gaussian) distribution. By applying the mean value theory to the frequency function it is found that

$$\log \overline{V^{\mathrm{g}}} = 2 \log \overline{V} + 0.148 = 2 \log \underline{V} + 0.296$$
 .

Further, as has been shown by CAMPBELL, the mean space velocity is equal to twice the mean radial velocity. On determining  $\log (\mathfrak{M}V^2)$  for different spectral

classes remarkable constancy was found. The total range of the values is only from 3,21 to 3,66 and most values are very close to the mean, 3,57. It thus seems justifiable to evaluate the masses. For spectral classes F5, G5, K3, and Ma a mass-luminosity relation was found as follows.

The surface brightness was derived by the aid of STRFAN's law. The following expression was derived for the surface brightness

$$j = M_{\text{Vis}} - M_{\text{Bol}} - 10 \log T_{\bullet} + \text{const.}$$

This formula was tested by comparison with the one derived by Hertzsprung in 1906 which was based on Planck's law and the measurements of visual sensibility by Langley,

Speciful chase		R		
И	F5	(+5	КЗ	Ma
-32 -10 +123 +5678	6,0 © 5.5 4,8 4,2 3,2 2,0 1,0 0,6	5.5 © 4,2 3,2 2,4 1,9 1,5 1,1 0,9 0,8 0,6	5,3 O 2,8 1,9 1,5 1,2 1,0 0,9 0,8 0,7 0,6	9,5 © 4,4 2,6 1,7 1,2
10				0,5

ABNEY, and others. The formulae involve quadratures. The excellent agreement is illustrated here:

T	Myn-Mad	BRARES	RESTRICTED	T	Myls-Mass	HEARES	FIERTERPENO
2540° 3000 3600 4500 6000	+2 <sup>M</sup> ,59 +1 ,71 +0 ,95 +0 ,35 0 ,00	+6=,32 +4 ,72 +3 ,17 +1 ,60 0 ,00	+6 <sup>1</sup> ,32 +4,68 +3,16 +1,58 0,00	7 500° 9000 10 500 12 000	+0*,02 +0 ,12 +0 ,31 +0 ,53	-0 <sup>ta</sup> ,95 -1 ,64 -2 ,12 -2 ,48	-0",93 -1,62 -2,09 -2,45

The connection of these results with the spectral classes was obtained by the aid of the spectral-photometric measurements of Wilsing giving of of 199 stars, mainly giants. In order to include dwarfs use was made of the un-

published colour indices determined by Shahes which should be regarded as provisional but which take account of the important difference in colour betwoon giants and dwarfs. This difference must be considered in any discussion of the surface brightness of stars of "late" spectral classes,

The change A<sub>1</sub>/dM could not be determined with accuracy and some extrapolation was necessary. A partial con-

Potsd Publ No. 74 (1919)
 Mt Wilson Comm 59, Wash
 Nat Ac Proc 5, p 232 (1919)

Spectral class	Clants	L, 14 → 0		Dwarfs		
	4/2	1	s <sub>e</sub> /T	1	At	
B()	1,36	-29,28				
B5	1,43	-2 ,14				
Λo	1.55	-1 .89				
λ5	1,76	-1 ,45				
Fo	2,04	-0.88				
175	2,35	-0 ,26	2.35	-0=,26	+3×.3	
Go	2,70	+0 .44	2,48	0 ,00	+4 .	
G5	3,10	+1 ,24	2,60	+0 ,25	+5 /	
UZI	3,70	+2 ,41	2,93	+0 ,90	+5 .9	
K5	4.37	+3 71	3.47	+1 ,96	+5 .1 +7 .1 +9 .1	
Ma	4,65	+4 ,25	4,30	+3 ,58	+9 1	
Mb	4,82	+4 ,58		, , , , ,	, , ,	
Mo	4,94	+4 ,81				

Olderi	# Orlonia	er Dontin	a Sonepli
Spectral class	Ma	Ко	Map
M	- 2 <sup>M</sup> ,6	+0M.1	-4×.2
doberved	+4 ,6	+2 2	+4 .5
desiculated .	+4 ,4	+2 ,4	+4 .5
Diam, observed ,	252 ①	25 0	506 O
Diam, calculated .	235 ⊙	27 ①	513 @
R (appr.)	80	30	15 @

trol of 1 was afforded by measurements of the diameter of three stars as performed by Pease

The following formulae given by Seares connect the angular diameter d, the linear diameter D, the mass  $\mathfrak{M}$ , the density  $\varrho$ , the surface brightness  $\eta$ , and the apparent and absolute magnitudes

The values of the masses and densities were also revised by means of Cepheids. If the pulsation theory is correct the mean density will vary inversely as the square of the period

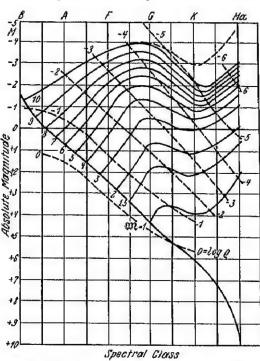


Fig 152 Nomogramaccoiding to Seares showing distribution of mass and mean density revised with the aid of Cepheids. The dotted curve at the top indicates the reduction to bolometric absolute magnitude for stars of spectral class F8—Ma of  $\mathfrak{M}=10$   $\odot$ 

$$\log \varrho = -2\log P + \text{const.}$$

Further the period-luminosity relation taken as.  $M = a - b \log P$ , where a and b are constants, determines the absolute magnitude. Thus the next last equation can be written.

$$\log \mathfrak{M} = -2 \log P - 0.6(M - j) + \text{const.}$$

Only small corrections to the data gained from other evidence were obtained from the 28 Cepherds for which the mass could be computed.

The decrease in mass may be partly or perhaps wholly accounted for by selection, but the possibility that mass may decrease with loss of energy by radiation is also suggested, a possibility which agrees with the theory of relativity and is not necessarily in conflict with Newton's mechanical principles.

Immediately after the work of Seares was published H. N. Russell pointed out that the spectrographic parallaxes ought to be dependent on the mass, and that thus by their very nature they are not very suitable for a determination of the dispersion in stellar mass. The

spectrographic magnitude  $M_s$  is a function of the temperature T and the density  $\varrho$ . The equation giving the density is easily transformed into

$$\log \mathfrak{M}_{\bullet} = \log \varrho + 0.6j - 0.6f(j, \varrho) + \text{const.}$$

The masses  $\mathfrak{M}_{\epsilon}$  are identical for stars with the same density and the same surface brightness, but the real masses may differ. Thus the masses computed by Seares should not be adopted in order to obtain the real dispersion in  $\mathfrak{M}$  and Russell suggests the use of trigonometric parallaxes for such a determination.

<sup>&</sup>lt;sup>1</sup> Ap J 55, p. 238 (1922), Mt Wilson Contr 226

The present writer found in 1924 the following results, which remain to-day (1929) substantially unchanged.

Trigonometric parallaxes . ±3,4 O
Spectrographic parallaxes . ±3,0 O
Spectrul proper-motion parallaxes . ±4,0 O

222. Stellar Masses from Spectrographic Parallaxes. In an extensive paper dealing with the ionization in stellar atmospheres A Pannekoer took up the question of a possible dependence between the intensities of the absolute magnitude lines and the masses. The Mount Wilson spectrographic determinations of parallaxes are founded on the relative intensity of some enhanced lines and some are lines of the stars. The relative intensities of are lines and enhanced lines of a certain element are wholly determined as far as their dependency on the degree of ionization is concerned by the relative position in the pressure-temperature-diagram of the ionization curve and the atmospheric curve, defined by

$$\log \phi \approx -10^{n-\tau} + 2.5\tau - 6.49,$$
  
$$\tau - \tau_1 \approx /\left(\log \phi - \log \frac{R}{h}\right)$$

where p is the pressure of the ionized gas,  $\tau$  the logarithm of the absolute temperature, and s a parameter depending on the ionization potential of the element.

The position of the atmospheric curve depends on the effective temperature T and the factor g/k. Stars of the same effective temperature, i.e. of the same spectral class, will show differences depending on the factor g/k. On account of the lack of data the coefficient of mass-absorption k has to be assumed to be constant. Further  $g = /\mathfrak{M}/R^2$  and  $L = 4\pi_0\sigma R^3$ , where  $\sigma$  is the surface brightness of a star. Then:

The reduction curves used at Mount Wilson have been adjusted by means of directly measured parallaxes for each separate spectral class. The real quantity measured at Mount Wilson is not L but  $L\Re_0/\Re$ , if  $\Re_0$  is the mean mass for the spectral interval considered.

In order to tost the theory use was made of dynamical parallexes. We then

have the relations.  $\mathbb{R}_{dyn} = 2 \left(\frac{\pi_i}{\pi}\right)^3$ ;  $\mathbb{R}$ 

 $\mathfrak{M}_{\mathrm{dyn}} = 2 \left( \frac{\pi_d}{\pi_{\mathrm{tr}}} \right)^3; \quad \mathfrak{M}_{\mathrm{sp}} = \left( \frac{\pi_{\mathrm{m}}}{\pi_{\mathrm{tr}}} \right)^3 \mathfrak{M}_0.$ 

As is evident from the following summary there seems to be a correlation between the two sets of masses:

log ng—log my	log my IR	logikaya	log Map	
+0.53	+0,53	+1,59	+1,06	5
+0,14	+0,16	+0,42	+0.32	6
+0,06	+0.13	+0,18	+0,26	9
-0,04	+0,06	-0.12	+0,12	8
-0.09	-0.05	-0.27	-0,10	7
-0,17	-0,12	-0.51	-0,24	7
-0,23	-0,25	-0.69	-0,50	4
-0,44	-0,47	-1,29	-0.94	4

From the double stars the following table was obtained:

Ma-Ha	log WA	R	Ma-Ma		*
-0 <sup>M</sup> ,3 -0 ,8	0,09	10	-1×,3 -2,9	0,26 0,36	10 9

<sup>1</sup> BAN 1, p 107 (1922), Obs 46, p. 304 (1923).

Predictions of the masses were made for a number of stars namely that the Cepheids should have small masses, and that the companions of the three pairs, α Herculis (3m,5; 5m,4; Mb, F9), Bu 8114 (6,5, 8,6, K2, F0), and y Delphini (4m,5, 5m,5; K1, F6), have a greater mass (13, 3 and 5 times greater) than the absolutely much brighter principal star of redder colour is of general interest.

Later on P. Doig1 compared the theory of Pannekoek with the evidence from binary stars. The following fourfold table in which  $\pi_{\text{spectral}}$  denotes the parallax derived on basis of the mean value  $\overline{M}$  of the absolute magnitude of dif-

ferent spectral classes is of interest.

	#spectral	nspectral
	$> \pi_{\rm tr}$	< ttr
$\pi_{\text{spectrographic}} > \pi$	tr 18	0
$\pi$ spectrographic $<\pi$	tr 2	14

This indicates the existence of a pronounced positive correlation between  $\pi_{\text{spectrogr}}$ and  $\pi_{\text{spectral}}$  When this happens the stars in question are more luminous than the normal star of their class and thus also more massive

The masses of 19 stars derived directly when compared with those computed according to Pannekoek's formula did show rather good agreement. On the other hand, the present writer2 found at the same time that there were no such systematic differences between the masses computed on the basis of trigonometric, spectrographic and spectral proper-motion parallaxes as were demanded by the theory of Pannekoek but it has to be added that we have to wait for more extensive data before any safe statements can be presented

Further investigations, which cannot be reviewed in detail here, have convinced me that there are no such deviations between masses derived from trigonometric and spectrographic and proper-motion parallaxes as make it possible to determine even mean mass values from an analysis of different parallaxes This does not exclude, of course, the possibility that there is a mass effect in the spectrographic parallaxes It is only to be regretted that this effect is evidently so small that it will require much work on the refinement of the trigonometric and spectrographic methods of determining the absolute magnitude before we can derive masses for single stars

Another way of showing the smallness of the mass-factor in spectrographic parallaxes is to use the relation

$$\Delta M = \Delta m$$

This relation does only hold good when no errors in m and M are present. In case of each quantity having mean errors of  $\varepsilon_M$  and  $\varepsilon_m$ , respectively, we can write  $\Delta M \pm \varepsilon_M = \Delta m \pm \varepsilon_m$ 

Even reasonable treatment of the data concerning spectroscopic binaries in the Mount Wilson material will lead to errors in M of the same size as those derived from single stars. If we had a mass-factor the equation would be

$$\Delta M + \alpha' \pm \varepsilon_M + f(bM + cM^2) = \Delta m \pm \varepsilon_m$$

if  $\log M$  is supposed to be  $= a + bM + cM^2$ . Although the material is small it seems that no appreciable mass-factor can be derived

223. Masses of F-K Stars. Gerasimovič has determined the masses of the stars of spectral classes F-K, starting from the following assumptions 1 the reversing layer of a star is in radiative and hydrostatic equilibrium. The absorp-

<sup>1</sup> JBAA 34, p 144 (1924) <sup>2</sup> V J S 59, p 203 (1924) 3 A N 227, p 145 (1926), Charkov Obs Publ, No 1, p 12 (1927)

tion lines that determine M are not of a chromospheric character, i. a they arise in the level where the selective radiation pressure is small in comparison to the gas pressure, 2 each line arises at the same optical depths in the reversing layers of all stars of the same spectral type. If these hypotheses are correct the intensity of a given spectral line is a function of the effective temperature and the gravity at the surface only. The chief cause of a variation in an intensity-ratio must be a change in the gravity. The following equation can be established:

$$M-2.5 \log \mathfrak{M} J = \varphi(M_a, T_a) = M_a + f(M_a, T_a)$$

where J is the surface brightness and  $T_s$  the effective temperature and the subscript s stands for spectrographic data. It follows from the above equation that:  $\overline{I(M_s, T_s)} = -2.5 \log \Re I.$ 

On account of the lack of data the direct method cannot be applied and we must proceed by successive approximations. At first it is supposed that

$$\log \mathfrak{D} = 0.4 [M - M_{\bullet}] - \log J + \overline{\log \mathfrak{D} J}.$$

From an analysis of the Victoria list of spectrographic parallaxes the following abbreviated results were found when the differences between the spectrographic and trigonometric magnitudes were grouped according to the magnitude:

These values are only approximate on account of my condensation of the data.

The systematic course of  $M_s - M_{tr}$  is very striking and according to Gerasi-

Absolute	P star		C) star	ni i	K sters	
magnitude	Mr-Mir	R	MMu	18	MMu	R
<0,0-0,9	+1×,4	6	+1 <sup>N</sup> ,0	30	1 0M,7	26
1,0-2,9 3,0-3,9	+0,2	26 40	-0 ,6 -0 ,3	29 19	0,0 -1,1	18
4,0-4,9 5,0-5,9	-0 ,3 -1 ,1	2B 13	10 ,1 -0 ,6	28	-1 .1 -0 .3	10

MOVIČ cannot be explained as a consequence of some systematic error in the trigonometric parallaxes. The same phenomenon as is illustrated above has been noted by van Rhijn<sup>1</sup>, who made a comparison between the Mount Wilson  $M_t$  and  $M_{tr}$  based on the Groningen determinations of  $\tilde{\pi}$  as a function of proper motion and apparent magnitude. Van Rhijn explains the phenomenon by the lack of sensitiveness of the spectrographic criteria for luminous stars. From the fact that the systematization in question also exists among the dwarfs Gerasinovič concludes that we cannot neglect the influence of stellar masses on the spectrographic parallaxes,

The largest uncertainty involved in the method is the determination of  $T_{\epsilon}$ . The author made use of the values of the surface intensity given by SEARES which are based on the data of Potsdam and Mount Wilson observers. In this way the following results were found:

G stars K stars log to H log Of H +0",3 0",010-0",020 +0M,4 26 +0,558 20 +0,424 +1 ,6 0,021-0,030 +0,034 24 -0.023+1 .3 14 0 ,031-0 ,060 -0,101 +3,0 43 -0,421+1 ,9 17 0 ,061-0 ,100 10 ~0,230 24 -0,476 +4 ,3 >0 ,100 | -0,383 | +5 ,3 | 18 -0,377 **[** +6 .5

 $\log \mathbb{R}$  clearly depends on the value of  $\pi$  and the same dependence also exists in the F stars. The dependence is partly caused by the well-known selection of

<sup>&</sup>lt;sup>1</sup> Gron Publ, No. 34, p. 60 (1923).

Ap J 55, p 198 (1922)

stars in all parallax-piogramms and partly by a general dependence between M and  $\mathfrak{M}$  A special investigation of the F stars proved that there is no dependence between n and  $\mathfrak{M}$  inside this spectral class.

Using 15 stars with known masses among the Victoria objects Gerasimovič

found the following relation

$$\mathfrak{M}_{\rm calc} = 0.80 \, \mathfrak{M}_{\rm obs}$$

The author points out that the conclusion of Pannekoek that the Cepheids probably have a very small mass cannot be maintained because the method it depends upon only gives the effective gravity, i.e. the gravity diminished by

radiation pressure.

Further on an examination is made with regard to whether the principle of the equipartition of the energy holds good  $\mathfrak{M}V^2$  was computed as follows. At first the space velocity  $V_1$  of a star relatively to the Sun was computed. If  $V_0$  is the velocity of the Sun relatively to the centroid of the stars and K expresses the systematic correction in the radial velocities to be applied to stars of a given spectral class, then

 $\overline{\mathfrak{M} V^2} = \overline{\mathfrak{M} V_1^2} - \overline{\mathfrak{M}} (V_0^2 + K).$ 

For  $V_0$  the value of W W Campell (20 km/sec) was adopted. From his earlier work Gerasimovic adopted K=+3.4 km/sec and +3.0 km/sec for F dwarfs and G giants respectively. For other groups K=0 was assumed. The following results are found

The weighted mean is 3,50, which may be compared with Seares's value 3,57. The good agreement is a fact that speaks strongly in favour of the correctness of the method. The considerable dispersion in  $\log \overline{\mathfrak{M}V^2}$  prevents that quantity being treated as constant for each star.

A detailed investigation of the probable errors of the calculated masses was next undertaken. The following orders of magnitude of the probable error were

found:

7 Prob error 0",010 ±2,5 M 0 ,050 ±0,52 M 0 ,100 ±0,29 M 0 ,200 ±0,19 M

Thus the mass of a giant star cannot claim individual accuracy, but when the parallax exceeds 0",070 the mass will possess some degree of individual accuracy. The masses computed by the aid of the Victoria parallaxes were also compared with the values that resulted from the Mount Wilson and Norman Lockyer parallaxes. The agreement of the data for small and moderate masses appears to be very satisfactory. It is not so good for the larger masses, and values of masses larger than 20 O are probably illusory. The mean masses were computed according to the following summary

	$M < 3^{11},0$	38	$M \ge 3^{\mathcal{H}},0$	n
F stars G stars	3,3 ①	33	1,5	82
	3,6	55	0,9	70
	4,3	54	1,0	26

Next the mass-luminosity iclation was investigated. The curves for the different spectral classes are somewhat different from the theoretical curve of EDDINGION<sup>1</sup>

<sup>&</sup>lt;sup>1</sup> M N 84, p 308 (1924)

This difference cannot be explained by the variation of  $\log MJ$ , but it can be explained by the assumption of a slight variation of the molecular weight during the evolution of the star.

Also the luminosity-density curve was derived on the basis of Bottlinger's photoelectric determinations of the colour indices. A linear relation between log density and absolute magnitude  $M_B$  was found for each spectral class:

Geraeimovič , 
$$\log q = 0.63 \ M_B - 2.17$$
  $\log q = 0.54 \ M_B - 2.52$  Seares ,  $\log q = 0.57 \ M_B - 1.33$   $\log q = 0.57 \ M_B - 2.55$ 

A catalogue of the masses of 71 stars, for which  $\pi > 0'',070$ , is appended to the paper. The mass of Arcturus comes out as 1,6  $\odot$  and that of 61 Cygnl as

2,20 and 3,50 respectively.

224. Colour-Mass-Density Relation. G ABETTI investigated in 1922 the masses and densities as derived from the data of double stars. The parallax-data were mainly based on Mount Wilson parallaxes or proper motion parallaxes according to KAPTEYN'S and VAN RHIJN'S formula. The table summarizes the most important of the results.

	Specin	al class	M.	Diference in	MA	Mass	Descrity	
	A	В		colour index	-124		Double	
Giants {	K2 G3	F0 17		+0=,80±0=,10 +0,22±0,13		15 O	<0,1 © <0,1	9
Intermediate	A2 F3 F7	A4 I78 G4	+2 .5	-0,06±0,04 -0,14±0,07 -0,24±0,09	十1 ,1 ±0 ,4	9 4,4 2,2	0,2 0,3 0,4	10
Dwarfs. , .	G3 G7 IX4	G5 K1 K6	+5 .7	-0 ,07 ± 0 ,04 -0 ,18 ± 0 ,05 -0 ,06 ± 0 ,03		1,5 1,2 1,1	0,5 0,6 0,8	7 7 9

Later on ABETTI has determined the colour indices of the components of 35 double star systems.

ABETTI has also applied the theory of PANNEKOEK for the derivation of stellar masses

225. Vox Zereal's Method. Up to 1921 the stars in the clusters were considered to have equal masses. This year H VON ZRIPHL published his interesting method which is derived from considerations concerning the distribution of molecules of a gaseous mass enclosed in a spherical space. The method can be applied to star clusters where a concentration of massive members has taken place around the centre and to star clouds in the Milky Way and it can certainly also be applied to clusters of anagalactic nebulae (galaxies). The problem of deriving the spatial distribution of stars within stellar clusters was at first attacked by E. C Pickering, who studied the globulars 47 Tucanae, a Centauri and M 13. He proved that the law of apparent distribution of stars, derived from the projected images of the clusters upon photographic plates, was the same for the three objects investigated. He tried to express the law analytically by the formula  $(1-r)^n$ , where r is the distance from centre and s a constant Some years later the problem of finding the spatial distribution from the projected distribution was solved by H. von Zeipel and next year a successful attempt was made by him to apply the results obtained from the dynamical theory of gases to the law of distribution of stars in globular cluster systems.

<sup>&</sup>lt;sup>1</sup> Aco del Lincol Rend 31, 1° Sem, p 359; 2° Sem, p 93 (1922).

Arcetri Pubbi Fasc No 40 (1923)

4 Harv Ann 26, p 213 (1897).

Acc del Lincel Rend 33, p. 554 (1924).

Ann Obs Paris, Méin 25, F (1906).

CR 144, p. 361 (1907)

The idea of treating the distribution of astronomical masses as the distribution of the molecules of a mass of gas can be traced back to Lord Kelvin's and G. H. DARWIN's part in the discussion concerning the meteoric hypothesis by Sir N. LOCKYER. Later on Lord KELVIN also discussed from the point of view of dynamical theory of gas the distribution of stars in our stellar system in relation to its age. Poincarés suggested in 1906 investigations based on the analogies between stellar systems and masses of gases and emphasized the great possibilities for extending our knowledge as to the construction of the Milky Way system. He also pointed out the difference between stellar systems and masses of gas. In the second case the mean free path is small when compared with the dimensions of the molecules but in the first case the mean free path is large in comparison with the dimensions of the stars. In the stellar system a very long time must elapse before a stage of equilibrium is reached and POIN-CARÉ assumed the Milky Way system to have not reached this stage as yet. In the globular clusters the influence of one star on the other is more pronounced and Poincaré suggested that the distribution of stars in clusters obeys the same law as that expressing the distribution of molecules in a mass of gas only subject to its own gravitational force.

The first step in the development of the theory is to compute a spherical distribution from knowledge of a circular one. The photographs give us the number of stars  $\Delta(r)$  per unit of area at the distance r from the centre. These apparent densities must be transformed into space densities D(r). If r is the projected distance,  $\varrho$  the radius vector, and  $l = \sqrt{\varrho^2 - r^2}$ , von Zeipel derives the equation:

$$\Delta(r) = 2\int_{0}^{\sqrt{R^{2}-r^{2}}} D(\varrho) dl,$$

where R is the limiting distance from the centre of the cluster. In order to eliminate dl this relation can also be written:

$$\Delta(r) = 2 \int_{-\sqrt{r}}^{R} \frac{D(\varrho) \varrho d\varrho}{\sqrt{\varrho^{2} - r^{2}}}.$$

Integrating by parts we have:

$$\Delta(r) = 2D(R)\sqrt{R^2 - r^2} - 2\int_{r}^{R} \sqrt{\varrho^2 - r^2}D'(\varrho) d\varrho$$

This equation is differentiated:

$$\Delta'(r) = -2D(R)\frac{r}{\sqrt{R^2-r^2}} + 2r\int_{-\sqrt{\ell^2-r^2}}^{R} \frac{D'(\varrho)\,d\varrho}{\sqrt{\ell^2-r^2}}.$$

Further we multiply with  $\frac{dr}{\sqrt{r^2-r_1^2}}$ , where  $r_1 < R$ , and then the integration between  $r_1$  and R is performed. Then we obtain:

$$\int_{r_1}^{R} \frac{d'(r) dr}{\sqrt{r^2 - r_1^2}} = -D(r) \int_{r_1}^{R} \frac{2r dr}{\sqrt{(R^2 - r^2)(r^2 - r_1^2)}} + 2 \int_{r_1}^{R} \frac{r dr}{\sqrt{r^2 - r_1^2}} \int_{r_1}^{R} \frac{D'(\varrho) d\varrho}{\sqrt{\varrho^2 - r^2}}.$$

<sup>&</sup>lt;sup>1</sup> London Phil Trans 180 A, p. 1 (1889). 
<sup>2</sup> Phil Mag 6th Ser. 2, p. 161 (1901).

<sup>&</sup>lt;sup>3</sup> BSAF 25, p. 153 (1906).
<sup>4</sup> Ann Obs Parls, Mém 25, F (1906).
<sup>5</sup> K Svenska Vet Akad Handl 61, No. 15, p. 109 (1921).

The order of integration is changed in the second integral

$$2\int_{0}^{R}D'(\varrho)\,d\varrho\int_{0}^{\varrho}\sqrt{\frac{r\,dr}{(\varrho^{4}-r^{4})(r^{4}-r^{4})}}$$

Further it is found that

$$\int_{0}^{\frac{2r\,dr}{\sqrt{(q^{\frac{1}{n}}-r^{\frac{n}{n}})(r^{\frac{n}{n}}-r^{\frac{n}{n}})}}=\pi_{\bullet}.$$

Hence.

$$\int_{0}^{R} \frac{d'(r) dr}{\sqrt{r^{2} - r_{1}^{2}}} = -\pi_{0} D(r) + \pi_{0} \int_{0}^{R} D'(q) dq = -\pi_{0} D(r_{1}).$$

Instead of  $r_1$ , r is used and instead of r,  $\varrho$  Then:

$$D(r) = -\pi_0^{-1} \int_{-r}^{R} \frac{d'(q) dq}{\sqrt[r]{q^2 - r^2}} = -\pi_0^{-1} \int_{-r}^{\frac{r}{2}} \frac{d'(\sqrt[r]{r^2 + r^2})}{\sqrt[r]{r^2 + r^2}} dl.$$

Next, von ZEIPEL makes the substitution:

$$p(r) = -\frac{1}{r} \frac{d d(r)}{dr}$$

which gives:

$$D(r) = \pi_0^{-1} \int_0^{\sqrt{p^2-r^2}} \dot{p} \left( \sqrt{p^2+r^2} \right) dl.$$

The star counts give  $A(r) + A_0$ , where  $A_0$  can be presumed to be a constant value due to the foreground and background stars. As can easily be shown, this effect will be eliminated,

The value of p(r) could be computed by the formulae for numerical differentiation, but as according to the above definition of p(r) it is not valid for small values of r, the following expansion into series will be used:

$$\dot{p}(r) = \frac{1}{n_1} \left\{ \frac{1}{288} \left( 28 \, n_1 - 11 \, n_1 + n_2 \right) - \frac{r^2}{1920} \left( 10 \, n_1 - 5 \, n_1 + n_2 \right) \right\},\,$$

where a is the number of stars in the region in question. Finally:

$$D(r) = \frac{\omega}{\kappa_s} \left\{ \sum p \left( \sqrt{r^2 \omega^2 + r^2} \right) - \frac{1}{2} p(r) \right\},\,$$

where  $\omega$  is an interval of l taken sufficiently small and  $l = 0, 1, 2 \dots$  in succession. [The problem of deriving a spherical distribution from a (projected) circular distribution on a plate has been solved more recently from a somewhat different point of view by S. D. Wicksell.]

The dynamical stage of a certain stellar agglomeration at the moment is expressed by the correlation surface of the 7th order:

$$\varphi(x, y, x, x, y, k, \mathfrak{M}, t) dx dy dx dk dy dk d \mathfrak{M}$$
,

where x, y, z are the coordinates and z, y, z the velocities. By applying a method of Gibbs it can be shown that the most probable state is expressed by:

<sup>1</sup> Lund Medd Sar I, No 104 (1924).

where V(r) is the potential of the group and r the distance from the centre Further  $f(r, \mathfrak{M}) dx dy dz d\mathfrak{M}$  is the frequency of stars of mass  $\mathfrak{M}$  and of coordinates x, y, z. Then

$$f(r,\mathfrak{M}) = \iiint_{-\infty}^{+\infty} \varphi \, dx \, dy \, dz$$

and according to the last equation but one which expresses the Maxwellian distribution

$$f(r,\mathfrak{M}) = \beta(\mathfrak{M}) e^{2h\mathfrak{M}V(r)} = \gamma(\mathfrak{M}) [/(r,1)]^{\mathfrak{M}}$$

The function  $\gamma(\mathfrak{M})$  is independent of r and the equation can be written

$$-\log f_{i}(r) = C_{i} + \mathfrak{M}_{i}[-\log/(r)], \qquad i = 1, 2, 3$$

where the subscript i refers to a certain subgroup,  $C_i$  is a constant independent of r, and  $\mathfrak{M}_i$  is the mass of a certain group or the mass-ratio of the group if one of these is selected as unit. The method thus gives the relative masses and not the absolute ones. The theorem of von Zeiffl thus says that for two sub-groups of stars in a stellar agglomeration there is proportionality between the mass-ratios and the logarithms of the spatial densities. The method cannot, of course, be employed when the objects are too few to permit a decent determination of the spatial densities.

VON ZEIPEL and LINDGREN¹ applied the method to the determination of the mass-ratios in Messier 37

As photographic magnitudes were used in von Zeipel's and Lindgren's work a reduction to bolometric magnitudes proved necessary. Such a reduction was made by A Wallenguist<sup>2</sup>, who obtained the following results

Wallfrquist			von	Zpieri & Lindo	ORBN
$\overline{M}_{ m bol}$	Mi/M <sub>9</sub>	71	Muol	M1/M2	11
1 <sup>M</sup> ,0 2 ,2	1,60 ± 0,09 1,00	231 312	1 <sup>M</sup> ,1 2 ,6	1,76	57 795
3 ,2 4 ,1	1,23 ± 0,05 (0,85 ± 0,06)	556 757	4 ,2	0,673	682

The values of the last group are uncertain, as the colour indices have not been observed directly

A Wallenguist<sup>3</sup> has measured the magnitudes of the open clusters M36 by applying the same method as von Zeipel and has also computed the mass-ratios

Mboj	M1/M1	n
-0 <sup>M</sup> ,8	1,57 ± 0,09	46
+1 ,8	1,00	130
+3 ,4	0,67	297

These results cannot be considered as accurate as those in the case of Messiei 37, on account of the paucity of the stars that build up Messiei 36, which makes the derivation of the spatial densities uncertain

A WALLENGUIST has recently applied the method of von Zeipel to the determination of the mass-ratios of special star-groups in Messier 3 The material

<sup>&</sup>lt;sup>1</sup> K Svenska Vet Akad Handl 61, No 15 (1921)

<sup>&</sup>lt;sup>2</sup> Ark Mat Astr Fys 20 A, No 26 (1928), Upsala Medd 36

K Svenska Vet Akad Handl (3) 4, No. 8 (1928), Upsala Medd 32
 B A N 5, p 67 (1929)

consisted of 848 stars in Shapley's and Miss Davis's Catalogue! The stars were divided into four groups, for which the following results were found

Group	Shed .	W/W.	В	von Zimen's theory	Kommuron's	M <sub>bel</sub>
Red "hyporgiants" White "hyporgiants" Ordinary red glants White stars	14*,69	1,297 ± 0,031	268	3,88 ()	3,90 @	-0 <sup>x</sup> ,31
	15 ,65	1,000	267	2,99 (0)	2,98 O	+0 ,65
	16 ,66	0,898 ± 0,117	197	2,69 (0)	2,10 O	+1 ,66
	17 ,09	0,620 ± 0,123	122	1,86 (0)	1,86 O	+2 ,09

Mo, the mass of the white "hyperglants", has been selected as unit

In order to reduce the determined mass-ratios into absolute masses the parallax of the cluster must be known As the most probable value of the parallux  $\pi = 0^{\prime\prime},00010$  is accepted. This leads to the numbers in the last columns. If SHAPLKY's value for the M of the cluster type variables had been used the four values of M would have been 5,480, 4,220, 3,790, and 2,620 respectivoly.

226. The Method of Freuedich and Hausanen. Independently of von ZEIFEL, E FERUNDLICH and W. HEISKANEN have developed an analogous method According to Shapley there seems to exist a "galactic" plane in the globular clusters in the sense that only the brightest stars have a spherical distribution, whereas the fainter stars show an elliptical distribution. Let IR. IR. be the ratio of the total mass of the elliptically distributed stars to the total mass of the spherically distributed stars, and let a and b be the axes of the ellipsoidally distributed stars and s' a measure of the ellipticity of the equipotential surfaces, then

$$\varepsilon'\left[1+\frac{\mathfrak{M}_{\bullet}}{\mathfrak{M}_{\bullet}}\left(1+\frac{3}{5}\frac{b^{2}\lambda^{2}}{a^{2}}\right)\right]=\frac{3}{10}\frac{\mathfrak{M}_{\bullet}}{\mathfrak{M}_{\bullet}}\frac{b^{2}\lambda^{2}}{a^{2}},\quad\text{where}\quad\lambda=\frac{a^{2}-b^{2}}{b^{2}}.$$

If the equipotential surfaces cut the equator at the distance a and the polar axis at the distance r, then  $s' = \frac{a}{r} - 1$ 

According to H. C. PLUMMER' and VON ZEIPEL' the density in the cluster increases ~ 74. Applying the alightly modified formula to Shapliny's material in M13 gives M./M. :, 0,5 This means that the mass of the spherically distributed stars, which amount to only 0,01 of the total number, should be at least two thirds of the total mass of the cluster. This will make the mean mass of the apherically distributed K and M giants 500 0, which seems incredible authors then repented Shapley's star counts on the basis of his star catalogue. and that of LUDRNDORFF It was found that there were such individual deviations in the distribution of the different classes of stars that the authors think it is doubtful whether the above formula can be applied. They therefore turned their attention to investigating the relative concentration towards the centre of the different classes and to applying the theory of gases. If q<sub>i</sub> is the number of molecules in unit space of a gas of atomic weight  $\mu_i$ , V the gravitational potential, and h and go certain parameters depending on the temperature and density at the centre, we have the equation

<sup>2</sup> f Phys 14, p. 226 (1923).

<sup>1</sup> Mt Wilson Contr No. 176 (1920).

M N 71, p 460 (1911), 76, p 107 (1915).

M N 71, p 460 (1911), 76, p 107 (1915).

K Svenska Vet Akad Handl 51, No. 5 (1913)

Potedam Publ 15, No 50 (1905)

The theory has been applied to the clusters M3 and M13. The colour male r corresponding to the A and F stars have been taken together to form one groups those corresponding to G, K, and M stars to form another (consider two special elements at distances  $r_1$  and  $r_2$  from the centre and attribute the subscripts  $r_1$  and  $r_2$  from the centre and attribute the subscripts  $r_1$  and  $r_2$  from the centre and attribute the subscripts  $r_1$  and  $r_2$  from the centre and attribute the subscripts  $r_1$  and  $r_2$  from the centre and attribute the subscripts  $r_2$  and  $r_3$  from the centre and attribute the subscripts  $r_3$  and  $r_4$  from the centre and attribute the subscripts  $r_4$  and  $r_5$  from the centre and attribute the subscripts  $r_4$  and  $r_5$  from the centre and attribute the subscripts  $r_5$  from the centre and  $r_5$ 

$$\frac{\mathfrak{M}_{A}}{\mathfrak{M}_{K}} = \frac{\log \varrho_{1}^{1} - \log \varrho_{1}^{0}}{\log \varrho_{K}^{1} - \log \varrho_{1}^{0}},$$

$$\varrho_{A}^{1} = \varrho_{0}^{(A)1} \cdot e^{-2h} \mathfrak{M}_{A} V_{1}, \quad \varrho_{1}^{0} = \varrho_{0}^{(A)2} \cdot e^{-2h} \mathfrak{M}_{A} V_{1},$$

$$\varrho_{K}^{1} = \varrho_{0}^{(K)1} \cdot e^{-2h} \mathfrak{M}_{K} V_{1}, \quad \varrho_{A}^{0} = \varrho_{0}^{(h)2} \cdot e^{-2h} \mathfrak{M}_{K} V_{2},$$

where

From the observed number of stars on the plates the numbers in space we it derived according to you Zeipel's formula. The following results were derived

Distance	M13	M3	Distance	Mis	M3
from centre	Ma/Ma	M <sub>K</sub> /M <sub>A</sub>	from centre	Wa/Wi	WA/W (
2' 3' 4'	1,420 1,135 1,240	1,761 1,865 1,518	5′ 6′	1,215	1,326

227. Martens's Method!. In order to obtain a handy expression of the exhaustion of the potential energy of a stellar cluster Martins assumes that the effects of collisions and passages are negligible when compared with the effect of the gravitation from the cluster. Further it is assumed that the measures of kinetic energy per degree of freedom are constant for all degrees a freedom and independent of the coordinates of position. These two assumptions mean in other words the assumption of dynamical equilibrium and equipart tion of energy.

MARTENS then performs a closer examination on basis of JIANS'S WOFF "The Dynamical Theory of Gases", in order to find out if the two assumptions are concordant

The stellar system under consideration consists of n stars having 3n coordinates  $q_1 = q_{3n}$ . Instead of the velocities  $dq_i dt$ , the variables  $p_i$  are introduces

The life history of the stellar system is represented by a certain curve the 6n-dimensional space determined by the rectangular coordinates of position and velocities

Next a great number of stellar systems is considered, so selected that  $\mathbf{t}$ 1 initial values of the 6n quantities  $q_i$  and  $p_i$  are so near each other that the  $\mathbf{t}$  presentative points can be treated as forming a continuous medium. The number of points per unit of 6n-dimensional volume or the density of this medium  $\mathbf{i} = \mathbf{t}$  is the time, the equation of continuity takes the form

$$\frac{\partial r}{\partial t} + \sum_{i=1}^{3n} \left\{ \frac{\partial}{\partial p_i} \left( r \frac{d p_i}{d i} \right) + \frac{\partial}{\partial q_i} \left( r \frac{d q_i}{d i} \right) \right\} = 0.$$

Combining this equation with the equations of motion and taking Dr/ as representing the increase in  $\tau$  as we follow the group of points in its motion. JEANS<sup>2</sup> has shown that

$$\frac{D\tau}{Dt} = \tau \sum_{i=1}^{8n} \frac{\partial^2 I_i}{\partial q_i \partial p_i},$$

The Dynamical Theory of Gases Fourth Edition Cambridge 1925

<sup>&</sup>lt;sup>1</sup> A Research on the Spherical Dynamical Equilibrium-Distribution of Stars Unequal Masses Göteborg 1928

where  $\frac{dE}{dt} = -2F$ , E being the total kinetic energy of the system and 2F being a quadratic function of the velocities and giving the rate of dissipation of energy. Jeans has shown that the right member of this equation is always  $\ge 0$ , and only = 0 if F = 0. It then follows as a consequence of collisions between stars that mechanical energy is transformed into heat and that the points representing different initial configurations of the stellar systems are crowded together and that, independently of the initial states, the final states of the stellar systems are the same

It can be shown on basis of J Ohlsson's investigations that the effect of collisions and passages can be fully neglected. Ohlsson thus estimates the time of relaxation measuring the rate at which the Galaxy as an effect of collisions approaches to equilibrium to be of the order of 10<sup>31</sup> years. The corresponding time as an effect of passages is found to be of the order of 10<sup>32</sup> years. These quantities are certainly much smaller in globular and open clusters but still the passages and then a fortiori the collisions have been neglected in Martins's

work

Then: F = 0 and  $D\tau/Dt = 0$  (Liouville's theorem)

A part of the stellar system consisting of N stars is then considered. The stars have not equal masses but can be ordered into  $\nu$  groups. The stars  $N_j$  in each group have the same mass  $\mathfrak{M}_j$ . Hence,

$$\sum_{i=1}^{r} N_i = N.$$

The stars are assumed to be material points. Every star then possesses three degrees of freedom and its state is determined by 6 quantities:

The space containing the N points is divided into \*\* equal elements of volume. The state of the stars is then statistically determined by certain quantities  $a_{ij}$ , giving the number of stars of mass  $\mathfrak{R}_i$  contained in the ith element of volume We have then:

 $\sum_{j=1}^{n} a_{ij} = N_j. \qquad (j=1,2,\ldots,\nu)$ 

Similarly to this distribution, called A by Jeans, there exists another distribution B, determined by the numbers  $b_{ij}$ , and so on. The task is to determine the  $a_{ij}$  in such a way that distribution A becomes the most probably one.

By variation of the last equations above the following - conditions are

found:

 $\sum_{i=1}^{n} \partial a_{ij} = 0. \qquad (j = 1, \ldots, r) \qquad (a)$ 

The  $N_j$  stars can be permutated in  $\frac{N_j!}{a_{ij}! \dots a_{ij}!}$  ways without changing the distribution A. The most probable distribution is the one that makes the volume containing the points of distribution A a maximum. This leads to the equations of condition:

$$\sum_{i=1}^{r} \sum_{i=1}^{n} \left[ \log \frac{n a_{ij}}{N_{j}} + 1 + \frac{1}{2 a_{ij}} \right] \delta a_{ij} = 0.$$
 (b)

Finally using the equation E = constant and taking:

$$\frac{\partial E}{\partial a_{ij}} = a_{ij}$$

<sup>1</sup> Lund Medd Ser, II, No. 48 (1927).

and disregarding terms of higher order of  $\delta a_{ij}$  it is found by variation from the energy equation

 $\sum_{i=1}^{i} \sum_{i=1}^{n} \varepsilon_{ij} \, \delta \, \alpha_{ij} = 0 \tag{c}$ 

The set of variation-equations (a) is multiplied by the arbitrary factors  $l_j$  and the last one (c) by a factor m. The expressions are then added to the equation (b). It is then found that the  $a_{ij}$  have to satisfy the equations

$$\log \frac{na_{ij}}{N_j} + 1 + \frac{1}{2a_{ij}} + l_j + me_{ij} = 0$$

The  $a_{ij}$  are supposed to be so great that  $\frac{1}{2a_{ij}}$  can be neglected. Further it is assumed that  $e_{ij}$  is independent of  $a_{ij}$ , although dependent of the other  $a_{ij}$ . The equation is then solved into.

 $a_{i,1} = \frac{N_1}{n} e^{-(1+l_i)-m\varepsilon_{i,1}}$ 

Introduce a function  $\tau_j$  so that  $\tau_j d\phi_{j1} d\phi_{j2} d\phi_{j3} d\phi_{j4} d\phi_{j5} d\phi_{j6}$  gives the number of stars within the limits  $d\phi_{jk}$ , where k=4 6, and whose masses are  $\mathfrak{M}_j$ 

Then  $\tau_1$  is proportional to  $a_{i1}$  and we can write

$$\tau_1 = C_1 e^{-m \, \epsilon_1},$$

where  $C_1$  is a constant and  $\varepsilon_1$  a smooth function of the values  $\varepsilon_{i1}$   $\varepsilon_1$  is assumed to have the form

$$\varepsilon_1 = \frac{1}{2} \beta_{11} \varphi_{11}^2 + \frac{1}{2} \beta_{12} \varphi_{12}^2 + \frac{1}{2} \beta_{13} \varphi_{13}^2 + \frac{1}{2} (\varphi_{11}, \varphi_{15}, \varphi_{10})$$

Then

 $\tau_1 d\varphi_{11} d\varphi_{12} d\varphi_{13} d\varphi_{14} d\varphi_{15} d\varphi_{16} = C_1 \left( e^{-\frac{1}{4} m \beta_{11} \varphi_{11}^2} d\varphi_{11} \right) ... \left( e^{-m I_1} d\varphi_{11} d\varphi_{15} d\varphi_{16} \right).$ 

This shows that the distributions of the coordinates are independent of one another

The mean value of the contribution of  $\varphi_{11}$  to the energy is

$$\frac{1}{2}\beta_{11}\varphi_{11}^2 = \frac{1}{2m}, \text{ and also } \frac{1}{2}\beta_{12}\varphi_{12}^3 = \frac{1}{2}\beta_{13}\varphi_{13}^2 = \frac{1}{2m}$$

It can also be shown that

$$\frac{1}{2} \mathfrak{M}_{j} \left( \frac{dq_{jk}}{d} \right)^{2} = \frac{1}{2m} \qquad (k = 1, 2, 3, j = 1, ..., \nu)$$

which expresses the law of equipartition of energy

The assumption that the  $\varepsilon_{ij}$  are independent of  $a_{ij}$  is then made subject to a special examination on basis of Charlier's<sup>1</sup>, Jeans's<sup>2</sup> and Ohi ston's<sup>3</sup> work and it is found that the assumption is justified when dealing with stellar systems and that equipartition of energy exists in a state of dynamical equilibrium. The author emphasizes the extreme difficulties presenting themselves when a scarch is made for the mechanism resulting in the equipartition of energy when collisions and passages are neglected. He quotes a postulate formulated by Charlier "Each population of individuals approaches asymptotically that state which can be proved to possess the greatest probability."

<sup>1</sup> Lund Medd Ser II, No 16 (1917)

4 Publ ASP 37, p 125 (1925)

<sup>&</sup>lt;sup>2</sup> MN 76, p 70, 555 (1915—16), Problems of Cosmogony and Stellar Dynamics Cambridge 1919

<sup>3</sup> Lund Medd Ser II, No 48 (1927) Also Dissertation Lund

MARTENS finds that if the equations which determine the most probable distribution of the positional coordinates are solved, the  $a_{ij}$  will be found to be independent of i, which means that the stars would be uniformly distributed over the whole space. But the task is not to seek for the most probable distribution among all possible ones but for the most probable distribution among those having a certain value of their potential energy. This is proved by applying the theorem of the virial i

If  $q_k$  are the rectilinear coordinates of N stars and  $Q_k$  the components of the acting forces in the same direction the equations of motion will be

$$\Re_b \frac{d^3q_k}{dt^3} = Q_b. \qquad (k = 1, \dots, N)$$

We designate by S the summation over all three directions of coordinates, then  $S \geq \mathbb{R}_k q_k^2$  is the moment of inertia of the system, and, as we are seeking stationary distributions, we write

$$\frac{d^3}{dt^3}S\sum_{k=1}^{H}\mathfrak{M}_kq_k^3=S\sum_{k=1}^{H}\mathfrak{M}_k\frac{d^3}{dt^3}q_k^2=0,$$

the bar over an expression denoting an average over a long time. The virial  $\vec{V}$  of CLAUSIUS is then found to be:

$$\vec{V} = -\frac{1}{1} S \sum_{k=1}^{H} q_k Q_k.$$

The following deductions are made on the assumption that the system is spherically distributed. The radius of the sphere is called R. It follows from the assumption of a limiting radius that the total gravitational force of all stars outside this sphere is zero. Thus only the forces due to the stars inside the sphere shall be taken into account. On another hand a number of stars will escape from the sphere at a certain moment, but these lesses are counterbalanced by outside stars passing into the sphere and as it is assumed that the distribution is stationary, both outside and inside the limiting sphere, the counterbalancing effect appears to be more or less the same as if the outgoing stars met an elastic wall and were reflected by it. Of course, the identity is not kept after the imaginary reflection; it is another star that pursues the broken orbit. The expression of potential energy is not changed except in the immediate neighbourhood of the limiting sphere and this applies also to the law of distribution which is a function of the potential energy. These circumstances overcome the principal difficulties presented by the escaping and invading stars.

If N stars move under the sole influence of their gravitational interactions it follows that a simple relation exists between the virial V and the exhaustion Q of potential energy of the forces, which has the form:

$$Q = \frac{1}{2} \sum_{i=1}^{N} \sum_{i=1}^{N} ' \times \mathbb{R}_b \, \mathbb{R}_i \, \frac{1}{\left[S(q_i - q_b)^2\right]^2}.$$

The apostrophe by the second  $\sum$  sign means that during the summation k = l must be excluded. \*\* is a numerical constant depending on the units used.

<sup>&</sup>lt;sup>1</sup> The virial is the sum of the attractions between all the pairs of particles of a system, each multiplied by the distance between the pair

Comparing the expressions for V and  $\Omega$  it is found in accordance with Edding-

$$V = -\frac{1}{2} S \sum_{k=1}^{N} q_{k} \sum_{l=1}^{N} Q_{k \, l} = \frac{1}{4} \sum_{k=1}^{N} \sum_{l=1}^{N} \kappa \, \mathfrak{M}_{k} \, \mathfrak{M}_{l} \, \frac{1}{[S(q_{l} - q_{k})^{2}]^{\frac{1}{2}}} = \frac{1}{2} \, \Omega$$

Applying the virial-theorem earlier quoted it follows that

$$T - \frac{1}{2}\Omega = 0$$

The equations of motion possess the wellknown integral

$$-\frac{1}{2}h = T - \Omega,$$

where h is an arbitrary constant. Thus

$$Q = h$$
 (d)

Next  $\Omega$  will be expressed as a function of the quantities  $a_{ij}$ . The expression for the exhaustion of potential energy can be written:

$$\Omega = \sum_{k=1}^{N} \sum_{l=1}^{k-1} \kappa \mathfrak{M}_k \mathfrak{M}_l \frac{1}{[S(q_l - q_k)^2]^{\frac{1}{2}}}$$

if the indices k are chosen in such a manner that  $Sq_k^2 < Sq_{k+1}^2$ . The neglection of irregular forces permits to substitute for the attraction of a number of discrete stars the attraction of a homogeneous sphere having the same mass as the sum of the masses of the discrete stars. The terms expressing the exhaustion of potential energy of attraction on the mass  $\mathfrak{M}_s$ ,  $\mathfrak{M}_s \sum_{i=1}^{s-1} \mathfrak{M}_l [S(q_l-q_s)^2]^{-\frac{1}{2}}$  are thus substituted by the expression  $\mathfrak{M}_s[Sq_s^2]^{-\frac{1}{2}}\sum_{l=1}^{s-1}\mu_l$ 

In the distribution A determined by the numbers  $a_{ij}$  the stars having the same index i are situated within a spherical shell. The harmonic mean distance of these stars from the centre is  $r_s$ . The stars in the element s contribute to the exhaustion of potential energy by a quantity

$$x \frac{\sum_{j=1}^{r} a_{ij} \, \mathfrak{M}_{j}}{r_{i}} \sum_{j=1}^{s-1} \sum_{j=1}^{1} a_{ij} \, \mathfrak{M}_{j}$$

and observing (d) we obtain:

$$\Omega = \varkappa \sum_{s=1}^{n} \frac{\sum_{j=1}^{j} a_{sj} \, \mathfrak{M}_{j}}{r_{s}} \sum_{i=1}^{s-1} \sum_{j=1}^{r} a_{ij} \, \mathfrak{M}_{j} = h. \tag{e}$$

The variations  $\delta a_{ij}$  are to be connected by the condition

$$\varkappa \sum_{s=1}^{n} \sum_{j=1}^{\nu} \delta a_{sj} \left\{ \frac{\mathfrak{M}_{j}}{r_{s}} \sum_{i=1}^{s-1} \sum_{j=1}^{\nu} a_{ij} \mathfrak{M}_{j} + \mathfrak{M}_{j} \sum_{i=s+1}^{n-1} \frac{\sum_{j=1}^{j} a_{ij} \mathfrak{M}_{j}}{r_{i}} \right\} = 0.$$

Further is

$$\sum_{j=1}^{r} \sum_{k=1}^{n} \delta a_{ij} \left\{ \log \frac{n \, a_{ij}}{N_j} + 1 + \frac{1}{2 \, a_{ij}} \right\} = 0$$

and '

$$\sum_{i=1}^n \delta \, a_{ij} = 0$$

<sup>1</sup> M N 76, P 525 (1916)

The  $a_{ij}$  are then found by using the method of indetermined multiphers Neglecting the term  $1/2a_{ij}$  the following set of equations is found.

$$\log \frac{n \, a_{ij}}{N_j} + 1 + l_j + m \times \mathfrak{M}_j \left( \frac{1}{\tau_i} \sum_{i=1}^{s-1} \sum_{j=1}^{\tau} a_{ij} \, \mathfrak{M}_j + \sum_{i=s+1}^{s-1} \frac{\sum_{j=1}^{s} a_{ij} \, \mathfrak{M}_j}{\tau_i} \right) = 0, \quad (f)$$

where  $l_j$  and m are arbitrary factors. To these  $s \cdot j$  equations are joined the j equations  $\sum_{i=1}^{n} a_{ij} = N_j$  and equation (e) above. We have thus  $s \cdot j + j + 1$  equations to determine the  $s \cdot j + j + 1$  unknown quantities  $a_{2j}$ ,  $l_j$  and m.

The radius of the sphere enclosing the stars in the system considered is R. If W is the volume then the volume of each cell is W/n and  $na_{ij}/W$  gives the density of stars of mass  $\mathfrak{M}_i$  at the distance  $r_i$  from the centre Further is introduced:

1,(1) = #4,1

If  $r_{s+1/s}$  is the radius of the spherical surface separating the cell s from the cell s+1 we have.

$$\frac{W}{n} = \int_{r_{n-1}}^{r_{n+1}} 4\pi_n r^n dr \quad \text{and} \quad a_{nj} = f_j(r_j) \int_{r_{n-1}}^{r_{n+1}} 4\pi_n r^n dr$$

On considering the quantities  $f_{j}(r_{r})$  as being continuous functions of r and assuming the calls to be thin we may put

$$a_{ij} = \int_{\tau_{i-1}}^{\tau_{i+1}} 4\pi_i \tau^a /_j(\tau) d\tau$$

Then the equations (f) are transformed following the same assumption. Applying the Laplacian operator  $\nabla^2$  to the expressions (f) and dropping the index s it is finally found:

$$\nabla^{2}\left[-\frac{1}{m + \mathbb{R}^{2}}\log\left(\frac{W}{N_{j}}e^{1+k_{j}}f_{j}(r)\right)\right] = -4\pi_{0}\sum_{i=1}^{r}\mathbb{R}^{2}_{i}f_{j}(r). \qquad (j = 1, \ldots, r)$$

This gives the equation

$$\frac{d^{2} \log f_{j}(r)}{dr^{2}} + \frac{2}{r} \frac{d \log f_{j}(r)}{dr} = 4\pi_{e} m \kappa \sum_{i=1}^{r} \mathfrak{M}_{j} f_{j}(r) \qquad (j = 1, \dots, r)$$
 (g)

Each one of these equations contains in its left member one of the unknown functions but in its right member all the unknown functions. By considering the equations for the potentials of gravitation it is found that:

$$\frac{1}{m \times \mathfrak{M}_{i}} \left( \log \frac{W}{N_{i}} e^{1+I_{i}} f_{i}(r) \right) = \frac{1}{m \times \mathfrak{M}_{j}} \left( \log \frac{W}{N_{j}} e^{1+I_{j}} f_{j}(r) \right)$$

$$\left( \frac{W}{N_{i}} e^{1+I_{i}} f_{i}(r) \right)^{1/m_{i}} = \left( \frac{W}{N_{j}} e^{1+I_{j}} f_{j}(r) \right)^{1/m_{j}},$$
(h)

or:

which are the relations used by von ZEIPEL and LINDGERN.

Introducing'

$$C_{ij} = \frac{N_i}{W} \left( \frac{W}{N_i} \right)^{\frac{N_i}{N_i}} e^{-\Omega + i\lambda i} + \frac{N_i}{W_i} \Omega + i\lambda$$
$$f_i(r) \approx C_{ij} [f_i(r)]^{\frac{N_i}{N_i}}$$

we have.

	۵	+0 007 +0 009 +0,011 -0,038
	log/3 calc	8 306—10 8,255 8,143 7,998
42	log f3 obs	8,313—10 8,264 8,154 7,960
	٥	+0 013 +0 021 +0,001 -0,008
	logfacale	\$ 888 - 10 8,861 8,789 8,692 8,484 8,212
4	log foobs	8,901—10 8,532 8,802 8,693 8,476 8,161
	٥	-0,009 +0,040 +0,046 -0,046 -0,019
	logfente	9,613—10 9,572 9,465 9,321 9,012 8,608
	logfobs	9,604—10 9,581 9,505 9,367 8,993 8,526
	∢	+0,079 +0,100 +0,079 -0,084 -0,168
	log/1 cale	9,154—10 9,082 8,893 8,640 8 095 7,383
	log 1, obs	9,233—10 9,182 8,972 8,556 7,927 7,350
	logr	0,000 0,000 0,602 0 954 1,800

and the differential equation then becomes

$$\frac{d^{2} \log f_{j}(r)}{dr^{2}} + \frac{2}{r} \frac{d \log f_{j}(r)}{dr} = 4\pi_{o} \times m \, \mathfrak{M}_{j} \sum_{i=1}^{r} \mathfrak{M}_{i} C_{ij} [f_{j}(r)]^{\mathfrak{M}_{i}/\mathfrak{M}_{j}},$$

where both the membra only contain one of the unknown functions. In order to find all functions of distribution we need only to solve one of the  $\nu$  equations. The other  $\nu-1$  functions are then found by aid of the relations (h).

For the application of this theory to a cluster there are required observations on functions of distribution of different groups of stars, classified according to attributes correlated to the masses of the stars. As such observations of globular clusters were not accessible Markens compared the results of his theory with the distributions in the open cluster M37 (NGC 2099) observed by YON ZEIPL and LINDGREN These authors divided the stars of M 37 according to their magnitudes and colour indices into four groups, p, q, u, w The p-stars were interpreted as g-grants, the q-stars as b- and q-stars, the q-stars as /-dwarfs and the w-stars as g-dwarfs From then observations von ZFI-PEL and LINDGREN have calculated the distributions faobs in space of the four types of stars given in the adjoining table Martens compared these observed distributions with those calculated (/1 calc /guale) on the supposition that the cluster is in its most probable state

It is obvious from the distribution of the differences A = obs—calc that the value of m determined for different groups would be about the same This is an indication of equipartition of energy on the different masses. Further the differences show that the stars are more concentrated to the centre of the cluster than is required by the calculated distribution. This phenomenon, well-known for distributions in globular clusters, disregarding unequalities of masses of the stars, is usually interpreted as displaying that the clusters are built up in adiabatic equilibrium instead of in isothermic According to the theory here developed there is, however, another possible explanation. Doubtless there are within the cluster stars that are not lummous enough to be observed. These stars do not influence the observed distributions, but as they contribute to the potential of the cluster they are able to affect the calculated distributions, as has been shown on the preceding pages, in a direction to diminish and perhaps abolish the differences of the table

Among other results found by Mariens the fact may be mentioned that if equipartition has taken place in a stellar cluster then the most probable state of distribution is expressed by the Maxwellian law Such a system has no limitation in space or, in other words, its radius is infinite. If the mass-ratios exceed 3/2 within such a system, the number of the smaller masses must be infinite, whereas the number of the greater masses is finite. It seems that

the adiabatic distribution in globular clusters can be explained by the assumption that within these objects the mass-distribution is the most probable one

228. Recent Work Concerning Masses of Spectroscopic Binaries. It is only four and a half decades since the first discovery of a spectroscopic binary was anounced. At present orbital elements are known for some 250 systems. When both spectra have been observed and also the system is an eclipsing binary, we obtain complete and, in most cases, very accurate knowledge of the components. When the system is not an eclipsing binary, but both spectra are known, we get the minimum values of the masses, because the orbital determination gives the quantities  $M_s \sin^2 i$  and  $M_B \sin^2 i$ . Reasonable assumptions concerning the value of  $\sin^2 i$  can also be made and thus our knowledge of the mean value of  $M_s$  for certain groups of binaries can be considerably advanced

The third case, i.e. when only the spectrum of one of the components is registered, presents several difficulties as far as the determination of the mass is concerned. This case is certainly the most common one. As soon as the components in a double star system differ two magnitudes or more, the chances are very small that both spectra will appear on the plates. The observations of a spectroscopic binary give in the case of one spectrum the so-called mass-function, f = 30% ain f = 30%, which can be written

$$(\mathfrak{M}_A + \mathfrak{M}_B) \sin^2 i = [3,01642 - 10] K_A^4 \left(1 + \frac{\mathfrak{M}_A}{\mathfrak{M}_B}\right)^3 P \left(1 - s^4\right)^{\frac{1}{4}}$$

where  $K_A$  is the semi-amplitude of the velocity variation for  $\mathfrak{M}_A$  and P the

period in days

R G. Attree has expressed doubts in his book "The Binary Stars", with regard to whether the mass-function can give any information concerning the masses of the stars. Generally the value  $K_A$  or a corresponding expression has been used and then, of course, the range is considerable. It is fair to use  $K_A$  in order to get a quantity that is proportional to the cube root of the mass, because in direct determinations of stellar masses we cannot get more than a fair knowledge of  $(\mathfrak{M}_A + \mathfrak{M}_B)^{\dagger}$  from our best determinations of stellar parallaxes. The use of  $K_A$  has also been recommended by Otro Struve and others.

STRUVE has assumed:

$$K_A = CP^{-\frac{1}{2}}$$

which is justifiable for certain groups of stars. The curve combining P and K corresponds very nearly to the equation  $K = CP^{-\frac{1}{2}}$  for P = 9 years to P = 2,45 days, (log C = 2,0695). LUDENDORFF has reached a number of important conclusions which are given already in ciph, 215 of this chapter.

Extensive use of STRUVE's formula has been made by BRER in his paper, "Zur Charakterisierung der spektroskopischen Doppelsterne". This extensive and valuable monograph cannot be reviewed here excepting from the point of view

of determination of stellar masses

From 434 objects BEER finds the value  $KP^{\frac{1}{2}} = 125,1$ . He makes use of the above relation for a discussion of the probability of a certain group of stars exhibiting variable radial valocities being binaries (c. g. the Cepheids) and classifies the real binaries according to the characteristics of the P, K-curves.

Ap J 60, p. 167 (1924)
 Barlin-Babaisbarg Veröli V, H 6 (1927)

BEER has collected 88 pairs showing both spectra, and finds the following frequencies of the values  $(\mathfrak{M}_A + \mathfrak{M}_B) \sin^3 i$ 

$(\mathfrak{M}_A + \mathfrak{M}_B) \sin^3 i$	St	(M) (+101) sin* ;	n	(9)24 + 902B) stn# #	71
>1000	2	8 -90	_	3,0-3,50	3
50-100	1	78	2	2,5-3,0	13
40- 50	-	6 - 7	-	2,0-2,5	1.1
30 40	3	5 - 6	5	1,5-2,0	1.1
20- 30	5	4,5- 5,0	_	1,0-1,5	8
10- 20	4	4,0~ 4,5	4	0,5-1,0	G
9 10	6	3,5-4,0	3	<0,5	1

This table seems to lend some support to the theory of III I LI RICH assuming the existence of preferential mass values (cf ciph 229)

The relation between mass and spectral class is illustrated in the following summary:

Spectrat class	1984 sin* #	MB sing s	Range for (MA + MA) sin* t	13
06-B4 B5-A4 A5-F4 F5-G4 G5-K4	13,180 2,71 1,80 1,01 0,87	10,50 ① 1,73 1,24 0,89 0,68	139 -2,600 26,4 -0,21 13,4 -0,52 3,37-0,87 2,10-1,05	21 30 18 15

In 33 cases the individual masses were known. By assuming  $\sin^3 i == 0.667$  the following mean values were found

Spectral class	$\mathfrak{M}_A + \mathfrak{M}_B$	11	$[\mathfrak{M}_A + \mathfrak{M}_B]$	Ħ	Adopted
O6B4	17,17 ①	9	20,28 ⊙	10	18.8
B5-B9	10,15	4	10,64	5	10,4
A0-A4	4,47	7	3,53	14	3,8
A5-F4	2,70	4	3,00	12	2,9
$F_5-G_4$	1,42	7	3,54	8	2,6
G5-K4	1,94	2	2,25	1	2,0

The values  $\overline{\mathfrak{M}_A+\mathfrak{M}_B}$  are the mean values derived directly from known inclinations (eclipsing binaries), whereas  $[\overline{\mathfrak{M}_A+\mathfrak{M}_B}]$  are the means derived from the above assumption as to the mean value of  $\sin^3\imath$ .

The group of stars later than F0 consists of 12 giants and 17 dwarfs No systematic difference with regard to the mean masses can be found which is contrary to what is the case when the masses of visual binaries are derived:

Spectral	G	lants	Dwarfs			
olass	(M)A+MB) sln2 ;	WA+WA	13	(MA+MB) sin's	MA + Win	11
F0-F4 F5-G4 G5-K4	1,90 O 2,38	2,85 O 3,57	7 5	2,34 O 1,69 1,55	3,51 ⊙ 2,53 2,32	4 10 3

The mass-ratios  $\mathfrak{M}_B/\mathfrak{M}_A$  have a mean value of 0,75 The distribution with regard to spectral class is as follows

<sup>&</sup>lt;sup>1</sup> AN 220, p 249 (1924)

Speciful	_	Mean				
	0,11-0,30	0,510,50	0,51-0,70	0,71-0,90	0,91-1,00	mar-cargo
06-B4 B5-A4 A5-P5 F5-G4	4	3 4 1 2	462	7 9 7 5	4 7 8 6	0,74 0,68 0,81 0,83
G5-K4			1	2	_	0,76
Sum	5	10	13	30	25	

A tendency of  $\mathbb{R}_n/\mathbb{R}_A$  to increase in the course of evolution seems to be present, but is not very pronounced.

There seems to be some relation between MR/MA and (MA + MR) sin's

as follows:

観点能力	(前4十版在) sint i		Wa/Wa	(D(1+112) acr?	•
0,32	7,15	10	0,86	5,09	10
0.52	4,37	10	0,89	6,53	10
U, <b>G</b> 9	7.54	10	0,95	4,38	10
0,79	3,68	10	0,99	5,01	10

The dispersion within the individual groups is considerable and the general

relation cannot be established at present.

BEER uses the quantity  $f^* = \mathbb{R}_R(\mathbb{R}_R + \mathbb{R}_A)^{-1} \sin i$  and divides the material into binaries showing one spectrum (n=151) and two spectra (n=93). Periods of  $1000^d$  or more have to be excluded, as has been pointed out by Ludendorff, as they are not comparable with short periodic systems on account of the very nature of the function f. The following correlation surface is found for the remaining 233 systems.

1	15				_			_					_
Spectral State	17											10 lo<0,10 001 bn<0,001	Section
O6-B4	ono two	4 8	1 4	3	3 2	2 2	1 3	3	3	4	3	5	32 19
B5-A4	one two	2 2	=	1	3	4	3 12	4	10 [	8	7	_	38 34
A5 F4	one two	1	_	1	2	•	4	-3	4 2	2	_5	_	21 19
F5~ G4	two	=	_	1	2	3	5	4 2	4	2	<b>3</b>	1	18
G5~K4	ono	] =	=	1	=	3	2	4	6		-	1	22
K5-M7	one two	=	=	=	=	=	1	1	=			=_	3
Sum	one	11	1 4	3	5	10	17	19	27	25 7	18	9	143

BEER has investigated the mean errors in the mean values of f and confirms the conclusion of LUDENDORFF that within each spectral class the mean value of f is practically constant and thus very suitable for a derivation of the mean value of the mass.

The ratio of the masses of B stars and A stars (including A stars and the following classes) is found to be 3,42 and 5,80 for stars showing one and two spectra respectively. A direct computation from the direct data which avoids using f gives 5,48 for the second group

The material concerning the spectroscopic binaries is given in J II Moore's "Third Catalogue of Spectroscopic Binary Stars" (which includes the material to July 1st, 1924) in Lick Bull No 355 (1924) and in Beley's paper (which includes the material to March 1927). On pages 122—124 Beer gives corrections and additions to the Third Catalogue. The student of spectroscopic binaries is recommended to consult these two sources, which give a complete collection of the material up to 1927, whenever investigations of a general nature concerning these objects are to be undertaken.

The correlation between the frequencies of one and two spectra is comparatively low. An analysis of the two frequencies has not yet been undertaken, but would undoubtedly reveal several points of interest.

BEER forms the equation

$$\left( \frac{\mathfrak{M}_{n}}{\mathfrak{M}_{A}} \right)_{\mathbf{I}} = \frac{f_{i}^{\frac{1}{2}} f_{i\mathbf{I}}^{-\frac{1}{2}} [\mathfrak{M}_{n} / (\mathfrak{M}_{A} + \mathfrak{M}_{B})]_{t\mathbf{I}}}{1 - f_{i}^{\frac{1}{2}} f_{i\mathbf{I}}^{-\frac{1}{2}} [\mathfrak{M}_{B} / (\mathfrak{M}_{A} + \mathfrak{M}_{B})]_{t\mathbf{I}}}$$

where the subscripts I and II refer to the groups with one and two spectra respectively. He finds from his material

Spectral	(Mn/M 1)11	14	(MH/M 1)1		ıı
class	(Stripst III	/*	(20(2))20(1)1	71	/11
A	0,683	30	0,415	36	32
$\mathbf{F}$	0,806	19	0,466	21	18
G	0,826	13	0,508	27	15

229. Preferential Values of Stellar Masses. In order to determine the masses and the mass-ratios of spectroscopic binaries J Herferich has investigated 173 pairs, of which 61 exhibited the spectra of both components. The Cepheids, stars of the same type as  $\beta$  Canis Majoris, and stars with periods larger than 1000<sup>d</sup> were excluded. Hellerich found that stars of the classes A to G did not have very different mean masses.

Spectral class	(MA +MB)sin**	73
A F G	2,72 ① 2,08 〇 2,07 〇	22 13

Within the classes Oc—B9 the range in the mass value is from 10 to 1390. On account of this dispersion no mean values were formed for these spectial classes. Besides, the material suggested that the masses were grouped around

certain maxima of frequency, viz 320, 220, 160, 100, and 2,5-3,00. Although the material is small, it nevertheless seems difficult to explain the

preferential values as due to chance. The frequency of large masses decreases very rapidly with the increase in the value of the mass.

The adjoining distribution of the values  $\mathfrak{M}_B/\mathfrak{M}_A$  was found

The mean values are

$\mathfrak{M}_{B}/\mathfrak{M}_{A}$	Ос-В9	A—G	Mu/Ma	Oe-119	Λ—G
0,1-0,2 0,2-0,3 0,3-0,4	3	1	0,6-0,7 0,7-0,8 0,8-0,9	3 3 4	\$ 5 10
0,4-0,5	1	1 2	0,1-0,0	7	13

Spectral class	Ma/M i	13.	Spectral class	Ma/M t	11
B0-B5 B8-B9 A	0,64 0,76 0,79	13 4 22	F G	0,88 0,86	13 3

No relation was found between the mass-ratio and  $(\mathfrak{M}_A + \mathfrak{M}_B) \sin^3 i$ 

<sup>&</sup>lt;sup>1</sup> A N 220, p 249 (1924)

HELLERICH recommends the use of the quantity /t and investigates the frequency of this quantity in his material. A decided difference with regard to the distribution of the /t values is found between the systems for which one spectrum has been observed and those for which both spectra have been observed in the first case these values are considerably lower than in the second case.

This remarkable difference may arise from a number of causes. It does not seem likely that a systematically different orientation in space of the orbits

Operiral class			1	
	One spectrum	,	Two species	Ħ
A stars . F stars	0,367 0,280	27 20	0,543 0,587	13

of the two groups can be present. Nor can any systematic difference be assumed in the mass values themselves or in the mean eccentricities. An inspection of the material shows that the mean periods of the two groups are not very different. The only possible explanation seems to be to assume that the mass-ratios of the binaries with double spectra really are systematically larger than the mass-ratios of the binaries with a single spectrum, which means that the dispersion in the single masses in the former case should be smaller than the dispersion in the latter.

Comparing the values of  $R_B/R_A$  and excluding stars for which  $R_B/R_A$  is smaller than 0,80 Hellerich finds for group I the following values for the mean mass-ratio:

Spootral class	教制版。	
A stors	0,37 0,29	27 20

In those cases where the companion has a considerably lower brightness than the principal star the mass of the companion will also be very small in comparison with that of the more

massive star. The theory implies that the dispersion in stellar mass is larger than has generally been assumed but it scarcely gains support from an investigation of visual binaries. Mass-ratios as low as 0,3 scent to be rather exceptional among the 50 pairs so far investigated. The enormous difference in luminosity of 150000 between Procyon and its companion corresponds to a difference in the masses of only 0,9 ©.

In a subsequent paper Hellerich returns to the question, if preferential values of stellar mass exist. He points out that the results at the Cape Observatory by Halm concerning the preferential values of colour indices also pointed in the direction that there are six maxima in the frequencies of masses computed from the absolute magnitude and temperature. Halm's maxima are

From the material at hand of spectroscopic binaries Hellerich found five maxima, viz 330, 220, 160, 100 and 2,5-3,50

The values 2,8 © and 10 © are common to both series, the value 1,3 © is weakly indicated in the spectroscopic material. The small values 0,66 © and 0,32 © are wanting in the spectroscopic material as they correspond to very small amplitudes in the curves of radial velocity. On the other hand, the large mass values 16 O, 22 ©, 33 © are not extant in HALM's sories, for the stars used by him are of classes F to K and, therefore, cannot have large masses, as is known from other investigations.

HALM's series of the frequency-maxima of stellar masses nearly forms a geometrical progression with the proportion 1/a. Extrapolating this series to large masses, one obtains 23  $\odot$ , 46  $\odot$ , 92  $\odot$ , 184  $\odot$ . The comparison with the

AN 221, p 49 (1924)

Report of H M. Astronomer at the Cape of Good Hope 1922, p 4.

Testing Halm's series with the material offered by visual binaries. Illet it rich

finds indications of a frequency maximum between 0.90 and 1.50

230. Dwarf Nature of Spectroscopic Binaries. E A KREIKIN has advanced the idea that spectroscopic binaries are generally dwarf stars. From the catalogues of J Moore and A Beer 97 systems with two spectra were collected The value of sin; was found to be much larger than has been assumed earlier When the log's of the values MASIN3 1 and MRSIN3 1 were plotted against spectral class a rather definite curve was found. As there is no reason why the mean value of Msin's should systematically depend on spectral class, the actual relation between M and spectrum will be found when the plotted curve is shifted over an interval corresponding to the logarithm of sin<sup>3</sup>? The masses of the giants were computed according to Eddingion's theory and the masses of the dwarfs according to Brill's investigation? The following table shows the result

Spectral	log	e Wi	log M sin 4	lognit-lognit sin3 *		
class	Giants	Dwarfs	log Main. 4	Ginnts	Dwarfs	
O5	_	2,00	1,90	A-1-1	+0,10	
$\mathbf{B}$ o	0,87	1,00	1,10	-0.23	-0.10	
B5	0,65	0,65	0,44	+0,21	+0,21	
A0	0,56	0,44	0,22	+0,34	+0.22	
A5	0,54	0,30	0,11	+0.43	+0.19	
Fo	0,52	0,18	0,05	+0,47	+0,13	
F5	0,45	0,08	9,99	+0,46	+0.09	
G0	0,44	0,00	9,95	+0,49	+0.05	
G5	0,43	-0,08	9,90	+0,53	+0,02	
Ko	•~~	-0,16	9,86	1 -105	-0.02	

Although in the case of the dwarf hypothesis theresiduals, exhibit a systematic um there is no doubt that they should not be preferred Uncertainty is involved in the computation of the mean masses he cause the frequencies in the Russell dia-

gram used have not been reduced to equal space. Anyhow it is evident that the dwarf hypothesis might be worth a serious consideration. Kreiken found for dwarf stars the value  $\log \sin^3 i = 9,905 - 10$  and thus  $\sin i = 0,927$  and for grant stars  $\log \sin^3 i$ =9,525 -10 and  $\sin i = 0,695$  which is very near the value 0,667 generally adopted

In order to test the result the hypothetical distances were derived from the masses computed by multiplying Msin32 by the two values 0,927 3 and 0,695 3 corresponding to the dwarf and giant hypotheses The masses were converted into distances by means of Eddington's mass-luminosity formula A comparison between the distances thus obtained and the distances derived from trigonometric parallaxes or spectrographic determinations of the absolute magnitude decides in favour of the value  $\sin i = 0.927$ 

231 Discovery of Mass-Luminosity Relation, The relation between stellar mass and luminosity was at first indicated in Eddington's works concerning the radiative equilibrium of the stars. It was concluded that the luminosities of giants vary approximately as M2 and of the dwarf stars as M2. The first time a mass-luminosity relation was established in an empirical way was, as far as I am aware, in a paper by Hertzsprung' in 1919 in which he derived the formula:

$$\log \mathfrak{M} = -0.06 M = -0.06 (m + 5 + 5 \log n)$$

Somewhat later C Luplau-Janssens went over Herrzsprung's material again, but preferred to leave the coefficient AM/AM unchanged. At the same

<sup>&</sup>lt;sup>1</sup> M N 89, p 589 (1929) <sup>2</sup> Berlin-Babelsberg Veröff VII, Heft 1 (1927) 3 MN 77, p 596 (1917) <sup>4</sup> A N 208, p 96 (1919)

<sup>5</sup> Undersøgelser over Doppelstjerner III (1919)

time independently of Hertzsprung A van Maanen' derived a mass-luminosity relation of practically the same form. From van Maanen's paper the following table has been prepared giving the mean values of M, M and log M together with

the corresponding dispersions around the means

The curvature of the line connecting the mean values of M and M and the small dispersion in the values below  $M \approx 4.5$  are notable results in this investigation. The

M±=n	10十四	log Witte log me	n
0,42 ± 0,33 1,63 ± 0,44 3,00 ± 0,35 4,63 ± 0,27 5,77 ± 0,40 10,7 ± 0,81	3,42 ± 2,04 1,72 ± 1,47 1,24 ± 0,29	0,94 ± 0,46 0,75 ± 0,33 0,46 ± 0,25 0,13 ± 0,33 0,08 ± 0,11 -0,21 ± 0,14	4 6 6 12 8 3

mean values of the mass compare favourably with later investigations when more extensive material has been available.

Of the subsequent treatments of the mass-luminosity relation we shall only mention those of F. H. Seares and W. J Luyten The latter derived the expression  $\log \mathfrak{M} = -0.09 \, (M - 4.8)$ .

In 1923 Herzzsprung returned to the question. From a list of 15 first-class determinations, which included our Sun, he determined the diagram reproduced in fig. 153 The general decrease of mass with luminosity is clearly shown.

The faint companion of Sirius +49 is extraordinarily massive in # comparison with its small intrinsic brightness.

HERTZSPRUNG assumed the following linear relation

 $\log \mathfrak{M} = -0.084 (m + 5 \log n)$ but remarked that the quadratic expression

m+5log n=-11log R+2(log R)<sup>a</sup> would represent stars of great mass somewhat better

He introduces the conception of angular mass being

$$(\mathfrak{M}_A + \mathfrak{M}_B) \cdot \pi^a = \frac{a^a}{P^a}$$

Knowing  $\mathbb{R}_d/\mathbb{R}_n$  and  $a^3/P^2$  we find the absolute magnitudes of each component reduced to the mass of the Sun to be:

$$m_A + 5 \log \pi + \frac{4}{7} \log \mathfrak{M}_A$$
,  $m_B + 5 \log \pi + \frac{4}{7} \log \mathfrak{M}_B$ .

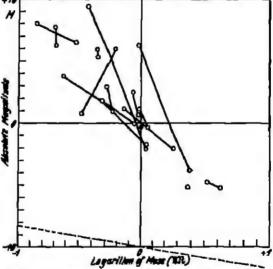


Fig 153 Mass-luminosity diagram according to HERTZPRUNG The full-drawn lines join the components of double stars. The single circle near the origo indicates the position of our Sun.

From the relation between mass and absolute magnitude it is possible to compute the parallax of a double star from  $m_A$ ,  $m_B$ , and  $a^2/P^3$  The formula will be  $0.86 \log n = \log n_d - \frac{1}{2} \log \left[1 + 10^{-0.084 (m_B - m_d)}\right] + 0.028 m_A$ .

The dynamical parallax  $\pi_i = \frac{s}{Pl}$  is computed in this case by assuming the mass-sum to be equal to the mass of the Sun.

If the above quadratic formula holds good the computation of  $\pi$  will be more complicated. Heretzsprung has given a table in his paper from which

<sup>1</sup> Publ ASP 31, p 231 (1919)

Mt Wilson Contr 226, Ap J 55, p. 165 (1922)
 BAN 2, p. 15 (1923).

<sup>•</sup> Hary Ann 85, No 5 (1923).

<sup>42\*</sup> 

the value of  $\log \mathfrak{M}_d$  is found by double interpolation, using  $m_B - m_A$  and  $5 + m_A + 5\log \pi_d$  as arguments. In accordance with the above quadratic formula,  $M_A$  is found and from the difference  $M_{\rm trig} - M_{\rm dyn}$  the ratio  $\pi_d/n_t$ , from which  $\mathfrak{M}_A + \mathfrak{M}_B$  is found.

Heretzsprung's Table of values of  $m_A + 5 \log \pi_d + 5$  (for  $\mathfrak{M}_A + \mathfrak{M}_B = 1$ )

log MA	0m		mp-m (									
	Car	1m	2m	3m	4m	5°n	10 <sup>1</sup> n	∞	m 1 1 5 1 5 log td			
-1,0	16,84	16,78	16,73	16,69	16,65	16,62	16,49	16,33	18,00			
0,9	15,52	15,46	15,42	15,37	15,34	15,30	15,17	15,02	16,52			
0,8	14,25	14,19	14,14	14,10	14,06	14,02	13,89	13,75	15,08			
0,7	13,02	12,96	12,91	12,86	12,82	12,78	12,66	12,51	13,68			
0,6	11,82	11,77	11,71	11,66	11,62	11,59	11,46	11,32	12,32			
0,5	10,67	10,61	10,55	10,51	10,47	10,43	10,30	10,17	11,(R)			
0,4	9,56	9,49	9,44	9,39	9,35	9,31	9,18	9,05	9.72			
0,3	8,48	8,42	8,36	8,31	8,27	8,23	8,10	7,98	8,48			
0,2	7.45	7,38	7,33	7,28	7,23	7,19	7.00	0,95	7,28			
··· 0,1	6.46	6,38	6,33	6,28	6,23	6,19	6,07	5,95	6,12			
0,0	5,50	5,43	5,37	5,32	5,27	5,23	5,11	5,00	5,00			
+0.1	4.59	4,52	4,55	4,40	4,35	4,31	4,19	4,09	3,92			
0,2	3.72	3,64	3,57	3,52	3,47	3,43	3,31	3,21	2,88			
0,3 (	2,88	2,80	2,74	2,68	2,63	2,59	2,47	2,38	1,88			
0,4	2,09	2,01	1,94	1,88	1,83	1,79	1.67	1,59	0,92			
0,5	1,34	1,25	1,18	1,12	1,07	1,03	0,92	0,83	0,00			
0,6	0,62	0,54	0,46	0,40	0,35	0,31	0,20	0,12	0,88			
0.7	-0,05	0,14	-0,22	~0,28	-0,33	-0,37	-0.48	-0,55	1,72			
0,8	0,68	0,78	0,86	0,92	0,97	1,01	1,12	1,19	2,52			
0,9	1,28	1,38	1,46	1,52	1,57	1,61	1,72	1,78	3,28			
1,0	1,83	1,94	2,02	2,09	2,13	2,17	2,28	2,33	4,00			
1,1	2,34	2,45	2,54	2,60	2,66	2,70	2,79	2,85	4,68			
1,2	2,82	2,93	3,02	3,09	3,14	3,18	3,27	3,32	5,32			
1,3	3,25	3,37	3,46	3,53	3,58	3,62	3,71	3.75	5,92			
1,4	3,64	3,77	3,87	3,94	3,99	4,02	4,11	4.15	6,48			
十1,5	-4,00	-4,14	-4,23	-4,30	-4,35				7,00			

In joint work with W S Adams and A H Joy, II. N Russfell has compared dynamical and spectrographic parallaxes in order to derive the masses of the stars. The number of stars for which such a comparison could be made was 327, including giants and dwarfs of spectral classes from O8 to M6. The stars were grouped in the following way.

Spectral class	$M_d$	Md-Me	$\pi_{\bullet}/\pi_{d}$	Residual	902	11
O8-B2	-1,2	+1,31	0,54	-0.02	6,2 ①	10
B3-B8	+0,5	+1,24	0,56	-0,07	5.6	10
B9-A1	+1,2	+0,61	0,75	+0,09	2,4	
gG9-gM6	+1,2	+0,67	0,73	+0.07		35
gF6-gG8	+1,6	+0,96	0,64	-0,04	2,5	28
A2-A4	+2,0	+0,55	0,78	+0,07	3.8	31
A5-A9	+2,5	+0,50	0,80		2,1	29
$F_0 - F_3$	+3,2	+0,69	0,73	+0,06	2,0	35
F4-F5	+3,3	+0,40	0.83	-0,02	2,6	17
dF6-dF8	+4,4	+0,68	0,73	10,07	1,7	24
dF9-dG0	+4,3	+0,39	0,84	-0.08	2,5	28
dG1-dG5	+5.2	+0.63	0,75	+0,03	1,7	25
dGo-dK1	+5.6	+0,56		-0,09	2,4	24
dK2-dK6	+6,5	+0,25	0,77	-0,09	2,2	25
dK7-dM6	+9,2		0,89	-0,01	1,4	21
dA-dF	+10.8	+0,01	1,00	-0.02	1,0	7
08-B1	-1,4	-0,32	1,16	十0,07	0,6	2
B2-B9		+1,64	0,47	-0,08	9,7	9
Dubl A C D	十0,6	+1,39	0,53	-0,07	6,8	22

<sup>1</sup> Publ ASP 35, p 189 (1923)

The values in the two last rows are derived from KAPTHYN's cluster parallaxes  $M_d$  is the absolute magnitude corresponding to the combined light of the pair and is based on the assumption that the sum of the masses of the components is = 0  $M_d$  is the absolute magnitude based on the spectrographic parallax. The mass  $\mathfrak{M}$  corresponds to the geometrical mean mass, from the ratio  $n_d/n_d$  which in its turn is the value corresponding to  $\mathfrak{M}_d - \mathfrak{M}_d$ .

The authors remark that the mean mass is by no means a simple function of the spectral class. But if the masses are plotted against the absolute magnitudes all the stars full into a straight line. The white dwarfs are no longer outstanding exceptions, their mass is small in the proportion to be expected from their low luminosity.

As a first approximation the relationship can be taken as linear and the

straight line:

 $\pi_a/\pi_a = 0.62 + 0.045 M_a$ 

as the relation curve. The residuals are given in the above table.

The values for the masses of B and A stars found by these authors did not amount to much more than 50 per cent of these found by Seares. The discrepancy anses from the following cause: Seares's material consisted of the stars known to be in relative motion, and for more distant pairs this involves a selection in

the sense that distant pairs of allow apparent motion are not included The result of this is too high an estimate of the mean rate of motion, and of the mean mass. A correction was applied by SEARES for the effect in question, but the later results show that the value has evidently been too small In the investigation now under review all well observed pairs were included, even if the apparent motion was very small Also, on account of the more extensive material, the

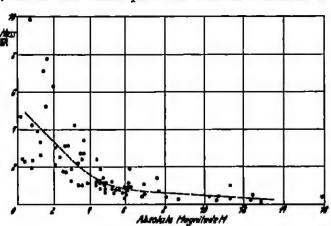


Fig 154. Relation between absolute magnitude M and mass M according to LUNDMARK. For this diagram the masses of double stars were derived using all available determinations of orbits and trigonometric parallaxes up till 1924. The dotted line represents the course of the mean values of various groups with regard to M.

values in the above table are certainly entitled to more weight as far as the carly spectral classes are concerned

In this paper the necessity of improving the dynamical parallexes by means of correction factors depending on the size of the mass was also pointed out

The dynamical parallaxes ordinarily given,  $\pi_d$ , should be multiplied by the factor  $(\mathfrak{M}_A + \mathfrak{M}_B)$  in order to be comparable with the parallaxes used in the above formula.

The dependence between mass and luminosity is really to be expected as follows from easy calculations. Combining the equation giving the

mass-sum in visual binaries with the equation of definition line " obtain  $\mathfrak{M}_A + \mathfrak{M}_B = 10^{3(\log n + 1) - 2\log P} \cdot 10^{0.6(m - M)}$ 

The empirical data show that there is some slight dependence between and the expression  $10^{3(\log n+1)-2\log P}$ , but a more obvious dependence between expression and the absolute magnitude. We can write

$$\mathfrak{M}_A + \mathfrak{M}_B = 10^{\gamma(m, M)} \cdot 10^{0.6M}$$

There is, using the actually determined masses, no dependence shown to m and M and there are no leasons that such a dependence should exist M = Mcipal point of the mass-luminosity relation thus can be derived with a theoretical deductions provided that log M can be expressed as a provided of M The higher terms in the expression

$$\log \mathfrak{M} = \sum_{i=1}^n a_i M^i$$

are derived on the basis of theoretical work, be it along the lines in lines. of in Jeans's theory of radiative equilibrium

Although the former in connection with his original theory of the in the of the stars showed that there is a general relation between mass and it magnitude it is not within the scope of this paper to present a kin it's count of earlier theoretical work. The student interested in this profiter adviced to consult Vol III/i of this Handbook

282. Eddingron's Mass-Luminosity Law1 and Cosmogonic Time 🛰 🛋 🔭 A theory concerning the stellar absorption coefficient ought to lead to love the determining the absolute magnitude of the giant stars for which the magnitude effective temperature are known. In order to avoid a determination of the solute values of the constants the observational data of Capella are the desired From these the absolute magnitudes of ordinary stars are computed at basis of the theory, regardless of whether they are grants or dwarfs. Are a transfer as to the giant and dwarf theory the absolute magnitude is a double-valued fur . \* of mass and effective temperature A star of mass 1 and temperature 5hf4) two possible magnitudes, viz that of the Sun at present and that of the when it passed through the same temperature on the up grade with a s larger surface area than now

The suggestion underlying the theory is that the dense stars like it. are in the condition of a perfect gas and will use in temperature if they waster a All ordinary stars are "grants" Theoretical reasons are given in the part of the EDDINGTON which assert that the stellar matter should be able to control 1 % an enormously high density before deviation from the laws of a prifer of a becomes appreciable

The results of Hertzsprung and of Russell, Adams, and Joy, which I am war been reviewed earlier, indicated that M plotted against M resulted in a county of the line, a conclusion which is difficult to reconcile with the giant and dwarf there are

According to the theory of radiation we have

$$1 - \beta = 0.00309 \, \mathfrak{M}^2 \mu^4 \beta^1$$

where  $\mu$  is the average molecular weight and  $1-\beta$  is the ratio of r = 1pressure to the whole pressure. The total radiation L of a star is proposition as a to  $\mathfrak{M}(1-\beta)/k$ , where k is the coefficient of absorption. In Edding 1972 \* 24 lier work h was believed to be approximately independent of temperature to the second second

<sup>&</sup>lt;sup>1</sup> M N 84, p 308 (1924)

density  $\varrho$ . The theory of nuclear capture and Kramers's theory, as well as other evidence suggest the form  $\hbar \sim \varrho/\mu T^{\frac{1}{2}}$  By the aid of this proportionality the following expression for the total radiation is found

$$L = \text{const.} \mathfrak{M}^{\frac{1}{2}} (1-\beta)^{\frac{1}{2}} \mu^{\frac{1}{2}} T^{\frac{1}{2}}.$$

The value of  $\mu$  is likely to be about 2,2 for Capella and Eddington adopted  $\mu$ =2,11. The following values computed from his formula show the general course of the mass-luminosity relation

1-8	Mante	Mad	Myja	T.	Spectral class
0,80	90,63 ①	- 6,71		26 200°	0
0.75	56,15	- 5,88	-	_	_
0,70	37.67	- 5,16	- 1	22 500	Oσ
0,65	26,66	- 4,52	(-2,2)		_
0,60	19.62	- 3,92	(-1,1)	-	
0,55	14,84	- 3,35	,	_	
0,50	11,46	- 2,81	(-1,1)	17460	B2
0,45	8,98	- 2,26	, <u> </u>	_	
0,40	7,12	- 1,72		_	
0,35	5,67	- 1,16	_	_	-
0,30	4,53	- 0,56	0,00	13260	B7
0,20	2,83	+ 0,81	0,87	10 520	AO
0,10	1,58	+ 2,82	2,88	8250	A8
0,05	1,00	+ 4.64	4,55	6290	P8
0,030 0,025	0,75 0,67	+ 5.93 + 6,38	6,17	5 160	G4
0,015	0,51	+ 7,63 + 8,61	8,03	4 540	Ko
0,004	0,26	+10,82	11,9	3210	Ko
0,0025	0,20	+11,95	_	_	
0,0015	0,16	+13,17	-	_	_
0,0010	0,13	+14,14	17,0	2550	Md

In this table have also been inserted the absolute visual magnitude and

the corresponding effective temperature and mean spectral class.

In this table as in the corresponding fig. 4 in Eddington's paper, the same effective temperature as that of Capella, 5200°, is assumed. For other temperatures the correction  $-2\log(T_{\star}/5200)$  has to be added to  $M_{\rm bol}$ . The whole range from 3000° to 12000° only introduces a correction of  $1^{\rm m}$ ,2.

The following table gives the correction to the magnitudes arising from the temperature term as well as the correction for reducing visual magnitude to

bolometric magnitude as derived by EDDINGTON in his earlier work1

Ta	-2 log T d 5200	Myle-Moul	T,	-2 log T./5200	Myte-Mbel	T <sub>0</sub>	-2 Lon T / 5200	Mets-Much
2000°	+0 <sup>M</sup> ,82		6000°	-0 <sup>1</sup> ,14	0,00	18000°	-1 <sup>M</sup> ,10	-
2500	+0 ,62	+2,65	7000	-0,28	+0.02	20000	-1 .19	
3000	+0,46	+1,71	8 000	-0,39	+0.05	25000	-1 ,38	
3500	+0 ,32	+1,04	9000	-0,49	+0,12	30000	-1 ,54	_
4000	+0,20	+0,80	10000	-0,59	+0,23	35000	-1 .68	
4500	+0,10	+0,35	12000	-0,74	+0,53	40 000	-1 .79	
5000	+0 ,02	+0,14	14 000	-0 ,88	_			
5500	-0 ,07	+0,05	16000	-1,00	_			ļ

The theoretical curve was compared by Eddington with the following observational data: 8 first-class determinations of masses of binary stars together with the mass of the Sun; 24 second class determinations of masses of binary stars. To these are added 6 double stars in the Hyades, 5 Cepheids, and 13 eclipsing binaries. The agreement between the 54 used mass-values derived

<sup>1</sup> MN 77, p. 605 (1917).

from the best observational data and the curve computed according to the theory is good, indeed. The average of the residuals is  $\pm 0^{\rm M}$ ,56, most of which might fairly be attributed to errors in the observational data, and the maximum discordance is  $1^{\rm M}$ ,7 Certain refinements of the nature of a second approximation are suggested by Eddington, who derives the following relation between a change in the molecular weight and a change in the absolute magnitude<sup>1</sup>

$$-\Delta M = \frac{9\beta + 8}{4 - 3\beta} \log e^{\frac{d\mu}{\mu}}$$

At the time this investigation was carried out the first approximation certainly sufficed. The accumulation of further data since their may invite us to make a second approximation.

The masses of the Cepheids were computed on the basis of the pulsation theory. The method is that of successive approximations. A value of  $\mathfrak{M}$  is assumed. From  $T_e$  (spectral class) the radius is deduced and then the mean density. The central density  $\varrho_e$  is 54,25 times the mean density. The period P is then obtained from the expression.

$$P \varrho_0^{\frac{1}{2}} = 0.29 (\gamma \alpha)^{-\frac{1}{2}}$$

where  $(\gamma a)^{\frac{1}{2}}$  is taken from M N 79, p 15, table V with  $1 - \beta$  as argument. The process is repeated until P stands. The highest value is 26,20 for Y Ophiuchi and the lowest 4,14  $\odot$  for RR Lyrae

Eddington inquires if, assuming that the gas-laws hold good for ordinary stars, we then should expect that each star will have the precise luminosity deducible from its mass and effective temperature or, in other words, whether the theory is accurate individually or only statistically. The sources of residual differences are principally abnormal composition and abnormal rotation. With regard to the first source an unduly large proportion of hydrogen would make the star fainter. With regard to rotation it has been shown by E.A. Millim that a rapid rotation makes the star slightly fainter, but that the effect is very small until the speed is sufficient to deform the star considerably. What is to be feared, concludes Eddington, is that the observed spectrum misleads us concerning the true value of  $T_{\theta}$ . An unsuspected binary ought to betray itself by having a magnitude fainter than that predicted from a knowledge of its combined mass.

The very interesting theoretical considerations as to whether it is physically likely that a dense star such as our Sun can obey the laws of a perfect gas cannot be given here. The student is referred to § 9 in Eddington's paper

The high density of the white dwarfs is not absuid. At a very low effective temperature smaller than that of a dwarf of spectral class M the star Shius B is probably able to produce in some way "an imitation of leading features of the F spectrum sufficiently close to satisfy the expert observer". The deviation of this star from the mass-luminosity curve is not surprising if the density is 53,000  $\odot$  new considerations enter into the calculation of k, since the elections are in the capture zone of two or more nuclei simultaneously. Also the deviation from the gas-laws may be considerable. On the other hand the star  $\sigma^2$  Eridan B agrees quite well with the mass-luminosity relation.

In Kramers's theory the absorption coefficient k contains<sup>2</sup> an additional factor  $\infty (1 + h\nu_1/RT)$  The effect of this factor was calculated and found to vary between +0.2 and -1.6 There are general reasons for accepting a correction factor of this form, which represents the ratio of the energy given up on capture

<sup>&</sup>lt;sup>1</sup> M N 84, p. 323 (1924)

at the mean ionization level to the mean free energy before capture. If the mass is supposed to be constant during the course of stellar evolution, then the mass-luminosity law is in disagreement with the views on stellar evolution accepted on the basis of Herzsprung's and Russell's work Eddington points out that the giant and dwarf theory definitely held the view that the influence of mass on luminosity was small and unimportant. It was thought that the stars along the main series had in the mean a lesser mass than the stars along the glant branch. The most generally advocated view was that the stars with smaller mass traversed their course more quickly than the heavier stars, although the theoretical arguments tend to show that the latter would reach the end-stage first. The results of Eddington show that the systematic difference in mass is not a minor detail, and that the correction to be applied before the Russell diagram can give the evolutionary course of individual stars is considerable.

Another possibility is that a star gradually diminishes its mass during its evolution. This would happen if the star is "burning itself away", i c if it obtains its energy of radiation by annihilating electrons and protons. A star burning itself up may increase continuously in density and internal temperature, although the effective temperature first rises, but then falls.

If the theory of annihilation of matter holds good the relative number of stars of different spectral classes can be computed, because the frequency of

a certain evolutionary stage will be proportional to the duration

The abundance of any stage should be proportional to the duration of of the stage if our is the amount of mass carried off as radiant energy during the stage then

 $\partial t \sim \int \frac{d\mathbf{R}}{L}$ .

Approximately L is proportional to  $\mathbb{R}(1-\beta)^{n}/\beta$  if the factor  $T^{-\frac{1}{2}}$  in k is neglected. Then

 $dt \sim \frac{\beta}{(1-\beta)^4} \frac{dR}{R}$ , or,  $\sim \frac{4-3\beta}{(1-\beta)^3} d\beta$ .

Integrating we find

 $\delta i \sim \delta \left\{ \frac{1+3(1-\beta)}{(1-\beta)^2} \right\}.$ 

The following table gives the cosmogonical time-scale according to EDDING-TON. Under the duration of stage is given the time it takes to develop between succesive values of mass or M<sub>bel</sub> given as arguments

However large the initial mass, there cannot be more than 20 left at the end of a billion years. If a cluster contains stars > 20, the age of the agglomeration cannot exceed 10<sup>11</sup> years. Now since most of the clusters contain absolutely faint and bright stars mixed

Mana W	M <sub>i=1</sub>	Duration of stage		
00 to 35 (	< -521	0,038 · 1019 years		
35 ,, 10	-5" to -2",5	0,065		
10 ,, 3,	]-2 ,5 ,, 0	0,214		
3.7 1.7	0 ,, 2 ,5	0,93		
1,73 ., 0,9	2,5,, 5	5.21		
0,92 ,, 0,5	5 , 7 ,5	36,3		
0,53 ., 0,3	7 ,5 ,, 10	281		
0,31 0,1		2190		

together the faint stars cannot have evalved appreciably. But, asks Eddington, if we have to deny the evolution of dwarf stars in clusters is there any point in assuming the evolution of dwarf stars in general?

<sup>1</sup> Nature 117, Suppl p. 25 (1926)

The numbers under the heading "duration of stage" should be proportional to the frequency of the absolute magnitudes or  $\varphi(M)$ . The theoretical luminosity-curve also agrees fairly well with the one found from observational evidence. This fact seems to the present writer to be the strongest support we have, at present, in favour of the theory of evolution by the loss of mass.

The frequencies of stellar masses among different absolute magnitudes have been derived by Luyten<sup>1</sup> on the basis of the mass-luminosity relation found by him,  $\mathfrak{M} = L^{0,225}$ , and the luminosity law of Kapteyn. Similar calculations have been made by J Ohlsson<sup>2</sup>, who has derived the distribution of stellar masses within ten parsecs on the basis of the material of the present writer and the mass-luminosity law of Eddington and of Jeans

	My		$\varphi(M_v)$	m	φ (M)
1 31	to	OM	5	3,16-4,00 ()	2
1		2	13	1.99 - 2.50	5
3	39	4	39	1,26 - 1,60	17
5		8	42	0.79 - 1.00	53
7	.,	8	62	0.50 - 0.63	57
9		10	30	0,32 - 0.40	45
11	19	12	12	0,20-0,25	19
13		14	3	0.13 - 0.16	8
		15	1 1	0,10	1

Eddington has also given a discussion of the fundamental quartic equation of the theory of radiative equilibrium in which the gradual increase in  $\mu$  from the centre to the boundary of the star is taken into account

For several practical purposes it has been thought to be conventent to express the mass-luminosity

law in a quadratic form of log M A least square solution of EDDINGTON's material has given

 $\mathfrak{M} = 10^{+0.6144 - 0.1576 M + 0.00112 M^4}$ 

This curve represents the material available with a sufficient degree of accuracy

233 Discrepancies between Seares's and Eddington's Results. (7 Shajn<sup>3</sup> has compared the masses as computed according to the theory of Seares<sup>3</sup> and according to that of Eddington. The agreement is unsatisfactory for the giant stars, and the divergence is of a systematic character. Eddington's masses of very high luminosity for late spectral classes are greater than the corresponding values of Seares, and the difference increases with increasing luminosity. For giants of early classes Seares's values are greater than Eddington's, while for late spectral classes the reverse is the case

Observational data of double stars, part of which have been obtained by Shajn at Pulkowa, lead to the following paradoxical result

Spectral class		1 2177		bol	Mn/MlA		
Primary	Secondary	(bolom)	Primary	Secondary	EDDINGTON	SRARES	71
K <sub>1</sub> G <sub>2</sub> F <sub>2</sub>	A8 A5 A5	2 <sup>m</sup> ,19 1 ,26 0 ,90	+0 <sup>M</sup> ,3 +0 ,6 +1 ,0	+2 <sup>17</sup> ,5 +1 ,9 +1 ,9	0,43 0,60 0,74	1,37 1,42 1,13	28 36

The result derived on the basis of Seares's theory is in conflict with other evidence concerning the mass-ratios in binaries and it does not seem very probable that so many systems like those of 85 Pegasi and  $\beta$  Lyrae should exist. It seems that a revision of the data used by Seares would be of much interest

<sup>&</sup>lt;sup>1</sup> Harv Ann 85, No 5 (1923) <sup>8</sup> AN 225, p 305 (1925)

<sup>&</sup>lt;sup>2</sup> Lund Medd Ser II, No 48 (1927).

<sup>&</sup>lt;sup>4</sup> Ap J 55, p 179; Mt Wilson Contr 226 (1922)

234. Jeans's Theory. Sir James Jeans has brought rather severe criticism against Eddington's researches on the mass-luminosity relation. It is not possible to give a full account here of the contents of Jeans's papers or to declare which method is to be preferred. It seems that the results reached by both the eminent authors by means of analysis do not differ very much as regards a good representation of the observational material

JEANS claims that, when the problem is treated in a sufficiently general way, the supposed mass-luminosity law disappears entirely as a theoretical law, so that a star of given mass can always adjust itself so as to radiate energy at whatever rate may happen to be required by the generation of energy in its interior A general relation is found to exist between the mass, luminosity and surface-temperature so that the said adjustment can be made in only one way. The whole interior constitution of a star is uniquely determined by its mass and its rate of generation of energy

The main point of difference between Jeans's work and that of Eddington is that the former considers the ratio  $\lambda$ , gas-pressure over radiation-pressure, or  $\beta/(1-\beta)$  to vary within one and the same star, whereas Eddington assumes this quantity to be constant throughout a star. Jeans is of opinion that in those cases most favourable for constancy  $\lambda$  varies  $\infty$   $T^{\frac{1}{2}}$  and that a variation of 1000 between different regions in the same star can hardly be dismissed as

impossible.

The gas-pressure, p, and radiation-pressure, q, are defined as follows.

$$p = \frac{\Re}{m\mu} \varrho T; \quad q = \frac{1}{3} \varepsilon T^4,$$

where m is the mass of the hydrogen atom, a the radiation constant,  $\mu$  the mean molecular weight,  $\Re$  the universal gas-constant, and  $\varrho$  the density

The dynamical equation of equilibrium is then

$$\frac{d}{d\tau}(p+q) = -\frac{7\ell}{r^2} \int_0^r 4\pi_e \varrho r^a d\tau, \qquad (1)$$

where  $\gamma = 6.66 \cdot 10^{-8}$  (gravitation constant).

If H is the outward flux of radiant energy per unit area, then the equation of transfer of radiation is.

$$H = -\frac{16\sigma T^0}{3\epsilon_0} \frac{\partial T}{\partial \tau} \tag{2}$$

where  $\sigma$  is STEFAN's constant of radiation  $= \frac{1}{4}aC$  and c the opacity of the star at the point considered. The energy is generated at a rate of  $4\pi s$  per unit volume and the average value of s inside a sphere of radius r is denoted by  $\bar{s}$ . The flux of energy accross a sphere of radius r surrounding the centre of the star must be equal to the total generation of energy inside this sphere so that

$$4\pi_{\bullet}r^{\bullet}H=4\pi_{\bullet}\int\limits_{0}^{r}4\pi_{\bullet}\varepsilon\varrho r^{\bullet}\,dr$$

The second of the above equations then takes the form

$$\frac{4aCT^*}{3o}\frac{dT}{dr} = -\frac{\overline{s}\varrho}{r^2}\int_0^r 4\pi_s\varrho r^s dr$$

<sup>1</sup> MN 85, p 196 (1925).

All theories agree that the main part of c is  $\sim \varrho/\mu T^3$  Eddington assumes an additional factor  $T^{-\frac{1}{2}}$  and Jeans puts  $c=\frac{\varkappa\varrho}{\mu T^3}T^{-n}$ , where  $\varkappa$  is a constant. The integral, that is common to the equilibrium-equation and the radiation-transfer-equation can be eliminated and then the following is obtained

$$\frac{d}{dr}(p+q) = \frac{3C\Re\gamma}{a\kappa m} \frac{T^n}{\bar{\epsilon}} \frac{q}{p} \frac{dq}{dr}$$

Further it is assumed that  $\bar{\epsilon} = \bar{\epsilon}_0 T^l (l)$  being a small and positive constant and  $\bar{\epsilon}_0$  another constant). This expresses the tendency of  $\bar{\epsilon}$ , the average generation of energy, to decrease from the centre as we pass out to the cooler external regions

We can now put 
$$\frac{T^{n-1}}{\overline{\epsilon}_n} = \zeta q^s \tag{3}$$

where, since  $q = \frac{1}{3}aT^{4}$ , we have 4s = n - l Putting  $p = \lambda q$  and denoting  $K = \frac{3}{a \times m} \frac{C \Re \gamma \xi}{a \times m}$  the equation (3) becomes

$$q\frac{\partial l}{\partial q} = \frac{Kq^*}{l} - (\lambda + 1)$$

or taking  $Kq^8 = x^2$ .

$$\frac{1}{2}\operatorname{sul}\frac{\partial\lambda}{\partial\nu}=v^2-\lambda(\lambda+1)$$

The most general solution of this equation is obtained by assuming for  $\lambda^2$  an expression of the form

$$\lambda^{2} = x^{2} (A + B x^{-1} + C x^{-2} + D x^{-3} + ) + x^{-4/8} (\alpha + \beta x^{-1} + \gamma x^{-2} + \delta x^{-3} + v^{-8/8} ($$

The method of equating coefficients of equal powers leads to

$$\lambda^{2} = \frac{2}{s+2} x^{2} \pm \frac{4}{s+4} \left(\frac{2}{s+2}\right)^{\frac{1}{2}} x + \frac{2}{s+4} \pm \frac{4(s+2)}{(4-s)(s+4)^{2}} \left(\frac{2}{s+2}\right)^{-\frac{1}{2}} x^{-1} + \cdots + \alpha x^{-\frac{1}{2}} \left[1 \mp \frac{2}{s} \left(\frac{s+2}{2}\right)^{\frac{1}{2}} x^{-1} + \cdots \right]$$

The first part of this equation is the standard solution for  $\lambda^2$ . In the interior of a star, in regions where x is large in comparison with its value at the boundary, the actual solution may be supposed to coincide with the standard solution. The series in which the standard solution is expressed is convergent in the special case of s=0 as long as  $Av^2>\frac{1}{4}$  or  $\lambda>0.207$  or  $i-\beta<0.828$ , which corresponds to a mass less than 1240. When s is  $\pm 0$  the limits of convergence will be different but as the value of s will be small the series can be assumed to converge for all reasonable mass-values.

Further it is shown that p+q can be taken equal to  $S\varrho^n$ , where  $n=k\varphi$  and  $\varrho \sim \mu \varrho^T$ 

The mass of a star is found from the equilibrium-equation to be

$$\mathfrak{M} = -\frac{r^2}{r\varrho} \frac{d}{dr} (p+q) = -\frac{r^2 Sn}{r} \varrho^{n-2} \frac{d\varrho}{dr}$$

The equilibrium-equation is transferred to the standard form discussed by Emden<sup>1</sup>, viz'

 $\frac{1}{R^2}\frac{d}{dR}\left(R^2\frac{d\sigma}{dR}\right)+\sigma^{\frac{1}{n-1}}=0,$ 

<sup>&</sup>lt;sup>1</sup> Gaskugeln p 61 (1907)

where  $r^2 = \frac{nS}{(n-1)4\pi_{e7}}R^2$  and  $\varrho^{n-1} = \sigma$  The only solutions of astrophysical interest are those for which  $d\sigma/dR$  vanishes when R = 0. The most general solution will be

$$\sigma = /\sigma_1, \quad R = /\frac{n-2}{2n-2}R_1$$

where f is a constant and  $R_1$  and  $c_1$  refer to the particular solution tabulated by EMDEN When  $\lambda$  is large the expression for  $\Re$  becomes:

$$\log \mathfrak{M} = \frac{3}{4(2s+3)} \log \bar{s}_0 + \frac{3n-4}{2n-2} \log f + \text{const.},$$

where the constant term contains only absolute constants of nature.

For very small values of  $\lambda$ 

$$\log \mathfrak{M} = \frac{6}{4s+3} \log s_0 + \frac{3n-4}{2n-2} \log f + \text{const.}$$
 (4)

The consideration is restricted to the simple case l=0, which corresponds to uniform generation of energy. Then the emission E is equal to  $4\pi_s \bar{s}_s \Re$  or.

$$\log \bar{s} = \log E - \log \Re + \text{const}$$

The two equation (3) and (4) then take the form

$$(2s+3,75)\log \mathfrak{M} = \frac{3}{4}\log E + (2s+3)\left(\frac{3n-4}{2n-2}\right)\log f,$$

$$(4s+9)\log \mathfrak{M} = 6\log E + (4s+3)\left(\frac{3*-4}{2n-2}\right)\log f$$

At the surface of the star the following equations are valid

$$\frac{1}{3} a T^4 = \frac{E}{8\pi \cdot Cr^3} = \frac{(n-1) \cdot 7}{2Cn SR!} E / \frac{n-2}{n-1}.$$

Hence.

$$4 \log T = \log E - \log S - \left(\frac{n-2}{n-1}\right) \log f + \text{const}$$

and from the dynamical equation of equilibrium combined with the equation by Exden  $\log \mathbb{R} = \frac{3}{2} \log S + \left(\frac{3n-4}{2n-2}\right) \log t + \text{const}$ 

If S is eliminated from these last two equations we have

$$4\log T + \frac{2}{3}\log \Re = \log E + \frac{2}{3(n-1)}\log / + \text{const}$$

By eliminating f from this equation and (4) and introducing absolute magnitude and temperature the resulting equation becomes:

 $c_1 \log T + c_2 \log \mathfrak{M} + c_1 M = \text{const.}$ 

where:

$$c_1 = 36(\varphi - 1) + 18(\varphi - 24) s$$
,  
 $c_8 = -(2s + 3.75) + 6(\varphi - 1) + (3\varphi - 4) s$ ,  
 $c_8 = 0.3[-1 + 12(\varphi - 1) + (6\varphi - 8) s]$ .

If the values of T, M and  $\mathfrak{M}$  were known for at least three stars with very high accuracy, it would be possible to use the data to evaluate the ratio of  $c_1: a_0, c_3$  and so to determine the values of  $\varphi$  and s. Instead an average solution of six stars (Sun, Capella A and B,  $\alpha$  Centauri A and B, and Sirius A) was carried out. The best fit is obtained from the approximate expression:

$$\frac{1}{2} \log T + 8,75 \log \mathfrak{M} + M = 11,17$$

The computation of the values of s and  $\varphi$  led to impossible results and then the equation was adjusted to

$$M + 2 \log T + 11,92 \log \mathfrak{M} = \text{const}$$
 (\lambda large)

For stars of small  $\lambda$ 's the following equation was derived

$$M + 4 \log T + 3.25 \log \mathfrak{M} = \text{const}$$

Jeans points out that these results are in some respects in very good agreement with those obtained by Eddington. For small masses ( $\lambda$  large) the equation of Jeans shows that for T= const. the total rate of energy-emission  $\varepsilon$  is  $\sim \mathfrak{M}^{1,7}$ , whereas in Eddington's theory it is  $\sim \mathfrak{M}^{1,1}$ . For stars of very great mass Jeans finds  $\varepsilon \sim \mathfrak{M}^{1,3}$ , while Eddington has  $\varepsilon \sim \mathfrak{M}^{1,1}$ .

EDDINGTON's theory, which was based on the assumption s=0, predicted a hard-and-fast relation between the rate of emission of radiation and the mass  $\mathfrak{M}$ . This relation will be represented by a single curve in a chagram in which  $\epsilon$  and  $\mathfrak{M}$  are taken as coordinates. According to Jeans's theory there is an infinite number of such curves in the  $\epsilon$  and  $\mathfrak{M}$  plane as soon as s differs even infinitesimally from zero. The only part of the plane that is ruled out is that in which the star would not be in a gaseous state.

The two equations for  $\mathfrak{M}$ , T, and M give the limiting forms of the curves in regions where  $\mathfrak{M}$  is small and large respectively, and from these the assembly of curves can be constructed as in Jeans's fig 2. Eddington's curve would be approximately represented by any one of the curves for which  $T=\mathrm{const}$ . According to Jeans there seems to be no reason why a star should keep its surface temperature constant during its evolution, so that evolution along a mass-luminosity curve would seem to be entirely improbable

One of the curves in the diagram will correspond to the temperature  $T_1$  which divides dark stars from visible ones. The observed values will, of course, all fall above that curve. A surface temperature  $T_2$  may also be imagined such that when the surface of a star has temperature in excess of  $T_2$  it radiates energy with such extreme rapidity that its surface temperature falls almost immediately below  $T_2$ . The observed stars will fall below that upper-limit curve. This seems to agree approximately with the observed facts as for instance shown in Eddingron's diagram.

In a subsequent paper 1 Jeans assumes a solution in ascending powers of s of the differential equation treated above as follows

$$\lambda = \Lambda_0 + s \Lambda_1 + s^2 \Lambda_2 + \cdot$$

and finds:

$$\lambda = \left[ \left( x^2 + \frac{1}{4} \right)^{\frac{1}{2}} - \frac{1}{2} \right] + \left\{ -\frac{x^2}{4x^2 + 1} \right\} A_0 s - \left[ \frac{x^4 + x^2}{(4x^2 + 1)^2} + \frac{x^4 - x^2}{2(4x^2 + 1)^2} \right] A_0 s^2 + \cdots,$$

where  $A_0 = (x^2 + \frac{1}{4})^{\frac{1}{2}} - \frac{1}{2}$ 

The solution is rapidly convergent for small values of s. It is found from the data that the closest fit is for s around 1/18. For such values the terms containing  $s^2$  can be omitted. A table in the paper gives  $A_0$ ,  $\psi_0 = \frac{A_0}{s}$ ,  $1 - \frac{s^2}{4s^2 + 1}$ ,  $1 - \beta$  and  $\mathfrak{M}$  with s as argument

By using the new expression of the mass-luminosity law the following is derived, viz

$$(2s+2.5)\log M + 4s\log T - (s+0.5)\log E + (2s+4)\log \mu + (4s+7)\log \psi = \text{const}$$

<sup>1</sup> M N 85, p 394 (1925)

In this formula  $\psi = 1/x$  and  $\log E = -0.4M + \text{const.}$  Introducing M we obtain

$$(2s + 2,5)\log M + 4s\log T + 0,2(2s + 1)M + (4s + 7)\log \psi = \text{const.}$$

From the six stars used before the value s = 1/18 is derived and hence

$$m + \log T_0 + 11,75 \log 90 + 32,5 \log \psi_0 = 8,332$$

A comparison has been made between this formula and Eddington's material by J Ohlsson<sup>1</sup> The agreement is just as good as between Eddington's formula and his material

In a reply to JEANS's criticism EDDINGTON<sup>2</sup> states that the principal point at issue is the dependence of M on  $T_s$ . He writes the fundamental equation of the theory in the form:

$$d\left(p + \frac{1}{3} a T^4\right) = \frac{4\pi_0 c G R}{L a n} d\left(\frac{1}{3} a T^4\right),$$
  
$$d\left(p + \frac{1}{3} a T^4\right) = -g_Q dr,$$

where p is the gas-pressure,  $\frac{1}{2}aT^n$  the radiation-pressure,  $\mathbb R$  the mass, L the energy radiated per second,  $\kappa$  the absorption coefficient, c the velocity of light, G the constant of gravitation;  $\tilde{s}$  is unity at the boundary and varies inwards in a way determined by the distribution of the source of the star's energy. As long as the mass is unaltered the solutions of these equations are homologous. If, keeping the mass of every element fixed, we multiply its linear dimensions by R, the following factors must be introduced: T is multiplied by  $R^{-1}$ , p by  $R^{-2}$ , p and  $\frac{1}{2}aT^2$  by  $R^{-4}$ , p by  $R^{-2}$ , p by  $R^{-2}$ , p by  $R^{-3}$ , p and p by p by

$$L \sim R^{-n}$$

Purther:

By eliminating R and converting into absolute magnitude:

$$-\delta M = \frac{10\pi}{2+\pi} \delta (\log T_4).$$

For Eddington's law of absorption  $n=\frac{1}{4}$ , and the same correction is obtained as was given in his paper of 1924. To make n differ greatly from  $\frac{1}{4}$  would, as Eddington states, "be to reject altogether the law of absorption on which I have based my conclusions; but, of course, I do not suppose the law to be exact, and I have nothing against values of n reasonably near to 1, say, between 0 and 1".

EDDINGTON points out that if a given rate of generation of energy is greater than the rate of radiation L, fixed by the formula, then the energy of the stars is increasing, and the star is expanding indefinitely. By the above formula L varies as  $R^{-*}$  and therefore diminishes.

An analysis of Jeans's paper has convinced Eddington that there is nothing singular about his value  $n = \frac{1}{4}$  and that the exponent 4 does not affect the magnitude-mass-temperature relation in the two cases considered. Furthermore the mass-luminosity relation is not reached by treating  $\lambda$  as a variable quantity. Jeans's generalisation of the problem consists in limiting  $\lambda$  between the two values 0 and  $\infty$ .

M N 85, p 403 (1925).

<sup>1</sup> Lamd Medd Ser II, No 48 Also thonis Land (1927)

235. The Cosmogonic Time-Scale by Jeans and Smart. The results reached by von der Pahlen (of ciph 216) could certainly be improved if the cosmogonic time-scale established by Jeans of Eddington (see ciph 232) were used. The procedure according to Jeans was taken into account that possibly positive and negative electric charges fall together and annihilate one another, there energy being transformed into radiation. The discovery of the mass-luminosity relation increased the probability of this conjecture enormously.

JEANS has derived the relation1

$$\frac{d\mathfrak{M}}{dt} = -\alpha \mathfrak{M}^3,$$

where  $\alpha = 5.2 \cdot 10^{-88}$  is found by taking the values for the solar system  $\mathfrak{M} = 2 \cdot 10^{33}$ ,  $-\frac{d\mathfrak{M}}{dt} = 4.2 \cdot 10^{12}$  Solving the equation he finds the time required for a star to pass from mass  $\mathfrak{M}_A$  to mass  $\mathfrak{M}_B$  to be given by

$$t = \frac{1}{2\alpha} \left( \frac{1}{\mathfrak{M}_H^3} - \frac{1}{\mathfrak{M}_1^3} \right)$$

JEANS has also given in this connection the following interesting theorem concerning the relation between mass and size of orbit of a star

From the motion of a particle under a central force  $\mathfrak{M}/r^2$  the equation

$$\frac{d}{dt} \left[ \frac{1}{2} \left( \left( \frac{dr}{dt} \right)^2 + r^2 \left( \frac{d\theta}{dt} \right)^2 \right) - \frac{\mathfrak{M}}{r} \right] = -\frac{1}{r} \frac{d\mathfrak{M}}{dt}$$

is readily deduced1, which becomes

$$\frac{d}{dt} \binom{\mathfrak{M}}{2a} = \frac{1}{r} \frac{d\mathfrak{M}}{dt}$$

when a is the major axis of the orbit

Averaging over a complete revolution, Jeans finds

$$\frac{d}{dt}\left(\frac{\mathfrak{M}}{2a}\right) = \frac{1}{a} \frac{d\mathfrak{M}}{dt},$$

from which follows

$$\mathfrak{M}a = \text{const}$$

If our Sun ever was a B star or if its mass ever was 40 the time clapsed since this epoch must be about 7.1 · 10<sup>13</sup> years

SMART<sup>3</sup>, who has connected the above differential equation with the theory of Eddington, finds a scale in substantial agreement with that of Jlans. By three different procedures he has derived the following values of t necessary for a star to pass from different values of  $\mathfrak{M}_A$  to  $\mathfrak{M}_B = 1 \odot$ 

The scale must be still longer, because no account is taken of the increase in mass necessary on account of the meteor frequency. The investigations of the frequency of meteors show that they are not restricted to our solar system but are universal phenomena. Taking into account the frequency of meteors we find that the mass of the Sun will be doubled during a period of 10<sup>13</sup> years. Thus the increase of the stellar mass due to encountering meteors will partly counterbalance the secular decrease of the mass.

<sup>&</sup>lt;sup>1</sup> M N 85, p 2 (1924)

<sup>&</sup>lt;sup>2</sup> M N 85, p 423 (1925)

286. Bril's Theory and Parallax-Method for Binaries<sup>1</sup> According to the theory of radiative equilibrium he<sup>1</sup> should be constant within a certain star (h is the mean absorption coefficient of the total radiation) but should vary from star to star with the size of the mass. If we assume the relation.

to hold good, it follows from statistical considerations of data concerning magnitudes, parallaxes, and masses that the relation.

holds good for nearly all stars. In order to see the reason for this we must transform the expression. If a is the constant in STEPAN's law and M is the gas constant, we have the equations:

$$Q = \frac{\mu a \beta}{3 \Re (1 - \beta)} T^0,$$

$$h = 3.28 \cdot 10^{57} \cdot \frac{a}{3 \Re (1 - \beta)} T^{-1}.$$

Further the central temperature  $T_o = 1.7 T$  is introduced and the radius R Then:

$$T_o = \frac{6,9011 \, \Re}{\mu \beta R} \left( \frac{3 \left( 1 - \beta \right)}{\kappa_o \sigma G} \right)^{\frac{1}{2}}.$$

According to the definition-equation

$$1 - \beta = \frac{h \cdot a}{4\pi \cdot a \cdot G}$$

and thus,

$$\varepsilon = \frac{12\pi, oG\Re}{a \cdot 3, 28 \cdot 10^{47}} \frac{(1-\beta)^{4}}{\beta} \left(\frac{T_{*}}{1.7}\right)^{\frac{1}{4}}$$

and.

The central temperature is rather constant, varying as it does between  $35 \cdot 10^{\circ}$  and  $40 \cdot 10^{\circ}$  degrees. The constancy of  $he^{\frac{1}{6}}$  is mainly determined by the quantity  $\beta^{\frac{1}{6}}$ . If  $\Re$  varies between  $10 \odot$  and  $0.16 \odot$ , the corresponding variation in  $\beta^{\frac{1}{6}}$  is from 0.73 to 1.00.

Independently of the theory of the stellar absorption coefficient the quantity het can be expressed in quantities furnished by observational work. If the stars are in radiative equilibrium, the radiated energy is equal to the energy produced in the interior of the star:

$$\pi_{\bullet}acR^{a}T^{i}_{\bullet}=a\mathbb{R},$$

where  $T_{\bullet}$  is the radiation temperature

If the value of  $ks^{\frac{1}{2}}$  from the above definition-equation is substituted in the present expression, k becomes equal to  $4G(1-\beta)\Re(sR^{\frac{1}{2}}T_0^{\frac{1}{2}})^{-1}$  and thus:

$$h\sqrt{s} = 4G(\pi, 0)^{\frac{1}{2}} s^{-\frac{1}{2}} (1 - \beta) \mathfrak{M}^{\frac{1}{2}} R^{-1} T_{\bullet}^{-2}$$

Introducing the numerical values of the constants and selecting solar units we obtain as the final equation:

$$\log k \sqrt{s} = 3,459 + 2\log \frac{c_1}{T_s} - \log \frac{R}{R_O} + \log (1 - \beta) + \frac{1}{2} \log \frac{R}{R_O}.$$

Berlin-Habelsberg Veröff 7, H i (1927)

In order to determine the numerical value of  $k\sqrt{\epsilon}$  the material of Rabel (38 pairs  $\pi < 0'',040$ ) and that of Bottlinger<sup>2</sup> (17 eclipsing variables) together with data for the Sun and Capella were used. The value 2,85 for  $\log k\sqrt{\epsilon}$  resulted from 68 stars

Brill discusses at length the derivation of  $\mathcal{I}_{\mathfrak{o}}$ , the radiation temperature corresponding to the radiation temperature of the bolometric magnitude of the central part of the star disc. The colour temperature of a star refers to the course of the energy curve in a certain part of the star spectrum and corresponds to the

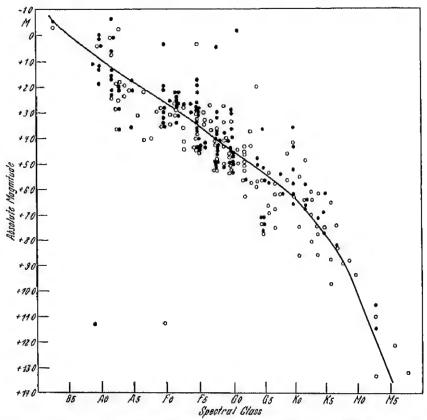


Fig 155 The Russell diagram as derived by Brill on basis of parallaxes of binaries using the theoretical relation ket = const Full circles refer to primaries and open circles to secondaries of binary stars

temperature of a black body radiator whose energy curve in the same part has the same form as that of the star. The radiation temperature refers to the intensity of the emitted radiation and corresponds to a black body radiator that emits radiation in equal intensity to that of the star. If the conception of effective temperature is to be preserved it ought to be defined as the temperature of a star for which the total emission of a black body radiator equals that of the star.

In order to obtain accurate values of the colour temperature it is necessary to supplement the visual and photographic measurements with bolometric,

<sup>&</sup>lt;sup>1</sup> A N 225, p 217 (1925).

<sup>&</sup>lt;sup>2</sup> Atti della Pontificia Accad (1924).

radiometric, and thermoelectric measurements in the ultra-red. The radiation temperature cannot be determined without a knowledge of the stellar diameter. Only a few stars have been measured as yet with interferometric methods; thus our knowledge of the radiation temperature is very restricted. For the Sun the following values of the radiation temperature are derived

Endiation temp, of the Sun from Bolom, data Viscal data Photogr data Mosan solar radiation 5775° 6075° 5835° Contral solar radiation 6075° 6435° 6190°

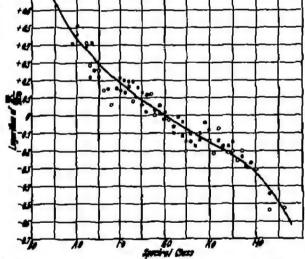
The following are the results from the stars:

Object	Spectral	Italiya	Apprent magnitude	Rad temp. of the vis. magn.	Colour temperature
Sun . Arcturus . Aldobaran Butelgauze . Antares .  \$\beta\$ Pegusi	G0	961",2	-26=,90	c_/T = 2,36	c <sub>2</sub> /T=2,05
	K0	0 ,0100	+ 0 ,24	3,44	3,50
	K8	0 ,0100	+ 1 ,06	3,82	4,39
	M1	0 ,0235	+ 0 ,92	4,69	4,65
	M2	0 ,0200	+ 1 ,22	4,66	4,77
	M3	0 ,0105	+ 2 ,61	4,66	4,61

At present we can do no better than assume equality between the radiation and the colour temperature,

The following temperature scale was assumed.

Spectral class	T	<b>√</b> T
O5	28000°	0,51
130	20800	0,69
B5	16900	0,85
Ao	13 000	1,10
A5	10200	1,40
Fo	8 300	1,72
gF3	7 200	2,00
drs	7 200	2,00
gGo	6 050	2,37
dGo	6240	2,30
gG5	4880	2,96
dG5	5 560	2,58
gKo	4310	3,33
dKo	4910	2,92
gK5	3 380	4,24
dK5	3910	3.07
gMo	3 200	4.49
dMo	3 420	4,20



For 123 visual pairs with known orbital elements BRIL has computed the radiation-energy

Fig 156. Relation between logarithm of stellar mass and spectral class according to Britz. Full circles refer to primaries in binary stars and open circles to secondaries.

parallaxes no, which enter into the expression log R/Ro owing to the relation:

 $\log R/R_{\odot} = 0.2 (M - m - \Delta m) - \log n_{\rm re} + 4.946$ 

where M is the surface-intensity magnitude, m the apparent visual magnitude and  $\Delta m$  the correction to bolometric magnitude. The computation of  $n_m$  has to be performed by means of successive approximations. For this purpose an extensive table is given in Brill's paper with  $1-\beta$  as argument,  $\log{(1-\beta)}$ ,  $\log{M/M_{\odot}}$ , and  $\Delta\log{(1-\beta)}$ :  $\Delta\log{M/M_{\odot}}$  as functions, Further the expressions  $\frac{1}{2}\log{M/M_{\odot}} + \log{(1-\beta)}$  and  $\Delta\log{M/M_{\odot}} \cdot \Delta\left[\frac{1}{2}\log{M/M_{\odot}} + \log{(1-\beta)}\right]$  are given in order to facilitate the necessary interpolations.

The agreement between  $\pi_{re}$  and  $\pi_{tr}$  or  $\pi_{s}$  is very good indeed. The masses, mass-ratios, dimensions, densities, and central temperatures are also determined and entered in the catalogue.

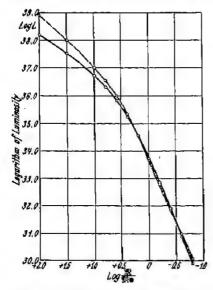


Fig. 157. Relation between logarithm of stellar luminosity and mass. The fulldrawn curve is the relation derived by Brill on the assumption that kes const. and the dotted curve is the relation according to EDDINGTON.

The agreement of the derived Rus-SELL diagram with the observed one shows that the relation between the mass and the product  $k \varepsilon^{\dagger}$  as derived by Eddington is in agreement with the observations. Furthermore it also proves the probable reality within a wide range of the formula of BRILL  $(k\varepsilon^{\frac{1}{2}} = \text{const})$ , which is partly based on the theory of radiative equilibrium and partly on an empirical foundation,

The agreement between the mass-luminosity relation according to EDDINGTON and according to Brill is very good. There are practically no deviations for the luminosity range  $\log L = 30.0 - 36.5$  (M8 to B0 stars roughly) or for the entire main series.

287. Mass-Reduction by Annihilation of Protons and Electrons. C. LÖNNQUIST1 has examined various hypotheses concerning the evolution on the basis of Edding-Ton's theory by using the empirical Russell diagram as guidance and test.

The investigations of Eddington in 1924 showed that it is the difference in mass and not in intensity that causes the considerable difference in the luminosity

of the giants and dwarfs. Although it is still possible that the stars develop from the giant stage to the dwarf stage in the traditional way there is no longer any explanation why they should develop in just that way. But if such an evolution takes place, then the mass reduction must be investigated. Such a reduction is not only dependent on a possible throwing off of matter into space. The stars also radiate away enormous quantities of energy, and as energy is equivalent to mass the stellar masses must be diminished in the course of time, if no compensating factors exist.

It has been shown by Eddington that the energy lost by radiation cannot be fully compensated by the energy liberated by contraction since the time-scale thus obtained is altogether too short. If the mass 11,5 0 is taken, such a contraction-development from the giant M to the giant F stage would take only 30000 years, and for the Sun itself 1,5 · 107 years. From geological evidence it is found that the age of the Earth must be 10° years at least and the minimum age of the Sun ought to be at least 1010 years.

The investigations of F. W. ASTON in 1920 gave rise to the hypothesis of EDDINGTON<sup>9</sup> that the helium in the stars is built up of hydrogen. This process involves a change of 0,008 of the mass into energy. It seems also that something

<sup>&</sup>lt;sup>1</sup> Ark Mat Astr Fys 20 Λ, No. 21. Also thesis Upsala (1927).

Brit. Assoc. Report 1920, p. 45. This theory seems also to have been presented independently by J. Perrin: Annales de Physique 2, p. 89 (1919), and Revue du Mois 21 p. 113 (1920).

similar can be postulated concerning the composition of other light atoms, but the effects in these cases might be considerably smaller. It seems hardly possible to reach an amount exceeding 0,040 of the mass. The time the Sun would require for such a mass-reduction is 4,5 · 10<sup>11</sup> years, which is sufficient for geological demands if the Sunhas from the beginning an abundance of hydrogen of 10 per cent. But if this hypothesis is accepted the evolution will principally follow a mass line, as has been pointed out by Lönnguist, and the Russell diagram cannot mark the evolution-course of the stars, but only the loci of the most stable equilibrium points of the stars

EDDINGTON points out that helium must have been produced somewhere The doubts of some physicist that the interior of the stars may not have a sufficient temperature are met with the advice "to seek a hotter place" EDDINGTON seems to assume that the processes of building up the atoms already occur in the nebulae so that they have taken place to a great extent while the stars are in an early stage of evolution. The stars can hardly contain hydrogen any longer. EDDINGTON'S arguments against the occurrence of hydrogen in the

stars are based on the following views.

A large percentage of hydrogen would decrease the molecular weight  $\mu$  so much that the radiation pressure would become insignificant in comparison with the gas pressure even in case of the most massive stars known. The radiation pressure would lose most of the importance ascribed to it as an explanation of the fact that the stellar masses are situated within comparatively narrow limits

On account of the change in the value of  $\mu$ , entering in the luminosity formula with the expression  $\mu^{\dagger}$ , a considerable amount of hydrogen would alter the mass-luminosity relations. Besides, if the abundance of hydrogen differed for stars of the same mass, the stars would not lie along a mass-luminosity line, but would exhibit greater or smaller deviations from it. Lönnquist finds from a lengthly discussion that the assumption of the importance of the radiation pressure for the size of the star-masses is untenable, and that it does not form any valid argument against the presence of hydrogen in the stars. While a not inconsiderable proportion of hydrogen appears necessary for Capella in order to obtain agreement between the theoretical and observed luminosity, varying proportions of hydrogen in stars of the same mass appear to lead to not inconsiderable deviations from the luminosity as computed from Eddington's luminosity law. The testing of that law by means of stars of known masses and luminosities cannot be made with such accuracy as to allow a decision concerning the nature of the individual deviations. The theory requires special revision as regards the abundance of hydrogen.

The radioactive hypothesis cannot explain, in its original form, a considerable mass reduction. The radioactive processes have, as far as is known, the property of being independent of temperature and density. In order to have an important mass reduction one would have to imagine, with JRANS, another kind of radioactivity. He has suggested an annihilation of matter within the atom nuclei together with a liberation of energy. To describe this as radioactive would then be an accentuation of these processes—just like the radioactive—being inde-

pendent of density and temperature.

JEANS'S theory introduces a third hypothesis, the boldest of them all, namely the annihilation of protons and electrons with transformation of the mass into energy. This idea is not new and it arose even before the question of the evolution of the stars had advanced any considerable way. EDDINGTON mentions J. LARMOR as one of the precursors of this theory and as early as in 1904 JEANS expressed

himself in favour of this line of thought, while Eddington suggested the hypothesis for the first time in 1917. MACMILLAN also supposes the contrary process to take place, i.e. a transformation in space of the radiations of the stars into matter, into protons and electrons from which the nebulae arise. In this way a circulation is obtained between mass and energy, which is certainly of much importance for cosmology.

The annihilation of protons and electrons may be supposed to be a nucleus process analogous to the radioactive ones or the result of a collision between a free electron and a nucleus proton. EDDINGTON conceives both possibilities. In the former case the process evades every calculation regarding dependence on the outer physical conditions. The process might possibly depend on the very constitution of the atom nucleus. In the second case the density and

temperature may be thought of as deciding the rate of the process.

Lönnguist's paper is partly devoted to an examination in detail of the second of the above-mentioned cases, which the author calls the hydrogen hypothesis. He finds that the known facts concerning the components of the double stars seem on the whole to agree with the hydrogen hypothesis. For the development of the widely separated binaries from close pairs an evolution with mass reduction seems necessary. The long time-scale associated with such an evolution is of extreme importance for cosmogonic problems. The evidence of the clusters has also been investigated. The facts scarcely decide in favour of one or the other theory of evolution, but they do not seem to confirm RUSSELL'S evolution scheme. Stars are probably formed with very different masses. Only the larger ones are checked in the giant stage, while the smaller ones go directly into the main series.

288. The Theory of RABE. The aim of this investigation was to establish the relation between the absolute magnitude, the temperature, and the mass of dwarf stars. It has to be assumed that there exists a one to one relation between  $M = T_{\bullet}$ , and  $\mathfrak{M}$ , which is also in agreement with the empirical and theoretical results. On account of the comparatively high density of the dwarfs it is comparatively easy to define the conception of the stellar surface that is necessary for the theory developed. It is sufficient to start from the surface conditions of our Sun and to assume that the thickness of the layer from which the visible radiation has its origin is small in comparison with the radius of the star. But on the other hand, it has to be assumed that the layer in question has such radial extension that the surface radiation can be considered to be emitted by a black-body radiator. Above such a surface a cooler atmosphere may be situated, which, of course, would absorb part of the radiation. The results of spectral analysis show that the amount of this absorption is comparatively small for classes earlier than F, but becomes appreciable in that class, and increases continuously to the end of the main series. The absorption is certainly selective so that the coefficient of transmission is a (unknown) function of the wave length. It is then necessary to use a mean value of the coefficient which is a function of the surface temperature and the mass, as the gravitative power exerts an influence on the general atmospheric condition of a star. The stars have to be assumed to be perfect sphere: and the size of the surface is thus determined by means of the mass and the mear density. This quantity can be considered, at least at a first approximation to be a function of the surface temperature and mass. Although BERNEWITZ' could not establish a definite relation between the mean density and the mass still the probability that such a relation exists is very great3.

A N 225, p. 217 (1925). <sup>9</sup> AN 213, p. 1 (1921). In fact, such a relation was established by ABETTI in 1922.

Let  $s_0$  be the intensity of radiation of a surface element, p the mean value of the coefficient of transmission, T the effective surface temperature, and o a factor of proportionality, then the observable radiation i of a surface element is:

$$s = pi_0 = cp(c_0/I)^{-4}$$
.

Let further  $\varrho$  be the mean density and C another factor of proportionality. Then the total radiation of I the star is

$$I = C (\mathfrak{M}/\rho)^{\frac{1}{2}} p (c_{\bullet}/T)^{-4}$$

If this quantity is transformed into magnitudes we have:

$$M + \Delta M = \Phi + 10 \log c_0 / T - \frac{1}{2} \log \mathfrak{M} + \frac{1}{2} \log \rho - \frac{1}{2} \log \rho. \tag{1}$$

dM is the correction of the visual absolute magnitude M to belometric magnitude and  $\Phi$  a constant.

As a result of numerous trials RABE selected the following expression for  $\varrho$  and  $\dot{p}$ .

 $\varrho = c(c_0/T)_1^m \mathfrak{M}^1,$  $\varphi = (T/T_0)^m \mathfrak{M}^n \le 1.$ 

 $T_0$  is the limiting temperature for which at unit mass an appreciable atmosphere sets in The second equation does not seem very plausible from a theoretical point of view but RABE gives a reason for its use. If we pass over to solar units the above equation takes the form  $\rho = (T_0/T)^* \Re^2$ .

Then the equation (1) takes the form

$$M + \Delta M = (10 + \frac{1}{2}\pi + \frac{1}{4}\pi) \log c_0 / T - [\frac{1}{2}(1 - \lambda) + \frac{1}{4}\mu] \log \mathfrak{D} + \Phi - \frac{1}{2}\pi \log c_0 / T_0 - \frac{1}{4}\nu \log c_0 / T_0.$$
 (2)

The unknowns  $\kappa$ ,  $\lambda$ , r,  $\mu$ , and  $T_0$  can be determined from the observational data. If p should be larger than one, the terms containing  $\nu$  and  $\mu$  must be dropped. The masses were determined from 38 dwarf binaries with a parallax equal to or larger than 0",040. The values of  $\Delta M$  were derived from the radiation law of Planck and the spectrophotometric measurements of Wilsing. Further  $M_{\odot} = 4.79$ , the observed value of  $c_0/T$  for the Sun = 2,40,  $p_{\odot} = 0.71$ , and hence  $c^2/T_{\odot} = 2.40 \cdot p_{\odot}^2 = 2.20$ , and  $\Phi = 1^m,42$  were used.

Next the value of  $\lambda$  is determined. For stars earlier than F5 it has very nearly the value 1 and thus the density-ratio of such stars can be determined without any knowledge of  $\phi$ . The author finds  $\lambda = 0.293 + 0.012 \times$ . The value of  $\times$  is situated between 2.5 and 3 and the last value is adopted. The coefficient of log M in the above equation,  $b = -[\frac{1}{4}(1-\lambda) + \frac{1}{4}\mu]$ , is determined from binaries of equal spectra and varies with the spectral class:

Spectral class			Spectral chas	3	
Go G4	1,98 2,35	9	Ko K4	-2,28 -4,23	7 6

This, if real, suggests a complicated form for the functions  $\rho$  and  $\dot{\rho}$ . At present it does not seem possible to decide whether the variation is real or not. If  $\dot{b}$  is taken as -2.71,  $\mu$  is found to be  $\frac{1}{2}$ .

It is unavoidable that the determination of the different constants must be affected with some uncertainty owing to the paucity and in several cases the uncertainty of the data. RABE finds the following two formulae:

Stars without atmosphere (p=1):  $M_{bol}=15\log c_s/T-\frac{1}{2}\log \mathfrak{M}-0.29$ . Stars with atmosphere (p<1):  $M_{bol}=20\log c_s/T-\frac{9}{2}\log \mathfrak{M}-1.63$ .

In order to have one formula the following expression is adopted

$$M_{\rm bol} = \frac{1}{1} \log \frac{c_2}{T'} - \frac{2}{9} \log M + 0.90.$$

Here  $c_2/T'$  has to be selected in such a way that both the formulae are represented

The essential point in the theory of RABE is that M is considered to depend on the temperature much more than is the case in the theory of Eddington The theory is of considerable interest and ought to be compared with the empirical data as soon as more observations have been collected

The  $c_2/T$ -value in the above formulae corresponds to the surface temperature and is related to the effective temperature  $T_s$  in the following way

$$\log (c_2/T_s) = \frac{9}{2} \log \frac{c_2}{T} - \frac{1}{6} \log \mathfrak{M} - 0.134$$

The effective temperatures that result from the material of RABE are in very good agreement with those computed according to the methods of SFARES and of BRILL. If the  $c_2/T$ -values are diminished by ten per cent they are in very good agreement with the corresponding values derived by M N SAHA¹ on the basis of his theory of ionization. It is certainly very interesting that the theory of RABE is able to explain most of the differences between the results of BRILL and SAHA.

Using the temperature-scale thus established RABE has computed the absolute magnitudes and the masses and derived the following mean errors

Spectral	Z.	fern errors	
class	in M	in log M?	11
A0-F9 G0-G9 K0-Mdp	士0 <sup>11</sup> ,34 士0 ,48 士0 ,32	士0,19 士0,17 士0,11	22 23 20

RABE then makes a revision of his system and finds from a discussion of the values of  $m_{\text{O}}$  and  $c_2/T_{\text{O}}$  a correction that should be added to the constants in his equation. He finds

$$\log \frac{c_2}{T} = \frac{1}{6} \log \varrho - \frac{1}{6} \log \mathfrak{M} + 0.342$$

For the application to binaries the equations giving the mass-luminosity relation are changed into the following forms:

$$\log \pi = 9\log \frac{c_2}{T} - \frac{2}{3}\log \frac{\mathfrak{M}_A}{\mathfrak{M}_A + \mathfrak{M}_B} - 2\log a + \frac{4}{3}\log P - \frac{3}{5}(m+5+\Delta m_{\mathrm{bol}}) - 0.288.$$

Stars with atmosphere

$$\log \pi = -6\log \frac{c_2}{T} + \frac{5}{6}\log \frac{\mathfrak{M}_4}{\mathfrak{M}_A + \mathfrak{M}_B} + \frac{5}{2}\log a - \frac{5}{3}\log P + \frac{3}{10}(m + 5 + \Delta m_{\text{bol}}) + 0,546.$$

Computing the parallaxes and comparing with those actually determined RABE has found the mean error of one value to be  $\pm 0.295\pi$ .

The mass-ratio of stars where both the spectra have been observed but no orbital elements are known can be computed from the formula

$$\log\left(\frac{\mathfrak{M}_B}{\mathfrak{M}_A}\right) = \frac{9}{25} \left[ 20 \left( \log \frac{c_2}{T_B} - \log \frac{c_2}{T_A} \right) - (m_B - m_A) - (\Delta m_B - \Delta m_A) \right]$$

<sup>&</sup>lt;sup>1</sup> Zf Phys 6, p 40 (1921), Ap J 50, p 220 (1919), Phil Mag (6) 40, p 809 (1920), 41, p 267 (1921), London R S Proc (A) 99, p 135 (1921)

The following table summarises the results of RABE

Spectral class	Temperature T	18	e	-	
Λ 2,3	9400°	2,29 0	0,43 @	1,74 ①	3
17 3,4	7900	2,78	0,77	1,42	11
17 8,0	6600	1,07	0,98	1,02	8
G 1,0	6400	0,92	0,98	0.96	12
G 6,0	6100	0,88	1,22	0,88	10
K 1,7	5600	0,61	1,27	0,78	9
K 5,0	5000	0,69	1,96	0,70	8
M 2,5	3800	0,36	3,58	0,45	4

The diameters d are accurately represented by means of the linear relation d = 1.03 + 0.00023 (T - 6500°).

In a subsequent paper RABB¹ has taken up a remark by BRILL that the mass and the surface temperature cannot be considered to be independent of each other. In order to decide between the influence of the temperature and the mass upon the absolute magnitude it is appropriate to consider stars of unequal mass but of the same spectral class. RABB used a number of new data, but could not find that his general conclusions ought to be changed. In order to show that the correlation between mass and luminosity is not as high as is generally believed he quotes the following well-determined cases where the absolute magnitude has been computed from Eddington's mass-luminosity law.

Object	Spentrati olean	æ	<b>H</b> <sub>₹</sub>	Mod	M <sub>essle</sub>	Make - Mark
Pogasi A y Virginis A Pogasi B r Cygni A Procyon A Bcorpdi A 9 Argus A B Sun F Urs Majoris A	F3 F0 (F5) F1 F5 F2 G0 (G2) G0 F9	8,60 © 4,48 4,00 2,48 1,13 1,02 10,96 4,38 1,00 0,68	1 <sup>11</sup> ,79 2 ,39 2 ,29 2 ,14 2 ,92 3 ,04 3 ,46 4 ,06 4 ,06 4 ,90 5 ,26	1 x,78 2 .37 2 ,29 2 .12 2 ,92 3 ,03 3 .43 3 .98 4 .89 5 ,25	-2 <sup>M</sup> ,42 -0 ,85 -0 ,45 0 ,96 3 ,92 4 ,29 -2 ,79 -0 ,41 4 ,56 6 ,28	+4*,20 +3 ,22 +2 ,74 +1 ,16 -1, 00 -1 ,26 +6 ,22 +4 ,39 +0 ,33 -1 ,03

The difference  $M_{obs} - M_{calc}$  shows such a definite dependence on  $\mathfrak{M}$  that it seems to indicate that M does not depend on  $\mathfrak{M}$  in such a high degree as was producted in the theory of Eddington.

The author gives the following mass-luminosity-temperature relation.

Special ciam	Absolute magnitude	Temperature T	198	o./T
В0	-3 <sup>M</sup> ,0	20400°	15.7 O	0,70
D5	-0,4	12400	7.2	1,15
ÃO	+1 ,1	9800	3,8	1,45
	1 ,9	8900	2,2	1,60
A5	2 ,5	8200	1,8	1,74
FO		7300	1,4	1,9
IT5		6500	1,10	2,20
Go	4 .5	6100	0,94	2,33
G5	5,2	5800	0,75	2,47
Ko		5000	0,63	2,8
K5 Mo	7 ,6	4200	0,43	3,4

<sup>1</sup> AN 231, p 79 (1927).

289. Convergence of Mass-Ratios with Increasing Age. One of the important consequences of the theory of Eddington was pointed out by Vogt<sup>1</sup>. It follows from the theory that \( \Delta N/\mathbb{M} \) varies in direct proportion to \( \mathbb{M} \). In the case of double stars the mass-ratio  $\mathfrak{M}_A/\mathfrak{M}_B$  must thus become smaller and more nearly equal to one the "older" the pair is. Vogr mainly made use of 85 double stars in LEONARD's dissertation<sup>3</sup>. The mass-ratios were not known and had to be computed from Eddington's mass-luminosity relation. In the table giving the results  $S_A$  denotes the spectral class of the principal star.

$S_A$	MA/MB	п	$S_A$	MA/Ma	#
gM	18,4	2	A	1,6	9
$\mathbf{g}\mathbf{K}$	2,7	6	dF	1,3	23
gG	1,9	9	dС	1,25	18
$\mathbf{g}\mathbf{F}$	3,0	5	dK	1,23	11
$\mathbf{B}$	4,6	8	$d\mathbf{M}$	1,19	2

In order to investigate the possibility that the mass becomes smaller with the age of the star, one can also make use of the relation;

$$\frac{\Delta \mathfrak{M}_A}{\Delta \mathfrak{M}_B} \sim \frac{L_A}{L_B}$$
,

where L is the luminosity. Voct computes the values  $[\mathfrak{M}_A/\mathfrak{M}_B]$  for a double star whose principal component is of spectral class A with a mass of 2,5 @ and  $\mathfrak{M}_A/\mathfrak{M}_B=1.6$  and whose components undergo in the course of evolution a massreduction in proportion to their luminosities. These values compare with the mass-ratios actually derived in the following way;

SA	P.KB	MA/MB]obs	[W.1/W.B]0.
A F G K M	2,5 1,5 1,0 0,7 0,4	1,6 1,3 1,25 1,23 1,19	1,6 1,2 1,10 1,06 1,04

According to Voct the probability is thus comparatively great in favour of the opinion that the Russell diagram gives the general course of stellar evolution,

240. Vogr's Extension of EDDING-TON'S Theory. The theory of EDDINGTON

is based on the assumption that the product kQ is constant, where k is the coefficient of mass-absorption and Q the mean value of the energy produced per unit mass and time within a sphere with the radius r. H. Vogra has derived the mass-luminosity relation in the case when kQ is not constant, but varies in some general way with r. The two fundamental equations give:

$$L = \frac{4\pi_c a cg r^2}{3k} \frac{dT^4}{dP} = \frac{4\pi_c cG}{k} \mathfrak{M} (1-\beta) \left[ 1 + \frac{P}{1-\beta} \frac{d(1-\beta)}{dP} \right],$$

where  $dP = -g \varrho dr$ ,  $P = \Re \varrho T/\mu + \frac{1}{3} a T^4$  or the sum of the gas-pressure and light-pressure, and  $g = G\mathfrak{M}/r^2$ .  $\mu$  is the molecular weight, g the gravitational force,  $\varrho$  the density, T temperature,  $\Re$  the universal gas constant = 8,26 · 107, and a Stefan's constant =  $7.63 \cdot 10^{-15}$ . L and M correspond to the values within a certain radius r, but their total values may be introduced if P,  $1 - \beta$ , and k are referred to the layers near the surface. The equation can be transferred by applying the relations:

the relations: 
$$T^4/T_1' = (1-\beta)/(1-\beta_1) \mathfrak{M}^2/R^4 \quad \text{and} \quad T/T_1 = \beta/\beta_1 \mathfrak{M} \mu/R$$

existing between  $1-\beta$ ,  $\mathfrak{M}$ , and  $\mu$  in the case of homologous stars. In these equations the subscript one refers to a homologous star of unit mass, the

<sup>&</sup>lt;sup>1</sup> Z f Phys 26, p. 139 (1924). 8 A N 226, p. 302 (1926).

<sup>&</sup>lt;sup>2</sup> Lick Bull 10, p. 169 (1923).

radius and mean molecular weight of which are equal to one. By eliminating Tbetween the above equations we get:

$$\frac{(1-\beta)}{\beta^4} = \frac{1-\beta_1}{\beta_1^4} \mathfrak{M}^{\bullet} \mu^4 = \varphi(\mathfrak{r}) \mathfrak{M}^{\bullet} \mu^4,$$

where  $\varphi(t)$  is a function of the distance t from the centre of the star expressed in units of the radius r. It follows from the last equation that;

$$\frac{1}{1-\beta}\frac{d(1-\beta)}{dt} = \frac{\beta}{4-3\beta}\frac{1}{\sigma(t)}\frac{d\sigma(t)}{dt}.$$

Further:

$$\frac{1}{a} = \frac{1}{P} \underbrace{\frac{dP}{dt}}_{\frac{1}{\varphi(t)} \frac{d\varphi(t)}{dt}}$$

is introduced. The luminosity-mass equation then becomes:

$$L = \frac{4\pi \cdot oG}{\hbar} \mathfrak{M} (1-\beta) \left[ 1 + a \frac{\beta}{4-3\beta} \right].$$

The coefficient of absorption k corresponds to the homologous niveausurfaces, and its dependence upon  $\mathfrak M$  and R can be taken  $\sim \varrho^1 T^*$  where  $\lambda$  and F are arbitrary powers of the donsity and of the temperature. A is then brought into the form:

$$h = \text{const} (1 - \beta)^{r/4} \Re^{1+r/3} / R^{3+r}$$

Further  $L = 4\pi R^{\frac{1}{2}} + aoT^{\frac{1}{2}}$  and R can thus be eliminated and the effective temperature substituted.

In reality AQ is not such a function of P, T and Q that the stars are homologous systems,

Because of that, a and  $\varphi(t)$  will vary with  $\mathbb{R}$  just as the density-distribution

varies from star to star with the total mass.

241. Statistical Investigations Concerning the Mass-Ratio in Binaries. E. B. WILSON and W. J. LUYTEN<sup>1</sup> have used accurate mass-ratios for 69 spectroscopic binaries for a statistical investigation. By taking z = log Ra/Ma and by taking the mass-ratios m, and m, both ways in each pair a symmetrical distribution was necessarily obtained of the 138 values of z. The dispersion og is ±0,26 ±0,02 and the ratio of the fourth moment about the mean to the square of the second moment about the mean is 4,3 ± 0,4, whereas a normal error curve gives 3.0. In a previous note the authors have found for 14 binaries and the Sun the value of the dispersion of log IR to be 0,36 ± 0,03. The value of σ for the logarithm of the mass-ratios of these 14 systems is 0,30 ± 0,04.

If 7 is the coefficient of correlation between the logarithmic masses of the components in binaries we have:

$$r = 1 - \sigma_s^3/2\sigma^3$$

By using the above data r is found to be 0,74 and thus there appears to be a high degree of correlation between the masses in the pairs or a great tendency for the masses to be equal, which is also a very general assumption. It should not be overlooked, however, that there is probably a strong observational selection at work The authors inquire what would be the standard deviation of a for the statistical distribution of the 406 hypothetical binaries that could be constructed by pairing in all possible ways the 29 stars used in a previous note (see ciph. 219)

<sup>1</sup> Wash Nat Ac Proc 10, p. 433 (1924).

with  $\sigma = \pm 0.36$ . They find  $\sigma'_x = 0.50$  or nearly double the value of  $\sigma_x$ . In the material of 69 actual binaries that was investigated there is not one with a mass-ratio greater than 5, whereas in the 406 hy pothetical binaries there are 79. Assuming that these high mass-ratios, if they existed, would not be observed and measured the authors find for the remaining 327 pairs a dispersion of 0.31, which is not far from the value of 0.26 that is actually found.

The following table is computed on the basis of the material available:

$\mathfrak{M}_B/\mathfrak{M}_A$	Discovery- chance	Luminosity ratio	Wa/WA	Discovery- chance	Lumbosity ratio
1/20 1/10 1/5 1/3	1/9000 1/220 1/14 1/3,7	1/100000000 1/400000 1/25000 1/600	1/2 1/1,5 1	1/1,6 1/1,2 1	1/70 1/11 1

In view of the very great luminosity ratios it might appear reasonable to believe that the discovery-chances have been overestimated, and that when the discovery-chance is considered the observed mass-ratios are more scattered than would be the case if the two components were selected at random. It seems that there is considerable probability that the apparent clustering of the mass-ratios about unity is due to observational selection.

242. Theoretical Derivation of the Mass-Ratio in Double Stars. The question whether the Russell-diagram represents loci of equilibrium during the evolution course or an actual course of evolution ought, as has been pointed out by G. Shajn¹, to benefit from an examination of double stars. Because of the equation  $\Delta m = \Delta M$  we can write, applying Eddington's theory and denoting the secondary by the subscript A and the primary by B,

$$-0.4 \, dm = \frac{7}{4} \left( \log \mathfrak{M}_A - \log \mathfrak{M}_B \right) + \frac{9}{4} \left[ \log \left( 1 - \beta_A \right) - \log \left( 1 - \beta_B \right) \right] + \frac{4}{4} \left( \log T_A - \log T_B \right).$$

The mass-ratio cannot be determined without a knowledge of the temperature and of  $\frac{1-\beta_A}{1-\beta_B}$  as a function of  $\frac{\mathfrak{M}_A}{\mathfrak{M}_B}$ . The observational material was augmented by using systems for which the absolute magnitude is known only by indirect or statistical methods. Thus computations were made for 342 systems, most of which are certainly physical pairs. The results are summarised as follows:

Giants			Dwarfs		
Spectral index	WA/WA	n	Spectral index	101A/101B	п
0,0-0,4 0,5-0,9 1,0-1,4 1,5-1,9 2,0-2,4 2,5-2,9 3,0-4,5	0,88 0,72 0,66 0,62 0,45 0,56 0,37	78 12 33 20 18 9	0,0-0,4 0,5-0,9 1,0-1,4 1,5-1,9 2,0-4,5	0,88 0,85 0,70 0,63 0,35	65 16 15 12 4

For systems with components of B stars the values of  $\mathfrak{M}_A/\mathfrak{M}_B$  for the first three spectral intervals are: 0,68, 0,41, and 0,34 respectively. The fact that the spectral index increases with  $\Delta m$  and the result of Leonard that in giant systems the spectrum of

the companion belongs to an earlier class than that of the primary, whereas in the dwarf systems the spectrum of the secondary is of a later class, lead to the conclusion that these relations indicate the course of the stellar evolution, which will be that indicated by Russell.

<sup>1</sup> M N 85, p. 245 (1925).

<sup>&</sup>lt;sup>2</sup> Lick Bull 10, p. 169 (1922).

ATTERN 1 has shown that the mass-ratios of spectroscopic bluaries increase with advancing spectral class from B to G. The same relation results from SHAIN'S material

БКАЈИ			Arress		
Spectral class	<b>四点图</b>	A	Spectral class	<b>深山田</b> 。	
110-139 A0-A9 F0-F9	0,60 0,77 0,78	50 69 109	B0-B8 B9-A5 F	0.70 0.75 0.92	11 16 3

SHAJN does not think that these facts can be taken as proving that a gradual decrease of mass takes place during the lifetime of a star The existence a priori of systems of very unequal masses can be expected. Further, the two spectra are not independent of each other. When the primary is M or K, the companion

may exhibit a spectrum of gM-A, but very seldom of a late spectral class. In a dwarf system of, say, class K the spectrum of the secondary is dK or dM Thus it is natural to expect an average decrease of ASp with increasing Ma/Ma as is actually found.

248. LUNDMARK'S and LUYTER'S Differential Method . The statistical relationship between the two forms of energy in the stars, the radiant energy, expressed as absolute magnitude, and the inert energy, expressed as mass, was derived from differential data of spectroscopic binaries When both spectra of a spectroscopic binary have been observed an accurate value for the mass-ratio or Alog M is found from the amplitudes  $K_1$  and  $K_2$  by means of the relation:

$$-d\log \mathfrak{M} = \log K_1 - \log K_2 = a.$$

In many cases there are estimates of the relative brightness of the two spectra and thus also the

and

difference in absolute magnitude  $\Delta M$  can be determined. If the spectroscopic binary is an Algol variable the value of AM can be determined comparatively accurately from the determination of the orbit.

parallax are known (Compare fig. 154.) Suppose we have the relation.

Fig 158 The relation between absolute magnitude and mass as integrated from mass-ratios

and differences in luminosity in spectroscopic

binaries. For comparison purposes Econtecton's curve [M N 84, p. 308 (1924)] has been inserted

and the curve derived on beats of double

stars for which the orbital elements and the

$$M_A = f(\log \mathfrak{R}_A),$$

$$M_B = f(\log \mathfrak{R}_B),$$

$$M_A = \psi(M_B).$$

The problem is then to solve the equation:

$$/(\log \mathfrak{M}_A) = \psi[/(\log \mathfrak{M}_A + a)]$$

The Binary Stars, p 207 New York (1918)
 Ark Mat Astr Fys 20 A, No 18 (1927); Upsale Modd No. 34.

or to determine the form of when  $\psi$  and a are given. In practice it will be sufficient to use a graphical method and to construct the curve  $M = f(\log \mathfrak{M})$  from values of  $\frac{d \log \mathfrak{M}}{dM} = \frac{d \log \mathfrak{M}}{dM}$  for given values of M. The following mean values for the differential quotient were obtained:

MAD	A log M	1)	Ман	A log Wi	11
Brightost to $-2^{M},0$	-0,168	4	$+2^{11}$ ,0 to $+4^{11}$ ,0	-0,060	6
$-2^{M},0$ ,, 0,0	-0,221	16	4,0,, 6,0	-0,060	9
0,0,, $+2$ ,0	-0,102	17	6,0,, faintest	-0,073	3

As constant of integration the value  $\mathfrak{M}=1\odot$  for M=5.0 was selected. The following relation resulted:

M	logW	M	ы	log NR	M
-2 <sup>N</sup> ,0 -1,0 0,0 +1,0 2,0	0,780 0,595 0,410 0,295 0,195	6,0 ⊙ 3.9 2,6 2,0 1,6	+5 <sup>M</sup> ,0 6,0 7,0 8,0 9,0	0,000 0,060 0,130 0,200 0,275	1,0 0,87 0,74 0,63 0,53
3,0	0,130	1,3	10 ,0	-0,350	0,45

The agreement between this curve and that derived by Eddington is comparatively good. The values  $\Delta M$  were not reduced to bolometric magnitudes, but an inquiry has shown that such a reduction will not materially change the results. The same applies to the inclusion of new material available.

244. The Masses and Luminosities of the Eclipsing Binaries. Dean Mc Laughlin<sup>1</sup> has discussed the contribution of the eclipsing variables to stellar luminosities and masses. Altogether 48 eclipsing stars have been observed for radial velocities. In 28 cases the two spectra have been measured and in 3 others the rotation effect has been observed. In 21 cases the mass-ratio is known from the amplitude-ratio  $K_1/K_2$ . The mass-ratio has been plotted against  $L_A$ , the luminosity of the brighter star, and a smooth curve has been drawn. From this curve the value of the mass-ratio corresponding to any value of  $L_A$  could be read. It was then possible to calculate the hypothetical mass of each component. Altogether the masses have been calculated in 41 systems, and in 38 of these linear dimensions and densities are known. Hence absolute magnitudes and hypothetical parallaxes may be calculated. By using Seares's values for surface brightness  $J_A$  the formula:

$$M_A = J_A - 5\log r_A + 4.75,$$

where  $r_A$  is the geometrical mean of the major and minor axes of the star, gives the absolute magnitude. The apparent magnitude  $m_A$  of the bright component alone is obtained from:

$$m_{AB} - m_A = 2,5 \log(1 - L_A),$$

where  $m_{AH}$  is the apparent magnitude of the system at maximum brightness. Then:

$$\log n = 0.2 (M_A - m_A) - 1$$

gives the hypothetical parallax. Further:

$$\Delta M = m_B - m_A = 2.5 \log[L_A/(1 - L_A)].$$

<sup>&</sup>lt;sup>1</sup> A J 38, p. 21 (1927).

<sup>&</sup>lt;sup>2</sup> Ap J 55, p. 198 (1922).

The bolometric magnitudes have been calculated from the formula given by RDDINGTON.  $M_{bol} = 4.75 - 5.0 \log r_{A} - 10 \log T_{A}/5860^{\circ}$ 

The bolometric magnitudes have been reduced to Eddington's standard curve for  $T_{\bullet}=5200^{\circ}$  by applying the temperature correction term:

$$2\log\frac{T_*}{5200^\circ}.$$

The Russell diagram shows that the dwarf sequence is well determined by the eclipsing binaries. Yellow and red giants are almost totally lacking. The relation of mass to spectral class is shown in the following synopsis.

Spectral class	-	Blam	Palm
O8,5	35 O	2	4
B0-B2	16,6	6	4
B3-B5	5,2	12	8
B8-A0	3,1	18	14
A2-A8	2,7	- 8	5
FO-F5	0.7	5	5 3
F8-G5	1,1	10	5
Mi	0,6	2	1

Then the mass-luminosity diagram was formed The scattering around the relation curve was found to be comparatively large. The sources of appreciable errors must be limited to the radii and the effective temperatures. It does not seem likely that in any case errors of the radii could affect the result by as much as one magnitude, which would correspond to an error of roughly 30%

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in the radius. The effective temperature should not introduce an error greater than half a magnitude. Thus a deviation of 1<sup>M</sup>,5 ought to be relatively infrequent, but at least five well-determined stars equal or exceed that limit, and several others of less certain mass so far exceed it that no reasonable adjustment of temperature will bring them within 1<sup>M</sup>,5 of the relation curve. The author is of the opinion, which is also shared by me, that we are not justified in saying that the mass and effective temperature of a star determine a unique value of the luminosity.

Mc Laughlin has pointed out that if there is a strict one-to-one correspondence between mass and luminosity within a group of stars with the same effective temperature but with different masses, the density of each star would be uniquely determined. The curves of constant dimensions and temperatures have been calculated from Eddington's mass-luminosity relation. The figure provides a check on the calculated density, since the point for any given star will fall in a position corresponding to the assumed radius, regardless of whether the star satisfies the theory or not.

Few of the stars show such great deviations from the theoretical densities that the calculated ones would have to be multiplied or divided by 8 or a greater factor. It is very doubtful whether as great a change of radius as 30 per cent would be permissible in any of these cases. Considerable deviations are also shown in other cases. Nor would an adjustment of the scale of effective temperatures remove the disagreement between observation and theory.

246. The Upper Limit for the Stellar Masses. H. Voot has discussed this important question<sup>1</sup> The observations suggest that an upper limit exists and the theory concerning the interior of the stars indicates that unstable conditions must arise as soon as the radiation prossure equals the amount of the gas pressure. Voot assumed an arbitrary law of density distribution within a star (q = F(r)) possessing spherical symmetry. The amount of energy  $L_r$  passing in unit time through the niveau-surface at a distance r from the centre is

$$L_r = -\frac{4\pi_s a c r^4}{3h\rho} \cdot \frac{dT^4}{dr},$$

<sup>1</sup> A N 230, p 241 (1927)

$$L_r = \frac{4\pi_e cG}{k} \mathfrak{M}_r (1-\beta) \left[ 1 + \frac{P}{1-\beta} \frac{d(1-\beta)}{dP} \right],$$

where  $\mathfrak{M}$ , is the mass within the distance r. If a star is compared with a homologous star with  $\mathfrak{M}=1$ , R=1, and the mean molecular weight m=1, the following relations exist:

$$T^4/T_1^1 = (1 - \beta)/(1 - \beta_1) \, \mathfrak{M}^2/R^4$$
,  
 $T/T_1 = \beta/\beta_1 \, \mathfrak{M} \, m/R$ .

Putting:

$$\varphi(\mathfrak{r})=(1-\beta_1)/\beta_1^1,$$

we have:

$$(4 - \beta)/\beta^4 = \varphi(\mathfrak{r}) \mathfrak{M}^2 m^4$$

from which we obtain:

$$\frac{1}{1-\beta} \cdot \frac{d(1-\beta)}{d\tau} = \frac{\beta}{4-3\beta} \cdot \frac{1}{\varphi(\tau)} \cdot \frac{d\varphi(\tau)}{d\tau} ;$$

combining with the equation for  $L_r$  we obtain:

$$L_r = \frac{4\pi_e c G}{k} \mathfrak{M}_r (1 - \beta) \left[ 1 + \psi(\mathbf{r}) \frac{\beta}{4 - 3\beta} \right]$$

where:

$$\psi(\mathbf{r}) = \frac{1/\varphi(\mathbf{r}) \cdot d\varphi(\mathbf{r})/d\mathbf{r}}{1/P \cdot dP/d\mathbf{r}} = \frac{1/\varphi(\mathbf{r}) \cdot d\varphi(\mathbf{r})/d\mathbf{r}}{1/P_1 \cdot dP_1/d\mathbf{r}}.$$

Denoting by  $Q = L_r/\mathfrak{M}_r$  the mean energy produced we have:

$$kQ = 4\pi_0 c G (1-\beta) \left[1 + \psi(\mathfrak{r}) \cdot \beta/(4-3\beta)\right].$$

The equation says that within homologous stars the quantity kQ varies comparatively little as the mass becomes larger. It is also clear that when we are considering very heavy stars, a small change in the function kQ will correspond to a change in  $\psi(\mathbf{r})$  that is as much larger as is the value of the mass. If the mass approaches an infinite value, the formation of a star is only possible if kQ is independent

of r and has a constant value equal to  $4\pi_{c}G$ .

If kQ is not a constant, but proportional to a function of r, it can be shown that  $1-\beta$  reaches, either in the central parts or in the shells near the surface, the value 1 according as kQ increases as we proceed to or from the centre. Then the upper limit for the value of the mass is reached, as every further contribution of matter to the star will be driven away by the radiation pressure. — In reality the condition kQ = const. will not be fulfilled in the interior parts of a star, because it is very unlikely that the quantity kQ is such a function of temperature, density, and pressure that it would have a constant value for such a distribution as corresponds to the condition kQ = const. Already for that reason the masses of the stars must have an upper limit.

In the preceding lines it is assumed that the stars do not rotate. If rotation

is taken into account the conclusions will remain principally unchanged.

The question whether an upper limit exists for the stellar masses has also been discussed by W. Anderson<sup>1</sup> and later by G. I. Pokrowski<sup>2</sup>. The former starts from the energy formula:  $E = \frac{3kM^3}{5r}$ ,

where k is the constant of gravitation, E the potential energy, and r the radius. The formula is valid if infinitely scattered matter is united into a homogeneous sphere (star) of radius r. In the cosmical cloud from which the sphere is formed

<sup>&</sup>lt;sup>1</sup> A N 218, p. 205 (1923); Z f Phys 53, p. 597 (1929). 
<sup>2</sup> Z f Phys 49, p. 587 (1928).

the potential energy E is assumed to have been uniformly distributed If the material mass of this cloud is  $\mathfrak{M}'_1$ , the mass corresponding to E  $\mathfrak{M}_2$ , the mass of other energy present  $\mathfrak{M}''_1$ , and the total mass  $\mathfrak{M}$  so that

$$\mathfrak{M}=\mathfrak{M}_1+\mathfrak{M}_1'+\mathfrak{M}_2=\mathfrak{M}_1+\mathfrak{M}_2,$$

we have  $\mathfrak{M}_{\mathbf{a}} = E/c^{\mathbf{a}}$ , where c is the velocity of light. The above equation can then be transformed into

 $E^2 - \left(\frac{5rc^4}{2k} - 2\mathfrak{R}_1c^2\right)k + \mathfrak{M}_1^2c^4 = 0.$ 

which when solved gives

$$L = \frac{57c^4}{6k} - \mathfrak{M}_1 c^6 + \left| \frac{257^4c^4}{36k^4} - \frac{57c^4 \mathfrak{M}_1}{3h} \right|^{\frac{1}{4}}$$

E has thus real values only when

Thus the mass of a star has an upper limit A maximal value of MR is derived from the above inequality and this gives a maximal value for the total mass of the cosmical cloud

 $\mathfrak{M} = \frac{5rc^2}{6k} = \begin{pmatrix} 5 \\ 6 \end{pmatrix} \begin{pmatrix} c^2 \\ 2 \end{pmatrix} \begin{pmatrix} 3 \\ \pi \cdot o k^2 \end{pmatrix}^{\frac{1}{2}},$ 

where  $\rho$  is the density of the star

In an analogous way Pokrowski has derived a maximum value that only differs from that of Anderson in the respect that the numerical factor (1) is not present

The upper limit corresponds to a value of log M = 35 and thus enormous masses could exist

246. Relation between Stellar Mass and Proper Motion. When the masses of visual double stars are being derived the great difficulty is the determination of the parallex. The data must necessarily be selected. The systems for which orbits have been determined must either be exceptionally massive or the linear separation must be relatively small. It seems very reasonable to suppose that the latter provides the greater part of the explanation.

J Jackson<sup>1</sup> has tried to use the proper motion instead of the parallaxes in order to test the masses independently. The proper motions were divided by the dynamical parallaxes  $\pi_{\ell}$  and the resulting linear motions analyzed by Airy's method. The following results were found

Stars with known orbita

Squateal rios	Conditates of apex	Velocity astr mate per year	199	•
A2	258°,5   32°,0	2,18	13,4()	21
1/5	267 ,5   20 ,1	3,07	4,81	52
(12	290 ,6   41 ,6	4.79	1,27	30
K2	269 ,3 + 10 ,2	8,17	0,26	12

Stars with short arcs only

Apentral alives	Countinates of apex	Velocity nate units per year	TO.	
136	278°   32°	2.07	12,6 ②	24
A2	267 ,2 + 35 ,8	2.16	11,02	83
1:4	261 ,0   24 ,2	3.91	1,87	102
(-3	293 ,6   41 ,7	6.63	0,38	74
K1	269 ,3   25 ,6	4.87	0,96	42

<sup>1</sup> MN 83, p. 444 (1923)

A comparison was made with the mass values of Seares. The agreement is good when the fact is taken into account that Seares's results refer to geometrical mean masses and Jackson's to  $[\overline{\mathfrak{M}}]^3$ . Owing to the small dispersion in  $\mathfrak M$  the two values do not differ much.

The present writer has derived a mass-proper-motion relation. The derivation of the masses on the basis of spectral proper-motion parallaxes has convinced me that it will be possible to find a rather definite relation between  $\mathfrak{M}$  and  $H=m+5+5\log\mu$ . Such a relation will be of use for deriving the frequency of stellar masses from the frequency of absolute proper-motion magnitudes.

Using 62 cases of well-determined individual masses the following relation

has been found by a least-squares solution;

$$\log \mathfrak{M} = 0.9750 - 0.1021 H + 0.00131 H^2.$$

Using the relation between mass and absolute magnitude as derived in ciph. 232 (p. 666) and making the assumption that M = H - 5.6 the following formula was found:  $\log \mathfrak{M} = 1.6262 - 0.2037H - 0.00412H^3$ .

247. Relation between Stellar Mass and Form of Orbits of Binary Stars. Already in the early material it seemed suggested that there is a relation between the total absolute magnitude and excentricity of binaries. As the difference in mass  $\Delta \mathfrak{M}$  is directly dependent upon the difference in M the existence of the thought relation would prove a relation between stellar mass and form of the orbit of double stars. It seems obvious that no definite relation can be established. Using different determinations of trigonometric and spectrographic parallaxes of stars the absolute magnitudes of 347 binaries have been approximated by  $\mathfrak{m}^{cl}$ . The coefficient of correlation between excentricity, c, and absolute magnitude M was found to be:

$$r = +0.388 \pm 0.048$$

and the regression lines:

$$M = 0.360 \, e + 1.586$$
,  
 $e = 0.032 \, M + 0.273$ .

The correlation found is not very high but should probably be taken as real. This result has been doubted by H. Siedentoff<sup>2</sup> who finds when treating the spectroscopic and the visual binaries separately no correlation between M and e and thinks that the correlation above is spurious and a result of selection in the material<sup>3</sup>.

Earlier C. D. Perrine<sup>4</sup> has dicussed the question of a dependence of orbital excentricity upon the absolute magnitude of the components of binary stars. He used the difference  $\Delta M$  and compared with e and found the following relation:

Limits of s	ē	īMí	n
0,00 to 0,29	0,19	0,60	7
0,30 ., 0,44	0,37	1,29	16
0,30 ,, 0,44	(0,37)	(0,95)	(15)
0,45 ., 0,58	0,50	1,32	18
0,59 and larger	0,71	2.04	16
0,59 ,, ,,	$(0,71)^8$	(1,47)	(15)

<sup>&</sup>lt;sup>1</sup> Ark Mat Astr Fys 20 A, No. 12 (1927); Upsala Medd No. 20.

<sup>1</sup> Göttingen, Univ Sternw Veröff H. 3 (1928),

<sup>3</sup> If so the conclusions concerning stellar masses and their relation to luminosity will also be affected to a certain extent.

<sup>&</sup>lt;sup>4</sup> A J 33, p. 180 (1921).

<sup>&</sup>lt;sup>5</sup> Excluding 85 Pegasl.

<sup>&</sup>lt;sup>0</sup> Excluding Sirlus.

This seems to be a pretty well established relation but on another hand a similar grouping made by me on basis of 116 pairs and represented graphically in Fig. 159 does not seem to reveal any correlation between c and M. It thus seems that we have here one of the many problems where our present material is insufficient to give a definite answer upon the inquiry

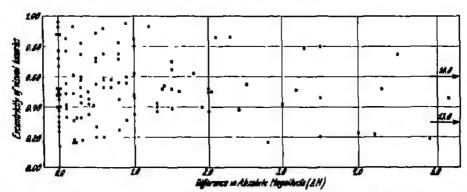


Fig. 159 Test for a supposed relationship between excentricity of visual binaries and the difference in absolute magnitude 4M between the components

248 The Mass of the Orion Nebula. The method of determining stellar masses is not restricted to the binary stars. It applies to every cases of a rotating body where the period of revolution can be determined for a particle at a certain distance. Thus the mass of the solar system could be approximated when an outside observer had observed the difference in velocity between the Sun and Neptune as soon as he had a knowledge of the linear distance between the two bodies

It was found by Fabry, Buisson, and Bourger when they were applying the interferometer method, that internal motions existed within the Orion nebula and that the character of the motion was that of rotation. Later on Campulla and Moore<sup>1</sup> determined the radial velocities of 96 points near the Trapezium. The motion is of rotational character, although considerable individual deviations occur. In order to determine the amount of rotation it has been assumed that the nebula rotates as a rigid body within a distance of 2' from the centre. With the aid of a least square solution the plane was found that gives the closest representation of the velocities. This corresponds to a rotational component in the radial velocity amounting to 5 km/sec at a distance of 2'

If M is the central mass and is the (infinitely) small mass of a particle at the distance r, v the linear velocity, and k the gravitation constant, we have

Or

where a" is the distance of the point considered in seconds of arc, v is the linear circular velocity at this point measured in km/sec. Next the parallax has to be derived. In a paper of mine still unpublished it has been found that the value:

$$\pi_{\text{Oring}} = 0'',0030,$$

Lick Publ 13, p 96 (1918).

derived from a discussion of absolute magnitudes, proper motions, motions of binaries etc., and the distribution of stars in front of the dark nebula accompanying the bright one is the best that can be derived from the existing data.

Thus the minimum mass of the nebula is found to be 48 0, which is not astonishing when one remembers that the trapezium-stars alone are certainly

very massive<sup>1</sup>.

The value thus derived is the minimum mass of the nebula; on account of that we cannot locate the axis of rotation and the observed rotation is thus a component of the actual rotation.

The method can also be applied to the anagalactic objects.

249. Planetary Nebulae. The central stars of planetary nebulae are O stars that evidently do not differ from the ordinary O stars in any other way except that they are surrounded by nebulosity. W. H. WRIGHT has said that the disparity among the central stars in planetaries is no larger than the disparity among non-nebulous O stars.

The extensive survey of the spectra of 125 bright-line nebulae at Lick Observatory has revealed the important fact that several planetaries show internal motions that are most likely interpreted in terms of rotational motions. The internal motions are in several cases of a very complicated nature and there are certainly other phenomena present that change the spectral lines, such as a possible extension or outward motion of the gaseous envelope, differential effects of radiation pressure, ZEEMAN or STARK effects, etc. Still, it seems to be justifiable to try to find a general rotational component.

In 23 cases it seems possible to derive a rotation component. The uncertainty is considerable, but still there seems no doubt that the planetaries are very massive

and bodies of a low temperature.

ObJe	ect	Distance from centre	Rotation component in km/sec	Parallax π	Mass of star and nobula	Density of central	Temperature of central star
NGC	1535	4",4	4,0	0",0017	46 ⊙	4390 ⊙	38 · 103
J 320	_	3 ,1	6,6	0 ,00062	240	22400	34 . 103
IC	2165	4 ,2	2,8	0 ,00025	149	9320	51 • 109
NGC	2392	15 ,0	16.0	0.0015	2900(?)	4470	27 · 109
	2452	10.0	14,0	0,00019	11500(?)	1000000000(?)	85 • 103
	3242	0, 13 5, 5	6,2	0,0018	156	40900	58 · 10 <sup>9</sup>
IC	4593	2,05	2,15	0,00095	13,3	480	22 · 10 <sup>3</sup>
NGC	6210	3 ,5 4 ,5	6,4 4,0	0 ,0014	113 57	7270 } 3650 }	36 · 10 <sup>9</sup>
	6543	3 ,5	5,0	0,0023	43.5	5600	40 - 103
	6565	3 ,0	7,0	_	-	-	
	6572	4,0	2,8	0,0019	19,4	540	31 · 10 <sup>a</sup>
	6567	1 ,8	7,5	0 ,0005	220	58000	45 · 10 <sup>a</sup>
	6720	25,0	2,0	0,0012	94	415000	72 · 10 <sup>3</sup>
	6741	4 ,1	2,4	0,00025	107	128 000	58 · 10 <sup>9</sup>
	6807	1,0	4.3	0 ,00019	1100	2860000	66 • 108
	6818	9,0	2,4	0 ,0011	54	2090000	70 - 103
	6826	10 ,4	4,0	0 ,0020	94	4820	34 · 10 <sup>3</sup>
TO	6886	2 .8	5,0	0 ,00032	250	156000	52 - 100
IC	4997	2 ,4	5.7	0 ,00019	460	26800	35 • 103
NGC	7009	{4 ,5 9 ,0	4,5 6,1	0,0029	36 132	178 000 } 650 000 }	50 · 103
	7026	3 .7	18,4	0 ,00045	3100	8140000	45 • 100
	7027	5 ,5	10,0	0 ,00044	1420	18000000	86 · 10a
	7662	5 ,6	8,0	0 ,0018	230	151000	52 · 10 <sup>9</sup>

Land Obs Circ 3, p. 64 (1931).

To this table should be added the remark that the densities have been computed on the assumption that all the mass is concentrated into the central star. This seems reasonable when one considers recent work concerning the formation of gaseous nebula.

The parallexes are generally the ones derived by H Zanstra<sup>1</sup> In some cases parallexes have been derived by me according to the same method. The

same applies to the temperatures of the central stars

Although the dispersion in the density values is considerable there seems to be a rather definite relation between the temperature and density. Thus

T	8
32(NK) °	3 800
17 (XX)	38000
75 (XX)	6000000

This may be due to a systematic error in the temperatures but it might also be a real phenomenon. It is interesting to see that the densities, although high in many cases, still are not above the upper limit assigned to the density of matter. Thus E C Stonker has on basis of Lodington's theory on stellar evolution computed an upper limit for the central densities of the stars on reasonable assumptions, he finds this limit to be 5 10° ©.

260. Mass of the Stellar System. The total mass of the stars in the Milky

Way System is given by

$$\mathfrak{M}_{\mathrm{tot}} = N \iiint \mathcal{D}(\alpha, \delta, r) \, \mathfrak{M}(M, \alpha, \delta, r) \, d\alpha \, d\delta \, dr \, dM$$
,

in which  $\mathfrak{M}(M, \alpha, \delta, r)$  is the mass of an individual star of absolute magnitude M at the point  $\alpha, \delta, r$ , and N the number of stars per cubic parsec in

the vicinity of the Sun

At present we cannot suppose anything else than that the mean mass of a certain number of stars is the same everywhere, that is, that  $\Re(M, \alpha, \delta, r)$  is independent of position Luytun has adopted the density law of Kapteyn. The above formula simplifies to

$$\mathfrak{M}_{\mathrm{lot}} = \overline{\mathfrak{M}} \cdot N_{\infty}$$

where  $N_{\infty}$  is the total number of stars in the universe and is obtained by means of the relation

$$N_{\infty} = 0.0451 \int_{0}^{\infty} 4\pi_{\rm e}(5,102)^{2} \varrho^{2} \Delta (\varrho) d\varrho$$

 $\varrho$  being the polar semi-diameter of the homologous ellipsoids around the Sun and  $\Delta(\varrho)$  the density of stars in space. Further according to Kapteyn

$$\log \Delta(\varrho) = -5.356 + 4.890 \log \varrho - 1.200 \log^2 \varrho$$

LUYTEN funds:

$$N_{\infty} = 1.5 \cdot 10^{\circ}$$
.

For IR he adopts 0,945 0 and thus

Z f Astrophys 2, p 329 (1931)
 Harv Ann 85, No. 5 (1923)

MN 92, p. 662 (1932)

The value of  $N_{\infty}$  is perhaps six times too small, as is suggested if we adopt the results of Seares. On the other hand Luyten's value of  $\overline{\mathfrak{M}}$  seems to be too large. I have adopted  $\mathfrak{M} = 0.6 \odot$ . Thus the total mass should be:

$$\mathfrak{M}_{\rm tot} = 5.4 \cdot 10^9 \odot.$$

251. The Masses and Mass-Ratios of Stellar Systems. In 1916 V. M. SLIPHER<sup>2</sup> announced that the spiral nebula NGC 4594 rotates in its own plane approxmately as a rigid body. This conclusion was confirmed by the subsequent work of F. G. Peases at Mount Wilson. Later on the rotational motion of the Andromeda nebula was also established by means of the measurements of Pease and ADAMS4. Already in 1914 M. WOLF5 had found a rotational component in the motion in Messier 81, but details were not published until later on. The results given below for Messier 33 and Messier 51 are poor, as the rotational motion is based on the difference in motion between the centre and one outside object in each case, NGC 598 and NGC 5194, respectively.

The method of computing the mass is the same as in the case of double stars. Uncertainties are involved principally on account of the uncertainties in the parallax adopted and the inaccuracy in assuming that the inclination of an anagalactic object is derived from its ellipticity.

C	Object	Wiot.	Mtot
Audromeda	Nebula	1,8 · 109	-17,8
		7.6 - 1011	-24.2
		3 + 1010	17,0
Messier 33		1.5 - 1010	15.1
Messier 51		1 1010	-16.0
Our Milky	Way System .	1 1011	- 16

The mass derived from values for the spectrographic rotation is dependent on the immediate effect of the gravitation. The gravitational mass thus also includes the dark matter within the anagalactic objects, such as extinct stars, dark nebulae, and meteors. On the other hand an approximation of the mass of an anagalactic object can be derived from the total absolute magnitude. This involves the assumption that the mass-luminosity relation is the same in different parts of the universe. On account of the fact that the proportions of different spectral classes within different galaxies do not vary considerably, and that hence the luminosity curve seems to be rather equal, it seems justifiable to assume as a first approximation the universality of the mass-luminosity relation. The luminous mass so derived does not include the dark matter and thus it will be possible to obtain an approximation of the ratio, Dark matter/Bright matter, in the cases where both the mass-values have been estimated.

Ratio: Dark + bright matter
Bright matter

	u u			
Object	Ratio	()bject	Ratio	
Messier 84	30:1	Messier 51	10:1 6:1 10:1	

<sup>1</sup> Mt Wilson Contr No. 301 (1925); Ap J 62, p. 320.
3 Wash Nat Ac Proc 2, p. 517 (1916).

Wash Nat Ac Proc 4, p. 21 (1918).

VJS 49, p. 462 (1914).

Upsala Medd No. 40; Ark Mat Astr Fys 21, No. 10 (1928); Popular Astronomisk 8 V J S 49, p. 162 (1914). Tidskrift: 10, p. 19 (1929).

In the case of double nebulae the mass-ratio of the components can be determined from measurements of the spectrographic rotation. Let two particles, in each of the two components, be at the same angular distance d'' from the centre, then their linear distances are equal and the mass-ratio will be

$$\mathfrak{M}_h/\mathfrak{M}_A = V_h^1/V_A^2$$

where  $V_A$  and  $V_B$  are the circular velocities at the said distance. The application of the method will involve much observational work, but it does not seem to be impossible to find cases where one ought to be able to photograph both the spectra of regions at such distances from the nucleus that decent values of  $\mathfrak{M}_B/\mathfrak{M}_A$  can be derived

Assuming that the mass-luminosity law holds good we can take the ratio  $E = I/\mathfrak{M}$ , where I is the luminosity and  $\mathfrak{M}$  the mass within unit space. Then

$$\pi_{AB} = \frac{i_A}{E_A d_A} \binom{V_\bullet}{V_\bullet}^2 = \frac{i_B}{E_B d_B} \binom{V_\bullet}{V_B}^2$$

where  $V_0$  is the velocity of the Earth, d'' the angular distance from the contre, z the apparent intensity Determinations of  $V_A$  and  $V_B$  can make a contribution to the value of E in both systems or test the binary character of the pair.

252. The Angular Moments of Visual Binaries. Shinzo Shinjo and Yoshikatsu Watknare derived in 1918 the masses and the angular moments of visual double stars. If H denotes the angular momentum of a system we have

$$H = 2\pi_e a^2 l^2 \pi^{-1} (1 - o^2)^{\frac{1}{2}} \Re_A \Re_B (\Re_A + \Re_B)^{-1}$$

if the terms caused by the rotation of the components are neglected

The authors conclude that the masses and angular moments of star systems are, on the whole, of the same order of magnitude. The multiple systems have somewhat greater angular moments, the masses on the other hand remaining about the same. For spectroscopic binaries the angular moments are comparatively less than for visual binaries, the masses, however, being considerably greater. Our solar system has an angular momentum over hundred times less.

It is really very remarkable that the values of H are of the same order of magnitude, when one remembers that the fifth power of the parallaxes enters into the determination of the moments. It is difficult to avoid the conclusion that this result has a certain cosmogonic bearing. The authors compute the angular momentum of a primordial swarm of meteorites, which possesses spherical symmetry and is isolated from other external influences, and also suggest a theory for the explanation of the celestial rotation, perhaps the most enigmatic problem in cosmogony

268. The Origin of Binary Stars. H. N. Russells has pointed out that the problem whether the binaries are the result of fission or condensation in a nebula can be advanced by means of studies of the triple and multiple systems. Systems originating from independent nuclei should not show any definite relations between masses or relative distances. An analysis of the problem shows that if a gaseous mass divides by fission without external disturbance into two parts the distance of the centres at the time of division is greater and the density

Ap J 31, p. 185 (1910)

Mem Coll of Sc Kyoto Imp Univ 3, No 7, p 199 (1918).

less the more unequal the parts (components) are. The ratio in which the initial distance can be increased by tidal action increases as the components become more unequal. The smaller component has the greater density immediately after the separation. The contraction necessary for a second fission is less for the more massive component. The ratio of the dimensions of the separate masses in the case of the second fission to that in the case of the first is always small. The increase in density between the fissions is very great.

The distribution of masses that is found among binaries makes the fission theory very probable. As the orbital elements are known only to a small extent, it is necessary to investigate the distribution of the (projected) distances,  $S_2$ and  $S_1$ . Only pairs with common proper motion were used; of 800 such pairs 74 are triple or multiple. It seems that the fission theory accounts for existing peculiarities of arrangement and gives a simple and fairly detailed account of their origin. The stars for which the separation is 1000 astronomical units exhibit two maxima of frequency, of which one,  $S_2/S_1 = 0.45$ , can be accounted for by fission theory, but the second,  $S_0/S_1 = 0.40$ , cannot. The theory that multiple stars have developed from nebulae that originally had well defined nuclei corresponding to the members of the system must in any case be called on in order to account for such wide groups as the Trapezium in Orion. In the case of the binary stars it seems reasonable to adopt the fission theory.

254. Concluding Remarks. Whereas the magnitude of the stars can be measured directly and their colour estimated or their colour equivalents derived in terms of magnitudes, the dimensions and the masses of the stars cannot be measured by any direct method except in the case of the apparently brightest stars, the diameters of which can be measured by the aid of interferometer

methods.

The important elements, stellar dimensions and stellar masses, are thus derived or inferred quantities that are therefore not only affected by the errors in the observed quantities, but also by the uncertainty concerning the constants in the equations connecting the given quantities and those required for. The dimensions can be derived for all stars for which we possess tolerable knowledge of the quantities M and  $c_0/T$ . It cannot be said that we have a reliable temperature-scale as yet, in spite of all the varied research work carried out within this branch. As regards the masses our knowledge must be restricted for a long, long time to binary stars, and the application of the results to ordinary stars will certainly be justifiable, but will, no doubt, increase the uncertainty of the conclusions.

The third element considered here, the density of the stars, can be determined from observations of binary stars. The parallax does not enter and thus the density will be determined with fair accuracy as soon as the temperature is known.

The present situation with regard to the possibilities of deriving stellar dimensions and stellar masses seems rather satisfactory. The standardization of the temperatures (colours) inaugurated by Herrzsprung could easily be extended to embrace several thousand intermediate stars. The parallaxes available will give linear dimensions of fair accuracy for at least a thousand stars. The new interferometer at Mount Wilson will furnish a means of measuring the dimensions of perhaps fifty stars or more, thus making it possible in the near future to standardize the system of computed diameters.

It might at first seem that the further extension of our knowledge of stellar masses will advance very slowly. But the discovery of new eclipsing binaries or the orbital determination of pairs that have been previously insufficiently

observed will add many good cases within a short time to our previous stock. The discovery by AITKEN of a number of visual binaries of short period makes it possible for us to obtain within the next ten or twenty years orbital elements of a number of binaries. Many of these AITKEN pairs are very imperfectly known as regards their parallax, proper motion, spectral class, and other attributes, but they can easily be entered on current programmes. It also seems likely that the publication of AITKEN's extension of the Burnham General Catalogue of double stars will considerably increase the number of new binary star orbits. It does not seem to be too optimistic to expect to have gained a knowledge of 500 individual stellar masses ten years from now Anecessary condition for the proper increase in data concerning the masses is intimate co-operation between the astrophysicist and the representatives of astronomy of position

The approximations to the spectral-mass relation, mass-luminosity relation, and mass-temperature-luminosity relation hitherto reached will no doubt be more accurately established within a short time from now. The results of Eddington, Jeans, and others concerning the theoretical mass-luminosity relation will certainly be improved upon by the aid of now observational data in the near

future.

An application of the interferometer methods to the method of determining the mass-ratios seems to be of interest. If stars that take no part in the motion of the components of binaries, but that are not too far from them, are measured interferometrically, the results concerning the mass-ratios should be obtained in a much shorter time than when the derivations are based on meridian observations

The general attitude of astronomers towards the problems we have dealt with in this paper sometimes seems to involve a certain overestimation of the bearing of certain theoretical results. It sometimes happens that the reasoning goes round in a circle, or goes if the mass of a star does not agree with Eddington's curve this does not prove anything concerning the correctness or incorrectness of the result. This is a commonplace, but still it seems to me that it should be pointed out. It has often happened that when new results have been prosented it has been asked "How does that result compare with Eddington's, Jeans's or Russell's formula"? Of course, such comparisons should be made, but if there is only poor agreement it is not necessary for the observers to apologize and to regret that the observations do not fit the theoretical demands

I am so far from denying the value of investigations of theoretical problems within astronomy that I wish to say that many efforts must be made on the part of the theorists in order to advance a number of questions on the basis of the new available material. We really should feel under much obligation to the theoretical astronomers for their splendid contributions, theories give us the best guidance with regard to the requirements of future work and, what is most important, theories discover and formulate the general laws of Nature. Without any theories the astronomical observations would be a quite worthless collection

of dead figures and descriptions

But the theoretical interpretations of astronomical facts are always changing. Theories do good service and are dismissed. New theories are advanced and serve for a longer or shorter time. The solid construction on which astronomical theories are embroidered consists of the vast accumulation of recorded facts that has been going on from antique times up to recent days

## Chapter 5.

## Stellar Clusters.

By

H. SHAPLEY-Cambridge, Mass.

With 21 illustrations.

## a) Introductory Survey<sup>1</sup>.

1. The Significance of Clusters. We designate as star clusters those groupings of stars in which the members are known to be gravitationally associated or may be assumed from their apparent positions relative to each other to constitute distinct physical organizations. Such a category includes both the typical globular systems and the more numerous and less well defined open clusters which range, for instance, from the Hyades to the fairly compact system of Messier 11.

There are also, in all parts of the sky, among the faint stars thousands of less obvious groupings. The studies of star distribution on the astrographic charts by Turner<sup>2</sup>, and by Öpik and Lukk<sup>3</sup>, indicate that the distribution is not at random. Working on this problem with Harvard plates<sup>4</sup>. I have shown that the clusterings and vacancies are real and are not to be attributed to occultation by nebulosity. The observed irregularities in the star counts, beyond those allowed by the law of chance, are to be attributed in general to the very prevalent stellar associations, which are not commonly recognized by casual inspection, and cannot be separated from surrounding stars except through laborious investigations.

The typical star clusters, however, are in themselves numerous and widely distributed, and their many problems are intimately interwoven with some of the most significant questions of stellar organization and galactic evolution. The general study of clusters deals with a wide variety of subjects. It involves, for instance, the problems of super-giant stars, stellar luminosity curves, irregularities in stellar distribution, star streaming, island universes, and the genesis of galactic systems; it considers primarily, however, the composition, structure, distribution, and cosmic position of the easily recognizable galactic and globular clusters, and in the following sections these groups will receive almost exclusive attention.

2. Historical Notes on Clusters. The history of the scientific study of star clusters is neither extensive nor very significant. Several clusters of naked eye

Obs 48, p. 173 (1925).

\* Publ Obs Astr Univ Tartu (Dorpat) 26, No. 2 (1924).

\* Harv Circ 281 (1925).

<sup>&</sup>lt;sup>1</sup> Since the manuscript for this chapter was submitted to the publisher in May 1930, several important studies of star clusters have appeared. Only a few of these could be considered in the course of proof reading. November 1932.

stars-for example, the Plendes, Praesepe, Coma Berenices-have of course always been known, though their definite assignment to the cluster category came with the work on proper motions in the last fifty years. In a few constellations the majority of the brighter stars are now known to he near together in space, and to form physical systems. Among such constellation groups are Taurus, Orion, Ursa Major, Perseus, Scorpio, Sagittarius, and Vela But no close physical connection exists for the bright stars of Cassiopela, Lyra, Aquila, Canes Major, and many others,

A score of the brighter galactic clusters and half a dozen of the globular clusters can be seen with the naked eye under good conditions. These objects were probably all known, therefore, to the ancients, but only a few appeared in our permanent records before the second half of the eighteenth century

The records of HIPPARCHUS contain references to the double cluster in Persons and to Praceape, although neither was recognized as a group of distinct stars until the invention of the telescope. Both were first resolved by GALILEO, who described "the nebula called Praesope", "not one star, only, but a mass of more than forty small stars"!

Messier 22, the first globular cluster to be recorded as such, was discovered by IIILE? in 1665, a Centauri was noted as a lucid spot in the sky by HALLEY in 1677, and had previously been known to BAYER as a hazy star, and to Prolemy as a star in the cloud on the Horsk's back; in 1702 Kirch discovered Messler 5, and the famous Messier 13 (the Hercules cluster), the brightest in the northern sky, was accidentally found by HALLEY in 1714.

The open cluster Messler 11 had already been recorded by KIRCH in 1681, but the majority of bright galactic clusters, except the Plenades and the Hyades, were first recorded us such by MKSSIKR3 in 1771. The conspicuous groups of stars around a Carinao and the cluster near x Crucis were discovered by Sir TOHN HERSCHEL

For both open and globular clusters, as well as for bright nebulae of all kinds, the systematic listing by MESSIER in 1784 marked an epoch in the recording of observations of star groups The Herschels advanced the work materially Especially significant were the General Catalogue published by Sir John Herschel in 1864, and its important sequels by Drever in the New General Catalogue and the Index Catalogues,

SCHULTZ and BARNARD were among the pioneers in determining visually the positions of the individual stars in globular clusters. The powerful photographic method of charting axeltions was first used by the HENRYS and GOULD for galactic clusters, and by Schringer, Ludendorff, and von Zeiper for globular systems.

The Pleindes, the Hyndes, Praesope, h and z Persel, and some of the other bright galactic groups have, for the past fifty years or more, been the subject of frequent investigations of positions and proper motions. It is not unfair to say, however, that, except for studies of these nearby objects, the work done on individual clusters before the present century is now of little value. The development of photographic methods, the modern large telescope with its rapid spectroscope, and the standardizing of magnitude sequences have all tended to make the carlier work obsolete. The present views of the nature, dimensions, and significance of the globular clusters are less than twenty years old

GALLERO, Skilorous Nunchus, 1610, Allers, Star Names and their Meanings, p 113 (1899); see Shapley and Howarth, A Source Book in Astronomy, p 49 (1929)

R Wolly, (reschichte der Astronomie, p 420 (1877)

Hist de l'Acad R des Sci., Paris 1771, p 423

Phil Trans 154, p 1 (1864)

A very full bibliography of the work done en clusters is to be found in Appendix C of Star Clusters, Harv Obs Monograph No 2 (1930)

In striking contrast to the present conception of a hundred globular clusters and hundreds of thousands of extra-galactic nebulae spread throughout measured millions of light years, with diameters of hundreds of light years for the clusters, and thousands of light years for the star clouds and nebulae, is the picture suggested by HALLEY's comment on his discovery of the Hercules cluster:

"But a little patch—and similar to the lucid spot around Theta Orionis (Orion Nebula), Andromeda (Andromeda Nebula), and in the Centaur (or Centauri)—most of them but a few minutes in diameter; yet since they are among the fixed stars... they cannot fail to occupy spaces immensely great, and per-

haps not less than our whole solar system.'

## b) Classification, Number, and Distribution.

8. A Comparison of Galactic and Globular Clusters. It is proposed to adopt in the present treatment only two main divisions—globular clusters and galactic clusters<sup>1</sup>. The principal characteristics of globular clusters are strong central concentration and richness in faint stars (fig. 4 and 2). The galactic clusters (fig. 3), looser and much less populous, are extremely varied; for example, Messier 11 is relatively rich, Messier 35 is irregular, the Pleiades and Messier 16 are nebulous, and Messier 103 and N.G.C. 1981 may be but accidental groupings. The so-called moving clusters are merely the brighter and nearer of the galactic types in which radial or transverse motions have been measured.

In future studies, especially in the Magellanic Clouds, we may find examples of clusters in a transitional stage between the richer galactic groups and the most open globular clusters. At present, however, there seems to be a rather sharp division which distinguishes the globular clusters as a special group of sidereal organizations—a group limited to about one hundred objects. The galactic clusters grade indefinitely into multiple stars in one direction, and in another into the condensed systems like Messier 11 and N.G.C. 2477 which closely simulate loose globular clusters.

Clear discrimination between galactic and globular clusters is also possible on the basis of distribution in the sky. The most conspicuous feature of the distribution is that galactic clusters are almost exclusively in the Milky Way and distributed irregularly throughout all galactic longitudes, while the globular clusters are rather widely scattered in latitude, but quite restricted in longitude. The globular clusters are, in fact, mostly in one half of the sky, as will be shown in subsequent diagrams.

4. The Number of Clusters. Thousands of new nebulae and millions of stars have been disclosed by modern telescopes and photographic plates, but the essentially complete listing of globular clusters antedated photography. Every recognized globular cluster except one bears a number from the New General Catalogue of Dreyer, and all but a few were catalogued more than ninety years ago in the earlier Herschelian lists. This early completion of the discovery of the globular clusters led Bailey<sup>2</sup> to suggest that the limit of the region occupied by these systems had been reached, a suggestion that appears to be supported by subsequent work<sup>3</sup>.

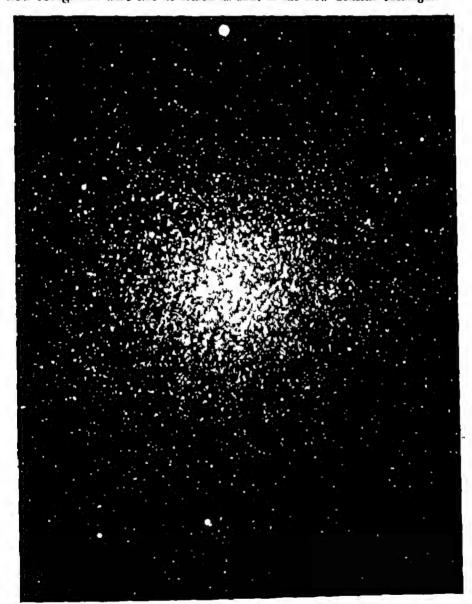
There is, however, a vast difference between cataloguing an object and

<sup>&</sup>lt;sup>1</sup> The term galactic cluster, suggested by TRUMPLER [Publ ASP 37, p. 307 (1925)] and others, is a natural name for the non-globular cluster, which is almost without exception near the galactic plane. It replaces the term "open cluster" which has caused some confusion because of the open type of globular cluster.

<sup>2</sup> Harv Ann 76, No. 4 (1915).

A special study now in progress at Harvard, of the environs of the Large Magellanic Cloud adds several new globular clusters to the list; some of them may not be outlying members of the Cloud, and two or three are not N.G.C. or I.C. objects. In A N 246, p. 171 (1932) LAMPLAND and TOMBAUGH report that N.G.C. 5694 is a typical globular cluster.

recognizing its true character. Many of the entries given in the New General Catalogue (N G C) as globular clusters have proved to be something else, generally galactic groups or extra-galactic nebulae, and thirty-four of the globular clusters now recognized were not described as such in the New General Catalogue.



1/1g 4 Colobular cluster & Contauri, taken with 13-inch Boyden telescope at the Harvard Observatory

The large photographic telescopes have been of service in recent years in examining many faint and doubtful NGC objects, and an occasional addition to the list of globular clusters has resulted. A number of remote groups are still

questioned, however, even after some of them have been tested with large reflectors. The most doubtful globular clusters, which are marked with daggers in Appen dix A, are the following1:

N.G.C.	Radec	Galacilo	Distance <sup>3</sup>	Notes
1651 5946 6352	0438-71 1528-50 1718-48	295+04	32,2 19,7	Rejected; see Harv Circ 271 (1925). A small, poor, loose cluster in a rich region. A comparatively large cluster of very laint stars.
6535	1759-00	354+10	26,7	on the edge of the Milky Way.  A small cluster on the edge of a rich region, with few stars.
6539	1759-08	348+06	38,7	A very faint cluster in a large obscured atea

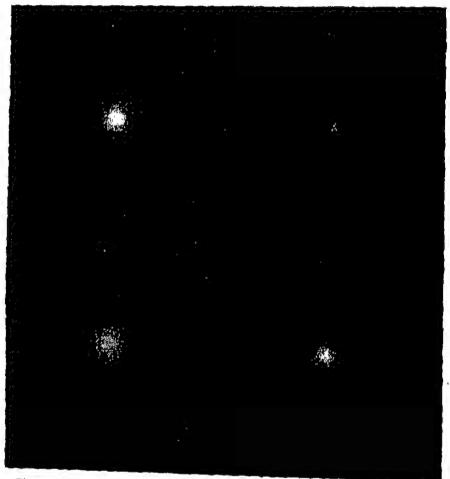


Fig. 2. Four exposures of the globular cluster Messier 13 taken at Mount Wilson.

1 SAWYER and SHAPLEY, Harv Bull 848 (1927).

The approximate positions for 1000 in equatorial coordinates are conveniently contracted for tabulation into the form here given; the first four figures give the hours and minutes of right ascension, and the sign and subsequent figures indicate the declination in degrees (and may be extended to minutes, if desired). The distance in kiloparsees is estimated on the assumption that the clusters are globular.

The numbers of globular clusters have been discussed by Bailly, Hinks, Bohlin, and Miss Clerke, but the data on which their estimates are based lack homogeneity. Melotte's catalogue, however, which was made from the Franklin-Adams plates and contains eighty-three globular and one hundred and sixty-two galactic clusters, constitutes a fairly homogeneous list of all clusters with diameters greater than one minute of arc and brighter than the sixteenth or seventeenth photographic magnitude. His list of galactic clusters is revised and extended in Appendix B, which contains 249 entries. From his list of globular clusters a few objects have been dropped, others have been added, mainly as a result of Hubble's work and my own with the 100-inch and 60-inch reflectors at Mt. Wilson. The total number accepted for the table in Appendix A is 103,

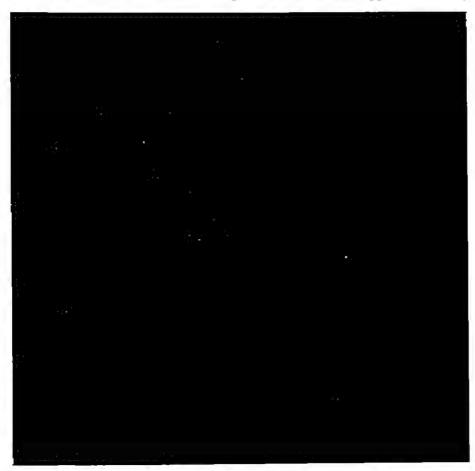


Fig 3 Galactic cluster NGC 3552 taken with the 13-inch Boyden telescope at the Harvard Observatory

including ten globular clusters in the Magellanic Clouds. An example of a recent addition is the observation at the Lowell Observatory, verified at Mount Wilson,

Ваньку, Harv Ann 76, р 43 (1915), Никв, М N 71, р 693 (1911). Вопык, Svenska.
 Vet Akad Handl 43, No 10 (1909), Съвики, Problems in Astrophysics (London) p. 428 (1903).
 Mem R A S 61, р 75 (1915).
 See Footnote 3 on page 700.

that the object NGC 2419, described in the NGC as "pB, pI, lE 90", vgbM, \*7 8 267", 4" dist", and not listed by MEIOTER, is in fact a remote globular cluster in a part of the sky that is otherwise devoid of these systems

Some of the faint extra-galactic nebulae, as yet unresolved, may prove to be essentially globular star clusters, perhaps with greater distances and dimensions than those now known. A comparative study of the distribution of light throughout the images can, however, give us some indication of their nature, then distribution with respect to other extra-galactic objects will probably show most of them to be sidereal systems of a higher order than globular clusters

5. Classification of Galactic Clusters. In the studies of galactic clusters at Harvard we have for some time followed a two-dimensional classification. One parameter is related to the apparent number and concentration of the stars and may be called compactness, the other depends on the distribution of spectral classes among the cluster members.

The classification based on appearance is intended to cover the whole range of galactic clusterings, from multiple stars to globular clusters. The subdivisions

are as follows

a) Field irregularities. That there are many deviations from random stellar distribution is obvious from star counts, or even from a casual inspection of photographic plates in nearly any region of the sky. There seems to be no immediate need of attempting to unravel or catalogue such non-uniformities in stellar fields, but the assignment of a classification letter to the field irregularity is recognition of its significance in stellar distribution.

b) Star associations. In this category fall wide-spread moving clusters, such as the Ursa Major group, and the peculiar stars of high and parallel velocities. The class will be recruited largely through studies of proper motion and radial

velocity. It grades imperceptibly into the next class

c) Very loose and megular clusters, typified by the Hyades and the Pleiades. The large cluster of bright stars around a Perser might be placed in this class, or better, perhaps, placed with the Orion Nebula cluster in class b Classic corresponds in general with Balley's D3 and with Millotti's IV

d) Loose clusters Messier 21 and Messier 34 are examples of a class

equivalent to BAILLY'S D2 and MIJOTIE'S III

e, f, g) Compact clusters. These three groups are equivalent to BMIRY'S D1 and MELOTE'S II. The division into three types is on the basis of richness and concentration, examples are Messier 38, Messier 37, N G C 2477. In the classification of clusters the globular systems follow immediately after class g. In fact, several of the most compact class g. galactic clusters appear more nearly like globular clusters than do the loosest globular clusters classified as such by criteria other than appearance.

In practice the galactic clusters are generally taken to compuse only classes at to g. The distribution among these classes of the 249 clusters listed in Appendix B.

15 as follows

Class	Number
C1 (3)	74 (11115)01
C	22
d	85
e	67 46 29
£	46
g	29

I have found it convenient to divide galactic clusters also into two principal groups on the basis of the spectra or colors of the component stars (1) The Pleiades type, and (2) the Hyades type Each includes members of classes c to g

In the Pleiades type the stars, almost without exception, lie along the "main branch" of a Russell diagram, with the earliest classes B or A; in the Hyades type, yellow spectral classes occur with the same apparent brightness as the predominant A stars,

More than ninety-five per cent of the galactic clusters for which spectral classes or colors have been determined fall into one or the other of these two groups, which are about equally numerous. There are a few aberrant clusters. Messuer 67, for instance, appears to be a variant of the Hyades type in that blue giant stars are absent. Prominent examples of the Plelades type are the double cluster in Perseus, Messier 36, and Messier 34; the Hyades type includes Messier 11, Messier 37. Praescope, and the scattered cluster in Coma Berenices

TRUMPLER has also proposed and used a classification of galactic clusters based on spectral composition. For clusters that he has so far observed he uses Types 1a, 1b, 2a, and 2f, with provision for other types if found. Type 1 is equivalent, in general, to my Pleiades type, and type 2 corresponds to the

Hyades type

6. Classification of Globular Clusters. Notwithstanding the general similarity of globular clusters in size, form, content, and absolute brightness, there are many deviations from the average Clusters such as Messler 19 and  $\omega$  Centauri are conspicuously elongated; Messler 62 is strikingly non-symmetrical; N.G.C. 4147 is deficient in giant stars; and nearly one third of the globular systems are so loosely organized that their inclusion in the list depends on such further criteria as high galactic latitude, the presence of cluster-type variables, and the appearance of thousands of faint stars on long exposure photographs.

Until recently no systematic attempt has been made to classify the globular clusters beyond noting that some were variable-rich, some variable-poor; some open, some compact. A detailed examination by Miss Sawyer and the writer of the globular clusters on good Bruce photographs, which are available in the Harvard collection for practically all the 103 systems now listed as globular, shows that many intermediate forms exist between the loosest and most concentrated clusters. Instead of classing the clusters, therefore, in the two or three broad and obvious categories, such as compact, medium, loose, we arrange them in finer subdivisions, in a series of grades on the basis of central concentration. For the classification of individual clusters reference may be made to Appendix A. Class I represents the highest concentration towards the center, and Class XII the least. The distribution among the various classes and the mean photographic magnitude for each class are as follows:

Class	Magnitude	Number	Class ,	Magnitudo	Number	
I	8,85	4	VII '	7,90	8	
П	7,80	7	VIII	7,85	10	
$\Pi$ I	6,76	7	IX	8,84	10	
IV	9,01	12	x	8,88	9	
V	7,88	12	XI	9.54	9	
VI	8,91	11	XП	9,58	4	

The present classification of globular clusters is essentially a description of apparent central concentration. It is interesting therefore to note that there is no correlation of class with integrated photographic magnitude as determined

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<sup>&</sup>lt;sup>1</sup> Publ A S P 37, p. 307 (1925). A more recent study of galactic clusters is presented by Thurspier in Lick Bull 14, p. 154 (1930), where he gives a more complex, three-dimensional classification. The investigation also includes statistical material on distances, magnitudes, dimensions, and spectra.

from Harvard plates of small scale. The distribution of magnitude among the various classes is shown in the scatter diagram in Figure 4, where also the mean magnitude for a given class is plotted as a cross, and the average class for each interval of one magnitude is plotted as a circle.

To maintain homogeneity, the classifications of globular clusters were all made on plates with the scale of 1 mm = 1'. Superposed stars have occasionally interfered somewhat with the assignment of the class, especially for N.G.C. 4147, 6284, 6453, 6553, 6569, 6624. A few peculiarities were noted that are not completely taken care of by our classification based on central condensation alone. For

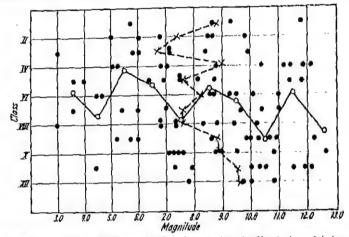


Fig. 4. The scatter diagram of classes of globular clusters (ordinates) and integrated photographic magnitudes. Circles and crosses indicate means.

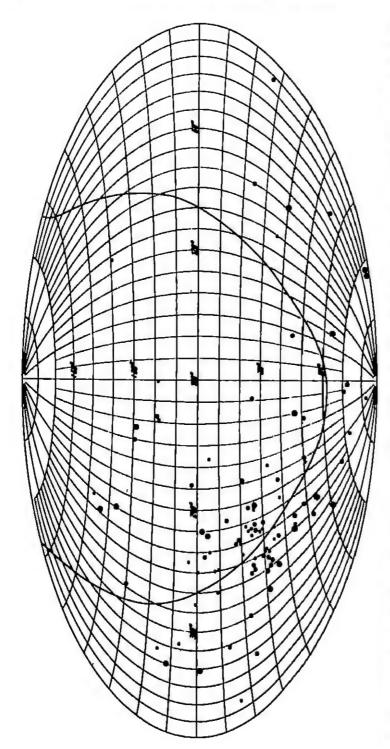
instance, the bright cluster  $\omega$  Centauri is peculiar in what appears to be a remarkable uniformity in the magnitudes of the brighter stars. Clusters somewhat similar to  $\omega$  Centauri in this respect are N.G.C. 5272 (Messier 3), 5927, 6273, 6656 (Messier 22). These clusters also resemble each other in their moderate concentration (Classes VI to VIII), and two of them,  $\omega$  Centauri and Messier 3, are the richest of all in variable stars. It should be noted, however, that the clusters with many variable stars are scattered throughout all classes.

In conclusion we observe that the classes of globular clusters are probably indicators of developmental age. They should prove increasingly useful in studies of linear diameters, motions, luminosity curves, and the deeper problems of the origin and life history of stellar clusters.

Table i. Typical Globular Clusters of the Twelve Classes.

Class	N.G.C.	R.A. (1900)	Dec. (1900)	Pg. Mag.	Class	N.G.C.	R.A. (1900)	1300, (1900)	l'g. Mag.
II III IV V VI	104 1866 7099	9 <sup>h</sup> 10 <sup>m</sup> ,0 21 28 ,3 0 19 ,6 5 13 ,3 21 34 ,7 19 2 ,0		5,7 5,0 3,0 8,0 6,4 4,6	VII VIII X X XI XI	6402 6218 288 6809	19 33 .7	-23° 59' - 3 11 - 1 46 -27 8 -31 10 -16 10	3,6 7,4 6,0 7,2 4,4 10,8

7. Clusters in or near Obstructing Nebulosity. The large groups of bright B stars in Orion, Scorpio, and elsewhere are associated with important bright and dark nebulosity. The Pleiades nebulosity is well known. A number of



The galactic circle is shown 5. Distribution of globalar chaters an equatorial coordinates. Small dots molicate more distant chaters. by a heavy line. The chatters in the Magellanic Clouds have been omitted.

nebulous galactic clusters, such as Messier 8, are on record, and clusters of the sort also appear in the Magellanic Clouds. It is doubtful, however, if man is would be known of the nebulosity in these galactic clusters if their distance.

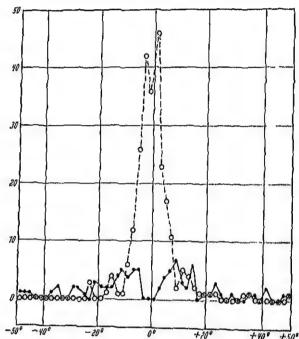


Fig 6 Numbers of galactic clusters (chicles) and globular clusters (dots) for two degree intervals in galactic latitude

were ten times a epacif By implication, there fore, it bulesty in pides to clusters may be more common, their appoint from general mepochem

There are a few its dividual philadar sta Star, N G C B, 2 N G C 61 H, and N G C 6569, that are in or near to cognized dark or hum nous nebular Of these, the first appears to be dummed by one of the long dark treatter : from the Coal Sack, The second is at the edge of the heavy is Ophica ha nebulosity N to C tister is march day lold in Sagittarius but may also be involved in wepset obscuring achillesity

Fo what extent the magnitudes and colors in galactic and globular

clusters are directly affected by associated nebulosity is not as yet determined. For individual nebulous stars Seares and Hubbit have found a role effect and presumably a corresponding deficiency in apparent brightness

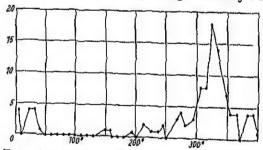
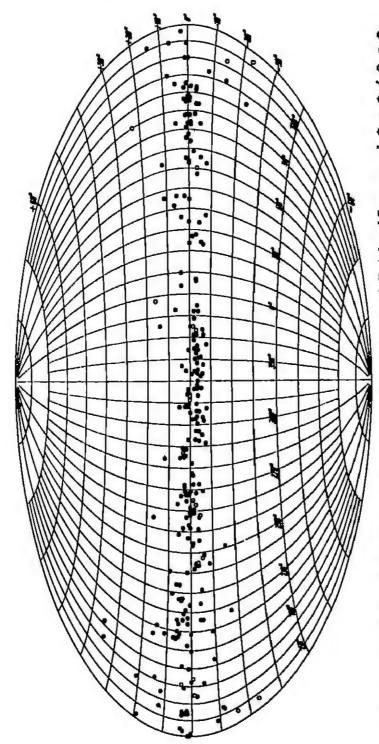


Fig 7 The frequency distribution of globular clusters in galactic longitude. Ordinates are numbers of clusters, abscissae, degrees of longitude.

8. The Apparent Distribution of Globular Clusters. In legace 5 is shown the distribution of globular clusters; theremarkable contrast in the galactic affiliation of the galactic and globular clusters is shown in Figure 6. The equatorial and galactic coordinates of globular clusters are given in Appendix A, and a discussion of their distribution in space appears in later sections, The remoterness of the

The remoteness of these cluss account for their observed scarcity near the galactic equator without seriously affecting at the same time the distribution of the nearer galactic clusters.

In Figure 7 is shown the distribution of globular clusters in galactic longitude. From this diagram and the preceding figure we find that the center of the system



c, 0; d, 0, e, 0, f, 0, g, • Fig. 8. Distribution of palacific clusters in galactic coordinates. Cluster classes are indicated as follows

of globular clusters lies in the direction of galactic longitude 327°, galactic latitude 0°. The probable error of this determination is about one degree. The corresponding equatorial coordinates are right ascension 17h 28m, declination -- 29°.

9. The Apparent Distribution of Galactic Clusters. The distribution of galactic clusters in galactic coordinates is shown in Figure 8. The high concentration in low latitudes is evident. The galactic clusters with latitudes greater than ±15° are given in Table 2. The high latitudes for Coma, Praesepe, the Pleiades, and the Hyades, are not remarkable, because the parallaxes are relatively large and the linear distances from the galactic plane are relatively small. The fainter galactic clusters in high latitude merit further detailed study.

Table 2. Galactic Clusters with Latitude Greater than 4: 15°.

NO.C	Gala	elle	Remarks				
N.G.C.	Longitude	Latitudo					
188	90°	+23°					
752	105	-23					
Melotte 22	134	-22	Ploindos				
Melotte 25	147	-23	Hyades				
2243	206	-16					
2281	142	+18					
2420	166	+21					
2548	196	+17					
2632	174	+34	Praesope				
2682	184	+33	Messier 67				
Melotte 111	200	+85	Coma Berenices				
I 4665	358	+16					

An interesting and significant result of the special surveys that have been made of objects once doubtfully classed is the evidence that nearly every faint little-condensed cluster in galactic latitude higher than 15° or 20° is really globular, although for many of them short exposures and visual observations had originally recorded few stars. Long exposures, however, bring out the globular nature of such clusters. Nearly all the similar faint objects along the galactic equator remain open groups, with no condensed background of faint

stars appearing on long exposures.

10. Peculiarities in the Distribution of Galactic Clusters. The clusters listed in the catalogue in Appendix B do not extend deep into the galactic structure; they tell us nothing of the center or of the boundaries. There is significance, however, in certain peculiarities of their distribution. Already we have noted that in contrast with globular clusters they are rather uniformly dispersed in galactic longitude, and also that they are largely confined to the low galactic regions where globular clusters are scarce. There are two additional features of their distribution that are worth consideration: (4) the infrequency of galactic clusters in the first quadrant of galactic longitude; there are very few of these systems in the Aquila-Cygnus region of the Milky Way; (2) the narrow restriction of the clusters to low galactic latitudes in the direction of the galactic center and their wide dispersion in galactic latitude in the opposite part of the sky.

This second phenomenon might be explained as a consequence of the motions of galactic clusters in long orbits around the nucleus in Sagittarius. If their orbital inclinations differ from zero, when seen from the earth's eccentric position in the Galaxy those in the direction of the center would on the average appear to be in lower latitudes than those away from the center. It is probable that none of the galactic clusters that are now beyond the center of the Galaxy enters

our catalogue.

The alternative and, I think, preferable interpretation is that galactic star clusters are associated largely with particular galactic star clouds. Irregularities of distribution and concentration in low galactic latitude are therefore merely consequences of the distribution of the nearer star clouds. If the galactic clusters are closely affiliated with various star clouds, we may find them differing systematically in spectral and structural characteristics from one part of the aky to another We already have an indication of such diversity in the orientation of the axes of elongation, discussed in ciph 24 below. The brighter clusters of Auriga are rich and not strongly condensed (Messier 36, Messier 37, Messier 38); many of the small condensed clusters of Sagittarius are nebulous, and the groups in Carina are systematically bright,

# c) On the Spectral Composition of Clusters.

11. Integrated Spectra of Globular Clusters. Integrated spectra were determined for several clusters many years ago at the Lick, Mount Wilson, and Lowell Observatories, mainly by FATH1 and SLIPHER, who found spectra of composite character, principally classes F and G. The HENRY DRAFER Catalogue records without close classification the integrated spectra of numerous clusters.

Miss CANNON has recently examined closely all available Harvard photographs showing spectra of globular clusters. The results are briefly summarized in Table 3, which gives the N G.C designation, the cluster class, and the spectrum. For some clusters, such as N.G C 4147 and 6624, the observed spectrum may be largely due to one or two stars, and they of course may be foreground objects.

Table 3 Spectra of Globular Cinatora,

N.G.C.	Charles Class	Spectral Cines	N.G.C.	Class	Spectra. Class
104	ш	G5	6293	IV	G5
362	Ш	G5	6304	VI	K:
1261	п	Ğ	6316	ш	GS
1851	п	Go	6333	VIII	K.
1866	IV	178	6341	IV	G5.
1904	V	F8	6356	II	Ko
2808	I	Ko	6388	пі	K
4147	IX	A7:	6397	IX	G:
4590	X	Note	6441	III	Ko
5024	v	Note	6541	mı	G
5272	VI	G	6624	VI	Mo
5286	l v	Go	6626	IV	G5
5824	I	FS	6637	V	K2
3904	V	G.	6652	VI	K5
5986	VII	F8	6715	ш	F8
6093	п	Ko	6723	AII	G5:
6121	IX	F	6752	VI	Go
6205	v	Go	6864	1	GO
6229	AII	Noto	6934	VIII	Go
6254	AII	Note	7078	IV	F
6266	IV	Ko	7089	п	IF5
6273	VIII	G51	7099	v	I'8
6284	IX	F:			

N.G C. 4590 Dark lines are seen in the violet.

5024 Dark lines Hô, H, and K faintly seen.
6229, Several dark lines are seen, apparently including H and K. 6254. Dark lines in the violet appear to be H, R, and H C.

<sup>1</sup> Lick Bull 5, p. 74 (1908); Mt Wilson Contr 49 (1911).

Hery Bull 868 (1929).

A frequency diagram of the classes is given in Figure 9; classes F, G, and K of Table 3 are taken as Fo, Go, and Ko. The class of spectrum does not appear to be closely related to cluster class, apparent magnitude, or any other significant property of the clusters. We have here only an indication of the probable diversity

in predominant type of the stars that are effective in producing the integrated spectrum.

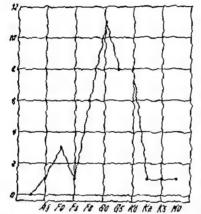


Fig. 9. Frequency curve of integrated spectra of globular clusters. Coordinates are numbers of clusters and spectral classes.

12. Stellar Types in Globular Clusters. From integrated spectra and colors we pass to the types of individual stars in globular clusters, noting some similarities to the distribution of types in the Galaxy, but also some important differences.

al Common Spectral Classes. The color indices in various globular clusters show a normal range from about -0,3 to +1.6. This indicates, no doubt, the presence of all spectral classes from B to M; and normal spectra have in fact been directly observed from A to G. The average color index<sup>2</sup> in Messier 13 is -1-0.55, corresponding to the spectrum gF4.

Seventeen per cent of the stars in Messier 13 brighter than the working limit

(photovisual magnitude 15,5) have negative color indices. In Messier 3, on the other hand, there is a smaller proportion of negative color indices (4,7 per cent down to photovisual magnitude 17,00), but an excess of Class A stars of about the magnitude and color of the cluster type variables. It should be noted, however, that an error in the zero point of either photovisual or photographic magnitudes would shift the spectral frequency curve bodily. Such error may exist, and may not be inappreciable.

b) The Color-Magnitude Arrays. The distribution of color indices and photovisual magnitudes are shown for Messier 22 in Table 4. The tabulated quantities are numbers of stars? The last tabulated line or two are near the practical fainter limit for magnitude work and may be deficient in numbers and inaccurate. The color classes, b, a, f, ..., corresponding to the color index intervals -0.4 to 0.0, 0.0 to +0.4, +0.4 to +0.8, ..., are nearly analogous to the spectral classes B, A, F, . . . This analogy is close because the cluster stars under study are all giants; the agreement would not be so satisfactory for dwarfs.

In the array for Messier 22 the dispersion of magnitude within any one color class is conspicuously small. All stars are included which are brighter than the magnitude limit of the photovisual plates and within 5' of the center of the

1 SHAPLEY, Mt Wilson Comm 44 (1917).

SHAPLEY, Mt Wilson Contr 116 (1917); see also Prass, Mt Wilson Ann Rop 9, p. 219 (1913); 10, p. 268 (1914); SAMFORD, Mt Wilson Ann Rep 14, p. 212 (1918); Pop Astr

<sup>27,</sup> p. 99 [1919].

Harv Obs Mon 2 (1930); Harv Bull 874 (1930). Ten Bruggencate has plotted the coordinates (my magnitudes and colors) for the individual stars used in making the color-magnitude summaries for Messier 13 and Messier 3. (Die Sternhaufen, Borlin, 1927). I think there is little gain and some desger in defailed subdividing of the observational material. Experience with the photometric measures in globular clusters leads to a bellet that the group values presented in my color-magnitude arrays go as far as is justifiable in subdivision.

Sharks, Mt Wilson Comm 16 (1915).

Table 41 Color-Magnitude Array for Messier 22

	Color Clast													
Limits of Photoviscal Magnitude	< ъо	b0 to b5	b 5 to a 0	a 0 to a 5	4.5 10 10	10 lo 15	15 to 80	#0 #5	to ko	k O to k 5	k 5 to pa 0	to to	>= 5	AJI Colors
10,20-,39 ,40-,59 ,60-,79 ,80-,99 11,00-,19 ,20-,39 ,40-,59 ,60-,79 ,20-,39 ,40-,59 ,60-,79 ,80-,99 13,00-,19 ,20-,39 ,40-,59 ,60-,79 ,80-,99 14,00-,19	111111111111111111111111111111111111111		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 40 26		1 1 1 8 12 34 39 39 2				1111110001000111111111			1 1 3 3 1	1 4 7 9 5 5 9 5 14 13 25 11 100 203 57 106 71 156 8 3
70tals	1-	3	36	68	105	138	123	57	45	17	10	12	8	623

cluster It is of interest that more than six per cent of the stars have negative color indices, the cluster resembling in this respect Messier 13 rather than Messier 1.

No correction has been made in the color-magnitude array for superposed stars. The cluster lies in a rich star cloud in Sagittarius, and probably ten per cant of the stars included in this discussion are not cluster members. The color-magnitude array is therefore applicable both to the cluster and to the star cloud, and the small dispersion in brightness of both together suggests that the two are associated. The color-magnitude arrays establish the fact that in the condensed clusters, as well as in some loose galactic groups, the average color is redder the higher the visual brightness. The result naturally bears on current considerations of the evolution of stars.

The general similarity of globular clusters, especially in the color-magnitude relation for giant and supergiant stars, is shown by a comparison of the brightest stars in Messier 3 and Messier 13 with the brightest stars in the faintest and most remote globular cluster known. N G.C. 7006 is five times as distant as Messier 3 and Messier 13, yet the most luminous stars in all three clusters have about the same average color and the same progression of color with magnitude. The mean results are as follows

Mean Color Number of Mana Photographio Magalinda Glass Index 十1,09 38 16,46 N.G C. 7006 +1,15 35 13,17 Momior 3 36 +1.02 12,72 Momier 13

<sup>1</sup> Sec Hery Bull 873 (1930)

Mt Wilson Contr 155, p. 8 (1918).

A similar result is found in all globular clusters tested, though some, such as

N.G.C. 4147 and N.G.C. 5053, are less populous in giant stars.

13. On the Masses of Giant Stars. The color-magnitude array can be transformed into a relation between spectral class and mass by means of the observed mass-luminosity relation for galactic stars. It is necessary to assume that we can safely replace color class by spectral class for giant stars; the uncertainties involved both in this assumption and in the temperature scale, used for reduction from photovisual to bolometric magnitude, are not negligible, but still they are not serious enough to falsify the results except for stars of extreme color. It is possible that the chief source of error lies in the mass-luminosity curve itself, which depends mainly on nearby double stars and possibly is inapproprintely applied to single stars, especially in a globular cluster.

The computation of the stellar masses in terms of the sun's mass for successive intervals of magnitude and color has been carried through for Messier 22; the results are shown in Table 5. The distance modulus,  $m_{pv} - M_{pv} = 14,16$ ,

Table 5.	The Mass-S	pactrum	Relation	for	Messior	22.
----------	------------	---------	----------	-----	---------	-----

Apparent Pv. Mag.	Spectrum	Absolute Pv. Mag.	Absolute Bol. Mag.	Mass		
11,2	M2,5	~2,96	-4,62	29:		
,4	K9.0	-2.76	~4,10	22,4:		
,6	K5,8	-2,56	-3,72	17,8		
,8	K3,0	-2,36	-3,13	14,1		
12,0	K1,0	-2,16	-2,74	11,7		
,2	G9,0	-1,96	2,41	10,0		
.4	G7,0	-1,76	2,10	8,3		
,6	G5,5	-1.56	-1,84	7,4		
.8	G4,0	-1,36	-1,58	6,5		
13,0	G2,5	-1,16	1,30	5.9		
,2	G1,2	-0,96	- 1,16	5,4		
,4	F9,8	-0,76	-0,80	4,8		
,6	F7.8	-0.56	~0,58	4,5		
.8	F5.8	~0,36	-0,36	4,1		
14,0	F3,0	-0,16	~0,16	3,9		
,2	A9,5	+0,04	+0,04	3,7		
,3	A6,8	+0,14	+0,07	3,6		
,4	B7.5	+0,24	~0,49	5,7		

is taken from Appendix A; the reduction to bolometric magnitudes and the computation of the masses are made with the aid of tables given by EDDINGTON 1. The masses of the reddest stars would have been from ten to twenty per cent less with Brill's scale of temperatures and corrections to bolometric imagnitude 4. The values of photovisual magnitude and spectrum in Table 5 are read directly from the curve drawn through a plot of the colors and magnitudes of the individual stars that appear in the color-magnitude array.

Masses for the average giant stars of various spectral classes in Messier 22 are as follows:

A0 A5 F0			<4.8	F5 .			,	4.0	Ko				,	10,8
A5.,			<3.5	Go.	,	,	,	4,9	IX5	,	,	,		16,5
Fo	6		<3.6	G5 .				7.0	Mo					24.0

It is possible to give only upper limits of average mass for classes A0, A5, and F0 because of the incompleteness of the observational material for the corresponding intervals of color index.

<sup>1</sup> Internal Constitution of the Stars, Chapter VII (1926). Babelsberg Veröff 5, p. 16 (1924).

For the rich galactic cluster Messier 37, von Zerfel and Lindgeen find the mass of the giant g5 stars 2,15 times as large as the average mass of the b and a stars1, in good agreement with the present results. They have used space distribution of the stars as a criterion and a measure of the masses of different types.

It is interesting to note the small dispersion in color for stars of a given photovisual magnitude. Accepting the mass-luminosity relation, we can only conclude that in a globular cluster such as Messier 22 the grant stars of a given

mass have a very small spread in surface temperature.

- 14. Spectra in Individual Galactic Clusters. Numerous investigations have been made of the colors and magnitudes of galactic clusters, notably by TEN BRUG-GRNCATE, DOIG, GRAFF, HERTZSPEUNG, PICERRING and PLEMING, RAAB, SEARES, SHAPLEY, TRUMPLER, and VON ZRIPEL and LINDGREN. The HENRY DRAPER Catalogue contains spectral data for only the brightest clusters. The Harvard material is discussed first, followed by brief accounts of a few individual clusters and the spectral classification of clusters by TRUMPLER.
- a) Harvard Studies. Mrs. Flemings tabulated the spectra for seven galactic clusters, the Pleiades, Praescpe, Coma Berenices, I.C. 2602, N G C. 3532, Messier 6, and Messier 7. The stars for which spectra are classified are distributed over a larger area than that actually covered by the clusters, and foreground stars of course cannot generally be differentiated and excluded Some very faint stars, barely distinguishable on the plates, are included. The results are summarized for Class A in Table 6.

Table 6. Percentage of Class A Stars in Seven Galactic Cinsters.

Charter	Stam Classified	Stars in H.D.C.	Percent Class A
Piciados . Praesspo I C. 2602 . N G C 3532 Coma . Monsior 6 Messior 7	91 90 64 204 117 91 346	58 135 75	65 31 77 93 15 75

<sup>\*</sup> Limits indefinite.

Although the classification was crude, and for some stars quite uncertain, the existence is clearly shown of a different spectral distribution in Praesepe and Come from that in the other five clusters. It is the same distinction that is now recognized in the Pleiades and Hyades types, or in TRUMPLER's types 1 and 24.

The frequency of A stars in galactic clusters has led to attempts to determine spectral parallaxes on the basis of the material of the Henry Drayer Catelogue: but because of the wide dispersion in magnitude the attempts are not always happy.

b) Spectra in the Brighter Galactic Clusters. The Pleiades, the Hyades, and Come fall under the head of "very loose and irregular clusters".

Svenska Vet Akad Handl 61, No. 15, p. 126 (1921).

Bee bibliography in Hary Mon No. 2 (1930).

E. C. PICKERING, Harv Ann 26 (1897); see also Table 6.

Publ A S P 37, p 307 (1925). See note 1, p. 705, on his later work.
 Doio, J B A A 33, p 201 (1925); RAAB, Lund Medd, Série II, No. 28 (1922).
 HERTESPRUNG, M N 89, p. 660 (1929) See also Harv Bull 764 (1922)

division c in the classification of galactic clusters in ciph 5 Figure 10 shows for the Pleiades the spectrum-inaginitude relation as compiled by Hertzsprung<sup>1</sup>. The spectral data on h and  $\chi$  Person, Messier 11, and two southern clusters may be summarized as follows

1 The Double Cluster in Perseus Sixty-six bright stars in the double cluster in Perseus, classified mainly by Trumpler<sup>2</sup>, range in spectrum from A0 to B9, and in magnitude from 5,5 to 10,9. Two matters of exceptional interest

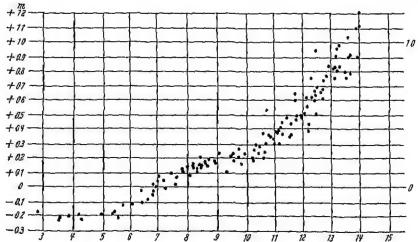


Fig 10 Relation of color to luminosity in the Pleiades Ordinates, color indices, abscissae, photographic magnitudes (From Herzsprung)

in this cluster are the fact that a large number of the brighter stars show the c-character, and that the numerous bright line stars are by no means the brightest members of the cluster

- 2 Messiei 11. In supplementing my earliei work on the colors in Messiei 11. I found in from plates made with the 100-inch reflector at Mount Wilson that the brighter spectra are chiefly of class A. This observation was later verified by LINDBLAD on other Mount Wilson spectrograms. The spectral classes of fiftynine stars in and around the cluster have since been given by TRUMPLER.
- 3 NGC 3532 and NGC 3766 The distribution of spectra in two southern galactic clusters has been derived by Becker from his own photographs made at La Paz<sup>5</sup> He finds percentages as tollows

	B0-B7	B8-A1	A5-A8	Ro	K4	Number of Stars
NGC 3532 NGC 3766	 3,8 44,2	86.3 39.5	1,5 4,7	8,4	11,6	131 13

4 Lick Bull 12, p 10 (1924) A N 236, p 327 (1929)

<sup>8</sup> The magnitudes determined for this cluster are apparently in error, probably by a constant amount, notwithstanding the consistency of the Mount Wilson photometric plates [Mt Wilson Contr 126 (1917)] The color indices are systematically too great, as shown by my own spectrum plates (unpublished), and subsequently by the similar work of Lindblad and Trumpler A correction of -0,4 to the photographic magnitudes is indicated by an unpublished Harvard plate, but even then the colors and spectra are inconsistent. There is a probability of differential light absorption within the cluster.

For NGC 3532 Mrs. FLEMING recorded ninety-three per cent of the 204 stars as Class A<sup>1</sup>

c) TRUMPLER'S Investigations The kinds of spectral distribution among the stars of a galactic cluster, first recognized in the early Harvard work, and amplified by all subsequent studies, are defined in some detail in TRUMPLER'S scheme of classification (ciph. 5 above), and a number of galactic clusters have now been assigned by him to the classes and their subdivisions. For fifty-two clusters the relative numbers in the various classes are as follows

Тура	Number	Туре	Number
1 b	24	2f	1
16	6	Others	1
28	20		

It will be seen that the Pleiades type proponderates among the systems bright enough to classify. This may, however, be an effect of selection, as Type 1b contains far brighter stars than any of the others. The bearing of this selection on estimates of distance is considered on page 748, footnote 1.

### d) Variable Stars in Star Clusters.

15. The Prequency and General Properties of Variable Stars in Clusters. Periods have been determined for 466 variable stars discovered in forty-five globular clusters<sup>3</sup>; all but nineteen are found to be cluster type Cepheids. There is a slight correlation between frequency and galactic latitude, the rich clusters having a greater mean distance from the galactic plane than have the poor. The latter are distributed equally throughout all classes, while the rich clusters are confined to the intermediate classes. It seems unlikely that observational selection is responsible for this result; the effect, however, may be due in part to the decreased discovery chance in a very condensed cluster

The general properties of variable stars are discussed alsowhere. There is no evidence that the Capheid variables in clusters, whether of short or long period, are different in their various characteristics from those in the Galaxy at large. The color changes and light curves are of the usual sort. The long period variables in 47 Tucanae are also normal in period, range, and form of light curve.

Certain features of cluster variables, however, are to be noted. The great majority are, on the average, 1,5 to 2,0 magnitudes fainter than the brightest stars in the cluster (see clph 31 below). There is observed, particularly in ω Centaurl, Messier 3, Messier 5, and Messier 13, a definite fainter limit to the magnitudes of Cepheids, similar to that found in Miss Leavett's survey of the Magallanic Clouds. The negative results of the searches for faint variables, and the form of the period-luminosity curve, which flattens conspicuously for periods less than a day, suggest that dwarf Cepheids do not occur. There is likewise no convincing evidence of eclipsing binaries in any globular clusters; but the faintness of such stars would preclude their discovery on most of the existing plates.

The peculiarities of variables in clusters lie in the relative numbers of different types and subtypes as compared with those in the galactic system, galactic star clouds, or the Clouds of Magellan; but it is to be noted that very serious factors of incompleteness and selection affect the comparison of clusters

See Table 6 above.

LUDENDORFF, volume VI, chapter 2.

Previous to 1930
Harv Circ 173 (1912).

But see GUTHNICE and PRACER, Sitzber Prouss Akad Wiss 1925, p. 508.

with the Galaxy, and also that there appear to be just as great differences in variable star content between clusters as there is, say between  $\omega$  Centauri of 47 Tucanae and the solar neighborhood

16. A Summary of Known Variables. Despite a careful search, few variable stars are definitely known to belong to galactic clusters, some that have been tentatively assigned to such systems are of unrecognized type, and probably he in the surrounding star fields. Many have been found, however, in globular clusters, as remarked above The history of their discovery is short Examining some of his earlier photographs, Di Common first noted the probable variability of some stars in Messier 5. Professor E C Pickering2 in 1889 and Mr David PACKER<sup>8</sup> in 1890 also made some carly observations of the variables in globular clusters, which were independently confirmed by Barnard a few years later But the whole development of this special branch of variable star astronomy is essentially due to Professor Bailey, whose extensive research on globular clusters, begun about thirty years ago, is the basis of much of our knowledge concerning cluster variable stars. Employing mainly the photographs made at Arcquipa with various telescopes, BAILLY has found the majority of cluster variables now known, and has made by far the most important investigations of light curves and periods. Aside from BAILEY's work, the discovery and study of the variables has been almost exclusively the work of Miss Woods at Harvard, BAADE and LARINK at Bergedorf, and the writer and his collaborators at Mt Wilson and Harvard [see references in Harv Mon No 2 (1930)]. LARINK has made an extensive check of Bailey's periods for cluster-type variable stars in Messier 3, finding that, after a twenty-year interval, 82 periods were unchanged and 29 probably had varied My similar check on 54 of Balley's variables in Messier 5 results in periods accurate to within a tenth of a second; in this cluster nearly all the periods are constant throughout an interval of thirty vears

The data at present available concerning the variable stars in globular clusters are summarized in Table 7 Clusters examined with care but without discovery of variable stars are also included in the table. Some stars suspected of variability are omitted in the absence of numerous or decisive observations. Three of these, for instance, are in the Hercules cluster, where my measures on a few plates can not be considered to furnish sufficient evidence of variability. In crowded regions and for close doubles the photographic development (EBER-HARD) effect may produce spurious variability, for it varies from plate to plate under ordinary working conditions Aside from this and similar uncertainties, which lead to the inclusion and exclusion of suspected variables, there is another element of incompleteness in these tabulated results because of the difficulty of thoroughly examining the centers of clusters, and also because of the small number of plates sometimes involved in the surveys In general it may be said that scarcely a cluster has been examined with the accuracy and thoroughness necessary to detect ordinary echpsing stars of short range or narrow minimum, and to exhaust the possibility of Cepheids of small range

M N 50, p 517 (1890), 51 p 226 (1891)
 A N 423, p 207 (1889), Harv Circ 2 (1895)
 Sid Mess 6, p 351 (1890), 10, 170 (1890), Engl Mech 51, p 378 (1890).

<sup>4</sup> A N 147, p 243 (1898)

<sup>&</sup>lt;sup>5</sup> SHAPLEY, Mt Wilson Contr 116, p 79 (1915)

<sup>8</sup> EBERHARD, Z f Phys 13, p 288 (1912), Publ Astrophys Obs Potsdam No 84, p 1 (1926)

Table 7 Summary of Variables in Clusters.

					_			Clus	tors,
N.G.C.	٨	p	Class	Hillip- Licity	Vari- ables	Por <14	had   > 14	Sua- pooted	References
104	272°	-44ª	III	8	7	_	3	_	1, 2
288	214	-88	X	9	2			_	3
362	268	-46	пі	8	14	l –	_	_	1
1851	211	-34	II	þ	3	_		_	4,5
1904	195	-28	v	9	5	_	_	_	1
2419	148	+23	VII	9	26	_	l		40
3201	244	+10	x	9	61	- 1	_	_	6, 7
4147	227	+78	IX	_	4		_	8	8, 42
4590	268	+37	x	9	28	27	1	-	9, 10
4833	271	- 8	VIII	9	5		l <u>-</u>	_	5
5024	307	+79	v	9	42	[	_	_	11, 12, 41
5053	310	+77	XI	8	9	8			13
5139	277	+16	VIII	8	132	95	5	_	1, 14
5272	8	+77	VI	8	166	110	1	79	1, 15, 16, 17, 18, 19
5286	280	+10	v	9,5		-		/3	20
5466	8	70	ΧП	9	14	12	_		12
5904	333	十45	V	ó	84	69	3	8	1, 21
5986	305	+13	VII	_	1	-	]	_	1 2
6093	320	+18	II	10	4	_	_	=	1, 39
6121	319	+15	IX	9	33	3	_	5	22
6205	26	+40	v	9,5	7	1.	2	3	1, 17, 23, 24
6229	41	+39	VII	7,3	1			-	8
6266	320	+ 7	IV	8	26	_	_		1
6293	325	+ 8	ĬŸ	9	3	_		_	25
6333	333	-1-10	viii	ģ	1			_	3
6341	35	+34	īv	8	14	_	_		17, 26
6362	293	-17	x	8	17	_	_	_	27, 28
6397	304	-12	IX	9	2	_	_		1
6426	356	+15	IX.	ó	2			_	40
0539	348	+ 6	X	9 9 9	1		_		29
6541	317	-12	ш	á	1	_	_		30
6553	333	- 4	XI	á		_	_	2	25
6584	310	-18	VIII	9	_		_	_	20
6626	336	- 7	IV	ó	9	_	_		ī
6656	338	- 9	VII	8	21	9	2	4	1, 31, 32, 33
6712	353	- 6	IX	_	1		_		8 21, 22, 33
6723	327	-18	VII	9,5	17	16	_	_	1, 34
6752	303	-26	VI	2,3	1	-	_	_	1 37
6779	30	+ 7	x	8	i	-	_	2	25, 35
6809	335	-24	хì	9	2				1 1
6864	348	-28	I	9	11	_	_	5	25, 36
6981	3	-34	ĪΧ̈́	_	29	29		5	8, 25, 36
7006	32	-20	Ī	_	11	111	_		25, 37
7078	33	-29	IV	8	74	60	1	_	1, 21
7089	22	-37	II	9	11	~	;		1, 38
7099	356	-48	Ÿ	9	3	_	l - l		1
7492	23	-65	хп	9	9		1 _	5	3
7734	4,3	-03	·	y	, ,	_		)	1 2

1 Balley, Harv Ann 38, p. 2 (1902) 2 Balley, Harv Bull 783 (1923). 3 Mt Wilson Observatory, unpublished. 4 Balley, Harv Bull 802 (1924). 5 Miss Swore, unpublished. 6 Miss Woods, Harv Circ 216 (1919) 7 Balley, Harv Circ p. 234 (1922) 8 Miss Davis, Publ A S P 29, p. 260 (1917). 9 Shapley, Mt Wilson Contr 175 (1920). 3 Mt Wilson 10 SHAPLEY, Publ A S P 31, p 226 (1919). 11 HAADE, Hamburg Mitt 5, No. 16 (1922) 13 BAADE, Hamburg Mitt 6, No 29 (1928) 12 BAADE, Hamburg Mitt 6, No 27 (1928). 14 INNES, Union Circ 59, 201 (1923). 15 SHAPLEY, Mt Wilson Contr 91 (1914). 16 BHAP-17 GUTHIROX and PRACES, Sitzber Process Akad LEY, Mt Wilson Contr 176 (1920) 18 LARDER, Bergedorf Abhandhingen 2, No 6 (1921) 19 BARMARD, Wiss 1925, p. 508. A N 172, p. 345 (1906). 20 BAILEY, Hary Bull 801 (1924) 21 BAILEY, Harv Ann 78 23 RAJ 1, p. 16 (1924) 22 Mim LMAVITT, Hary Circ 90 (1904) LEY, Mt Wilson Contr 116 (1917) 25 SHAPLEY, Mt Wilson Contr 190 (1920) Woods, Harv Bull 773 (1922). 27 Miss Woods, Harv Circ 217 (1919). 28 Miss Woods, (Continued next page helow.)

and

## e) The Distribution of Stars in Globular Clusters.

17. Are Cluster Stars Arranged Spirally? In order to determine whether the frequently described spiral structure in or near the center of globular clusters could be seen on large scale photographs, I made a series of exposures on bright northern globular clusters some years ago with the Mount Wilson reflectors The exposures varied in length. When only a few hundred stars were shown in a cluster, the spiral structure could almost invariably be traced, if the exposures were longer, the spiral arms became inconspicuous, or another set of arms, sometimes with different center and pitch, was found or imagined. The conclusion was reached that the phenomenon is wholly illusory. The significance to be attached to chance groupings and chance vacancies decreases remarkably with increasing exposure time. Nebulous obscurations that are reported to conceal the brighter stars are found, upon deeper penetration, to be ineffective for the more numerous faint stars, and therefore they cannot be real

Spiral structure is the easiest form to visualize in centrally concentrated random groupings-especially when the number, pitch, thickness, origin, length, symmetry, and definiteness of the spiral arms are all arbitrary. Structural features other than flattening and central concentration may be present, but it is certainly madvisable to conclude definitely, from knowledge of only a small percentage of the total number of the stars, that such structure occurs Probably in only one globular cluster (Messier 22) have stats as faint as the sun been photographed, and in only a tew of those studied for stellar distribution have

stars other than giants or supergrants been thoroughly examined.

The a priori argument against the existence of spiial form in the images of globular clusters is, of course, simply that the clusters are three-dimensional Cleanly traceable spiral aims would mean a most remarkable and unbelievable arrangement of stars in systems that are always nearly spherical. The discussion in eigh. 22 of the ellipticity of globular clusters will show how little they are flattened Even the images of the much sparser galactic clusters are very rarely so elongated that we can assume them to be essentially two-dimensional

18. On the Laws of Distribution. The first detailed numerical consideration of the space arrangement of stars in globular clusters was made by Professor E. C Pickering who examined the distribution in ω Centauri, 47 Tucanae, and Messier 13, and proposed general empirical relations connecting surface

density, y, with the distance from the center, r, in the forms

 $y = \int (1 - r^2) dz$ 

 $y = \int (1 - r)^n dz$ 

Subsequently much time has been devoted to studies of the laws of the distribution of stars in globular clusters. Various formulae relating the number of stars per unit volume, N, with distance from the center of the projected image

<sup>&</sup>lt;sup>1</sup> Hary Ann 26, Chap XI (1897)

unpublished. 29 HUBBLE, letter 30 Miss Woods, Harv Bull 764 (1922), see also A N 215, p 391 (1922) 31 Harv E 33 BAILEY, Pop Astr 28, p 518 (1920) 31 Harv Bull 848 (1927) 32 Zô-Sé Annals 10 (1918) 35 Mis 34 BAILEY, Harv Circ 266 (1924) DAVIS, Publ ASP 29, p 210 (1917) 37 Wash Na 36 Mt Wilson Contr 195 (1920) Ac Proc 7, p 152 (1921) 38 CHEVREMONT, BSAF 12, pp 16, 90 (1898) 39 BAILEY Harv Bull 798 (1924) 40 BAADE, letter of June 8, 1932 41 GROSSE, AN 246, P 2 42 BAADE, AN 230, p 353 (1930).

r, or with  $\varrho$ , the distance from the cluster center, have been derived (or assumed) and applied to published counts of stars We have, for instance, from von Zeipel,

$$N(\varrho) = \frac{1}{\pi} \int_{\varrho}^{R} \sqrt{(r^{2} - \varrho^{2})} \frac{d}{dr} \left( \frac{1}{r} \frac{du}{dr} \right) dr$$

where R is the radius of the cluster and s is the number of stars in the corre-

sponding unit area of the projected image

The problem of finding a law of space distribution from the law of apparent distribution in a globular star system has been solved by von Zeitel, who has been the leader in the attempt to deduce the structure of clusters from observation of stellar distribution. He was the first to utilize in this problem the principles of the theory of gases. Analogies with the kinetic theory have encouraged a number of theoretical and observational researches, but as yet no completely satisfactory representation of the observations has been found

It seems unnecessary to treat in detail the history, methods, successes, and failures of these various investigations of distribution. No other phase of the study of globular clusters has been so frequently and thoroughly described. Special attention should be called, however, to the discussions by H. C. Plummer, ten Bruggercate, Ströngren, Eddington, Jeans, Parvulesco, and Martens<sup>1</sup> A further important step has been made by von Zeipel and Lindgren, who proceed, from the assumption that the stars of different masses are distributed in equilibrium in relation to surrounding stars, to the determination, from the observed distribution, of the mean masses for various color classes and absolute luminosities. They have used the method with success in the study of the rich galactic cluster Messier 37, and Wallenguist has further discussed their analysis and applied the method to his own study of the magnitudes in Messier 36. Freundlich and Heiskanen have provisionally applied it to the study of the distribution of stars in globular clusters, but the observational material is yet too uncertain for satisfactory results.

That the discussions of the adiabatic or isothermal distributions of stars in globular clusters have been unsatisfactory in practice is not surprising, since the data from which comparisons have been made are inherently faulty. The best chance for improvement and successful application of the theory lies in the few rich galactic clusters from which the foreground and background stars can be satisfactorily differentiated. For the globular clusters, however, the crowded centers and the attendant difficulties with EHRHARD effect and background contrast vitlate the counts, except for the outer parts. Furthermore, the available counts deal with only the few hundred or few thousand supergiant stars; tens or hundreds of thousands of fainter stars, which must play a major rôle in stellar distribution, have not yet appreciably entered the investigations. TEN BRUGGENCATE has recognized the importance of ellipticity in the distribution of stars in globular clusters, but otherwise all discussions of the problem have

ignored this lack of radial symmetry.

The star counts that have been used for the study of globular clusters are almost exclusively those of Bailey at Harvard and of Pease and Shapley at Mount Wilson Photographs on a larger scale are needed. Special attention should be given to the brighter and more open globular clusters (ω Centauri, N.G.C. 3201, N.G.C 6397), and also to "giant-poor" anomalous systems and those clusters like N.G.C. 2477 that are possibly intermediate between the globular

See references in Harv Mon No 2 (1930). See also the later papers by HEURMANN and SIEDEMTOFF, ZiPhys 54, p 183 (1929) and ZiAstrophys 1, p. 67 (1930).

and the galactic types Tables and figures of the distribution of the stars in globular clusters are given for several of the brighter clusters by Pickering, Plummer, von Zeipel, and Heckmann and Siedenfoff

In conclusion, we must admit that the situation is not very hopeful. The frequency is (loughly) inversely proportional to the fourth power of the distance from the center, this holds only for giant stars in the typical globular clusters. The law of distribution of fainter stars is even less definitely known. We find them more widely dispersed than the giants, but we can say nothing of their distribution within the central sphere of ten parsecs diameter, where the crowding of brighter stars "burns out" the photographs

The distribution of brightness in a globular cluster as a function of distance from the center has been investigated by Hertzsprung for Messier 3, by Hogg

and by NABAKOV for Messiei 13, and by Schilt for & Centauii1

19. Luminosity Curves for Stars in Clusters Distribution in absolute brightness as well as in space can be satisfactorily studied as yet only for the giant and supergiant cluster stars. Although, as we have seen, the space distribution is not independent of the influence of dwarf stars, the fragmentary absolute luminosity curves have a meaning and a certainty that are essentially unimpaired by such forced neglect of the dwarfs. Moreover, with the use of more powerful telescopes, especially on the borders of bright southern clusters in high galactic latitude, we shall soon be able to extend both the general luminosity curves and the luminosity curves for specific color classes to stars as faint as the sun or fainter. In the near future we should therefore have for the globular clusters much more satisfactory data on the frequency of luminosities than we now have for stars of the general galactic system.

The labor of determining magnitudes and colors on a satisfactory photometric basis is so considerable that luminosity curves will come slowly, for only three globular clusters are the color and magnitude surveys at all extensive. It is necessary, therefore, to resort for the time being to general luminosity curves based on provisional magnitude scales, except for the giant stars in the three

systems for which results are herewith presented

a) Frequency Distribution of Grant Stars Observations of frequency distributions in Messier 3, Messier 13, and Messier 22 are combined to give Table 8. Results are tabulated for six intervals of color class iedder than fo Stars redder than k5 are grouped together, since the data are insufficient for class in alone, for classes b and a the observational limits cut off the luminosity curves so quickly that the results are not significant. Probably the curve for class f is also affected both by the confluence of giant and dwaif series and by the magnitude limitations of the catalogues Distance moduli used for reduction from apparent to absolute photovisual magnitudes are taken from Appendix A The absolute photovisual magnitude limits of the catalogues are +0,4 for Messici 22, +0.5 for Messier 13, and +1.6 for Messier 3. The table is therefore of low weight for stars fainter than  $M_{pv} = +0.5$  The picliminary maximum at 0,0 for interval fo to f5 is probably related to the humps in the general luminosity curves of these three clusters (Figure 41), which are caused mainly by an abundance of blue stars and variables The average dispersion of absolute magnitude for the various intervals of color is about half a magnitude, which is probably well in excess of the observational eriors

<sup>&</sup>lt;sup>1</sup> Hertzsprung, A N 207, p 89 (1918), Nabakov, R A J 1, p 109 (1924), Hogg. Harv Bull 870 (1929), Schilt, A J 38, p. 109 (1928), Pop Astr 36, p 296 (1928) See also Hogg's recent discussion of the luminosity distribution in six globular clusters A J 42, p 77 (1932)

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Alminio Photo- ional Magnitudo	Color Class  fo to 15   15 to go   go to g5   g5 to k0   k0 to k5   >k5									
m mathemano	10 to 13	15 to g0	g0 to g5	#5 to #0	ko to k5	>k5	All Colors			
-4,0 to -3,5	-	_	_	1	1	1	3			
-3,5 to -3,0	1	l –	_	1	_ [	11	13			
-3.0 to -2,5	_	2	-	5	13	18	13 38			
-2,5 to -2,0	1	1	5	16	11 1	5	39			
-2,0 to -1,5	1	7	34 28	32 32	6	2	82			
-1,5 to -1,0	8	24	28	32	4	1	97			
-1,0 to -0,5	18	85	71	20	1	_	195			
-0,5 to 0,0	103	136	73	7	1 1		320			
0,0 to +0,5	91	132	44	5	1 1	_	273			
10,5 to +1,0	38	31	8	1	_		78			
-1,0 to +1,5	85	_ 31	1				117			
Totals	346	449	264	120	38	38	1255			
	M									
<i>n</i>	111			<del>                                     </del>			59			
		17 1		1 1			KELDO			

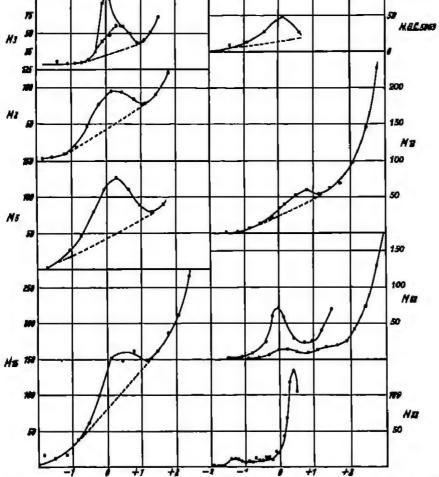


Fig. 11 Luminosity curves for eight globular clusters Ordinates are numbers of stars, abscises are photographic absolute magnitudes (approximate).

Until we have obtained data from other clusters, there is little point in fitting the usual exponential curves to the observations. Some of the asymmetries may be real in the curves representing magnitudes and practically disappear in the corresponding curves showing the distribution with respect to total radiation or mass

- b) The Preliminary Maximum General photographic luminosity curves based on provisional magnitude scales are given in Figure 11 for eight globular clusters. All the plotted material except that for NGC 5053 is derived from my work on Mount Wilson plates. The methods of estimating the magnitudes and some of the numerical data are published elsewhere. The curves suggest two general comments, which are followed below by a few special notes on the individual clusters.
- i There is a considerable variety in form, an indication of the impropriety of using any method of parallax determinations that depends on the form of only the brightest portion of the general luminosity curve
- 2 Without exception, all the globular clusters show preliminary maxima, which fall within half a magnitude of the median magnitude of cluster type variables, as indicated by the two heavy vertical lines in Figure 11. We have evidence in all of these globular clusters, though it is not shown graphically for NGC 5053 and Messier 22, that the general luminosity curve rises sleeply and high for stars fainter than the critical absolute luminosity near absolute magnitude zero. The bunching of stars at this particular brightness is probably of considerable significance in the economy of globular clusters. The resultant hump in the luminosity curves has possibilities in the measurement of distance

3 Details concerning Figure 11

- a) The preliminary maximum for Messier 3 is partially due to the hundred and fifty known variable stars, when the cluster type variables are omitted from the diagram we have the milder and fainter hump shown by the broken line and small circles
- b) For Messier 2, Messier 5, and Messier 15 the variable stars have not been excluded, but they are not sufficiently numerous, even in Messier 5, to contribute much to the very conspicuous preliminary maxima

c) The somewhat fragmentary luminosity curve for NGC 5053 is derived

from data published by BAADE2, with variables excluded

d) The preliminary maximum for Messier 13 is built up largely by stars of small or negative color index; the cluster has no definitely recognized cluster type Cepheids

e) For Messier 68 the two luminosity curves result from stars in different selected areas, measured on two plates. The curves are in fair agreement, a

second preliminary maximum at M = +1.4 is suggested

f) The fragmentary luminosity curve for Messiei 22 is based on an unpublished catalogue, prepared at Harvard from my Mount Wilson photographs. The wide displacement of the maximum from absolute magnitude zero suggests that the correct distance may be ten to twenty per cent larger than that given in Appendix A; but further work on the magnitudes of the fainter stars is necessary before anomalies of the luminosity curve can be taken seriously.

# f) The Forms of Clusters.

20. Definition and Difficulties. By the ellipticity of globular clusters we may choose to refer either to the symmetrical elongation of integrated images on photographs, or to the systematically greater number of stars along one axis of the projected image than along any other, as determined by detailed star

<sup>&</sup>lt;sup>1</sup> Mt Wilson Contr 155 (1917), 175 (1919) <sup>2</sup> Hamburg Mi

<sup>&</sup>lt;sup>3</sup> Hamburg Mitt 6, No 29 (1928)

counts Both of these phenomena can be explained most naturally by assuming that the clusters are oblate — that is, that the gradient of the space density of the stars differs in different directions from the center and is usually symmetrical about a polar axis and an equatorial plane Probably the forms of the integrated photographic images are related as directly to star density as are the counts.

It is difficult, however, to determine the actual bounds of a globular cluster along various radii, or even the limits of the projected image, because of (1) the unknown and possibly peculiar density laws in different directions for a flattened stellar system, (2) the confusion with foreground stars, (3) the present lack, near the edges of individual clusters, of sufficiently long exposures made

with large reflectors

The detection of the planes of symmetry, moreover, depends on the degree, the orientation, and the nature of the clipticity. Thus, if the ratio of minor to major axis is near unity, if the polar axis is nearly parallel to the line of sight, or if the property of concentration toward a plane is confined to the fainter unobserved stars in the cluster, the successful analysis of form is impossible

Early studies of globular clusters, such as BAILEY's star counts1, dealt with but one or two thousand stars in each cluster, while the underlying ellipticity usually becomes evident only when large numbers of stars are considered. Consequently, nothing very definite was known of the important fact of deformation until the systematic star counts on Mount Wilson photographs were analyzed. Later it was noted that the numerous faint stars frequently make their presence known on masse as well as in detailed counts, so that the diffuse integrated images of clusters photographed with small telescopes can be used to study cluster forms, even if few or no individual stars are shown. The counts, however, are sometimes more exarching. For example, in Messier 13, described below, the Harvard plates do not show, on inspection, the marked ellipticity revealed by the counts, they indicate, if anything, a slight olongation in a direction 45° from the major axis. The same is true of some other clusters. When an integrated image is clearly elliptical, the numerical ellipticity shown by star counts is very large. In a condensed cluster the EBERHARD effect and other difficulties may interfere seriously with the determination of the frequency of sters as a function of the distance from the center, but errors arising from such sources do not affect measures of the orientation of the major axis of the cluster image.

21. The Blongation of Messier 18. Among the globular clusters whose forms were investigated by the writer, partly in collaboration with Mr. Peasi, Mrs. Shapley, and Miss Sawyer, the Hercules cluster, Messier 13, best illustrates

the nature of the allipticity throughout a wide range in magnitude.

The stars in Messier 13 were counted on nine plates, and the results arranged for analysis in a framework of twelve equal radial sectors and a series of concentric rings. The plates are of various exposure times, ranging from one minute to five hours. The counts of the total number of stars in each of the twelve equal sectors show the amount of ellipticity and its change with magnitude. The counts for each of the zones between concentric circles show how the degree and direction of ellipticity varies with distance from the center of the cluster.

In Table 9 the numbers of stars are given for six different plates for each sector separately, but with the zones not differentiated. For the two photographs of longest exposure Table 10 again gives the number of stars in different sectors, but divides the material into four zones for each plate. The central regions are too much burned out to be included in the star counts.

<sup>1</sup> Hary Ann 76, No. 4 (1915).

PRASE and SHAPLEY, Mt Wilson Contr 129 (1917).

Table 9. Ellipticity for Different Exposures in Messier 13.

Duration	Total	T	Number of Stars in Sectors											
of Exposure	Number of Stars	15°	45ª	75*	105°	135°	165°	195°	2250	255°	285°	315*	343*	
6 <sup>n</sup> 15 22 37.5 94 300	5 800 7 700 14 150 16 600 25 000 30 000	163 296 734 749 1261 1126	1340	433 744 913 1475	235 396 859 1008 1590 1416	1580	213 314 638 853 1431 1232	569 779 1338	154 230 583 804 1343 1085	259 684 974 1486		235 309 852 963 1580 1368	305 738 763 1361	

Table 10. Ellipticity and Distance from Center in Messier 13. (Results from two plates.)

Distance		Number of Stars in Scotors										
from Center	15°	45°	75°	105°	135°	165°	195"	2250	255*	285°	315°	345°
2' to 4'	623	668	750	762	764	728	712	683	758	778	718	670
4' to 6'	358	361	423	464	476	386	330	352	402	438	479	394
6' to 8'	168	207	212	236	226	202	188	194	214	248	249	198
8' to 10'	112	104	90	128	114	115	108	114	112	126	134	99
3' to 5'	560	640	624	684	788	642	586	597	629	658	712	662
5' to 7'	362	374	410	471	431	360	302	292	358	396	424	394
7' to 9'	204	220	220	261	244	230	191	196	200	246	232	202
9' to 11'	141	136	116	118	130	129	131	124	130	157	134	100

The ellipticity is illustrated in Figure 12, which shows the amount and position angle of the elongation at different distances from the center. The cluster is

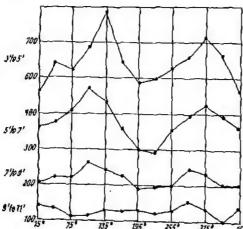


Fig. 12. Ellipticity of Messier 13 for different intervals of distance from the center. Ordinates are numbers of stars and abscissae are position angles.

seen, from these tables and from the figure, to be conspicuously elongated, showing approximately twenty-five per cent more stars in the direction of the major axis than in the direction perpendicular thereto. The ellipticity, which shows throughout the cluster from center to edge, appears in all magnitudes from the thirteenth to the twentleth and fainter, though it is relatively inconspicuous for the stars brighter than the fifteenth magnitude.

22. Ellipticity and Orientation of Globular Clusters. Over half a million stars have been counted in the course of the Mount Wilson and Harvard studies of the forms of globular clusters. By means of star counts the position angles of the major axes have been found for

twelve systems, and evidence of approximate circularity or asymmetry adduced for a few others. Direct estimates of the position angles for the integrated images of most of these clusters are found to agree closely with those determined from the laborious counts; hence further surveys of the forms have been made using only the direct estimates of ellipticity on small scale plates.

<sup>1</sup> H. Shapley and Martha B. Shapley, Mt Wilson Contr 160 (1918).

a) Orientation of Major Axes The allipticity and orientation given in columns 13 and 14 of Appendix A are based on a Harvard investigation<sup>1</sup>, except for starred values which are taken from the earlier Mount Wilson counts<sup>2</sup>. The allipticity is expressed as ten times the ratio of the minor to the major axis. The orientations, with respect to the galactic circle, are given only for those thirty-nine clusters in which the ellipticity is 8 or less, or if 9, only when the orientation could be certainly determined<sup>2</sup> The orientation with respect to the galactic circle is reckoned from the "galactic cast" (direction of increasing longitude) through the "galactic south"; negative angles consequently indicate reckoning from the east in the opposite direction

b) Inclination to Galactic Circle The data bearing on the relation of the elongation to the plane of the Galaxy are collected for thirty-seven globular clusters in Table 11 (N.G.C. 1866 and N.G.C. 1978, in the Large Magellanic

Cloud, are omitted from the table).

Table 11 Orientation of Globular Clusters

NGC	Cles	Geleciis Latitude	Distance from Galactic Piens kps	Degree of Blongation	Inclination to Galactic Circle
104	Ш	-45°	- 4,8	8	-55°
362	IΠ	-47	- 9,4	8	+65:
1851	II	-34,5	- 8,1	9	-75
1904	v	-28	- 9,6	9 9 8	+ 5
2298	VI	-15	- 6,9	8	+39
2419	VII	+23	+11,9	9	-56
2808	I	-11	- 3,1	9 8	+84
4833	VIII	- 8,5	- 2,2	8	-80.
5024	v	+79	+17,9	9	-79
5053	XI	+78	+17,0	8	-61
5139	VIII	+15	+ 1,8	8	+30
5272	VI	+77.5	+11,9	8	+54
5897	XI	+29	+ 8,0	8	-441
5904	V	+46	+ 7,8	9 8 9 9 8	+16
6101	X	-16	- 5.7	8	+35
6121	IX	+15	+ 1,9	9	+72
6139	П	+ 6	+ 3.1	. 9	-64
6144	XI	+15	+ 4,8		-22.
6205	V	+40	+ 6,6	9,5	-63
6235	x	+12	+ 5,9	8	+89
6266	IV	+ 7	+ 2,3	8	+16
6273	VIII	+ 9	+ 2,6	6	-28
6341	IV	+35	+ 6,4	8	+16:
6356	п	+ 9	+ 7,8:	9	-14
6362	x	-18	- 4.7	8	+78:
6397	IX	-12,5	- 1,2	9	+73
6402	VIII	+14	+ 4,8	9	+76
6440	V	+ 2	+ 1.71	8	+10:
6441	m	- 6,5	- 2,2	8	+40
6517	IV	+ 6	+ 5,2	8	- 41
6626	IV	- 7	- 2,0	9	+18
6638	VI	- 7.5	- 3.9	8	-27
6652	VII	-13	- 5,3	868989988898888888888888888888888888888	-111
6656	VII	- 9	- 1,1	8	+18
6779	X	+ 8	+ 2,8	8	+12:
7078	IV	-28	- 6,1	8	+11
7089	п	-36	- 8,2	9	-80

<sup>1</sup> SHAPLEY and SAWYER, Harv Bull 852 (1928).

SHAPLEY, Mt Wilson Comm 45 (1917).

That is, position angles without a colon in Hary Bull 852 (1927).

Although the estimates here presented are probably better than any previously made. I feel that they are not of much significance except for the few clusters for which the ellipticity is conspicuous and the orientation angle is given without a colon. The average deviation of a position angle from the values previously determined from Franklin-Adams charts is about 30°, an indication of the inherent difficulty of the estimates. Some of the clusters are definitely asymmetrical. For most of those not listed in Table 11 the deviations from circularity are small, or the clusters are too faint or too involved in a star field for useful determinations of form. Notwithstanding the difficulties and uncertainties, for all but eighteen of the ninety-three clusters in Appendix A the degree of ellipticity is estimated.

Attention should be paid in the future not so much to small and difficult objects as to closer analyses of the distinctly asymmetrical systems and of the brighter clusters in which the degrees of ellipticity can be studied with respect to colors and magnitudes. From detailed investigations, as you ZEIPEL has shown, we may hope to get information on the masses of stars of different rolors and luminosities, using as criteria of mass the distribution with respect to the

centers and to the hypothetical galactic planes within the clusters's.

Although the estimates of orientation are admittedly uncertain, the measures show definitely that large and small values are scattered throughout all distances from the galactic plane. In order that the equatorial plane of a cluster be parallel to the plane of the Galaxy, parallelism of the major axis with the galactic circle is a necessary though not a sufficient condition. We need to know the true form, or an equivalent, and get another component of the inclination, before we can fix the plane of the cluster in space; at present there is little prospect of measuring the true oblateness. The equatorial planes in the clusters with low inclinations of course may or may not be parallel to the galactic plane; those with high inclinations are certainly not parallel. There is no good evidence as yet that the clusters are not inclined at random in space.

23. Some Peculiar Clusters. A few globular clusters that depart considerably from a spherical form have been studied. They are of interest in connection with the possible dissolution of clusters and also in considerations of the distribu-

tion laws.

a) Messier 3 (N.G.C. 5272), Messier 5 (N.G.C. 5904), and Messier 62 (N.G.C. 6266). It is difficult to account for such pronounced and deep-scated asymmetries in globular clusters as those of Messier 3, Messier 5, and Messier 62. For Messier 3 the distance from other stellar systems is now, and probably for hundreds of millions of years has been, extremely great; the galactic latitude is +77°,5. There is no evidence of occulting matter in the cluster or in front of it that might be responsible for a spurious appearance of irregularity. The measure of asymmetry is illustrated by the following data4, based on the counts of two Mount Wilson plates, the numbers of stars being given for thirty degree intervals of position angle;

Position Angle. . . . . 15° 45° 75° 105° 135° 165° 195° 225° 285° 315° 345° Number of Stars . . . 244 234 246 220 198 242 222 282 292 321

Further work should be done on this cluster, as the counts on different plates

<sup>1</sup> H. SHAPLEY and MARTHA B. SHAPLEY, Mt Wilson Coutr 160 (1918). FREUNDLICH and HEISKANEN, Zf Phys 14, p. 226 (1923).

See discussion by TEN BRUGGENCATE, Die Sternhausen p. 72 (1927). Pease and Sharley, Mt Wilson Contr 129 (1917).

For Messier 5 we have comparable data from a long exposure plate showing 15000 stars, made by Prase and counted by Miss Davis<sup>1</sup>, the star numbers referring to a region between 3' and 15' from the cluster's center.

15° 45° 75° 105° 135° 165° 195° 225° 255° 285° 315° 345° . . 924 1016 972 861 693 783 870 978 1037 955 907 952 Position Angle Number of Stars .

The asymmetry of Messier 62 is shown numerically in the following counts based on a Mount Wilson photograph, a central burned-out area one minute in diameter being excluded

. 15° 45° 75° 105° 135° 165° 195° 225° 255° 285° 315° 345° Position Angle. Number of Stars 67 56 67 45 35 42 49 56 68 79 72 72

When opposite sectors are combined, the position angle of the major axis appears to be about 75°, the values of the angle estimated from the integrated image are 70° and 55° for two independent determinations.

Messier 62 is the most irregular globular cluster. Does absorbing nebulosity cause its apparent asymmetry? Or has collision or encounter deformed it?

b) Messier 19 (N.G C 6273). Figure 13 and the estimated ellipticities in Table 11 show that Messler 19 is the most elongated globular cluster so far studied. The circular coordinates of the diagram are position angles; the radial coordinates are relative numbers of stars in each thirty-degree sector. The position angle of the major axis of the diagram is 15°, and along this axis there are more than twice as many stars as along the minor axis Photographs show no evidence of a double nucleus. Since the galactic intitude is +9°, and the major axis is inclined less than thirty degrees to the galactic circle, the equatorial plane of the cluster is probably nearly parallel to the galactic plane.

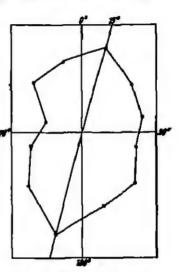


Fig 13. Diagram of star density in Messier 19

Considering this extreme example, we conclude that the flattening of a cluster is systematically of a lower order than that of spirals and the galactic system

c) Messier 22 (N G C 6656). The form of globular clusters near the galactic plane may have an important bearing on the relationship of the Galaxy and galactic clusters to the globular systems. Messier 22, in galactic latitude -9° and one of the nearest globular clusters, is significantly situated for a test of deformation and of the orientation of its central plane. On a photograph which shows more than seventy thousand stars from the twelfth to the twentieth magnitude, most of which are undoubtedly members of the cluster though it is located in the direction of a rich galactic star cloud, a detailed count has been made .

The number of stars in the direction of the major axis is nearly thirty per cent greater than the number along the minor axis. The orientation of only 18° and the high allipticity, which suggests that we see the cluster edgewise, indicate that it may lie nearly parallel to the galactic plane.

SHAPLBY and DAVIS, Publ ASP 30, p 164 (1918)

Mt Wilson Contr 160, p 7 (1918); Harv Bull 852, p. 25 (1927).

SHAPLEY and DUNCAM, Pop Astr 27, p. 100 (1919)

d)  $\omega$  Centaum (NGC 5139) The 128 cluster type variables in  $\omega$  Centaum appear to be preferentially along the equatomal plane of the system. Table 12 and Figure 14 illustrate this remarkable distribution. The data are obtained

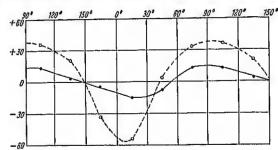


Fig 14 The distribution of stars in ω Centauri Ordinates are percentage excesses along the various radu indicated by the position angles (abscissae). The full line shows that the position angle of the major axis for all stars is about ninety degrees. For the variables alone (broken line) the axis is about the same, but the relative excess is three times as great

from Harvard plates, which show the ellipticity for all distances from the center.

Table 12 Distribution of 5000 Stars in  $\omega$  Centauri (Results from two plates)

Width of						Sec	tors						Mean
Zone	150	45°	75°	105°	135°	165°	195°	225°	255°	285°	315°	3450	MENT
3' to 6'	148	129	151	182	165	159	164	173	203	182	198	163	168
6 to 9	84	89	151	142	139	113	105	119	153	163	125	117	125
9 to 12	66	81	96	74	64	79	64	68	88	97	74	68	77
12 to 15	44	54	61	61	57	57	40	59	57	59	51	45	54
3 to 9	232	218	302	324	304	272	269	292	356	345	323	280	293
9 to 15	110	135	157	135	121	136	104	127	145	156	125	113	130
3 to 15	342	353	459	459	425	408	373	419	501	501	448	393	423
Variables	8	6	17	12	9	5	2	16	11	17	16	9	11

The numbers of variables in opposite sectors are combined in making the diagram. The relative amplitudes of the two curves show that towards the supposed plane of symmetry the variables are three times as condensed as the stars in general, and the latter exhibit such strong ellipticity that  $\omega$  Centauri is easily seen to be elongated on all photographs

24. The Structure of Galactic Clusters. a) Orientations. Only for the comparatively rich and compact galactic clusters is it possible to estimate the orientation. The loose systems—classes a, b, and c—are generally of too indefinite size and membership to show significant boundaries. Eighty-one clusters are found sufficiently condensed for examination, of these, fifty-seven show measurable orientations. Taken as a whole, the clusters appear to be oriented at random, within the uncertainty of the determinations. In points of detail, however, we see that the average inclination to the Galaxy differs from place to place, so that in some regions the clusters appear to be mainly aligned with the galactic circle, in others they are oriented approximately at right angles to it. Tables 13 and 14, showing the mean inclination for intervals of galactic longitude and latitude respectively, indicate that there is no correlation of orientation with either longitude or distance from the galactic plane.

Mt Wilson Comm 45 (1917)

<sup>&</sup>lt;sup>2</sup> Harv Mon 2, sec 33 (1930), see also Collinder, I and Circ No 2 (1931).

Table 13 Longitude and Inclination

Mosm Gaisotic Longitude	Number of Clusters	Mean Inclination	Moen Gelectio Longitude	Number of Charters	Megn Inclination
82°,6	5	60°	242°,2	6	30
128 ,0	5	55	279 1	5	62
156 ,5	5	33	302 ,3	5	53
183 ,5	5	42	322 ,3	5	31
201 .7	5	44	337 ,6	6	33
217 ,9	5	50			-

Table 14 Inclination and Distance from Galactic Plane

Mana Rain f (in persons)	Number of Clusters	Meen Indication	Mean Inchation	Number of Clusters	Moon Rain parsons)
677	5	45°	80°	7	69
425	5	38	70		203
265	5	47	66	4	167
196	5	34	59	7	279
143	1 5	51	47	5 1	215
100	5	52	40	5	131
62	5	47	29	6	281
30	5	39	18	5	175
17	6	53	12	4	222
6	6	47	4	4	108

b) The "shoulder" effect. A peculiarity in the distribution of stars has been observed in a number of galactic clusters, and leads to the conclusion that their dimensions are much larger than at first appears. Mosaier 67 plainly exhibits this unusual distribution. A summary of the average star density, photovisual magnitude, and color index is given in Table 15 for 232 stars of the cluster. There is no decrease of star density, or change of average magnitude or color outside a circle of 6',5 radius about the center of the cluster, but inside that circle the density, brightness, and redness of the stars increase towards the center.

Table 15. Average Star Density, Photovisual Magnitude, and Color Index in Messier 67

Distance from Center	No. of Stars	Area in Sq. Minutes	No. Stars per Square Martie	Ay Py. Mag.	Average Color Index	Namber Beokground	of Stars Claster
0',0- 2',5	35	19,6	1,78	12,49	+1,00	6	29
2,5-4,5	- 64	44,0	1,45	12,85	+1,00	13	51
4,5-6,5	49	69,1	0,71	12,32	+0,91	21	28
6,5-8,5	30	94,3	0,32	13,03	+0,81	28	2
8,5-10,5	34	119,5	0,28	13,06	+0,82	36	(-2)
10,5-11,5	20	69,1	0,29	13,11	+0,80	21	(-1)
Total	232	-	_	-	-	125	107

If it is assumed that the constant density outside the circle of radius 6',5 refers to the background or foreground stars, the cluster appears to be composed of about one hundred stars scattered over an area of radius 6',5. Further study, however, indicates that the evidence is misleading. The background density of 0,3 stars per square minute is nearly ten times as large as would be expected for the galactic latitude and the photovisual magnitude concerned. This condition suggests that the cluster with radius 6',5 is merely a well-marked nucleus of brighter and redder stars in a much larger system. Further counts made on Wolf-Palies photographic charts of all stars within a degree of the center of the cluster show that the system extends far beyond the limits of the plates used

for the magnitude work. The real diameter may be as much as one degree. If Messier 67 is roughly spherical in form, the space occupied by the nucleus is about a hundredth of the total volume of the cluster. The total membership is approximately five hundred stars between photovisual magnitudes ten and fifteen, but only the central concentration of one hundred and fifty stars is noticeable in an ordinary survey.

The "shoulder" effect has appeared in studies of Messiei 11, Messiei 37, and other galactic clusters Trumpler found it in Praesepe, the Pleiades, and h Persei<sup>1</sup> The change of radius with magnitude (outside the nucleus) is shown for h Persei in Figure 15, based on data accumulated by VAN MAANEN and

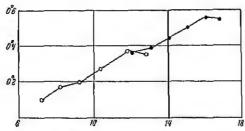


Fig 15 Relation of radius to magnitude for h Perser Ordinates are distances from the center in degrees, abscissae, photographic magnitudes (From Trumpler)

TRUMPLER, the effect is even more pronounced for the Pleiades and Praesepe

c) Additional Remarks on Galactic Clusters Various other studies have been made of the structure of galactic clusters. Of especial value is the work of von Zeipel and Lindgren on the magnitudes and distributions in Messier 37. The luminosities tabulated by them (Table 16) illustrate the double maximum for class a stars, a phenomenon that may be of some value in estimating the distances of galactic clusters. From the space distribution for different mathematical statements of the space distribution for different mathematical statements.

gnitudes and colors they have determined, by the ingenious method devised by von Zeipel, the approximate mean masses of the stars of various spectral classes. The method has been applied by Wallenguist to other galactic clusters

Table 16 Luminosity Curves for Various Color Classes in Messier 37

Limits of		Color Classes									
Magnitude	ь	a	ſ	g	k	m					
] 11,0	0	2	0	0	0	0					
11,0~11,5	0	4	1	1	0	0					
11,5-12,0	0	12	0	5	0	0					
12,0-12,5	7	21	0	10	0	0					
12,5-13,0	8	18	0	1	0	0					
13,0-13,5	20	16	3	0	1 .	0					
13.5 - 14.0	5	37	2	0	0	0					
14,0-14,5	3	29	7	1	0	0					
14,5-15,0	1	19	16	3	1	0					
[ 15.0	0	2	38	9	1	0					

KÜSTNER and CHEVALIER have made accurate modern catalogues of positions in several galactic clusters, which will be of importance for future analyses of proper motions. Photographic and photovisual magnitudes of stars in Messier 35, Messier 36, and other northern clusters, as determined by Wallenguist, afford material for the discussion of bolometric magnitudes, luminosity curves, density laws, and probable mean masses, as well as star colors. The ratio of field stars to cluster stars for five thousand stars in the faint northern cluster N G C 7789 is shown in Table 17.2. It is well to observe from the first line that the rapidly decreasing ratio does not mean the total absence of dwarf stars from the cluster, or even their relative scarcity.

<sup>&</sup>lt;sup>1</sup> Allegheny Publ 6, No 4 (1922)

<sup>&</sup>lt;sup>2</sup> Mt Wilson Contr 190, p 7 (1920)

Tabel 17 Star counts for NGC 7789

Photographic Magnitude Interval	] 16	16-17	17-15	18—19	19-20	Total
Clustor Stars Flaki Stars , Ratio	347 592 0,59	210 256 0,82	155 666 0,23	266 1178 0,23	126 1475 0,09	1104 4167

The structure of well known moving clusters and streams of stars, such as the groups in Taurus, Ursa Major, Scorpio, and Perseus, has been treated by numerous writers1. The group motions are essentially parallel to the galactic plane, though the clusters are flattened variously with respect to the direction of motion; the flattening of the Perseus and Ursa Major clusters is at right angles to the direction of motion, while the Scorpio group is flattened parallel to the galactic plane, and the Hyades cluster is nearly spherical

## g) The Transparency of Space.

25. Early Investigations of Light Scattering In all researches on the structure of the stellar universe the possibility of the loss of light in its passage through interstellar space must be recognized. If the loss of visual light due to absorption or scattering in space should be as much as a millionth of one por cent in each hundred million mules, stars thurty-five hundred light years away would appear about two magnitudes too faint. Uncertainty in the coefficient of scattering is, therefore, very serious in studies of the distances of faint stars.

The early work on light scattering indicated high absorption in space KAPTHYN in 1914 derived a coefficient, expressed in stellar magnitudes per parsec, of 0,0003, corresponding to a change of a tenth of a magnitude in color index for each three hundred parsecs of distance. At the beginning of the work on star clusters at Mount Wilson (1915) the following values were on record for the increase of color index with each parsec of distance.

Observer	 TONES	KAPTEYN	Kno	TURMER	VAN RHIJE
Coofficient	 0.00047	0,00031	0.0019	0,0030	0,00015

In all work yielding positive results the stars of small proper motion have appeared to be redder In view of the fact that small proper motion is now recognized as characteristic of highly luminous stars, this excess of redness is to be regarded as merely a correlate of bright absolute magnitude, rather than as indicative of light scattering. The work of SEARES and others has clearly shown differences in color for giants and dwarfs.

There remains, however, some evidence of a tenuous local cloud of absorbing matter, estimated by King as extending to a distance of thirty parsecs, reddening the stars at the rate of d = 0,0003 magnitudes per parsec, but affecting more distant stars only by a constant (and negligible) amount

A more declaive test of light scattering is to be found in the study of colors

of objects at much greater distances, such as those of globular clusters

26. Blue Stars in Messier 18. After KAPTRYN's work on light scattering, and the contemporary results of KING, JONES, and VAN RHIJN, which independently confirmed it, the discovery in 1915 of stars with negative color indices in Messler 13 was unexpected. A critical examination of photovisual and photographic magnitude scales failed to assign the apparent blueness of the cluster

<sup>&</sup>lt;sup>1</sup> See references in Appendix D of Harv Mon No 2 (1930).

See references in Apparatus of Harv Mon No 2 (1930)

Bee references in bibliography of Harv Mon No 2 (1930)

Mt Wilson Contr 116 (1915)

stars to observational error. Out of 495 stars with well determined color indices, 86 were found to be of color class b, and 63 of class a

With a scattering coefficient of d=0.0003 (Kapienn's last value), and an assumed distance for the cluster of as little as a thousand paisecs, practically no negative colors should appear if the stars are of usual spectral classes. With the obviously better parallax of 0",0001, the color index produced by Kapii yn scattering should be +3.0 for stars of spectral class A, and many color indices should be greater than +4 in a typical distribution of spectral classes. It was found from the Mount Wilson photometric work that the range of color index

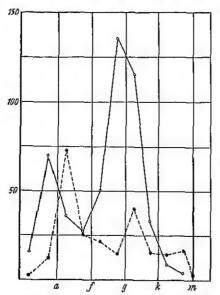


Fig 16 Frequency of color classes in Messier 13 (full line) and in the neighborhood of the sun (Yerkes Actinometry) Coordinates are relative numbers of stars and color classes

observed in Messiei 13 is the same as that found among nearby galactic stars, as illustrated in Figure 16 (The direct correspondence of color class with spectral class in this cluster has been verified by the spectrograms made by Pease<sup>1</sup>). There are no color indices in the cluster larger than - $\frac{1}{2}$ . The largest admissible color excess appears to be about  $0^{\rm m}$ , 1, and, even if this excess is attributed entirely to light scattering, we derive d=0.00001, a thriften of the value derived by Kapieyn, and a fifteenth of the value found by van Rhijn from a consideration of the stars in the Yerkes Actinometry

The foregoing upper limit of scattering is so small as to be entirely negligible in dealing with nearby stars in high galactic latitudes, but a more accurate value is desirable, and fortunately it can be found from studies of external stellar systems.

27 Faint Blue Stars in the Milky Way. The galactic latitude of Messier 13 is +40° fhat light scattering is absent in this direction is no proof that it does not occur elsewhere, especially in low ga-

lactic latitudes where stars and diffuse nebulosity are concentrated. To make the test more comprehensive with respect to galactic latitude and longitude, the search for negative color indices has been carried out in several distant cluster systems, on the assumption that a normal range of color index and the presence of numerous blue stars are strong evidence of the transparency of space in the directions and to the distances considered. The results are in Table 18, where the observed extremes of color are shown in the fourth and fifth columns, and, in the next two columns, the mean photovisual magnitude and mean color index for a group (usually ten) of the faintest blue stars. The distances in the last column are taken from the tables in Appendices A and B

Similar results have been obtained for faint stars in four Milky Way fields, and Seares has found faint blue stars in the Selected Areas that fall in low galactic latitude

Considering the relatively large distances of the tabulated objects, and their wide distribution, we appear justified in generalizing the results of the

See ciph 12 SHAPLEY, Mt Wilson Comm 44 (1917)

Table 18 Test for Space Transparency in Various Regions

Citation	Galactic		Color	Index	Moun Py	Mars Color	Distance in
	Longitude Latitude		Largest	Smallest	Mag.	Index	Elloparace
Moreter 3	12° 27 33 139 142 154 189 332 338	+78° +40 -28 + 1 + 3 - 1 + 46 - 3	+1,77 +1,42 +1,50 +2,12 +1,50 +1,31 +2,00 +1,67 +2,05 +2,06	-0,39 -0,52 -0,21 -0,45 -0,30 -0,15 -0,04 -0,11 -0,45 -0,16	15,1 16,54 16,0 13,5 12,5 11,5 12,3 14,6 14,34 14,32	-0,16 -0,34 -0,14 -0,16 -0,23 -0,07 -0,02 -0,10 -0,28 -0,08	12,2 10,3 13,1 1,1 1,2 0,8 0,8, 10,8 6,8

study of Messler 13, and in concluding that interstellar media, throughout the distances here concerned, have no serious effect on the color of light. This conclusion does not bear on obstruction of light by recognised diffuse nebulosity (dark and bright), nor on the colors of nebulous stars, nor on the absorption within galactic clusters which has been found lately by several investigators and sometimes interpreted, perhaps prematurely, as evidence of strong general space absorption

28. Colors in Other Distant Objects. The magnitudes and color indices of thirty-eight supergiant red stars in N G C 7006 have been measured. Even at a distance more than five times that of Messier 13, no abnormal redness appears in this cluster, and there is no other peculiarity in its star colors, although its radiation has travelled through space for an interval of 180000 years. The mean color index of 1,10 for the brightest thirty-five stars, which is comparable with that of 1,15 for Messier 3 and 1,03 for Messier 13, shows that the reddening does not exceed a tenth of a magnitude. Therefore the absorption coefficient, expressed as change of color index for each parsec of distance, is d < 0,000002

This same coefficient of space absorption was found by LUNDMARK and LINDHLAD<sup>8</sup> in a study of the Andromeda Nebula. Investigations at Harvard of the cloud of three hundred bright extra-galactic nebulae in Coma and Virgo<sup>4</sup> have resulted in the determination of the coefficient, d < 0.00000007

29. Messier 5 and the Relative Speeds of Blue and Yeilow Light. One significant consequence of the study of variables in Messier 5 has been a determination of the relative speeds of light of different wave lengths. Periods ranging from six to twenty hours, with an average of thirteen hours, have been found for a large number of stars; many of them are known to within a fraction of a second. The steep rise to maximum brightness of a typical cluster type Cepheid variable makes the time of median magnitude on the ascending branch more accurately determinable than the times of maximum or minimum. It was found by Wendell at Harvard and by the writer at Princeton that the time of median magnitude can be determined to within two or three minutes.

For the revision of the periods and for the test of the speed of light I made five special series of photographs of Messier 5 in 1917, using the 60-inch reflector of the Mount Wilson Observatory. The exposures of twenty to thirty minutes

<sup>1</sup> SEARES and HUBBLE, Mt Wilson Contr 187 (1920)

SHAPLEY, Mt Wilson Contr 165, p 5 (1918); see also SHAPLEY and MAYBERRY, Mt Wilson Comm 74 (1921).

Ap J 50, p. 386 (1919) Through an error the value is printed ten times too small Shapley and Ames, Harv Circ 294 (1926)

Harv Ann 73, Part 2 (1917), Harv Bull 763 (1922), Harv Ropr 5 (1923), Wash Nat Ac Proc 9, p 386 (1923); see also ciph 16 above

that were necessary to record the yellow light with an isochromatic plate and yellow filter were interrupted in the middle for an exposure of one or two minutes on an ordinary plate sensitive to blue light. In this manner the variable stars were photographic in two regions of the spectrum at essentially identical times. Photographic and photovisual observations were carried on throughout several hours of the night. Each run of plates gives fragments of the light curves of all the variables, but since the average period is thritten hours, for only a few stars in each series was the light rising from minimum through median to maximum during a given night's run on the cluster.

The measurement of the plates yielded 6300 magnitudes, from which fourteen measures of the times of median magnitude both in blue and in yellow light were obtained for eleven different variables. The results appear in Table 19. The maximum effective wave length for blue light is approximately 4500 Å, and for yellow light, 5500 Å. The observed difference in the times, t, of rise to median

magnitude,

$$\Delta t = t_{\rm pg} - t_{\rm pv}$$

is given in thousandths of a day in the fourth column. Thus a positive residual would indicate that the yellow light is measured as arriving first

Table 19 Differences in Times of Median Magnitudes

Number of Variable	Photographic Range	Photovisual Range	11	Weight
1	1 <sup>m</sup> ,2	O <sup>10</sup> ,7	{ +01,009 -0,001	3 2
4	1,4	0,9	-0,005	1
8	1,1	0,7	-0.012	1
12	1,3	1,0	-0 ,005	2
81	1,5	1,05	+0,001	1
20	0,9	0 ,7	0,000	2
28	1,2	0,8	+0,006	2
59	1,0	0,7	-0,003	1
63	1,2	0,9	-0.002	3
64	1,0	0,7	-10,005	1
18	1 ,1	8, 0	100,001	3 2

It is seen immediately that there is no measurable difference in velocity, the values of  $\Delta t$  being of the order of the uncertainties of measurement, six are positive, seven are negative, and one is zero. The mean value of the difference in time required for the passage of blue and of yellow light over the distance from the cluster to the earth is

Blue - Yellow = 
$$-0^{d}$$
,00012  $\pm 0^{d}$ ,0007 =  $-10$  seconds  $\pm 60$  seconds.

We have determined in this experiment merely an upper limit to the difference in speed. We find that since the distance to the cluster is approximately 11000 parsecs, light of these two colors, which differ by twenty-five per cent in wave length, differs in time of arrival at the earth by no more than one minute after traversing space for more than thirty-five thousand years. In other words, the relative size of the probable error indicates that the chances are even that the speeds of blue and yellow light do not differ by more than one part in twenty thousand million; probably they do not differ at all

From eleven determinations of the maxima for nine variables in Messier 5, a similar equality in speed was found for blue and yellow light. In this result,

also, the probable error exceeds the observed average difference, but the determination has much less weight than the one based on median magnitudes

It is to be noted in conclusion, however, that the essential equality in speed does not necessarily indicate a perfectly transparent interstellar medium. As GROOSMULLER1, among others, has pointed out, a large amount of dust and gas can exist in space without measurably affecting the speed of light.

### h) The Distances and Dimensions of Clusters.

80. The Photographic Period-Luminosity Curve. The correlation of absolute magnitude with period for Cepheid variables is discussed in detail elsewhere?. But the importance of the period-luminosity curve in obtaining the distances of globular clusters is sufficiently great to justify a brief consideration here of some outstanding features Because of their bearing on the investigations of cluster magnitudes and distances, it is well to mention the derivation of the adopted photographic period-luminosity curve, and the determination of its

zero point,

a) The Photographic Period-Luminosity Curve The curve relating period to magnitude was obtained from variables in the Small Magellanic Cloud. The plot of the median apparent photographic magnitudes against logarithms of the periods for 106 variables is shown in Figure 17 Points of low weight are enclosed in circles, and the periods determined by Miss LEAVITT are indicated by crosses. A few of the stars diverging most widely from the curve may not be actual members of the system, but the fairly high galactic latitude (-33°) makes rather unlikely the occurrence of typical Cephelds except as members of the Cloud.

The deviations from the curve in Figure 17 are not larger than might be expected in view of the difficulties of observation. The average deviation in magnitude of the thirty-two variables whose periods Miss LEAVITT obtained is 0,19, for the seventy-four other stars it is 0,25, for all, 0,23 The systematic magnitude deviation from the curve is -0,063 for the LEAVITT variables and +0,049 for the others, showing a negligible systematic difference between the earlier and the later work

Some of the dispersion in magnitude can be attributed to the thickness of the Cloud in the line of sight, but between the variables at the near and far edges this correction amounts to only 0.14 magnitudes. If  $\alpha$  is the angular radius of a sensibly spherical system, the maximum dispersion in magnitude arising from the thickness is given with sufficient approximation for remote systems by

$$\Delta m = 5 \log \left[ (1 + \sin \alpha)/(1 - \sin \alpha) \right]$$

The correction is thus independent of the distance and real thickness. The diameter of the Small Cloud is 3°,6 and the extreme correction to mean values

is therefore less than a tenth of a magnitude,

Other factors contributing to residuals from the pornod-luminosity curvo are the EMERHARD effect and obstruction by nebulosity. To these may be added actual deviations for the periods and magnitudes from average conditions—that is, a true scattering which may arise from differences in mass, structure, or other physical properties. We should also consider errors in the periods and the observational uncertainties for individual variables, which may easily amount to two tenths of a magnitude. Errors due to the failure to resolve double stars are not likely to be serious

<sup>1</sup> HEMBL on DAMPKHING, 22, p 153 (1924)

LUDENDORFF, Volume VI, 2, chapter 2.

In Figure 47 only two stars with periods shorter than a day are included. There appear to be many others of this sort in the Cloud<sup>1</sup>, but they are not considered in the present discussion because of the relative weakness of the magnitude scale fainter than 17,0. These cluster type variables will soon be studied with a large reflector, when short exposure photographs and better magnitude sequences can be used.

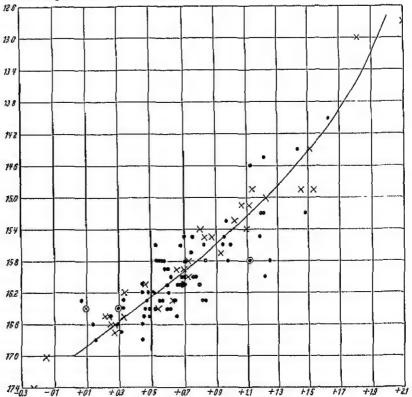


Fig. 17 Photographic period-lummosity curve Ordinates are apparent magnitudes; abscissae are logarithms of the periods Crosses refer to periods determined by Miss Leavitt Circles enclose values of low weight

By grouping the points plotted in Figure 17, first in order of the logarithms of the period, and then in order of apparent magnitude, we get the two sets of means shown in Table 20. All magnitudes of Cepheids in this chapter are median values: that is, (max + min)/2

Table 20 Data for the Photographic Period-Luminosity Curve

Mean I og P	Mean Magnitude	Number	Absolute Magnitude	Mean Magnitude	Mean Log P	Number	Absolute Magnitude
-0,194	17,2	2	-0,12	17,00	+0,054	4	~0,32
+0,253	16.51	17	-0,81	16,44	0,437	33	0,88
0,610	16,08	53	-1,24	15,99	0,677	36	-1,33
0,986	15,48	21	1,84	15,51	0,871	17	1,81
1,357	14,93	11	2,39	15,05	1,267	9	-2,27
1,961	12,90	2	-4,42	14,38	1,380	5	-2,94
				12,90	1,961	2	-4,42

<sup>1</sup> SHAPLEY, Wash Nat Ac Proc 8, p 69 (1922)

The distance modulus for the Small Magellanic Cloud (see crph 39) is 17.32, and the absolute magnitudes for variables in the Cloud are therefore given by M=m-17.32. In the fourth and eighth columns of Table 20 are the absolute magnitudes corresponding to mean values of  $\log P$ 

A by-product of work on the period-luminosity curve is a determination of the relation between period and spectral class, shown in Figure 18 The period-

Spectrum curve is discussed by Ludendorff, in Vol VI, Chapter 2, of this Handbuch. It may be noted here that the relation holds for long-pariod and RV Tauri variables, as well as for the cluster types.

b) The zero point, MAIthough the form of the period-luminosity curve and the deviations from it are now fairly well known, we remain for the time being in a state of suspense with regard to the zero point Originally based on

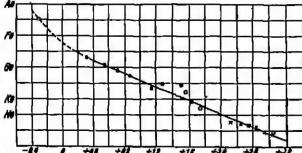


Fig 48. The relation of spectral class (ordinates) to logarithm of the period (abscissed) for variable stars. Open circles refer to RV Tauri variables, crosses to long period variables, dots to Copheid variables, and the open square to the mean cluster type Copheids.

the parallactic motions of the few bright Cepheld variables for which accurate Proper motions were available, the zero point has been the target of much discussion and suggested revision.

KAPTEYN and VAN RHIJN believed that the large observed proper motions of cluster type Cepheids in the Galaxy show them to be dwarfs and necessitate an enormous shift of the zero point I had adopted, with consequent disaster for my measures of galactic dimensions. Later discussions of the proper motions and radial velocities of these variable stars indicated, however, that they could not be used in the manner adopted by KAPTEYN and VAN RHIJN. Many of the stars of this subtype belong to the well known high velocity group, and when allowance is made for their high space velocities, the proper motion data are not in disagreement with the zero point indicated by the classical Copheids.

The most thorough study of the zero point is that by R E Wilson. He concluded that the distances that I had based on the period-luminosity relation should be decreased by twenty or thirty per cent, but in view of the new generally accepted Kapteyn correction to Boss' proper motions, this change in the zero point by Wilson may be, as he himself pointed out, largely effaced. In the most recent discussions of Cepheid motions Oort gets 1,06 ± 0,26 (m. e) as the correction factor to my parallaxes, using Mount Wilson measures of radial velocity.

So far as they go, the trigonometric parallaxes in the Yale Catalogue and the Mount Wilson and Upsala spectroscopic parallaxes support the system based on the period-luminosity curve. VAN MAANEN has found satisfactory agreement of his trigonometric parallaxes with the values from the period-luminosity relation.

<sup>&</sup>lt;sup>2</sup> BAN 1, p. 37 (1922). Hary Circ 237 (1922); R.E. Wilson, A J 35, p 35 (1923).

In view of Wilson's work, however, and of other indications that the nearer galactic Cepheids give too bright a zero point 1, I have made a provisional correction of +0,23 magnitudes, which reduces to 0,00 the absolute photographic magnitude of cluster type variables. The correction has been applied to the period-luminosity curves, and to all the computed distances appearing in this chapter. It amounts to a systematic decrease of eleven per cent in the distances computed from older period-luminosity curves.

Awaiting the completion in a few years of the McCormick and Mount Wilson investigations of the proper motions of a large number of galactic Cepheids, we adopt this corrected zero point and the scale of distances dependent on it

The resulting absolute magnitudes in clusters and Magellanic Clouds are accordant with a large body of astronomical observations, and compatible with recent astrophysical theory. There seems to be no serious inconsistency in the resulting luminosities, except that the revision has made the maximum brightness of stars in globular clusters surprisingly low. I am inclined to predict that the correction to the zero point now adopted will never exceed a quarter of a magnitude, and that it may be in either direction, but this prediction should be made with caution because of the increasing evidence of peculiar drifts and of heterogeneity in the star structure in the immediate vicinity of the sun

81. Distances of Globular Clusters Obtained from Cepheids and Bright Stars. From the period-luminosity curve distances can be determined directly for all the globular clusters in which the Cepheid variables have been studied and magnitude scales determined. In Table 21 are collected all the relevant observational data now available from my own studies<sup>2</sup>, and also, for N G C 5053 and N G C 5466, the magnitudes measured by BAADE with the Bergedon reflector For the sake of homogeneity, the magnitudes measured at Bonn by Kusiner

for three globular clusters (M3, M15, and M56) were not used

a) The Observations The new material represents a considerable expansion over that in hand twelve years ago. The determination, in 1917, of the parallaxes of sixty-eight globular clusters included only seven for which the variable stars had been studied, and for two of these the preliminary data could not be used quantitatively. As variable stars in clusters are fundamental in calibrating methods of determining distances, I have given considerable attention since 1917 to the discovery and observation of variable stars in clusters. Mount Wilson plates and various series in the Harvard collection have been used for this work. I am indebted to several assistants at Mount Wilson and Harvard for aiding in this laborious research, and especially to Miss Sawyer who has taken an active part in the recent revision of cluster distances.

There are now nineteen instead of five clusters in which variable stars have been measured sufficiently to enter the new determination of distances. Of the 730 variable stars in these nineteen clusters, 524 have been studied enough to be useful in fixing the "median magnitudes" for the clusters concerned. In 1917 the absolute magnitudes of the high luminosity stars had been measured for only twenty-eight clusters, we now have measures on the brighter stars in forty-eight systems.

b) The Methods For a new determination of distances and distribution, I have followed in principle, though not in detail, the methods developed and

<sup>&</sup>lt;sup>1</sup> See various papers by Ten Bruggencate, Curtis, Doig, Kienle, Mai mquist, and Strömberg Since this chapter was written in 1930 there have been further discussions of the zero point by Gerasimovič [A J 41, p 17 (1931)], Nordsfröm [Lund Obs Circ 2 (1931)], and others

<sup>&</sup>lt;sup>3</sup> From Hary Bull 869 (1929)

<sup>3</sup> Harv Bull 869 (1929)

Table 24 Magnitudes of Variables and Bright Stars

Table 21 Magnitudes of Variables and Bright Stars  Photographic Magnitude Preliminary Motor								
N G.C.	C=	Verlebin	Photographic 25 Br	6th Star	30th Bitter	Preliminary Modulus	Hotes	
104	ш	_	13,09	12,4	13,4	14,33	Note 1, 47 Tucanno	
288	х		14.80	14,5	15,1	15,87	Note 2	
362	пі	15.5 (4)	14,12	13,5	14,8	15,49		
1904	V	-	15,29	15,01	15.73	16,61	Mession 79	
2808	I	_	14.9	14,3	15,4	16,25		
3201	X	14.52 (5)	13,52	13,3	13,8	14,57	Note 3	
4147	IX	16,8 (1)	16,58	16,23	16,93	16,99	GP, note 6	
4590	X	15,90 (6)	14,80	14,31	15,08	15,87	Monator 68	
5024	V		15,07	14,94	15,26	16,36	Mondor 53	
5053	XI	16,19 (8)	15,65	15,1	16,0	16,15	GP	
5139	VIII	14,37 (5)	12,91	12,6	13,1	14,22	∞ Contanri	
5272	IV	15,50 (8)	14,23	13,92	14,45	15,48	Memier 3	
5466	XП	16,17 (6)	15.72	15,1	16,2	16,16	GP	
5897	XI	10,17 (0)	15,15	14,9	15.4	16,16		
5904	v	15,26 (8)	13.97	13.74	14,27	15,26	Mondor 5	
6093	п	15,20 (0)	14,88	14,72	15.09	16,24		
6121	ıx	14,27 (6)	13,88	13,3	14,4	14,29	Note 4, GP, Monaler	
	IX	14,47 (0)	15,76	15,2	16,3	16,22	GP	
6144	x	_		15,2	15,9	16,57		
6171	v	45 20 (4)	15,46	13,45	13,92	15,10	Momier 13, Noto 5	
6205	IX	15,20 (4)	13,75		14,31	15,07	Mossior 12	
6218		_	13,97	13,56	16,37	17,36		
6229	VΠ	, –	16,18	15,90	16,8	17,28		
6235	X	-	16,17	15.7	14,38	15,17	Memier 10	
6254	νп		14,06	13,35		16,37	Irrog , Messier 62	
6266	IA	16,40 (6)	15,87	15,6	16,1	16,70	Monder 9	
6333	VIII	-	15,61	15,08	15,88	15,18	Messier 92	
6341	IV	_	13,86	13,60	14,16		indaki. 55	
6356	ш	_	17,16	16,86	17,44	18,51	GP	
6397	IX	. –	12,61	11,9	13.1	13,67	Mosslor 14	
6402	AIII	_	15,44	14,85	15,86	16,56	HILLSON 14	
6535†	XI:		15,9	15.3	16,4	16,89	Noto 3	
6541	III	14,42 (4)	13,35	12,7	13,8	14,53	Mondor 28	
6626	IV	_	14,87	14,49	15,11	16,14	ACCEPTANT 40	
6638	VI	( l	16,22	15,90	16,60	17,48	Manufact 00	
6656	VII	14,06 (5)	12,93	12,80	13,26	14,12	Mounter 22	
6712	IX	-	16,10	15.65	16,36	17,17	ł	
6723	VII	15.33 (6)	14,20	13.7	14,8	15.37		
6752	VI		13,26	12,8	13,6	14,47	341 26	
6779	X	_	15,31	14,98	15,70	16,39	Momier 56	
6809	XI	_	13,58	12,9	14,2	14,58	Memler 55	
6864	I	( -	17,06	16,76	17,35	18,43	Mossior 75	
6934	IIIV	-	15,78	15,33	16,11	16,91	Wlan ac	
6981	IX	16,80 (8)	15,86	15.53	16,20	16,86	Messier 72	
7006	1	18,96 (6)	17,50	16,99	17,89	18,91	** .1	
7078	IV	15,63 (7)	14,31	14,13	14,55	15.63	Mondor 15	
7089	П	15.71 (4)	14,61	14,25	14,76	15,81	Momier 2	
7099	v		14,63	13,77	15,04	15,80	Memior 30	
7492	XII	-	16,82	16,3	17,1	17,22	GP	

<sup>1</sup> The long period variables in 47 Tucanas (Harv Bull 783) could not be safely used in measuring the distance. 2 The mean magnitude of the 25 brightest stars was determined at Mount Wilson to be 14,81, with a range of 14,38 to 15,04. 3 The magnitudes of N G C, 3204 and N G C, 6541 may be considerably in error due to unsatisfactory comparison sequences. They are not included in the determination of the reduction curves for apparent integrated magnitudes and diameters, though they are appropriately used in constructing Table 22. 4 For N G,C, 6121 the sore point of the magnitude scale depends on both Harvard and Mount Wilson measures of Mount Wilson plates. 5 The measurement of the 25 brightest stars was determined at Harvard to be 13,76 with a range of 13,4 to 14,1 6 Baans has recently studied this difficult system [A N 239, p. 353 (1930)] and his better results give a modulus 16°,52 ± 0°,05. He correctly reassigns the cluster to a much earlier class (on the basis of new long exposure plates)

described in 1917. As before, the reasonable assumption is made that the median absolute magnitude of variables with periods less than a day is constant from cluster to cluster. The difference between the median magnitudes of the variables and the magnitudes of the brightest stars is again found, on the average, to be so definite a quantity that brighter star magnitudes themselves can be used as criteria for those clusters where variable stars are lacking or have not been analyzed. We go farther by taking measures of integrated apparent brightness (total magnitude) and angular diameter as criteria of relative distance, using these measures, after appropriate calibration, not only to strengthen the determination for the forty-eight clusters whose variables and bright stars have been studied in some detail (Table 21), but also for the other forty-five clusters now known in the galactic system for which we have as yet no measures of variables or of individual bright stars.

c) The Results A few of the essential details of Table 21 should be mentioned. The classes in the second column are those described in ciph 6 and listed for all globular clusters in Appendix A. The apparent median magnitude of cluster type variables is in the third column. When a cluster contains long period Cepheids, their magnitudes are reduced to the cluster type median by means of the period-luminosity relation and are then combined with

the magnitudes of the cluster type variables

Since we have adopted zero as the absolute photographic magnitude for cluster type Cepheids, the third column actually contains a direct determination for numeteen clusters of the distance modulus, m-M=5 ( $\log d-1$ ), where d is the distance in parsecs and m is the apparent median photographic magnitude.

The parenthetical numbers in the third column are the combining weights assigned to the mean median magnitudes of the variables in each cluster. These weights depend on the number of variables, on the detail with which periods and light curves are known, and on the estimated accuracy of the magnitudes. The means of the third column are used in conjunction with the distance moduli derivable from the next three columns to determine the preliminary modulus in the seventh column.

The fourth column contains the mean magnitude of the twenty-five brightest stars (after the exclusion of five of maximum brightness in order to avoid, or at least to diminish, the effect of optical doubles and of the chance superposition of bright field stars). A weakness in using this method lies in the dependence of the area in each cluster surveyed on the compactness or distance of the cluster, or on the richness of the foreground of galactic stars. Uniformity of selection was strenuously sought, and I am convinced that for most clusters the mean of the twenty-five brightest stars, as well as the magnitude of the thritieth star, would not be appreciably disturbed by including or excluding too much of the dense central region

In the following columns are given the apparent magnitudes of the sixth and thirtieth stars in each cluster, the sixth star is the brightest object and the thirtieth the faintest included in the mean of the twenty-five brightest

The difference between the median magnitudes of the cluster type variables (third column) and the magnitudes of the three succeeding columns are found to depend on the class of the cluster. Table 22 gives the readings from the smooth curves that represent the changes of the three sets of differences with class. In the earlier work a single constant value, 1,28, for the difference between the median and the twenty-five brightest, was used; the two other sets of differences were not then considered in obtaining distances. The range of variation now found for med.—25 br. is from 0,92 (Class XII) to 1,34 (Class I).

The present method of using three different points in the sequence of apparent magnitudes is essentially equivalent to comparing, from one cluster to another, the general luminosity curves for giant stars. Its advantage over provious practice lies in the allowance it makes for abnormal distribution—or even small deviations from the average—in limited groups of stars. The extended method is obviously justified by the non-parallelism of the three curves representing the relation of reduction factors to class of cluster.

A comparison of the modulus from variable stars alone (third column of Table 21) with the preliminary modulus (seventh column) based on bright stars and variables together, indicates how satisfactorily the data for bright stars agree with the results from the variables. The agreement shows, in fact, to what extent one typical cluster is comparable with another inside the various classes.

d) Giant-poor Clusters. A number of the clusters of the more open classes (Classes IX—XII) were found upon examinations for star frequency to be poor in giant stars. Their luminosity curves are abnormal. Such objects are indicated by the letters GP in the last column of Table 21. They were not used in deriving differences in Table 22 for normal clusters, and the irregular cluster Messler 62 (N.G.C 6266) was also excluded.

Table 22 Reduction to the Median Magnitude of Cluster Type	Variable Stars.
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Class of Chapter	Median — 25 Br	Medias 61 Star	Median—30th Star	
I	1,34	1,77	1,04	
II	1,33	1,74	1,01	
ш	1,32	1,71	0,98	
IV	1,30	1,68	0,95	
v	1,28	1,64	0,92	
VI	1,24	1,60	0,89	
VII	1,20	1,56	0,86	
AIII	1,15	1,51	0,83	
TX.	1,10	1,46	0,80	
x	1,05	1,40	0,77	
XI	0,99 :	1,34	0.74	
XII	0,92	1,29	0,71	

The GP clusters with measured variables were used, however, to determine special reduction factors for all the "giant-poor" clusters. A study of these abnormal systems shows that the following mean values can be satisfactorily used in reducing the magnitude measures to the standard median magnitude of the cluster type variables.

e) The System of Weighting. For the typical clusters for which bright star magnitudes have been measured (Table 21) the reductions to "median magnitude" are made directly with the aid of Table 22, and the three resulting determinations for each cluster are combined with weights 2, 1, 1, for the mean of 25, 6th, and 30th, respectively, to get the preliminary distance modulus. The modulus from variable stars, when available, was, of course, included with appropriate weight in the mean value in the seventh column of Table 21. The final weight of each preliminary modulus is therefore the weight in the third column (from the variable stars) increased by four.

32 Distances of Globular Clusters Obtained from Diameters and Integrated Magnitudes. Further steps in deriving the distances of the clusters are now obvious and need only be summarized. Plotting the values of the preliminary modulus in Table 21 first against the angular diameter and then against integrated brightness<sup>1</sup>, we get two empirical curves that may be used for the derivation of the distance modulus of any globular cluster for which the total magnitude and angular dimensions have been measured. The coordinates of these curves are given in Tables 23 and 24

Table 23 Modulus-Diameter Curve for Globular Clusters

Table 24 Modulus-Magnitude Curve for Typical Globular Clusters

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Modulus	I og Dinmeter	Modulus	Integrated Magnitud	
14,0	1,30	14,0	3,1	
14,5	1,20	14,5	3.7	
15,0	1,05	15,0	1.5	
15,5	0,89	15,5	5,6	
16,0	0,67	16,0	0.7	
16,5	0,42	16,5	8,1	
17,0	0,24	17,0	9,4	
17.5	0,11	17.5	10,5	
18,0	0,02	18,0	11,4	
18,5	9,92	18,5	12,2	

a) Angular Diameters The adopted diameters, which are given for all globular clusters in Appendix A, are based on measures made at Harvard on photographs of Series A (Bruce 24-inch refractor) and of Series AX and AY, which are made with short focus cameras, double weight is assigned to the large scale plates. It should be noted that the measured angular diameter of a cluster depends on exposure time, the recorded diameters, d, are therefore not exactly proportional to the parallaxes nor related by the normal formula d=k 100,2m to the integrated apparent magnitudes, m. This limitation, however, does not decrease their value as a measure of relative distances

In general the measures of diameter refer to the nucleus or the main body of the cluster. Plates of long exposure, made with large telescopes, when carefully counted and analyzed, show that the clusters are of considerably greater extent than is recorded in these "surface" measures of angular diameter. The distribution of cluster type variables also frequently indicates the wide dispersion of cluster stars. For example, BAILEY<sup>2</sup> notes the existence of variables 19' from the center of N.G.C. 3201, though the "working diameter" in the catalogue is 7',7, in agreement with the value given in the N.G.C.

b) Integrated Appaient Magnitudes The photographic magnitudes for globular clusters are on a convenient but not the conventional scale. They were measured by Miss Sawyer on plates of the AX and AY scries. The scale is much more open than in the customary Pogson system and as a result the integrated brightness listed in Appendix A ranges from the third to nearly the thirteenth magnitude. It the scale were on the usual system of stellar magnitudes, this difference of ten magnitudes would indicate a range of one hundred in the relative distances, rather than the factor of ten which is actually found

The measures of brightness are, however, fairly accurate, since much care was taken in the selection of plates and of magnitude sequences. Photographic images of globular clusters depend on the lenses, plates, and photographic development, and for the brighter and larger clusters are necessarily uncertain

<sup>1</sup> Harv Bull 852 (1927)

<sup>&</sup>lt;sup>2</sup> Harv Circ 234 (1922)

<sup>&</sup>lt;sup>3</sup> Harv Bull 848 (1927)

not only because of the size and texture of the photographic image, but also because of the scarcity of suitable comparison stars and the general weakness of photographic sequences for bright magnitudes. With the warning that these new measures of brightness cannot be used for the computation of absolute magnitudes or for comparison with visual integrated magnitudes for the determinations of color index, or, as DUFAY¹ has discovered, used directly for the derivation of relative distances, we can proceed to make important indirect use of them, when properly calibrated, to get at the distances of clusters for which we have no data on individual bright stars or variables

c) The Distance Moduli and Their Weights Unit weight is assigned to each of the determinations of cluster distances based on magnitude and on angular diameter. When other values are available, as in forty-eight of the clusters, the weight four is assigned to the modulus depending on the bright stars, and the weight for the modulus from variable stars is that given in Table 24 above For instance, the four values of the modulus for Messier 3 (N G C. 5272) are 15,50 (variable stars), 15,45 (bright stars), 15,23 (diameter), and 15,0 (integrated magnitude) The corresponding weights are 8, 4, 1, 1 The adopted mean modulus is 15,43, corresponding to a mean distance of 12,2 kiloparsecs or about 40000 light years.

For the "glant-poor" clusters the modulus from the angular diameter is derived from the curve for normal systems, but the modulus from the integrated magnitude is derived from a smoothed curve based on only the clusters that are deficient in giant stars. Loose globular clusters, such as NGC 288 and NGC 3201, may approach the deficient condition, but the variable reduction factors of Table 22 largely correct for minor systematic deviations from average

conditions of magnitude frequency.

The adopted mean modulus for each cluster is given in Appendix A, followed by a letter indicating the quality of the determination. The assumed quality depends on both the final weight of the modulus and the accordance of the various determinations. The letter "a" indicates the values of highest weight, the letter "e" refers to the most uncertain determinations, which are, unfortunately, still too numerous. The distribution among the qualities is, a 13,

b 25, c 23, d 17, and e 15.

For clusters in which there is good material on variable stars, the determinations based on total magnitude and diameter contribute but slightly to the finally adopted modulus. The computed distances for nearly half of the clusters, however, depend entirely on the relatively low weight determinations of the apparent brightness and diameter. Efforts will be made within the next few years to extend the work on variables and magnitudes of individual stars. As a result, alterations in the distances of individual clusters can confidently be expected, but it is practically certain that the scale of the system of clusters and of the Galaxy will not be affected thereby. The zero point correction predicted above is the only agent likely to disturb the general scale of distances.

d) Comparison with Earlier Results. As previously noted, we have made a systematic correction of eleven per cent to the distances of globular clusters through making a provisional alteration in the zero point of the period-luminosity curve. On comparing the individual distances now given (Appendix A) with those previously obtained through my investigations at Mount Wilson\*, the average difference is found to be twelve per cent (after allowing for the systematic change). The revision of the individual distances has therefore not

<sup>&</sup>lt;sup>1</sup> Lyon Bull 44, p 59 (1929)

Mt Wilson Contr 152 (1918).

been at all diastic, though in a few cases where the early material was unusually weak it has been more than thirty per cent. Because of the great increase in the basic photometric data and in the number of globular clusters whose Cepheid variable stars have been studied, the present values are much more secure than

those formerly determined

At times during the past twelve years the scale of distances has been challenged, and evidence of argument advanced to show that I had derived cluster distances and galactic dimensions that might be from five to one hundred times too large. It is madvisable to take space to reproduce here or even to summarize these many discussions, because the general order of distances, and consequent galactic arrangement, is now very generally accepted. It should suffice to mention ten Bruggencate, Charlier, Crommelin, Curris, Doig, Hopmann, Kapilyn and van Rhijn, Lundmark, van Maanen, Malmquist, Oort, Parvullsco, Perrine, Schouten, Sfares, and R. E. Wilson as principal contributors on one side of the other of the discussion, and for the details refer to their papers which are listed in the general bibliography of star clusters in Harvard Observatory Monograph. No. 2

33 A Working Catalogue of Galactic Clusters (Appendix B). The discussion of the number and distribution of galactic clusters in ciph 9 was based on a new and fairly homogeneous catalogue which is given in Appendix B. Although intentionally incomplete because of the adopted restrictions which exclude poor or indefinite groups, as well as the galactic clusters in the Magellanic Clouds, the catalogue is probably the most serviceable yet compiled for the general study of galactic clusters. Miss Payne is responsible for the classification of the individual clusters and for the estimates of magnitudes and of numbers of stars. The classifications (sixth column of the catalogue) are on the system proposed in ciph 5. The galactic coordinates are on the Harvard system (Pole at 12th 40th, +28th). The angular diameter is from Melotic's catalogue, except when in heavy type, in which case the estimate was made by Miss Roper using Harvard photographs; it is necessarily approximate and generally refers to the obvious nucleus. Detailed star counts nearly always extend the diameter

The orientation, expressed as the position angle of the major axis of an elongated cluster with reference to the galactic equator, was estimated independently by Miss Payne and the writer on Harvard photographs for the more compact galactic clusters (Melotte's Class II), the results, which are very accordant, are discussed in ciph 24 above. The ninth column of the catalogue indicates the approximate number of stars that could be assigned to each cluster on plates whose fainter magnitude limits are as given in the tenth column. In the clusters for which this fainter limit is not given, the majority of the cluster

stars are much brighter than the limit

It is probable that many stars within the bounds of a cluster are superposed members of the intermediate galactic field, for these systems usually lie in rich regions in low galactic latitude. Obvious bright foreground stars were not considered in choosing the fifth star for each group and estimating its magnitude. It is probable, therefore, that nearly always the estimated magnitudes in the eleventh column actually refer to a star that is near the maximum luminosity in its cluster. How bright absolutely that object may be depends to some extent on whether it is a member of a Pleiades or a Hyades type of cluster, and also whether the cluster is poor or rich in stars. No claim to accuracy is made for these estimated magnitudes; they are given as rough indicators of the brighter

<sup>1</sup> Pickering, Harv Ann 56, p 1 (1912)

limit of apparent magnitude, and as a means of making prehminary estimates of the distances and space distribution of galactic clusters.

34. Parallaxes of Galactic Clusters. Direct trigonometric measures must necessarily fail to give useful information on the distances of galactic clusters. even when they are as near as the Ploiades Measures of proper motions and fairly extensive studies of the spectral composition of some of the nearer galactic clusters have led to useful estimates of the approximate distances. For ten systems, including the Pleiades, the Hyades, Praesope, Messier 11, Messier 37, the double cluster in Perseus, and the bright cluster in Coma Borenices, the distance in kiloparsecs has been determined through more or less detailed studies of motions, magnitudes, and spectra, and is entered between the twelfth and thirteenth columns of Appendix B The sources are given in the notes at the end of the catalogue. The accuracy of these ten values is not high, except for the Hyades.

For other galactic clusters no equally dependable measures of the distances are yet available, though provisional photometric or spectral parallaxes have been published by various investigators. Doig! and RAAB! in particular have analyzed the spectral data and derived usoful preliminary estimates for many of the brighter groups My own early values for a number of the galactic clusters are systematically too great; the published estimates were admittedly very provisional, and gave distances that now appear on the average to be two or three times too large because of the tentative assumption that the brighter stars were of exceptionally high luminosity

TRUMPLER's spectroscopic and photometric researches on galactic clusters, which have been in progress for some years, should eventually give fairly accurate values of the distances of many of the galactic clusters; his method involves the use of luminosity curves for various spectral classes in the clusters. or, what is essentially the same, the use of a RUSSELL diagram for fixing the distance modulus The final standardization of his system of distances will probably await much serious work on the absolute luminosity dispersion for stars of Class A.

In 1931, P COLLINDER published an exhaustive study of galactic clusters,

dealing with their structural properties and distribution in space.

Spectroscopic parallaxes should eventually give the distances of a number of galactic clusters which contain late type stars; and with the development of dependable spectroscopic methods for early type stars, such as those foreshadowed by Miss WILLIAMS, in analyses of absorption lines in Class A spectra, the spectrum line method may turn out to be the most dependable one for measuring the distances of galactic groups. It will be a procedure much less time-consuming than the RUSSELL diagram method

Since the accurate determination of the distances of galactic clusters is still mainly in the future, it seems worth while for the time being to tabulate direct photometric estimates. Assuming that the fifth star in order of brightness in a galactic cluster has the absolute magnitude of an average bright Class A star, +0,5, we derive the distances given in the twelfth column of Appendix B. In the thirteenth column are given the distances corresponding to an assumed absolute magnitude of -0.5. Since we are dealing with objects selected on

<sup>1</sup> JBAA 35, p. 201 (1925). Lund Modd Serie II, No. 28 (1922).

Mt Wilson Comm 62 (1919).

Preliminary publication in Lick Bull 14, p. 154 (1930), after the completion of this manuscript,

Publ A 8 P 37, p. 307 (1925).
 Lund Obs Ann 2 (1931).
 Harv Circ p 348 (1929).
 Miss Arcur has extended the method and applied it to various galactic clusters. [Harv Circ 352 (1930); Harv Bull 882 and 883 (1931)].

account of high luminosity, these greater distances are probably more nearly correct. They have therefore been used in computing, in the next two columns, the linear diameter of each cluster in parsecs and the distance of the cluster from the galactic plane. The wide range in linear diameters, reflecting in part the difficulty of estimating the bounds of a galactic cluster, is a striking feature of these computed results. The smallest objects appear to be only a few light years in diameter, and the largest more than fifty. Not much weight can be put on individual values of the distance, but it is practically certain that these values are of the right order of magnitude and can serve to give a correct idea of the distribution of galactic clusters in space. The light they throw on galactic dimensions is considered in ciph 42

35. Radial Velocities of Globular Clusters. The measured radial velocities of globular clusters range from -350 to +315 km/sec. From Table 25 it can be seen that there is no clear dependence of velocity on class of cluster, galactic latitude, angular diameter, total magnitude, or distance from the sun. The only appreciable correlation appears to be that of speed with distance from the solar apex, pointed out by Stromberg. The dependence is in the sense of increasing

velocity with increasing distance from the solar apex

The simplest interpretation of the relation of speed to position in the sky is based on the assumption that the apparent systematic drift of the clusters is but the reflection of the motion of the local system in the Galaxy. When corrected for this motion, the average speed of globular clusters remains high—approximately a hundred kilometers a second, but as a group, the globular clusters are essentially at rest with respect to the whole galactic system, unlike the extra-galactic nebulae, which show a large K term apparently dependent on distance

The radial velocities of globular clusters have been measured mainly by SLIPHER at the Lowell Observatory Except for two or three clusters, all measures refer to the integrated images and not to individual stars. The study of differential radial motions in a globular cluster is one of our important future problems. The successful measure of the proper motions in globular clusters, also, must await the photographs of the future. VAN MAANEN has shown that the proper motion of Messier 13 as a whole and its average internal proper motion are less than 0",001 annually, an amount to be expected from a consideration of the distance and the radial velocity. The values of the annual proper motions are slightly larger for Messier 2 and Messier 56, but are consistent, he finds, with my estimated distances and the average radial velocities.

<sup>&</sup>lt;sup>1</sup> The assumption that the fifth star in the cluster is not more luminous than -0.5 implies, in general, that the star is not earlier in spectral class than B8. For a cluster of the spectral constitution and richness of the Pleiades, this assumption would therefore give too small a distance. IRUMPLER has found that about half the clusters he has classified are of the Pleiades type, but, as pointed out in eight 14, this proportion is probably too large because of observational selection. The clusters of the Pleiades type are apparently poor in highly luminous stars of early type, for of lifteen enumerated by RAAB, not one has a fifth star of class as early as B5. The adopted method, therefore, probably does not lead to serious systematic error.

<sup>&</sup>lt;sup>2</sup> Mt Wilson Contr 292, p 5 (1925) A suggestion of a dependence of velocity (corrected for solar motion) on galactic latitude and therefore on mass of the intervening star fields is discussed by the Bruggencate [Wash Nat Ac Proc 16, p 111 (1930)], who seeks a trace of the red-shift, characteristic of the spectra of distant spiral nebulae. The material is as yet insufficient to establish the correlation securely, or to discriminate among its possible interpretations.

<sup>8</sup> Mt Wilson Conti 284 (1925)

<sup>&</sup>lt;sup>1</sup> Mt Wilson Conti 338 (1927)

Table 25 Radial Velocities of Globular Clusters

NGL		,	Byectrone	Augular Diameter	Pg. Mag.	Distance (kpc.)	Radial Velocity
1851	11	-34°,5	-	5'.3	6,0	14,3	+315km/sec
1904	V	-28	I - I	3,2	8,1	20,4	+235
5024	V	+79	1 - 1	3,3	6,9	18,2	-180
5272	VI	+77.5	G	8, 9	4,5	12,2	-130
5904	V	+46	G	12.7	3.6	10,8	+ 10
6093	II	+18	Ko	3,3	6,8	17.5	+ 70
6205	V	+40	Go	10,0	4,0	10,3	-265
6218	IX	+25	-	9,3	6,0	11,0	+160
6229	IIV	+40	1 - 1	1,2	9,7	29,8	-100
6266	IV	+ 7	K0	4,3	7,0	18,6	+ 50
6273	AIII	+ 9	G5 (	4,3	6,8	16,3	+ 30
6333	IIIV	+10	K?	2,4	7.4	20,8	+225
6341	IV	+35	G5	8,3	5,1	11,2	-160
6626	IV	- 7	G5 [	4 .7	6,8	16,6	O
6934	VIII	-20	Go	1,5	9,4	24,9	350
7078	IV	-28	F	7,4	5,2	13,1	- 94
7089	II	-36	F5	8,2	5,0	13.9	- 10
7099	V	-48,5	178	5.7	6,4	14,6	-125

36. Dimensions and Star Densities of Clusters. It is impossible to say how many stars constitute a typical globular cluster. Our photographs can reach only a little way down the main sequence towards the dwarfs. When we attempt to go further, the high density of the central stars "burns out" the photograph and conceals the information we might otherwise obtain. From available counts on our most suitable photographs of the brightest clusters we estimate that in the average globular cluster there are more than twenty thousand stars brighter than absolute magnitude +5. To the same magnitude limits, the population of an average galactic cluster is less than two hundred stars.

The diameter of a globular cluster is also indeterminate. It is probable that the actual linear dimensions depend on the brightness of the stars involved, becoming greater for stars of lower luminosity and mass; the same dependence appears also in galactic clusters. From Table 23, which gives the relation of distance modulus to angular diameter for normal globular clusters, we can compute the following relation of linear diameter to distance.

Distance	Modules B-M	Angular Dismotor	I de ventr Discretan
10 kpc	15,0	11',2	33 pc
20	16,5	2,6	16
30	17.4	1,4	13
40	18,0	1,02	12
50	18,5	0,85	12

The measured decrease of linear diameter with increasing distance is of course mainly photographic. The loss of light in space is here of minor significance. We under-measure the angular diameters of remote clusters because of the failure of outlying faint stars to rise to measurable prominence on the photographic plate. I think we can safely take the diameter of a typical globular cluster to exceed thirty-five parsecs, but the diameter of the nucleus, in which the brightest stars are concentrated, appears to be only one third as large.

The average linear diameter of the galactic clusters for which definite estimates can be made (Appendix B) is 6,24 parsecs. Few galactic clusters

<sup>1</sup> See, for example, Pop Astr 27, p 101 (1919)

See Figure 15

exceed twenty parsecs in diameter Trumpler has determined preliminary distances from observations of magnitudes and spectral types for fifty-two systems. He finds a range in linear diameter from 3,5 to 25 parsecs, with the

great majority between 4,5 and 10 parsecs

The number of stars per cubic parsec in a typical globular cluster cannot be computed at present, except for the supergrant stars. It is obvious, when the dwarfs are taken into consideration, that the distances separating stars at the center of a rich globular cluster are on a planetary rather than a stellar scale. It seems probable that sooner or later we should have evidence of stellar encounters in such crowded regions; but only one nova in a globular cluster is now on record—the seventh magnitude object in Messier 80, which appeared in 4860.

The space density and the distances separating individual stars can be more readily computed for galactic clusters when reliable estimates of the parallaxes become available, and when we have made sufficient allowance for superposed stars. Trumpler's study of one of the richest of the galactic clusters, Messier 11, provides material that illustrates the conditions in these systems. He finds that the cluster is 1250 parsecs distant. It has in the rich Scutum star cloud, which has a star density nearly four times that of the average field of the galactic belt. The cluster itself is made up of about 480 stars brighter than magnitude 15.5, distributed over an area approximately a quarter of a degree in diameter. The bright stars are concentrated within a central area of less than 4' radius.

For stars brighter than absolute magnitude +4,5 the relation of density to distance in Messier 11 is found to be as follows

Distance from Center in Parsees	Stars per Cubic Parsec	Distance from Center in Parsecs	Stars per Cuble Parsec		
0,27	83	1,68	4,9		
0,60	80	2,04	2,2		
0,96	33	2,40	0,5		
1,32	9,5				

The central density of Messiei 11 is much higher than that of the average galactic cluster. In contrast with the density of 83 stars per cubic parsec for Messiei 11 is the density for Messiei 37 of only eighteen stars per cubic parsec for stars brighter than absolute magnitude +4,5. The corresponding number for Messiei 36 is twelve (Wallenguist), for the Pleiades, 2,8 (if the parallax is taken as 0",008), and, for the vicinity of the sun, 0,011. The average separation of stars at the center of Messiei 11 is one light year.

TRUMPLER points out that "an observer at the center of Messier 11 would find about forty stars with parallaxes of 2" or more and which would appear three to fifty times as brilliant as Snius shines in our sky". It is quite probable, however, that this display would be very dull compared with the show at the center of the Hercules cluster.

# i) Star Clusters in the Magellanic Clouds.

87. Types of Clusters and Nebulae. Both globular and galactic clusters appear in the Magellanic Clouds, the latter type exhibiting much variety in richness, dimensions, and nebulosity. In the New General Catalogue and the Index Catalogues 41 clusters and nebulae are listed within the limits of the

<sup>2</sup> Lick Bull 12, p 10 (1925)

Later revised to 1340 parsecs Lick Bull 14, p 154 (1930)

Small Cloud and 301 within the Large Cloud. The descriptions, however, are meager, and photographic plates reveal scores of clusters and nebulae that have not yet been catalogued and described. For the Small Cloud a catalogue by Shapley and Miss Wilson<sup>1</sup> gives 237 new objects, chiefly nebulous stars and groups of stars. A manuscript catalogue of the star clusters in the Large Cloud, recently prepared from Harvard plates, contains 110 new entries—nearly doubling the number known from Herschel's survey and subsequent investigations. A complete catalogue and analysis of the clusters in the Magellanic Clouds, however, must await future surveys with the reflectors, since the telescopes at present available do not permit adequate resolution of the small groups.

Among the great number of nebulae in both Clouds, none has been found which could be assigned safely to the spiral class. As would be expected from their total absolute magnitudes, mainly between -3 and -7, they are for the most part of the diffuse and irregular types, with a meager sprinkling of planetaries. Of the many diffuse nebulosities in the Large Cloud the greatest is the famous "Looped Nebula", 30 Doradus. Its absolute brightness probably exceeds magnitude -13, and its total diameter, including the fainter wasps and loops of nebulosity, is thirty paraecs or more.

88. The Globular Star Clusters. Dunlop, Sir John Herschel, and others have described many of the compact star groups in both Clouds as globular. The N G.C. records sixteen globular clusters in the Large Cloud and two in the Small. On the basis of photographic material Balley, Melotte, and others have remarked that few if any of these objects are correctly assigned. In fact, none of them is now retained as truly globular. On the other hand, the accepted globular clusters, listed for both Clouds in Table 26, are not described as such in the N G.C., though they all appear in that catalogue. The existence of globular systems in the Magellanic Clouds affords a valuable opportunity for the comparative study of globular and galactic types, and for the examination of the relation of globular clusters to galaxies.

The first two clusters of Table 26 belong to the Small Magellanic Cloud; the eight others to the Large Cloud. The angular diameters and integrated magnitudes are given on the same basis as in Appendix A for globular clusters in general. The diameters, therefore, are not indicators of the extreme bounds of the clusters—they are rather measures of nuclei. N.G.C 416 in the Small Cloud is more uncertain than the others and later may be dropped

It is seen that the globular clusters in the Large Cloud range from the compact Class II to the fairly open Class VIII. In earlier considerations of clusters in the Large Cloud® seven objects were listed as possibly globular. Of these N.G.C. 1651 has now been definitely dropped®, and N.G.C. 1835 and N.G.C. 1856 have been added to the list. Later analysis may show that some of the following N.G.C. objects are globular clusters4.

1711	1926	2056	2133
1789	1939	2058	2134
1852	1944	2065	2157
1872	1986	2107	2164
1903	2019	2108	
1016	2031		

<sup>1</sup> Harv Circ 275, 276 (1925)

Harv Bull 775 (1922); Harv Circ 271 (1925)

It was included in Harv Bull 848, 849, and 852 as a doubtful object.
In 1932 (two years after the completion of the manuscript) a dozen new globular clusters were found in the vicinity of the Large Cloud (Harv Bull 889).

Table 26 Globular Clusters in the Magellanic Clouds

NGC	R A 1900	Dec 1900	Gale	ectic	Angular	Integrated	Class	Adopted	Quality
NGC	K A 1900	Dec 1900	Long	Int	Drameter	Magnitudo	VIII.75	Modulus	330-03113
416 419 Mean 1783 1806 1831 1835 1846 1856	1h 5m,0 1 5 .4 4 58 ,8 5 2 ,4 5 5 5 ,8 5 7 ,7 5 10 ,1 5 13 ,6	-72° 53',5 -73° 25,1 -66° 8,1 -68° 8,0 -65° 3,6 -69° 32,1 -67° 35,0 -69° 15,1 -65° 34,9	262° 262 242 245 247 245 247 245 247	- 13° - 42 - 37 - 36 - 35 - 34 - 34 - 34	1,4 - 1,4 0,9 1,3 1,2 1,2 2,1 2,2	11,3 10,2  10,1 10,6 10,0 9,9 10,4 8,8 8,0	VI IV VIII VIII VIII VIII	18,05 17,36 17,50 17,32 17,94 17,38 17,44 17,56 16,76 16,58	c d c d c c d
1978 Means	5 28 ,1	-66 18,5	242	-33	1,0	10,2 9,61 上 0,24		17,72 17,25   0,11	-
	Ì	1	1	)	)	(m e)	)	(m c)	)

In none of the globular clusters of the Magellanic Clouds have variable stars been found, nor have the brighter stars been measured individually. The final test as to whether the doubtful objects are typical globular systems, or merely open groups involved in nebulosity, will be in future examinations for variable stars, and in the study of density and luminosity laws.

Miss Cannon has thrown doubt on the globular nature of a number of bright objects in both clouds by showing that their integrated spectra are of early class; we have already seen that practically all typical clusters belong to Classes F and G. Thus she finds

NGC	Spectrum .	NGC	Spectrum
294	A?	2107	A ?
1872	A3	2134	Λ
1903	Λ	2157	A2
2041	A3	2164	A5

The spectrum of NGC 419, in the Small Cloud, resembles Class K in its distribution of light and in the faint appearance of the G band and of lines H and K. The spectrum of NGC 416 is too diffuse and faint to classify. The spectral class<sup>2</sup> of NGC 1866, in the Large Cloud, is F8, that of NGC 1835 is possibly G5, though for it and the other compact clusters of the Large Cloud the spectral images on the Harvard objective prism plates are too difficult for classification.

89. Distances of the Clouds. Values of the distances of the Magellanic Clouds can be based on measures of the globular clusters, but from Cepheid variable stars more accurate results are obtained, which can then be used to determine the absolute magnitudes of the clusters. In the minth column of Table 26 the distance modulus is given for each cluster, derived from the measures of angular diameter and integrated photographic magnitude. In the use of these data we follow the principles developed in an earlier section on the distances of globular clusters of the galactic system. In getting mean values of the modulus for each cloud, weights were assigned as follows.

Quality	Weight			
c	4			
d	2			
C	1			

<sup>1</sup> See Appendix A

<sup>&</sup>lt;sup>3</sup> Harv Bull 868 (1929)

While clusters of quality c may be accepted as almost certainly globular, some

doubt still attaches to those qualified as d and o

The mean modulus derived for the Small Magellanic Cloud is nearly identical with the value 17,55, previously derived from 107 Cepheid variable stars. With the adopted revision of the zero point of the period-luminosity curves the distance modulus from the variables becomes 17,32. Accepting this value we have for the Small Magellanic Cloud.

n = 0'',0000345Distance = 29 kiloparsecs
= 95 000 light years
Linear Diameter = 6000 light years.

At this distance the integrated absolute magnitude is -7.12 for N G C. 419, the only object that appears definitely, from the survey of existing plates, to

be a globular cluster

For the Large Magellanic Cloud the mean distance modulus from eight globular clusters is 17,25, with a mean computed error of only one tenth of a magnitude. But the Copheid variable stars should eventually give us a much more dependable value of the modulus. The modulus derived from a recent study of the variables is 17,10. Adopting this value, we obtain the following results for the Large Magellanic Cloud.

π = 0",000038

Distance = 26,2 kiloparsecs
= 86000 light years

Linear Diameter = 10800 light years

The corresponding mean absolute photographic magnitude of a globular cluster in the Large Magellanic Cloud is -7.46 (weighted mean). The absolute values range from -9.1 to -6.5, an indication of the degree of uncertainty involved in assuming a constant integrated absolute magnitude for globular clusters. The spread is considerably less if the cluster N G.C 1866 is assigned to the foreground rather than to the Magellanic Cloud, and it would be very small indeed (-7.2 to -6.5) if the newly admitted N G C 1856, when analyzed with a large telescope, proved to be a nebulous open group

40 On the Relation of the Clusters to the Magellanic Clouds. The angular diameters of the globular clusters in the Large Cloud are at most two or three minutes of arc; the angular diameter of the Cloud as a whole is slightly more than seven degrees. Enormous and rich as we know a typical globular cluster to be, it is obviously small compared with ordinary external galaxies. The clusters of the various sorts, however, are important in the general appearance of the Clouds, and especially in the make-up of the high luminosity population.

The distribution of the open clusters throughout the Clouds is much the same as the distribution of the Cepheid variable stars and of the general stellar population, on the other hand, the accepted globular clusters in the Large Cloud are almost exclusively to the north, and N.G.C. 1866 and N.G.C. 1831 lie quite outside the main structure of the Cloud. There are, however, a half dozen variable stars, apparently of the Cepheid class, in the same region as these clusters, and long exposures on short scale plates show that the outlying clusters and variables are within the observable bounds of the Cloud.

<sup>&</sup>lt;sup>1</sup> SHAPLEY, YAMAMOTO, and WILSON, Harv Circ 280 (1925), see also SHAPLEY, Herv Circ 255 (1924)

The asymmetrical distribution of the globular clusters in the Large Cloud has led some to surmise that the globular clusters of the galactic system may also be eccentrically arranged with respect to the general galactic structure, and therefore that they cannot be used as I have used them, in estimating minimum values of galactic dimensions. But this one-sided distribution of the globular clusters in the Large Cloud is modified by the inclusion of N G C 1835 and N G C 1856 in the list accepted at present, and it would be quite altered if a considerable proportion of the list of suspected globular clusters prove to be typical systems. The two clusters N G C 1789 and N G C 1944, both of which are strongly suspected as globular, he far from the center of the Cloud on the south—directly across from the outlying globular clusters of Table 26

It is of significance that the 1400 known variable stars in the Large Cloud and the 969 in the Small Cloud<sup>1</sup> avoid the numerous open clusters. In this respect the Clouds are like the galactic system, where open clusters are free of variable stars of all kinds. The globular systems in the Magellanic Clouds, are, of course,

too compact to have been scarched as yet for variables

Possibly the most striking fact arising from the study of globular clusters in the Magellanic Clouds is the low absolute magnitude of their brightest stars when compared with the brightest objects in the open and nebulous groups. If the new values of the distance moduli are correct, there is scarcely a star in the ten accepted globular systems of the two Clouds that exceeds —3 in absolute photographic magnitude. This result, however, is in complete agreement with the condition found in globular clusters of our own galactic system. In contrast, the individual stars in scores of the nebulous star groups in the Magellanic Clouds appear to exceed —3 in absolute photographic magnitude, and in many groups they attain the excessively high luminosities of —5 and —6. This again is in agreement with the data on absolute magnitudes in galactic clusters, especially in those large early spectrum groups in Orion, Scorpio, and elsewhere that are associated with bright nebulosity.

It may be remarked in conclusion that, notwithstanding their remoteness, isolation, and high galactic latitudes, the Magellanic Clouds may be more closely alhed to our galactic system than we have heretofore supposed. It is probable that the observed high speed recession of the Clouds should be assigned almost wholly to the motion of our local system in the Galaxy. Apparently the Clouds are not in rapid motion with respect to the sum total of the galactic system, or

the system of globular clusters

# j) Dimensions of the Galaxy.

41. Membership in the Galaxy Our galactic system, as here defined, is composed of the aggregate of stars and nebulae whose distribution appears to be organized with respect to the galactic plane. Globular clusters are therefore included, with galactic stars and galactic clusters and nebulae, but the Magellanic Clouds and the extra-galactic nebulae (spiral nebula family) are outside the organization.

A final judgment, however, of galactic membership must await more information on speeds and masses, and on the phenomena of galactic rotation. Possibly some of the remote globular clusters (e.g. N.G.C. 7006, N.G.C. 4147, and Messier 75) are actually independent, being either fugitives from the Galaxy,

<sup>2</sup> Hary Rep. 61 (1929)

<sup>&</sup>lt;sup>1</sup> LEAVITT, Harv Ann 60, No 4 (1908) Approximately 600 new variables have been found on Harvard plates of the Large Cloud since 1930 (as yet unpublished)

or only chancing for the moment (cosmically speaking) to be moving in this part of space. On the other hand, the Magellanic Clouds may sometime be shown to be affiliated with our Galaxy, or, at least, with a local group of galaxies including the three Andromeda nebulae, Messier 33, and some others.

In measuring the Galaxy we should at the start admit indefinite limits, and also striking irregularities, not only in the interior but probably also at the edges. The dimensions discussed below are therefore not to be taken too literally as marking the boundaries, or even as giving sharp limits of star density. At best we measure or estimate the distances of the remotest attainable stars, or groups of stars, which yield to present methods and which appear to be members of the galactic system.

- 42. The System of Galactic Clusters. Although the loose star groups contribute little to our knowledge of the dimensions of the Galaxy, their space distribution may be mentioned here as bearing on the structure of the nearer parts of the Milky Way. The catalogue of 249 galactic clusters in Appendix B contains galactic longitude, approximate distance, and R  $\sin \beta$  (distance from the galactic plane). Some features to be noted in the distribution of the galactic clusters are:
- 1 The contrast in galactic distribution of galactic and globular clusters (see Figure 6).
- 2. Close confinement of galactic clusters to the neighborhood of the galactic plane
- 3 The relative nearness of galactic clusters to the sun, which results in a distribution essentially free from effects of the obstructing clouds that contribute much to the anomalous distribution of the globular clusters. The galactic clusters are in large part members of our local system and the circumjacent star clouds.
- 48. The Higher Systems of Globular Clusters. To illustrate the space distribution of the ninety-three known globular clusters of the galactic system (Appendix A), the following rectangular coordinates have been computed for all

$$X = R \cos(\lambda - 327^{\circ}) \cos \beta,$$
  

$$Y = R \sin(\lambda - 327^{\circ}) \cos \beta,$$
  

$$Z = R \sin \beta,$$

where R is the distance in kiloparsecs,  $\beta$  is the galactic latitude, and  $(\lambda - 327^\circ)$  is the galactic longitude measured from the direction of the center of the cluster system. The latitude, longitude, distance, and  $R\sin\beta$  are given in Appendix A; the computed quantities X and Y are given in Table 27

a) Eccentric Position of the Solar System A diagram of the distribution of the globular clusters in the plane of the Galaxy (XY plane) is shown in Figure 19. Crosses indicate clusters lying on the north of the galactic plane, and dots those on the south; the smaller the symbol, the more distant is the object from the plane. The equality of the division by the galactic plane of the supersystem of clusters is remarkable—forty-seven clusters are on the north, forty-six on the south.

The direction to the center of the system, derived from the apparent positions of globular clusters, is seen to agree with the direction on the basis of space coordinates; in Figure 19 there are forty-six positive values of Y and forty-six negative values, with Y = 0 for one cluster. (The remote system N.G.C. 7006.

<sup>1</sup> SHAPLEY, Harv Repr 61 (1929).

Table 27 Coordinates of Globular Clusters

NGC	R cos f( × co-(1-327°)	R cos β κ sin (λ−327°)	исс	$\frac{R\cos(\beta \prec \cos(7-327^{\circ}))}{\cos(7-327^{\circ})}$	R cosβ ∧ sur(λ 327°)
104	+ 2,8	- 3,9	658+	18,6	- 5,0
288	- 0,5	- 0,1	6024	- 21,7	1,2
362	+ 4,5	- 7,5	6626	16,2	1 2,3
	T 463	-13,7	6637	- 18,4	106
1261	5,0	-10,6	6638	-29,0	1 1,3
1851		-13,2	6205	1 4,0	6,0
1904	-12,3	-23,4	6218	- 9.5	2,9
2298	-10,4	- 0,5	6229	- 6,7	1-21 h
2419	-28,0	-15,6	0235	-28,0	( '0"
2808	+ 3,0	- 9,0	6254	-10,0	1 2,9
3201	+ 1,1		6266	-1 18,3	1,6
4147	- 0.9	- 4,5	6273	- 16,0	0.7
4372	+ 5.0	- 8,0	6281	1-27.6	0.5
4590	+ 6.7	-10,7	6287	27,1	1 0.5
4833	+ 8,8	-13,0			- 0,8
5021	+ 3,2	→ 1,3	6293	22,8	1,8
5053	+ 3.5	- 1,0	0304	-  25,0	
5139	+ 1,2	- 5,0	6316	31,5	- 0,8
5272	1 2,0	+ 1,7	6325	46,0	1 0,1
5286	+16,0	-17,0	6333	20,3	1 2,1
5466	+ 3,8	+ 3,1	63 11	] 3.3	1 8,6
5634	- 19,8	5,8	6342	1 39.1	1 1.1
4499	+14.0	-18,0	6352	1 18.4	(5,0)
5824	+24,4	-11,9	6356	+ 48,5	- 6,0
5897	+15.0	- 4,0	6362	+ 12,0	0,8
5904	+ 7,4	+ 0,6	6366	1 26,3	1 9,1
5927	-1- 16,8	11,0	6388	- 16,6	4,2
5946	+27,2	-17.0	6397	1 5,1	~ 2,1
5986	-1 15,4	- 6,2	6402	+ 17,7	- 7.2
6093	+16,5	- 1,9	6652	1-23.0	1 0,6
6101	£14.7	-13.5	6656	[ - 6,3	<b> - 1,2</b>
6121	+ 6,9	- 1,0	6681	18,7	1 10
6139	+27,7	- 8,5	6712	23,2	1 11,6
6144	+17.3	- 2,4	6715	-1 18,6	1 1.9
6171	+ 19,4	1,7	6723	+11.7	0,2
6426	+31,3	+17,4	6752	- - 6,7	3,0
6440	-+49,5	+ 7,0	6760	23,1	1 16,8
6441	+21,0	- 0,2	6779	J- 9,1	1 17,8
6453	+ 50,0	- 0,4	6809	+ 7,9	1,2
6496	+21,2	- 4,5	6864	-1-40,7	14.8
6517	+470	+17,1	6934	11,1	1 18.7
6522	+ 35,8	+ 0,6	6981	-[-15,6	11,4
6528	44,0	+ 1,2	7006	4-22,4	1 48,0
6535	+23,0	+12,3	7078	-1 4,7	10,6
6539	+35.8	+13,8	7089		9,2
6541	4 8,6	- 1,5	7099	-1- 8,6	
6553 6569	+ 26,6 + 29,1	+ 2,6 + 0,5	7492	-1 6,4	+ 9.1

with coordinates X = +22.4, Y = +48.0, falls outside the limits of the diagram)

The origin of coordinates for Figure 19 — that is, the position of the observer — is on the border of the globular cluster system. The center of gravity of the system of clusters, indicated by an open square, has the coordinates X = +16.4, Y = -0.3 (or Y = +0.2 if the remote and isolated NGC 7006 is included)

Probably ten or twenty globular clusters, within the limits of space represented by the diagram, await discovery. Obscuring nebulosity possibly conceals most of these systems, of which the existence is intimated by the scarcity of

observed points in the right half of Figure 19. Of course we need not assume high regularity in distribution, or even approximate circularity in the projected array, but it is probably the observational difficulties caused by nebulosity and by the small dimensions and faut magnitudes of remote clusters, and not

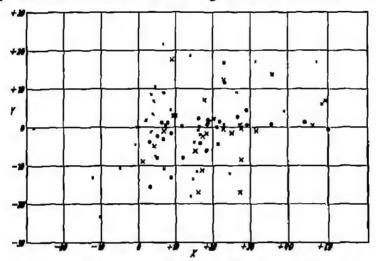
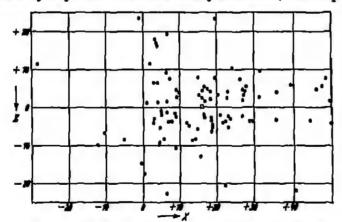


Fig 19 Distribution of globular clusters in the plane of the Galaxy The sun is at the origin of coordinates.

inherent irregularities, that have produced the apparent deficiency for X greater than +30 kiloparsecs. On the left side of the diagram, from X = 0 to X = -20, where the survey may be considered sufficiently exhaustive, the complete absence



Itig 20 Distribution of globular clusters in the XZ plane,

of clusters from one quadrant is even more striking and significant structurally than the scarcity of values of X greater than +30.

The cluster at the extreme left is N G.C. 2419—an object in a region far from other clusters, found through studies of the Lowell Observatory photographs.

<sup>1</sup> Hery Bull 776 (1922)

b) The "Region of Avoidance" The same asymmetrical position of the sun with respect to the supersystem of globular clusters is shown in Figure 20, where all ninety-three systems are plotted on the XZ plane. The center of gravity, that is, the algebraic mean values of X and Z, indicated by an open square, is at  $X=\pm 16.4$ ,  $Z=\pm 0.4$  NGC 2419 again stands out on the extreme left.

The most interesting feature of Figure 20, which represents a section perpendicular to the galactic plane, is the "region of avoidance". The scarcity of globular clusters in low galactic latitudes is again in evidence. Here is a central section 2,5 kilopaisecs (8000 light years) in diameter, in which no globular cluster has been found. On the other hand there is only one galactic cluster out of the

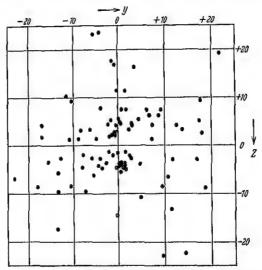


Fig 21 Distribution of globular clusters in the YZ plane

249 listed in Appendix B that does not fall well within this mid-galactic segment and that cluster, NGC 2243, is of doubtful nature and uncertain distance Practically all known galactic stars and nebulae also fall within this "region of avoidance"

- c) Projection on the YZ Plane. Figure 21 shows the distribution of globular clusters projected on the YZ plane, which is perpendicular to the line joining the sun and the center of the system at galactic longitude 327°, galactic latitude 0°. The "region of avoidance" is again clearly shown, and also the essential symmetry of the globular cluster system, for the numbers of clusters in the four quadrants are 23, 24, 22, and 24 Again N G C 7006 is outside the diagram, with coordinates Y = +48.0, Z = -20.4
- 44. The Distance to the Galactic Center. It appears to be a tenable hypothesis that the supersystem of globular clusters is coextensive with the Galaxy itself. Researches on variable stars in the Milky Way¹ will eventually afford an instructive check on this hypothesis. Until we have such direct measures we can only assume that the galactic system is at least as large as the system of globular clusters. We have shown rather convincingly that the globular clusters are galactic members or associates.

<sup>1</sup> Shapley, Harv Repr 51 (1928)

The algebraic mean of the values of  $R\cos{(2-327^\circ)}\cos{\beta}$  gives a preliminary indication of the distance to the center of the cluster system, and provisionally, therefore, of the distance to the center of the Galaxy. In so far as it depends on the globular clusters now known, the uncertainty of the distance does not exceed ten per cent. Further research on faint globular clusters, especially if now ones be found, will be more likely to extend the system than to reduce it; on the other hand, the distances of the more remote clusters are the least certainly determined and must be given low weight. We shall adopt as the distance to the center

R<sub>g</sub> = 16 kiloparsecs = 52000 light years

The galactic star clusters and the ordinary individual stars are too near the sun to contribute effectively to the determination of the distance to the center. But the direction to the center, as is well known, is confirmed by the counts of funt stars<sup>1</sup>, and through the recent studies of galactic rotation by Lindrich, Oort, J. S. Plaskett, Schilt, and others; it is shown, though less definitely, by the distribution of Milky Way star clouds, planetary nebulae, Class O stars, and other objects of high luminosity. Practically all types of stars, however, with the possible exception of the novae and Cepheid variables, are too faint absolutely and too infrequent in number to contribute to the current surveys of galactic regions that are near or beyond the center of the cluster system.

Studies of the cluster type Cephoids and the long period variable stars in the southern Milky Way have led the writer and Miss Swore to a value of the distance of the centrally located star clouds that is very much like the value given above. The variable star investigations of several observers at Harvard tend to support this suggestion that the heavy star clouds in Ophiuchus, Sagittarius, Scorpio, and neighboring constellations are parts of a massive stellar nucleus of the galactic system. The distribution of the cluster type Cephoids in these regions suggests that the nucleus extends perhaps half way from the center toward the sun. The speed of rotation about this nucleus is approximately 300 kilometers a second at the sun's distance from the center

One important feature of the galactic central region is that the center itself lies behind heavily obscuring nebulosity. The dark clouds at the center are apparently but a part of these causing the rift in the Milky Way that extends from Cygnus southward to Centaurus; they seem to be largely responsible for the apparent avoidance of the mid-galactic regions by globular clusters.

45. On the Size and Structure of the Galaxy. An inspection of Figures 19 and 20 gives only a rough idea of the total diameter of the flattened galactic system. The most remote globular clusters are the following:

N.G.C.	Distance kps	и.д.с.	Distance kps
6325	46	6517	50
6342	40	6528	44,4
6356	50.	6864	48,5
6440	50;	7006	56,8
6453	50		

NORT, Recharches Ast Obs Utrecht 8, p. 113 (1917); BEARES, Mt Wilson Contr 347 (1927).
SHAPLEY, Hary Rope 52 (1928)

Some of these values are uncertain, the distances may be greater or less, but the superior distance of NGC 7006, a cluster in Vulpecula with  $R=56.8~\rm kpc$  = 185 000 light years, seems to be well attested by observations on its individual stars and on its cluster type Cepheids<sup>1</sup>

The greatest distance separating two of the clusters is

NGC 7006 - NGC 2298 = 80 kilopai sees

Several other clusters are nearly as widely separated, N (r ( 2298 in Puppis is 71,3 kiloparsees from N G C 6517 across the sky in Ophiuchus, and N (r ( 2419 in Lynx is 79 kiloparsees from N G C 6453 in Scorpio. We may take such distances to indicate the extreme dimensions of the galactic system, for certainly most of these globular clusters, if not all, are integral parts of the Galaxy.

It does not follow from the wide dispersion of globular clusters that individual stars of the Galaxy are so widely dispersed, but it appears reasonable to maintain that the greatest diameter of the Galaxy in its plane is not less than seventy thousand parsecs, and it may be thirty per cent larger. The thickness of the system varies with distance from its center, being perhaps ten to fifteen thousand parsecs at the galactic nucleus, and one-half as much out where the solar system is located. Occasional isolated stars, however, and, of course, the globular clusters extend to twenty thousand parsecs and more from the galactic plane, lying well outside the relatively thin mid-galactic stratum.

The most remote individual stars known in the Galaxy are the novae and a few long period Cepheid variables, of faint apparent magnitude, studied by Gerasimovič, Miss Swope, Miss Harwood, and others, on Harvard and Nantucket plates. Some of these appear to be well beyond the galactic nucleus, with distances comparable with those of the remoter globular clusters and the Magellanic Clouds. Since progress is rapid in the discovery and study of faint variables, it will be advisable to postpone the discussion of the part they play in the measurement of the extent and orientation of the galactic system. It may be twenty years or more before the detailed picture of the structure of the galactic star clouds can be drawn.

It is of significance, however, to compare the picture of the Galaxy that grew out of the carber work on clusters and the local star system<sup>2</sup> with that resulting from the more recent studies of galactic structure<sup>3</sup>. The earlier view vizualized the Galaxy as a unified discordal stellar system, evolved from amalgamating star clouds and clusters. The local cloud was mapped out and described as one of the minor elements. The Galaxy was considered, not a single spiral nebula, but rather an organization of many half-digested star clouds and clusters, moving in an extensive stratum of stars and galactic nebulae.

It was suggested that the obvious dynamical equilibrium of a globular cluster, acquired originally at a great distance from external perturbing matter, results in a delicate adjustment that readily breaks down under stresses such as those prevailing in a large galactic system, further, that faint stars in a globular cluster, as in the galactic system, are of small mass and therefore of more than average velocity, so that in their motions in the cluster they frequently attain great distances from the center. When such globular systems approach or mingle with other clusters or the dense stellar fields in the mid-galactic segment, the dwarfs will preferentially become scattered through encounters. The massive

<sup>2</sup> Mt Wilson Contr 157, Sect 7 (1918)

<sup>3</sup> Harv Circ 350 (1930)

<sup>1</sup> Shapley and Mayberry, Mt Wilson Comm 74 (1921)

cluster stars, which are mostly of high luminosity, and which are concentrated to the center and endowed with low peculiar velocities, will retain their cluster organization longer in a disrupting neighborhood. A globular cluster thus becomes a galactic cluster which slowly dissolves into the galactic field. Flattening and distortion of galactic clusters and star clouds arise through the "encounter machinery" discussed by Jeans, and through rotation. Star streaming appears to be a complication of the various motions in and of the local system and general galactic field.

The galactic system, it appears on this interprotation, is in an advanced stage of the survival of the most massive. In size the spiral nebulae are not comparable to it, ours is a Continent Universe if the average spirals are considered Island Universes

The relation of galactic and globular star clusters to each other, and their relation to star clouds and galactic systems, remains obscure in many respects. Yot the recent study of these structures brings increasing evidence that the above interpretation should be extended. Its modification is necessitated, in part, by difficulties such as the scarcity of clusters intermediate between globular and galactic groups, and the slowness or even impossibility of the amalgamation of clusters and star clouds with no more potent a resisting medium available than the galactic star field with its infrequent encounters. In view of these obstacles, and others related to the distribution of dark nebulosities and the anomalous position of the Galaxy among other systems, the amended hypothesis is advanced that our galactic system is noither a spiral, such as the Andromeda Nebula, nor a single unified discoidal star system, like a Magellanic Cloud on a grand scale. It is rather a super-galaxy—a flattened system of typical galaxies It is comparable, in mass and population, with the Coma-Virgo cloud of bright galaxies, rather than with one of its members. Within the galactic system are fairly distinct galaxies, such as the local system, the Scutum star cloud, and the great star fields in Sagittarius. The dark nebulosities are associated with the local evatem

Galactic star clusters, from the new point of view, are not evolved from globular systems. They are probably the results of a quite different developmental process. The test of the amended hypothesis has in future studies of star distribution and motions, faint variable stars, and the accurate determination of the space distribution and affiliations of galactic clusters.

## Appendix A. Catalogue of Globular Clusters.

The material on which is based the catalogue of globular clusters has been described in the text. For three clusters, N G C. 4372, N G.C. 6356, and N G.C. 6864, special notes appear at the end of the catalogue. Daggers after the N.G.C numbers in the first column indicate questionable objects (ciph. 4). Galactic coordinates are on the Harvard system (Pole 12<sup>h</sup> 40<sup>m</sup>, +28<sup>o</sup>). The values of the ellipticity and orientation are described in ciph. 22. Colons in the orientation column indicate less certain values, and asteriaks mark those derived from star counts on Mount Wilson plates. The magnitudes and diameters are explained in part h), and there and in part j) are described the derivation of the distances listed in the last three columns of the catalogue.

<sup>&</sup>lt;sup>1</sup> Harv Circ 350 (1930)
See Addendum on p. 773,

CI, footnote on NGC 4147 on page 741

Appendix A Cutalogue of

							Append	IX IX	Outun	, Free
	T	1		Gala	ictic	Angilla	Integrat	( la.,	Spec	No of
NGC	Name	RA 1900	Dec 1900	Long	J at	Diameter	ed Magni tude	Class	trum	Variables
104	47 Tuc	0h 19m,6	-72°38′	272°	-45°	23'	3	III	(75	7
288	-	0 47 ,8		157	88	10.0	7,2	X	(15	2 14
362	₫ 62	0 58 ,9		268	-47	5,3	6,0	III II	G	14
1261		3 9 ,5	-55 36	237	-51.5	2,0	8,5	II	``	3
1851	₫ 508	5 10 .8		212	-34.5 $-28$	5,3 3,2	8,1	v		5
1904	M79	5 20 ,1	-24   37 $-35   54$	194 213	-26	1,8	10,1	vi		-
2298	=	6 45 ,4	-35 54 +39 6	148	+23	1 .7	11,0	VII		
2419 2808	_	9 10 ,0		249	-11	6,3	5.7	I	Ko	<b>.</b> ⊶
3201	⊿ 445	10 13 .5	-45 54	244	+ 9	7,7	7,4	X	-	61
4147		12 5 ,0	+19 6	226	+79	1.7	10,3	IX	A7	5
4372n	_	12 20 ,1	-72 7	269	10	12,0	7,8	XII	-	-
4590	M68	12 34 ,2	-26 12	269	+36	2,9	7,6	X		28
4833	_	12 52 ,7	-70 20	271	- 8,5	4 ,7	6,8	VIII	-	5
5024	M53	13 8 ,0	+18 42	305	+79	3.3	6,9	V	-	40
5053		13 11 ,5	+18 13	309.5	+78	3,5	10,5	XI	-	132
5139	ω Cen	13 20 ,8	-46 47	277		23 9,8	3	VIII	(т	160
5272	M3	13 37 ,6	+28 53 -50 52	280	十77.5 十10	1,6	8,5	v	Go	0
5286 5466	4 300	13 39 ,9		8	+72,5	5,0	10,0	XII		11
5634		14 24 ,4	- 5 32	310,5	-1-48,5	1,3	10,4	IV	-	-
I4499	_	14 45 ,0	81 49	275	-20	3,1	11,5	XI	1	-
5824	-	14 57 ,8	-32 40	301	+21	1,0	9,3	I	1.8	
5897	_	15 11 ,7	-20 39	312	- 29	7,3	7.3	XI	-	-
5904	M5	15 13 ,5	+ 2 27	332	+16	12,7	3,6	V	(r	84
5927	_	15 20 ,8	-50 19	294	+ 4	3,0	8,8	IIIV		*
5946†	1552	15 28 ,2 15 39 ,5		295,5	十 3,5 十12	1,3	10,6	VII	1.8	1
5986 6093	M80	15 39 ,5	-37 27 $-22$ 44	305	+18	3,3	6,8	ÎÏ	Ko	4
6101	-	16 14 ,4	-71 58	284,5	-16	3,8	9,5	X	-	
6121	M4	16 17 ,5	-26 17	319	+15	14,0	5,2	IX	F	33
6139		16 21 ,0	-38 36	310	+ 6	1,3	9,8	II		
6144	-	16 21 ,1	-25 49	319	+15	3,3	10,3	XI	-	-
6171	35.3	16 26 ,9	-12 50	332	+22	2,2	8,9	X	Go	
6205	M13	16 38 ,1	+36 39	27	+40	10,0	4,0	IX.	CiO	7
6218 6229	M12	16 42 ,0	- 1 46   +47 42	344 40	+25 +40	9,3	6,0 9,7	VII		1
6235		16 47 ,4		327	+12	1,9	10,8	X		- '
6254	M10	16 51 ,9		343	+22	8,2	5,4	VII	-	
6266	M62	16 54 ,9		322	+ 7	4,3	7,0	IV	ιζυ	26
6273	M19	16 56 ,4		324,5	+ 9	4,3	6,8	[ VIII	G5	-
6284	-	16 58 ,4		326	+ 9	1,5	10,0	1X	I.	
6287	-	16 59 ,1		328	+10	1.7	10,4	VII		
6293 6304		17 4 ,0		325	+ 7	1,9	8,8	IV	(+5 15	3
6316	_	17 8 ,2	1 .	323 325,5	+ 5	1, 6	9,2	III	G <sub>5</sub>	
6325	1 -	17 11 ,9	1	327,5		0,7	11,9	IV		
6333	M 9	17 13 ,3	-18 25	333	+10	2,4	7,4	VIII	172.5	1
6341	M92	17 14 ,1	+43 15	36	+35	8,3	5,1	IV	G5	14
6342	. –	17 15 ,3	-19 29	333	+ 8	0,5	11,4	IV		-
63521		17 17 ,5	-48 22	309	8	2,5	7.9	XI		
6356°	₫ 225	17 17 ,8		334	+ 9	1 ,7	8,6	II	KO	
6362 6366	225	17 21 ,5		293	18	6,7	7,1	X		17
6388		17 22 ,4		346 313	+15	3,4	12,1	III	ĸ	_
6402	M14		- 3 11	349	+14	3,0	7,4	VIII	-	
6397	4 366			304,5		19,0	4,7	IX	G?	2
6426	-	17 39 ,9		356	+15	1,3	12,2	IX		
6440	-	17 43 ,0		335	+ 2	0,7	11,4	V	-	-
6441	_	17 43 ,4		321	- 6,5	2,3	8,4	III	Ko	=
6453	1 —	17 44 ,	7 - 34 36	322,5	- 5.5	0,7	11,2	IV	~	-

Globular Clusters

NGC	RHOL	Orient.	P	actographic	Magnitud		Adopted	Quality	Dirlance kps	R sin #	2 cos #
MGC	пири	Orall	Ver	Bright	6th	30th	Modulus		r.he	Epo.	- Ele
104	8	-55°	-	13,09	12,4	13,4	14.17	b	6,8	- 4,8	4,8
288	9	_	- 1	14,80	14,5	15,1	15,81	ь	14,5	-14.5	0,5
362	8	+65	15.5	14,12	13.5	14,8	15,55	Ъ	12,9	- 9,4	8,8
1261	9.5		-	- 1	- 1		16,72	0	22,0 14,3	-17.2 $-8.1$	11,7
1851	9	-75	=	15.29	15,01	15,72	16,54	Ъ	20,4	- 9,6	18,0
1904	9	+35 +39:		- 15,29	13,01	.31/2	17,12	d	26,5	- 6,9	25,6
2419	9	-56	_	_	-	_	17,41	d	30,3	+11.9	28,0
2808	8	+84		14.9	14,3	15,4	16,05	ь	16,3	- 3.1	16,0
3201	9	-	14,52	13,52	13,3	13,8	14,81	C	9,2	+ 1,4	9,1
4147	_	-	16,8	16,58	16,23	16,93	16,93	ь	24,2 9,6	+23.7 - 1.7	4,6 9,5
4372	9	-	-	14.00	44.74	45.09	14,91	G B	15,5	<b>一 1.7</b> 十 9.1	12,0
4590	9	-80:	15,90	14,80	14,31	15,08	16,01	0	15,9	- 2,2	15.7
4833	8	-79*		15,07	14,94	15,26	16,30	6.	18,2	+17.9	3.5
5024 5053	8	-61	16,19	15,65	15,1	16,0	16,20	a	17,3	+17.0	3.6
5139	8	+30	14,37	12,91	12,6	13,1	14,15	b	6.8	+ 1,8	6,6
5272	8	+54	15,50	14,23	13,92	14,45	15,43	n	12,2	+11,9	2,6
5286	9,5	-	-	_	-	-	16,89	d	23,9	+ 42	23.5
5466	9	-	16,17	15.72	15,1	16,2	16,16	ь	17,0	+16,2	5,1
5634	9	-	_	- 1	_	_	17.49	C	31,4	+23,2	20,5
I 4499	9	- 1	_	-	- 1	_	16,91	0	24,1	+10,4	27,2
5824	-		_	45.45	14,9	15,4	17,32	ь	16,4	+ 8,0	15,5
5897	8 9	-44' +16	15,26	15,15	13,74	14,27	15,17	8	10,8	+ 7,8	7.5
5904 5927	9	710	15,20	13/9/			16,56	d	20,5	+ 1,4	20.1
59461		_	_	_	_		17,54	d	32,2	+ 2,0	32,1
5986		_	_	-	_	_	16,14	C	16,9	3.5	16,6
6093	10	-	_	14,88	14,72	15,09	16,22	R.	17.5	+ 5.4	16,6
6101	8	+35	-	-	-		16,60	d	20,8	- 5.7	20,0
6121	9 8	+72*	14,27	13,88	13.3	14,4	14,30	b	7.2	+ 1.9	7,0 29,1
6139	9	-64	_		45.0	16,3	17,34	d	29.3 18,1	+ 4,8	17.5
6144		-22:	_	15,76	15,2 15,2	15,9	16,29	Ъ	21,2	+ 7.9	19,6
6171	9.5	-63*	15,20	15,46	13.45	13,92	15.07	B.	10,3	+ 6,6	7.9
6205 6218	7,3	-03	13,20	13,97	13,56	14,31	15,21	b	11,0	+ 4.6	9,9
6229				16,18	15,90	16,37	17,37	ь	29,8	+19,2	2,8
6235	8	+89	-	16,17	15.7	16,8	17,28	C	28,6	+ 5.9	28,0
6254	9	-	_	14,06	13.35	14,38	15,26	b	11,2	+ 4.2	10,4
6266	8	+16	16,40	15,87	15,6	16,1	16,35	C	18,6	1 2.3	18,4
6273	6	-28	_	-	-	-	16,06	C	16,3	+ 4,4	16,1
G284	10	-	-	-	-	_	17,24	d	28,0	+ 4.4	27.7
6287	2	_	-	_	_	_	17,24	0	23,1	+ 2.8	22,9
6293	9.5	_	_	=	_	_	17,02	0	25.3	+ 2,2	25,2
6304 6316	8,3	=	=		_	_	17.52	d	31,8	+ 2,8	31,6
6325	1 -	_	_	l –	_	_	18,3	0	46	1- 4,8	46.
0333	9	_	_	15,61	16,76	15,08	16,61	b	20,8	+ 3,6	
6341	8	+16	1 -	13,86	13,60	14,16		b	11,2	+ 6,4	
6342	-	-	_	_	_	-	18,0:	0	40	+ 5,6	
6352	t 9	1	_		1.00	-	16,48	d	19,7	- 2,7	
6356		-14	] -	17,16	16,86	17,44	18,51	d	15,1	+ 7,8	
6362		+78		-	_		15,90	8	29	+ 7.5	
6366			_		_		16,20		17,3	- 2,4	
6388		+76	=	15,44	14,85	15,86	16,48	8.	19.7		
6397	j	+73		12,61	11,9	13,1	13,76		5,6		
6426		1 -73	_	-		-	17.85	0	37.1	+ 9,6	35,5
6440		+10	4 -	-	l -	_	18,5	0	50	+ 1.7	50:
6441		+40	] =	I -	l –	-	16,62		21,1	- 2,2	
6453		_	I -	-	I -	<b>—</b>	18,5:	0	50	- 4,8	50

Catalogue of Globular

NGC	Name	RA 1900	Dec 1900	Gal-	Lat	Angulai Diameter	Integra ted Mag nitude	Class	Spec trum	No of Variables
			<u> </u>	Tong			minuc			
6496	_	17h 51m,8	-44° 14'	315°	-10°,5	2',2	9,7	ПX	-	
0517		17 56 ,4		347	+ 6	0,4	12,1	IV		
6522	_	17 57 ,2		328	5	0,7	11,0	V1		
6528	-	17 58 ,4	-30 4	328,5	- 5	0,5	11,8	V		
6535†	_	17 58 .7	→ 0 18	355	4 9 ,5	1.3	11,9	X1	~	
6539†		17 59 ,4	<b>-</b> 7 35	348	+ 5	1,3	12,6	X.		
6541	△ 473	18 0 ,8	-43 44	317	-12	6,3	5,8	III	(r	
6553	_	18 3 ,2	-25 56	332,5	- 5	1,7	10,0	XI	5-W	0
6569		18 7 ,2	-31 51	328	- 7 ,5	1,4	10,2	VIII		
6584	₫ 376	18 10 ,6	-52 15	309,5	-17	2,5	8,3	VIII		()
6624		18 17 ,3	-30 24	330	10	2,0	8,6	VI	Mo	-
6626	M28	18 18 ,4	-24 55	335	- 7	4,7	6,8	1V	(15	9
6637	M69	18 24 ,8		329	-11	2,8	7,5	V	1/2	
6638	_	18 24 ,8		335.5	7 .5	1,4	9,2	VI		
6652	***	18 29 ,2		328,5	-13	1,7	8,7	VI	N5	-
6656	M22	18 30 ,3		337	- 9	17,3	3,6	VII	-	21
6681	M70	18 36 ,7		330	13 ,5	2,5	7.5	V	+-	***
6712	_	18 47 ,6		353,5	- 6	2,1	9,9	IX	-	1
6715	M54	18 48 ,7		333	-15	2,1	7,1	III	1.8	-
6723	√ 573	18 52 ,8		328	-19	5,8	6,0	VII	(.5?	17
6752	⊿ 295	19 2 ,0		303	-26.5	13.3	4,6	VI	(-()	1
6760		19 6 ,1		3	5	1,9	10,9	IX		pm
6779	M56	19 12 ,7		30	+ 8	1,8	8,8	X.	~	1
6809	M55	19 33 ,7		336	-25	10,0	4.4	XI		2
6864n	M75	20 0 ,2		347	-27	1,9	8,6	1	60	11
6934		20 29 ,3		20	-20	1,5	9,4	VIII	60	
6981	M72	20 48 ,0		3	-34	2,0	8,6	1X	-	29
7006	35.4	20 56 ,8		32	-21	1,1	11.8	I		11
7078	M15	21 25 ,2		33	-28	7,4	5,2	IV	Ţ.	74
7089	M 2	21 28 ,3		21	36	8,2	5,0	II	1.5	10
7099	W130	21 34 ,7		355	-48 ,5		6,4	V	1.8	3
7492	****	23 3 ,1	-16 10	22	-64	3,3	10,8	XII		9

Notes to Appendix A

NGC 4372 The distance depends only on the diameter measure. The cluster appears to be partially obscured by one of the streamers from the Coal Sack nebula. A special investigation of the magnitudes is being made on Harvard plates.

NGC 6356, 6864 The distance depends only on the magnitudes of the bright stars, since the integrated brightness and diameter appear to be abnormally large. There may be obscuring nebulosity in the field of NGC 6356

Clusters, (Continued.)

N.G.C.	Hilpt	Orient	r	hotographi	o Magalius	de	Adopted	Quelliv	Distance	R sto #	R con A
Nusca	- Allyc	Orani,	Yat	Bright	64	30th	Modnite	Quality	kpe	kpe	hpc
6496	_	_	ı	-	-	_	16,90	d	24,0	- 4.0	21.6
6517	В	-4°	_	-	7	_	18,5	0	50	+ 5.2	50
6522	_	- 1	_		~		17.78	G	36,0	- 3,2	35,8
6528	_	-	_	_	~	<b>–</b>	18,24	0	44,4	- 3.9	44,1
6535†	_	[ - [	_	15,9	15.3	16,4	17,13	d	26,7	+ 4,4	26,3
6539†	9	-	-	-	-	_	17,94	0	38,7	+ 3,4	38,4
6541	9	- 1	14,42	13,35	12,7	13,8	14.76	a	8,9	- 1,8	8,7
6553	9	-	_	-		-	17,14	C	26,8	- 2,3	26,7
6569	9,5	_		-	-	_	17,35	o	29,5	- 3,8	29,2
6584	9	-	_		~	-	16,56	C	20,5	- 6,0	19,6
6624	10	-	_	-	~	_	16,74	C	22,2	- 3.8	21,8
6626	9	+18		14,87	14,49	15,11	16,10	6	16,6	- 2,0	16.4
6637	9	-	_	-	-	_	16,36	C	18,7	- 3,6	18.4
6638	8	-27		16,22	15,90	16,60	17,36	b	29,6	- 3.9	29.3
6652	8	-11:	_	_	~-	_	16,87	d	23,6	- 5,3	23,0
6656	8	+18	14,06	12,93	12,80	13,26	14,16	n.	6,8	- 1,1	6,7
6681	9.5	_	_	_		_	16,41	G	19,2	- 4.5	18,8
67121	-	_	_	16,10	15,65	16,36	17,10	d	26,2	- 2,7	26,0
6715	10	-	_	_	-	_	16,44	d	19.4	- 5,0	18,7
6723	9,5	- 1	15,33	14,20	13,7	14,8	15,44	b	12,3	- 4.1	11,7
6752	_	_	_	13,26	12,8	13,6	14,62	1 <sub>0</sub>	8,4	-3.8	7,4
6760t	_	-	-		-	_	17,28	0	28,6	- 2,5	28,5
6779	8	+12:	_	15,31	14,98	15,70	16,54	Ъ	20,3	+ 2,8	20,0
6809	9	_	_	13,58	12,9	14,2	14.74	ъ	8,8	- 3.7	8.0
6864	وا	[ - [	_	17,06	16,76	17.35	18,43	d	48.5	-22.0	43,2
6934	9	-	_	15,78	15,33	16,11	16,98	b	24.9	- 8,5	23,4
6981		-	16,80	15,86	15.53	16,20	16,84	A	23,3	-13.0	19,3
7006	-	-	18,96	17,50	16,99	17,89	18,77	ь	56,8	-20,4	53,0
7078	8	-11	15,63	14.31	14,13	14,55	15.60	G	13,1	- 6,1	11.6
7089	9	-80°	15,71	14,61	14,25	14,76	15,72	R.	13.9	- 8,2	11,3
7099	j ģ	_	-	14,63	13,77	15,04	15,82	Ъ	14.6	-10,9	9.7
7492	9	-	_	16,82	16,3	17.1	17,01	0	25,2	-22,7	11,1

Appendix B

Catalogue of Galactic Clusters1

		Notes	_	١ .		l 		]	1	1	-	' 1	1	ļ	2	1	40		, 1	1	1	4	1	1		10	1	1	1	9	ı	1	1	I	i	١
	RSID	¼=-0,5 pc	7.7	1 0	1 + 12	++	+403	02 -	1	+ 57	- 26	+ 63	+	1 34	9	-405	-136	-136	A+ 18	- 80	+ 43	<168	+166	669-	-205	57	+169	- 46	+ 19	15	-288	+ 24	-161	-230	-486	1
	Linear	M=-0,5 pc	14.4	,	t V	) 1/	4 4 0 00	100	0,0	9,0	1,7	1,2	17	2,8	25,	13.8	[263	26.3	<. <.	99	2,3	\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	7,9	44	3,6	10	50,0	160	63	10	128	83	13,1	3 2	9 1	44
ľ	e,	M = -0	3.80	2 5	2,0	4 4	10 5	1.15	0,66	2 75	1 15	1 38	1 15	1,91		1 05			99 03	2,29	1.15	99 03	1,82	5.0	0,83		1.15	4,57	0,87	_	1,10	1,91	1 00	1 10	2,09	1 66
	Distance	M=+0,5 W	2.40	1.26	1 74	0.91	661	0,72	0,42	1,74	0,72	0.87	0 72	1,20	0,79	99'0		16,2		1,45						-	0 72	2,88	0,55	0 04	69 0	1 20	0,63	69 0	1 32	103
. l	Mag	5th Star	1 8							11 7															9 1					ı			9 3			
Catalogue of Galactic Ciusters	Approx	of Plate	13 ш	50	1	13	16	128	12,8	128	12,8	12,8	128	12,8	12,8	12	ī	1	12,8	12,8	12,8	12,8	12,8	ı	13.2	I	12,8	ı	12.8	1	I	1	12,6	13	13	126
DIACEL	No of	Stars	35	20	50	30	30	40	100	9	9	50	20	30	80	20	1	1	50	40	11	80	30	40	40	ı	12	40	80	1	30	40	09	13	10	tr O
10	Orient	0	ı	1	1	1	Ind	Ind	84	1	1	i	1	I	81	Ind	63	\$	l	1	i	I	1	Ind	I	ı	1	1	71	1	33	Ind	7.1	1	69	١
211801	Approx.	meter	13,	Ξ	7	9	15	4	10	7	'n	m	ın	in	11	45	36	36	30	10	7	18	I.S	30	L L	1	1	12	55	ı	9	15	10	0.	ξ.	O
9 9	Class		*4~4	Ð	٥	ð	υ	ס	ø	ψ.	D	Ö	d	Þ	0	゙゙゙゙゙゙	44	a)	ゼ	Φ	ש	þ	v	a	U	U	ø	U	Φ	v	U	e U	o)	o '	ď	ซ
	Galactic	Lat	4-1	d	Ò	0	23	'n	ęŋ	+ 1 5	4	C)	0	4-1	0	22	w	'n	4	0, 2	ч	14	'n	00	#	13	×	0	<b>Y</b> M	13	72	0	0	-12 1	-11 7	ا ان
	Gal	Long	88	88,5	88 5	88 5	90	24,5	94 5	95	96	96,5	86	86	86	105	102,5	103	106,5	104	103	111 5	105,5	114,5	123,5	134 5	110,5	120	120	147	148,5	129 5	147	153.5	154	136
	Dec. 1900		+60	+59	+62	+62	+84	+ 58	+57	1 62 47	100	+63	+61	9	160	+37	+56	+ 56	+61	+57	+61	+43	+62	+46	+36	+23	+62	+49	+ 20							
	R.4. 1900		<b>SI</b>	24	25	27	35	6	12	1 22 8						51	12	15	25	56	3	35	m	_	52	41	200	61	_	4.	40	43	4 57 ,6	4, 1	ا ۾	13
	ر الا		103	129	133	146	188	436	457	559	581	637	654	629	663	752	869	\$84	Mel 15	957	1027	1039	H	1245	1342	Pletades	1502	1513	1528	Hyades	1647	1664	1746	1807	1817	1857

1 Described in ciph 33, above

	}	200	۱	ı	ı	7	· 00	0	١.	ı	ı	ı	10	1	ı	ı	ı	ı	:	44	1	13	ı	ı	14	ı	ı	15	1	i	1	ı	ı	16	ı	ı	ı
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	I heart Dismeter	X=-0,5	>3.6	2.8	3.0	4.9	10.7	8,4																			ı	3,7	18,1	5.5	15,9	ţ	3,3	1,7	6,5	22	4,8
	8	#	>4.17	0,79	208	1.10				2,19	2.19	2,0	62.0	0,79	3,0	V5.01	2.19	8,33	9,12	₹0,76	15.8	₹0,76	r r	2,00	<0.76	0,76		8,0	6,92	0,95	2,19		0,95	0,95	32	0,95	1.15
	Distract	M-+0,5	>2.63	0.0	25	69.0	1.1	1,4	. 1	1,38	1,38	3,2	0,50	0,50	1,91	>3,16	1,38	5,25	5,76	84,00	10,0	\$4.6V	1,45	1,05	A0,48	0 48	I	0,5	4.37	0,60	1,38	1	0,0	09'0	20-	09'0	0,72
	Ä	Star Star	[12=,6	0	11 .1	7. 6	1	7. 6	ı	11 2	±	13	0, 6	0' 6	6, 11	[13	11 2	1, 11	14 ,3	18 ,9	15 .5	6. 87	11 .3	10 ,6	9, 8	80	ı	0	13 ,7	4, 6	11 2	l	4, 6	4. 6	13	4 6	o Q
	Appell	of Parts	ı	12=,6	12 .6	ı	١	2, 4,	1	13,0	13,0	1	13 ,0	1	+	1	14	15 ,5	ı	ı	1	*	13	13	ı	14	ı	1	14	‡	13 ,5	1	ı	ı	1	13,55	8, 01
Ded.)	No. of	200	8	8	\$	8	8	150	ı	25	8	\$	8	18	30	8	R	ይ	9	16	တ	a	8	옸	20	8	ı	8	옸	25	8	!	S,	4	କ	ድ	S,
Continued.	t de	•	1	ı	Ind	Pog	Ę	ı	1	ı	1	5	4	ı	1	19	ı	1	9	ı	ı	ı	13	17	0	ı	i	2	47	ı	1	E	Z	ı	R	z	ı
	Agent	1	R	7	10	a	ä	8	'n	<b>14</b>	4	4	\$	49	ug	•••	∞	14	4	\$	m	<u></u> 옷	'n	15	R	10	+	2	٥	8	23	9	ဌ	9	-	œ	5
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	Galactio	I.e.	+ 70,4	+ 0 7	+ 1 .6	+ 2,0	+ 2 .4	+ 4 .5	+14,4	+ 1 ,6	+ 2.7	+ 2 .8	9 6 +	1.1	7.4-	0,1	7.8 -	4,01	-16 ,5	9' 0	4 3 .6	7. 6 -	+11 ,7	118 ,4	0, 6	+ 1 ,5	+10 .4	1.01	4 + 8	+ 1.7	- 5 6	+13 3	1.0 -	++1	+21 ,1	+ 1 ,5	9' + +
	10	Long	•	141 ,5		140	143	145	131	154	154	7.		163 ,5	171				206 .5		169 .5					180		189 ,5			205 ,5			205 .5	166	Ŕ	28.5
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	T C		1883	1893	1907	252	98	2090	2126		I 2157	22.53	2168	2169	2186	<b>3</b>	215	238	200	24	252	32	1266	2281	13	23	230	2333	75.7	2353	202	2355	2360	2362	2420	2421	3423

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Linear	Diameter M=-0,5 pc	4,2	67	4	12,8	8.0	6.4	13.9	6.1	99	3.0	4t (U	99	16	23.0	112	4	00	3.7	12	0,0	ių.	2 2	1 ;	2,5	0	11,6	7. Ci	9,1	20	56	4,4	3,1	7,9	13	12.8	00
93	V=-0,5 kpc	1,82	4.57	1,66	1,82	1.10	4.37	1 91	2 63	1 26	1,45	2 09	2,29	1 38	1,32	1 82	0,95	0 95	1,26	0 95	1 91	1 91	2,51	2	4 37	90 0	3 98	2	3,47	1 32	2 19	0.5	151	1 82	5.0	2 19	2 19
Distance	W=-0,5	1.15	2 88	1 05	1.1	0.69	2,7	1.20	1 66	0 79	0 91	1,32	145	0.87	0,83	1 15	09'0	090	0 79	09 0	1 20	1 20	158	0,	2 75	0 04	2,51	m 13	2,19	0,83	1,38	3,2	0,95	1,15	3.2	138	1.38
	Mag 5th Star	10 m S	12 8	40 .6	10 .8	0	12.	10	11.0	10,01	10 3	11 ,1	11 3	10 2	10 ,1	10 8	9 4	4, 6	10 0	7 6	10 9	10 9	11 5	- 8	12 .7						11,			10 8			11 2
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	Onent	25	; 1	8	11	1.5	1	14	n 1	1	1	Ind	Ind	15	: 1	89	1		16	I	I	1	69	ı	1	1	ì	9	36	1	1	1	ı	5,5	. (n	1	!
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	NGC		Me /		2439	2437	2447	2455	2477	2479	7407	7,60	7000	2000	2509	2510	4557	74047	2567	2507	25071	2587	2627	2622	2635	T 2201	2550	2660	2676	1 0202	2333	20/07	2071	E 5	2682	2818	1.2488

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	Library	20-8	3.6	71.7	7,6	11,5	4,2	410	3,2	10,5	<del>1</del> ,1	9,1	1,5	+,	6,1	23	1,5	64	9,1	2.6	75	6,1	9,9	1	7.	4	4	13,5	41,4	1,1	6,0	7.7	ιų v	7.7	1,1	5,5	7.3	80
	6	9	47.4	×3,98	0,3	1,3	288	0,46 0,46	1,38	3,5	ä	0,52	1,05	र्ध	1.74	90	S,	99,0	5.25	2,63	0,95	525	1,51		1,05	4. 86.	8	6,61	7.9	2,0	0,3	6,61	8	6,61	į.	1,58	0,83	251
	Distract	K = +0,3 M	9	>2.51	70	0,83	ă	00°0>	0,87	1,51	0,13	0,33	9,0	0,76	1,10	4,	0,33	0,42	3,31	1,66	09'0	3,31	0,95	•	99,0	0,87	0,87	4,17	2,0	0.57	70	4,17	0,76	4,17	0,83	9,1	27,0	1.58
	×	i d	408.7	22.5	7	10 ,1	11 ,8	17 .8	10	11 4	9	80 1,	9, 6	0,0	10 .7	11,0	8.1	9, 8	13 ,1	11 ,6	4 6	13 ,1	<b>*</b>	ı	9, 6	5 5	10 L	13 ,6	#	و ب	7.	13 ,6.	6, 6	13 ,6	1, 01	10 ,5	7.	11 ,5
	Appear	d Pil	128.5	2 1	ı	1	2	1	1	ı	1	1	13	13	13	13	13	13	1	53	13	13 .5	13 ,6	ı	13 ,6	13 ,6	13 6	ı	ı	13 ,6	13 ,6	4.	13 ,6	#	13 ,6	13 ,6	13 ,5	13 ,5
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	3	Log	2 0000	247 5	251	248 x	252	353	25	257	257	257	258,5	259	260	260	36.	262.5	262.5	265	265	267	267,5	200	267.5	368	768	260	260	3	271	277.	2	1	17	3.18 5.18	284	284.5
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	R sin B	pc pc	- 23	+ 54	+ 94	+104	68 十	+ 53	+126	-186	145	- 75	-105	-122	-130	+ 70	- 50	-145	- 56	4	+ 13	- 70	- 63	-475	- 105	- + V	+	× ∨ ∨	>-637	- 108	7    -	+1+	1	- 97	62 -	-227	- 82	ļ
	Linear	W=-0,5 pc	7.9	26	9'9	4,6	212	48	s, S	4 4	\$ 10	2	80	6,4	14 5	09	09	17,5	38	17	1,6	လွှဲလ	61 4.	13 14	4,0	<1,7	17	+ + V	78,7	10,0	학	53	0,8	3,6	5.4	6	7.6	1
	8	M=-0,5 kpc	1 82	1 10	3,80	1 58	1 82	1,82	6 61	3 80	6 61	0,63	1,91	1,10	1,66	0.83	2,29	2 00	1,3	145	0 79	1,51	1,66	3 98	4 57	<0,38	0 57	<0.38	>5,01	2,29	151	0 10	0,3	2,51	1,05	1 45	2 63	1
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	Approx	Mag Lim of Plate		10 5	13 ,6			13 ,6	1	13 ,6	ı	10	13 6	13 6	13 ,5	13 5	12, 2	13 5	13 ,5	1	13 ,6	1	1	13 31	1	I	12 2	12 ,2	1	12, 21	1	13 S	1		57	13	1	I
ned )	No of	Stars	50	30	30	16	120	80	30	100	30	30	120	35	30	120	09	9	8	10	20	30	25	20	20	120	0+	200	70	9	30	20	52	3	30	200	9,	l
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	Approx	meter	15'	so.	9	10	40	6	က	4	ťΩ	10	12	50	30	25	6	30	01	*	-1	20	'n	22	'n	10	10	40	9	10	10	IS	5	10	12	14	9	<b></b>
	5	Class	44	Ф	ø	o	ъ	44	ø	Ŧ	44	ヤ	44	ש	Ö	ø	4	ø	שי	44	44	ø	4-1	ø	ש	υ	44	v	44	ø	44	יט'	T	þ£	o o	ø	44	b0
	Galactic	Lat	ဝိ	4	+ 1 +	'n	c)	4	**	d					4 +	+ 4 8	1 19	- 4 2	100	+ 0 +	+ 1,0	1 2 ,6	1 2 7	8,9 -	1 1 3	0	4.0十	Ŧ	۲							0, 6		খ
	Gal	Long	282°,5	285		287 ,5				293 5								300 .5		306				301 5				312 ,5		309 .5		307	316	316	17.0	307 5	317	327
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		R A. 1900	22	28	36	41	1	80	26	4	47	10	10	10	-	Š.	200	24	27	200	100	100	30	41	43	47	8	40	10	, נר זר	3 17	1 1	5 16	200	: =	17 16 .9	17	
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	$R \sin \beta$ $M = -0.5$	pc	+ 46	-108	-272	1 25	+ 56	+663	18	1 41	13	- 81	-205	+100	+275	-102	+ 17	4	+1034	-406	-135	- 10	- 12	+ 41	<b>∔</b>	-177	- 80	-185	13	+118	+	+ 11	+480	6	- 22	-362	- 38
,	Drameter	M=-05	2,8	5,8	74,4	1	126	8,8	1,1	18	8	2,3	2,3	1,7	7.3	6,7	1,8	33	73	16,8	3,0	67	22	0.8	1,7	7.7	47	4 4	2,13	2,9	1,6	4 1	13,3	4,0	1,2	3+8	4 8
		M = -0.5 kpc	0,79	2,00	>5,01	5 01	2 88	5 01	0 79	0 79	5 01	0,79	2,00	0,95	5,01	1,15	0,79	0 95	0	2,88	2 40	2 88	0.25	2 88	2,88	1,32	0,79	5 01	0,79	5 01	2 75		4,57	2,75	2 00	3 98	2 75
	Dist	M=-0,5 2 kpc	0,50	1,26	>3 16	3 16	1,82	3,16	0.50	0,50	3 16	050	1,26	09'0	3 16	0 72	0,50	09,0	3,2	1,82	1,51	1 82	0.16	1,82	1 82	0.83	0.50	3 16	0,50	3,16	1,74	1,17	2,88	1,74	1 26	2 51	1,74
	Mag	5th Star		11 0	[13	-	11,8				13	0, 9	11,0	4, 6	13 0	8, 8,	0' 6	9 4	13							10 1		13	0, 6	13			12 ,8			12 5	11 ,7
	Approx	of Plate	13m	13	1	ı		1	13	1	1	i	1	13	1	ı	1	1	ı	1	13	1	1	ı	1	ì	ı	ı	13	ı	1	13	13	ı	ļ	13	1
	No of	Stars	40	20	50	9	50	150	30	50	15	20	100	20	30	35	40	20	80	100	30	20	25	10	20	20	40	40	50	25	27	120	20	8	18	200	25
namman)	Ornemt	•	l	1	1	1	† 	1	1	I	1	1	Ind	1	ı	1	1	1	Ind	23	1	ı	1	ı	1	1	1	ı	١	1	1	20	1	1	ı	Ind	ı
_	Approx.	meter	12,	2	m	1	131	9	iņ.	\$	4	2	4	9	10	20	∞	12	м	50	ıo	00	30	-	7	20	20	ריז	10	7	N	12	10	'n	7	30	•
	Class		đ	P	4-1	ø	Þ	יסי	Þ	ಶ	р	ט	b,Q	ď	e	9	ש	Þ	φø	е	ø	e	o	þ	þ	ש	P	שׁ	ď	ø	ซ	ø	ש	rd	v	v	Þ
	Galactic	Lat		- 3,1	'n	0		~	4	n	0	w	10	9	'n	W	*	0	11	8	3	0	C.	0	0	7	เก	N	4	7	0	0		0			
	Gali	Long		6,5			47	41 5		27 5		24	24 ,5	47, 5	35, 55	33 5	46 ,5	15			57 ,5		60 ,5		5, 59	63	66,5	69		76 ,5			83 ,5				83 ,5
	Dec. 1900		+100	+ 4 4	+	1-20	+46	+39	+23	+22	+29	118	+18	+43	+40	+26	+40	+38	99+	+27	+45	+51	+48	+54	+53	+46	+49	+53	+ 57	109	+60	+61	+67	+61	09+	+ 56	109
	R.A. 1900	1		(1	'n	56	35	37	38	46	48	48	49	0	7	7	19	30	53	30	19	27	28	40	40	Ţ	11	11	43	50	1	19	4,	49	51	22	
	N.G.C.	,																																			7790

#### Notes to Appendix B

1 Mossier 103

2 Distance from WALLENGUIST, Upsale Medd 42 (1929)

3 h and z Porsol, flith star assumed of magnitude -2 ,5 TRUMPLER [Publ ASP 38, p 352 (1926)] gives a distance of 2,3 on the beals of the mean magnitude for Class Ao. 4 Measter 34

5 Memier 45, the diameter from RUSSELL, DUGAR, and STEWART.

6 Distance and diameter from Russell, Dugan, and Stewart corresponds to an angular radius of nearly two degrees

7 Moesier 38

8 Messier 36, distance from Wallenguist, Upsale Medd 32 (1927)

9 Mossier 37, distance from you ZEIPEL and LINDOREN, Svenaka Vot Akad Handl 61, No 15 (1921).

10 Mossier 35

11 Scarcely resolved 12 Eccentric in an alliptical diffuse nebula.

13 S Monocarotis in cluster, 14 Mouster 41

15 Monaicr 50 16 r Canis Majoris in cluster.

17 Memier 46, an important photographic catalogue by Chevalter 18 Mossier 93

19 Praceope, Mossier 44, distance from Russell, Dugan, and Stewart

20 Messier 67

21 Diffuse nebula in a coarse cluster 22 7 Caringo involved

23 Coma Berenless, distance from Russell, Dugan, and STEWART

24 N Crucis.

25 Not resolved, a photograph of N G.C. 6540 appears in Pop Astr Tidak 8, p 62 (1927).

26 Mount Wilson plate.

27 Messler 6. 29 Mosaler 23.

28 Mossier 7 30 Momier 21.

31 Mossier 24 33 Mossier 18

32 Memier 16. 34 Mossier 17, nebulosity.

- 35 Memsler 25
- 36 Messier 26, TRUMPLER finds a distance of 2,75 [Lick Bull 14, p 122 (1929)]. 37 Memier 11, distance from TRUMPLER.

39 Mondor 29.

38 Messler 71, 40 Memior 39

41 Mossier 52, distance from Wallengular, Upsala Modd 42 (1929).

Addendum Current work on problems of both our own and external systems, in progress since this section was written, contributes effectively to our view of galactic atructure and indicates the necessity for gathering much more evidence before any conclusive theory can be advanced. For instance, there have been important studies at Harvard, Mount Wilson (STEUBINS), and McCormick Observatories on the integrated magnitudes and colors of globular clusters. The absorption extending out from the "region of avoidance" appears to affect the magnitudes and distances of clusters in low latitudes, making uncortain and impractical the estimate of the dimensions of the Milky Way in its own plane, but, on the other hand, the Harvard studies of faint cluster type variables in high latitudes (Wash Nat. Ac. Proc in proce, 1933) indicate a total guiactic extent of the order of that given above,

### Chapter 6

# The Nebulae.

Ву

### Heber D. Curtis-Ann Arbor, Mich

With 58 illustrations in the text and on a plate

## a) Introduction.

1. Definition of Nebulae. In the early historical development of the field, any object that was non-stellar with the limited telescopic powers available, and that did not appertain to the solar system, was termed a nebula. The earlier lists and even the more important later catalogues have in general made no complete or satisfactory distinction as to the character of the nebulous object, and the genetic influence of such reference media as the great catalogues of Dreyer have involved the subject in a number of contradictions through the inclusion of such non-nebular classes as the globular star-clusters and the spirals. These inconsistencies persist in all the modern bibliographical apparatus of the field, and doubtless can never be entirely removed. Further reference to these difficulties will be made in ciph 4 and 34

2. Historical Notes. As in most fields of astronomy, research on the nebulae

may be divided into three moderately well-marked periods

A. The period preceding 1782, marked by visual or spotadic telescopic observation, and now of little more than historical interest. A few brighter star-clusters and the Great Spiral in Andromeda, which can be made out by the unaided eye, were noted very early. Aratus (300? a d) mentions Praesepc; Al-Suff (ca. 960 a.d.) notes Andromeda, Hevelius (1690), Halley (1715), and La Caille (1755), catalogued a few of such brighter objects. Messier's lists of 103 bright nebulae and clusters appeared in 1771 and 1781—82 See Appendix No. 1 for the modern identification of these objects, for which Messier's numbers are still in frequent use.

B. From 1782 to 1898 To Sir William Herschel must be given the unchallenged rank of pioneer in the field of nebular discovery. For nearly a quarter of a century following 1782, with tremendous zeal, with instruments which would seem totally inadequate to the modern observer, with an acuity of vision which has perhaps never been surpassed and which is a constant source of amazement to those who review his work with the much more powerful instruments of the present day, he discovered and catalogued in eight classes (cf. Appendix No. 2) 2509 nebulae and clusters

Second only to the work of his famous father was the continuation made by Sir John Herschel, who observed 2307 nebulae at Slough, and 1708 southern

1

<sup>&</sup>lt;sup>1</sup> Herschel's numerous papers in the Phil Trans and other media are now most easily accessible in: Scientific Papers of Sir William Herschel, Published by the Royal Society and the Royal Astronomical Society 2 vols, quarto London (1912).

objects on his expedition to the Cape of Good Hope, in the years from 1830 to 1847 He collected his own and his father's discoveries in his General Catalogue of Nebulac1, containing 5079 entries, and referred to as GC in the older literature.

The impetus which had been given to the work of nebular discovery by the HERSCHELS brought a large number of other workers into this field in the middle third of the nineteenth century Space prevents more than a mention of the names of Rosse, Lassell, Stephan, D'Arrest, Swift, Schönfeld, Bond, and Voger. To Rosse is due the first detection of the spiral form; he discovered perhaps twenty spirals with the 6-foot reflector. There were many observers in this period who concentrated solely upon the discovery of new objects, with little care for accuracy of position. Others, as D'ARREST's, made careful determinations of position, which may conceivably serve as a point d'appui for

proper motion investigations of the distant future

C. 1898 and following. While there is no well-marked line of demarkation between the second and third chronological divisions, the year 1898 may be conveniently taken as the starting point of the modern epoch, even though the very first photographic and spectrographic results are considerably earlier in point of time. The discovery of bright lines in the spectra of gaseous nebulae was made by Sir WILLIAM HUGGINS in 18644, to whom also is due the first spectrogram (of the Orion Nebula) in 1882. The first nebular photograph (also of the Orion Nebula) was taken by DRAPER in 18804 The first extensive sories of nebular photographs is due to Sir IRAAC ROBERTS, and was made in the years from 1885 to 1904. His photographs confirmed Rosse's discoveries of spirals, and increased the number of known spirals to about forty.

It now seems strange that an immediate wider application of photography did not at once follow the significant pioneer efforts of Roberts, Draffer, Com-MON, HUGGINS, JANSSEN, and others. During the two decades following 1870 a considerable amount of purely stellar photography was carried on, but the great value of the reflecting telescope was not fully appreciated until its epochmaking revivification by KERLER, at Lick Observatory, in 1898—1900. KERLER's results showed the following salient advances, which have formed the norm for

much subsequent nebular research®

1 Reflecting telescopes of moderately large focal ratios (1.5 to 1:6) are the most efficient instruments known for nebular research.

2. A wealth of structural detail was shown, impossible to secure visually or with refractors

3. A predominantly spiral form was shown to exist in a large proportion of the objects recorded. About 40 objects had been previously found to be spiral

1 Phil Trans (1864)

Siderum nebulosorum observationes Havnianses (1867), 1942 entries.

CR 94, p 94 (1882).

Amer J Se (3) 20, p. 433 (1880).

Lick Publ 8 (1908).

The first stellar photograph was taken with the 15-inch equatorial of Harvard College Observatory on July 17, 1850, by Mr Whipple working under the direction of Professor Bown. An image of α Lyrae was obtained

Proc R S London 13, p. 492 (1864)

Porhaps the main reason for this neglect of the reflector came from purely mechanical considerations. With scarcely an exception, reflecting telescopes from the days of the elder HERSCHEL down were mounted and equipped most crudely, in comparison with the mechanical excellence developed in the mountings of refracting telescopes. LASSELL's reflector at Malta utilized man-power for its "driving-clock", a workman gave one revolution per second to a heavy flywheel suitably geared to the telescope. There was, in this period, scarcely a single raflector possessing adequate rigidity, accurate clock-work, or convenience of manipulation.

4 Very large numbers of very small and faint objects were recorded "A conservative estimate places the number within reach of the Crossley reflector at about 120000. The number of nebulae in our catalogues is but a small fraction of this." See ciph 36

Keeler's piogram with the Ciossley reflector was continued and completed by Perrine (1901—1903), and extended by Curtis (1909—1918) Later, the magnificent 60-inch and 100-inch reflectors at Mt Wilson, in the hands of Ritchey, Hubble, Pease, Duncan, Humason, and others, have secured larger scale nebular photographs of the highest perfection. A vast amount of survey data has been accumulated by the Harvard workers and on the Franklin-Adams star charts. All work in the radial velocities and spectrographic rotations of the spirals goes back to the extensive pioneer contributions made by Slipher, at Lowell Observatory. In Europe, to mention but a few, notable investigations have been carried out by Wolf, Reinmuth, Wirtz, Holetschek, Hagen, and others. In the still comparatively neglected southern heavens, a beginning has been made by Perrine, at Cordoba, and by Knox-Shaw and associates, at Helwan. More complete details of the progress which has been made since 1900 in the nebular field should be sought in the separate sections.

8. Bibliographical Notes<sup>1</sup>. The culmination of a century of discovery, marked by some slight progress in delineation of form and classification, was marked in 1888 by Drever's collection and revision of all previous results in his New General Catalogue (NGC), which, with his two supplementary Index Catalogues (I, II), contains 13223 entries. These are still the most complete catalogues of nebular objects, and the indispensable basis for all succeeding surveys.

The older nebular literature refers frequently to nebulae by the Messier number M, by Sh W Herschel's Classes and numbers, by the numbers in Sir J Herschel's lists (JII), or by the same author's General Catalogue number (GC). The bright spiral numbered 4303 in the New General Catalogue (NGC), may then possibly have also the designations M61, I 139, JII1202, or GC2878. This is a source of considerable confusion and loss of time in consulting references in the older literature. Appendices Nos 1, 2, 3, and 4, give finding lists for locating such references in the NGC, which is the only method that should be employed in designating such objects. Throughout this treatment, nebulae will accordingly be referred to solely in the forms 7619, I 562, II 2418 (i.e., their numbers in the NGC or in the Frist and Second Index Catalogues), and with the omission of the qualifying letters NGC.

While many faint nebulae have been photographed which are not given in the NGC (see Appendix No 7), to be found in various published lists, the most comprehensive and homogeneous photographic catalogue of such NGC objects as can be reached from northern latitudes is doubtless that due to Reinmuth, with 6251 entries of NGC objects, a summary of the photographic work at Konigstuhl by Wolf, Reinmuth, Wirtz, and others<sup>2</sup>

There are already many thousand small nebulae listed that are not included in the NGC, and Hubbie has estimated that there may exist as many as 3 · 10' small and faint objects in the great group of the spirals (see ciph 36). The labor of observation and subsequent cataloguing adequate to a really complete

<sup>2</sup> Die Herschel-Nebel nach Aufnahmen der Königstuhlsternwarte, Publ Sternw Heidel-

berg 9 (1926)

<sup>&</sup>lt;sup>1</sup> J L E DREYER, A New General Catalogue of Nebulae and Clusters of Stars Mem RAS 49 (1888), Index Catalogue of Nebulae found in the Years 1888 to 1894, ibid 51 (1895), Second Index Catalogue of Nebulae and Clusters of Stars, containing Objects found in the Years 1895 to 1907, ibid 59 (1908)

Durchmustering of all such objects brighter than magnitude ca. 20 is so tremendous that it will doubtless be necessary to leave its completion to the centuries following our own. Even the systematic study and classification of the 25000 ± objects of present lists, as suggested by the Committee on Nebulae and Star Clusters of the International Astronomical Union (1925), demands international co-operation Λ new General Catalogue of Nebulae in the form of a card catalogue is being prepared by Lundmark at Upsala¹ and will be available for consultation by investigators. About 16000 cards have been written out, and it is expected that the complete catalogue will enumerate 35000 objects, publication is planned within the next few years.

A card catalogue which the author has compiled of literature relating to the nebular and allied fields since 1890, with the inclusion of older works of importance but with the omission of minor notes and papers of a purely general or popular nature, contains over 2000 entries. It is manifestly impossible, therefore, to aim at completeness in the bibliographical references quoted in treating this subject. In general, only a few of the more important references can be cited, and the names of numerous investigators must perforce be omitted

4. Classification and Units. A descriptive summary of the present status of the subject of the nebulae manifestly requires a less complicated and detailed system of classification than might be deemed necessary for the purposes of a catalogue. For this reason, the field is treated in this paper under its larger outlines. as follows:

The Diffuse Nebulae

- 1 Dark Nebulgo.
- 2. Comic Clouds
- 3 Lyminous Diffuse Nebulac

The Planetary Nebulae.

The Spirals

- 1 True Spirals.
- 2. Barred Spirals.
- 3. Elliptical and Globular Objects.
- 4. Magallanic Type Spirals

In Appendix No. 5 are collected a considerable number of systems of nebular classification which have been suggested or used by investigators of the field

There are some elements of inconsistency in all existing systems of classification, that of this treatment included. The genetic development of the field, largely through the influence of the Herschels and the NGC, which perforce combined in one catalogue all diffuse nebulae, planetaries, clusters, and spirals, has forced us into a somewhat illogical position as regards nomenclature and classification. There has never been any difficulty as to the sogregation of the clusters as a class, inasmuch as they are not nebulae at all. The spirals are likewise not nebulae, in the rigorous sense, yet these objects form the overwholming preponderance of all existing "nebular" catalogues. We are presented with the dilemma, on the one hand, of continuing to distort somewhat the true concept of bona-fide nebulous matter by calling them "spiral nebulae", "anagalactic nebulae", "extra-galactic nebulae", "non-galactic nebulae", "außergalaktische Nebel", and the like, or, on the other hand, of abandoning entiraly this lack of nomenclatural rigor forced upon us by the historical development of a field

<sup>1</sup> Publ A S P 42, p. 31 (1929)

The comparatively rare cases where emission lines have been detected in the spectra of spirals may doubtiess be adequately explained as due to the inclusion of true luminous nebuleaity. See ciph, 48.

in which the substantiation of the non-nebular character of the spirals is less

than fifteen years old

The author would personally prefer to use the term "galaxies" or "external galaxies", rather than the word "spirals" in describing these objects1, thus avoiding the partial inconsistency that no spiral structure is discernible with present resolution in the small elliptical and globular members of the class. The name "spiral" may, however, be regarded as a more or less satisfactory com-

A unit frequently used for the distances and dimensions of spirals in recent research literature is the parsec, which is the distance corresponding to a parallax of 1" This concept of distance is less familiar to investigators in allied fields of science, and the unit of distance employed throughout this treatment will be the light-year, abbreviated to Iy, and equal to 9,46 · 1012 km, or 5,87 1013 miles 1 parsec =  $3.26 \text{ ly} = 3.1 \text{ } 10^{13} \text{ km}.^2$ 

1 E g , H Shapley, Note on a Remote Cloud of Galaxies in Centaurus, Harv Bull 871, The Coma-Virgo Galaxies, I-VI, ibid, 865 to 869 and 873 (1929)

With an error of ca 8%, which is entirely negligible in comparison with the uncertainties of present cosmic data, the transfer from light-years to paraccs, or vice versa, may be made through the simple relations

$$D_{13}$$
 3/10 =  $D_{\text{parsees}}$   
 $D_{\text{parsees}}$  10/3 =  $D_{13}$ 

Of the equivalent methods of expressing the distance of a spiral, all of which may be found in the literature of the past decade

$$\tau = 0'',000\,0007$$
 $D = 1.4 \cdot 10^{0} \text{ parsecs}$ 
 $= 4.8 \cdot 10^{0} \text{ l y}$ 
 $= 4.5 \text{ A}$ 

the value in light-years has some advantages on the score of easy visualization

The added "historical" element involved in the use of the light-year as a measure of galactic distances is of great interest and value. Though the light-year was not used as a formal unit in his time, attention was perhaps first called to this point by Sir William

HERSCHEL (Coll Sc Papers 2, p 213)

a telescope with a power of penetrating into space, like my 40-feet one, has also, as it may be called, a power of penetrating into time past it may be proved, that when we look at Sirius, the rays which onter the eye cannot have been less than 6 years and 41/2 months coming from that star to the observer. Hence it follows, that when we see an object of the calculated distance at which one of the remote nebulae may still be perceived, the rays of light which convey its image to the eye, must have been more than nineteen hundred and ten thousand, that is, almost two millions of years on their way, and that, consequently, so many years ago, this object must already have had an existence in the sidereal heavens, in order to send out those rays by which we now perceive it"

The following short table gives a number of the units which have been used in ex-

pressing the enormous distances of other galaxies

```
= distance traversed by light in 1 year = 9,46 1017 cm
Light-year
                                    = distance for \pi = 1'' = 3.261 \text{ y} = 3.1 \cdot 10^{18} \text{ cm}
Parsec
Cubic parsec
                                    = 34,65 \text{ l.y}^3 = 2,9 10^{55} \text{ cm}^8
Kiloparsec
                                  = 10^8 parsecs = 3260 \text{ l.y}

= 10^8 parsecs = 3.26 \cdot 10^6 \text{ l y}
Megaparsec
Sternweite, Macron, Astron
                                    = parsec
Simometer
                                     = 10^6 \text{ astr units} = 15.81 \text{ y}
Siriusweite
                                     = distance for \pi = 0'', 2 = 16,31 \text{ y}
                                     = distance of Great Spiral in Andromeda, supposed to be
Andromede
                                            of the order of 1000 ly at the time this unit was
                                            suggested by VERY!
```

= an unnamed unit used by DE SITTER in recent papers A  $= 1.06 \cdot 10^{0} \, \text{ly} = 10^{21} \, \text{cm}$ 

## b) The Diffuse Nebulae.

**5.** Definition. The diffuse nebulae, which are rightly to be regarded as par excellence the actual nebulous elements of the cosmos, are irregular cloud-like formations (ex Lat nebula = cloud) of tremendous extent, of random and incheate structure, of the utmost tenuity, and composed of finely divided matter or matter in the atomic or molecular state.

In apparent size, they vary from small irregular patches or detached wisps to complicated structures of enormous extent and volume. Several of Herschel's regions of diffuse nebulosity cover over 7 square degrees, while the "North America" in Cygnus (7000) has an area of about 10 square degrees. There are even larger areas of very faint diffuse nebulosity in Orion, Taurus and Perseus¹ which must cover over 100 square degrees in their extreme dimensions

6. Number and Distribution. The diffuse nebulae are essentially and definitely galactic in distribution, and are rarely found at any considerable distance from the galactic plane. Save as possible constituents of other galaxies (see ciph. 48), all are apparently within the bounds of our own galactic system. They are, moreover, nearly always more or less closely associated with stars

While no accurate data are available as to the total number of the diffuse nebulae, it seems fairly certain that this total is not large, and that this class does not form 10% of existing nebular catalogues. One may conservatively estimate their number as roughly 1000.

CURTIS, in the Crossley Reflector program, sought to secure a photographic record of all NGC objects with the Horschellan characterization B or L; the program was otherwise at random. He photographed 56 diffuse nebulae, as against 513 spiral, from which may be deduced a total number of ca. 1000 objects in this class.

CHARLIER® plotted the galactic coordinates of 11 475 NGC entries (reproduced as Figure 29), excluding all objects known to be planetary, annular, clusters, or of stellar type. For the zone 30° in width between galactic latitudes +15° and -15°, he found that the number of nebulae per 25 square degrees was but 1,3, and the numbers in the zones at ±15° were twice as great as those at ±10°. As the diffuse nebulae are most frequently seen in low galactic latitudes, if the area of the Milky Way be taken at 10800 square degrees (probably excessive), one would expect only ca 560 such objects, to which total would be added the numbers of any diffuse nebulae lying farther from the galactic plane

HARDCASTLE'S counts of nebulae observed on the Franklin-Adams plates may be regarded as referring to the brighter objects of the entire sky. In this count there were tabulated:

Spiral or probably spiral				,		173
Riongated, spindle-thaped, oval		٠	٠			233
Diffuse		٠				51
Small, just distinguishable from	etar Imagos				_	327
Total						784

This proportion of 6,5% again points to the number of the diffuse nebulae as of the order of 1000. New objects of the class are occasionally discovered, and doubtless additions will be made in the future, but present photographic surveys of the Milky Way area are of such completeness that no large number of such accessions is to be expected.

<sup>&</sup>lt;sup>1</sup> Cl. Ross, Ap J 67, p. 280, Plates VI and VII (1928)

Lick Publ 13 (1918) Lund Modd (I) No 98 (1921) MN 74, p. 699 (1914)

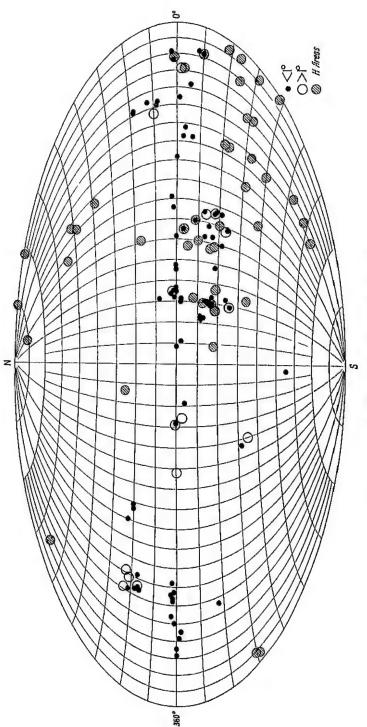


Fig 1 Galactic Distribution of Diffuse Nebulae

7. Physical Characteristics of Diffuse Nebulae. The spectral characteristics of nebulous matter will be treated later in ciph 15, 16 and 25, while reference will be made to the large body of theory based on quantum relationships as applied to the nebulosity of planetaries in ciph. 31 and 32 In the present section will be collected data referring more particularly to the mechanical attributes of such matter, even though it will occasionally be necessary to anticipate in part the conclusions of later sections.

The following subdivisions of the field seem clearly indicated

A Dark nobulas, see ciph 8.

B Cosmic Clouds (??), see ciph 9

C. Luminous diffuse nebulae

1 Showing emission spectra.

2. Exhibiting reflection or resonance effects

3 Variable in light

Not infrequently several of the sub-classes mentioned will occur in one and the same object. As to outward appearance, etc., the following characteristics may be noted:

- 1. Irregularity In general, there seems to be no such thing as a regular diffuse nebulosity, or one with clear-cut and sharp periphery. The pointed ends of certain fan-shaped nebulosities (see Figure 8; I 59) approach most closely to a definite boundary. In the great majority of cases, however, no sharp and clear-cut boundary can be made out in the random and irregular formations of the diffuse nebulae
- 2. An enormous variation in apparent luminosity. This range is very great; from objects like BARNARD 33 (see Figure 3), which are like a drop of ink by contrast with the brighter regions around, and which are non-luminous or, at best, very faintly luminous, to objects as bright as the Trapezium Region of the Great Nebula in Orion (see Figure 9), for which Wirtz<sup>1</sup> finds an areal brightness of magn. 7,76. His corresponding value for the central part of the Great Spiral in Andromeda is but 8,82.

Extreme tenuity. The really significant datum for any theory of the diffuse nebulae (and doubtless for the planetaries as well) is a density almost

vanishingly small (10- to 10- 10?)

The intimate alliance of luminous and dark matter in numerous diffuse nebulae leads one naturally to a theory postulating similar, or at least closely allied, constitution of the two sorts. Fluorescang or resonating molecules seem a reasonable hypothesis for the luminous diffuse nebulae, and this does not require the assumption of inordinate masses. If one postulates, however, a similar atomic or molecular condition for the matter in the dark diffuse nebulae, it is found that the density necessary to produce the amount of absorption observed requires "excessive" total masses.

While most of the evidence as to the extreme tenuity of diffuse nebulosity is of an indirect nature, it is somewhat surprising that one such line of evidence may be derived from a phenomenon within the solar system. As to the possible density of a swarm of fluorescing molecules, we have no very close analogies in other phenomena, yet the work of Schwarzschild and Kron<sup>®</sup> is very suggestive. In this brilliant piece of research, these authors determined the effective density of the matter within the tail of Halley's Comet on two assumptions, and from photographic data secured at Teneriffe with relatively small and inexpensive apparatus (two identical lenses of 2,5 cm. aperture, used extra-focally!). The

<sup>1</sup> Lund Modd (II) No 29 (1923).

<sup>1</sup> Ap J 34, p. 342 (1911)

second of these postulates assumes that the light in the tail of this comet is given off by fluorescing molecules with a radius of the order of 10<sup>-8</sup> cm. Though there is evident danger in comparing fluorescing molecules so different as may be their in a diffuse nebula and in a comet's tail, the analogy is illuminating and im not be rejected as an impossibility. For the density in the tail of Ilain, Comet, on this assumption, is 4 · 10-21.

Further induced evidence, pointing to densities vanishingly small, may be derived from mass limitations. We may assume for the distance of the torus Nebula in Orion a quantity of the order of 103 ly, a rough mean of the deter minations of several investigators. The tremendous diffuse nebulosity while fills most of the central portion of the constellation of Orion, of which the will known Trapezium Nebula (1976) is but a bright minor part, can scarcely contain less than 105 cubic ly (1058 cm 3) if at the distance adopted With a density of 10-24, the mass of the entire structure would then be about 10 · O. a very moderate total If, however, the effective density were as great as 10<sup>-15</sup>, the mass involved (ca 10<sup>10</sup> · O) would be so great as to dominate the gravitational motions of all

this portion of our galaxy

Allied with the subject of finely divided matter in a state of vanishing tenuity, the question of "stationary" or "inter-stellar" gaseous clouds should be briefly touched upon. There is manifestly a possible contradiction in any right correlation of two presumably different states of matter, even two different sorts of matter. For the inter-stellar clouds of this type are detected through the behavior of the lines of ionized calcium or sodium, whereas these have not yet been discovered in the spectra of either the diffuse or the planetary types. of nebulosity EDDINGTON, GERASIMOVIČ and STRUVE, and others have postulated the existence of uniformly distributed diffuse matter in inter-stellar space, with densities of 10-24 (EDDINGTON), or 10-26 (GERASIMOVIČ and STRUVI), and temperatures of 10000° to 15000° abs, as defined by the molecular species At such temperatures, while most of the Ca will be in the form Cail. there should be one part in 3000 of CaII, one part in 2 · 100 of NaI, and one part in 2.10° of Ca<sub>I</sub> It was calculated that this amount of Ca<sub>II</sub> should show absorption in a thickness of ca 3 1012 l.y This should theoretically show in all Main, though the strength of the stellar H and K lines of Ca makes it practically impossible to detect this in stars of types later than B5, unless the star is a limity of large range, or has a peculiar velocity of the order of 100 km/sec. There should also be a correlation between the distance of the star and the intensity of the absorption

PLASKETT and PEARCE<sup>4</sup> in a series of brilliant papers, have studied the behavior of the Ca<sub>H</sub> lines in a list of 261 stars of types earlier than B5, maily all of which are close to the galactic plane and within the Milky Way structur. The results are remarkable The speed and direction of the solar motion comes

[1928]

If uniformly distributed at the first density named, the total mass within a spheroidal

galaxy 10000 l.y thick and 60000 l y in diameter would be ca 6 ⋅ 10<sup>10</sup> ⊙

Throughout this treatment, in the interests of uniformity, ionization will be represented by the Roman numeral subscripts alone, that is, the designation for the spectrum only will

be employed, and we shall write, for example, On instead of O+++

<sup>&</sup>lt;sup>1</sup> Proc R S London 111, p 424 (1926), Ap J 69, p 7 (1929), 65, p 163 (1927); 67, p 151

Strictly speaking, Ca++ should be used for the state, and Cam for the spectrum corresponding to that state The subject is involved in a good deal of confusion at preunt on the nomenclatural side, there is a tendency on the part of some physicists to abandon the use of the + sign, and it seems probable that this will eventually be abandoned entirely, though there is as yet no international agreement on the subject

<sup>&</sup>lt;sup>4</sup> Publ Astroph Obs Victoria 2, p 335 (1924), M N 84, p 80 (1924), 90, p 243 (1934)

out practically the same as that determined from naked-eye stars in general, though the apex is displaced about 20° to the eastward. The K-term for these inter-stellar clouds is negligible. A rotational term, 7A, of 7,9 km/sec., seems indicated. Assuming for the factor A the value 0,0052 km/sec per ly., a center of gravity is found for the inter-stellar clouds at a distance of 1400 ly and in longitude 335°. This inter-stellar matter is found to be uniformly distributed, and the mean distance of the stars treated is twice that of the clouds.

For the dark clouds in Taurus, with apparent dimensions about 9°·3°, Pannekoek¹ derives a distance of 450 ly, giving an actual area covered about 20·60 ly. From probable assumptions as to the absorptive power of a gas, he finds that a gas would have to have a density of 10<sup>-15</sup> to produce an absorption of 2 magn. But with this density the total mass of the Taurus dark clouds would be 4·10°·O, which would be expected to have a marked effect upon the motions in this portion of the galaxy. Such a gaseous absorption would also be expected to exert some selective action on the spectra of stars observed through it, all of which leads Pannekoek to regard a cloud of material particles as the more probable state

C. Scharkn<sup>a</sup> has investigated the dark nebulae in Cepheus through an analysis of the spectral types of the stars in this region. He derives three dark nebulae at different distances: 1 absorption 0,3 magn., distance 810 l.y., 2. absorption 0,6 magn., distance 2500 l.y.; 3. absorption 1,5 magn., distance 2600 l.y.

The extended investigations of TRUMPLER and L. T. SLOCUM on absorptive matter in our galaxy should be mentioned here. Both authors find

a coefficient of absorption amounting to 0,0001 magn. per Ly

II. N. Russell's has investigated the theory that the dark nebulae consist of finely divided matter, i.e., fine "dust" In a cloud composed of spherical particles of radius r and density  $\varrho$ , distributed at random so that the average quantity per unit volume is d, the extinction of a ray of light in passing through such a cloud will be e stellar magnitudes per unit of distance, where e is given by the equation:

 $s = 0.814 \frac{qd}{q\tau}.$ 

In this equation, q is a factor introduced to take care of the variation when the particles are of dimensions comparable with the wave-length. It is nearly unity for particles larger than 2 to 3 wave-lengths, and a maximum, 2,56, when the circumference of the particle is 1,12 times the wave-length. For visual light the maximum opacity occurs when the radius of the particles is 0,086  $\mu$ , and a cloud of rock particles of this size and density 2,7 will exert an absorption of 1 magn. if it contains but 0,0116 mg./cm.\* in cross-section, regardless of its thickness.

RUSSKIL further suggests that this matter is repelled from the stars by radiation pressure, the giant stars being the main cause of such repulsion. The gravitational action of the cloud itself is regarded as the force which holds it together. An extinction of 10 magnitudes (quite sufficient for opacity) would

be produced by particles 144 \mu in diameter.

On Russell's highly reasonable theory, diffuse nebulae would be composed of two sorts of matter 1. actual minute particles which would provide for the opacity of the dark nebulae without the postulation of inordinately great masses, and, 2. Intermingled atomic or molecular matter which by reflection, resonance, or fluorescence produces the observed intrinsic luminosity. On this theory,

<sup>&</sup>lt;sup>1</sup> Amsterdam Proc 23, No. 5 (1920).

Ups Modd No. 50 (1930)
 Lick Bull 15, p 123 (1931).

Lick Bull 14, p. 154 (1930).
 Wash Nat Ac Proc 8, p 115 (1922).

BARNARD's dark spot in Ophiuchus, if 500 ly distant, would need to have a total mass only about equal to that of the sun See further ciph 8 and 42

8 Dark Nebulae<sup>1</sup> A very considerable number of areas of dark nebulosity or occulting matter have been observed in our own and in neighboring galaxies

Such dark nebulae are of the following modes of occurrence, though it is not maintained that these are necessarily a manifestation of the same phenomenon

1 Dark spots seen against the luminous background of large diffuse nebulae; type example 6523 (M8 Sagittarii)

2 Similar isolated spots seen against the background of the stars type

example, Barnard's Dark Nebula at 17h 57m, -27° 50'

3 Peripheral occulting matter surrounding masses of luminous diffuse nebulosity, as shown by diminution of star density, type examples, 7000 (America Nebula), the dark lanes extending from the nebulosity II 5146 about  $\varrho$  Ophruchi.

4 Larger areas of occulting matter as indicated by decreased density of

stellar distribution, of the references in the preceding Section

5 Calcium clouds in space, as evidenced by the behavior of the calcium lines in certain stellar spectia

6 In other galaxies, the evidences of peripheral occulting matter so frequently

seen in edgewise spirals, of ciph 42

Whether any of the numerous dark or obscuring nebulae are entirely non-luminous is an open question. It is quite possible that we have, throughout the class of the diffuse nebulae, a regular progression from objects giving no light whatever to objects of the intrinsic brightness of the Nebula in Orion, and that a division of the group into bright and dark objects is superfluous. These dark nebulae are best seen by contrast, set off and accentuated by the luminous background of the Milky Way or of bright nebulosity. In some of these cases it is possible that the apparent lack of all luminosity is only subjective, rather than real. Certain it is that Barnard has recorded the detection of exceedingly faint luminosity in most of the so-called "dark" nebulae.

In distribution, the dark nebulae, like the luminous members of the class,

are definitely galactic, as may be seen from Figure 2

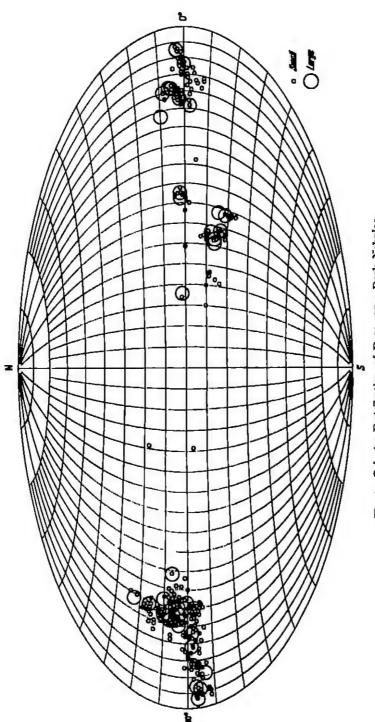
It seems certain also that we have to do with essentially the same sort of material in both cases, as is evidenced by the very frequent occurrence of the two sorts, luminous and non-luminous, in the same object

One of the most striking examples of this alliance is exhibited in the nebulosity south of  $\zeta$  Orionis<sup>2</sup> This remarkable region contains the bright diffuse nebulae 2023, 2024, I 431, I 432, and I 434, and the dark nebula BARNARD 33, which projects into and seems to be nearer than I 434. The main feature of this remarkable region is the long wisp-like diffuse nebula I 434, which extends for

<sup>2</sup> J C Duncan, Bright and Dark Nebulae near & Orionis Photographed with the 100-inch Hooker Telescope Ap J 53, p 392 (1921) Cf also, W II Pickering, Harv Ann 32, p 66, and Plate III, Fig 3 (1895), I Roberts, Ap J 17, p 74, with Plate IV (1903), M Wolf, M N 63, p 304, Plate 11 (1903), J E Kerler, Lick Publ 8, Plate XIII (1908), E E Barnard, Ap J 38, p 500, Plate XX, Fig 1 (1913), H D Curtis, Lick Publ 13, p 23, and

Plate II, Fig. 5 (1928)

<sup>&</sup>lt;sup>1</sup> E E BARNARD, On the Dark Markings of the Sky with a Catalogue of 182 such Objects Ap J 49, p 1, 360 (1919), Catalogue of 349 Dark Objects in the Sky Carn Inst Publ No 247 (1928), Ap J 31, p 8 (1910), 38, p 496 (1913), Pop Astr 23, p 596 (1915), W S FRANKS, M N 65, p 160 (1905), 90, p 326 (1930), T E Espin, Dark Structures in the Milky Way R A S Can 6, p 225 (1912), 16, p 218 (1925), Investigation of Star Gaps with a Catalogue of 202 such Areas, M Wolf, A N 161, p 130 (1903), 219, p 109 (1923), 223, p 89 (1925), M N 64, p 838 (1904), Seehger-Festschrift (1924), p 312; K Lundmark, Ups Medd 12 (1925), J G IIAGEN, A N 224, p 421 (1925) See also references under ciph 9, II Knox-Shaw, Obs 37, p 98 (1914)



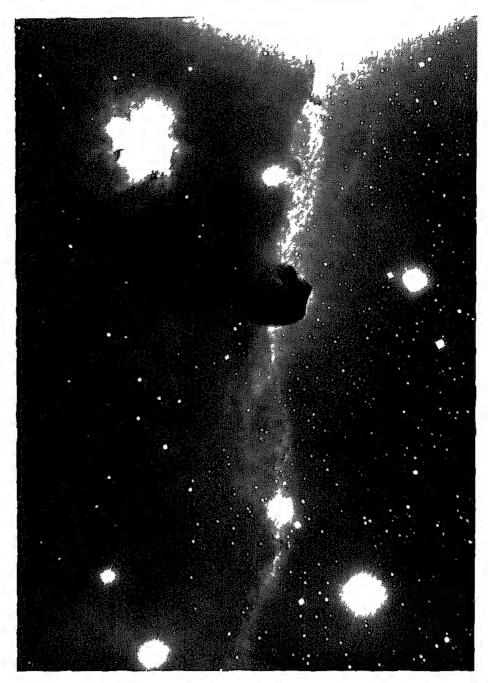


Fig. 3 Dark Nebula south of Zeta Oitonis (Barnard 33, near 1431) (Mt. Wilson graph)

nearly 1° to the south of  $\zeta$  Orionis. To the west of this is very faint, tex diffuse nebulosity and numerous faint stars, to the east lies a large area

nebulosity, with very few stars showing. From this dark area a "bay" about  $4' \cdot 5'$  juts across I 434 at a point about 30' south of  $\zeta$ , this is quite clear-cut and dark except for a small wisp in its northern portion, while the transition from dark to luminous matter is very abrupt at the western and southern edges, resombling nothing so much as a blot of ink. Even at these western and southern edges, however, the largest scale photographs show a very narrow rim of luminous nebulosity belonging to the dark "bay" rather than to I 434 beneath it

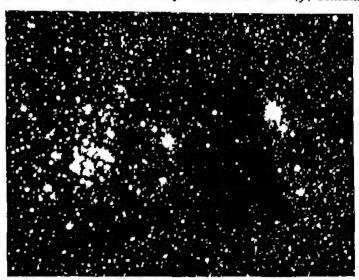


Fig. 4. The Dark Nobula Bannard 86 ( $\alpha = 17^{\circ} 57^{\circ}$ ,  $\delta = -27^{\circ} 50^{\circ}$ ) (Lick Photograph.)

Duncan suggests that four distinct types of diffuse nebulosity are exemplified here 1. the ropy, branching nebulosity of I 434, 2 the more compact nebulosity of 2024; 3. the nebulous stars 2023, I 431, 432 and 435; 4 dark nebulosity, best exemplified by Barnard 33 described above

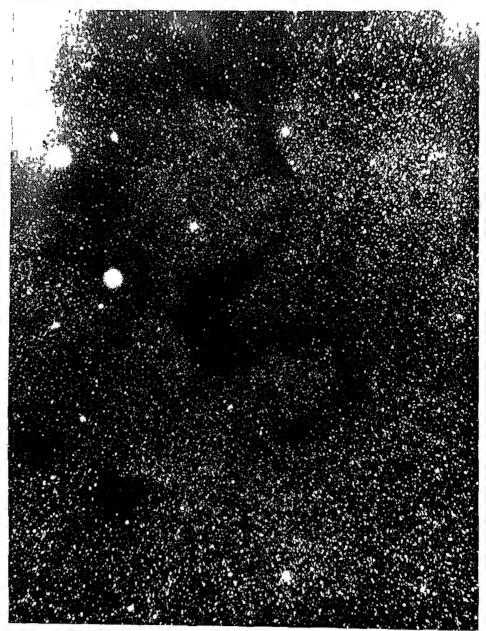
Numerous larger areas are known where occulting nebulosity is more or less clearly indicated. Among these may be mentioned the Northern "Coal Sack" (20<sup>h</sup> 56<sup>m</sup>, 4-51°30'); Barnard 144, described as a large, semi-vacant region 6°·3°, the area about 3° in diameter southeast of θ Ophiuchi (Barnard 78), where an exposure of two hours with the Crossley Reflector shows almost a stellar desert, or the region at 18<sup>h</sup> 55<sup>m</sup>, -37°, of which Knox-Shaw says<sup>1</sup>, "There are as many as twenty réseau spaces (each 5′ 5′) in which not a single star appears on a two hours' exposure with the reflector. These dark spaces are especially noteworthy as the region can not be said to be in the Milky Way, being 19° from the galactic plane and well away from the visible star clouds."

9. Cosmic Clouds. Vastly greater areas of slightly occulting dark matter or very feebly luminous nebulosity have been catalogued by HAGEN and his associates.

<sup>&</sup>lt;sup>1</sup> Holw Bull No 9 (1912)

<sup>8</sup> J G Hagen, A N 213, p 351, 214, p 449 (1921), 225, p 383 (1925), 227, p 391 (1926), A N Jub-Nr., p. 13 (1921), M N 81, p 449 (1921), Scientia (1922), p 185, Mem S A It (3) 1, p 9 (1920), Publ A S P 39, p. 167 (1925). Att Pont and Spec Vat persim (1922 and ff), G Aretti, Universo 9, No 4 (1928), shows that the Barnaed-Hagen idea of dark nebulae was anticipated by Seccili in 1877, F Becker, A N 223, p. 303 (1925), 225, p 129 (1925), 224, p. 113, 235 (1925), J. Hartmann, ibid 229, p 61 (1927), J Hopmann, ibid 238, p 285 (1930), W I' Rigge, Pop Astr 30, p. 203 (1924), J Stein, V J S 61, p 250 (1926), C. Wietz, A N 223, p 123 (1925); K Haidrich, Ibid 241, p 397 (1931)

to which he has given the name cosmic clouds. These areas are often very large, 30 to 50 square degrees, and certain parts of the sky are held to be



lug 5 The Dark Nebula BARNARD 72 (Yerkes Photograph)

almost completely covered by them Becker¹ gives in the final column of his General Catalogue the degrees of obscuration caused by obscure nebulae in the

<sup>1</sup> A Preparatory Catalogue for a Durchmusterung of Nebulae Spec Vat 13 (1928)

same field of view with the entry, on a scale of increasing density from I to VI. There are apparently none of the 4100 NGC entries in the main catalogue which are not affected in this way! This is regarded as confirming the fact that the cosmic clouds are not a galactic phenomenon. If one will refer to HAGEN's chart.



l'ig 6. The Diffuse Nebula NGC 6514 (Trifid) (Lick Photograph)

It will be found that in the portion of the lune bounded by  $\delta = +45^{\circ}$  to  $\delta = +90^{\circ}$ , and  $\alpha = 130^{\circ}$  to 230°, the area which Hagen holds to be covered by cosmic clouds is at least 75%, or about 3000 square degrees. These clouds seem actually to aliun the Milky Way, Hagen locates comparatively few in the Milky Way structure (cf. in this connection the chart of distribution of Barnard's dark nebulae, Figure 2)

<sup>1</sup> MN 71, p 434, Plato 9 (1921).

The status of the cosmic clouds postulated by 11 to 1 N is still (1931) in doubt He has pointed out that III RSCHI L's large areas of diffuse nebulosity (52 suc) were noted by Hirschier, but the number is 45, as 7 regions were counted twice coincide with certain of the cosmic clouds he has observed1

On the other hand, attempts to corroborate Hagen's results by photo graphy seem to have been uniformly unsuccessful. Hormann has supported these appearances by analogies drawn from the photography of laint nebular coming to the conclusion that the eye, in observing extended areas, has sensitivity about live magnitudes fainter than can be detected with a large reflector photographically (?)

HARIMANN, from some indications that the cosmic clouds may be actuall faintly brownish or reddish in color, has suggested the use of extremely rapi lenses plus a color-filter as a possible means of securing a photographic record Wiriz holds that these appearances are subjective, rather than objective, an represent in reality the contrast with the apparent brightness of the varior celestial backgrounds2 Ivanov3 failed to photograph the cosmic clouds note by H  $\kappa$  in and Bicklik in the regions of V and W Draconis, and R and S an

Патркиси describes in detail an extended series of attempts to photograp the cosmic clouds by means of plates hypersensitized in the green. He record tarking in all attempts save one, taken with an  $t=1/4.8~{
m Zerss}$  triplet of  $t04\,{
m mm}$ aperture, on which he believes he has secured a faint record. Numerous observe have felt that HAGIN's observations should be repeated by other investigator with other instruments, and in other climates! Some such corroboration scen indispensable before the cosmic clouds, of the number and extent assumed,  $\omega$ be regarded as completely substantiated

The Tartu counts of about 250000 stars to phot magn 14,5 on the Par Astrographic Charts<sup>5</sup> were at first thought to give a considerable measure of support to HAGEN'S results. In a belt 2° wide at \(\delta = \frac{121}{21}\) Optic catalogue 196 obscured regions. From these counts it was estimated that the entire sl would show some 14000 similar patches and that, were this obstructing materi removed, about five times as many stars would be visible in low galactic latitude

SHAPLEY® has remyestigated this question with plates of longer exposuon twenty-two of the Paris regions which had been employed in the Lartii count taken with the 21-inch and 16-inch refractors, and showing stars from one three magnitudes fainter than the Paris Charts. A real obscuring nebulosi should conceal such fainter stars much more effectively than would be the ca for magn 14,5. While left LUKK's counts to that magnitude were in all cas verified, and her localized vacancies and clusterings corroborated, it was four that the count to fainter stars in practically all cases obliterated such log megularities. On the Harvard plates covering the same regions as the twenty-ty selected Paris charts, seven clusterings and twenty eight obscinations we surveyed, together with the surrounding unaffected areas. When laint sta alone were considered, all of the clusterings and all but four of the obscuratio disappeared

Shapti  $\chi^7$  has secured similar negative results from the Harvard star comon the region of X (anci), reported by HAGLN\* to be surrounded by cosn clouds. Supply concludes from these results, as did Wiriz, that Habit

M N 86 five papers (1926), 87, p 1 (1927)
 A N 224, p 267 etc (1925)
 M V B M No S, p 57 (1927) <sup>1</sup> M N 86 live papers (1926), <sup>8</sup> M V B M No 8, p 57 (1927)

<sup>2</sup> A N 224, p 267 etc (1925) <sup>8</sup> M V B M No 8, p 57 (1927)

<sup>1</sup> e g, I undwark, Publ A S P 34, p 191 (1922), Hagi n's reply, ibid, p 321

<sup>6</sup> L Opik and Fel M I ukk, Publ Lattu (Dorpat) 26, No 2 (1921)

<sup>6</sup> Harv Circ 281 (1925) <sup>7</sup> Harv Bull 831 (1926) <sup>8</sup> A N 225, p 383

<sup>8</sup> A N 225, p 383 (192

cosmic clouds are apparently observable phenomena, but are merely the effects, in general, of the uneven distribution of the stars brighter than the fifteenth magnitude, and that, except in well-known nebulous regions near the Milky

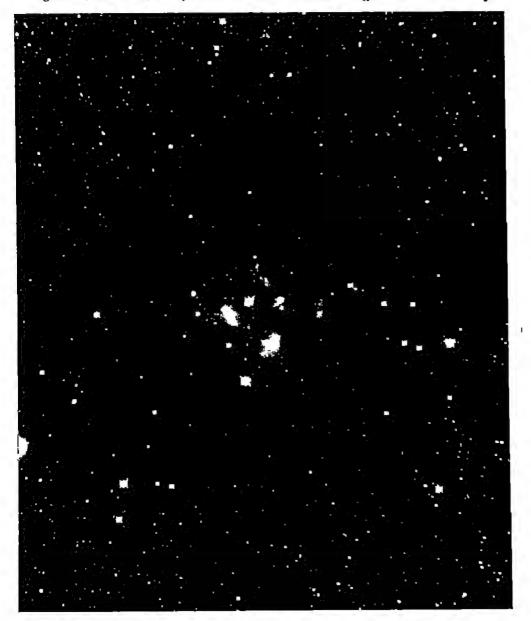


Fig 7 NGC II 5146 This object combines luminous and non-luminous diffuse nebulosity, shown clearly in its structure and in the marked falling off in the number of stars at its periphery (Mt Wilson Photograph)

Way, the obscurations suggested by the Tartu investigations are apparent rather than real.

10 Distances and Dimensions of Diffuse Nebulae Direct determinations of the distances of the diffuse nebulae by the parallax method are manifestly impossible because of the lack of sharp definition in the configurations of the



Fig 8 The Diffuse Nebula NGC I 59 (Northeast of γ Cassiopeiae) (Lick Photograph)

two main classes seen, irregular and texturcless clouds, or tangled masses of wisps and streamers. It is evident that the distances of these objects can only be derived by induced methods, and on the basis of more or less probable analogies or extrapolations. As the stars involved in such nebulosities have been found to be mainly of the earlier types, reasonable assumptions as to the average

distances of such stars of the given type and magnitude furnish an approximation to the distance of the nebula. Similar indirect evidence may be secured from star counts, in the case of dark nebulae, from the radial velocities and proper motions of involved stars, when available from involved variable stars<sup>1</sup>, etc.

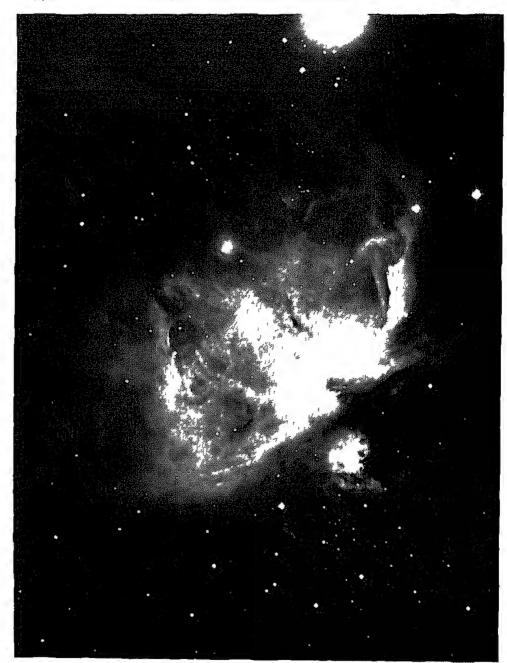
Variables in Diffuse Nebulae.

NGC	Number	Magn.	Discoverer
2264	20	14 (max.)	Wolf, AN 221, p. 379 (1924)
6514	3		1.AMPLAND, Pop Astr 27, p. 32 (1919); Publ ASP 33, p. 267 (1921)
6727	1	8,6-10,5	INNES, Union Circ 33 (1916)
7023	2	-	Perrine, Lick Bull 1, p. 187 (1902)
1 405	i	_	Harv Bull 786 (1923)

Table 1. Distances of Diffuse Nobulac.

NGC	٥	ð	Туре	Distance lul y.	Obs.
281	Oh 47m,4	+ 56° 3′	Diffuse	3600	L (LUNDMARK)
I 59	0 50 .7	60 11	Diffuse	250	L
II 1805	2 24 ,5	-61 3	Diffuse		L
I 348	3 38 ,2	- -31 31	Diffuse	350	GINGRICH
1 370	3 30 12	10- 3-			L
_	3 41	- -24	Pleiades	350	L
_	3 25	-1-28	Dark neb.	460	L
I 405	5 9 .7	-1-34 21	Star + neb.	2300	L
I 410	5 16	-1-33 23	Neb. + cl. + lane	1500	L
I 417	5 20	-+ 34 12	Ncb. + cl.	3200	L
2070	5 39 ,5	69 5	Diffuse	large	L
2070	5 30	- 5 27	Orion		L
	3 30	3 21		400	BERGSTRAND
				600	KAPTEYN
				1800	TRUMPLER
	( ) 7	-]-20 31	Diffuse	3600	L
2175	6 3 7		Neb. star	3200	L
I 446	6 25 3		Cl, - - diff. neb.	800	i.
2245	6 27 ,2		Cl. + neb.	1500	Ĺ
2237	6 27		Var. neb. + star	large	L
2261	6 33 17	-1- 8 49	Br. + dark neb.	3300	L
_	6 35 .5	-1- 6 59	Neb. star		1.
12° 2771	7 0 6	-12 11	n Carinae	2200	1.
	10 41 ,2	- 59 9	Ncb. + stars	1100	Ĺ
5189	13 26 4	-65 28	Dark neb. + star	550	l L
	16 14	19 59		460	L
r-	16 20	-25	ρ Oph, region Trifid neb.	550	L
6514	17 55 7	-23 2	Dark neb.	4000	L
-	17 55 ,1	-27 50	Diff. M8	1600	Î.
6523	17 58 4	-24 20	Dark neb. + star		Ĺ
	18 11	19 43	Dark neb. + stat	1600	ī
	18 9	18 15	Diffuse	3600	L
6618	18 15	-16 14	Dark nob. 4 star		L
	18 55	-10 52	Neb, region	400	L
-	18 55	-37 6	Dark nob.	650	L
-	19 14	+ 7 32	Dark neb	1300	L
	19 35	+10 20		1600	L
-	19 54	+34 30	Dark neb.	620	Ĺ
7000	20 50	- -44 0	Diff. (America)	560	Buch-Anderson
				220	DUNCAN
			Diff. I dowle	650	L
7023	21 0 ,5	+67 46	Diff. + dark	360	ī
_	21 35 ,0	+67 42	Neb. star	3600	L
-	21 35 ,9	+57 2	Br. + dark + cl.	3000	SCHALEN
7	22	+59	Copheus, dark	4100	L
7635	23 16 .5	+60 39	Nob. star	4100	12

LUDRNDORFF, Handbuch VI, Chap. 2, p. 243.



Lig 9 The Diffuse Nebula NGC 1976 (The Great Nebula in Orion) (Lick Photograph)

The approximate distances of a number of typical diffuse nebulae, both Iuminous and non-luminous, are given in the preceding table. Nearly all the values have been derived by Lundmark<sup>1</sup> by various induced methods, a few

<sup>1</sup> Publ ASP 34, p 40 (1922)

ave been added from other sources. The majority of the values given must

ne regarded as subject to very large uncertainties.

The actual dimensions of many of the larger diffuse nebulae must be neasured in tens or even hundreds of light-years. On the basis of the estimated listances given in the table above, 6523 (M8) will be about 11 Ly. long; the vmerica Nebula (7000) must extend over  $40 \pm {\rm Ly}$ .; the very large faint nebulosity in the constellation of Orion must be over 400 Ly. in diameter, etc.

11. Luminous Diffuse Nebulae. The salient characteristics of the diffuse rebulae: indefinite and random structure; extreme tenuity; general association with stars; and galactic distribution, have been noted in the preceding sections. In proceeding from such more mechanical qualities of structure and form to the acts of their constitution as exhibited by their spectra, the peculiarity is at once met that the diffuse luminous nebulae show two sorts of spectrum; one howing emission lines, and another sort resembling the spectra of the involved tars, ascribed to reflection or to some sort of resonance effect. This will necessitate a separate treatment.

There seems, furthermore, no reason to doubt that the spectra of the plantary nebulae and those of the diffuse nebulae which show bright lines are caused by the excitation of the same sorts of matter, for the most part in similar conditions is to density and ionization. This similarity has been well put by W. H. WRIGHT: "The spectra of the planetary nebulae differ much more among themselves than some of them do from the spectrum of the Orion Nebula. Whether or not the spectral similarity which exists between the planetaries on the one hand and the Drion Nebula on the other indicates approximate equality of physical constitution lepends upon the sensitiveness of the nebular spectrum as an index of the state of its source."

In spite of this similarity in the spectra of the two classes, however, it has been thought best, with the aim of segregating the pertinent data of each class, o treat the spectra of the diffuse nebulae and the planetaries separately. The mission spectra exhibited by certain of the diffuse nebulae will therefore be given in eight 45, and this matter will be repeated, with the addition of the cries relationships and ionization potentials assigned by Bowen, under the planetary nebulae in ciph. 25.

12. Proper Motions and Internal Motions (Visual). The older literature of the subject contains numerous references to researches attempting to show hanges or motions in the larger diffuse nebulae<sup>2</sup>. These attempts were based upon the often vague and inaccurate visual descriptions of earlier observers, and are now of value only as examples of energy and perseverance unfortunately lirected.

Though the advent of the photographic process has given a far greater degree of attainable precision, the available time interval is still far too short to establish motions larger than the unavoidably gross errors of measurement of the ill-defined wisps, streamers, or other structural features of the diffuse nebulae<sup>3</sup>. Aside from apparent changes due to light variations in a few variable diffuse nebulae, there seem to be no certain evidences of structural changes detected as yet. Lampland has pointed out that the intricate structure and

<sup>&</sup>lt;sup>1</sup> Lick Publ 13, p. 262 (1918).

<sup>&</sup>lt;sup>2</sup> c. g. E. S. HOLDEN, On the Proper Motion of the Trifid Nebula. Amer J Sc 34, p. 433 to 458 (1877).

<sup>3</sup> The classification of the "Crab" Nobula, 1952, is somewhat uncertain. The changes which Duncan has noted in this object will be described later in ciph. 27.

<sup>4</sup> Publ A S P 28, p. 192 (1916).

definite character of some of the delicate filaments in the diffuse nebula 6092 [the beautiful "Net-work Nebula" in Cygnus, cf. Lick Publ 8, Plate 63 (1908)]

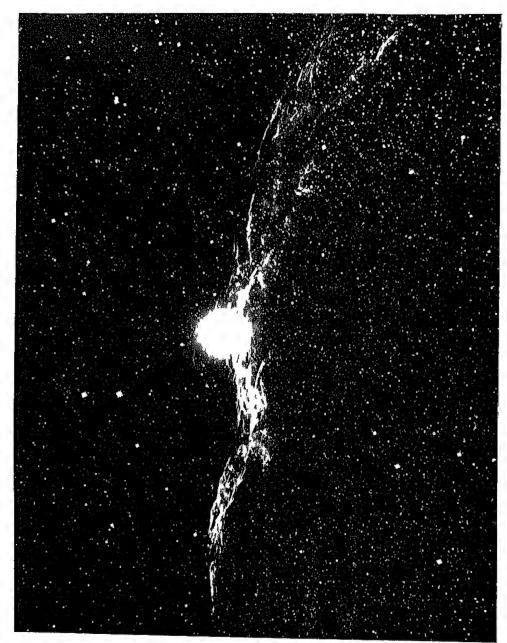


Fig 10 The Diffuse Nebula NGC 6990 in Cygnus (Mt Wilson Photograph)

should make it possible to detect comparatively small motions, and has studied two plates of this object separated by an interval of about 14 years. He states

that there are apparently elight displacements in small portions of some of the filaments in the southern part of this nebulosity. Duncan notes several new filaments found at the northern end of the "nebulous wreath in Cygnus"1 CURTISE made measures of features in 10 large diffuse nebulae on Crossley plates with a time interval of about fifteen years, with the conclusion, "the most that can be said, both from the measures and from careful examination, is that there has pretty certainly been no change in the intricate formations of these enormous objects as large as one second of arc during the past fifteen years".

18 Radial Velocities of Diffuse Nebulae Such of the lummous diffuse nebulae as have an emission spectrum, with much of the light concentrated in a few bright lines, are suitable for radial velocity determinations, unless too faint. a condition which unfortunately prevails. Observing the Nebula of Orion in 1872, Huggins determined the position of the chief nebular line as 5005 A. he attributed it to nitrogen, and ascribed its displacement as due to a recession of the Orion Nebula from the sun MAUNDER's attempts on the same nebulas showed variations too large to permit any definite conclusion

It remained for KERLER® to secure the first definite radial velocity results on nebulae. He employed a grating spectrograph attached to the 36-luch refractor at Lick Observatory, using the third or fourth order. He determined the radial velocities of the Orion Nebula and of thirteen planetaries. When it is recalled that this was done visually, in the "prehistoric" days of the spectroscopic method, and that his values are in close accord with later spectrographic results, his achievements in this field must be regarded as an observational triumph (on Orion Kirkler, -+17.7 km./sec , CAMPBELL and MOORE, -+17.5 km./sec )

Very few radial velocities are known for diffuse nebulae. From the descriptions, 5 nebulae in the Greater Magellanic Cloud may possibly be of the diffuse type, these have the mean velocity of the Cloud, +- 276 km/sec. Others are

	Object	I' (am's motion renoved	
Orlon		0,1 km /sec	
3372	y Carinno	<u> </u>	
6514	(1 rifid Nebula)	+21	
6523	(MR Sagitturii) .	-1 8	
	(Horseshoe Nob )	4 20.7	

14. Turbulence Effects in Diffuse Nebulae. Although radial velocities are known for but a few diffuse nebulae, in one case we possess fairly accurate knowledge of the relative motions of different portions of the same nebula, that of Orion Kerler (loc cit ) had earlier considered the question of relative radial velocity in different parts of the Orion Nebula, but obtained negative results He estimated that differential radial volocities as great as 8 km /sec, in the brighter parts of the nebula would have been detected Vogar, and EBERHARD? found evidences of differential velocities in the Orlon Nebula, indicating that the radial volocities of the material east of  $\theta_1$  Orionts was 5 or 6 km/sec larger in the positive sense than that of the material 0',6 west of this star,

<sup>1</sup> Mt Wilson Year Book No 29 (1930)

Proc R S London 20, p 383 (1872) Groenwich Spectr and Phot, Results (1884 and 1887)

H D CURTE, Proper Motions of the Nebulae Publ ASP 27, p 214 (1915) In all, CURTE made measures on 150 objects of the various classes, based on Crossley negatives with time intervals averaging about 15 years. Cuntis is since convinced that the probable errors of measurement on such vague and diffuse elements or nebulous nuclei are vastly larger than the quantities sought. He therefore now regards the numerical results derived in his paper as meaningless, and relegates them to the status of the older visual comparisons

Lick Publ 3, p 165 (1894)
CAMPDELL and MOORE, Lick Publ 13, p 77 (1918) \* Ap J 15. p 307 (1902).

Our modern results on this nebula are due to the brilliant application of the interferometric method by Buisson, Fabry and Bourger and to the detailed and accurate spectrographic survey of the Orion Nebula by CAMPHELL and MOORE 2.

The French investigators, with high technical skill, made use of an interferometer with a preliminary telescopic magnification (80 ×), so that the resulting interference rings formed a picture of the chosen region, an area about 4' square about the Trapezium. Measurement of the diameters of the interference rings will then give, first, the mean radial velocity of the nebula as a whole by using some known radiation as  $H_{\gamma}$ ; secondly, variations in different diameters of a given ring of known (or unknown) source give at once the relative radial velocities of the portions of the nebula covered by this ring; and, finally, certain assumed laws connecting the limiting order of interference with the atomic mass and the absolute temperature make an estimate possible as to the effective temperature of the nebular matter,

The authors measured 58 points on the interference rings, distributed in 12 directions from the Trapezium, and within a radius of about 2'; their resulting mean value for the radial velocity of the Orion Nebula was +15,5 km./sec.

As to the turbulence effects observed, they write: "The rings show local deformations in certain regions, indicating, in certain portions of the nebula covering a very small area, irregularities of speed which may amount to about 10 km./sec. Movements of this sort are manifested in the region to the southeast of the Trapezium in the direction of the star Bond 685. Moreover, there are great collective movements; with respect to the mean velocity, the northeast region is withdrawing at a speed of something like 5 km./sec., while the southwest region is approaching at pretty nearly the same speed. In general, the part of the nebula which we have studied has a sort of rotary movement about a line southeast-northwest, but with numerous irregularities."

15 plates were taken, with étalon separations ranging from 0,13 to 2,8 mm. The final values found for the wave-lengths of the chief violet nebular lines are:

> 3726,100 A 3728,838 A.

Next, by the use of the formula,

 $N = 1.22 \cdot 10^6 \sqrt{m/T}$ .

where N is the limiting order of interference, m the atomic mass, and T the absolute temperatures, and through the use of étalons of gradually increasing separation, they set the limiting orders of interference as follows:

Hydrogen . . . . . . . . . . . . about 10000 "Nebulium". . .

This value of the interference limit was regarded as indicating a source of atomic mass about 3 as the origin of the "nebulium" lines. Also, by the use of the same formula, a high effective temperature, in the sense of molecular motions involved, was derived, amounting to 15000° abs.

This empirical formula should not be taken too seriously, as is indicated by its failure In this case; the atomic mass of O is 8.

The formula in question was derived by Schönrock, Ann d Phys (4) 20, p. 995 (1906), and later, with a slightly different constant, by RAYLEIGH, Phil Mag (6) 29, p. 274 (1915). It involves, in the latter case, a postulated intensity difference of 1/40 (2,5%) as the minimum detectable in the formation of an interference ring. Though in no sense a rigorous formula, the temperatures found are probably of the right order.

<sup>&</sup>lt;sup>1</sup> Ap J 40, p. 241 (1914); cf. also ibid., 33, p. 406 (1911).
<sup>2</sup> Llck Publ 13, p. 96 (1918).

The researches of CAMPBELL and Moore confirmed the results secured by the interferometric method in most respects, but did not support the idea of a general rotation. In all, 86 spectrograms were taken, and the total of the exposures amounted to nearly 400 hours. In an area 2' square about the Trapezium they found a total velocity range of 13,5 km./sec., and interesting plates are given in the work quoted, tabulating the excess or deficiency of radial velocity at the numerous points observed in the nebula. "...a consideration of the charted velocities, especially those in the outer southwestern areas, seems to negative the suggestion of a rotation of the nebula. While the intermediate region from

1' to 4' northwest, west, and southwest of the Trapezium is a region of prevailingly low radial velocities, moderately low radial velocities are to be found also to the northeast, east, and south of the Trapezium . . . but when we consider all parts of the nebula covered by our observations, we are inclined to favor the hypothesis of great collective variations of velocity rather than a rotation as the prevailing factor," Widening of the lines in certain regions suggests that the radiations in such areas may be coming from widely different depths in the nebula, the different strata having different radial velocities. See further ciph. 16 and 28.

15. Luminosity of the Diffuse Nebulae: Gaseous Spectra. A considerable number of the diffuse nebulae exhibit an emission spectrum of the type associated with matter in a gaseous condition. The type example of this class is the Great Nebula in Orion: because of its intrin-

Table 2. Wave-lengths of Lines in the Orion Nebula (WRIGHT).

Mehura (vocani).						
¥(1 V)	Intensity	Origin				
3704	2	## 3703,9; He 3705				
3712,4	1	Hr = 3712,0				
3722	2	$II\mu = 3721.0$				
3726,16	40	On; B., F. & B., 3726,100				
3728,91	30	O <sub>II</sub> ; B., F. & B., 3728,838				
3734	2	H2, 3734,4				
3750	3	117 3750,2				
3771	6	Hr 3770,6				
3798	10	110 3797,9				
3820	1	He <sub>1</sub> 3819,6				
3835,5	1.5	$H\eta$ 3835,42				
3868,74	40	Unidentified				
3888,96	40	<i>Πζ</i> 3889,05; He 3888,64				
3964,8	10	He <sub>1</sub> 3964,7				
3967,51	30	Unidentified				
3970,08	40	H <sub>8</sub> 3970,07				
4026,2	10	Heir; Her 4026,2				
4068,62	5	$  \mathbf{S}_{\Pi}  $				
4076,22	2	$S_{II}$				
4101,74	60	<sub>1</sub> Hδ 4101,74				
4120,6	1	110, 4120,8				
4144,0	1	He <sub>1</sub> 4143.7				
4267.1	1	C <sub>II</sub> 4267,14				
4340,46	100	$  H_{Y}   4340,47$				
4353	1	Unidentified				
4363,21	6	O <sub>III</sub>				
4388,0	4	He <sub>1</sub> 4388,0				
4471,54	20	11e <sub>1</sub> 4471,49				
4658,2	2	Unidentified				
4712,6	1	1Ie <sub>1</sub> 4713,2				
4861,32	70	<i>Πβ</i> 4861,33				
4022,2	1	He <sub>1</sub> 4921,9				
4958,91	50	Om				
5000,84	70	O <sub>111</sub>				
5876	_	J-1e <sub>1</sub>				
6563		$ I\alpha $				

sic brightness, the spectrum of this nebula has been more studied than any other, just as it was the first diffuse nebula in which bright lines were observed visually and later photographed.

In the preceding table are given the lines observed in the Orion Nebula by WRIGHT<sup>1</sup>, Additions to the identifications have been made from Bowen's papers.

<sup>&</sup>lt;sup>1</sup> The Wave-lengths of the Nebular Lines and General Observations of the Spectra of the Gaseous Nebulae. Lick Publ 13, p. 191—239, with many plates (1918). This monograph is the most complete collection of observational data on the gaseous nebular spectrum existing.

These lines will be found also, with the addition of numerous others found in the planetaries, and with screes relationships and ionization potentials, in Table 7.

ciph 25

The lines at 5007 A and 4959 A have had a long and interesting history under their older designations,  $N_1$  and  $N_2$  for which the hypothetical source "nebulium" was postulated. The identification of these and other formerly unknown lines in the spectrum of the gaseous nebulae as multiply tomzed O and  $\tilde{N}$ 15 due to Bowi Nt

It will be seen from the identifications in Table 2 that the more prominent features of the emission spectrum of gaseous diffuse nebulae are  $H_1$ ,  $H_{c_1}$ ,  $O_{H_2}$ and  $O_{III}$  A single weak line, 4267 A, is ascribed to C, and two are possibly  $S_{II}$ Although  $H\alpha$  is visible in Otion, the two lines of  $N_{\rm H}$ , 6548 and 6854 A, so prominent in many planetaires, as well as the weaker lines of  $N_{\rm HI}$  at 4634 A and 4644 A, are not found. The puzzle which had been presented for so many years; by "nebulium" has thus been almost completely solved by Bowen. Of the stronger lines, only the two at 3869 A, intensity 40, and 3968 A, intensity 30, remain unidentified

Hubbi E<sup>2</sup> tabulates the following twenty-nine diffuse nebulae with emission spectrum, only thateen of which were known as such before

Table 3 Diffuse Nebulae with Emission Spectra (Hubber)

Number	Pv m	agn and stars by	l spectru volved	ni of	kemaks
28 t	8,6	10,2 11,6	Oc   B0		4 components of BD 1 55 191
I 59	1		{		ban nebulae near y Cass
1491	10	),6	130		,
1199					}
1621	,	14,0	Oe	,	3 st, magnitudes estimated
T 405	] :	5,8	Bo	b	Boss 1249,   faint continuous
1952		<b>&gt;</b> 0	1	Bo	Also strong continuous
1972	5.1	, <b>7,</b> 9 ,8	Bi		Orion 4-st in Trapezium   Bond 734
I 131	,	1,43	131	1,	Bay neb near a Octobis
202	1		Į.		Also faint continuous
2175	1 2	7,5	Ou	5	BD   20' 1281
2237	7.1		[ Oe	•	1 brightest st of cluster
	1		-		Union Circ No. 7 (1911)
2359	11	1,0	Od		Magn estimated
3372			1		
5128	1				
6302	1		1		
6357 6511	7.8	8,5	Oes	120	1
6523	6.1	6,9	()(5		Trifid 2 comp of BD 23°338 2 brightest st m M8
6611	8,3	9.3	i O(5	Bo	3 brightest st in M16
6618	1 ",	214	1		, magnitude in the major
6888			]		
6960	11		)	Į	f 1
6922	13		1		I normous loop in Cygnus
7000	1			[	America uch Cf also Wort Sitzh Heidelb Akad, Abt 27
7635			1	(	(1910)

<sup>&</sup>lt;sup>1</sup> J. S. HOWPN, Nature 120, p. 173 (1927), 123, p. 150 (1929), Publ A S P 39, p. 295

<sup>(1927),</sup> Ap J 67, p t (1928)

2 The Diffuse Galactic Nebulae Ap J 56, p 162 (1922), Mt Wilson Court No 241 (1922). This is the most comprehensive monograph on the diffuse nebular which has appeared to date,

16. Emission Variations. The relative intensities of the lines in gaseous nebular spectra, whether of the diffuse or planetary types, vary in a very striking and puzzling manner, not only in different objects of the same class, but also in different portions of the same object. The Orion Nebula is the most striking example of this phenomenon among the diffuse nebulae.

This variation in the relative intensities of nebular emission lines is a problem which has yet received no entirely satisfactory explanation (see, however, ciph 28, 31, and 32). It is conceivably in some way connected with variations in the extremely low densities of these objects or of parts of the same object, as in Orion. Modern physics can parallel the enormous temperatures of stars (Andreson's exploding wires), or temperatures near the absolute zero (ca. 1° K.), it can also deal with relatively high pressures. It is unfortunate that the gases occluded from the walls of our laboratory apparatus, as well as the great length of the mean free path, limit us to rarefactions whose ultimate tenuity is perhaps of the order of 10. If, and that the presumably very fertile experimental field in densities less than this by factors of the order of 10. If seems forever closed to us. Our stellar and nebular laboratories will long remain our only source of ionization phenomenon in gases of densities vanishingly small.

CAMPBELL and MOORE (loc cit), in their work on Orion, have tabulated a great variety of ratios for the intensities of the  $N_1$ ,  $N_2$ , and  $H\beta$  lines, ranging from  $N_1$ ,  $N_3$ ,  $H\beta = 10$ , 3,5 for the center of the Trapezium region to 0,0,10 in the neighborhood of the detached nebulosity 1982 in the northeast quadrant, whereas the normal ratio in the planetaries is 10,3,4. Campbell and Moore, and Wilson, in the work quoted give also the values for the following five objects.

NGC	$N_1$	N.	11/4	YIK	$N_1$	$N_{\bullet}$	$n\mu$
1976	10	3	5	(1523	3	1	40
1372	10	1	5	6618	10	3	5
6514	3	1	10				

HUBBIR adds data for 12 others

NIL	$N_1 + N_2$	IIA	Nec	$N_1 \mid N_1$	118
1499	1	2	6611	1	3
1 423	1	1	6888	O	2
1 434	0	5	6960 ]		2
2024	1	3	6992	U	4
2175	1	3	7000	0	2
2237	2	1	7635	O	5
E424	(1	2			

Kerier took perhaps the earliest photographs of the Orion Nebula through a color screen, and found  $N_1$  and  $N_2$  concentrated in the Huygenian region Hartmann, by a similar method, corroborated these results, and noted that 3727 A was of much greater extent Slipher worked spectrographically over a large part of the more distant nebulous regions in the constellation of Orion, in general confirmation of Campbell's earlier visual observations, and found that the emission lines decreased in strength till out at NGC 2068 the spectrum was continuous. ". then the variation in the spectrum may be said to begin

<sup>&</sup>lt;sup>1</sup> CAMPBELI'S discovery of this effect in different areas of the Orion Nobula, and Schrimen's attempts to disprove, formed an interesting and lively tilt of the carlier days of the spectracopic method Cf J Schrimen, V J S (1897), p. 51, Ap J 7 (1898), C Runge, lbkl 8, p 32 (1899), CAMPBEL, WRIGHT, SCHARBERLE, and ATTERN, lbkl 6, p 363 (1897), W W CAMPBELJ, lbkl 8, p 317 (1899), 9, p 312 (1899)

W W CAMPIREL, lbkl 8, p 317 (1899), 9, p 312 (1899)
Ap J 9, p 133 (1899)
Ap J 21, p 389 (1905)

<sup>4</sup> Publ A S P 31, p 212 (1919)

in the center with the usual emission type which loses strength (different substances differently) with distance outward and ends finally, in the most distant masses, with a continuous spectrum of the normal stellar absorption type" Wright (1921, unpublished) using a quarz shiless spectrograph attached to the Crossley Reflector, found the relative sizes of the monochromatic images  $H_{V_1}H_{\beta} > N_{1,2}$  The latest determination of variations of state or constitution of the Orion Nebula, made with powerful apparatus (a large objective prism), has been carried out by W J 5 Lockyfr. The outstanding feature of Lockylr's plates is the great size of the image due to 3727 A, next in size are  $H\beta$  and  $H\gamma$ , following these in order of size come 5007 A, 1959 A, and 3869 A, which is the smallest of all. The radiation from the Huygeman region is found to be composed almost entirely of hydrogen and  $N_1$  and  $N_2$ , the Messierian branch contains these elements plus 3727 A, the outlying regions are composed almost entirely of 3727 A. Similar interesting variations are noted in the planetaries (see ciph 28), and have formed the basis of the quantum state theories of these objects

17. Luminosity of the Diffuse Nebulae Reflection or Resonance Effects. A relatively large proportion of the diffuse nebulae fail to show any emission lines whatever, or show them at best very faintly upon a background of relatively strong continuous and absorption spectrum. As nebulae with an emission spectrum are more easily identified than those with a continuous spectrum, if of the same surface brightness, Hubbit regards it as probable that diffuse nebulae with continuous spectrum are actually more numerous than those with bright lines. He catalogues 33 diffuse nebulae with continuous spectrum, of which but 8 were known earlier. See Table 4

Table 4 Diffuse Nebulae with Continuous Spectra (Hobbit)

Number	Py migh and spi involv	elrum of stars ed	Remaks
1333 I 318 Pleades	10,6 8,4 9,8- 10,6	138 136 138—A2 135	BD   31°643 involved 9 stars   Maia and Merope "The whole spectrum   is a true copy of that of the brighter   stars of the Plejades" (Stiem R, Lowell   Bull 2, p. 26 (1912))
Brown.		_	α [h 11th, δ - 28° 2'
•	12,5	IV8	$\alpha = \frac{1}{122}$ , 1, $\delta = \frac{1}{124}$ ° 32′ Star is probably a dwarf
1579 H 2087	12,0 12,2	\0 -B5	2 stars
1788	10,0 13,0	B8	2 stars
11 2118	_	-	Great neb n p Rigel
1977	16	131	BOSS 1364 STIPHER [Publ A S P 31 p 214 (1919)] finds spectrum continuous, crossed by a few bright H lines, On absent
2023	7,8	132	Neb around BD - 2 1345
2068	10,1 -10 8	B5-B8	BD FO° 1177 STIPLER (LC) finds no bi lines Spectrum continuous, crossed by II and He absorption, the former series strong the latter weak, as in advanced B type stars
-		- 	$1 \alpha = 5^h 45^m$ , $5$ , $\delta = +1^o$ Brightest portion of great "spiral" in Orion

<sup>1</sup> M N 90, p 580 (1930)

(Continued.)

Number	Pv. magn. and sp invol		Remarks
2183	14,0	133	
•	1,3,5	131	Bright uncatalogued "comet" neb, $\alpha = 6^6 3^m$ , $\delta = 4.18^\circ 42'$ .
1 - 446	11,3	131	
1 447	8,1	. 131	BD 108 1159.
2245	10,7	131	Bright IIB suspected.
2247	8,8	B2p	Bright $H\beta$ and $H\gamma$ .
2261	var,	Peĉ.	Approximates a nova spectrum Cl Stipmer, Lowell Bull 3, p. 63 (1918)
	8,2	BI	Uncatalogued neb. about BD 12"1771
	3,1	132	Nebulosity about $\pi$ Scorpil.
11 5592	4,2	132	Nebulosity about r Scorpii-
4601	7.1 8,4	138 Ao	4 stars.
4603	7.8	132	Neb. about BD - 24"12684.
4604	5,2 - 5,0	B2- B3	2 components of ρ Ophiuchi. Stipites Lowell Bull 2, p. 155 (1916), finds spec trum continuous and probably like tha of ρ.
4605	4,9	B3	Neb. about 22 Scorpii.
6726	7,2 9,4	139	Neb. about BD 37" 13023- 4.
0727	()		
6729	var,	Gp }	R Cor Austr; resembles T Tauri. Sы рива, Lowell Bull 3, p. 66 (1948), find weak emission on strong continuous
6914	0,3 -9,0	135	BD -  41"3731 and 3737.
7023	7,2	132p	Prase, Publ A S P 27, p. 240 (1915) finds strong continuous crossed by absorption lines. Stapmer, ibid. 30 p. 63 (1918), finds 11 and 11e absorption H emission, which is strong in H and apparently identical with the stap inbedded in the nebula.
7120	10,2 12,4	B3- B8	3 stars,
11 5146	10,0	131	BD +46"3474.

The positions given in Tables 3 and 4 are for 1920,0. For data and deductions summarizing the character of the stars involved, see ciph. 19.

18. Variable Diffuse Nebulae. A few diffuse nebulae are definitely known to be variable.

These comparatively rare examples of variable nebulae are of great theoretical interest, and have certain characteristics in common:

- 4. Nearly all are fan-shaped, with a variable or suspected variable at the tip (in T Tauri the star is slightly removed from the tip of the fan).
- 2. All seem to lie in dark lanes or gaps, presumably filled with non-luminous matter.
- 3. No certain correlation has yet been derived between the stellar and the nebular variation<sup>1</sup>.
- 4. The example most thoroughly studied, Hubble's variable nebula, shows no actual outward or other movement of formations.

The irregular and hap-hazard character of the variations in these objects, and the lack of correlation with variations in the involved stars, seem to negative any explanation involving the lighting up of successive regions outward by light pulses from the star. The dimming of the structural features by passing clouds

<sup>&</sup>lt;sup>1</sup> LAMPLAND, however, states in his last paper that 2261 is generally faint at times when the star is faintest.

Viriable Diffuse Nebulac

Number	1	ð	Description
15.5	f <sup>h</sup> 16 <sup>m</sup> ,1	[9 17'	Histos variable nebula near the variable for 1 for (Md.) bright lines). Conspicuou in 4570 this nebul has been very funt since 1000. I other observator discussed by BALNANA ALNAS p. 112 (450.1) of p. o. (1895). 59. p. 572 (1899). Sketch und de cription by Prvst. Vp.] (5.5. p. 89. (1917). No paralleli urchi decin established between the variation of the tribula nebula. Situated in a dayk lim.
2215	6 27 ,2		Bright for shaped in isocytending to strom in apparently stellar nuclei. 5% of little structural details for in a dark lane. Viriation suspected by Privat MCWilliam Contr. No. 186 (1996).
2261	6 53 7	S   19	Hubbit s variable behala a bright tan begin free about 2' 1' extending to the noof the variable R Memora Be (9,5-13'). Hubbit s plates how no variation in the nucleus, and he found strong continuous position. Ap J. H. p. 100 (1917). Is p. 351 (1917). Strong Lowell Bull 5, p. 60 (1918) with mexposure of 4, hour found a spectrum stikingly in embling that of a nove of also Ap J. 20. p. 198 (1909). By p. 36 (1911).  LAMPIAND in Pop Asti 26 p. 149 (1918) 17, p. 81 (1919). 29, p. 632 (1921), 34 p. 624 (1926), and in the late of paper (abstract) in Publ A. S. P. 45 p. 200 (1931). The the results of a study of several hundred plate. Liken with the 12 inch is flector. While all parts of the mobils are subject to variation, there is no outward movement of the parts, which evidently him by reflected to locally engendered light. The appropriate displacement and motions of parts of the structure recyclently only apparent. Verlags and obsernation processive displacements of boundaries of the expectant progressive displacements of boundaries of the expectant progressive displacements of boundaries of the expectant bright of the correspondence of described as periodic that there are recording No correlation has been found between the light variations of the nucleus and that of the incline treating of affection has been found between the light variations of the nucleus and that of the incline treating of affection has been found between the light variations of the nucleus and that of the incline treating of affection has been found between the light variations of the nucleus and that of the incline treating of affection has been found between the light variations of the nucleus and that of the incline its factor.
3172	10 11 ,2	59 9	Nebulosity about $\eta$ (armae Larly discussion with regard to suspected variability of three object (from visual descriptions only) to be found precent in M \\ 31, 32, 34, and 36. Not confirmed by modern photographs
6511	17 56 ,3	23 2	The Trifid Nebula A Highlity Suggested to Leave
6729	18 55 ,2	37 6	Pop Astr 20, p. 631 (1920). Dark matter involved settling is variable nebula discovered by him at Athens in 1861, a fan shapedwip with the variable R Cor North at the tip, and lying in a pronounced dark region. The star varies [arregulary from ca magn. (1,5 to 1 x s. (Hav. Bull 805 (1921)). Stripin R, I owell bull 3. p. 66 (1918) in a 20 hour exposure, found spectrum of novaetype. No ecitam correlation between a unation of dar und of nebulosity. Cf. also, KNON ShAW. He has Bull 4. p. 341 (1915). I, p. 482, with plates, (1920). No dar (1914). Innis, Union Che. No. 33, p. 266 (1916). No. 36, p. 285 (1916). Lampand. Pop Astr 25, p. 659 (1917).

of occulting matter, quite heterogeneous as to density, has been suggested, and derives some measure of support from the location of these nebulae in dark lanes or gaps

A theory put forward with some hesitation by Lampland would ascribe the irregular variations in the nebular luminosity to a luminescence or fluorescence engendered by the passage of the body through clouds of non-luminous matter. This, also, is supported by the inflicit in which such nebulae are found. There are some very strong objections to such an explanation. 2261 seems to have remained unchanged in structure during all the period through which it has been observed. The theory would then require a density in such dark clouds vastly less than that of the luminous matter itself (10<sup>-24</sup>?), else this would be changed in configuration or even swept completely away by the passage of the non-luminous matter through its structure. Further work is urgently needed on the spectrum and light variation of the involved stars, as well as on changes in the nebulosity, before a satisfactory theory can be derived for these interesting objects.

19. Evolutionary Status of the Diffuse Nebulae. No definite decision can as yet be given as to the precise evolutionary position of the diffuse nebulae Without any precise formulation of the successive steps of the process, and by tacit analogy with early or later forms of the now discredited Kant-Laplace nebular hypothesis, it has long been customary to regard the diffuse nebulae as the first step in the evolutionary process which has formed the stars. Man's mind demands a logical sequence in such an evolutionary process, and it is possible that the insistence of this demand occasionally blinds us to the fact that the "logic" of the process may have been injected from our own laws of thought, or by fallacious analogy with totally unalled developmental gamuts. Provided, however, that we cast uside all somewhat vague modern indications of an eternal or cyclically renewed universe, and that we assume an initial state of undifferentiated heterogeneity, it must be admitted that such a theory possesses a measure of sequential harmony, and is to that extent alluring

In roughest outlines, such a theory will run

4 An initial chaos of completely mixed or shuffled primordial elements, a tohu-wa-bohu

2 Gradual and irregular accretions into very rare and tenuous, non-luminous clouds, the existing creation of matter by "cismic" rays from other already existing sources of radiation, the formation of "dark" nebulae.

3. Development under contraction of higher molecular speeds and "tomperatures", light emission, the luminous diffuse nebulae, containing only a few of the "earlier" forms of matter

4 (travitational condensation of this luminous nebulosity into the "young-est" stars, the process is nearly finished in such cases as the Pleiades nebulosity, final development within the stars of the "later" and more complex forms of matter, etc

It is said that ROWLAND jokingly laid down the dictum to a student that if a theory could not be right, the next best thing was for it to be exactly and diametrically wrong. It is not impossible that the rather attractive theory outlined above is exactly wrong. It is at least as probable, a priorl, that the nebulosity surrounding the Pleiades and other high temperature stars may be being emitted, rather than a residue of evolutionary contraction processes

<sup>1</sup> Cf F W, Hanne, On the Passage of a Star through a Nebula Ap ] 53, p. 169

1

Our best summary of the facts that may bear on any theory of the diffuse nebulae is due to HUBBLE (l. c.). From the average spectral types of the stars involved in nebulosities of the emission and the absorption spectrum types, he has drawn the following important conclusions (cf. Tables 3 and 4 above):

- Stars involved in nebulae having continuous spectrum are nearly all of Class B1 or later.
- Stars involved in nebulae having emission spectrum nearly always have spectra earlier than Class B1, rarely showing any bright lines.

Hubble therefore holds that all nebulae of the diffuse type are intrinsically non-luminous, and that in every case the luminosity of nebulae showing an emission spectrum is excited by an involved hot star of earlier type, while the luminosity of those displaying a continuous spectrum is due to simple reflection or to some sort of resonance phenomenon, from similarly involved stars of later type. "A casual inspection of diffuse nebular structure and configurations of involved stars suggests that the association is for the most part temporary. This may be one fundamental distinction between diffuse nebulae and planetaries, for in the latter the central stars must be permanently associated with the surrounding nebulosity; otherwise their central positions could not in general be maintained."

These significant results introduce another difficulty in the long current assumption or theory that diffuse nebulosity forms the initial stage of stellar evolution. For most modern theories hold that the typical star begins its life as a red giant, of relatively low temperature, reaching the high temperature of the B stars only much later in its life history. If the primordial state of the stellar matter was nebular, and if this process is in some cases still incomplete, the fact that practically no red stars are involved in such nebulosities becomes a very serious objection to the older theory, and one that it seems impossible at present to remove.

There are, however, several very serious exceptions, as admitted by Hubble. to his theory that the light of the diffuse nebulae comes in every case from involved stars. Notable among such exceptions are the America (7000) and Network (6995) Nebulae: vast structures in which no bright stars whatever seem to be physically involved. If such objects are not intrinsically luminous, one can only make the assumption, on Hubble's theory, that the luminosity is in some way engendered from the stars of neighboring regions of the Milky Way.

## c) The Planetary Nebulae.

20. Definition of the Planetary Type. The term planetary has long been restricted to a limited class of relatively small and clearent nebulae of emission spectrum, possessing a more or less definite spheroidal or annular symmetry with regard to a center which is nearly always stellar. Their apparent dimensions average less than 1', though this is greatly exceeded by some of the giants of the class (e. g., 7293 is 45'·12', and doubtless the largest planetary known); not a few of the genus are so small as to be apparently stellar in large telescopes. In apparent surface luminosity, they range from objects with the brightest nebular matter known (7009, 7027) to faint disks several hundred times less intense, which leave only a slight impression in an exposure of two hours (7139). While there are some exceptions to the rule, the typical planetary has a central star, whose apparent luminosities range from the 9th to the 19th magnitude, or fainter.

21. Number and Distribution of the Planetaries. In distribution, the planetary nebulae are definitely galactic, with a marked concentration in the Milky Way regions from  $\alpha = 18^h$  to  $20^h$  See Figure 14

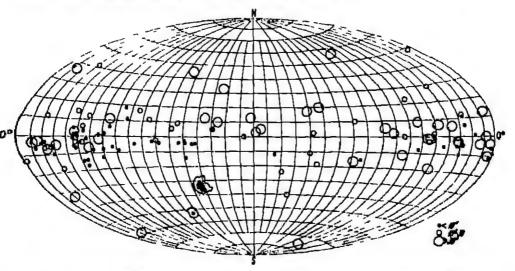


Fig. 11 Galactic Distribution of the Planetary Nebulae. It will be noted that these distant from the galactic plane are in general the larger members of the group, which are presumably closer. The smaller and more distant objects are closer to the galactic plane.

Pewer than 150 objects of this class are at present known, nor does it seem probable that future surveys will add greatly to this total. The most complete collection of data on the planetary nebulae yet published will be found in Volume 13





Lig 12a and b The Planetary Nebula NGC 6720 (Ring Nebula in Lyra) (Lick Photograph )

A photograph of the object is shown at the left, at the right is a sketch by Currus showing the intricate structure

About 135 are noted in the NGC lists as planetary or provibly planetary. A few have since been discovered by Humason, Humble, Prank, Innes, Jonekinker, Curtis, and others. At the time of publication of Vol. 13 of the Lick Publ. (1918), but 78 were known morth of declination — 34°. The following considerations indicate that no great increase for humber of planetaries is probable.

1 To tost this point, Curres examined with a slitless spectroscope (Lick Publ 13, p. 73) 50 small objects within 25" of the Milky Way which have the NGC descriptions, small, very

2 The rayision of the Drafts Catalogue increased the number of listed stellar spectra.

1 The rayision of the Drafts Catalogue increased the number of listed stellar spectra.

1 Troin 9(x) to 227(x) But one new object with a planetary spectrum was found.

of the Publications of the Lick Observatory, 1918, to be referred to henceforth as Lick Publ 13, with the omission of the date. It contains the following monographs:

Part III. The Planetary Nebulae, by H. D. Curtis.

Part IV. The Spectrographic Velocities of the Bright-Line Nebulae, by W. W. C. VII. BELL and J. H. MOORE.

Part V. The Radial Velocity of the Greater Magellanic Cloud, by K.F. Wulson. Part VI. The Wave-lengths of the Nebular Lines and General Observations of the Spectra of the Gaseous Nebulae, by W. H. Wilgett.

22. Forms Assumed by the Planetary Nebulac. Of the 78 planetaries north of decl. -34°, depicted by Curtis in Lick Publ 13, 55 have a central star, as follows:

	40		2452	0572	6891
	246		2610	6578	6894
	650		3242	6620	6905
$\mathbf{II}$	1747		3587	6629	7008
I	351		4361	6720	7009
	1501	1)	3568	0751	7030
	1514		6058	6772	7139
	1535	11	4593	6778	7293
J	320		6210	6781	7354
1	418		6309	6803	7662
	2022		6369	0804	
H	2149		6430	6818	
	2371		0445	6826	
	2392		6543	0853	
	2438		6563	6881	

8 very small planetaries, only 2" or 3" in diameter, may possibly possess a central star, though their small size makes it impossible to distinguish such. These are:

	6644		6807
11	4732		6833
11	4846	11	4007
	6790		5117

No central star can be made out in the following 13 objects:

1952 H 2165	0537 0505	0886
J 900	11 4776	7027 11 5217
2440 H 4634	6741 6884	

4 planetaries are binuclear, trinuclear, or too irregular to classify:

1952 J 900 2440 7037

From a consideration of the data given above, it seems evident that the typical planetary has a central star, of Class O.

The planetaries may be further classified as to apparent form:

A. Forms apparently helical.

6543 7293

B. Annular forms; main feature a circular or elliptical ring.

	246	2438	6369	7662
_	1535	2610	6720	, –
1	418	3242	6804	
	2022	3587	6894	
	2392	4361	7(XI)	

C. Disks showing brighter edges; elliptical rings less perfect than those under (B), fading out at the extremities of the major axis, and giving the impression of ellipsoidal shells.

П	1717	6058	6751	6854
	1501	6561	6772	7009
	1514	6565	6781	7139
11	2165	(1720)	6804	7354
	2452	0741	6818	7662

1) Forms like those under (C), but with a more pronounced truncated effect, as though the ends at the terminations of the major axis of the shell had been out off, faint answe are generally seen at these extremities

40	6561	7026
650	6720	
2371	6778	
6058	6851	
(1415	6905	

E Objects considerably furnter along and at the ends of the major axis, this group contains some nebulae from all the first four classes

10	6445	7009
1501	6563	7026
1514	6 <b>5</b> 65	7139
11 2105	6720	7293
J 900	6741	7354
2372	6772	
245H	6778	
2152	6848	
(H)5H	6853	
0360	6905	

It incular or elliptical disks, fading out slightly at the periphery, and without discernible structure. Most of these are small, and the lack of structural details may be only apparent.

1	151	6537		6629		6884
J	120	0572	ΙĮ	4776		6886
11	1568	6567		6803	11	5217
11	4014	0578		6879		
	6440	6620		GNR1		

H. Stellar planetaries. These are indistinguishable from a star on the scale of the Crossley negatives, but have been shown by visual observations to have a minute disk. In all probability they differ from the objects under (F) only in

Mechanical and quantum theories of the forms assumed by planetaries will be treated in clph. 30, 31, and 32.

28. Proper Motions of the Planetary Nebulae. The almost stellar image presented by a planetary when observed with small apertures, as by a meridian circle, and the stellar nucleus exhibited in many of the group when higher powers are employed, have made these objects attractive subjects for position measures for over a century. The total number of measures on a few of these planetaries by filar nucrometer, meridian circle, and photographic plates is quite large.

If any combination of position measures of three-quarters of a century ago with modern photographic positions has any chance of a trustworthy result in the nebular field, we should expect this from the almost stellar appearance of certain planetures. Lundmark<sup>1</sup> has discussed all available older measures

<sup>&</sup>lt;sup>1</sup> Ups Medd No 39 (1928)

(using recent plates for the final term) of six of the better determined planetaries, plotting the positions on charts and determining the proper motions graphically Reference to the "scatter" of these significant and illuminating diagrams (the

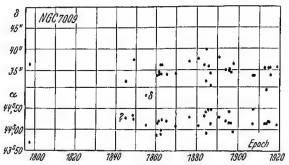


Fig 13 Positions of the Planetary Nebula NGC 7009, 1794 - 1920 (LUNDMARK) No certain proper motion 15 obscivable

contains van Mianen's latest values. These values of van Mianin are considerably more trustworthy, depending solely upon modern large scale photo graphic plates with an average time interval of 11 years. His probable cirous are



Fig 14 The Planetary Nebula NGC 7293 (Lick Photo graph ) This beautiful object is the largest known planctary, and is about 15' 12' It appears to be two turns of a helix

cal method are due to van Maanen His values, with some additions, have been collected by LUNDMARK and are given in Table 6, with the apparent and the derived absolute magnitudes of the central stars. To these values have been added

values for 7009 are reproduced m Figure 13) will convince anyone that absolutely nothing certain can be known of the proper motions of the plane taries (or other nebular types) through the support of the older visual observations, the only definite conclusion is that the proper motions of the planetaries must be very small

The following table gives LUNDMARK'S values, together with those derived from nearly the same material by other in vestigators. The last column

0",0010 in a, and 0",0012 m  $\delta$ , the mean parallax resulting from his values in combination with the rota tion results of Campbell and Moore is 0",001, giving a mean mass of  $180 \cdot (\cdot)$ , and a mean absolute magnitude for the central stars of 14

In Table 5 I u LUND MARK, VM VAN MAININ. WIRIZ, Ma MAKIM SON. NAC NICHOLSON (IC vision of Curris), Ly HN In each pair of values, the proper motion in a is given above, with that in declination below

24. Distances and Dimensions of the Planetary Nebulae While a number of investigators have discussed the parallaxes of the planetanes by various indirect methods, practically all results by the trigonometri

<sup>1</sup> Mt Wilson Conti No 406 (1930)

the dimensions of the planetaries and their distances, the latter are manifestly subject to large uncertainty

Table 5 Proper Motions of Planetary Nebulae

Object	Interv	ī.n	W	Ma	NAC	lø	VM (11 y )
2371	45 y	一",040 十 ,041			-",016 + ,074		
2392	65 y	800, - 800, -	-",004 - ,010	)	ı	) 	
6058	11 y	}		Ì	· !	)   	",000 - ,000
6543	118 y	,013 ,007	,(NX) - ,014				£00, + 000,
6572	91 y	十 ,012 一 ,009	+ ,003 - ,004		- ,008 + ,024	+*,006 - ,017	- ,004 + ,007
6720	11 y		i l				+004 +,008
CHO4	11 y			,			,008 - ,002
6905	11 y	ì	\ 		1		- ,006 (000,
7009	123 y	+ ,006 + ,004	009  -   048		\ \		,,,,,,
7662	121 y	+ ,012 + ,011		- ,024 + ,026	- ,005 + ,020		(  ,022) (-  ,004)

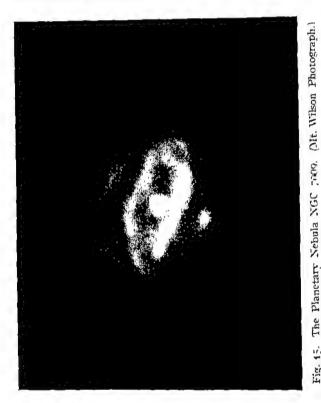
Table 6 Distances and Dimensions of the Planetary Nebulac

NtA	) Haru	e Lear	Many.	N <sub>obs</sub>	Ital	Jakt.	Other values
ММ	Are	l y		- 004	π	17	7
40	60"	0.12	11,6	+ 1,6	F",003	1000	
1501	56	,06	13,0	+ 8,7	16	200	
1514	120	,95	8,0	-0,5	2	1600	
1952	360	,96	15,5	1 9.2	6	600	
21122	28	.04	14,2		. 8	400	1
2371	60	,09	13,5	+8,3	11	3(M)	
2392	17	,04	10,0	1 5.5	20	160	1  -",006 S
3242	40	,(12	12,2	+7.8	31	100	
1I 4593	15		10,0	_			- ,(x)7 S
CHISH	43	-	13.0	-	16		
6210	43		11,7		- 3 '	-	
6543	22	,04	11,3	8,4	29	100	
6572	16	,09	10.8	[-0,8	. 3	1000	
6720	83	,66	14,7	18,5	2	1600	4 ,015 N
6778	25	,08	14,8	1 6,3	5	650	
6804	63	,05	13,4	-1-9.7	20	160	f - ,002 5
30°3639	5	,04	10,2	1 1.7	2 '	16(N)	L ono L
6826	27		9.5	_	_	_	- ,006 5
6853	480	.77	13,7	-1 8,3	10	320	1
6891	15	,02	12,1	1 8,0	17	190	
6905	44	,05	14.5	+9.7	13	250	[
7(K)8	86	,10	12,8	+8,2	14	230	1
7026	25	,(14	15,1	F9,9	£1	3(2)	1
7027	18	,04	10,9	- -4,4	8	4(10)	
7293	900	,38	13.3	11,1	38 ,	86	1
7625	200	,20	8,5	-  4,2	16 !	200	'
7662	32	,02	12,9	+9.3	21 1	150	

B = SWARTHMORR, N = NEWKIRK, I. = Late

It seems fairly certain that the values given above are much too small as regards distances and diameters, and that these must be multiplied by some

as regards distances and diameters, and that the same as yet unknown factor, perhaps as large as 3 or 5. The mean absolute magnitude (about +8) is much lower than that derived from van Maanen's last determinations of proper motion (+3). Gerasimovič¹ has discussed this dilemma, deducing from van Maanen's (earlier) proper motions in combination with the Lick radial velocities a mean abs. phot. magn. for the nuclei of -1-5.9. By various indirect methods, using the angular galactic dip, galactic rotation, and novae at the planetary stage, he derives



+4.9 as the most satisfactory value of M, and points out: "None of the indirect methods used above has given so low an absolute magnitude (+8.1), or so large a mean absolute parallax (0",012) as derived from the Mt.Wilson parallax plates. No other case is yet known for which the discrepancy between trigonometrical parallax determinations and the results of indirect methods is as great as for the peculiar group under consideration. The explanation of this paradox seems therefore to be of much importance." As a possible course of the difference in the content of the con

portance." As a possible cause of the difference, he somewhat doubtfully assigns the existence of some sort of "sampling error" in the selection of the Mt. Wilson objects.

5 111 本 小は 一日 一日 一日 The remaind of the Particular No.

<sup>1</sup> Harv Bull No. 864 (1929).

25. Planetary Spectra; Spectrum of the Nebulous Matter. While the spectrum of the nebulous portions of the planetary nebulae is in most respects a duplicate of the emission spectra of the diffuse nebulae, there are a number of points of difference. In the case of the fainter lines, these differences may arise from the far greater areal luminosity of such an object as 7027 as compared with the Trapezium region of Orion. In other cases, it is possible that actual differences of state or constitution may be indicated. These differences do not seem, however, to be vital, or to indicate different sorts of component matter. There are also frequent differences among the planetaries themselves, as well as



Fig. 17. Objective Spectrogram of the Planetary NGC 7662. (Photograph by WRIGHT.)

in comparison with the diffuse nebulae, in the relative intensities of the lines, as noted for the diffuse nebulae in ciph. 16.

Table 7 is composite, in that it includes all the lines measured by Wright in various planetaries; for the peculiarities of individual objects, reference should be made to his monograph in Lick Publ 43. The series relationships and ionization potentials are as given by Bower!. The intensities are mainly for 7027; in a few cases these are merely estimates.

Table 7. The Spectrum of the Planetary Nebulae.

7 LA.	Source	Series designation	Excitation potential, y.	Intens.	Notes
3313	Om	$3h^{3}P_{1} - 3m^{3}S$	36,72	1	1
3342	Om	$3k^{3}P_{a} - 3m^{3}S$	36,72	-	5 2 3
3346	Oty?	$3m^{3}I^{5} - 3n^{3}I)$	51,76	- 1	2
3420,2	N1/ 2	38 S - 38 P	47,	20	3
3445	$O_{\Pi}$	$3m^3P_a$ – $3n^3P_a$	40,66	8	
3704	$H\mathcal{E}$ , $He_1$	23 13 73 11	13,49; 24,22	_ '	4
3712	Hr	-	13,49	- 1	4
3723	11µ		13,48	-	4
3720,10	$\Theta_{0}$	$a^1S - a^2D_2$	3,31	50	4 5 5 4
3728,91	$O_{11}$	$a^{\dagger}S - a^{3}D_{a}$	3,31	30	5
3734	11λ .		13,47	_ [	4
3750	11×		13,45	3	6
3759	Om	$3 k^{4} P_{a} - 3 m^{4} D_{a}$	36,19	4	
3771	111	arm tag to the	13,43	4	
3798	110		13,41	5	
3820	Hei	$3^{9}P - 6^{9}D$	24,11	i + 1	
3835.5	11 11		13,38	8	
38-10-2	11.7		_	5	
3868,74				70	7
3888,96	115, 11e <sub>1</sub>	285 3871	13,33; 22,92	10	8
3935	Caus	$4^2S - 4^2P_2$	3,14	_	i
3964.8	He	$2^{1}S$ $1^{1}P$	23,65	5	9
3967.51	1 11	• • • • • • • • • • • • • • • • • • • •		70	9
3970,08	Hr		13,27	30	_
4009	Het	$2^{1}I^{1} - 2^{1}I^{2}$	24,22	1-	1
4026,2	Неп. Нег	23 P - 50 1)	53,78; 23,95	1	1
	rieg, rier	21 212	201101 -2122	1	1
4064	· ·	$a^4S - a^2P_2$	_	20	10
4068,62	Su	$a^{\dagger}S = a^{\dagger}P_{1}^{2}$		2	10
4076,22	Str	$3h^2S - 3m^2P_2$	30,35	1	
4097,3	Nut	$3k^2S - 3m^3P_1$		70	
4104,74	H8, N <sub>III</sub>	2K-9 2M-X-1	T C (1/1 (C)	, , , ,	,

<sup>1</sup> Ap J 67, p. 1 (1928).

## (Continued)

111	Source	Series designation	1 scitation potential, v	Inten	Nith
	Tic	237-575	23 88	1	
4120,6	HeI	21 P-61 1)	24,12	ı	
1114 0	He	2-1 -0 12	53,76	1	
<b>42</b> 00	Hun	$3n^{3}D-4^{2}I$	20.87	5	
4267 1	Cit	3117-4-1		4363	
4310 16	$H_{2}$	_	13 00	1	1.1
4353	-			80	, -
4363 21	$O_{111}$	$a^{1}D - a^{1}S$	4,53		
1303.0	He	$2^{1}P - 5^{1}D$	23 95	5	
1416	$O_{II}$	$3k^2P_{12} - 3m^2D_{23}$	26 18	1	
	He	$3k^{2}P_{1} = 3m^{2}D_{2}$ $2^{3}P_{-} + 3D$	23,61	4	
1471 54	Hen		53,14	2	
4541,4	Hell		1	l.	
45715		$3m^2P_1 - 3n^2D_2$	33,01	2	
4654,1	N <sub>III</sub>	$3m^2P_2 - 3n^2D_3$	33,01	5	
4640,9	$N_{III}$	$3^{11} - 1^{12} = 3^{11} - 3^{12}$		1	1,
4649 2	CIII	3.2-2.1	30,1	ż	L
4658,2	_	-	1	191)	• •
4685 76	Hell	l Mari	50,82		
4711,4	_	-		(0	
4712,6	He	23P-135	23,50	5	
4725 5		<del>-</del>		- 1	
4740,2		-		20	1.1
4861,32	$II\beta$	~	12,70	20	
4922 2	He,	2'P-4'D	23,61	2	
	On	$a^3 P_1 - a^1 D_3$	2,50	200	
4958,91		$a^{3}P_{2}-a^{1}D_{2}$	2,50	500	
5006 84	O <sub>III</sub>	$2^{1} \stackrel{2}{5} - 3^{1} \stackrel{D}{P}$	23,00	1	
5017	He,	2-1-1-1			
5411,3	Hen		53,10	· .	l
5655		_		:	
5737	_	_	1	1	
5754,8		_		1 1	
5875 7	He	$2^3P - 3^3D$	22,98	8	
6302	] –	] -		5	
6313				2	
6364	_			2	i .
6548 1	$N_{II}$	$a^{9}P_{1}-a^{1}D_{2}$	1,89	10	Ì
6562,79	$H\alpha$	1 8	12,04	100	)
6583 6	N <sub>II</sub>	$a^{\eta}P_2 - a^{1}D_2$	1,89	30	\
	He	$2^{1}P - 3^{1}D$	22,98	1	1
6677		$a^{1}S - a^{2}D_{0}$	24,70	1	10
6730	$S_{II}$	4.2-4.135		,	141
7009		-2.35 -2.5	22.63	1	
7065	He <sub>I</sub>	$2^3 P - 3^3 S$	22,63	t	
7138	_	_		I.	15
7325	OIL	$a^{2}D - a^{2}P$	5,00		1.5

Notes to the table of wave-lengths

Note 1 The electron configurations in this table are indicated by Bowks as follows. Terms arising from the most stable configurations, n being the number of valence electrons remaining in the atom.

(2) 2s, (n-2) 2p electrons ,	u
(2) 2s, $(n-3)$ 2p elections and an excited selection	λ.
(2) 2s $(n-3)$ 2p elections and an excited p election	m
(2) 2s, $(n-3)$ 2p electrons and an excited d electron	n

The numeral preceding these letters indicates the total quantum number of the excited electron, these letters are omitted in one- and two valence electron systems, since for all the cases considered here the type of the term is the same as the type of the orbit of the excited electron.

Notes 2, and 3. These are the lines reported by Paimler at 337  $\parallel$  and 315  $\parallel$   $\mu\mu$  Note 4. Observed in Orion, but not in planetaries

Note 5 Buisson, Fabry and Bourger derived the wave-lengths 3/26,100, 3728,838 Note 6 Hz 3750,52

Note 7 The strong lines at 3868,74 and 3967,51 are still unidentified. Carbon has been suggested. 1. Bernan, reported in Pop Astr 39, p. 184 (1931), has studied the behavior of those lines, whose intensity ratio is constant in various planetary nebulae. He rejects the explanation of their origin as due to \$\epsilon\$\_{111}\$ and considers the availability of \$P\_{111}\$ or \$\epsilon\$\_{111}\$.

Note 8 HZ 3889,051 He 3888,64

Note 9 Suspected with intensity 10 in

BD +30°3639

Note to Cf Bowse, Nat 123, p 450 (1929) Note 11 Suspected in Orion, not in planeturies

Note 12 See Note 7 Lines of Cat 4647.4,

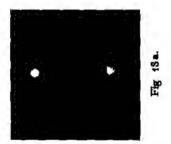
4650,7, 4651,6

Note 13 MERRILL finds this line in R Aquaril and BD -12°5145

Note 14 Unidentified

Note 15 MERRII L gives 7135,6 and 7330.4

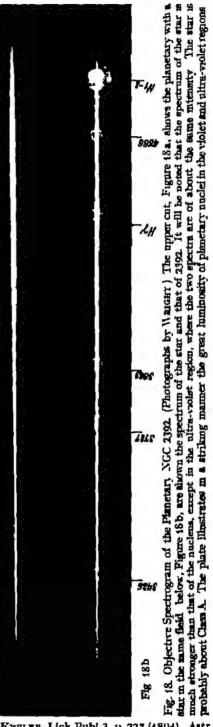
26 Planetary Spectra; Spectrum of Planetary Nuclei<sup>1</sup>. The resomblance of the spectrum of planetary nuclei to that



of the WOIF-RAYFT stars, tentatively suggested by PICKERING, has been established beyond all doubt by the extensive researches of WRIGHT

The main characteristics of the spectrum of planetary nuclei are:

- 1 A marked and uniform extension of continuous spectrum into the ultraviolet
- 2 The occurrence of bright bands identical with those observed in the WOLF-RAYIST stars (Class O). The relative strength of these bright bands with respect to the continuous spectrum varies from object to object, in some, as 7026 and 6751, they occur almost without it, while in others they are barely visible against the strong continuous background.



<sup>&</sup>lt;sup>1</sup> В С Ріскевіна, А N 127, р 1 (1891), Ј Е. Кикіли, Lick Publ 3, р 227 (1894), Astr and Astroph 13, р 497 (1894), W Н WRIGHT, Ap J 40, р. 466 (1914), Lick Publ 13 (1918)

Out of 30 planetary nuclei, WRIGHT finds that about one-half are Class O stars, and regards the evidence as unequivocal that the nuclei of all the planetary nebulae belong to the same stellar division as the Class O stars. The sequence will then be:

1. Nebulae without nuclei.

2. Nebulae with nuclei. These nuclei are in all cases stars of very high temperature, and in half the cases show the Wolf-Rayer bands.

3. Class O stars, with no (observed) nebulous surroundings. Temperature

high.

The number of the Wolf-Rayet stars is about the same as that of the planetary nebulae. Miss Payne<sup>1</sup> enumerates a total of 238; of these 106 are of galactic occurrence, 39 are planetary nuclei, and 33 are in the Magellanic Clouds.

The spectral classifications of planetary nuclei have been tabulated by Miss.

PAYNE in tables VI, II, of the work quoted.

Table S.

Object	Spectrum classification	Onject	Spectrum classification	
40	WIII	6629	Cont.	
246	06	11 4776	W 114	
II 1747	W	6720	Conk.	
I 351	//r	6751	WHI	
II 2003	Cont.?	6790	Cont.	
1514	08	6803	Cinit.	
1535	Cont.	30° 3639	WIII	
I 418	O7w	6826	Oow	
2022	Cont.	6833	Cont.?	
II 2149	· O7	6879	Cont.	
2392	O8w	6891	Cont.	
3242	Cont.	II 4097	Contac	
4361	Cont.	6905	WILL	
II 3568	· Cont.	7000	Cont.	
6058	Cont.	7020	WHI	
II 4593	07 + Cont.	II 5217	WIII	
6210	W	I 1470	0	
II 4634	Cont.	7635	()7	
6543	WI	7662	Cont.	
6572	WI	, ,,,,,,	,,,,,,	

(The small w in the above Table indicates WOLF-RAYET lines in addition to continuous spectrum; WI has the line at 4686 A stronger than combined lines near 4.340 A; W111 has the 4686 A line weaker)

WRIGHT has suggested a classification of the planetaries based upon the relative intensity of characteristic lines, as follows:

- ,				
Class I, 4686 A present in the nebula				Type object
a) 3426 A stronger than 3445 A.		. ,		. 7027
b) 3445 A stronger than 3426 A c) 3445 A and 3426 A absent	4 4	• •	,	7000
Chas 11, 4000 A absent from nebula, 3860 A provi	an t			
a) 1860 stronger than 175	CILL			
a) 3869 stronger than $H\delta$ . b) 3869 A weaker than $H\delta$ .				6572
Class TTT 1004 1				- 12419
Class III. 4686 A and 3869 A absent				. 1 .118

Further details as to the application of spectroscopic theory to the planeturies will be found under ciph. 28 and 31.

<sup>1</sup> The Stars of High Luminosity. Harv Monograph No. 3 (1930).

27 Radial Velocities of Planetary Nebulae; Rotation. Our knowledge of the radul velocities of the planetary nebulae north of declination — 14° is very satisfactory and complete, thanks to the work of CAMPHELI and MOORE, south of this our results are due to Wilson (Lick Publ 13). Details as to the radial velocities of individual planetaries should be sought in the tabulation given on pages 168—9 of the papers quoted.

The more important results of CAMPBELL and MOORE, and Wilson may be

summarized

1 6 planetaries show abnormally high velocities. These are

5871	- 127 km /sec	6644	- 1-2±15 km./sec
6567	+133	II 4732	134
11 4699	- 117	II 4846	F 165

These values are excluded from the averages which follow

2 17 nebulae (12 probably of planetary type) in the Greater Magellanic Cloud show an average radial velocity of  $\pm 276\,\mathrm{km}$  /soc. The velocity spread is small, and there is no doubt that this represents the radial velocity of the Cloud as a whole

3 1 planetary in the Smaller Magellanic Cloud has a radial velocity of +168 km/sec. With less certainty, this may be regarded as indicating the

approximate velocity of this Cloud

4 96 objects of planetary type yield a speed of -29,6 km/sec for the solar motion. The mean radial velocity of 31 of these with diameters less than 5" is 28 km/sec, while that of the 65 larger objects is 31 km/sec. Those volocities are about five times the average radial volocities of the B-type stars.

5 Of 46 planetaries examined, 25 showed internal motion effects, which may be interpreted as rotations about axes approximately perpendicular to the line of sight, while 4 are not 40 interpretable. The most elongated planetaries show the highest rotational speeds and, in general, the speed of rotation of outer

strata is less than that of strata nearor the center,

6 With some more or less probable assumptions, the mass of a planetary

seems in general to exceed that of the solar system

Physical change has been noted to date in but one object, and that is the "Crab Nebula", 1952. While it is somewhat doubtful whether it is a typical planetary, reference to its internal motions will be included at this point. Variations ascribed either to luminosity changes or to motion were first noted by Lampiano and this nebula was later subjected to careful investigation by Duncan. His measures are based upon Mt Wilson plates separated by an interval of 11.5 years. For twelve selected nebular points or configurations, radial motion outward from the center was definitely indicated, amounting to 1",54 in the interval. This displacement, if at a velocity of 25 km/sec, would correspond to a distance of 1001y, and Duncan points out that it is necessary to assume neither an enormous distance nor an extraordinary velocity in the nebular particles in order to believe that the observed motions are real

28. Spectroscopic Distribution Effects. The phenomenon of varying distribution of matter indicated by different spectral lines in the Nebula of

Orion has already been noted under clph 16 above.

Objective prism spectrograms likewise show more remarkable and equally definite evidence of differences in ionization distribution or constitution of

<sup>&</sup>lt;sup>1</sup> Publ A S P 31, p 79 (1921)

<sup>2</sup> Wash Nut Ac Pros 7, p 179 (1921), with plate

different elements in the shells of many planetaries. Campbell 1 had already called attention in 1894 to the differences in the diameters of the spectroscopic images in I 418. This effect was perhaps first noted photographically by Woll 2 and corroborated by Burns for the Ring Nebula in Lyla 3. Wright has illustrated many cases in his monograph in Lick Publ 13, and most of the data in the following summary are derived from his researches.

Table 9 Distribution of Planetary Materials (Wright) Sizes of Rings of Formations

NGC	I arg	gest	> Smalle	nt.	Notes
40 I 351 1535 I 418 2022	II 3727	_ Πβ	1171	1686 N <sub>1-2</sub>	No difference noted Slight difference Slight difference
II 2149 II 2165 2392	3727 3727 —	3967	- 1686 -	3426 —	Differences in intensity but no in size
2410 3242	3727	$N_{1-\frac{n}{2}}$	4686	3126	Large differences Slight differences
II 4593 6309 6543 II 4776 6720	3727 3727 3727 3727 3727 3727	N <sub>1-2</sub> N <sub>1 2</sub> N <sub>1 2</sub>	-   II -	1686 - 1686 1686	Nearly equal  Some structural differences  Wort  Burns, Ha 3727  Wright
6741 6751 6818 6826 688‡	3727 3727 	3869 II	1686	3126 N <sub>1 2</sub> 3426 1686	Structural differences Structural differences
6886 6891 7009 7026 7027	3727 3727 3727	3869 - N <sub>1 2</sub>	11 +686	3126 1686 4686?	Notable structural differences About same size
7662	3869	$N_{\stackrel{1}{\text{II}}^{-2}}$	} 1542	3126	Notable structural differences

It will be noted from the above compilation that the largest image in the majority of cases is given by 3727 Å,  $O_{\rm HI}$ . The smallest ring is generally either 3426 Å ( $N_{\rm IV}$ ?), or 4686 Å,  $He_{\rm HI}$ . Reference should be made at this point to the far more detailed results secured by Birman, discussed in ciph 33. Birman determined isophotal contours for the various spectrographic images, and his diagrams show remarkable variations, not only in size, but in contour, so that the distribution due to a given state may be entirely unlike that given by another See Berman's diagrams, reproduced as Figures 25 and 26, a, b, c

<sup>&</sup>lt;sup>1</sup> Astr and Astroph 13, p 491 (1894)

<sup>&</sup>lt;sup>2</sup> V J S 43, p 283 (1908), also Geschichtete I michemission im Ringnebel Szb Heidelb Ak, Abh No 27 (1911), Die Spektia zweiei planetarischei Nebel, ibid., Abh 35 (1911) Dei Ringnebel und dei Dumbbellnebel, ibid., Abh 1 (1915), NGC 2438, ibid., Abh 2 (1916)
<sup>3</sup> Lick Bull 6, p 92 (1910)

29. Turbulence Effects in the Planetaries. This name is chosen to designate one of the most remarkable characteristics of the spectra of some of the planetary

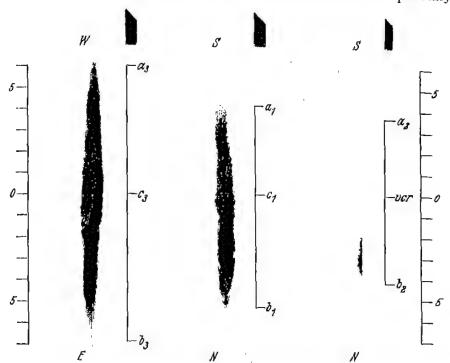


Fig. 19. Drawings of the  $N_1$  Line in NGC 6210. a minor axis; b and c major axis. (Moore.)

Tuble 40. Turbulence Effects in Planetary Nebulae.

NGC	Descriptions
Mit.	Discription
40	The line $N_1$ is not straight, but a very flat, $S$ ,
2392	The line $N_1$ is single at its outer ends, with an irregularly doubled central portion.
3242	The nebular lines are tortuous, with a suspicion of doubling in the central part of $N_n$ .
6210	The $N_1$ line is torthous and irregular, with a slight doubling in an exposure along
	the major axis.
6543	The $N_{\rm g}$ line is torthous, with several slight bends.
6572	The $N_1$ line is irregular and wavy.
6567	The nebular lines are S-shaped.
6720	The $N_1$ line is wavy, with a marked bowing toward the red in the central portion
	along the minor axis.
6818	The N <sub>1</sub> line is tortious at the ends, and is slightly but clearly doubled, though irregularly, over the central portion of the planetary.
6891	N <sub>1</sub> irregular, and on some plates a very flat S.
7009	W. irrogalar: a very flat S.
7026	N <sub>1</sub> broad and very irregular, with marked minor effects of turbulence.
7027	1 M whence an account local irregularities and moltimes.
7662	I M is doubled to be control worken with interesting differences between major,
	I minus and diagonal axis positions of the slit. On the major axis, the rea com-
	I would be at convenient one and of this doubling while the Violet computation is the
	attenues at the other and. The confours of the life 4000 A SHOW STIRE
	differences from those displayed by the chief nebular lines.
	See Figure 22.
	I a tildare man

WRIGHT and MOORE, Publ A S P 44, p. 307 (1929).

nebulac, a phenomenon so peculiar and so anomalous that no entirely satisfactory explanation seems as yet attainable. These phenomena differ from nebula to nebula, and the differences defy verbal description, so that reference should be made to the spectra exhibited pictorially in the papers of Wright and Company

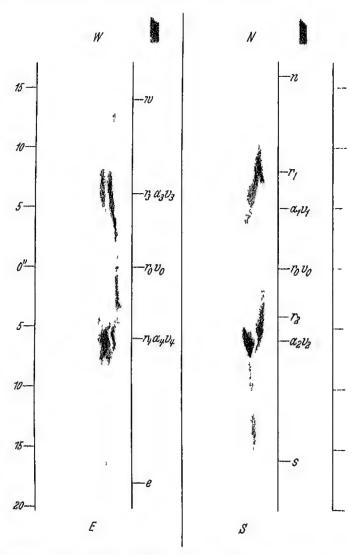


Fig 20 Drawings of the  $N_1$  Line in NGC 2592 a minor axis, b major axis (Moore)

BLIT and Moore in Lick Publ 13, and particularly in the sketches made by Moore, three of which are reproduced here as Figures 19, 20, and 21

While this phenomenon has some resemblance to the turbulence effects observed in the Orion Nebula, it is difficult to connect it with the distribution effects described in the preceding Section, and motions of the different elements or states of the same element seem to be involved. It is exhibited in the slit

spectrograms of a considerable proportion of the brighter planetaries, which show an astonishing complexity in the doubling, bowing, or distortion of the lines of the brighter radiations. There are, in addition, frequent minor differences between the appearances along the major and minor axes of the planetary disks.

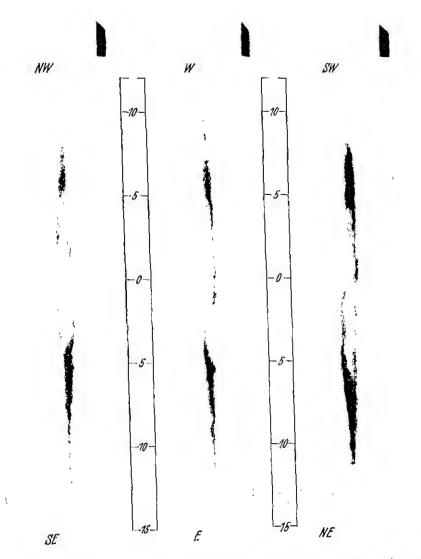


Fig. 21. Drawings of the  $N_1$  Line in NGC 7662. a minor axis; b diagonal axis; c major axis. (Moore.)

The radial velocities measured at different parts of the doubled lines in 2392 vary from +36 to +130 km./sec. The local irregularities in these spectral images are so masked by the process of photographic enlargement that they are best studied in Moore's drawings. Evidence for these turbulence effects is assembled in Table 40.

Polarization tests gave no support to the Zefman or Stark effects as possible causes of these irregularities and doublings, and relative radial motions seem an admissible explanation

Curtis (Lick Publ 13, p. 66tt), from his studies of planetary forms through direct photography, attempted to set up reasonable mechanical models for the production of these curious spectrographic phenomena. He found that most of the peculiarities in these bowed and doubled lines could be produced by the

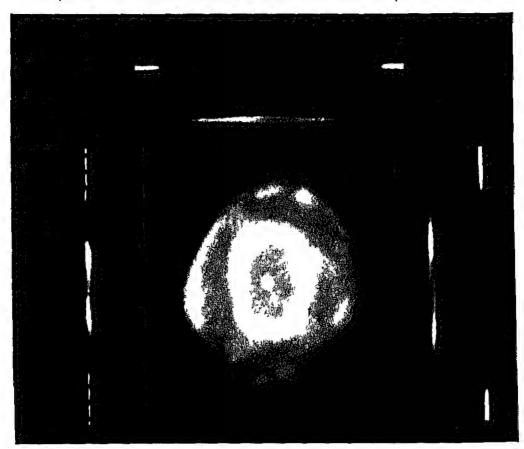


Fig 22 The Planetary Nebula NGC 7662, and Imbulence Effects (Lick Photographs) The central figure is a drawing of the planetary by Curits. The spectra on each side and above are by Wright and Moore — At the left is the image of 5007 A ( $N_1$ ) with the slit along the major axis of the planetary, while the upper figure is the configuration of the same line with the slit along the major axis. The line at the right is that due to 4686 A, with the slit along the major axis. It will be noted that there are striking differences in the images of 5007 A and 4686 A with a complete reversal of pattern — In their bearing on theories of planetary structure and ionization state distribution, these remarkable photographs are doubtless the most significant which have been secured to date

assumption of a planetary as a homogeneous, somewhat truncated spheroidal shell of gaseous matter, a form which seems to have numerous analogues in the photographic data. Matter falling in from the polar zones of such a shell, toward the nucleus, would, at various increasing inclinations of the equatorial plane of the rotating structure to our line of sight, produce through pure radial velocity

effects, first, shallow 5-shaped lines, next bifid lines, and finally, at 90°, lines which would be symmetrically doubled across the central portion of the planetary, while remaining single at the ends

This mechanical explanation, with the assumption of some degree of turbulence and irregularity in individual portions or features, would produce essentially all the line forms and anomalies exhibited (see Lick Publ 13, Plate XXVI, Ing 84). Yet it is probable that the matter is far from being so simple as this The varying sizes of the planetary shells produced by different elements, or even by different ionizations of the same element, together with the difference in the contours of 4686 A and 5007 A found by Wright and Moore, indicate that the planetary is a structure whose complexity may not be a problem of the grosser laws of matter, or of the devising of mechanical models, but rather a complexity whose source lies in temperature conditions and the quantum theory. In conclusion, it would seem that no satisfactory theory of the curious phenomena of these distorted and doubled planetary spectral lines exists as yet, a vast amount of further work is indicated on these objects with instruments of greater power, and the field will inovitably prove to be a very rich one,

80. Mechanical Theories of Planetary Structure. It has been noted in the precialing Section that, of all the various mechanical models set up by way of trial, ( trans found that the assumption of a homogeneous truncated spheroidal shell formed not only a close representation of observed profiles, but satisfied the prouhar turbulence effects as exhibited by the spectrum line distortions

There are numerous planetaries which, in projection, give the effect of a shell of luminous matter apparently detached from the nucleus, and even with the regions between this shell and the nucleus nearly devoid of matter. Curtis investigated this condition for available planetaries in Lick Publ 43. If the thickness of such a shell, supposed to be spherical, be expressed by d, with respect to the external radius, the brightness of the projected transparent ring should exceed that at the center of the planetary by the factor  $\sqrt{2/d}-1$ , giving the following values for various assumed shell thicknesses

Utilekness of shell	Helative brightness
0.001	44.7
.01	14,1
.1	4,4
.3	2,3
.5	1.7

For 25 planetaries, with a mean brightness of the projected ring equal to 2,5 times that of the central areas, the mean thickness of the shell was estimated at 0,26 that of the external radius, and hence in good agreement with this conception of their structure. For ten other planetaries, however, the estimated brightness of the ring was far in excess of the value computed from the estimated thickness of the shell. The mean relative brightness of the ring was 32 times that of the central area, while the mean thickness of the shell was about 0,39, instead of the approximately 0,002 required by theory

There is no very satisfactory explanation of such exceptional cases. That these exceptions are due to the fact that the objects are true rings, instead of shells, seems to be negatived by the fact that such rings would not be expected to be, in practically every case, arranged in space with the planes of the rings essentially perpendicular to our line of sight. This is not impossible, but almost infinitely improbable.

Also, the existence of peripheral rings of occulting matter in the equatorial planes of the planetaries, tentatively suggested by CMPBITI and Moori as an explanation of the frequently fainter matter along and at the ends of the major axis, seems likewise to be negatived by probability considerations. There is practically a complete lack of planetaries showing an asymmetry in brightness on the two sides of the major axis, hence, it such peripheral rings exist, the equatorial planes of the planetaries must, practically without exception, pass through our position in space

GERASIMOVIČI has further considered the shell forms assumed by the planetaries. He has made a more accurate derivation of the relative optical thickness of such a shell and the central areas of a planetary through a somewhat complicated integral expression which takes account both of the direction of the emitted radiant energy and the curvature of the spherical shell. He thus derives the following values.

	1 stmr	ted relativa thicky	ics of Shill
Optical thicl ness	0,1	0.2	0,3 0.1
	Ratio of lum	lnosity of ring to	that of the center
2	18	1,4	1,1
6	4.1	3, 3	2 7
10	7 5	5,6	4,1

Using these values and (urits' estimates of the thickness of the rings and the relative intensities, he derives a quantity, \$Im\$, for the absorption due to the nebular matter, and finds also the photographic magnitude of the nucleus, were the nebular verticemoved. The average value of the photographic magnitude thus found for the nucleus 7,7, agreeing well with the value 6,7 found by Wilson for 83 O-type stats. (Alrasimovič regards the mean parallax of 0",014 as determined by Van Mannen for 20 planetary nucleus as about 10 times too large, and with his revised values he finds that the absolute brightness of the nucleus is inversely proportional to the square of the linear diameter of the planetary. He further derives the mass of the shell of a normal planetary as of the order of 2.0, with an average density of 10. 10, for the temperature over the sphere of maximal density he gives the abnormally low value of 8° abs.

There have been a number of attempts to explain the mechanism of such suspended and ocassionally apparently detached spheroidal shells. It ans a has treated the possible adequacy of radiation pressure in supporting such detached shells. Milne, however, after an extensive investigation of the theory of a chromospheric atmosphere, comes to the conclusion that any such detached shell of gas, e.g., Carl atoms, is an impossibility under the action of radiation pressure, or at least until it absorbs more radiation than it emits, and is thus in an unsteady thermal state. "An atmosphere partially supported by radiation pressure is so strongly condensed toward its base that it can hardly be distinguished from the reversing layer itself, either theoretically or observationally."

81 Quantum Theory and Planetary Structure In this and the following Sections there will be reviewed certain new tendencies in the theory of the diffuse and the planetary nebulae, that may be differentiated from those of the past by the factor of atomic constitution or molecular state, for these comparatively

<sup>&</sup>lt;sup>1</sup> A N 225, p 89 (1925) <sup>3</sup> M N 85, p 111 (1924)

<sup>&</sup>lt;sup>2</sup> M N 83, p 481 (1923)

recent developments, which must be regarded as still in the formative period. the name quantum theory werns most applicable, and can lead to no confusion1

32. The Theories of ZANSTRA, BOWEN, CARROLL and BERMAN ZANSTRA® has employed HUBBIF's observational data for a theory of the luminosity of nebulous matter with involved stars. Compare also Russkii's original suggestion of excitation in emission nebulae by radiation from a very hot body

HUBBIR's results are re-summarized thus

1 The light from a patch of diffuse nebulosity having a continuous spectrum is the equivalent of the startight interespical (stars of classes H; and later)

2 The light from a patch of diffuse nebulosity having an emission spectrum is the

equivalent of the startight intercepted (stellar classes mainly 140 and Oo5)

) The light from a patch of nebulosity in a planetary is, on the average, 4 to 5 mingaltudes brighter than the equivalent of the starlight intercepted (stars of classes on lier than (No5)

Assuming that the emitting star is a black body of temperature T, Zanstra first derives from the quantum theory the number, N, of "photographic quanta" intercepted per second by the given patch of nebulosity,

$$N_{\mu h} = \Omega \frac{2\pi}{c^4 h^3} T^3 \int_{\sigma^2 - \frac{1}{2}}^{\sigma_1} dx,$$
 $\lambda_1 = \frac{h_{I_1}}{kI}, \qquad \chi_1 = \frac{h_{I_1}}{kI},$ 

where

Ω ~ solid angle intercepted.

6.54 · 10 87

1.372 10 14

The emitted light from the nebulosity may be due first to the mechanism of ordinary excitation, though this is regarded as too weak to cause the luminosity observed. The more important part is considered due to ionization and successive recombination. An atom in the normal state is capable of absorbing all the energy of a wave-length shorter than the head of the LYMAN series, frequency  $= p_0 - 32.84 \pm 10^{14}$  The number of quanta thus absorbed will be

$$N_{al} = \Omega \frac{2 + R^{4} k^{a}}{e^{4} k^{a}} T^{a} \int_{e^{r}}^{\infty} t^{a} dx$$

Although his findings were not at all in accord with modern results based upon more accurate knowledge of wave-lengths, the detailed investigation of the problem of the nebular spectrum by J. W. Nicirolson should be mentioned here. The more important of his papers ara

The pressure of radiation on reflecting spherical particles. M.N. 70, p. 544 (1910)

The spectrum of nebulum MN 72, p 49 (1911) The constitution of the Ring Nebula in Lyra MN 72, p 476 (1912)

On the new nebular line 2 1353 MN 72, p 693 (1912)

Hydrogen and the primary constituents of nebulae MN 74, p 204 (1914)

The constitution of nebulae MN 74, p 486 (1914)

On the nebular line 2 3729 MN 74, p 623 (1914)

The atomic weights of the elements in nebulae M N 78, p 349 (1918)

Atoms with nucleus 2c were regarded by Nicholson as the origin of 3869 A, one with nuclous 3s produced \$187 A, while "nobulium" was attributed to an atom with nuclous 40 His "protofluorine", postulated for the corona, was hold not to occur in nobulae. The atomic weight of nobulium was placed at 1,31

\* Ap J 65, p 50 (1927)

Ohn 44, p 72 (1921); Wash Nat Ac Proc 8, p 115 (1922).

The free elections thus "knocked out" of the atom will recombine with the nuclei by falling back to one of the different levels, emitting the continuous spectrum at the head of the Lyman, Baimer Paschi n series etc. Subsequently the elections in the higher levels will return to the normal level either directly, under emission of the Lyman series, or in steps, emitting the other 11 lines. In this way a number of continuous spectra and line spectra will be produced (see Eddington's discussion below).

After a discussion of the quanta affecting the photographic plate,  $\angle ABSTAT$  derives the following ratio of the number of photographic quanta energing from a patch of nebulosity,  $N'_{ph}$ , to the number of photographic quanta in the starlight intercepted by the patch,  $N_{ph}$ 

$$\frac{N'_{ph}}{N^*_{ph}} \sim \frac{N_{nt}}{N_{ph}} = \frac{\int_{r_0}^{\infty} v^2_{-1} dx}{v^2_{-1} dx}, \qquad \frac{v_0}{r_0} = \frac{32.84}{5.95} \cdot \frac{10^{11}}{10^{11}}, \\ \int_{r_0}^{t_0} v^2_{-1} dx, \qquad \frac{v_1}{r_2} = \frac{5.95}{0.10 \cdot 10^{11}},$$

Evaluating the integrals in this expression, the following actual ratios for different stellar temperatures are derived

T	Ratio $N_{Ph}'/N_{Ph}$	Ratio in acignitudes	1	Ratio $N_{Bh}/N_{I/h} \mid 1$	, itio m magnitud
15 000° 20 000 25 000 30 000 35 000	0,0075 ,006 ,271 72 1,41	5,51 2,95 1,11 0,36 0,37	10000 50000 100000 150000	2 50 5,1 18 101	(1 (9)) 1 (5) 3 (0) 5 (1)

In this table, a unitiatio occurs at about 35000", and the stellar temperatures, for the mechanism suggested, are

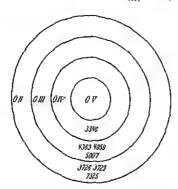


Fig 23 Bowen's Ionization Theory of Planetary Structure (After Bowln)

Тург	Lat
Bi	21000
Bo	28000
()	3.1 (10)(1)

ZANSTRA'S later values require a much higher temperature than this, because of similarity in the comparison with observation, however, his latest theory will be discussed along with Bric MAN'S below

Bowin<sup>1</sup>, following certain of Zanstra's conclusions, has set up an interesting and convincing mechanism for the planetaries, based upon the quantum theory and postulating exceedingly high temperatures for the central star. The resulting theory shows considerable resemblance to the observed data.

As a first approximation, he assumes a central star with a surface temperature of 150000° K, surrounded by an atmosphere of oxygen of very low density. At this temperature, from the strong photo-electric absorption of light of greater frequency than the ionization frequency of the atom or ion, oxygen in the insertion.

<sup>1</sup> Ap J 67, p 1 (1928)

mediate neighborhood of the star could not exist in a state of ionization lower than  $O_V$  (author's  $O^{++++}$ ). Occasionally an electron will unite with such an  $O_V$  ion, emitting the  $O_{VV}$  spectrum, to be immediately ejected by the radiation below

160 A. After traversing a distance represented by the inner circle in Figure 23, the radiation of wave-lengths below 160 A will have been so completely absorbed that now  $O_{\rm IV}$  can exist in the region outside, and by a similar process there will be a region farther out where  $O_{\rm III}$  may exist.

This mechanism gives a series of concentric shells whose diameters increase with the decrease of the ionization potentials of the ions present

within them. Bowen's theory thus furnishes a possible explanation of the relative sizes observed for the monochromatic images of the planetaries.

Bowen regards a temperature of at least 100000° necessary for the hottest planetary nuclei.

EDDINGTON and WOLTHER<sup>2</sup> have discussed the difficulty of an adequate explanation of the great strength of such "forbidden" lines in comparison with the ordinary lines of the spectrum. EDDINGTON suggests that

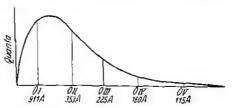


Fig. 24. Ionization Mechanism in Planetary Nebulae. (After Bowen.) The distribution in frequency of quanta omitted by a black body at a temperature of 150000° K.

λ	Source	Size
3426 A	N <sub>IV</sub>	Smallest
3346	OW	11
4086	Hell	Next in size
3313	}	
3342	$\}$ $O_{117}$	23
3444	1	1
4859	, OII	Large
5007	On	
3726	On	Largest

this difficulty may be removed by a simple addition to Bowen's original condition, namely, that the stimulating radiation must be so weak that the atom is unlikely to absorb a quantum during the full duration of the metastable state. The strengthening of the forbidden emission is then merely relative to that of the ordinary emission. He gives the following illustration of this effect:

"Let (2) be a metastable state, the forbidden transition being  $2 \to 1$ . Let (3) be the state next above (2), from which there is an ordinary transition to (2). The full duration of (2) is taken as 1 sec., and that of (3)  $10^{-8}$  sec.

First let the radiation be moderately strong so that each atom . . . absorbs about once in 10  $^3$  sec. Then practically all the atoms arriving by any route from state (3) will forthwith emit, only about 1 in 10 $^5$  being arrested and jerked to some higher state by absorption. A fixed proportion will emit the line 3 > 2 and reach state (2). Of these, only 1 in 1000 will go on to state (1); the others are forestalled by absorption which diverts them to higher states. Accordingly the forbidden emission in  $2 \rightarrow 1$  is very much less than ordinary radiation.

Next let the radiation be so weak that each atom absorbs but once in 10 seconds. As before, the atoms arriving in state (3) will forthwith emit, a fixed proportion of them traveling to state (2). But now  $^{10}/_{10}$  of these will go on to state (1), because the chance of absorption (once in 10 seconds) is only  $^{11}/_{10}$  of the chance of emission (once in 1 second). There will be more quanta emitted in the forbidden line  $2 \rightarrow 1$  than in the ordinary line  $3 \rightarrow 2$ , because (2) is the end-point of other transitions besides  $3 \rightarrow 2$ , and  $^{10}/_{10}$  of all of them are followed by  $2 \rightarrow 1$ .

A forbidden line starting from state (2) becomes more or less equivalent to an ordinary line starting from state (3)."

<sup>1</sup> M N 88, p. 134 (1927).

A late and quite complete theory of such spectral excitation is due to CAR-ROLL<sup>1</sup>. His work is based largely on certain observational data of H. H. Plas-RETT<sup>2</sup> with the correction of certain of his conclusions attributed to errors in the equations employed<sup>3</sup>. The existence of the so-called forbidden lines is taken, as by most previous investigators, as an indication that the density must be very low, as otherwise the atoms would be disturbed by collisions. Also, as pointed out by Eddington, the stimulation by radiation is assumed to be very weak.

The processes postulated as affecting an atom of H are:

1. Capture of an electron by an ionized atom; effects small.

2. Excitation from the normal state by electron collision or by absorption of a line of the LYMAN series; effects small.

3. Ionization, photo-electric, or by electron collisions. The predominant

cause.

4. The numbers of atoms, electrons, or quanta of any particular specification are assumed to be constant.

The mean density is taken as  $10^{-20}$ , giving a mean free path which lies between  $2.25 \cdot 10^{12}$  and  $2.25 \cdot 10^{11}$  cm, with an average duration of free path of the order  $40^{7}/T^{1/2}$  seconds. For all probable temperatures this is more than  $10^{4}$  seconds, while the life of excited H atoms is  $10^{-5}$  sec., or less. Collisions (and radiation as well) are accordingly regarded as insignificant in removing atoms from excited states.

CARROLL carries out extensive probability investigations as to the relative frequency of excited atoms in the various states and under different modes of excitation, and reaches the following general conclusions:

1. The H atoms are nearly all ionized,

2. The temperature is of the order of 10000°.

3. The Balmer emission lines are generated by electron captures by ionized atoms and their subsequent transitions.

4. The dilution of the radiation is of the order of 1012.

5. The density is of the order 10 21.

6. While Lyman absorption must occur, indeed not much less nor more frequently than ionization, it has little effect in producing Balmer lines.

7. The mechanism of ionization is presumably photo-electric rather than

electron collision or line absorption,

A late and coherent theory of the nebular phenomena in the planetaries, based in large part upon investigations of intensity and isophotal contours of individual monochromatic images obtained with slitless spectrographs, is due to Berman and Zanstra<sup>4</sup>.

Zanstra's results are based upon slitless spectrograms taken with an ultraviolet spectrograph in the primary focus of the Victoria 72-inch reflector, while Berman's were obtained with a two-prism quartz spectrograph in the primary focus of the Crossley Reflector at Lick. In both cases the monochromatic images were studied with registering microphotometers. Because of the brightness of

M N 90, p. 588 (1930).
 Harv Circ 335 (1928).
 PLASKETT'S answer, Obs 54, p. 49 (1931).

<sup>\*</sup> D. H. Menzel, The planetary nebulae. Publ A S P 38, p. 295 (1926); The dilution of radiation in a nebula, ibid. 43, p. 70 (1931); Physical processes in gaseous nebulae, ibid. 43, p. 334 (1931); L. Berman, A spectrophotometric study of certain planetary nebulae. Lick Bull 15, p. 86 (1930); H. Zanstra, Untersuchungen über planetarische Nebel. Erster Teil. Die Leuchtprozesse planetarischer Nebel und die Temperatur der Zontralsterne. Z I Astroph 2, p. 1 (1931); Publ Astroph Obs Victoria 4, p. 209 (1930). Earlier ruferences

these objects, most of the results were obtained on 6543 and 6572; BERMAN gives data also for 11 4593, 6826, 7009, 7027, and 7662.

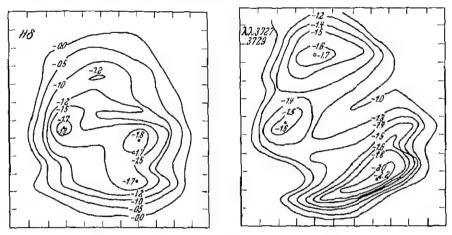


Fig. 25. Contour Diagrams of the H and  $O_{\rm H}$  Constituents of NGC 6543. (After Berman.) Note that the distribution of the two sorts of material is radically different within the same planetary.

Berman's isophotal contours are shown below in Figures 25 and 26, as an illustration of the power of the method. They give in compact form a mass of

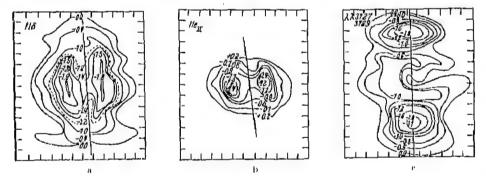


Fig. 26a, b, and c. Contour Diagrams of H,  ${\rm He_{H}}$ , and  ${\rm O_{H}}$  in the Planetary NGC 7009. (Berman.) The distribution of the three elements is entirely different;  ${\rm He_{H}}$  is smallest, and  ${\rm O_{H}}$  largest.

data as to the distribution of different elements or ionizations which is vastly more complete than earlier data. Berman's total integrated intensities of the different sources (from his Table VII) are given below in Table 41.

Taking the ratio of the intensity of  $O_{\rm HI}$  to  $O_{\rm H}$  as a rough measure of the degree of ionization, Berman determines the following percentages of ionized  $O_{\rm HI}$ :

Object	Ο <sub>111</sub> /Ο <sub>11</sub>	Fraction of O <sub>I</sub>	Object	опт/оп	Fraction of O <sub>H</sub> louized
6543 6826 6572	1; 0,47 1; 0,13 1; 0,08	83 % 87 92	7009 7027	1: 0,02 1: 0,02	98 98

Table 11. Total Integrated Intensities of Planetary Sources (BERMAN).

Source	λ	6543	6826	6572	7009	7027
OIII	5007	-1,54	- 1,67	2.00		
OIII	4959		-0,71	-2,09	2,52	-2,69
Om	4363		+1,86	-1,03	-1,44	-1,61
OIH	3445	_	7 1,00	-⊦ 1,84	- -2,1.1	+1,58
$O_{II}$	3726, 3729	+0.03	+0,20		_	+ 1,47
			70,20	+0,27	+1.37	+1,30
$H\beta$	4861	0,00	0,00	0,00	0,00	0,00
$H_{\gamma}$	4340	+0,44	+0.61	+0,60	+0.57	+1,02
113	4102	+0.86	+0,83	+1,16	+ L06	-J- 1,68
$H_{\ell}$	3970	(+1,27)	(+1,20)	(+1,48)	(-1-1,51)	
$H\zeta$	3889	(+1,65)	(+1,50)	(+1,82)	(-1,98)	(-1-2,09)
$H\eta$	3835	+1,95	+ 1,71	+2,05	2,42	(+2,40)
$H\theta$	3798	+2,34	-	+2,49	1-21-12	+2,74
$H_{t}$	3771			+2,61		+3,03
$H\varkappa$	3750		none.	+2,79	_	- -3,43
$H\varepsilon + 3867$	_	+0,72	- - 0,54	+0,61	10.20	_
$H\zeta + \mathrm{He}_{\mathfrak{l}}$	_	+1,12	+0.96	-1-1,43	+0,39	- -1,04
Hen	1606	,	0,70	1-1,43	+1,02	- -2,38
Hen	4686	_	-	_	+2,18	+1,03
Hen	4542	_	_		_	-1-3,60
Hor	4200	_	_	_	_	4,3
let( - - He <sup>11</sup> 5) j	4471	+2,47	+2,46	+2,61	+2,66	- - 3,04
Ho	4026	+2,36	-	-1-2,69	_	-1-3,54
110	3889	(+2,15)	(+1,97)	(+2,74)	(- - L,60)	- -4,0
$S_{II}$	4069, 4076		_		, , , , ,	
$N_{HI}$		1,		_	_	
7,111	4634					
Nm	4641	} ;	_		_ '	+2,69
CItt	4649	įJ į			'	1 2,09
?	3967	(+1,72)	(+1,40)	11100		
?	3869	+0,07	+0,05	(+1,26)	(十0,87)	(+i,56)
3 [	4571		70,03	-0,17	-0,56	- -0,04
?	3426		-	-	~	-+-4.15
,	3346			~ ]		-0.09
'	2210	_	_	-	1	-1-0.92

Zanstra considers two mechanisms of the luminous process:

- 1. The mechanism of re-combination.
- 2. The mechanism of electron impact, regarded as the cause of the "nebulium" lines.

Placing

$$x = \frac{h\nu}{kT},$$

he derives the following formulae for the determination of the temperatures of the central stars:

Mechanism 1, 
$$\int_{x_0}^{\infty} \frac{x^3}{e^x - 1} dx = x_0 \int_{x_0}^{\infty} \frac{x^3}{e^x - 1} A_x dx,$$

where  $A_r$  is the arbitrary measure of relative intensity derived from the observations. Similarly for

Mechanism 2, 
$$\int_{x_0}^{\infty} \frac{x^8}{e^x - 1} dx - x_0 \int_{x_0}^{\infty} \frac{x^8}{e^x - 1} dx = \sum_{\theta} \frac{x^4}{\theta^2 - 1} A_{\theta}$$

where the original paper should be referred to for the derivation and for the measures.

A table is then derived for the temperature as a function of the difference in brightness between the nucleus and the nebular matter, and from this the temperature values are derived for 22 planetaries. These are given below in Table 12, with the addition of Berman's values, when available. The latter author determined the temperatures separately for H, He<sub>I</sub>, and He<sub>II</sub> on the hypothesis of ionization and electron capture, and according to the theory of impact excitation for the  $N_1$  and  $N_2$  images. Both authors note that the greater the difference in brightness between the nebula and the nucleus the higher should be the temperature. "Failure to observe nuclei in planetary nebulae with the above spectral characteristics may reasonably be attributed to the high temperature rather than to the non-existence of the nuclear stars (Berman)." The mean of Berman's values have in general been taken.

It will be noted from this table that there is a considerable measure of agreement in the values derived, and that the authors both attribute exceedingly high temperatures to planetary nuclei. Closely similar results as to a high average nuclear temperature have been obtained through a number of methods of analytical attack by Vorontsov-Velyaminov<sup>1</sup>.

Table 12. Approximate Temperatures of Planetary Nuclei, derived by Zanstra from Luminosity Differences, Nucleus-Nebulosity, with the Addition of BERMAN'S Values.

	Object $m_{\mathrm{meb}}$ , $m_{\mathrm{nur}}$ if		,	Temperatures		
Object		ır	ZANSTRA	BERMAN		
650	16,6	(),()	6,7	85 000°		
1535	11,6	8,8	2,8	38 000	}	
1952	(5,0	8,4	7.5	100 000		
2438	16,6	9,8		85000		
2392	10,0	8,4	1,6	31000	1	
3232	11,7	7,1	4,6	55000	1	
3587	14.3	0,4	4,9	55000		
4361	12,8		2.7	37 000		
1 4593			-	-	25000°	
6210	11,7	8,5	3,2	40000	1	
rel 4.5	19	10,4	8,6	140000	i	
6309	14.5	10,7	3,8	45000	1	
65:13	11,3	8,1	3,2	40 000	33 000	
6572	10.5	8,4	2,1	34000	43 000	
6720	l·1.7	8,8	5,0	70000		
6804	13,4	11,8	1,6	31000	į	
6818	14.9	8,8	6,1	70000	-	
6826	10,8	8,1	2.4	35000	27 000	
6853	13,6	7.3	0.3	75000		
0905	14.5	10,7	3,8	45000		
	12,8	12,2	0,6	28000	1	
7008	11,7	7,2	4.5	50000	40 000	
7000	111/	1		-	50 000+	
7027 7662	12,7	8,4	4.3	50000	i	

33. Evolutionary Status of the Planetary Nebulae. There seems fittle doubt that the class of the planetary nebulae must be regarded as an exceptional, and doubtless very rare, branch of cosmical evolutionary development. We must consider them as presumably of catastrophic origin; Iusus naturae impossible to fit in any orderly fashion within a reasonable gamut of stellar evolution.

ч R A J S, pp. 15, 122 (1931).

The arguments for such an exceptional status are two fold

t their rainty of occurrence. Fewer than 150 are it present known. It is quite probable that the nucleus of a planetary is in all cases a Worr RAST star These, too, are an exceptional class, and the number known at pre-em excluding the planetary nuclei and those in the Magellanic Clouds, is 100 or about that of the planetaires. Because of this rarriy, the planetaires can nor went be placed either at the beginning or the end of the general course of stelling evolution, except by making most improbable assumptions. There have been attempts, also, because of their small numbers, to link up the planetary clawith the novae, these attempts can not be said to have been very succession and meet with many difficulties as to spectrum and frequency

The planetaries are quite certainly fewer than 0.01% of the number of stars which may be assumed to be roughly within the apparent magnitude muniof the planetary nuclei. If thus appears impossible to postulate the planetary stage as one through which all stars pass, for it would then be necessary to assume that existence in the planetary stage can be but a negligible period in the his

history of a star, and only a lew thousand years in duration

2 If the attempt is made to place the planetaries at any point in the stellar progression, then relationship with the Class B stars would seem most probable in fact, any connection whatever with red stars seems entirely out of the question Here we meet the almost insuperable difficulty caused by the observed last that the average space velocity of the planetaries is live times that of the average Class B star

LUDENDORM, however, has assembled some data which partially remove this difficulty. For known double stars of Classes Oc to Bo, he assembles the values of  $f = a/(1+a)^3 M \sin^4 t$ , where  $a - m_0/m_1$ , and M $m_{\lambda} + m_{\gamma}$ far as is known,  $a/(1+a)^4$  is always less than 1, hence a large value of f will indicate a large value of M. CAMPRILL and MOORI had already derived outle large values for the masses of certain planetaries. The radial velocities of the centers of mass of the systems were then freed from the effects of the solar motion and the K-term, giving a quantity  $\gamma_0$  . The available material was then grouped in the class subdivisions Oe to B5, and B8 and B9, following the values of I as follows

Value of /	10 lugar than the me Classes Octo B5, proportion	m value 2.5 km/sec Classes 198 and 119, proportion	
0,75	7 out of 12, 58%	2 Stars 100%	
0 10 to 0 75	5 out of 13, 38%	2 out of 5, 33%	
0,10	0 out of 12, 0%	0 out of 5, 0%	

There is thus indicated a marked increase of velocity with increasing mass, with the conclusion that the systems with largest mass possess velocities which approach those of the planetary nebulae, hence the deduction that large velocities may be expected for bodies with the masses attributed to the planetaries, and that their large velocity, on this assumption, is no bar to a connection between these objects and the O and B stars. There remain the difficulties as to the small frequency of these objects, in which respect they are still exceptional

Certain of the recent planetary theories of the quantum type postulate nuclei of tremendous temperatures, 50000° to 100000° abs, or more if these high values are substantiated by tuture observation and analysis, it will be merely one more proof of their exceptional nature

<sup>1</sup> Uber die Beziehungen der planetarischen Nebel zu den Helmm-Steinen AN 212, P 3 (1920) and 221 P 357 (1924)

## d) The Spirals.

84 Historical Note on the Spirals. In the cosmogonies of the eighteenth century, most nebulae were regarded as composed of stars, but too distant to be individually resolvable. Certain clusters and stellar aggregations which had appeared nebulous with lower powers had been found to be resolvable when higher powers or larger telescopes were employed. Hence by analogy, reasonable enough in the light of their existing data, all nebulous objects were believed to be similarly resolvable. Huygens wrote in 1682 <sup>1</sup>

"Num caeterae nobulesae olim existimatae, atque ipsa Via Lactea, perspicillo inspectae nullas nobules habere comperiuntur, neque aliad case quam plurium stellarum congeries et frequentia"

GATHEO, (ASSINI and MICHELL regarded nebulae as thus resolvable; HALLEY, DERHAM, LAMBERT, KART, and LACAILLE maintained the existence of nebulous masses

Such was also Sir William Herschel's earlier belief, namely, that all objects of a nebular texture could be resolved into stars if only sufficient power could be applied. Certain of his earlier papers contain references to other Milky Ways and to distances of the order of 10<sup>20</sup> km, which have striking resemblances to the conclusions of the island universe theory. These beliefs were abandoned by 1791 through the conviction that there were many objects which were intrinsically nebulous in character, and impossible to resolve into stars. The cosmogonical speculations of Kant, Lahbert, Michell, and others, may be dismissed as philosophical rather than observational deductions.

It is an interesting fact that the spiral nature of these objects seems completely to have escaped the Herschels. It is doubtful whether a single one of their objects contains this word in its description; it certainly is not given as an abbreviation, nor does the concept occur in any of their notes or papers describing the various types of nebulae observed. The spiral nature of these colestial objects was first discovered by the Earl of Rosse, with his 6-foot reflector. The spiral character of 5194 (M51) was first noted in 1845, and announcement was made in 1840.

Von Humbot pr's view at the time of the publication of his Kosmos (4845—50) was essentially the same as Herschel's later position. Cortain nobulous objects were regarded as truly gaseous, while others of different texture were thought to be composed of stars. For the latter objects you Humboldt coined the expressive plunes, "Weltinsel", which is perhaps the parent of the more modern "Island universe".

A completely different phase was brought into the puzzling problem of the nebulae by the first spectroscopic observations. It was at once recognized that nebulae showing bright emission lines (the diffuse and planetary classes) must be truly guscous. Here, again, an insufficiently evidenced analogy was to impede unduly the final solution of the enigma. Because of the great numerical preponderance of the objects now known as spirals, it was found that the majority of the "nebulae" showed no bright lines, but a continuous spectrum, in which much later the more prominent Praunnores lines were detected. These were frequently called "white nebulae", a name coined for them by Young. It was tacitly assumed that these objects also must be gaseous, premising some as yet unknown form of spectral excitation, or reflection effects from Milky Way stars.

Opera Varia (1784), p. 540.
 Kosmos 3, p. 487, et passim.

Brit Am Report (1849), p. 53

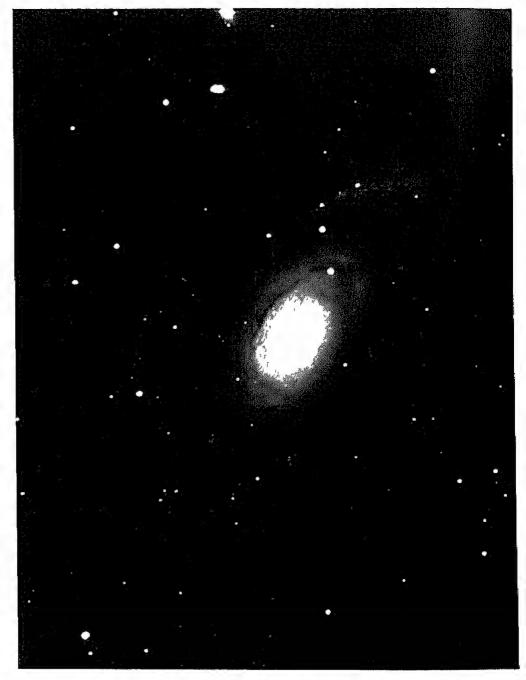


Fig 27 The Spiral NGC 3031 (M81) (Lick Photograph)

To this latter theory, the fact that the spectra of the white nebulae were later found apparently identical with those of solar type stars gave some measure of support

It had long been known that the "nebulae" were to be found in greatest numbers in the regions about the galactic poles, but it remained for PROCTOR1 and WATERS\*, through their conclusive and convincing charts of distribution, to emphasize beyond question the radical differences between the class of nebulae as a whole and the stars as to predominant galactic arrangement (See Plate I. Figure 28, at the and of this volume, and Figure 29)

So keen a thinker as HERBERT SPINCER, in fact, regarded this peculiar grouping of the "white nebulae" about the galactic poles as a conclusive proof

of alliance with, rather than dissociation from the stars

"In that zone of calculationary where the stars are excessively abundant, achains are rare, while in the two opposite celestial spaces that are furthest removed from this zone nebulae are abundant. Scarcely any nebulae ite near the galactic circle, and the great mass of them lie round the galactic poles ('an this is mere coincidence? When to the fact that the general mass of the arbulue are antithetical in position to the general mass of the stors, we add the fact that the local regions of nebulae are regions where stars are scarce, and the further fact that single nebulae are habitually found in comparatively sturiess spots, does not the proof of a physical connection become overwhelming?" [II SPENCER, I be Nobular Hypothosis (1854), p 112.]

"Have we, on the other hand, any satisfactory reasons for regarding the nebulae as can we indicate any argument which may be looked upon as definitely external gulaxics? pointing to such a conclusion? I know not of one" [Proctor, the Universe of Stars

(1878), p 105 j
"The question whether nebulio are external galaxies hardly any longer needs discussion
"The question whether nebulio are external galaxies hardly any longer needs discussion It has been answered by the progress of research. No compotent thinker, with the whole of the available evidence is fore him, can now, it is sufe to say, maintain any single nebula to be a star system of co-ordinate rank with the Milky Way" [Clerker, I be System of

the Stars (1905), p 119]

"Opervation and discussion of the radial velocities, internal motions, and distribution of the spiral nebulae, of the real and apparent brightness of novae, of the maximum luminosity definitely to oppose the Island Universe' hypothesis of the spiral nebulae Publ A S P 31, p 261 (1919) ]

Here and there occusional voices were raised in protest, but in view of the prevalence of such ideas, the definite pronouncements of Schrinks and others had little effect

(Pollowing a description of a spot regram of 71/4 hours reposure time, which showed the spectrum of the Nebula of Andromeda to be essentially similar to that of solar-type

stars)
"Der Andromedanobel gehört zur Klasse der Spiralnebel, die sämtlich ein kontinulerliches Spektrum geben. Nachdem nun die bisherige Vermutung, daß die Spiralnebel Stern haufen selen, zur Sicherheit erhoben ist, liegt es nahe, dieses System mit unserem bizsternsysteme zu vergleichen und auf die große Abnilehkeit des letzteren speziell mit dem Andro-" [] SCHKINKE, AN 148, p 327 (1899) ] modunula I liinzuweben

The discovery of novae in spirals by Ritchey and Curtis in 1917. followed by a large number of similar discoveries by others (see clph 52), gave a new unpetus to the then almost discarded "island universe" hypothesis. The theory was at once strongly supported by ( parist, and others, and by assuming essential similarity between galactic and spiral novae, very great distances were derived for the spirals SEARRS's results on the color of the spirals, the influence of

<sup>1</sup> M N 20, p 337 (1869) <sup>a</sup> M N 33, p. 406 (4873)

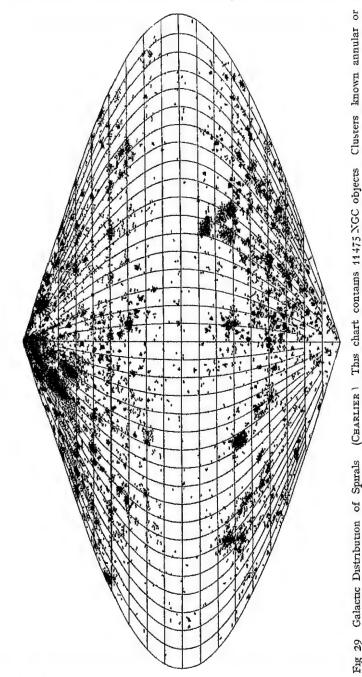
Publ A S P 29, p. 480, 210, 213, 257 (1917), Lick Bull 9, p. 108 (1917)
 If D Custrs, The Nobulao, in Adolfo Stabl Lectures (1917), Modorn Theories of the Spiral Nebulao, lecture before Weeth Acad Sc March 1918, 9, p. 218 (1919), H. Shape INY and H D CURTIS, The Scale of the Universe, a debate hold before the Nat Acad Sc at Washington, April 26, 1920, published in Bull Nut Res Council 2, part 3, No 11 (1921) SHAPT BY's carlier views as published in Publ A S P 30, p 53 (1918); 31, p 261 (1919), and in this debate have since been modified to strong support of the spirals as external gulaxies

While the chart contains the diffuse nebulae these are comparatively few

and occur near the galactic plane. For all practical purposes, this is the most complete chart extant of spiral distribution

planetary nebulae, and stellar nebulae were excluded

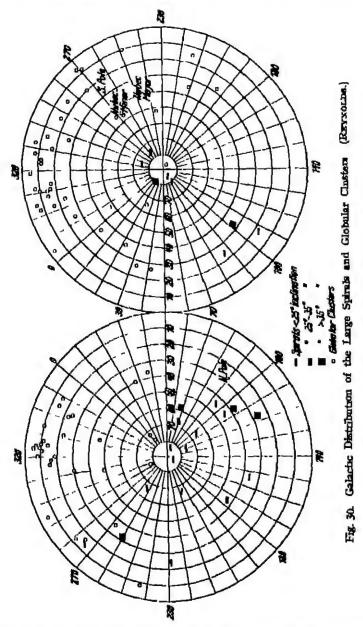
CHAMBERLIN and Moulton's planetesimal hypothesis, which suggested the origin of the solar system from a relatively small spiral structure, and vanMaanin's



values of the internal motions in the spirals, secured in 1922 and following, for a time made full acceptance of the theory difficult to many. All doubts as to

the island universe character of the spirals were finally swopt away by Hubble's discovery of Cephoid variables in these objects in 1924

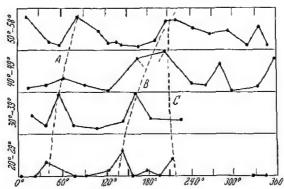
At present it may safely be said that the combination of the lines of evidence



secured from the peculiar space-distribution of the spirals, their enormous radial velocities, their star-like spectrum, and the occurrence of novae and Copheld variables within their structures, has nullified all former objections. The theory that the spirals are conglomerations of stars, comparable in many cases with

our own galaxy in size and in number of component units, is now universally accepted.

35 Apparent Distribution of the Spirals, Super-Galaxies<sup>2</sup>. The fact that there is a marked concentration of "nebulae" about the galactic poles has long been known, and has been the subject of numerous papers. This tendency, first clearly indicated by Procion and Walers, is shown as well in all subsequent



lig 31 Variation of Nebular Distribution with Galactic Longitude (Slares) Distribution of nebulae in the north galactic hemisphere according to galactic longitude (abscissae) Four curves for the latitude intervals are noted in the margin A, B, C, are the more-or-less hypothetical lines of maximum frequency I and C correspond to the maximum in longitudes 50° and 220°

studies of the smaller spuals. All agree in showing that the concentration about the north galactic pole is greater than about the southern, and in indicating a marked falling of in numbers as the galactic plane is approached. This diminution is clearly shown in Curis' counts of small objects (Lick Publ 13)

Calactic Intitudes	Number per square degree
+15° to +90° -15° to -90° -30° to -15° -30° to 30°	31 28 21

Such variations in distribution have been more thoroughly studied by SLARLS,

who finds definite differences with galactic longitude. See his Figure reproduced as Figure 31

That our own galaxy should thus be situated about midway between two tremendous groups of several million galaxies each, and be, by such unique location, still more definitely an "island universe", is, of course, not an impossibility, whatever objections may be uiged against this on the score of probability. This uniqueness of location and this exceptional isolation must be accepted, however, unless one prefers to assume a reasonable degree of uniformity of distribution for the 10<sup>7</sup> or so galaxies accessible to our telescopes, and to postulate, from the analogy of the phenomenon seen in so many spirals (see ciph 42), that a similar tremendous ring of occulting matter in our galactic plane and for the most part outside the Milky Way structure, cuts off from our view the spirals that would otherwise be seen in the zone between +15° and -15° galactic latitude

A recent development of the highest interest is the substantiation by Humason of the arrangement of certain spirals in great groups, or "super-galaxies",

1 I his acceptance is not quite unanimous, cf ciph 58 Also "La maneia de formaise de las nebulosas espirales es indudablemente la postulada poi Chamberlin y Moulton para explicar el origen del sistema solar, el paso de un cuerpo a poca distancia de otro, con la expulsion de materia en forma de dos corrientes o brazos Ahora se sabe que las espirales son sistemas mas pequeños y muy probablemente dependientes del sistema galáctico" C D Perrinl, Asoc Cult de Conf de Rosario (Argentina) No 2 (1930)

2 R A Proctor, M N 29, p 337 (1869), S Waters, ibid 33, p 406 (1873), 54, p 526

<sup>2</sup> R A Proctor, M N 29, p 337 (1869), S Waters, ibid 33, p 406 (1873), 51, p 526 (1894), J H Ri ynot Ds, ibid 81, p 129 (1921), 83, p 147 (1923), 84, p 76 (1921), R F Santord Liek Bull 9, p 80 (1917), F Herizsprung, A N 192, p 261 (1912), C Easton, ibid 166, p 130 (1904) C Abbe, M N 27, p 264 (1867), S I Bailey, Sc N S 25, p 565 (1909), A R Hinks, M N 71, p 588 (1911), E A Fath, Pop Asti 18, p 544 (1910), F Slaris, Ap J 62, p 168 (1915), P Doig, J B A A 33, p 238 (1923)

which possess contiguity of location and have, moreover, recently been found to possess radial velocities of nearly the same size for such of their component members as have been observed. Their special interest lies in the strong resemblance of such a structure of groups or super-galaxies to Charlier's theory of an infinite universe. As this characteristic grouping will be discussed in some

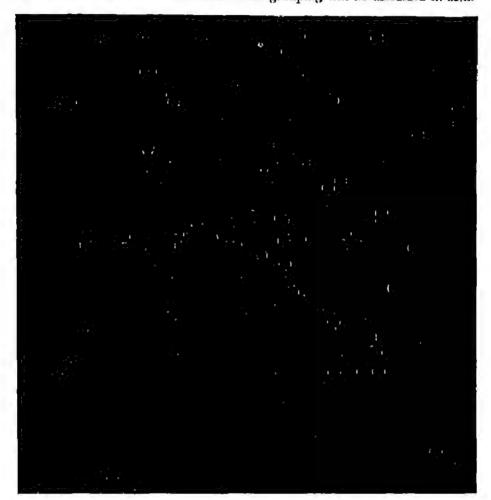


Fig 32 Cluster of Small Spirals (Lick Photograph) This is a portion of the rich region at 12 55, | 28° 50′ It is 38′ 39′ in size, and shows 249 small spirals and elliptical objects

detail in ciph 56, 68, and 78, the details of such super-galaxies will be left for the Sections noted.

86. The Number of the Spirals<sup>1</sup>. Early in his program of photography with the Crossley Reflector, and when the total number of regions observed was relatively small, Krkier discovered a very large number of very small and hitherto

<sup>1</sup> J E INERLER, A N 151, р 1 (1899), M N 60, р 128 (1899), I Jek Publ 8, Introduction (1908), С D Ренкив, Ар J 20, р 356 (1904), I Jek Bull 3, р 64 (1904), А J 29, р 70 (1915), Н D Сияти, Publ A S P 30, р 159 (1913), Proc Amor Phil Soc 57, р 513 (1918), Lick Publ 13, р 12 ff. (1918), К J РАТИ, А J 28, р 73 (1914), К P SARFORD, Lick Bull 9, р 80 (1917), Р Н SKARRS, Ар J 62, р 168 (1925), К Ниявык, Science, Suppl 73, No. 1904 (1931)

unrecorded nebulous objects in all regions well removed from the Milky Way. At that time he estimated the total number accessible in the sky with the Crossley Reflector as 120000. When it is recalled that only about 11000 nebulae had been catalogued up to 1900, the increase of roughly 1000% made by Keptek stands out as a contribution to cosmogony of the highest rank.

The question has since been investigated by Pierrine, (URIIS, PATH, SAN-LORD, SEARES, and HUBBLE The various estimates are given below in tabular form

Keller	1899	120 000		
PLRRING	1904	500 000	(eventually	a million)
CURTIS	1913	700 000	,	
ГАТН	1911	162 000		
CURTIS	1918	722000	(eventually	a million)
SLARES	1925	300 000	,	
HUBBLL	1931	30 000 000		

There is little value in reviewing here the efforts which have been made to reconcile the smaller estimate of FATH (162000) and the larger ones of PERRINI and CURTIS (10000000  $\pm$ ), CURTIS' support of these larger values may be found in Lick Publ 13. The great power of the 100-inch telescope has shown clearly that the number of small objects of the spiral class is very great.

As pointed out by W W CAMPBELL, there is less difference than appears at first sight between Hubble's value and those secured from the Crossley surveys, when one takes into account the larger volume of space accessible to the larger instruments. Hubble's estimate is for the entire number of such objects existing in the spherical volume of space whose radius is the distance of the most remote objects found on the Mt Wilson plates, without regard to those occulted in the Milky Way area. As, other things being equal, the 100-inch reflector should penetrate 2,83 times as far into space as the 36-inch (1055b) Reflector, the former should therefore command a volume of space about 22,0 times the volume accessible to the latter. Assuming that the distribution of these objects in space is roughly uniform, and making reasonable additions to the Perrine-Curis totals for those objects which are prevented from recording then images on the negatives by obstructing materials in our Milky Way system, it will be seen that there is a very satisfactory agreement in the two sets of estimates with regard to the density of distribution of the spirals. No one can predict, naturally, whether this observed density of distribution continues indefinitely See further ciph 77-79

- 37. Conspectus of Forms Assumed For the purposes of this treatment, the spirals are considered under the following main headings
- 1 True spirals, objects which show the spiral arms so characteristic of the class
- 2 Barred spirals, marked by a nearly straight band across the nuclear portion
  - 3 Elliptical objects, with no spiral structure discernible by present resolution
  - 4 Irregular and Magellanic type spirals

While the field is conveniently divided thus, there is a very wide difference in the forms assumed. The following examples, taken for the most part from the list and descriptions in Lick Publ 13, will give a partial illustration of such variation in details of structure. Edgewise or greatly clongated spirals have in general been omitted, as in such the essential features are masked by the inclination of the object to our line of sight.

There is no very large amount of agreement as to the relative proportions of the different types of spirals. The most important factor in the percentages found seems to be, as would be expected, in the aperture of the instrument used

HARDCASTLE's counts of the brighter nobulae on the Franktin-Adams star charts, after the exclusion of objects evidently of the diffuse type, give 173 as spiral, 233 of the elliptical type, and 327 objects so small as to resemble star



Fig 31 'The Magellank Lype Spiral NGC 4449 (Mt. Wilson Photograph)

images Shapleys finds a very small proportion of spirals in the 2829 objects catalogued in Hary Ann 85, p 413 (1924)

Spheroklal		,				80%
Spindle						12%
Oval .						7 %
Spiral			len	Н	than	1 %

However, in his study of the Coma-Virgo cluster of galaxies<sup>8</sup> he reports a slight preponderance of the bona-fide spiral type, 30 to 27, and of 167 objects in the Coma A cloud, 48% are classified as spiral and 5% as irregular Shapley and Ames Ind much smaller proportions on the Bruce plates (8% spiral and 4% irregular), but admit that "obviously the recording of spiral structure is

<sup>&</sup>lt;sup>1</sup> M N 74, p 699 (1914).

<sup>\*</sup> Hary Bull 838 (1926)

Harv Bull 808 (1924)

<sup>4</sup> Hary Bull 876 (1930).

largely a matter of telescopic resolution" Doubtless the most trustworthy proportions are those found by Hubbli in his detailed and valuable monograph, "The Extra-galactic Nebulae", in Ap J 64, p 321 (1926), as follows

Flliptical	23%
Normal and barred spirals	71%
Irregular	3 %

It is the belief of the writer that the proportion of true spirals may be even larger because of instrumental limitations in recording the smallest objects of the

spual class, see ciph 40

38 True Spirals. These are the "normal" spirals of Hubbit, and the term is self-explanatory, in these the characteristic spiral whorls are more or less clearly seen, nearly always making then start from a nuclear portion at points very closely 180° apart. They vary in size and in the distinctness with which the spiral arms are shown, from minute objects where faint traces of spiral characters can just be made out, to enormous structures like 224 (Andromeda) and 598 (M33), where the spiral arms are clearly shown, and where the obtainable scale is such that many portions of the arms can be resolved into stars.

The nuclear portion shows considerable variation in both the true spirals

and the barred variety

Nuclear portion		1 × unples				
Rather large	$\begin{cases} 151, \\ 4011, \end{cases}$	221, 1736,	221, 5218	2903,	1501	
Small and bright	29,	200,	628,	772	3137	
Smart and origin	334 F, 3938,	3180, 1826,	3523, 5033,	3650 5055,	\$ 140	
Irinuclear?	7752					
Quite faint	253,	3556,	1321			
No nucleus apparent	1337,	2537,	7511			
There is also a wide variation in th	e character of	the wi	orls			
Delicate and very compact	188,	2775.	5055,	5800		
Rather compact	278,	1068,	2811,	1730		
Moderately open	221,	4826,	5191	5		
	[ 598,	628,	697,	1637.	1642	
Open, generally with knots	2532, 334 h	3147.	3181,	3108.	41334	
open, generally with knots	1 334 h	3686,	3726,	3892	3035	
	(4321,	5326				
I wo branched or S-shape	ſ 3625,	1051,	4236,	5217.	5 (10)	
•	l 6217,	6296,	7610			
Single whorl?	7393					
With satellite		(near	16 (2).	5101.	1/53	

39. Barred Spirals The designation "barred spiral", introduced by Hubbit is far preferable to " $\varphi$ -type spirals", used earlier by Curits. These interesting objects have as their characteristic feature a straight or nearly straight barrof matter across a nucleus which is generally rather indistinct. Sometimes the whorls will apparently start from the ends of this bar, in other cases, the whorls may form nearly a perfect ring with the bar as a diameter. See Figure 34, where four of these objects are shown

Among the barred spirals are

Barred spirals	$\begin{cases} 613, \\ 2859, \end{cases}$	1300, 3351,	1326, 3367,	1530, 3501, 5921,	1781 3691
Barred, Saturn-shaped	( 4340, 936,	4391, 1455	1725,	5921.	7179

Hubble (1 c) lists 59 barred spirals, and it would seem that it is a by no means rare type. See ciph 62-64 for references to its possible significance in theories of spiral structure.

40. Elliptical Spirals; the Provenance of the "Minute" Spirals. The type example of this class is 221, the bright oval companion south of the Great Spiral in Andromeda Hubbi P lists 93 objects of this type, ranging from E0 (practically round) to E7 (considerably clongated), at which point the transition to the class of true spirals is held to occur Strictly speaking, this class contains the overwhelming majority of the spiral class, simply because the smallest flecks are necessarily recorded without distinguishable structure

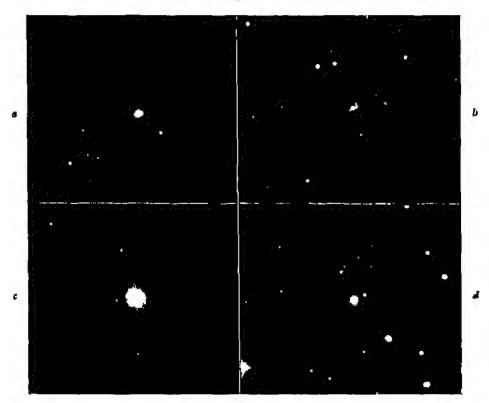


Fig 34 Four Burrod Spirals a NGC 1300, b NGC 1530, c NGC 3351; d NGC 5921 (Link Photographs)

Some doubts have been expressed as to the provenance of the countless very small round or elliptical objects, and their right to be classed with the genus of spirals. The writer in 1918 made the following generalization (Lick Publ 13, p. 12).

"It is my belief that all the many thousands of nebulae not definitely to be classed as diffuse or planetary are true spirals, and that the very minute spiral nebulae appear as textureless disks or evals solely because of their small size. Were the Great Nebula in Andromeda situated five hundred times as far away as at present, it would appear as a structureless eval about 0',2 long, with very bright center, and not to be distinguished from the thousands of very small, round or eval nebulae found wherever the spirals are found There is an unbroken progression from such minute objects up to the Great Nebula in Andromeda litself, I see no reason to believe that these very small nebulae are of a different type from their larger neighbors."

Though this conclusion has been objected to as a "daring extrapolation", the writer feels that all the ovidence as to distribution, character, radial velocity,

etc, which has been obtained since 1918, serves only to strengthen this opinion, and were he re-writing it today, his only mod fications would be minor changes in the phrasing so as to avoid the word "nebula" as far as possible. The writer finds no escape from the conclusion that all the objects of the spiral class, near or distant, 2° or 5" in diameter, with or without visible whorls, round, spindle-shaped or clongated, are stellar aggregations of structures closely similar, and presumably of the same order of actual size. He places the smallest objects seen on the Crossley plates, 3" to 5" in diameter, at a probable distance of 10° ly, at this distance an object 3" in diameter would have a linear diameter of 14500 ly.

There are doubtless a considerable number of objects like 221, whose projected outline is that of a slightly elongated ellipsoid, with any other exterior formations either non-existent or too faint to be recorded. As is well known, the type form of the spiral is a flat, discordal structure, roughly circular in plan, and with thicknesses  $^{1}/_{5}$  to  $^{1}/_{10}$  the diameter. When seen edgewise or nearly so, such objects will appear only as narrow spindles, with all evidences of spiral structure obliterated by the high inclination to the line of sight, whereas objects like 221 will present nearly the same cross-section from any point in space. These may

be regarded as, in effect, ellipsoidal star clusters of gigantic size

That the vast majority of the small round and elliptical objects are necessairly of the same type as 221 does not follow, though their precise nature, on any assumption, requires some measure of extrapolation. The detection of spiral structure is very markedly a function of the apparent size of the object, of the aperture of the telescope and its focal length, of plate grain and exposure time. Any of the considerable number of large spirals with somewhat accentuated central condensations or nuclear regions, if removed to several hundred times then present distance, would lose all details of spiral structure through the limits of the photographic process. The relatively very much brighter central portions of such objects as 224 and 598 require no excessive exposure times at their present distances, for many of these objects an exposure of a few minutes is adequate to obtain a legible record of the nuclear condensation, while an exposure of twenty times this length will be needed to show the whorls as strongly. Assuming these objects removed to a distance 100 times as great, our present reflectors will still be able to obtain a record of the nuclear portions in an exposure of one to three hours. But, for the same object at the greater distance, any adequate record of the outlying whorls will now require an exposure of ten to twenty hours, if such were possible without undue sky blackening, even then, because of the minuteness of the structural features, these would be further obliterated by the factors of plate grain and telescopic resolution

41. Irregular and Magellanic Type Spirals There are a number of quite inegular objects of the spiral class, where the spiral structure is only faintly indicated, or entirely lacking, in some a looped or falcated structure made up of systehes as green Among each shreet are spiral spirals.

of patches is seen. Among such objects are

1 428, 1156, 2359, 2537, 2777 3034, 3077, 4214, 4401, II 2571 4618, 5144, 7309

Even more inregular are objects of the Magellanic type, of which our best examples are the Magellanic Clouds and such objects as 4449 (see Figure 33 and 35). While lacking the characteristic spiral formation, the Magellanic Clouds must be regarded as among our most "valuable" spirals because of their nearness (0,1 1061 y) with the consequent facility of study of individual components

42. Occulting Matter in the Spirals, and its Bearing on Observed Distribution. No description of the forms assumed by the spirals would be complete

without a reference to the occurrence of non-luminous occulting matter, the evidence of the spirals seen edgewise or nearly so proves that these are relatively

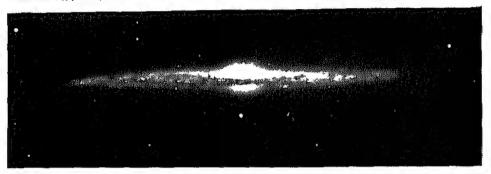


Fig 35 The Large Magellanic Cloud. (Harvard Photograph.)

flat, round structures, and the occulting matter seems to occur in a peripheral band around the circumference. The characteristic has long been known, and was the source of some of the "bifid" and "double" objects noted by the Han-

SCHLIS and ROSSE CURIS has treated this subject in lick Publ 13, with illustrations showing the phenomenon in 77 spirals. This occulting matter may be

1 Irregular dark patches, generally in the central portions of the spiral, as in 147, 205, and 2655



lug 36 The Edgewise Spiral NGC 1565 (Mt Wilson Photograph)

2 As manifested in spirals whose planes make a moderate angle with the line of sight, where one side is definitely fainter than the other, or seems to extend to a smaller distance on one side of the major axis. Examples, 2083, 2841, 4192, and 5033

3 Dark lanes clearly in evidence on one side of the major axis in spirals

of small inclination to the line of sight, as in 3623, 4 (29, and 3169)

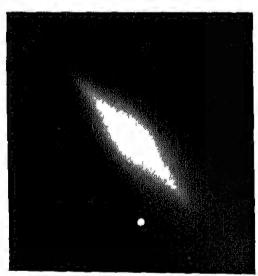


Fig 37 The Edgewise Elliptical Spiral NGC 3115 (Mt Wilson Photograph)

4 Spirals seen almost exactly edgewise, and showing indubitable evidence of a peripheral equatorial occulting ring, as in 4565 (finest example of the class), 891, 4591, and 5746

Though not observable in all edgewise spirals, the phenomenon is so frequent a one that it must be regarded as a very common characteristic of the spirals as a class. This evidence, by analogy solely, may then be iegaided as lending considerable support to the hypothesis that a similar peripheral band of occulting matter in the plane of our galaxy, and in large part presumably outside its structine, serves to cut off from our view the distant spirals which he near the projection of our galactic plane in space1

Indirectly, also, such a theory lends support to the belief that our galaxy is but one of many similar structures, as held by Exston and others, and more recently supported by Trumpler's investigations of the amount and localization of absorption within our galaxy. Though this theory is supported only by the

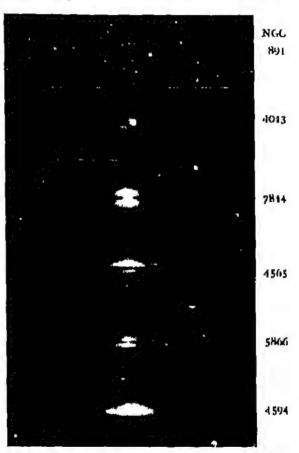
<sup>1</sup> Cf also R I SANFORD Lick Bull 9, p 80 (1917)

significant analogy of numerous external galaxies, it offers perhaps the best explanation of the curious fact presented by the peculiar distribution of the spirals, found in greatest numbers near the galactic poles, but almost never seen within the actual Milky Way structure, a phenomenon for which no other adequate explanation exists

48. Proper Motions of the Spirals. Regarded as an external galaxy, a relatively close spiral at a distance of 10° ly, and assumed to possess a motion

of 104 km /sec across our line of sight, would exhibit an annual proper motion of 0".007. If we limit the velocity across the line of sight to but 10" km /sec, a quantity of the order of the radial velocities of the larger and nearer spirals observed to date, the annual proper motion will be but 0",0007 Bearing in mind the very difficult character, from the standpoint of measurement, of even the best spiral nuclei and knots, together with the relatively short time interval yet available (ca. 30 -) years for photographic comparison and ca 75 years for visual), and the minuteness of the probable proper motions of these objects, the conclusion seems certain that the definito detection of proper motion in the spirals is far beyond existing methods and obtainable observational data

A very large amount of honest and painstaking effort has been expended on this problem, beginning with the carefully determined positions of such observers as



ldg 38 Coculting Rifocts in Spirals. (Lick Photographs.) Photographed by H D Currus with the Crossley Reflector

1)'Arrest three-quarters of a century ago, and extending to the photographic

<sup>1</sup> Van Maanen, Mt Wilson Contr No. 111 (1916), No. 136 (1917), No. 158 (1918), No. 482 (1920), No. 204 (1921), No. 237 (1922), No. 270 (1923), No. 290 (1925); No. 321 (1926), No. 356 (1928), No. 391 (1929), No. 405 - 8 (1930), C. Wirtz, Strassb Ann. 4, p. 412, 304 (1912), A N 203, p. 497, Criticized by Kobold and Serlicher, p. 299 and 305 (1917), 206, p. 409, 246 (1918), S. K. Kobtinsky, Bull Acad St Pôtersb (1916), p. 871, K. Rrimmutt, Pols Heidelberg 7, p. 444 (1915), O. J. Lee, Pop Astr 34, p. 492 (1916), J. M. Hawkes, Dete Che Publ. 3, p. 435 (4923); C. O. Lambland, Pop Astr 22, p. 631 (1914), 24, p. 658 (1916), Lowell Bull No. 73 (1916), F. R. Harnard, A. J. 30, p. 175 (1917), K. Lurdmark, Pop Astr 30, p. 623 (1922), Publ. A. S. P. 44, p. 408 (1922), M. Wolff, Publ. Hoktolberg 3, p. 409 (1909), 6, p. 34 (1913), A. N. 190, p. 229 (1912), 202, p. 447 (1916)



Fig 39 The Spiral NGC 7217 (Mt Wilson Photograph) An excellent example of a spiral with compact and delicate whorls

measures and discussions of van Maanen, Lampland, Lundmark, and others, in recent years

With a full appreciation of the sincere and careful investigation which has been devoted to this difficult problem, but with the conviction that any tabulation of the often contradictory results would only mislead and cause confusion, the

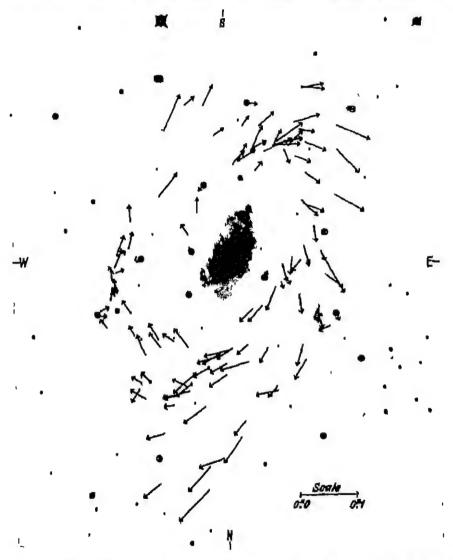


Fig 40. Internal Motions in NGC 3034 (MSI) as determined by VAN MAANES (VAN MAANES). This spiral has been chosen as a typical example of VAN MAANES's derived motions. It will be noted that the motions are prevailingly outward along the spiral arms. The arrows indicate the magnitude and direction of the mean annual motions, and their scale (0".1) is indicated on the illustration. The comparison stars are inclosed in circles.

author profers to omit any discussion of past proper motion results on the spirals, and to refer the reader to the references quoted, VAN MAANEN'S values for several

will be found in ciph 45. We have as yet no certain knowledge of the proper

motion of any spiral

44. The Spirals as a System of Reference There is, however, a possible interesting by-product of the apparent total lack of a motion of translation in the spirals. Then tremendous distances, and then lack of detectable proper motion, give us a large number of essentially "stationary" points of reference, which should eventually prove to be of great importance in studies of the rotation of our own galaxy. The assumption of average fixedity seems amply justified, for small motus peculiares ought to be at random and to disappear in the mean If then two sets of measures at a considerable time interval could be made of a large number of small and almost stellar spirals uniformly distributed in galactic longitude, preferably not more than 30° from the galactic plane, and referred to adjacent faint stars (magn 18+), it is concervable that results of great value might be secured as to the rotation of the galaxy, local irregularities, etc Were our galaxy rotating in 108 years, stars in the peripheral regions would be expected to show tangential annual proper motions with reference to such points d'appur of the order of 0",01, which might be detectable with some certainty in 100 years

45. Internal Motions of the Spirals, Visual Determinations. At a distance of 10°1 y, annual motions across our line of sight will correspond to

actual velocities as follows

Annual motion 0",0001 0",001 0",01 0",05 Velocity, km/sec 145 1450 14500 72500

These results indicate that, on the island universe hypothesis, internal motions in the spirals must be enormous to be detected by present methods. Such high velocities will also presuppose the existence of mordinate masses.

A vast amount of work has been done by VAN MAANEN in his investigations of spirals for internal motions. VAN MAANEN's more important results are given

below in Table 13

It will be noted from this tabulation that all eight objects agree in showing a stream motion outward along the spiral arms amounting to about 0",02 annually in the mean. The average distance of these spirals is 2,6 10<sup>8</sup> ly, so that this motion would correspond to an actual velocity of 79000 km/sec. In general, van Maanen's values indicate a quasi-rotation in the direction of the concave side of the spiral arms, which seems directly opposite to the spectrographic results of Stipher (see ciph 46). In his final paper 2 van Maanen investigates all possible sources of error in the plates or in the methods of measurement which he employed, and concludes that the values he has given represent actual motions of roughly the order found. He has accordingly derived distances for the larger spirals ranging from 10<sup>8</sup> to 10<sup>1</sup> ly, with diameters ranging

<sup>1</sup> A VAN MAANLN, See the references under preceding section, K Lundmark, Internal motions of Messiei 33 Ap J 63, p 67 (1926), Mt Wilson Conti No 308 (1926), On the internal motions of spirals Publ A S P 34, p 108 (1922), J II Jeans, Internal motions in spiral nebulae M N 84, p 60 (1923), W II SMARI, The motions of spiral nebulae Ibid 81, p 333 (1924), W J A Schouten, Probable motions in the spiral nebula Messier 51 Obs 42, p 441 (1919), D Parchomenko, Eine von den möglichen Interpretationen dei inneren Bewegung in den Spiralnebeln A N 222, p 369 (1924), B Meyermann, Die innere Bewegung in den Spiralnebeln Ibid 221, p 239 (1924), J Jackson, On the influence of comparison stars on photographic proper motions MN 84, p 401 (1924), J II Jians, On the internal motions in spiral nebulae Obs 40, p 60 (1917) and 44, p 352 (1921), S Kostinsky, Motions in M 51 stereoscopically determined (Russian) Bull Acad St Pétersb (1916), p 871, M N 77, p 233 (1916)

Table 13 Internal Motion in Spirals, from van Maanen

Object	Proper motion			100				
Обрасц	6 7		a		8		Ausual Internal anotions	
598 (M 33)	4 0	77,003	C	7",00-1	399 nobular points measured blean stream motion outward along arms, + 0",020, mean transverse, -0",003 Periods deduced from 60 000 to 240 000 years 1.0 NDMANK's measures of same object gave mean stream motion + 0",002, mean transverse - 0",0004			
2403	+	,002		,000	Mean rotational, 0",015, mean radialoutward - -0",014, with considerable differences with distance from center Periods deduced, 50000 to 120000 years			
3031 (M81)	1	,014	-	,005	Stream motion outward along arms of 0",039, combined with alight transverse motion of +0",007 Deduced period, 58000 years			
4051	-	,003	1	,015	Radial motion outward 0",014			
4736 (AI94)	-	,014		,000	Stream motion along arms of 0",024, plus transverse motion of 0",009			
5055	+	,005		,015	Stream motion outward + 0",019, combined with transverse motion of 4-0",004 Slight decrease with distance from center			
5195 (M51)	-	,001	1	,006	Mean stream outward, $+0^{\prime\prime}$ ,021, mean transverse, $+0^{\prime\prime}$ ,008			
5457 (M101)	-1	,005	-	,012	Rotation of 0",022 at 5' from center Motions provailingly outward, with slight increase of rotation toward center Deduced period, 85000 years.			

from a few light-years to several hundred. As noted later, both Jeans and Brown have published theories of spiral structure to fit the magnitude of the motions found by VAN MAANEN.

LUNDMARK has pointed out that the outward motions found by VAN MAANEN mean the comparatively rapid disintegration of the spiral, and that, with such motions, no spiral could exist longer than 3 · 10° years as a shining body.

The measures of VAN MAANEN and the conception of the spirals as individual galaxies can not both be true, unless we are willing to assume velocities in the spiral arms which must occasionally amount to one-third the velocity of light. It seems impossible, moreover, to reconcile these values with the direction of the spectrographic velocity of rotation.

The intervals available for VAN MAANEN's measures were under twenty years. There seems at present no escape from the conclusion that these carefully made measures are subject to some instrumental error as yet undetected, and that they must be rejected until confirmation is secured by other observers and with materially increased time intervals. In view of the numerous other lines of evidence which now point so unequivocally to the adequacy of the island universe theory of the spirals, no other course is open

46. Rotation of the Spirals; Spectrographic. Spectrographic ovidence of the rotation of a spiral was first secured by V. M. SLIPHER in 1914, and evidence

<sup>&</sup>lt;sup>1</sup> V M Stipher, The detection of nebular rotation, Lowell Bull 2, p.65 (1914), Spectrographic observations of nebulae Pop Astr 23, p 24 (1915); Spectrographic observations of nebulae and star clusters. Hild 25, p 36 (1917), Spectrographic observations of the rotation of spiral nebulae Ibid 29, p 272 (1921), P G Prans, The rotation and radial velocity of the spiral nebulae NoC 4594 Wash Nat Ac Proc 2, p. 517 (1916), Mt Wilson Comm No 32 (1916), Publ A S P 28, p 191 (1916), The rotation and radial velocity of the central part of the Andromeda Nebula. Wash Nat Ac Proc 4, p.21 (1918), Mt Wilson Comm No 51 (1918).

has since been obtained by Stipiller and by Peasi for the rotations of a number of objects of the spiral class. Rotations have been definitely established by Stipiller for six objects, and these effects are suspected in a number of others. Those definitely determined are

221, the well-known elliptical companion south of the Great Spirit in Andromeda 224, Andromeda (M31)

1068, (M77)

2683

3623, (M65)

159 F

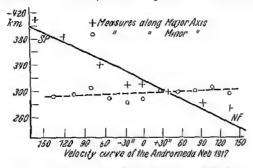
On the assumption that the side of the spiral which shows the most prominent lanes or other occulting effects is the nearer to us, which seems a certainty, STIPHER states that all these spirals rotate in the same direction. "The direction is that in which the arbor of a spiral spiring turns when the spiring is being wound up." STIPHER found that the rotation in 224 was greater near the nucleus, the inclination of the lines of 4594 indicated a speed of 100 km/sec at 20" from the nucleus (PLISI, 330 km/sec at a distance of 2' from the nucleus)

The two papers by Prasi contain the most detailed as well as the most authoritative information yet available in this exceedingly difficult field (an exposure of 80 hours was necessary on 4594, and 79 hours on Andromedal) For 4594 he found that the velocities, as determined by a least squares solution, followed the linear relation

$$v = -2.78 \text{ v} + 1180 \text{ km/sec}$$

and similarly he found for the Andromeda spiral (224)

That is, in both spirals the angular speed of rotation is essentially the same for different distances from the nucleus. This relation gave a speed of 58 km/sec at a point 2' from the nucleus in 224. In this object also,



1-1g 41 Rotational Velocity Diagram of NGC 221 (Andromeda) (Prase)

a plot derived from an exposure taken with the slit along the minor axis of the spiral likewise shows a linear relation, but with a much smaller slope than that derived from the spectrogram along the major axis

These rotational results of Pease, in their indication of a rotation obeying a linear instead of a quadratic law with varying distances from the nucleus, are of tremendous theoretical interest. They apparently require that we abandon

the dynamical models of every earlier theorist, in which the component elements move in orbits obeying the inverse square law. It would seem that the only theory which can satisfy these spectrographic results is one of the nature of the still uncompleted theory of Brown (see ciph 63), in which the particles are assumed to move in central ellipses, under a law of attraction of the form  $-n^2r$ 

47. Spectra of the Spirals, Stellar Type The great majority of objects in the spiral class show a continuous spectrum crossed, where the brightness of

the object permits the use of a sufficient scale for their detection, by the dark absorption lines characteristic of stellar spectra, and in all essential features a duplicate of the integrated spectrum of the Milky Way or of a star cluster. It is this almost invariable continuous spectrum which earlier carned for them the name "white" nebulae. The descriptions of their spectrum will almost always be of the form solar type, like a Class G star, type G0 or later, etc Reference should be made here to the investigations of Lundhark and Lindhlad' on the effective spectra of celestial objects. They investigated 24 objects in all, and obtained the following mean values.

Number	Class	Wave-hingth maximum	Equivalent stalar class
6	l'Innutary Cluster	4130 A 4190 Λ	B±
14	Spiral	4290 A	G2

See also clph. 49, 50

48. Spectra of the Spirals; Emission Lines There are some relatively rare and for that reason very puzzling exceptions to the almost universal rule that the spectrum of a spiral is such as would be obtained from a large congenes of stars. The total number of such exceptional cases is unknown, but it is probably not large. Among these may be noted.

1068 Velocity |- 11(0) km /sec Continuous spectrum with absorption lines, crossed by nobular emission lines. SLIPHER, Lowell Bull 3, p 59 (1917) reports that these lines are not images of the slit, but small disks. N<sub>1</sub> and N<sub>2</sub> were found strongly mellined, indicating a velocity of 300 km /sec. at 1' from the nucleus

Nucleus like a planetary nobula, showing bright H, 4686 A, and O lines (HUMARON)
Continuous spectrum crossed by some absorption lines and by nebular emission

lines (Stripter)

4051

4211

4449

This is a very irregular object of the Magellanic type, cf. Figure 33. Prable [Ap ] 46, p 24 (1917). Plata VIII, b)] notes the presence of 230 nobulous stars or patches (note the authory with the Large Magellanic Cloud). Noted as continuous plus possible authorised by Wells in Sitzber Heldelberg Ak, Abt A, Nr 15 (1912). Stipenes describes as strong continuous spectrum crossed by the strong emission lines possible to the guszous nebulae. He records  $H\delta$ ,  $H\gamma$ , 4686 A,  $H\beta$ , 4959 and 5007 A, and derives a radial velocity of  $-\frac{1}{2}$  200 km/sec

A passible explanation for such exceptions to the almost universal absorption character of the spectrum of the spirals is doubtless to be found in the assumption of a large number of masses of the type of the diffuse or planetary nebulae intermingked in the prevailingly stellar composition of occasional spirals, 4449 contains 230 nebulous stars or patches, 278 patches of diffuse nebulosity (or planetaries) have been catalogued in the Greater Magallanic Cloud, a number of such diffuse patches have been noted in 224 (Andromeda) and other large aprairs. Were the Cloud removed to 400 times its present distance, it would appear as an unresolved patch not unlike 4449, and about 2,5 long

It is probable also that, in such a case, the emission lines are vastly easier to record than the continuous spectrum of the background of stars. With the very long exposures which are necessary to secure even a faint record of the continuous spectrum of an integrated mass of stars in a cluster or spiral, and bearing in mind the advantage of concentration of the emission spectrum of such nebulous inclusions into a few hight lines, it would seem possible that such nebulous patches would easily be spectrographically recorded as emission

lines overlying the continuous background,

<sup>&</sup>lt;sup>1</sup> Plustagraphic offective wave-lengths of nebulae and clusters. Ap J 46, p. 206 (1917), 50, p. 176 (1920).

By way of illustration of this point using the ratio of speed between the spectrograph attached to the Lick Refractor and the quartz spectrograph of the Crossley Reflector, as given by Faih, = 1.25, Faris's instrument should have recorded easily in 30 minutes the bright lines of 6853 (the Dumb-bell Nebula), whose areal brightness is given as 10,8 by Wiriz Fath secured nothing at all of the continuous spectrum of the spiral 5194 in an exposure of 14,5 hours, although Wiriz' value for the areal brightness of this spiral is 10.9

49. Color Indices of the Spirals, the Results of Spares! Considerable work has been done by Spares, Shappey, and others, on the color indices of objects

or different parts of objects of the spiral class

Taking two series of exposures, one on ordinary photographic plates and the other on isochromatic plates through a color screen which transmitted the light to the red of 4900 Å, Sharfs found notable differences in different parts of the spirals 4254, 4736, and 5194. The nuclear portions are strong on the "yellow" plates. On the other hand, the branches and especially the condensations found along the spiral arms are very blue "the knots of nebulosity are certainly bluer than the bluest of the neighboring stars", and are described as resembling in that respect the central star of the Ring Nebula in Lyra. For elliptical nebulae, however, Hubbit reports that plates exposed through a visual color filter show no difference between the nuclear and the outer regions.

SHAPLEY, using the Holeschiek-Hopmann visual magnitudes for comparison with the photographic, has tabulated the color indices of 43 spirals, with

the mean results

	Number	Color index
All elliptical objects All spirals Triegular	12 28	+0,33 +0,22 -0,37

He points out for 7619 (not included in the tabulation) that this spiral, the faintest, fastest, and probably the most remote of those discussed, has the largest color index,  $M_{nh} - M_v = 2.8$  Hubble and Humason, however, (see ciph 55)

find a mean color index of +1,1 for the spirals they observed

Carpenter finds for 3034 (M82) no difference between the yellow and the blue images, although a photograph on a panchiomatic plate shows a substantially different distribution of brightness. For 5194 (M51), however, he corroborates the results obtained by Searls. The nucleus appears red, and has a color index of +1,6, there is a continuous increase in blueness in passing outward along the arms from their base, the color index varying from +0,6 near the nucleus to -0,3 at about one revolution from the nucleus. He suggests that such an effect might be due to the fact that younger stars are prevailingly near the nucleus, and older stars further out, most of the light in the latter case coming from the hotter stars of the giant sequence.

<sup>&</sup>lt;sup>1</sup> F II Searts, Prohomory results on the color of nebulae Wash Nat Ac Proc 2, p 553 (1916), Mt Wilson Comm No 36 (1916), Publ ASP 28, p 191 (1916), Distribution of color in certain spiral nebulae Pop Asti 25, p 34 (1917), The surface brightness of the galactic system as seen from a distant external point, and a comparison with spiral nebulae Ap J 52, p 162 (1920), Mt Wilson Contr No 191 (1920), II Shapiey, Note on the velocities and magnitudes of external galaxies Wash Nat Ac Proc 15, p 565 (1929), E b Carpender, The distribution of color in two extra-galactic nebulae (abstract) Publ ASP 43, p 294 (1931)

<sup>&</sup>lt;sup>2</sup> Ap ] 71, p 231 (1930)

50. The Radial Velocities of the Spirals<sup>1</sup>. The first radial velocity of a spiral (plates taken in 1914), the first spectrographic evidence of rotation of a spiral (1914), and the first spiral velocities of considerable magnitude, are due to V M Stipher Very noteworthy extensions to our knowledge of the radial velocities of the spirals have been made at Mt, Wilson through the work of Humason, Prase, and others

Very rapid progress has been recently made in this difficult field at Mt Wilson, owing to the use of the new RAYTON lens, which very materially shortens the expansive times medded. 46 spiral velocities secured thus have recently been published.

This lens, of very short focal length and remarkable focal ratio, is an 8-fold enlargement of a microscope objective, with an extra element added to provide for a source at an infinite distance. Its aperture is 50 mm, and its focal length is 32 mm, giving a focal ratio of 1 0,59, without doubt the highest ratio ever employed for such purposes. The dispersion at 4500 A is 418 angstroms per mm with two prisms, and about 875 angstroms per mm with one prism, the total length of the spectrum from 3888 A to 5015 A is only 2,67 mm! A wide slit can be used, 0,2 to 0,6 mm. While the probable error of a spectrogram taken with this remarkable lons is estimated to be of the order of 100 km./sec, this is of little importance in comparison with the large radial velocities which are being obtained

Radius velocities are now (January, 1932) available for 90 objects, this total includes the two Magellanic Clouds. The radial velocities of the spirals have the following salient characteristics

1 They are provailingly velocities of recognon (+)

2 They display an enormous range, from -300 km./sec to +19600 km /sec.

3 Remarkable groupings of spirals have been discovered by Humason, contiguous in apparent location in the sky, and with large radial velocities nearly identical in amount

Spectrographic observations of nobulao. Pop Astr 23, p. 24 (1915), Two nebulas with unparallolad velocities. Lowell Circ., January (1912), A.N. 243, p. 47 (1917), Spectrographic observations of nebulae and star clusters. Pop Astr 25, p. 26 (1917), M. Wolff, Spectrographic observations of nebulae and star clusters. Pop Astr 25, p. 26 (1917), M. Wolff, Reports in V.J. S. 49, p. 162 (1914), 80, p. 97 (1913), F. f. Paras, Radial velocities of nebulae. Pahl A.S.P. 27, p. 133 (1915), The radial velocity of M33. Ibid. 28, p. 33 (1916); Radial velocities of RGC 3379 and 1700. Ibid. 30, p. 235 (1918), Ap.J. 51, p. 276 (1920), M. L. Humsson, Radial velocities of two nebulae. Publ A.S.P. 339, p. 347 (1927). The large radial velocity of NGC 7619 Wash Nat. A. Prin. 15, p. 167 (1929), Radial velocity of cose nebula in the cluster of faint nebulae in Ursu Major described by Barde [A.N. 233, p. 65 (1928), Ap.J. 71, p. 356 (1930)], Radial velocity of two nebulae in the Persons Cluster. Ibid. 74, p. 355 (1930), Apparent velocity-shifts in the spectra of faint nebulae. Ibid. 74, p. 35 (1931), R. F. Sarprond, Radial velocity of NGC 2681. Publ A.S.P. 34, p. 222 (1922), The radial velocity of the companion to the Andromeda Nebula. Ibid. 38, p. 44 (1926), G. El. Tauram, The motions of the spiral nebulae. Pop Astr 24, p. 111 (1916), H. N. Rossall, Radiation pressure and constital motions. Ap.J. 33, p. 1 (1920), J. H. Revnottes, Radial velocities of spiral nebulae. Offs 45, p. 267 (1922), W. W. Campert and the Propose Radial velocities of spiral nebulae of the spiral nebulae. Repose and spiral nebulae to the stellar system. K.Sv. Vet Akad Handl. 60, No. 8 (1919), G. Stellmenn, Analysis of radial velocities of globular clusters and nog-radiation nebulae. Ap.J. 61, p. 354 (1928), L. Courvourier, Bestimming der absoluten Translation der Riche and the radiation Analysis of radial velocities of globular clusters and nog-radiation der Riche and the radiation Analysis of radial velocities. Ibid. 71, p. 354 (1930).

Ap.J. 74, p. 35 (1931)

lable 14 Radial Velocities of the Spirals

NGC No	Gala	ictic	Rul vel km /sec	Author	Spectral class	Δβαι (0 /0
205 221 224 278 380	63°,9 64',4 64',1 66',4 70',2	-22°,1 -23 ,1 -23 ,1 -18 ,2 -31 ,+	- 300 185 220 + 650 + 1400	Dum 5 5   5   11um	G81 1	Local Local Local Local Pisces Chistia
383 384 385 401 584	70 ,2 70 ,2 70 ,2 70 ,3 94 ,2	-31,4 -31,6 -31,6 -28,1 -68,9	+ 4500 + 4500 + 4900 - 25 + 1800	Ifum IIum IIum S	(13) (15) (15)	Piscos Clinter   Piscos Clinter   Piscos Clinter   Local   Local?
598 936 1023 1068 1270	77 ,0 110 ,0 88 ,5 115 ,7 93 ,9	-32,6 -54,7 -20,2 -52,2 -14,3	70 1300 300 920 4800	17 5 5 5 + Ilum	C+51 I	Local   Local   Local   Local   Porsens Cheder
1273 1275 1277 1700 2562	93 ,9 94 ,0 94 ,0 147 ,5 145 ,2	-14,3 -14,2 -14,2 -27,7 +28,0	+ 5200 + 5200 + 5200 + 800 + 5100	Hum Hum Hum L' Hum	(14) (14) (14)	Persons Cluder Persons Cluder Persons Cluder Focal Cancer Cluster
2563 2681 2683 2841 2859	145 ,2 110 ,0 132 ,9 109 ,7 132 ,6	+28,0 +38,4 +38,3 +43,0 +44,8	+ 4800 + 700 + 400 -+ 600 + 1500	Hum San S- - S Hum	(13	Cancer Chrice Total Focal Focal Focal Focal?
2950 3031 3034 3115 3193	98 ,0 85 ,2 84 ,3 190 ,1 154 ,7	+43 .7 +39 ,8 +39 ,4 +37 .7 +54 ,8	+ 1500 - 30 + 290 + 600 + 1300	Hum S S S Hum	(+3)	Total?   Total   Total   Total   Total?
3227 (1) 3368 3379 3489	158 ,7 170 ,3 176 ,3 175 ,1 176 ,0	+ 55 ,4 +48 ,5 +57 ,6 +58 ,0 +61 ,2	+ 1150 +19600 + 940 + 810 + 600	Hum Hum S S+ S+	(7-) P (75	Tocal? 1 co Chefci Focal 1 ocal 1 ocal
3521 3610 3623 3627 4051	197 ,7 86 ,4 181 ,4 181 ,9 104 ,5	+53 .5 +53 .5 +64 .7 +64 .7 +64 .6	+ 730 + 1850 + 800 + 650 + 650	S IIum S S	G2	l ocal Isolated   Local   Local   Local
(2) 4111 4151 1192 4214	83 ,4 92 ,1 97 ,1 207 ,0 102 ,1	+58,1 +71,2 +74,1 +75,9 +77,4	+11800 + 800 + 960 + 1150 + 300	Hum S S-1- Hum S	G2	Uisa Maj Claster Local Local Local? (Virgo) Local
4258 4374 1382 4449 4472	80 ,8 220 ,1 206 ,2 79 ,4 229 ,4	+67,8 +74,6 +80,2 +71,5 +71,0	+ 500 + 1050 + 500 + 200 + 850	S Hum S S	G4	Local Local? (Virgo) Local? (Virgo) Local Local? (Virgo)
4486 4526 4565 4591 4649	225 ,9 232 ,7 166 ,0 241 ,8 238 ,0	+75 .6 +70 .9 +86 .6 +52 .8 +75 .1	+ 800 + 580 + 1100 + 1140 + 1090	\$ \$ \$ \$+ \$		Local? (Vngo) Local? (Vngo) Tocal Local Local Local? (Vngo)

(Continued)

MIN	(winetin		Rad. vol.	Author	Spectral	
No.			kan./rae	varina	chicae	Allocation
4736	73 .1	174.7	± 290	S	GLL	Local
4826	262 .6	F85 .4	+ 150	S	GLI.	Local
4853	21 .1	188 1	1 7600	Hum	G1	Come Ber Chater
4860	27 .7	187.6	+ 7900	Hum	G3	Come Ber Cluster
4865	26 ,0	1-87 ,9	F 5000	Hnm	G3	Coma Ber Chaster
4872	24 ,4	1 87 .7	6900	Hum	G3	Coma Ber Cluster
4874	24 ,4	N7 .7	<b>⊢ 7000</b>	Hum	G4	Coma Ber Cluster
4881	35 .6	1 Ber , 60 .	F 6900	Hum	G3	Come Bor Cluster
4814	26,6	88 .2	F 6700	Hum	G3	Coma Ber Chuster
4895	26 ,4	86 ,5	-  8500	Hum	G4	Coma Ber Cluster
IT 4045	26,0	186 ,5	F 6600 .	Hum	GI	Coma Ber Cluster
5005	46 , 1	1 78 , 1	-  900	4		Local
5055	49.0	177,1	+ 450	S		Local
5194	49,0	1 67 ,5	- <b> - 25</b> 0	S	GLL	Local
5236	261 ,1	1 42 ,9	1 500	5	I	Local
5457	45 ,9	1 59 .1	- <b>+</b> 300	Hum	G+P	Local
5866	36 ,0	151,3	- 650	8		Local
6359	34 .9	1 13 .7	-  1000	Hum	G3	Leolated
6658	355 .4	14,6	-  4100	Hum	G3	Leolated
6661	155 ,0	14 ,6	-  1900	Hum	G5	Lolated
6702	18 ,5	1 18 .7	+ 2250	Hum	G4	Isolated
6703	18 ,6	0, 81 [	2000	Hum	G3	Isolated
6710	0,2	11 ,6	F 5100	Hum	G3	Isolated
6822	327 ,8	18,3	150	Hum	Pd	Local
6824	32 ,0	144,6	F 3200	Ham	G4	Isolated
7217	29 ,6	20,0	F 1050	Hum	G4	Local
7212	34 ,8	17 ,0	- 5000	Hum	G3	Liolated
7331	36 ,8	21 .7	500	5		Local
7611	30 , 3	48 ,8	1 1400	Hnm	G2	Pegasus Chreter
7616	40 , 1	-49 ,0	3900	Hnm	G1	Pegasus Chusten
7619	10 ,1	40,2	1 38(K)	Hnm	<b>G3</b>	Pegasus Cluster
7621	30 .3	49 ,1	1 3800	Hum	G2	Pegasus Cluster
7626	30 ,5	40 ,2	F 3700	Hnm	G3	Pognama Cluster
In Cl.	224	32	280	Wils		Local
5 CI	214	43	- 170	WIP.		Local

Notes to Jubio 14.

One of the brightest spirals in Charge's Cluster in Leo, α = 10<sup>h</sup> 24<sup>m</sup>,0,
 1 10<sup>h</sup> 50' (1930,0)
 1 1rightest object (No. 24) in Baars's Ursa Major Cluster, α = 11<sup>h</sup> 43<sup>m</sup>,3,

8 - 1 56° 8' (19 10,0).

These values are so exceptional in the respects mentioned that there is a tendency in recent literature to refer to them as "apparent" velocities. While it is not at present possible to render any decision as to the reality of these speeds, there is reason for the belief that they represent actual velocities, at least in greater part. For this reason, and for convenience, they will be referred to in the balance of this treatment simply as radial velocities. Because of their size and their provailing characteristics of recession, they have formed the basis of numerous speculations and have, in particular, been regarded as the subject matter for various types of "relativity universes".

So intimately have they come to be connected with such questions and with one theory of the distances of the spirals, that the pertinent data concerning the radial voice lites of the spirals will be segregated, at the risk of some repetition. The values are given at this point, with spectral class where known, galactic

coordinates, and allocation into groups. They will be given again, with derived data as to dimensions and distances, in ciph 56. See also Appendix 8.

The successive columns in Table 14 are as follows

Column 1 The NGC number

Columns 2 and 3 The galactic coordinates These are taken from Emanuetli's excellent tables, where the origin of galactic longitudes is chosen so as to make the longitude of the solar apex = 0

Column 4 The radial velocity

Column 5 The authority for the velocity. This is not always the observer, for example, the plates of 4192, 4374, 4853, 4860, 6702, 6703, 7217, 7242, and 7626 were obtained by Plase. In this column, Hum = Humason, S = Slipher, S+ = Slipher and others, San = Sanford, Wil = Wilson.

Column 6 The spectral class, when known, when standing alone, the values are as assigned by Humason, when tollowed by LL, they are from Lundmark and Lindblad

Column 7 Humason's allocation of objects to clusters of spirals. The term "isolated" is used for spirals of high velocity which may belong to similar clusters, not yet substantiated, while "local" is applied to objects which are presumably members of our own local system of galaxies.

51. Distances of the Spirals Parallaxes There have been numerous published values of direct parallaxes of the spirals in both the older and the more modern literature of the field. These give distances which are in diametrical contradiction with the values secured by other methods, and their range is wide. A tabulation of these conflicting and now almost universally discarded values could only cause confusion, and the writer prefers to omit all reference to them for this reason.

**52.** Distances of the Spirals from Novae Since 1917 a very large number of novae have been discovered in several spirals, among which the Great Spiral in Andromeda (224) leads the list. These are given in Table 15

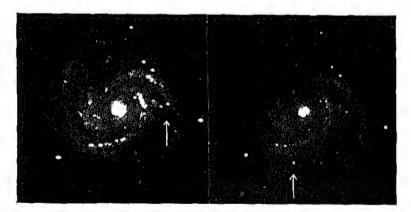
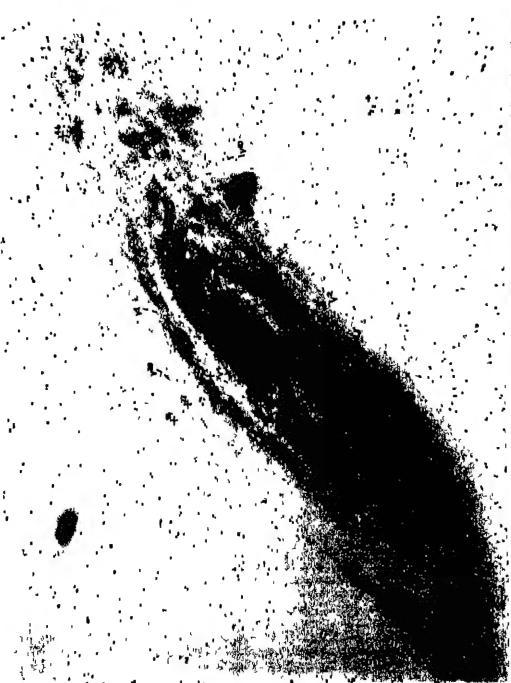


Fig 42 Two Novae in the Spiral NGC 4321 (Lick Photographs) Left taken April 19, 1901 Right taken March 2, 1914

The wealth of novae in the Andromeda spiral far exceeds the number of galactic novae (fewer than 40). As Hubble has well pointed out, aside from the uncertainty in the determination of the zero point, the mean absolute magnitudes are determined for the novae in 224 with much greater precision than for those in our galaxy.



From HURBLE, Ap J 69,

Table 15 Novae in Spirals

No	Number of novae	Mean magn at maximum	Notes
22	87	17,2	Including S Andromedae, which appeared in 1885 (magn 7,2 at maximum), 87 novae have been discovered in 221 (Andromeda). Nos 2 to 22 were discovered in 1917 to 1922 by R11 cills, Plast, Shaptly, Santord, and Humason Nos 23 to 86 were discovered by Humbi of which he has since rejected Nos 26, 36, and 39 as possibly long period variables. Nos 8; to 90 were found by Duncan, Publ A S P 40 p 347 (1928). S Andromedae is not included in the maximum given. The magnitudes cooldinates, dates of observation, etc., of these novae are assembled by Humbi in, "A Spiral Nebula as a Stellar System, Messier 31." Ap J. 69 p 103 (1929), Mt Wilson Contr. No. 376 (1929)
2103	- 1	16,5?	RIICHLY, Publ A S P 29, p 210 (1917)
2608	1	11 2	Woll, AN 210, p 373 (1920)
2841	t	16	PLASE, Publ A S P 29, p 213 (1917)
3031	1	18 ?	Rizchly, Publ A S P 29, p 210 (1917)
3147	1	14 ?	Mis Roberts, Publ ASP 29 p 211 (1917)
4303	1	14 ?	REINMUTH and Worl, Harv Bull 836 (1926)
4321	2	14	Curris, lick Bull 9, p 108 (1917)
4486	1	11,5	BAYANOWSKY, A N 215, p 215 (1922).
4527	1	15	Curtis, 1 c
5253	i	7,2	Mrs Liiming, Haiv (ne 1 (1895)
5857-8	2	18,5	RITCHIY, 1 c
6946	1	14,6	RITCHLY, 1 c
598			Hubbit, I c, p 119, footnote

The first attempts to determine the distance of the spirals by analogy with the galactic novae, made by Curiis¹ in 1917 were roughly of the right order, though rendered somewhat uncertain by the lack of accurate knowledge of the absolute magnitudes of galactic novae, an uncertainty which still persists Assuming tentatively that the galactic novae were at an average distance of 10000 ly, and with an average apparent magnitude at maximum of 5, he derived a difference of about 13 magnitudes between the galactic and spiral novae, indicating that the spirals were 400 times as far distant as the galactic novae. This gave a distance of the order of 4 · 106 ly for the spirals "(orrelations between the novae in spirals and those in our galaxy indicate distances ranging from perhaps 500000 ly in the case of Andromeda, to 10000000 or more light-years for the more remote spirals"

A slightly greater amount of data on the galactic novae has since become available, and several similar and more accurate correlations have been made. There are few who would maintain, however, that it may not eventually be necessary to multiply or divide the distances of spirals found by the novae method, by a factor of from 2 to 5. Our knowledge of the absolute magnitude of galactic novae at maximum must be regarded as still highly uncertain Lundmark has placed this at -6.1, while Hubble, determining the distance of 224 from Cepheids, places the mean absolute magnitude of galactic novae at -5.7

There are, in addition, some other difficulties. The absolute magnitude of S Andromedae, in order to correspond with the values found for the fameur novae in that spiral, must have reached nearly -15. This is a truly enormous

Wash Nat Ac Proc 9, p 218 (1919), Lick Bull 9, p 108 (1917)

value, though as a parallel instance we have but to assume that Tycho's nown (which reached an apparent nugnitude of about —5) was in reality as distant as 3300 ly. If the smaller spirals 3147, 4321, and 4527 are at a distance of 5 · 10° ly. (Hubble places 4321 at 4,6 · 10° ly), the absolute magnitude of the four 14th magnitude novae found in these objects must have been close to —12, the same is true for the novae found in 5253 by Mrs. Fleming. It would seem that we must assume two classes of novae to take care of all these discrepancies,—the one of roughly also magn.—5 at maximum, and a class of comparatively rare exceptions 10000-fold brighter.

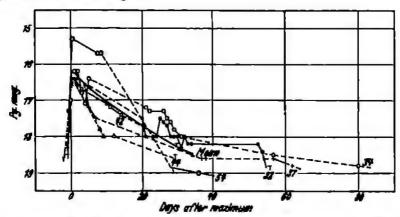


Fig 44 I light-curves of Six Novae in NGC 224 (Andromedia) (Husan R ) Observed near maximum

There is no doubt that the majority of the objects in 224 attributed to this class are really novue. While for many of the objects the data are fragmentary, Humma assembles the data for six which were observed over a longer interval (see Figure 44), and the composite light-curve of these has all the characteristics expected from novae in rapid rise, slow decline, and minor fluctuations

58. Distances of the Spirals: from Caphelds. The derivation of the distances of the spirals through the period-luminosity relation adduced for Capheld variables is due entirely to Hubbi & (1924). He has found 50 variables in 224, of which 40 are Caphelds, and 35 Caphelds in 598—9 have been discovered in 6822, none have thus far been reported from other spirals. The characteristics of these, together with 105 determined by Shapery in the Small Magellanic Cloud, and 6 from 6822, are shown in Hubbile's diagrams, reproduced below as Figures 45 and 46

Using Shapley's values for the Cepholds in the Small Magellanic Cloud, for which he had derived the relation.

$$m - M = 17.55$$
.

the corresponding modulus for 598 (M33) was found to be,

m-M=22,1, or a distance of 850000 Ly

Similarly for 224 (Andromeda), the modulus is,

$$m - M = 22,2$$
, or a distance of 9000001 y.

HUBBLE definitely calls attention to the fact that all these values are affected by any change of the zero-point of the Cephold period-luminosity relation, as derived by Shapley.

There have been a number of revisions of Shapily's values, of which one of the latest and most authoritative is that due to Advans, Joy, and Humason's

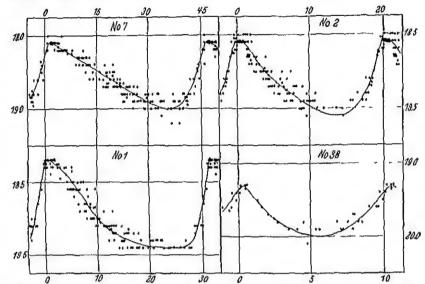


Fig 45 Light-curves of Four Cepheids in 224 (Andromeda) (Hubbi i) the ordinates are photographic magnitudes, and the abscissac, days

These authors have determined the spectroscopic absolute magnitudes of 80 (e-pheids with periods between 1,6 and 45,2 days, using an extrapolation from the

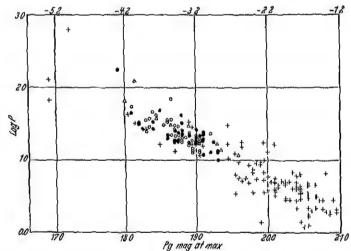


Fig 46 Period-Luminosity Relation for Cepheids in Spirals (Hubbil) The crosses refer to 105 Cepheids observed by Shapley in the Small Magellanic Cloud, the black disks, to 40 Cepheids in 224 (Andromeda), the open circles, to 35 Cepheids in 598 (M33), the triangles, to 9 Cepheids in 6822. The apparent magnitudes at maxima have been reduced to the distance of 224 by adding 4,65 to those in the Small Magellanic Cl., 0,4 to those in 598, and 0.55 to those in 6822. The absolute photographic magnitudes at the top of the diagram are based upon Shapley's zero point (m-M=17.55) for the Small Magellanic Cl.)

<sup>1</sup> Publ ASP 41, p 252 (1929, abstract)

reduction curves for ordinary giant stars, and with a comparison with trigonometric parallaxes for 16 monitors of the group. The derived mean of the spectroscopic absolute magnitudes is -1,74. As compared with Shapley's original value, these results show a displacement of the zero-point of about one magnitude, Shapley's values being the higher. This would serve to bring objects determined by the period-luminosity relation about 37% closer. A Kipper makes a somewhat similar investigation and changes Shapley's zero-point by 1,1 magnitudes; he regards this as the minimum change required, this would mean a diminution of spiral distances of about 40% or more

A more precise determination of cosmic distances by all these methods must await the accumulation of more accurate data on the maximum brightness of novae, of the brightest stars, and the Copheid variable stars. While present values of spiral distances show a fairly satisfactory measure of agreement between the results of the different methods employed, it must be remembered that the corresponding values of the galactic data are likewise intimately interdependent

64. Distances of the Spirals: from a Distance-Velocity Correlation. The radial velocities of the spirals have, as noted above, such magnitude and range, as well as provaling positive character, that these features have long been noted as differentiating them most sharply from any other class of celestial body. There have been numerous attempts to determine from these velocities the speed and direction of motion of our own galaxy (see references under clab 50 above, and also clab. 77). With the later enormous values of 4-3000 to +19600km/sec, there has come in certain quarters, however, the feeling that these can not be actual speeds, and attempts have been made to explain the observed speeds as due to distance, or as necessary consequences of one or another type of limited, quasi-spherical relativity universes

The idea that there might be a correlation between the radial velocity and the distance of a spiral seems to have occurred nearly simultaneously to Wietz, Lundmark, and Russell (in a suggestion made to Silberstein) in 1924. It has since been much more definitely treated, using a larger number of radial

velocities, by Hubble, DR Sitter, and Ookt.

Wirrz shows quite clearly from the velocities of the 42 spirals available at that time, that these velocities diminish with increasing diameter, i e, increase with increasing distance.

WINTZ, Argument for Diameter

Log (lian	Mean I'	No.	Log diam	Mean P	Nn.
0,24	-827 km /noc.	9	0,88	+ 355 km /sec.	10
0,43	-636	7	1,07	+ 334	5
0,66	-512	8	1,71	- 20	3

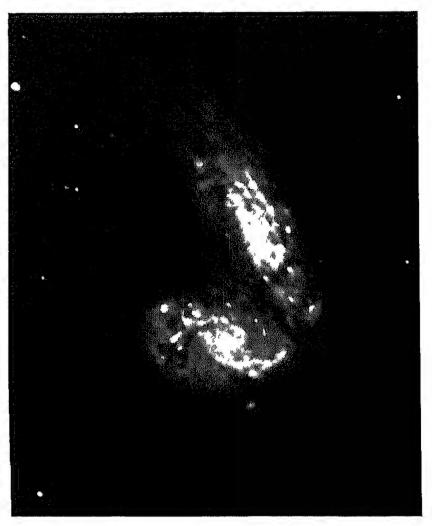
<sup>1</sup> A N 241, p. 249 (1931)

<sup>2</sup> C. Wirtz, Do Sittom Kosmologie and die Radialbewegung der Spirainebel A N 222, p. 21 (1924), K Lundmark, The determination of the curvature of space-time in do Sitter's world. M N 84, p. 747 (1924), K Hundle, Extra-galactic nobulae. Ap J 64, p 321 (1926), A relation between the distance and radial velocity among extra-galactic nebulae. Wash Nat Ac Proc 15, p 168 (1929), Mt Wilson Comm No 105 (1929), E. Hussell and M W Hummon, The velocity-distance relation among extra-galactic nebulae. Ap J 74, p 43 (1931), A Doss, Zur Statistik der nichtgalaktischen Nobel auf Grund der Künigstuhl-Nebellisten. A N 229, p. 157 (1927), H. Shaper, Note on the velocities and magnitudes of external galaxies Wash Nat Ac Proc 15, p. 565 (1929), J. H. Corr, Note on the velocities of extra-galactic nebulae. BAN 5, p 239 (1930); Some problems concerning the distribution of luminosities and peculiar velocities of extragalactic nebulae. Ibid 6, p 155 (1930), W de Sytter, On the magnitudes, diameters, and distances of the extra-galactic nebulae, and their apparent radial velocities. Did. 5, p 157 (1930), Wash Nat Ac Proc 16, p. 474 (1930), L. Steuerstein, Nat 113, p 602 (1924) See also references in ciph 69.

From these values he derived the relation

 $V(km/sec) = 914 - 479 \log diam$ 

LUNDMARK plotted the radial velocities against the distance, reproduced below as Figure 49. It will be seen from an inspection of this diagram that his scale of abscissae is greatly foreshortened by the scale he employed in lieu of



1 ig 47 The Spirals NGC 4567-8 (Mt Wilson Photograph)

more accurate distances, i.e., 50, 100, 150, etc., times the assumed distance of the Andromeda spiral, and that the relation indicated might have been more apparent with an expanded horizontal scale. He states "Plotting the radial velocities against the relative distances, we find that there may be a relation between the two quantities, although not a very definite one"

The results of Dose are based upon a statistical analysis of the Königstuhl nebular lists, with attempts to secure correlations as to brightness, etc. Taking

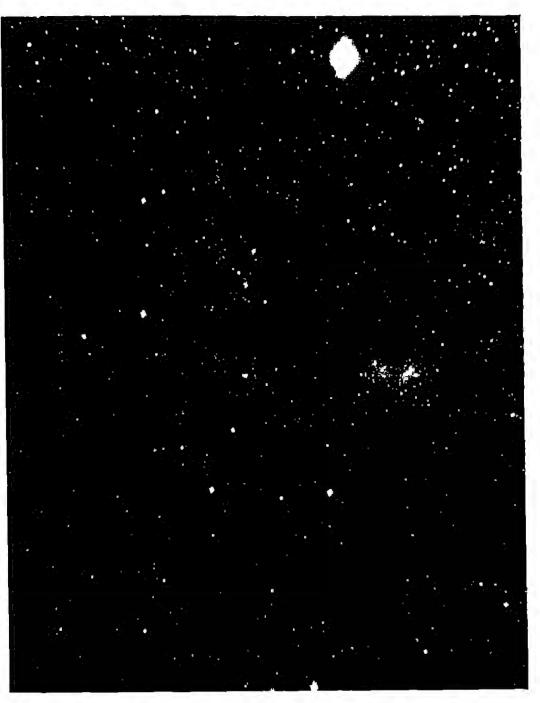
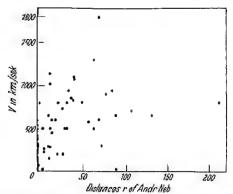


Fig 48 The Spirul NGC 224 (Andromoda) (Mt Wilson Photograph.) South proceeding portion.

Ц

the radial velocities of the 44 spirals available, he first made a solution for the direction of motion and speed of our galaxy, linding



l 1g 49 Radial Velocity Distance Correlation for the Spirals (Lundmark) The unit of distance is that assumed for 224

1	-	299° 8′
D	_	-  67° 32′
K	_	765 -L 110 km /sec

He then found, on correcting the individual values for this motion, that there is a slight but definite correlation between distance and radial velocity. No diagram is given, but he divides the spirals employed into three groups as regards size.

Group	Djameter	Radial velocity
I	120' to 6'	634 km /sec
II	6' to 3'	719
III	3' to 0',7	880

That is, the peculiar radial velocity increases inversely as the diameter of the object, or directly as the distance. Both Wirrz and Dosh, as is manifest, assume that the diameters are of the same order of magnitude

In his earlier paper, Hubbll took the distances of 22 spirals and the two Magellanic Clouds, estimated by various methods, as the basis, and introduced into the individual equations of condition for galactic motion a K-term varying as the distance, the equations taking the form

$$rK + X\cos\alpha\cos\delta + Y\sin\alpha\cos\delta + Z\sin\delta$$
 1'

Two solutions were made, the first by using the 24 spirals individually, and the second by combining objects apparently contiguous as to direction and distance into 9 groups. The solutions gave

	24 spirals	9 groups		
Y	65 + 50	+ 3 ± 70		
7	<b>├226 上 95</b>	+230 ± 120		
1.	- 195 土 10	-133 土 70		
K	$+465 \pm 50$	$+513 \pm 60$ km/sec	pei	106 parsecs
A	286°	269°		
D	- 40°	1 33°		
$V_{0}$	306 km /sec	247 km /sec		

As a result of a more detailed analysis, and with the employment of a larger number of velocities, Hubbie and Humason in their latest paper derive a value of 558 km/sec per 100 parsecs, which corresponds to

The values for this red shift with distance as determined by DI SIIIIR, and in Oori's earlier paper, do not differ materially from this value (Oori, however, later derives a smaller value, ca 90 km/sec per 108 ly

This interesting relation, should it persist to the most remote spirals, may lead to some curious and rather bizarie consequences. If the faintest and smallest spirals at present observable are at a distance of 100 ly, such objects should show a radial velocity of about +170000 km/sec, corresponding to a shift to

the red of ca 1500 Å. Unless counterbalanced by radiation coming in from rich ultra-violet regions, one might even expect the most distant spirals to be

myssible on account of reduces

Except for the nearer spirals, whose distances have been determined by other methods, it should be mentioned that earlier diagrams were simply plots of one variable charted in two dimensions, and that there was thus no reason why all the plotted points should not fall precisely upon the line of the correlation

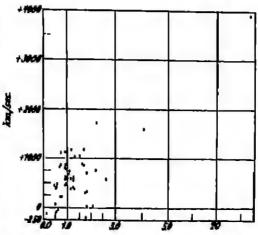
SHAPIFY, for example, criticized certain features of the velocity-distance corDistance in Histon light years

idg to Radial Velocity-Distance Correlation for the Spirala (Hubbu K and Humason). The small black dots in the lower left hand corner represent the only available observations up to 1928. The open circles represent recent observations.

relation, and pointed out that the total magnitude may equally well be regarded as a vital factor. Correcting the tabular radial velocities available for a galactic motion toward the apex  $A = 277^{\circ}$ ,  $D = -136^{\circ}$ ; V = 280 km./sec.

a galactic motion toward the ape and using the Harvard photographic magnitudes of the objects, he plotted the resulting radial velocities against the function  $10^{0.9 \, m^{-2.0}}$ . This corresponds to a plot of velocity against distance expressed in parsecs, provided space is assumed to be transparent, and provided that the absolute magnitude of the typical spiral is placed at 45

It will be noted from Shapiry's diagram reproduced as lelgure 51, that the internal agreement of the plotted velocities is fully as good as that for radial velocity alone. Reference may also be made here to Lundmark's diagram of the relation between areal brightness and the relative parallax of the spirals.



lig 51 Radial Velocity-Magnitude Correlation for the Spirals (Shapery). This diagram shows the relation of the reduced radial velocity to the quantity 10%2 m. 20

The latest treatment of this relation, the brilliant paper by Hubber and Hubbson (i.e.), has removed, at least in part, the effect of such criticisms. They have here made use of parallel correlations through the factors of absolute

<sup>1</sup> M N 86, p 877, blg 7 (1925)

magnitude and apparent diameter, relations which may be more fittingly included with the matter of the Section following this one

55 Distances of the Spirals Photometric, the "Average" Galaxy<sup>1</sup> Under this heading will be assembled certain photometric data, and deductions as to the distances of the spirals which may be made from them. See also the last portion of ciph. 54, and lugues 50 and 51.

Two main classes of photometric data have been obtained, from which

eventually statistical results of great value may be secured. These are

1. Estimates of the total magnitude of the spiral. Knowing the distance  $D_{\rm LV}$  of selected typical objects, the mean absolute magnitude of these may be deduced through

 $M = m + 7.6 - 5 \log D_{1v}$ 

or similar relations. Then, on the assumption that the "average" galaxy has a given absolute magnitude, the distances may be determined for other objects for which the total apparent magnitude is known. The method differs from that in which a mean diameter is assumed for the spirals in that the density of distribution within the spiral is a factor.

2 Isstimates of the areal brightness, expressed in magnitudes per square second of arc, or in other luminosity units. Our data in this field are due mainly to Wiriz.

The valuable researches of Wiriz on the areal brightness of the spirals seem not to have received sufficient attention as yet, and certain of his numerous correlations may fittingly be repeated at this point, the comparisons are with his quantity Mg, an areal brightness or unit luminosity

I Diameters There is a slight, but not very definitely established

tendency, for an increase of areal brightness with diameter

2 (ralactic Latitude II the absence of the spirals near the galactic plane is due largely to occulting matter, as suggested by Curits and others, a falling off in areal brightness would be expected as this plane is approached. No such tendency is noted. The mean areal brightness of 517 spirals shows but slight variation between  $\pm 80^{\circ}$  and  $\pm 80^{\circ}$  of galactic latitude, and as a matter of fact those nearest to the galactic plane have slightly greater areal brightness.

Calactic latitude	1 80	$\pm 60$	$\pm 40$ ,	1 20°	0,
Mg	11 62	11,65	11,80	11,83	11,35

C Wirtz, Flächenhelligkeiten von 566 Nebelflecken und Steinh infen Land Medd (II) No 29 (1923) While some values were found for the diffuse and planetary types, and clusters, he uses over 500 spirals in his correlations. Wirely labulates the dimensions, both visual and photographic when available, the areal brightness Mg, and the total brightness, H, expressed in mignitudes. His work forms one of the largest and most homogeneous body of data in this field. J. C. Picki ring, Hary Ann. 33, p. 135 (1900). Photometric areal brightness of H objects, ] Horrischik, Wich Ann 20 (1907) Total brightness of 576 objects. ] Hor MANN, Revision of Hollischik's results for 88 objects. A N 211, p. 425 (1921), J. H. Riv NOIDS, The light curve of the Andromeda Nebula, M. N. 72, p. 132 (1913), A. MARKOY, A. N. 231, p 329 (1929), correction abid, 235, p 113 (1930). By methods somewhat analogous to those of WIRIZ, he derives values of the surface brightness of 172 spirals (m per square second of aic), II Shapley, Note on the velocities and magnitudes of external galaxies Wash Nat At Proc 15 p 565 (1929), J S Parask Lyopour os Integrated photographic magnitude of the Small Magchanic Cloud Harv Bull No 840 (1926), P H Starls, the surface brightness of the galactic system as seen from a distant external point, and a comparison with spiral nebulae Ap J 52, p 162 (1920), Mt Wilson Contr No 191 (1920), J. Bicker, A preparatory catalogue for a Durchmustering of nebulae, the General Catalogue Spec Vat 13 (1928) For about 1100 objects the total magnitude is expressed in "grades" these may be converted into magnitudes on the scale of Wiriz by the formula,  $M=10^{m}$ , 32 (N-7), see his introduction, p  $\lambda II$ . See also the references under ciph 54 1011,86

3 Orientation and Form 503 spirals are treated for a relationship between the ratio of the major and minor axes, A, and the areal brightness. The observed areal brightness shows no connection with this ratio, and also no



14g 52 The Spiral NGC 4736. (Alt Wilson Photograph)

dependence upon from which side the spiral is observed. There is further no tendency to a parallelism between the planes of the spirals and the plane of the galaxy.

4 Radial Velocity. No adequate degree of corrolation is found between speed and areal brightness, though the radial velocities show a slight tendency to increase with diminishing areal brightness.

There are patent an logies between the larg spirals and our own galar

more

(60 000 Ly, Kaphyn, au others), see ciph 56 5111 114's estimate of a diamet of 3 105 by allots our g laxy to a much more c ceptional position in the group 221 (Andromeda) a pears likewise to be exce tional as regards lummosi distribution SLARLS four a wide difference between the areal bughtness of th spiral and that of our galact system as seen from a dista point in space, magnitude 23 | per square second are for our galaxy, as again magn 17 18 as estimat for several spirals. Marko however, in the derivation areal brightness for 172 sp rals, finds that 224 is 2 magn, or 12,2 times bright than the average spual, as

76 times brighter than o

assumptions of

modera

5 Total Brightness and Radial Velocity See also ciph 54 A fair well-marked increase of speed with diminishing total brightness is indicate

6 Distance—If the spirals are like galaxies, it would be expected the the areal brightness should be independent of the distance in the statistic mean—Using Lundmark's estimates of the distances of 216 spirals (subject error in comparison with more recent results), Wiriz finds that there is a marked decrease of areal brightness with increasing distance, the reverse is true for the diffuse nebulae.

D • 1051 v	100	10	20	13	9	1 7	6	5	ŀ
Mg No	12 21	12,11	11 67 33	11,52	11 12	11 10	10.89	10 70 7	10.58

The fact that areal brightness is found to diminish with increasing distant is regarded by Wirrz as an indication of the absorption of light in space.



Fig 53 The Spiral NGC 5194-5 (M51) (Mt Wilson Photograph)

galaxy In other work 224 may be exceptional, and thus a portion of the lack of agreement betwee our galaxy and the (typical) spirals would be removed

A recent treatment of this question from the standpoint of absolute manual, etc., is due to Lundmark<sup>1</sup>. He now derives an abs. magn. of ~5,7 f

<sup>&</sup>lt;sup>1</sup> Über die Bestimmung der Entfernungen, Dimensionen, Massen und Dichtigkeit für die nächstgelegenen anagalaktischen Steinsysteme VJS 65, p 275 (1930)

the galactic novae, in comparison with the value —5.5 found for those in 224 on the basis of Hubbi k's distance of that object derived from the Cepheids A relation is next derived for the mean abs magn of the 20 brightest objects in 8 spirals, in the form

$$-6^{3},8\pm0^{3},35+k\sigma_{M^2}=M_{aa}$$

From this relation he derives the distances, total abs magn , and abs magn of the 20 brightest objects,  $M_{\rm so}$ , as follows

Object	1 Halance	Total alm magn.	M.	
Large Mag (I	0,1 × 10 <sup>8</sup> ly	- 17.5	-6,5	
Small Mag ('1	0,1	-17.4	-7.4	
224 (Andromeda)	0,9	-17.2	-7.1	
205	0,9	12,0	_	
598 (M 13)	1,1	15,8	- 6,5	
6822	0,7	-17.2	7,2	

The latest and most authoritative investigations in this aspect of the subject, made as they are with the most powerful instruments, are due to Hubber and Hubbson (references under clph 54). While the primary purpose of their paper is the consideration of the velocity-distance correlation, it may be said that they have drawn upon all methods as yet known in the derivation of the distances of the spirals, the distances of nearer spirals forming a "zero point" rest upon the phenomena of novae and Capheids in spirals, for the more distant objects, they have combined the velocity-distance correlation with correlations based upon total absolute magnitude, the magnitude of the brightest stars visible in individual spirals, and apparent diameter-distance comparisons. Whatever changes may be made in the future in their adopted zero-point, and whether or not a velocity-distance correlation may be proved untenable, their values certainly represent the last that astronomy is able to secure from present observational data

The basal data are derived from 40 objects, for which distances have been determined from stars of recognized types, novae, Cepheld variables, irregular variables, helium stars and P ( ygni stars,

These objects, with the adopted distances, are,

Object	j Metapire	Total abs paym	Abs. mags brightest star	
Large Mag ()	0,095 104 1	y 16,6	5,8	
Small Mag ( ) .	0,085	15,8	-7,4	
6822	0,61	12,0	- 5,6	
598 (M33)	0,77	14,9	-6,3	
224 (Andromeda) .	0,8	-17,0	5,8	
221	0,8	13,2	! ~	
2015	0,8	- 12,7	-	
5457 (M101)	1,3	-13.1	-6,0	
2403	(2,1)	- 15.3	-6,0	
3031 (M81)	. (2,4)	- 16,0	~- 5,8	

For 40 spirals investigation was made of the mean magnitude  $m_r$  of the brightest stars, and the difference between this and the magnitude of the object. The mean of all values is  $m_r - m_a = 8.88$  magn

From these were derived the following important values:

Moun phot also maga brightest stars		- 6,0
Moan vis. also magn of spirals.  Mean plust also magn of spirals.		14,9 13,8
Mean color index		+ 1,1

Given  $m_s$ , the mean apparent magn of the brightest stars in a spiral its distance may be calculated by the formula,

$$\log D_{13} = 0.2 \, m_s + 2.7$$

A close correlation was found between the velocities and the most frequent or mean apparent magnitudes for the clusters of spirals and for two groups of

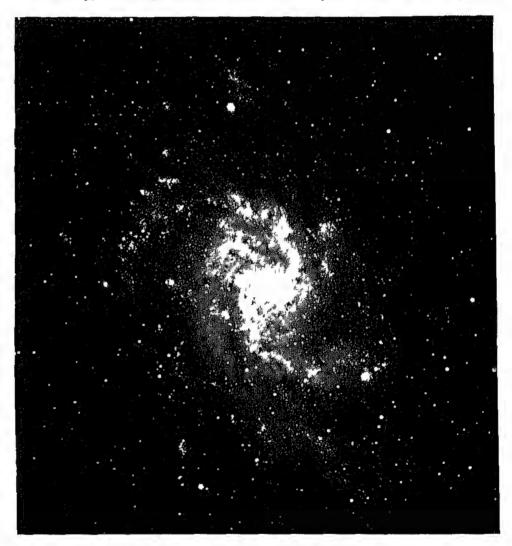


Fig 51 The Spiral NGC 598 (M 33) (Lick Photograph)

isolated spirals, and it was found that the ratio of the red-shift to distance is constant

The distances derived by Hubble and Humason, together with data on clusters of spirals, are given in the next section

Oort's latest treatment of the data now available finds a large spread in the values of  $m-5\log V$ , and concludes that either the luminosity curve of

isolated spirals deviates widely from the one found in clusters of spirals, or else that the galactic system is surrounded by an extensive local agglomeration, the peculiar velocities of which are much smaller than those of outside objects.

56. Distances and Dimensions of the Spirals. Given fairly reliable estimates of the distances of the spirals, and the apparent diameter, it becomes possible to determine their real dimensions, at least approximately. In Table 16 are collected the dimensions of the spirals for which radial velocities are known, and, except for the larger and closer spirals, these depend in general upon values secured through the distance-velocity correlation. If the distance-velocity correlation be accepted, the values of the diameters are still subject to some uncertainty, and it may be that those given for the smallest and most distant objects are two or three times too small, 4, because of uncertainties in this relation,

Table 16. Distances and Dimensions of Spirals: Velocity-Distance.

1 No.	2 Descr.	3 Dimens	A Mg	Rad. vel. km./sec.	6 Dist. 104 Ly.	7 Diameter Ly.
205 221 224 278 380	Spir. Ell. Spir. Spir. Spir.	8' + 3' 2,6 + 1,8 120 + 30 1,2 + 0,3	11 <sup>m</sup> ,7 8 ,0 8 ,8	300 - 185 - 220  - 650  - 4400	0,8 H 0,8 H 0,8 HH 5,0 H 24,0 HH	3 500 1 000? 31 000 1 750 2 100
383 384 385 404 584	Spir.? Spir. Spir.? PH. Spir.?	0,3 0,25 0,25 1,3 2	11 ,1 10 ,6	4500  - 4500   4900   25  - 1800	24,0 HH 24,0 HH 24,0 HH 4,2 dS 11,4 H	2 100 1 700 1 700 4 50 6 500
598 936 1023 1068 1270	Spir. Barr. Spir. Spir. Spir.	55 40 3 2 6 1,3 2,5 1,7 0,5 0,2	12 ,1 11 ,1 10 ,2 9 ,8	70   1300   300   920   4800	0,7 dS 7,7 H 3,d dS 2,3 H 36,0 HH	41 (00) 6 700 5 900 2 400 5 200
1273 1275 1277 1700 2562	Spir.? Spir.? Spir. Spir.? Spir.	0.5 0.5 0.4 · 0.1 0.5 · 0.3 0.4 · 0.2	12 ,4 11 ,1	5800  - - 5200  -  5200   800   5100	36,0 HH 36,0 HH 36,0 HH 5,1 dS 29,5 HH	5 200 5 200 4 200 700 3 400
2563 2681 2683 2841 2859	Spir, Spir, Spir, Spir, Spir,	1,1 : 0,5 2,5 : 1,5 10 : 1 6 : 1,6 1,4 : 0,7	11 pl	4800   700   400   1 600   1 500	29.5 HH 5.8 dS 3.2 dS 5.1 dS 8.5	9400 4200 9300 8900 4100
2950 3031 3034 3115 3193	EIL? Spir. Irr. Spir.? Spir	1,0 · 0,4 10 · 10 7 · 1,5 4 · 1 1,0 · 0,8	0,8 11,0	1 1500 30 1 290 1 600 1 1300	8.5 2.4 HH 2.6 H 3.3 H 7.6	2900 13400 5300 3800 2500
3227 3368 3379 3489	Spir. Spir. t Spir. EII. Spir.	3 1,2 0,5? 7 3,5 2 2,5:1	10 ,7 10 ,2 10 ,3	1150   19600   040  - 810  - 600	8,1 dS 105 HH 5,7 H 4,8 H 3,6 H	7 100 15200 11400 2800 2600
3521 3610 3623 3627 4051	Spir. Spir.? Spir. Spir. Spir.	1,0 · 1,0 1,0 · 0,7 8 · 2 8 · 2,5 4 · 2	10 3 11 ,0 10 ,9 10 ,6 12 ,0	730  - - 1850  - - 800   650   650	4,1 11 1 5,0 11 4,3 dS 5,4 dS	4 700 3 500 11 600 10 000 6 200

(Continued.)

			(Continued.)			
No.	2 Deser.	3 Dimens	$M_{\mathcal{G}}$	5 Rad, vol. km-/sec.	6 Dist. 10* Ly.	Diameter Ly.
4111 4151 4192 4214	Spir, Spir, Spir, Spir, Spir,	0',57 3,8 : 0',5 2,6 : 1,6 8 : 2 8 : 4	10 ,3 10 ,8 12 ,0 11 ,8	+11800 + 800 + 950 + 1150 + 300	150 B 5,8 H 7.3 dS 6,0 HH 2,8 dS	22000 6400 5500 13900 6500
4258 4374 4382 4449 4472	Spir. Ell. Spir. Mag. Spir.	20 · 6 2 · 1,8 4 · 2 3,5 · 2	10 .5 10 ,4 — 10 ,2	+ 500 + 1050 + 500 + 200 + 850	4,6 H 6,0 HH 3,7 dS 2,3 dS 5,7 dS	26800 3500 4300 2300 3300
4486 4526 4565 4594 4649	Elt. Spir. Spir. Spir. Ell.?	2 5 · 1 15 · 1.1 7 · 1.5	10 ,4 10 ,7 11 ,2 9 ,7 10 ,3	+ 800 + 580 + 1100 + 1140 + 1090	5,5 dS 3,9 H 7,6 H 7,2 H 7,5 dS	3 200 5 600 31 000 14 600 4 400
4736 4826 4853 4860 4865	Spir. Spir. Ell.? Ell.? Ell.?	5 · 3.5 3 · 4 0.3 0.5 0.5	11 <sup>m</sup> ,0	+ 290 + 150 + 7600 + 7900 + 5000	3,0 dS 1,3 dS 45 HH 45 HH 45 HH	4 400 3 000 3 900 6 500 6 500
4872 4874 4881 4884 4895	Spir.? Spir.? Ell.? Spir.? Spir.?	1,0 0,2 0,3 1,5 · 0,8 1 · 0,3		+ 6900 + 7000 + 6900 + 67001 + 8500	45 HH 45 HH 45 HH 45 HH 45 HH	13 000 2 600 3 900 19 000 13 000
11 4045 5005 5055 5194 5236	Ell,? Spir. Spir. Spir. Spir.	0,5? 4,5 · 1,5 8 · 3 12 · 6 10 · 8	10 ,9	+ 6600 + 900 + 450 250 500	45 HII 6,6 H 3,6 H 3,0 dS 2,9 H	6 300 8 600 8 300 10 400 8 400
5457 5866 6359 6658 6661	Spir. Spir. Spir.? Spir. Spir.?	27 3 · 1 0,2 0,4 · 0,2 0,5	12 ,2 10 ,9 —	+ 300 + 650 + 3000 + 4100 + 3900	3,0 dS 6,0 dS 21,6 dS 24 23	23400 5200 1200 3100 3800
6702 6703 6710 6822 6824	Spir.? Spir.? Spir.? Mag. Spir.?	0,2 0,3 0,2 20 0,9 · 0.5		+ 2000 + 2000 + 5100 - 150 + 3200	12 12 29 1,0 S	750 1 100 1 600 5 800 5 100
7217 7242 7331 7611 7617	Spir, Ell,? Spir, Spir, Ell,	2,5 · 2 0,5 9,5 · 2 0,7 · 0,3 0,2	11 ,4	+ 1050 + 5000 + 5000 + 3400 + 3900	6 29 5,2 dS 23,5 HH 23,5 HH	1 000 4 600 14 600 4 700 1 400
7619 7623 7626 L. Cl. Sm. Cl.	Ell.? Ell.? Ell. Mag. Mag.	0,8 0,3 0,7 432 216	11,6	+ 3800 + 3800 + 3700 + 280 + 170	23,5 HH 23,5 HH 23,5 HH 0,09 S 0,1 S	5 400 2 000 4 700 11 000 6 500

which has been determined from a relatively small number of moderately close objects, and, 2. because the observed diameters may not record the full extension of the spiral, for reasons noted in ciph. 40.

In the first column of the table will be found the NGC number, a brief characterization, when available, is given in column 2, in column 3 are given the apparent dimensions in minutes of arc, a single value indicating that the object is round, or nearly so, Wirtz' areal brightness, Mg, is given in column 4, column 5 contains the radial velocity, column 6 the distance, expressed in units of  $10^{4} \, \mathrm{ly}$ , in column 7 are given the computed diameters, given in ly Abbreviations used are H = Hubbir R, HH = Hubbir R and Hubbir R, dS = dS Siter R, dS = Shapi Fig. Where no letter follows a distance, it has been computed from the relation <math>D = V/170, where D is in units of  $10^{4} \, \mathrm{ly}$ .

The distances derived from the velocity-distance correlation are taken from Hudhik and Humason's paper in Ap J 74, p 43 (1931), where the following

data are assembled concerning super-galactic groups

The Coma-Virgo Groups

Cluster	) No LALLACA	No. in cL	No	Mean valually Rm./sec.	Mean photo.	Diam.
Virgo	6,0 × 10 <sup>a</sup> l y	(500)	7	+ 890	12,5	12"
Родания	23.5	100	5	+ 3810	15.5	1
Pincon	24,0	20	4	F 4630	15,4	() ,5
Cancer	29,5	150	2	F 4820	16,0	1 ,5
Persous	36,0	500	4	+ 5230	16,4	2 ,0
Comn Beronices	45,0	800	3	1 7 500	17,0	1,7
Ursa Major	72,0	300	1	1 11 800	18,0	0.7
Loo	105,0	400	1	4-1960D	19,0	0,6

We may include here Shapery's results on the diameters of spirals in certain well-populated clusters of external galaxies<sup>1</sup>

Number of galaxies in area		2775
Distance of Cloud A		10,5 10 <sup>4</sup> ly
Diameter of Cloud A		2 10 1 y.
Average diameter of component members		55(x) 1 y
Larger members of Cloud A		
4200 odgow upir		15 500 I y
4216 edgow apir.		18000
4304 open splr		48 600
4321 open spir	•	18900
4382 off		. (5300
4438 splr		24 (XX)
4501 compact spir	h 1	1H 000
4526 oll		18 300
4535 open aptr .		19400
4569 compact spir		16 5(X)
Distance of Cloud B	•	19 10 1 y
Distance of Cloud C		179 to ly
Distance of Cloud D	, ,	169 10 ly
Largest members of ( and D, Diameter		25000 ly
The Centagrus Group		
Number of galaxies in area		1000
Distance of group .		146 40 <sup>4</sup> ky
Length, 7 10°ly		
Width, 1,8 10 1 y		
Diamoter of largest members		45000 ly
Average diameter of members, 15"		9700 ly
The Ursa Major Group		
Distance of group (MAI uguist) .		100 · 10° Ly
Moan distance apart	1 1 1	6.7 10 1.y 7
Diameter of largest members	1 1 1	. 20000 ly
1 77 11-11 Dec Oct 184 (1990)		

<sup>1</sup> Hery Bull 863, 864, 874 (1929)

By way of summary, assuming only the distances and diameters which have thus far been determined for spirals and groups of spirals, there appear to be two main classes as regards size the majority have more moderate dimensions of 2000 to 9000 ly, with a class of grant spirals whose diameters range from 15000 ly to 50000 ly, or more. See also Hubbit 's values, given in Ap. l 61, p. 329 (1926).

Mention should be made here of the results derived by LUNDMARK in his extended paper, "The Relations of the Globulai Clusters and Spiral Nebulae to the Stellai System" [K Svenska Vet Ak Handl 60, No 8 (1920)]. In this paper he has derived distances for 276 spirals, taking the mean of values seemed from their apparent magnitudes and their apparent diameters. These are distributed as follows.

No of spirits	Adopted distrace	Density per 10 ° cub l y	No of spirits	Adopted distance	Density per to <sup>20</sup> cub fo
1	07 1061 y	5 3	()	0,0 10 <sup>6</sup> 1 y	0.3
1 [	1 3	1 1	10	7.2	0.2
4	2,2	0,5	18	9,1	1.0
2 {	3 4	0,5	25	13	0,07
3	3,9	0.5	62	22	0,017
6	4 1	0,5	65	11	0,003
7	5,0	0,4	63	101	DIRRIG3

Lundmark's distances from diameter and magnitude relations are in general larger than those found from the distance-velocity relation, as will be seen from the tabulation below comparing such objects as are common to the two methods

ACC No	Distance from dist vel corr	I USDMARKS dist from much and di un	NGC No	Distance from distact con	TONDWARKS dist
205 278 598	1,0 10 <sup>6</sup> l y 5 0 0 7	7.5 10 <sup>6</sup> l y 45 1 4	4371 1382 1419	6,0 10 <sup>0</sup> l y 3 7 2 3	3,4 + 10 <sup>6</sup> 1 x 6,0 6,5
936 1023	7 7 3.1	28   1	4472 1186	5,7 5,5	5,1 5,8
1068 2681	2 3 5.8	1,5 23	J\$26 4565	3,9 2 6	27 6,8
2685 2841 3031	3,2 5,1	10 1 7,6	1594 4736	7,2 3,0	1 11
3031	2,6	3 0	1826 5005	1,3	1,8 7.1
3115 3368 3521	3, 3 5 7	4,6	5055 5191	2 9 3,0	1.1
3623	4 1 5,0	6,3	5236 5217	2 9 3 0	8,6 3.7
3627 4051 4192	4 3 5,4 6,0	5,2   20 8,2	5157 7217 7331	3 0 7 0 5,2	10 27
4214 4258	2 8 4 6	10	,,,,,	312	11

57 Masses of the Spirals—In general, the estimates of the total mass of typical spirals are roughly of the same order as that derived for our galaxy. The latter is a quantity still imperfectly known, and any derivation of spiral masses requires a large measure of hypothesis and extrapolation—Opin's method assumes that the luminous materials of the spirals have the same coefficient of

<sup>1</sup> Ap J 55, p 406 (1922)

emission as those in our own galaxy, while Hubble (1 c) uses the spectrographic rotation. Lundmark assumes the mass-hubble law effective in all such systems, and starts from the total abs magn. (see the preceding Section). He points out that the total gravitational mass must be larger, and postulates largeration of dark material. The value derived from the total abs magn is styled the luminosity-mass, while that derived from spectrographic rotation values will be a gravitational mass. Lundmark assembles the following values, to which have been added determinations by Hubble (H), and Opik (O)

Object	Caravitation-mass	Ratio ital clark to itan autica	Stern per	Authority
224	0,2 · 1010O	20 1	0,006	1 1.
	3,5 10	44( \ 65)		11
	1.6 10			. 0
1594	2.0 10 <sup>9</sup>	!		11
	2,0 104	i		O
	100			One
	1 1010	30 1	0,042	l.
3031	70 1010	100 1	0,20	1.
5194	0,1 1010	10 1	0.012	1.
Coluxy	10 1010	10 1	0,08	ı i.

58. THE BRUGGENCATE'S Theory of Elliptical Spirals. The investigations of Hubbie, I'm Bruggencate, and others may fittingly be mentioned at this point

HUBBIE's very thorough and detailed investigation is based upon observations made with a self-registering microphotometer, and he derived isophotal curves for the following 15 elliptical objects

221	1278	1472	3115	4 182	4621
410	1281	1486	3179	4406	1749
584	4374	4552			

The isophotal contours are approximately circles for globular objects (Hubbi R's E0), except for the extremely clongated objects (E7), the deviations of the contours from symmetrical ellipses are slight. An interesting investigation is made of the projected densities of different types of structure, and he gives a comparison of the density distribution in the projected images of the mean elliptical soral, an isothermal gas sphere, and a bounded gas sphere

REYNOLDS believed that he had detected evidences of polarization in the spiral 4826 (M64). Green and Meyer, however, were anable to substantiate any such effect in a number of nebulae of various types which they tested

Somewhat in contrast to these failures to detect polarization are two Brug-Gencate's recent results. He investigates the spatial distribution laws of a nebula symmetrical through rotation, and extends the theory to the case where the isophotal surfaces within the object are concentric, counial, and similar ellipsoids of rotation. He finds a satisfactory agreement between his values and those observed by Hubble (supra). Based on Hubble's results, ten Bruggerichte concludes that all elliptical objects have the same axial ratio, about 10°3, and in support of this, the probabilities of different degrees of ellipticity are investigated. To a first approximation, the brightness within the ellipsoid diminishes

<sup>1</sup> Is Hubber 1 the distribution of luminosity in elliptical nebulae Ap J 71, p 231 (1930). P TEN BRUGGERG ATE, Die Helligkeitsverteilung im Junern elliptischer Nebel / f Astroph 1, p 275 (1930), 2, p 83 (1931), J H Reynords, Proliminary observations of spiral nebulae in polarized light M N 72, p 553 (1941). W K Green, An investigation of certain nebulae for evidence of polarized light Publ A 5 P 20, p. 108 (1917), W F Meyer, A study of certain polarized for evidence of polarization effects. Publ A 5 P 31, p 494 (1919)

as the inverse square of the distance from the center. He therefore interprets the elliptical objects as conglomerations of particles, rather than stars

"Die elliptischen Nebel dürften aus einem zentralen Kein bestehen, der als Lichtquelle dient, und dessen Licht in der ihn umgebenden Mateie nicht merklich absorbiert und remittert, sondern gleichmäßig nach allen Seiten gestreut und reflektiert wird. Die von Hubbert emprisch gefindene Beziehung, die Identität der Intensitätsverteilungen in den Projektionen aller elliptischen Nebel ausdruckt, bildet den Schlussel zum Verständnis des physikalischen Zustandes dieser kosmischen Objekte. daß elliptische Nebel keine durch ihre große Entfernung nicht aufzulosende Sternwolken sein konnen. (\*)

The structure is postulated as transparent throughout the greater part, and the particles reflect and disperse the light from the nucleus in all directions Taking Hubbit's value of the radius, call 1000 ly, the total average mass is placed at  $10^8$  O, and the effective density is of the order of  $10^{-25}$ . The diameter of the "nucleus" is of the order of  $10^3$  ly, with a mean density of about  $10^{-19}$ , the mean free path of the particles in the outer portions is of the order of 10 ly

There are a number of very serious objections to this theory of 1EN BRUGGEN-

- I All existing evidence as to super-galactic groups indicates that the elliptical and the true spirals are inextricably intermingled as to arrangement and location. This theory assumes an entirely different constitution for these bodies, as contrasted with their immediate neighbors in space. This is most improbable.
- 2 From this contiguity in space with the spirals, and from the areal and apparent brightness of the elliptical objects, then total abs magn must be of the same order as that of the spirals —15 to —17. This accordingly requires that the "nucler" of the elliptical objects be sources of tremendous energy, equivalent to absolute magnitude —15 or higher. No such "sources" are known with certainty.
- 3 Furthermore, we should expect that the light from such central sources would be polarized, or that it would show selective reflection or absorption effects. None have been detected
- 59. Theories of Spiral Structure: Introductory<sup>1</sup> The structure of the spirals, showing as it does so frequently two well-marked spiral whorls starting
- of spiral and planetary nebulae Ap J 4, p 97 (1896), Dynamics of a nebula A J 20, p 67 (1899), f C Chambi rin, On the possible function of disturbive approach in the formation of meteorites, comets, and nebulae Ap J 14, p 17 (1901), The origin of the earth Chicago (1916), E Strömgrin, Übei die Bedeutung kleiner Massenänderung für die Newtonsche Zentralbewegung A N 163, p 130 (1903), J II Jeans, The stability of a spherical nebulae Proc R A S Lond 68, p 454 (1901), Problems of cosmogony and stellar dynamics. Cambridge (1919), Astronomy and cosmogony Cambridge (1928), M Woll Length of axes and position angles of 52 oval nebulae M N 68, p 626 (1908), II Knox Shaw, On the inclinations of the planes of some spiral nebulae to the galaxy. M N 69, p 72 (1908), W Suthfriand, Bode's law and spiral structure in nebulae Ap J 34, p 251 (1911). I J J Sell, Evolution of the stellar systems, 2 (1910), E v d Pahlen, Über die Gestalten einiger Spiralnebel A N 188, p 240 (1911), P. Norkl, Über die Entwicklung der kosmischen Nebel. A N 188, p 353 (1911), E Belot, Explitance reprodusant les spires des nebuleuses spirales. C R 154, p 1780 (1912), G W Watker, Some problems illustrating the forms of nebulae Proc R S Lond (A) 91, p 440 (1915), G F Becker A possible origin for some Spiralnebulae Wash Nat Ac Proc 2, p 1 (1918), B Hlerassimovitch, Sur les mouvements tourbillonances dans les nébuleuses. A N 126, p 81 (1919), K Bottlinger, Zur Bildung der Spiralnebel. A N 210, p 5 (1919), C V L Charlier, Sur les nébuleuses spirales. C R 169 p 430 (1919), M Valier, Die Gestalt der Nebelflecke, insbesondere der Spiralnebel. A N 212, p 17 (1920), criticized by Notke, ibid, p 373, H Jettrilys, On Jeans' theory of the origin of spiral nebulae. M N 83, p 449 (1923), Jeans' answer, ibid. p 458 II Vog1, Beiting zur Entstehung der Spiralnebel. A N 220, p 97 (1923), H Groot, On the true shape of some spiral nebulae. M N 85, p 535 (1924), On the spiral form of some nebulae ibid, 86, p 146

from exactly opposite points on a nuclear portion, has long been a puzzle. No adequate, complete, and entirely satisfactory theory of the spirals as a result of classical dynamical laws has as yet (1932) been derived. A satisfactory theory of the forms assumed by the sorrals must then

A Furnish a reasonable dynamic explanation of the origin, shape, motions

within, and permanence of the spiral whorls

B It must explain why these take their origin at points 180° apart on a nuclear portion (very difficult!)

( The component matter of the structure must be taken to be discrete

stars, rather than gas, or dust particles

The literature of the field is already very extensive, and additions are

constantly being made to it

60. Agreement of Spiral Arms with Mathematical Spirals A number of mathematical curves show more or less close approximation to the observed forms of the whorls of the spirals Some of these, with the law of attraction required in outh case (Ser. I c.), are The gravitational sorral.

$$r^{2}(\psi - \psi')^{2} - c$$
,  $P = \frac{h^{2}}{4}$ 

The spiral of Archimedes,

$$P = \frac{h^4}{r^2} \left(1 + \frac{2a^4}{r^2}\right)$$

The logarithmic spiral,

$$r = a^{\theta}$$
,  $P = \frac{k^2}{r^2}(1 + \log^4 a)$ 

The lituus.

$$r^{4}(l) = u^{4}, \qquad P = \frac{h^{4}}{r^{4}} \left(1 + \frac{4a^{4}}{r^{4}}\right)$$

The hyperbolic spiral,

$$r(l) \quad a, \qquad P = \frac{h^4}{r^2}.$$

The parabolic spiral,

$$(r-a)^{\frac{n}{2}} = 4ca\theta$$
,  $P = \frac{h^{\frac{n}{2}}}{r^{\frac{n}{2}}} \left(1 + \frac{3a^{\frac{n}{2}}(2o+1)^{\frac{n}{2}}}{r^{\frac{n}{2}}}\right)$ .

Spirals of other types show even more complex functions. It will be noted that only for the gravitational, logarithmic, and hyperbolic spiral is the law of force a relatively simple one, being as the inverse cube of the distance, for the other common types of spiral the law of force depends upon the third and fifth, or third and seventh power of the distances. It is unnecessary to emphasize that no cosmic forces are known whose action varies in this way

(1926), J H REYMOLDS, The condensations in the spiral nebulae M N 85, p. 142 (1924). The forms and development of the spiral nebulae, ibid, 85, p. 1014 (1925). The spiral form and development of the Andromeda Nebula, ibid, 87, p. 112 (1926), F A. Ledemark, Note on the constitution of the spiral nebulae M N 83, p. 314 (1923). Approved by Reymolds, ibid, p. 182, criticized by Perrine and Gifford, ibid, p. 272, 283, E. W Brown, Gravitational forces in spiral nebulae. Pop Astr 32, p. 545 (1924), Ap J 61, p. 97 (1925) later views, Oles 51, p. 277 (1928), B Lindblad, Cosmogonic consequences of a theory of the stellar system. Ups Modd No. 13 (1926), On the spiral orbits in the plane of a spheroidal disk, with applications to some typical spiral nebulae, ibid. No. 31 (1927), On the nature of spiral nebulae. M N 87, p. 420 (1927), H Maris, The formation of spiral nebulae. Phys Rev (2) 31, p. 1103 (1929), C Parvut esco, Sur in dynamique des nébuleuses spirales R A J 3, p. 157 (1927), J C. Sol.A, Algunas consideraciones sobre las nebulesses en spiral Rev Soc Astr Esp 2, p. 149 (1929). Roy Soc Astr Esp 2, p 149 (1929)

There is a general, though not entirely unanimous, agreement among those who have investigated the whorls of typical spirals, that, on the whole, these curves approximate most closely to those of the logarithmic (also called equangular) spiral. In this curve, the angle between the tangent to the curve and the radius vector to the given point should be constant, and equal to are tan  $(1/\log_e a)$ 

E V D Pahli in made careful measures of the whoils of three large spirals 598 (M33), 5194—5 (M51), and 628 (M74). He found the agreement of all three with the logarithmic spiral relatively close (there are, in all such investigations, considerable variations in the density, width, or location of salient features in the whoils which can only be explained as chance inegularities, resulting doubtless from random differences of distribution in the original mass or aggregation). The spiral of Archim dels was tested in 598, but did not give nearly so good a measure of agreement as the logarithmic spiral. It was impossible to substantiate any similarity with Wieczynski's gravitational spiral (see ciph. 61).

- L BICKIR made measurements of the points in both whoils of 5194-5, with a least squares reduction. His measures result in an empirical spiral with characteristics as follows
- a) The two whoils are practically duplicates, and corresponding points stand diametrically opposite to each other, and equally far from a certain point near the middle of the central condensation
- b) Times of length  $r_p = a + bl^2$  may be drawn from the points of the real spiral to the line of sight which passes through the central point, and these lines, when displaced parallel to themselves to a point, all lie in a plane. The longitude of the node of this plane is 160°, and its inclination 42°.

The essential duplication of the whorls is taken as an indication that the motion is outwards, for it is deemed unlikely that matter coming in from outside would arrange itself in two identical whorls 180° apart. The assumption is made that the increase in the longitude of the moving particles is proportional to the time. Such a relation is found possible with a certain spheroid whose equator coincides with the plane of the spiral, in which each particle acts according to the inverse square of the distance, and with a density varying from the center outward. The law of such a required density variation is investigated, and the resulting calculated curve shows a fair agreement with the observed contour of the whorls.

II (GROOI made an extended series of measures on the following eight large spirals (nine sets are given, on 17 individual spiral arms, but one spiral was measured twice) 5194 - 5 (M51), 4258, 3198, 4321, 4501, 4725, 3623, and 3031. The logarithmic spiral, the spiral of Archimedes, and the litius were all tested All the 17 arms investigated could be properly represented by the logarithmic spiral. Only 5 whorls (two each in 3623 and 3031, and one in 4321) could also be represented by the spiral of Archimedes of the litius, and it was thought that this was partially explained by the fact that the arms of these spirals could be investigated only over a very limited range. Equations were set up for each whorl investigated, and the two found for 4321 may be selected as examples

```
1321 whoil I \log r = 12011 - \{8,9106\} q
1321, whoil II \log r = 11761 - \{9,0327\} q
```

The fairly close agreement of the constants of the equations for the two whorls in this and in practically all the other spirals studied indicates essential duplication for the whorls of individual spirals, and argues for an evolution proceeding from within outward. The total range in the value sof the angles

between the tangents to the whorls and the radii vectores is remarkably small (73° to 86°), the greatest range found for the two whorls of the same spiral was 4°, the mean value for all whorls measured is 79°. Some evidence was found for aksimess in the arms of 3031, the structure of all the others seems to be in one plane. Six other spirals were investigated by Groot in his second paper, with essentially the same conclusions.

REYNOLDS has measured the configurations of a number of spirals and, in general, agrees with Groot as to their correspondence with the logarithmic spiral. The objects investigated were 5247, 2835, 4254, 4321, 1232, and 5457. He finds, however, a greater degree of irregularity in the run of the angles between the tangent and the radius vector. "The angle made by the tangent of the curve with the radius vector is usually between 50° to 70° in the earlier part of the curve, but in more advanced stages the angle may be anything between 40° and 80°. In many cases these extremes may be observed in the two arms and hifurcations of the same spiral" He regards both the filamentous and the massive spirals as in an advanced stage of development, and points out that spirals developed for less than half a revolution are rare, while spirals developed for more than two revolutions in an actual spiral form are unknown.

61. Wilczyman's Gravitational Spiral. Most earlier theories attempting to explain spiral structure are influenced by the hypothesis of gaseous constitution. The most general assumption has been that of a rotating gaseous spheroid, though dust-clouds which have been repelled from regions near the galactic plane have also been suggested Schaerence even proposed that the spirals were formed by matter ejected from volcanoes! Repulsive forces acting from the nucleus outward have also been a favorite method (radiation pressure, etc.) giving rise to the "Dampistrahl" or "pin-wheel" theory of whori formation.

The theory of the origin of the solar system from a (small) spiral in the planetesimal hypothesis of Chamberlin and Moulton is well known. This theory suggests that a spiral would be formed by the disruptive tidal action of two stars making a close approach. While this theory has been carefully and rigorously worked out by its authors, they admit that the enormous dimensions of the spirals make their origin in this way untenable (solar system: mass 1,001 ©; diameter, ca. 0,001 Ly.; Andromeda Nebula: mass 3,5 · 10° ©, diameter ca. 31000 l,y l).

Among earlier attempts to identify the class of curve assumed, mention must be made of the gravitational spiral of Wilczynskii. His explanation is as suitable for a stellar composition as for other constitution. The component elements are assumed in his theory to revolve about a center of attraction under the action of gravitation, the inner components will manifestly rotate more rapidly than the components on the periphery, and initial irregularities as regards density of distribution will thus in course of time trail out into the whorls of a gravitational spiral. The number of whorl-turns will give an indication of the age of the spiral through the formula.

$$t = \frac{2\pi x}{\omega_1} \frac{1}{1 - (a/b)^{4/3}}$$

Here a and b are the radii of the circles between which the structure of the spiral lies,  $\omega_1$  is the angular velocity of rotation at the inner circle, u the number of turns, and t the clapsed time or age.

WILCZYNSKI's theory agrees with the observational data in the following respect: it gives a direction of rotation in the same direction as is indicated by SLIPHER's spectrographic determinations of rotation.

The theory appears to fail in the following points

- a) No adequate explanation is given of the diametrical symmetry of the two sets of whorls
- b) The curves of a gravitational spiral do not "fit" the great majority of the curves observed. One has only to draw a gravitational spiral on a sheet of semi-transparent paper and place it over available reproductions of spirals to establish the entire lack of agreement.

In this connection one may compare the theory of G F Becker, where the nebular aggregation is assumed to start in the form of an extended cylinder or rod, to which the term "bacular" is applied. Such forms, if existent at all, are exceedingly rare among observed spirals, the long and narrow spindles seem always to be more reasonably interpreted as relatively thin disks seen edgewise.

62 Jeans' Theory of Spiral Structure. Jeans' cather theory is a byproduct of his extensive stellar investigations collected in his Problems of Cosmogony<sup>1</sup>. Through a complicated dynamical investigation, the details of which can not be given here but must be sought in the work quoted, the initial state of a spiral is assumed to be a rapidly rotating, gaseous, lenticular disk, with sharp peripheral boundary, this form is regarded as represented by numerous examples of edgewise spirals (4565, 4594, etc.). Small tidal forces due to distant objects of the same class are postulated as the cause of the ejection of matter from points 180° apart on the periphery of the lenticular disk

"Thus our conjectural interpretation of all spiral nebulae is that they are masses of gas or clouds of dust in rotation, the rotation being so rapid that no figure of statical equilibrium is possible. In the earlier stages of their evolution, they must have passed through a series of figures of equilibrium of the Pseudo spherical type discovered in Chapter VII, until a sharp edge was formed. (Wayker has criticized this feature of Jlans' development.) After this, matter was ejected along the two arms originating from the spiral edge. At first the points of origin of these arms were determined by the infinitesimal tidal forces set up by other objects or the rest of the universe, subsequently, the tidal forces from the symmetrical arms themselves would suffice to confine the emission to two antipodal points."

Jeans' theory gives no statement of the law governing the forms of the arms thus tidally ejected, nor any comparison with the spiral forms observed. His earlier calculations of the distance between condensations in the spiral whorls, mass of the nuclear portion, etc., were influenced by the attempt to satisfy van Maanen's internal motions. In a later note<sup>2</sup>, Jeans revised his earlier computations to take account of the character of a spiral as an island universe. The differences are naturally considerable, in view of the change in the adopted distance of 224 (Andromeda) from 5000 ly. to 9000000 ly. The revised mass of the nucleus is  $5 \cdot 10^{12}$  g, or  $2.5 \cdot 10^{9}$  O, regarded as significantly near the estimated total mass of our galaxy.

63. Brown's Theory of Spiral Structure. Like Jeans, Brown in his earlier work on the subject had attempted to set up a reasonable gravitational mechanism to account for the spirals and at the same time to satisfy van Maanen's values of the internal motion. His second paper bids fair to be a very important contribution to the problem. Unfortunately, his complete analysis has not yet been published, so that comparison between theory and observation is not possible as regards the shape of the spiral arms<sup>4</sup>

<sup>&</sup>lt;sup>1</sup> Cambridge (1928) <sup>2</sup> M N 85, p 531 (1925) <sup>3</sup> Obs 51, p 277 (1928) <sup>4</sup> In the abridgements of this and other theories treated in the balance of this paper, as is permissible in a survey of progress, statements will frequently be phrased in the exact words of the author, but with the omission of quotation marks

The system of the spiral is supposed to originate in a lons-shaped aggregate of stars arranged in an ellipsoid of revolution. The distances between the component stars are very great in comparison with their diameters; the number of stars is postulated as very large. Furthermore, the number of stars in a given

volume of the ellipsoid is assumed to be everywhere the same.

A field of force varying directly as the distance was chosen, this field permits circular motion, and deviations from circular motion which are symmetrical across the center, which is a vital factor in explaining the diametrical symmetry of the spiral whorls. The mathematical treatment is then made to depend upon two well-known gravitational phenomena. If such a particle or star be attracted toward a fixed center with a force  $-n^2\tau$ , it can move in a central ellipse with a mean angular velocity, n. Uniform distribution of the stars within the ellipsoid, if the flattening be considerable, will then cause the star to move under a force  $-K\tau$ , in an ellipse whose center coincides with that of the ellipsoid, and every particle will be moving with nearly the same angular velocity about the polar axis of the flattened disk.

The initial requirement of constant density of distribution can be waived provided the amount of matter in a cylindrical volume standing on an element of area of the equatorial plane be proportional to  $(i - r_1^2/a^2)^{1/2}$ , where  $r_1$  is the distance of a particle (star) from the center, and a is the external radius. It is this function which admits of an observational test by counts of stars at different distances from the center. A dominating central mass is thus abandoned

in favor of the action of the entire field upon the star.

A near (but not too near) approach and passage of a similar aggregate of the same order of total mass disturbs this field by a kind of "tidal" force which has several effects which can be separately considered. Actual distortions of the figure are small, and are bound to be subject to oscillations which are soon masked by other effects. There also arise variations of density which have a maximum along one axis in the equatorial plane and a minimum along an axis perpendicular to it, a change of density also occurs along any radius of this plane, the linear rate of change being proportional to the distance from the center This gives the appearance of a bar, nearly straight, across the plane of the object, (Compare a similar feature in LINDBLAD's theory, clph. 64, and note the great importance of this feature as an explanation of the relatively frequent barred spirals.) The altered gravitational field will eventually cause this bar to coll into a spiral, the "colling" being produced by the radial variation of density. During the process the "arms" become denser, and the coiling (finally) becomes so close that the evidence of structure disappears. At this stage, the aggregate has reverted substantially to its original condition, and on Brown's theory the elliptical objects or close-packed and "compact" spirals may be "late" instead of "early".

Knots or subordinate aggregations in the arms are attributed (the least satisfactory of Brown's postulates) to the approach of another similar aggregate which starts a new set of arms, the intersection of the two sets producing the

condensations (?).

Brown's theory may then be summarized as requiring an initial very populous aggregation of stars which by rotation has assumed the shape of a flattened ellipsoid of revolution. The start of the spiral arms requires an approach to another similar large aggregation. The postulate of this approach is the most difficult point in this or any similar theory, such approaches would seem to be of almost vanishing rarity. The theory has the following very notable points of merit:

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a) It provides for the symmetry of the two whorls from the nature of the central force adopted

b) It gives a possible explanation of the frequent occurrence of barred spirals

c) Alone among existing theories, it offers a dynamical explanation of the rotational results secured by Pease (see ciph 46) in that the spiral rotates essentially as a whole

It does not, however, give any law for the curves observed in the spiral arms

64. Lindblad's Theory of Spiral Structure Lindblad has been almost the only modern theorist to make a comparison between theory and observation as regards the shape of the spiral arms. His theory rests upon a certain class of spiral orbits which are asymptotic to the peripheral edge of a flattened, rotating ellipsoid. The orbit of a material particle moving in a circular orbit outside the spheroid in the equatorial plane is derived in the form

$$\left(\frac{dy}{d\theta}\right)^2 = \varkappa \left[ \left(2 - \frac{1}{y^2}\right) \arcsin y + \frac{1}{y} \sqrt{1 - y^2} + \frac{4}{3} \mu y \right] + c_0, \tag{1}$$

where

$$\varkappa = \frac{e^4}{\arcsin e - e\sqrt{1 - e^2 + \frac{2}{3}\mu e^3}},$$

and

$$c_0 = 2e^2 \frac{(1-e)^2 \arcsin e - e \sqrt{1-e^2} - \frac{1}{3} \mu e^3}{\arcsin e - e \sqrt{1-e^2} + \frac{2}{3} \mu e^3}$$

In the above

r and  $\theta$  are the polar coordinates in the equatorial plane,

u=1/r,

y = e/r,

e = eccentricity of mendian section,

a = equatorial radius,

 $\mu = \text{ratio}$  of mass of nucleus to mass of spheroid

For (1) there is first substituted the symbolical expression  $\left(\frac{dy}{d\theta}\right)^2 = \psi(y)$ , and for a slightly disturbed motion, when the disturbance does not affect the value of the areal constant, h,

$$\left(\frac{dy}{d\theta}\right)^2 = \psi(y) + \Delta t \tag{2}$$

Since  $\psi(e) = 0$  and  $\psi'(e) = 0$ , for a value of y slightly less than e,

$$\left(\frac{dy}{d\theta}\right)^2 = \frac{1}{2} \psi''(e) (\delta y)^2 + \cdots \Delta c \tag{3}$$

The condition for the appearance of an asymptotic spiral orbit is then,

$$\psi''(e) > 0, \tag{4}$$

and this orbit possesses the characteristic feature that  $du/d\theta$ , or  $dy/d\theta$ , has a minimum value at y = e or u = 1, and a maximum value for some smaller value of y, corresponding to a greater distance.

<sup>&</sup>lt;sup>1</sup> LINDBLAD's papers on the subject have appeared at intervals preceding 1928 in the Ark Mat Astr Fys of the K Svenska Vetensk Akad, and issued also as Ups Medd The more important papers are Ups Medd Nos 13, 19, and 31 No 31 is Series III, Vol IV, No 7 of Handl K Svenska Vetensk Akad, and contains a summary of his preceding investigations, and diagrams showing agreement with the whorls of known spirals

LINDBLAD then selects four values for  $\mu$ : 0, 1/2, 1, and 2, which give for the ratios between the central mass and the total mass the values

0, 1/s, 1/s, and 1/s

With these values of  $\mu$ , and with values of  $\sigma$  equal to unity or very slightly less (e.g., for  $\mu=0$  the values  $\sigma=1,000,0,995,0,980,0,965,0,950, and 0,920 were successively chosen), he then performed the numerical integration of equation (1) and tabulated the resulting values of <math>\xi$  and  $\eta$ , and from these derived the corresponding curves. Those for  $\mu=0$  were found closest to observed spiral whorls.

The equation was next integrated for  $\mu = 0$  and s = 0.995, with the assumption of a small but finite disturbance. For this purpose the square of the area constant,  $h^2$ , was assumed to be 10% smaller than in the first integration. The resulting curve gave better agreement and later, using  $\mu = 0$  and  $\epsilon = 0.965$ , a quite close agreement was found for the calculated spiral and the arms of 3031 (M81). See Figure 55 and 56

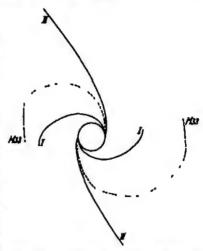


Fig 55 Theory of Spiral Structure. (LIMDHLAD) Theoretical curves] for s = 0,99, compared with the spiral arms of 598 (M33)

The impetus necessary to cause a star to pass from its orbit on the periphery of the rotating "mother system" over into the asymptotic spiral is assigned by LINDBLAD to one of two causes:

a) It is supposed that this may result from the tidal action of exterior systems, as in Brown's theory, producing a condensation along one axis of the system, and a corresponding rarefaction along the axis at 90° from this.

b) In the absence of sufficiently atrong tidal forces, it is postulated as conceivable that the matter rotating most rapidly in the "mother system" may be ejected as a consequence of a certain type of sectorial harmonic waves analogous to that which renders the MACLAURIN ellipsoid of a homogeneous liquid "ordinarily" unstable.

While it is pointed out that either of these postulated forces need be slight enough only to cause a star to pass over the boundary into an asymptotic spiral orbit, neither cause seems entirely convincing.

Furthermore, there is a "turning point" in all of Lindhiad's spiral orbits at a finite distance, except for the case  $\mu = 0$ , s = 1,000, where it is at infinity This point marks the greatest distance from



Fig. 56 Limbelan's Theory of Spiral Structure. The spiral arm of 3031 (M81) compared with the theoretical curve for  $\theta \approx 0.97$  (dotted curve) a is the apparentarin, b, the shape of the arm in the plane of the spiral, assuming an inclination of 60°

the nucleus which a star will reach in its asymptotic spiral orbit; after passing, this point its distance will decrease. While there are slight inward bendings at the outer ends of the whorls of some spirals, the theory is scarcely supported by these random and infrequent irregularities, and it is legitimate to ask why this re-entrant portion of the curves is not a prominent feature of most spirals.

H Vogr¹ has attempted to derive a theory which attributes the recession of the spirals and their internal mechanism to one and the same cause, a postulated "cosmic repulsion" This repulsion, from the results of Hubbli and Humason, is evaluated as

$$\frac{1}{R}\frac{dR}{dt} = \alpha = 1.8 \cdot 10^{-17} \,\text{sec}^{-1}$$

The equations of motion are then written in the form.

$$\frac{d^2r}{dt^2} - r\left(\frac{d\theta}{dt}\right)^2 + \frac{GM}{r^2} - \alpha^2 r = 0,$$

$$\frac{d}{dt}\left(r^2\frac{d\theta}{dt}\right) = 0, \quad \text{or} \quad r^2\frac{d\theta}{dt} = h,$$

in which  $\alpha$  is assumed not to vary with the time. Integration of these equations gives

$$v^{2} = \frac{2GM}{r} + \alpha^{2} r^{2} + Ch^{2}.$$

while the radius of curvature is given by

$$\varrho = \frac{v^3}{h \left[ \frac{GM}{r^3} - \alpha^2 \right]},$$

C and h are constants of integration

When  $\alpha^2$  is less than  $GM/r^3$  the orbit will be a spiral concave to the center of attraction, when  $\alpha^2$  is the greater, the curve will be of hyperbolic character and convex to the origin

Assembling the numerical data for 224 (Andromeda, outer portions),

$$M = 2 \cdot 10^{42} \text{ g}$$
  
 $r = 2 \cdot 10^{22} \text{ cm}$   
 $G = 6.66 \cdot 10^{-8}$ ,  
 $\alpha = 1.8 \cdot 10^{-17}$ ,

he finds that  $\alpha^2$  (GM/r³) = 0.02, approximately, 1 e , the spiral is here concave to the origin

Vogt's theory assumes

- 1 A "cosmic" repulsion as the "Dampfstrahl" component.
- 2 Motion outward along the spiral aims

It gives no explanation of the diametrical symmetry of the two spiral whorls. Furthermore, there should come a time when the whorls will change from a form concave to the origin to one which is convex. In the numerical example given, this will take place when r increases to a value 3.7 times its present value  $(50^{1/3})$ . That no spirals are found with such hyperbolic outer whorls, in fact, none with more than two or three spiral circuits, is naively attributed to the present youth of the universe

65. Theories of Spiral Structure Summary. It will be noted that the "pin-wheel" theory of the spiral arms, Lindblad's asymptotic spirals, Jeans' hypothesis, and all theories which postulate the ejection of matter at diametrically opposite points from a rotating spheroid, as well as van Maanen's measures, seem to require motions proceeding mainly outward along the spiral arms. It is not easy to reconcile this feature of most theories with Slipher's direction

<sup>&</sup>lt;sup>1</sup> Zur Dynamık der Spıralnebel A N 243, p 405 (1931)

of rotation of the spirals "the motion is invariably that similar to a spiral spring when it is being wound up" Equally difficult is a comparison of such theories with Prace's rotational results. Brown's theory of stars in a spheroidal mass, all rotating with nearly the same angular velocity, comes closest to observation in this respect.

Though the present writer does not share the philosophy of despair voiced by Jeans<sup>1</sup> it is perhaps fitting to close this discussion of theories of the structure of the spiral arms, none as yet entirely adequate, with a few quotations giving some of his recent views.

"It seems almost impossible to explain pure rotation dynamically in terms of known forces, and we are led to the disconcerting, but almost inevitable conjecture, that the motions

in the spiral nebulae must be governed by forces unknown to us

The only result that seems to emerge with some clearness is that the spiral arms are permanent features of the nebulae. They appear to have been formed in the process of ahrinkage, two convolutions or thereabouts being formed by each nobula, and to have been perpetuated in static form over since.

Their further interpretation forms one of the most puzzling, as well as disconcerting,

problems of cosmogony

Rach failure to explain the spiral arms makes it more and more difficult to resist a suspicion that the spiral pobulae are the seat of forces unknown to us, which may possibly express novel and unsuspected metrical properties of space."

66. Evolutionary Status of the Spirals. These considerations can be presented very briefly, in view of the length of the discussion to follow on the larger aspects of cosmogony raised by the spirals. There is a general agreement that the spirals are structures of a galactic nature. The larger members of the class, at least, seem to be vast congeries of suns, whose linear dimensions, masses, and total number of component stars are approximately of the same order as the similar relations in our galaxy. Our galaxy, in turn, is the most accessible spiral for study, just as our sun is the most accessible star.

Nothing is as yet definitely known as to the laws which govern the characteristic structure of the spirals, nor as to the direction of the evolutionary process exhibited in them as a class. We do not know certainly whether the process as now observed is one of formation, permanency, or disintegration However, from the time which light takes to reach us from such enormous distances (10° to 10° or more light-years), and from the analogy of the present similar condition of that member of the class in which we are situated, the relative permanency and quasi-eternal duration of these great structures seems a certainty. It seems further self-evident that they represent the main, if not the only, course of evolution exhibited by the macroscopic cosmos as accessible to our investigation

- 67. Cosmogonical Deductions: Introduction. A large literature is rapidly assembling whose subject matter is the formulation of that larger cosmos of which the millions of other galaxies (the spirals) form the individual units. While the greater number of such speculations (for few would claim for these any other terminology in the present state of our knowledge) are attempts to include the spirals and their predominant characteristics of size, constitution, and tremendous velocities of recession, in some form of "relativity universe", emphasis should here be placed upon the fact that this, at present, is not the only alternative. There are still two alternatives, and may forever be two:
  - 1. An infinite Newtonian universe of the CHARLIER type.
  - 2. A closed universe, infinite only in the relativity sense.

<sup>&</sup>lt;sup>1</sup> Astronomy and Cosmogony, pp 351-2 (1928).

68 The Charlier Infinite Universe<sup>1</sup>. There have been several vague and somewhat inchoate cosmical structures postulated by philosophers which involve the assumption of system on system (e.g., Lambert), but these must be dismissed as hypotheses for which observational bases did not yet exist, and more or less common as a speculation among thinking men of all time

In all older astronomical treatises, and in some which are comparatively recent, we find the familiar statement that an infinite universe is an impossibility, were it infinite, the night sky should be everywhere as bright as the sun. This objection can be shown to be mathematically true, granted only that a density of stellar distribution equal to that of our galaxy be assumed to extend outward without limit. A more serious and equally cogent earlier objection to an infinite universe came from the dynamical dilemma arising from an infinite mass-total, here also it can be shown that a regularly distributed infinite universe must give rise at some point to an infinite attraction and corresponding infinite velocities.

So far as is known to the writer, the first statement that these arguments against an infinite universe might be nullified by a particular and artificial arrangement of the component stars or systems is due to Proctor<sup>a</sup>

"But there is another way in which we may explain the darkness of the sky at night, without assuming either the extinction of light, or that occupied space is an infinitely minute speck amidst an infinity of vacant space. Assuming our system to form one of a finite number of such systems, separated from each other by distances bearing a very large ratio to the dimensions of each, and that thus a system of higher order is formed, which again forms one of a finite number of similar systems, and so on continually, the dimensions of each system of whatever order being always very small in comparison with the distance separating it from its neighbors, then there would no longer result as a necessary consequence even an appreciable illumination of the whole heavens."

OLBERS' criterion for the postulation of a uniformly luminous sky was as follows<sup>3</sup>

"So wird also nicht bloß das ganze Himmelsgewölbe von den Sternen bedeckt, sonde in sie müssen noch hinteremander in unendlichen Reihen stehen, und sich unteremander wieder verdecken Es ist klar, daß derselbe Schluß stattfundet, wenn die Firsteine nicht gleichförmig im Raume, sondern in einzelne Systeme mit großen Zwischennäumen verteilt sind."

Seeliger's treatment of the dilemma of infinite mass in the cosmos is contained in his paper, "Über das Newtonsche Gravitationsgesetz" 4

"Es wird deshalb notwendigerweise zwischen den beiden Annahmen eine Wahl zu treffen sein, i die Gesamtmasse des Weltalls ist unei meßlich groß, dann kann das Newtonsche Gesetz nicht als mathematisch strenger Ausdruck für die heitschenden Anziehungskiäfte gelten. 2 das Newtonsche Gesetz ist absolut genau, dann muß die Gesamtmaterie des Weltalls endlich sein oder genauer ausgedrückt, es dürfen nicht unendlich große Teile des Raumes mit Masse von endlicher Dichtigkeit erfüllt sein "

<sup>&</sup>lt;sup>1</sup> To call this hypothesis the Lambert-Charlier system is neither fitting nor just The speculations of Lambert, Kant, and other earlier thinkers are guesses, nothing more, and too deficient in scientific character to warrant the annexing of their names. A reference to the appropriate passages in Lambert's Cosmologische Briefe, Augsburg (1761), with its assumptions of multitudes of tomets, central "Regent" attracting masses, and the like, E g, p 304

<sup>&</sup>quot;Wenn die Frasternsysteme solche Körper zu Regenten haben, ob sie nicht wieder zusammen ein größeres System ausmachen, in dessen Mittelpunkt wieder ein Regent ist, der seinen Wirkungskreis durch dieses größere System ausbieitet? Die Systeme zusammen genommen machen bereits die Milchstraße aus Findet sich, daß jedes oder wenigstens nur eines derselben einen Regenten habe, so mag die Analogie sicher fortgehen, und die Milchstraße hat auch einen der sie ganz beherrsche und herumlenke"

CHARLIER's method of obviating the consequences of the criteria of OLBERS and SEELIGER may be described as a mathematical extonsion of the mystical speculations of early philosophers. He imagines the material elements of the cosmos arranged in a series of systems, with essential identity in the component elements of each system or stage

Let  $N_1$  stars, each of radius  $R_0$ , form a galaxy,  $G_1$ .

Let  $N_1$  galaxies, each of radius  $R_1$ , form a super-system of the second order,  $G_1$ 

Let  $N_a$  systems of the second order, of radius  $R_a$ , form a still higher system of the third order,  $G_a$ , etc, etc

A distance  $r_i$  is then defined on the assumption that  $N_i$  spheres of radius  $r_i$  would be equivalent in volume to the system  $G_i$ , that is,  $r_i$  satisfies the equation

$$N_{i} \frac{4\pi}{3} r_{i}^{3} = \frac{4\pi}{3} R_{i}^{6},$$

$$R_{i} = r_{i} \sqrt{N_{i}}.$$
(1)

OT

Then  $2r_i =$  the distance of a component in  $G_i$  to the next component. The mass of any system will be.

$$M_i = N_i N_{i-1} N_{i-2} \cdot N_2 N_1 M_0,$$
 (2)

where  $M_0$  is the mass of the initial element, a star.

Considering now a star  $G_0$  which lies on the boundary of a galaxy,  $G_1$ , and that each succeeding system in turn lies on the boundary of the next system above it, the total attraction of all such higher systems on the star  $G_0$  will take the form:

 $\frac{M_1}{R_1} + \frac{M_2}{R_2} + \frac{M_3}{R_2} + \cdots$ 

The condition for the convergence of this series is that  $M_d/R_i^2$  shall be less than  $M_{i-1}/R_{i-1}^2$ , or, from equation (2):

$$\frac{R_i}{R_{i-1}} > \sqrt{N_i} \,. \tag{3}$$

This is CHARLIER's fundamental relation, and if this inequality between the radii of the successive systems is satisfied, the total attraction of a CHARLIER universe on the given star will not be infinite, but finite. Such an arrangement will then satisfy the criterion of SEELIGER.

By a similar analysis it is further found that the criterion of Olders reduces to the same relation between the radii and the number of components, i.e., if this same inequality is satisfied, the total luminosity of an infinite Charlier universe as seen from a star thus situated will be finite in amount.

A value is next found for the total luminosity received by a star situated at the center of the lowest system, this amount is found to be greater than for any other location, and in addition the inequality satisfying the two criteria remains unchanged; hence the relative position within a system has no effect in invalidating the inequality.

If instead of the respective radii of the systems and supersystems one employs the distances between the elements of a system,  $2\tau_i$ , there results from equations (1) and (2) the following inequality which must be satisfied for both Olders' and Skeliger's criteria.

$$\frac{r_i}{r_{i-1}} > N_{i-1}^{i/2} N_i^{i/4},$$
 (4)

<sup>&</sup>lt;sup>1</sup> C. V. L. Charler, How an infinite world may be built up. Ark Mat Astr Fys 16, No. 21 (1921), Lund Medd. No. 98

and this in turn will reduce to

$$\frac{r_i}{r_{i-1}} > \sqrt[n]{N_i} , \qquad (5)$$

If the various systems are assumed to have each the same number of components. The velocity of a body at the limit of a system  $G_i$ , supposing that the velocity at infinity is zero, will be

$$v_i = \frac{h \sqrt{2M_i}}{\sqrt{R_i}},$$

whereas the velocity at the limit of the next sub-system below will be

$$v_{i-1} = \frac{h\sqrt{2}N\widehat{I_{i-1}}}{\sqrt{R_{i-1}}},$$

whence

$$v_i \quad v_{i-1} = \sqrt[3]{R_{i-1} \over R_i}, \tag{6}$$

resulting in the following inequality as regards the velocity necessary to satisfy the two criteria

 $v_i < v_{i-1} \sqrt[4]{N_i} \tag{7}$ 

If a particle falls inward from the limit of a system, supposed spherical, and with initial velocity = 0, the velocity will be

$$v = \frac{k \sqrt[k]{M_t}}{\sqrt{R_t}} \tag{8}$$

Now the interesting and highly significant fact in Charlila's theory of an infinite universe is that, so far as this is accessible at present, the arrangement of objects and systems is precisely what would be expected on such a theory. That is, we do have aggregations of 10<sup>10</sup> or more stars arranged in a galaxy, while at distances relatively very great compared with the distances between the stars or the diameters of the galaxies we observe a very large number, perhaps  $3 \cdot 10^7$ , similar galactic structures

It is perhaps not necessary to assume that we see more than a part of the super-system  $G_2$ , and the existence of such higher arrangements as  $G_3$  and  $G_4$  must remain highly speculative. There is a natural tendency to regard the well-populated clusters of galaxies in the Coma-Virgo, Ursa Major, Centamus groups, etc., as distinct  $G_2$  systems. Their comparatively limited numbers (1017) might be against such a deduction, and lend support to the consideration of such groups as merely local regions of greater density of population within the system  $G_2$ . Their community of radial velocity is, however, rather a strong argument for them  $G_2$  character, forming separate units in the super-system  $G_3$ . See Appendix No. 8

While an effort to set up an extended Charlier arrangement must be regarded as merely an interesting speculation, the attempt is not without value. One needs only to be limited by approximations to the mass of a galaxy, by assumed bounds to the total number of galaxies within  $G_2$  systems, and by permissible upper limits of velocity

It is, of course, entirely possible to speculate upon radically different arrangements under the Charlier scheme, and still satisfy the inequalities which render nugatory the criteria of Olbers and Seeliger. As a matter of fact, the tentative scheme illustrated in Table 17, should doubtless be changed to smaller values of the number of units in a  $G_2$  system, in view of data at hand for clusters of galaxies

6 yerlom	G <sub>e</sub>	G,	G <sub>0</sub>	G,
Object	Blar	Spiral	Super-galaxy	Super-system
N <sub>1</sub> M <sub>1</sub> R <sub>2</sub> Vol 1 d <sub>3</sub> Abs. magn Mean V <sub>1</sub> Av app. magn Av dist. apart Diam at av dist.	1 2 · 10 <sup>30</sup> g 7 · 10 <sup>3</sup> km — + 5 6,8 km./sec 30 l y	10 <sup>8</sup> stars 4 10 <sup>48</sup> g 3 · 10 <sup>4</sup> l y 3 10 <sup>87</sup> cm s 8 10 <sup>-84</sup> -15 168 km /sec. 12 10 <sup>7</sup> l y	10 <sup>6</sup> galaxies 4 10 <sup>48</sup> g. 10 <sup>6</sup> l y 4 10 <sup>51</sup> cm s 9 · 10 - 68 - 30? 1700 km / sec 25 3.5 10 <sup>18</sup> l y	10 <sup>8</sup> super-gal 4 · 10 <sup>36</sup> g 10 <sup>25</sup> Ly 3,6 · 10 <sup>36</sup> cm 9 · 10 <sup>-41</sup> -50?

Table 17 Tentative Illustration of Charlier's Systems.

Note The mass of the galaxy has been multiplied by the factor 2 to provide for non-luminous matter. The average distance apart prosupposes symmetrical cubical piling. The velocity and average distance apart are for the given system in the system  $\overline{l+1}$ .

Using 10° for the number of the spirals, and 10° for the number of stars in a spiral, etc., Charling derives the following inequality for the limiting angular diameter of a spiral.

$$\alpha < \frac{1}{N^{1/\alpha}}$$

whence the nearest spiral to us should have an angular diameter less than 5°,7; 224 (Andromeda) is about 2°. Also, he finds that the apparent magn. of the nearest spiral should not be greater than ca. 4,5 (Andromeda, 4,6 magn.) He finds furthermore that the radius of the farthermost spiral in the super-galaxy (with the numerical data assumed) should be smaller than 3',4, and it should be fainter than the 15th app, magn. His estimate of the distance of the most remote spiral, on these assumptions, is 54 · 10° l.y., doubtless too small, but of the order of some recent estimates. With the same initial data, he finds that the velocity of a spiral should be less than 178 times the velocity of the stars in our galaxy, giving a value less than 5300 km./sec (present maximum, +19600 km /sec)

There seems no escape from the conclusion that it is possible to arrange an infinite universe on Charler's scheme, without causing infinite luminosities or infinite velocities, and the close parallelism of his plan with the observed arrangement of the accessible visible cosmos is cartainly startling. Any mean velocity for spirals or for super-galaxies composed of spirals may be provided for by the postulation of suitable values for the masses, number of units, and distances apart. It is to be noted, however, that while the Charler construction can be made to provide for any mean velocity of the spirals, it must be admitted that, in its original form, it offers no explanation of the preponderance of velocities of recession. See Appendix No. 8 for further treatment

69. The Spirals and Relativity Universes: Introduction<sup>1</sup>. The very large amount of reference material, of which the more important treatments are given below<sup>1</sup>, on this aspect of the position of the spirals, together with the high standing

<sup>&</sup>lt;sup>1</sup> A. Riveterm (with Grassmann), Entwurf einer verallgemeinerten Relativitätstheorie und einer Theorie der Gravitation. Z f Math Phys Jan. (1914), Die formale Grundlage der allgemeinen Relativitätstheorie. Szber Berl (1914), p. 1030; Zur allgemeinen Relativitätstheorie, ibid. (1915), p. 778, Erklärung der Perihelbewegung des Merkur ans der allgemeinen Relativitätstheorie, ibid (1915), p. 831; Die Feldgleichungen der Gravitation, ibid (1915), p. 844; Die Grundlagen der allgemeinen Relativitätstheorie, Ann Phys 49, p. 769 (1916), also published separately by Bartn; Näharungsweise Integration der Feldgleichungen der

of the authors quoted, is a sufficient proof of the importance of this comparatively recent cosmological development, and warrants a somewhat detailed treatment

In roughest outline, the development of ideas postulating universes of the relativity type during the past thuty years has been about as follows

- 1 1900 Schwarzschild discusses the characteristics of non-Euclidean closed universes
- 2 1914-1918 EINSTEIN develops his general theory of relativity and postulates a closed cylindrical universe whose "radius" is a function of the amount of matter contained in it

Gravitation Szber Berl (1916), p 688, Kosmologische Betrachtungen zur allgemeinen Relativitätstheorie, ibid (1917), p 147, Kritisches zu einer von Herrn Dr Sittier gegebenen Lösung der Gravitationsgleichung, ibid (1918), p 270, Prinzipielles zur allgemeinen Relativitätstheorie Ann Phys 55, p 243 (1918), The new field theory Obs 52, p 82 (1929), Zum kosmologischen Problem der allgemeinen Relativitätstheorie 5/ber Beil (1931), p 235, W DE SITTER, On the relativity of mertia Amst Proc 19, No 9, 10 (1917), On the curvature of space, ibid 20, No 2 (1918), On Einstein's theory of gravitation and its astronomical consequences MN 76, p 699 (1916), 77, p 155 (1916), 78, p 1 (1917), 1hc. expanding universe Discussion of Lemaîtic's solution of the equations of the merital field BAN 5, p 211 (1930), Remarks on the astronomical consequences of the theory of the expanding universe, ibid, 5, p 274 (1930), On the distances and radial velocities of the extra-galactic nebulae and the explanation of the latter by the relativity theory of incitia Wash Nat Ac Proc 16, p 474 (1930), Some further computations regarding non-static universes BAN 6, p 141 (1931), Do the galaxies expand with the universe? ibid , 6, p 146 (1931); R C Tolman, On the astronomical implications of the de Sitter line element for the universe Ap J 69, p 245 (1929), The effect of the annihilation of matter on the wave-length of light from the nebulae Wash Nat Ac Proc 16, p 320 (1930), On the estimation of distances in a curved universe with a non static line element, ibid, 16, p 409, 511 (1930), G LEMATERT, Un univers homogène de masse constante et de rayon croissant, rendant compte de la vitesse radiale des nébuleuses extra-galactiques Ann Soc Sc Biux 47, p 49 (1927), translated into English in M N 91, p 483 (1931), On the random motion of material particles in the expanding universe Explanation of a paradox BAN 5, p 273 (1930), The expanding universe MN 91, p 490 (1931), On thermodynamic equilibrium in a non-static universe Wash Nat Ac Proc 17. p 153 (1931), McCrea and McVITTIE, On the contraction of the universe M N 91, p 128 (1930), Proc Edinb Math Soc (2) 2, part 3 (1931), G C McVIIIII, The problem of n bodies and the expansion of the universe M N 91, p 274 (1931), A S EDDINGION, On the mstability of Einstein's spherical world M N 90, p 668 (1930), cf Nat 125, p 850 (1930), On the significance of Einstein's gravitation equations in terms of the curvature of the world Phil Mag (6) 42, p 800 (1921), 43, p 174 (1922), K Schwarzschild, Übei den zulässigen Krümmungsradius des Raumes V J S 35, p 337 (1900); II D Robertson, On the foundations of relativistic cosmogony Wash Nat Ac Proc 15, p 822 (1929), A FRIEDMAN, Z f l'hys 10, p 377 (1922), P HARZER, Übei die astronomischen Ergebnisse dei allgemeinen Relativitätstheorie AN 227, p 81 (1926), K LANCZOS, Über eine stationäie Kosmologie im Sinne der Einsteinschen Gravitationstheorie Zf Phys 12, p 73 (1924), Über die Rotverschiebung in der de Sitterschen Welt, ibid , 17, p 168 (1923), V FREEDERICHEU A SCHECH-TER, Notiz zur Frage nach der Berechnung der Aberration und Patallaxe in Einsteins, de Sitters und Friedmans Welten in der allgemeinen Relativitätstheoile ZIPhys 51, p 584 (1928), K Lundmark, The determination of the curvature of space-time in de Sitter's world M N 84, p 747 (1924), H Vogr, Die Instabilität der Welt A N 241, p 217 (1931), Die kosmologische Deutung der Spiralnebel, ibid , 242, p 181 (1931), J Chazy, Liffet Doppler-Fizeau dans l'univers de de Sitter CR 183, p 1093 (1926), C Wires, De Sitters Kosmologie und die Radialbewegungen der Spiralnebel AN 222, p 21 (1924), F Spiraty, Beitinge zum kosmologischen Problem Ann Phys (4) 68, p 281 (1922), F Zwicky, On the red shift of spectral lines through interstellar space Wash Nat Ac Pioc 15, p 773 (1929), Phys Rov (2) 33, p 1077 (1929), L SILBERSTEIN, The determination of the curvature radius of spacetime M N 85, p 285 (1925), of ibid, 84, p 747 (1924). The curvature of de Sitter's spacetime derived from the globular clusters, ibid, 84, p 363 (1924), New determination of the radius of space-time Pop Astr 38, p 92 (1930), The radial velocities of globular clusters and de Sitters cosmology Phil Mag (6) 47, p 907 (1924), Nat 113, p 350, 602, 818 (1924), 114, p 347 (1925), 125, p 850 (1930), The size of the universe, attempts at a determination of the curvature radius of space time, Oxford Press, (1930), VIII +215 pp.

3. 1917—1929. DE SITTER, FRIEDMAN, TOLMAN, and others, develop further the idea of an Einstein closed, static universe, with excess of positive velocities among distant objects

4. 1927—1930 Lemaître finds a paradox in the static Einstein universe, and shows that it must be expanding. The latest papers of DE SITTER accept the idea of an expanding universe, and it is enthusiastically adopted by EDDING-

TON

"Hence the radius of the universe has expanded by one part in 2000 in the last million years. The result is impressive. It indicates that the radius of space has doubled within ordinary geological time. We conclude that the radius of space was originally about 1,2 · 10 1 y. that it has since expanded considerably, but to an amount practically undeterminable, and that its present rate of expansion is 1 per cent in about 20 million years—a rate which will continue indefinitely. The universe is now doubling its radius every 1400 million years and this rate will, if anything, slightly increase in the future. In 10 to years the spiral nebulae will be 10 magnitudes fainter than they are now. With a time scale of billions of years, astronomers must count themselves extraordinarily fortunate that they are just in time to observe this interesting but evanescent feature of the sky." (i) [M.N.9.), p. 677 (1930)]

5. 1929—1930. Tolman discusses the DE SITTER line element with rigor, and finds that the earlier conclusions as to uniform excess of velocities of recession are less inevitable than earlier held.

"The conclusion is drawn that the DE SPITER line element does not afford a simple and unmistakably evident explanation of our present knowledge of the distribution, distances, and Doppler affects for the extra-galactic nebulae" [Ap J 69, p 245 (1929)]

6 1930. Basing their investigation upon the line element of a universe containing matter scattered throughout and, in addition, with a concentration of matter around the origin, two Scotchmen, McCrra and McVrrre, come to the conclusion that a contraction process is as probable as one of expansion.

"It seems therefore that a condensation starting in an RINSTRIM universe would cause this universe to contract .. We must conclude that if the actual universe started as an Redination universe and is now expanding, as the work of Lemattre and Redinator suggests, this expansion can not have been caused by a redistribution of the matter into mussive nuclei. Thus, as yet, no mechanism for setting up the expansion has been found."

Schwarzschild's initial paper on this general subject is an academic discussion of the possibility of various types of hyperspace rather than a treatment along relativity lines. By making estimates of the lowest limits of error in angular measurements now attainable, he derives the corresponding limiting dimensions for several forms of hyper-space. In the case of hyperbolic hyper-space, he shows that any radius of curvature larger than ca. 63 l.y. would be difficult to detect by present methods. In elliptical hyper-space the corresponding minimum detectable radius of curvature is found to be ca. 2500 l.y., with a "distance around the world",  $\pi R$ , of  $8 \cdot 10^{\circ}$  ly.

The EINSTEIN field equations are now available in many treatises (see references quoted). The general course of the historical development of these theories as relating to the excess of velocities of recession among the spirals has already been outlined. A complete study of this entire development would involve, first, a large amount of repetition in the treatment of the line element by the various investigators, combined with some measure of confusion due to occasional differences in mathematical nomenclature, and, secondly, such a treatment would in many cases, for completeness, be involved with discussions of the relativity effects adduced for the deflection of light in a gravitational field, and the shift of the Fraunhoffer lines to the red in such fields: questions which are of interest in other fields of astronomical investigation, but in no way germane to the present problem of the spirals.

For these and other reasons, the detailed treatment of the work done by the multitude of investigators will be greatly abridged, and will be replaced with a somewhat composite treatment drawn in the main from two or three of the latest workers in this subject a method which has some elements of the illogical, but also many advantages on the score of convenience and brevity.

The investigation chosen to represent the EINSTEIN-DE SITTER universe will be that of Tolman<sup>1</sup> Several reasons have motivated this choice 'Ioiman's paper is one of the latest in point of time, and is definitely restricted to the problem set by the large positive velocities of the spirals. Furthermore, it not only possesses great clarity of treatment, but it appears to the present writer to display a commendable and judicial saneness, in that no all-embracing inspiration is claimed, but difficulties are finally emphasized

The subsequent theory of a necessarily expanding universe, as treated originally by Lemaître and Friedman, and also by Tolman on the theory of the annihilation of matter, will be drawn mainly from Limaître's original paper on the subject, and also from recent papers of Eddington and Distitut Following a description of these methods of treatment, a summary will be given of

the radu of various postulated relativity universes

70. Tolman's Critique of the DE SITTER Relativity Universe Tolman employs DE SITTER's form of the line element, as derived from Einstein's generalized equation

$$-8\pi T = G_{\mu\nu} - \frac{1}{2}Gg_{\mu\nu} + \lambda g_{\mu\nu}$$

and the line element itself is an expression in angular variables of an element on the surface of a four-dimensional sphere of radius R

$$ds^2 = -R^2 \left[ d\omega^2 + \sin^2 \omega \left\{ d\zeta^2 + \sin^2 \zeta \left( d\theta^2 + \sin^2 \theta d\varphi^2 \right) \right\} \right],$$

Substituting the variables  $\omega$  and  $\zeta$  by

$$\cos \omega = \cos \chi \cos \iota t,$$
$$\cot \zeta = \cot \chi \sin \iota t,$$

and placing further

$$\sin \chi = r/R$$
,

the equation of the line element is written in the form:

$$ds^{2} = \frac{1}{1 - r^{2}/R^{2}} dr^{2} - r^{2} d\theta^{2} - r^{2} \sin^{2}\theta d\varphi^{2} + (1 - r^{2}/R^{2}) dt^{2}. \tag{1}$$

The geodesic equations will take the following forms from the norm form (after Eddington)

$$\frac{d^3x_\alpha}{ds^2} + (\mu\nu, \alpha)\frac{d\nu_\mu}{ds}\frac{d\nu_\nu}{ds} = 0, \qquad (2)$$

$$\frac{d^2r}{ds^2} + \frac{1}{2} \frac{dr}{dr} \left(\frac{dr}{ds}\right)^2 - re^{-\lambda} \left(\frac{d\varphi}{ds}\right)^2 + \frac{1}{2} e^{\nu - \lambda} \frac{d\nu}{dr} \left(\frac{dl}{ds}\right)^2 = 0.$$
 (3)

This is integrated best by substitution of the values found from (5) and (6), finding the equation

$$\frac{dr}{ds} = \pm \sqrt{k^2 - 1 + \frac{r^2}{R^2} - \frac{h^2}{r^2} + \frac{h^2}{R^2}}.$$
 (A)

<sup>&</sup>lt;sup>1</sup> Ap J 69, p 245 (1929)

With  $\alpha = 2$  the geodesic equation is that of a particle moving in the plane  $\theta = \pi/2$ , with  $d\theta/ds = 0$ , in accordance with the equations:

$$\frac{d\theta}{ds} = 0, \qquad \frac{d^2\theta}{ds^2} = 0, \qquad \theta = \frac{\pi}{2}, \tag{4, B}$$

$$\frac{d^2\varphi}{ds^2} + \frac{2}{r}\frac{dr}{ds}\frac{d\varphi}{ds} = 0, (5)$$

the integral of which is:

$$\frac{d\,\eta}{d\,s} = \frac{h}{r^2}\,,\tag{C}$$

$$\frac{d^3t}{ds^3} + \frac{dv}{dr}\frac{dr}{ds}\frac{dt}{ds} = 0. ag{6}$$

The integration of (6) gives:

$$\frac{dt}{ds} = k e^{-r} = \frac{k}{1 - r^2/R^2}.$$
 (D)

In the above, h and k are the constants of integration; h can assume positive or negative values according to the direction of motion of the particle, while k, a time-like constant, can be only positive unless time is supposed reversible. For the special case of light, both h and h become infinite.

The form of the orbit is obtained by dividing (C) by (A), with rearrangement of terms:

$$d\varphi = \frac{h\,dr}{r^2 \left| \sqrt{\frac{r^3}{R^3} + \left(k^2 - 1 + \frac{h^2}{R^3}\right) - \frac{h^2}{r^3}} \right|}.$$
 (7)

This is the form of the relation, in Newtonian mechanics, applying to the shape of the orbit due to a central repulsive force proportional to the radius r. Hence in the DE SITTER universe the orbits of free particles are in general curved away from the origin,

Perihelion of the particle will be found by making  $dr/d\varphi = 0$ . Hence perihelion will be obtained by making the quantity under the radical sign in (7) equal to zero, or:

$$k^2 - 1 + \frac{r_M^2}{R^2} - \frac{h^2}{r_L^2} + \frac{h^2}{R^2} = 0.$$
 (8)

The velocity of motion of the particle in its orbit will be:

$$\frac{dr}{dI} = \pm \frac{(1 - r^2/R^2)}{h} \sqrt{k^2 - 1 + \frac{r^2}{R^2} - \frac{h^2}{r^2} + \frac{h^2}{R^2}}.$$
 (9)

From the equation of the original line element, putting  $ds^2 = 0$ , the purely radial velocity of light becomes:

$$dr/dt = \pm (1 - r^2/R^2). {10}$$

In both the preceding expressions the velocity becomes zero at r = R. Hence all movement ceases at the radius R from the origin. Furthermore, since the integral of (10) shows that light would take an infinite time to travel over the radius R, we can never have any information of events happening at R or beyond, and hence may speak of a horizon to the universe at this distance.

TOLMAN determines the DOPPLER shift in two ways, with the origin at the observer, and with the origin at the source. In the first of these methods, the period of emission, from equation (E), will be:

$$dt_o = \frac{k}{1 - r^2/R^2} ds, \qquad (11)$$

during which the source will have moved the justial distance

$$\partial_t = \frac{dt}{dt} dt_0 = \frac{k}{1 - \mu t_0} \frac{dt}{dt} dt_0,$$
 (12)

and, by equation (10) for the velocity of light, the time taken by light to traverse the distance will be

Hence the period of the light arriving or the origin will be

$$dt_{ij} = \frac{1}{1 - |I| R^{ij}} dt_{ij} \pm \frac{h}{(1 - |I| R^{ij})^2} dt_{ij} dt_{ij}, \qquad (11)$$

where the plus aga applies to recoding object. As the principal is propositional to the majority observed at the origin and do no the models is in the product in the constant.

$$\frac{df}{1} = \frac{h}{1 - r^2/R^2} + \frac{h}{(1 - r^2/R^2)^2} \frac{dr}{dt} - 1 \tag{11}$$

Sabstituting from equation (y), the Dorricks shift is obtained in terms of the parameters of the orbit and the distance alone

For the Dorrigen while with the source at the neutro, (14) will take the locus

By patting drift = 0 in equation (14), the Doppers a client of the supple in at purposes at the time of envision is

$$\frac{d1}{T} = \frac{b}{1 - PDR} = 1, \tag{17}$$

where re is the distance from the origin to pseudolion, and this equation, by the application of (6) can be rewritten in the form

Since he are not be negative and Re is larger than it, this may be written as the magnetity.

$$\frac{dl}{l} \ge \frac{1}{l(1-l)^2 l^2} - 1,$$
 (19)

or, expanding and neglecting higher order terms

whence the Durrent effect at pertrolog as positive, and would ordinarily be misspeeded as a velocity of recention.

However, it is not always possible, and the most valuable part of Toruas's analysis to be determinated of the approximate relative durations of the positive and negative Dorrects offices of the moving patitole in such a universe.

The equations of motion in a DE SITTER universe are completely reversible, as was first pointed out by Silberstein, and there seems no a priori reason why the number of positive and negative velocities among the spirals should not be approximately equal. Torman therefore next investigates the conditions for a reversed Dopplen effect, 1. s , as a particle in a peStres universe, though at rest at perficien, will give the effect of a positive velocity of recession, over what range of its orbit will this positive velocity effect be of sufficient magnitude to cancel its negative velocity as it approaches perihebon?

In order to investigate the range of such a reversed Doppler effect, 42/2 is set equal to zero in equation (15), giving as the condition for the radius r,. at which reversal takes place.

$$\frac{r_r}{R^2}-\frac{h^2}{r_r^2}=2-2k,$$

while equation (8) gives as the condition for perhelion

$$\frac{r_0^k}{R^k} - \frac{h^k}{r_0^k} = 1 - h^k - \frac{h^k}{R^k},$$

no that the reversed Doppler effect will be produced when an approaching source lies in the range between r, and rea. Since it is found later that k is of the order unity, and halks of the order zero, the range of such a reversed Doppler effect will be small Taking the radius re at which an oncoming source would come into observation as twice the distance to perihelion, which in its turn is taken as one-tenth of the distance to the horizon, which will give a Doppler shift at perihelion, d1/1 = 0,005, the fraction of the time of approach to perihehon during which the particle would lie within the range which produces the reversed

offect is only about 1/2 (0,038)

As possible explanations of the facts observed in the spirals, TOLMAN

considers in detail some four hypotheses.

A. The Hypothesis of Continuous Entry Here the uniform concentration of spirals within our observation would be produced by the continuous arrival of new objects to take the place of those which have passed perihelion and will never return. On this hypothems, as the range of the reversed Dorples effect has been shown to be so small, there should be nearly an equality of the velocities of approach and recession Only by making some rather radical assumptions as to the numbers of spirals which make perihelion at different distances from the origin, and making the assumption that the number of spirals which make perihedron at a given radius increase very rapidly with the radius, can the excess of velocities of recession be accounted for A linear increase of DOPPLER effect with distance is possible, but in no way inevitable. The radius of the observable universe must be at least ten times the range of distances at which spirals are now observed, as otherwise higher values would be expected than have been observed (order of 0,01) R would therefore not be less than 2 · 10 1.y.

B. The Hypothesis of Continuous Formation. The process of formation would be a continuing one, which will permanently maintain an approximately uniform concentration of the spirals. Thus idea is ahandoned as having little inherent probability. R on this hypothesis would be about 2 10° Ly

C. The Hypothesis of a Concentrating Fluctuation This assumes that the present concentration is the result of a finetuation from a smaller general concentration, which has occurred some time in the past. The chief demerit of this hypothesis is its appeal to some sort of special fluctuation in the concentration to account for the observed facts.

1 2

D The Hypothesis of Recent Formation, seems even more improbable than that of continuous formation, and for that reason may be abauted at once

The conclusion which Tolman draws from his investigation is that the DE Sitter universe gives us no simple, adequate and, more than all, inevitable explanation of the facts exhibited by the spirals. In particular, he shows that only by rather drastic ad hoc specifications can this assemblage of data be explained at all. In detail, it can not be regarded as a satisfactory mechanism for the production of the present excess of large velocities of recession.

71 An Expanding Relativity Universe the Work of Lemaîtri, Eddington, McCrea, and McVitte. If the spherical universe is to be permanent and unchanging, the solutions of Einstein and de Sitter are both permissible. Robertson, and others, have shown that these are the only two possible solutions under such a condition. Lemaîtri has shown, however, that these universes are intrinsically unstable. That of Einstein has been described as containing "all the matter it can hold", while that of in Siller is empty of matter. Eddington points out that there are an infinity of solutions for a spherical universe which is not in equilibrium, and that to every expanding solution there corresponds an individual contracting solution.

Lemaître places the pressure, p, equal to zero, while p is the density of the total energy. The density of the radiant energy will be 3p, and the density of the energy concentrated in matter,  $\delta = p - 3p$ .  $\delta$  is identified with T, while p and -p are identified with the components  $T_1$  and  $T_1 = T_2^2 - T_1^2$  of the tensor of material energy. The components of the contracted Riemannian tensor are calculated for the interval;

$$ds^2 = -R^2 d\sigma^2 + dt^2 \tag{1}$$

Here  $d\sigma$  is the element of length in a space of radius unity, R is the radius of space, and is a function of the time. This feature is the essential advance of Lemaître's analysis, and has been followed in the latest papers of Tolman, Eddington, and de Sitter

The equations of the gravitational field are written

$$3 \frac{1}{R^2} \left( \frac{dR}{dt} \right)^2 + \frac{1}{R^2} = \lambda + 8\pi \varrho \,, \tag{2}$$

$$\frac{2}{R^2} \frac{d^2 R}{dt^2} + \frac{1}{R^2} \left(\frac{dR}{dt}\right)^2 + \frac{1}{R^2} = \lambda - 8\pi\varrho. \tag{3}$$

In the above,  $\lambda$  is a cosmological constant whose piecise value (or even its precise signification) is unknown, it is, however, very small  $8\pi$  is Einsti in's constant, which is written  $\varkappa$  by Lemaître.

A solution is then sought for the case where the mass of the universe remains constant while the radius increases. Calling this total mass  $M=V\delta$  and placing  $8\pi\delta=\alpha/R^3$ , where  $\alpha$  is a constant, and by aid of the relation  $\varrho=\delta+3\rho$ , the principle of the conservation of energy becomes

$$3d(pR^2) + 3pR^2dR = 0. (4)$$

Einstein's constant .  $8\pi = 1.87 \cdot 10^{-27} \text{ c. g s.}$ Gravitation constant  $k = 6.675 \cdot 10^{-8} \text{ s.}$ Unit mass  $= 4.045 \cdot 10^{98} \text{ s.}$ Mass of sun  $= 1.87 \cdot 10^{-27} \text{ c. g s.}$   $= 4.045 \cdot 10^{98} \text{ s.}$  $= 2.32 \cdot 1.48 \text{ km.}$ 

 $<sup>^{1}</sup>$   $8\pi$  is a constant in "natural" units. Some values in the natural and in the CG5 system which are frequently employed in such investigations are

Placing  $\beta$  as the constant of integration, this is integrated to

$$8\pi p = \frac{\rho}{R^4},\tag{5}$$

and hence.

$$8\pi\varrho = \frac{\alpha}{R^6} + \frac{3\beta}{R^8}.$$
 (6)

Substituting these values in (2), he derives

$$\frac{1}{R^3} \left( \frac{dR}{dt} \right)^3 = \frac{\lambda}{3} - \frac{1}{R^3} + \frac{8\pi\varrho}{3} = \frac{\lambda}{3} - \frac{1}{R^3} + \frac{\alpha}{3R^3} + \frac{\beta}{R^4}, \tag{7}$$

where.

$$t = \int \frac{dR}{\sqrt{\frac{\lambda R}{3} - 1 + \frac{\alpha}{3R} + \frac{\beta}{R^a}}}.$$
 (8)

Placing  $\alpha$  and  $\beta$  equal to zero and integrating, the solution of DE SIFTER is found:

$$R = \sqrt{\frac{3}{\lambda}} \cosh \sqrt{\frac{\lambda}{3}} (t - t_0). \tag{9}$$

Einstein's solution will be found by making  $\beta = 0$  and R = a constant. Since dR/di and  $d^2R/di^2$  then become = 0 in (2) and (3), and

$$\frac{1}{R^2} = \lambda$$
,  $\frac{3}{R^2} = \lambda + 8\pi\varrho$ ;  $\varrho = \frac{2}{8\pi R^2}$ ,

whence.

$$R = 1/\sqrt{\lambda}; \qquad 8\pi\delta = 2/R^2, \tag{10}$$

and, from (3)

$$\alpha = 8\pi \delta R^4 = 2/\sqrt{\lambda}. \tag{11}$$

For Einstein's solution, (14) is not enough, the initial value of dR/dt must also be equated to zero. Putting

$$\lambda = 1/R_0^4. \tag{12}$$

and  $\beta = 0$  and  $\alpha = 2R_{\bullet}$  in (8), there results:

$$t = R_0 \sqrt{3} \int \frac{dR}{R - R_0} \sqrt{\frac{R}{R + 2R_0}} \tag{13}$$

Writing.

$$8\pi\delta = 2/R_E^4,\tag{14}$$

there results from (11) and (12)

$$R^{\bullet} = R^{\bullet}_{\sigma} R_{\bullet}. \tag{15}$$

The value of  $R_B$  the radius of the universe, deduced from the mean density on Einstein's formula (14), has been estimated at 8,8  $10^{10}$  Ly.

In order to find the DOPPLER effect for a universe of increasing radius, the equation of a ray of light from the line element (1) takes the form.

$$\sigma_{\rm s} - \sigma_{\rm l} = \int_{L}^{L_{\rm obs}} \frac{dt}{R} \,, \tag{16}$$

where  $\sigma_1$  and  $\sigma_2$  are coordinates characterizing the position in space,  $\sigma_2$  being the position of the observer and  $\sigma_1$  that of the source. A slightly later ray will leave  $\sigma_1$  at the time  $t_1 + \partial t_1$ , and arrive at  $\sigma_2$  at the time  $t_2 + \partial t_3$ . Whence:

$$\partial t_1/R_1 - \partial t_1/R_1 = 0$$
, and  $\partial t_2/\partial t_1 - 1 = R_2/R_1 - 1$ , (17)

where  $R_1$  and  $R_2$  are the values of R at the times  $t_1$  and  $t_2$  t is the proper time, if  $\delta t_1$  is the period of the emitted light,  $\delta t_2$  is the period of the light received. Thence

 $\frac{v}{c} = \frac{\delta t_2}{\delta t_1} - 1 = \frac{R_2}{R_1} - 1,\tag{18}$ 

which is the measure of the apparent Doppler effect due to the variation in the radius of the universe. It is equal to the excess over unity of the ratio of the radii of the universe at the time when the light is emitted and the time when it is received.

When r is placed for the distance of the source the approximate relation

holds

$$\frac{1}{R}\frac{dR}{dt} = \frac{v}{cr} \tag{19}$$

Utilizing the radial velocities of 42 spirals, and taking out a solar motion of 300 km/sec in the direction,  $\alpha = 315^{\circ}$ ,  $\delta = +62^{\circ}$ , Lematire, then derives a mean distance of 3,2  $\pm 10^6$  ly, and a variable radial velocity which amounts to 190 km/sec at  $\pm 10^6$  ly. Using equation (19), this gives

$$\frac{625 \cdot 10^{6}}{10^{8} \cdot 3.08 \cdot 10^{18} \cdot 3 \cdot 10^{10}} = 0.68 \cdot 10^{-27} \text{cm}^{-1}.$$

From this, by transformation and substitution in (13), (15), and (23), LI MAÎTRL derives the value

 $R_0 = 9 \cdot 10^8 1 \text{ y}$ 

By substituting,

$$x^2 = \frac{R}{R + 2R_0},$$

the integral of (13) is transformed to

$$t = R_0 \sqrt{3} \int \frac{4 v^2 dv}{(1 - v^2) (3 v^2 - 1)} = R_0 \sqrt{3} \log \frac{1 + v}{1 - v} + R_0 \log \frac{\sqrt{3} v - 1}{\sqrt{3} v - 1} + C', \quad (20)$$

and designating by  $\sigma$  the fraction of the radius of the universe traversed by the light in the time t, and using (16).

$$\sigma = \frac{dt}{R} = \sqrt{3} \int \frac{2 dv}{3x^2 - 1} = \log \frac{\sqrt{3}v - 1}{\sqrt{3}v + 1} + C', \tag{21}$$

from which Lemaître has derived the following table for  $\sigma$  and t as functions of  $R/R_0$ . The constants of integration in Table 18 were chosen so that  $\sigma$  and t

Table 18 DOPPLER Effect in Lumaitre's Expanding Universe

R/R <sub>o</sub>	t/R <sub>o</sub>	a in degrees	vjo	
1		-∞°	19	
2	-4.31	51	9	
3	-3,42	-30	5.7	
4	-2.86	21	4	
5	-2,45	-15	3	
10	-1,21	- 5	1	
15	-0.50	- ĭ,7	0,33	
20	0	o'	0	
25	+0.39	1	· ·	
00	∞	, ,		

should be zero for  $R/R_0 = 20$ The last column of the table gives the DOPPLER effects calculated from formula (49)

The shifts are seen to be excessive for all values of  $R/R_0$  less than 10, as Lemaitre well expresses it, there need be no speculation as to the formation of mirror or phantom images of the spirals or suns because, entirely aside from any questions of absorption of light in space, such

mages, if received, would be displaced several octaves into the infra-red! These results of Lemaître, obtained in 1927, have been the norm of most work in this field since that date, and his conclusions may be summarized

1 The mass of the universe is constant, and is connected with the cosmological constant,  $\lambda$ , through Einstein's relation.

$$\sqrt{\lambda} = \frac{2\pi^2}{8\pi M} \approx \frac{\pi}{4M} = \frac{1}{R_0}$$

2 The radius of the universe increases without limit from an asymptotic  $R_{\bullet}$  for  $t=-\infty$ .

3 The recession of the extra-galactic objects is a cosmical effect of the

expansion of space, and permits the derivation of a value for  $R_0$ .

4 The radius of the universe is of the same order as that deduced from the density by EINSTEIN'S formula

$$R = R_B \sqrt[3]{\frac{R_0}{R_B}} = \frac{1}{5} R_R.$$

EDDINGTON transforms the foregoing formulae into.

$$\frac{dR}{dt} = \sqrt{\frac{R^4\lambda}{3} - 1 + \frac{4M}{3\pi R}},$$

and points out that there are three cases which may arise 1. If  $M>M_R$ , the system can expand continuously from a very small to a very large radius. 2. If  $M< M_R$ , the right-hand side of the equation vanishes for two positive values of R, and is imaginary between these values. Hence the world will either start with a finite velocity of expansion and expand to one of these values of R, or it will start with a finite velocity of contraction, and contract to the other of these values. 3. The limiting case is when  $M=M_R$  As  $R\to R_R$ ,  $dR/dt\to 0$  like  $(R-R_R)$ , hence the time that the radius remains in the neighborhood of  $R_R$  is logarithmically infinite.

EDDINGTON secures the spectral shift by the relation:

$$0 = \frac{\partial t}{R(t_0)} - \frac{\partial t}{R(t)},$$

where R(t) is the radius of the world at the time t, hence:

$$\frac{\delta t_0}{\delta t} = \frac{R(t_0)}{R(t)}$$

Taking the red-shift of the spirals as determined by Hubble as 153 km./sec. per  $10^4 \, \mathrm{ly}$ , he finds that this expansion amounts to about 1/2000 of the velocity of light. Hence  $\partial t_i/\partial t = 2001/2000$  for an interval  $t_0 - t = 10^4$  years. From this relation, the radius of the universe is considered to have expanded by 1 part in 2000 in the last million years. Eddington places the total mass of such a universe at

DE SITTER'S values of the "initial" and "present" radii of the universe are,

respectively, 0,8 and 1,6 · 10° ly.

That the universe is not only as likely to contract as expand (as admitted also by Eddington), but that it must in fact contract if there exists a single condensation at the origin, was maintained by McCrea and McVrrre. If the start were made with an Einstein universe, and a condensation allowed to form, they maintained in their original paper that a process of contraction would be set up, which would persist indefinitely. They have since discovered an error in the analysis which led them to this theory, and now conclude that the total

<sup>1</sup> Obs 64, p 267 (1931)

volume of space is not altered to the first approximation by the change in the distribution of matter

In his latest paper Einstein has discussed non-static relativity universes, and has expressed a preference for a solution corresponding to a value  $\lambda = 0$  for the "cosmological constant" DE SITTER shows that a family of oscillating universes result, and has investigated these in his most recent paper in the BAN 6, p. 141 (1931)

He makes the assumptions that the total mass of the universe, M, is constant and that the pressure is zero, from which the field equations reduce to the single

form'

$$\frac{1}{R^2} \left( \frac{dR}{c \, dt} \right)^2 + \frac{1}{R} = \frac{1}{3} \lambda + \frac{R_1}{R^3}$$

where  $R_1 = \alpha/3 = \varkappa M/3 \pi^2$  Placing

$$y = \frac{R}{R_1}$$
,  $t = \frac{ct}{R}$ , and  $\gamma = \frac{1}{3}R_1^2\lambda$ ,

the equation becomes

$$\frac{dy^2}{dt} = \frac{1}{y} - 1 + \gamma y^2$$

The solutions of this equation are investigated graphically, with the aid of the relation

$$p = 1 - y + \gamma y^3$$

If  $\gamma$  is greater than 4/27, there is but one solution in which y increases from zero to infinity, i.e., an expanding universe

For  $0 = \gamma \le 4/27$ , there are two solutions, in one of which  $\gamma$  increases from  $\gamma_2$  to infinity, and oscillates between the limits 0 and  $\gamma_1$ ,  $\gamma_1$  and  $\gamma_2$  being the two points on the curve  $\rho = 0$  where  $\gamma$  has the prescribed value, and  $\gamma_1 < 1.5 < \gamma_2$ . There are then two families of solutions, a type of expanding universes, for positive values of  $\gamma$ , and the oscillating universes, for values of  $\gamma$  smaller than 4/27.

Very significant are DE SITTER'S comments on the not very successful attempts to correlate the "expansion times" of such universes and present beliefs as to the time scale of stellar evolutionary processes.

", the time scale of the evolutionary processes can only be formally fitted into the scheme of the expanding universe by means of such a tremendous extrapolation as to deprive the theory of all real meaning. This is only another way of expressing the utter impossibility, which has already been repeatedly pointed out, of reconciling the short time scale of the expanding universe with our ideas regarding the evolution of stars and stellar systems. In the theory of relativity a year and a light-year are equivalent, whilst in astronomy 10° light-years is a very large distance, but 10° years is a short time."

DE SITTER also derives expressions which indicate that while there is a quasi-expansion effect within a galaxy, this is so very much slower than the expansion of the universe as a whole as to be practically entirely negligible

72. The Size of the Universe According to Silberstein Radically different conclusions as to the dimensions of the curvature of space-time have been derived by Silberstein in his book, "The Size of the Universe" (1930) In this work he has collected and revised his earlier articles in scientific periodicals, and it thus forms the most accessible summary of his views. The book contains one of the clearest and best introductions to the methods of tensor manipulation and analysis as yet available in English (see also the same author's article, Tensor, in the Encyc. Brit.). Among the faults of the book are its marked polemic tendency, the apparent total rejection of modern results as to the distances of

the spirals, and the fact that most of the largest of the spiral valocities could not be included at the time the book went to press. It contains, however, valuable criticisms as to the validity of the Einstein and de Sitter universes, the author was the first to point out that negative valocities should be as apt to occur as positive ones; furthermore, Silderstein's method of attack differs from that of all other investigators in that he has applied his formulae to galactic objects

SILBERSTEIN'S development and method of attack is set forth in part V of the work referred to, to which reference should be made. His method consists essentially in the application of statistical methods for large groups of data, involving relations connecting the distance of perihelion, the speed which the object has in passing through perihelion, and the distance of the objects from the observer

For 20 clusters, he derives a value of the curvature radius,  $R = 10^8 \,\mathrm{ly}$ . For 38 spirals employed, he points out that R would be from 1 to 2,3 · 10° ly, but is unwilling to accept From 29 Cepheids he secures R = 4,7 10° ly. Using 459 stars from Young and Harper's list, he finds  $R = 6,4 \cdot 10^9 \,\mathrm{ly}$ . He finally adopts (p. 212, as of date of 1929)  $6,27 \cdot 10^9 \,\mathrm{ly}$ . This is roughly one-twentieth of the distances assigned by other investigators to the Coma-Virgo and Centaurus groups of external galaxies. The present writer feels that Silberstein's values for the "dimensions" of space are inordinately small, and that they will not stand the test of comparison with modern cosmical data, even if the inevitableness of some form of closed relativity universe be granted.

78, Various Determinations of the "Radius" of Space-Time.

Author	P, Ly.	Mass, g	Date
DE SITTER SILBERSTEIN, HUBBLE LEMAÎTRE EDDINGTON TOLMAN, INDICE THAN DE SITTER DE SITTER SILBERSTEIN, SILBERSTEIN	1,4 · 10 <sup>1</sup> 10 <sup>3</sup> 1,5 · 10 <sup>11</sup> 9 · 10 <sup>3</sup> 1,2 · 10 <sup>3</sup> 2 10 <sup>3</sup> 0,8 · 10 <sup>3</sup> 1,6 10 <sup>3</sup> 5,1 · 10 <sup>4</sup> 4,8 · 10 <sup>3</sup> 6,4 · 10 <sup>4</sup>	1,4 · 10 <sup>M</sup> 9 · 10 <sup>M</sup> 2,3 · 10 <sup>M</sup> 10 <sup>M</sup>	1917 1924 1926 1927, initial value 1930 1929 1930, initial value 1930, present value 1929, O-stars 1929, Cophields 1929, 459 stars

Table 19 Values of Radius of Curvature of Space-Time

The values range from 4.8 · 10° l.y. (SILBERSTEIN) to 1.5 · 10<sup>11</sup> l.y (Hubble), though most investigators have postulated values of the order of 10° l.y. Were the present writer to accept some form of closed universe as inevitable, he would regard a radius of the order of 10<sup>12</sup> l.y. as the minimum admissible

74. Summary: the Dilemma of Choice between an Expanding Relativity Universe and the Distance-Velocity Correlation. The recent history of theories of relativity universes has passed through a stage of great confidence, perhaps over-confidence, in which considerable finality was thought to have been attained. As far as certainty is in consideration, its present condition does not appear quite so satisfactory. Omitting for the present other possible theories of Newtonian character, to be discussed later, there seems a partial dilemma, as individual hypotheses, between the two theories on which most recent work has been done. It would seem necessary to combine into one system the distance-

<sup>1</sup> Publ Astrophys Obs Victoria 3, No 1 (1924)

velocity correlation and the expanding universe, and no treatment has yet appeared showing in just what way the two are combined

It has been customary in some quarters to consider the velocities secured under the distance-velocity relation as apparent velocities (aside from individual motus peculiares, of course). This can not be so if the theory is to be allied with that of an expanding universe, for in such a structure the velocities must be real. If they are real, and if the present value of 170 km/sec per 10°1 y holds indefinitely, the outer parts at a distance of 2 10°1 y must be expanding with the velocity of light. Velocities nearly that of light in the region just this side of a finitely near horizon, do not appeal to the reason, this is, however, no argument against it, for in a domain beyond the scope of experience (a four-dimensional manifold in a continuum of six-fold curvature) it would be expected, perhaps, that the relations or seeming paradoxes which are the results of the basal hypotheses may also be beyond the domain of experience

The simplest explanation of a distance-velocity relation (Burns) is the manifest one that the objects with highest speeds would have reached greater distances from us. This presupposes, however, a universe without re-entires, and, like the theory of an expanding universe, meets with insuperable difficulties when the attempt is made to visualize the "initial" state. As a further alternative, it is perhaps reasonable to assume that the vibrations of the light-ray (not its speed) may be slowed up by minute amounts in passing through tremendous distances, were this so, the velocities of recession exhibited would be only apparent, and the most distant objects would be invisible, not from a horizon limitation, but from redness.

On the alhed question of an expansion in a comparatively minute realm, one naturally recalls the K-term in stellar radial velocities. Such K-terms have been found by Campbell, and others, particularly in the early type stars. They have given rise to a great deal of discussion, pro and con, of which one of the most recent and thorough investigations is that due to Rosenhagen. If existing, such effects may be regarded as giving support to a theory of expansion, as an expansion of spiral distances should be accompanied by corresponding expansion im kleinen. Vogt considers that the spiral arms are due to this same expansion effect. Assuming a star in our galaxy at a distance of 10<sup>1</sup> ly to be subject to this expansion effect of 1 part in 2000 per 10<sup>6</sup> years, it should have a radial velocity, in this extreme case, of but 1,5 km/sec

75. Other Cosmogonical Deductions: an Aberration Effect Suggestions have been made that the high velocities of the spirals might produce an effect on the observed aberration Perrine<sup>2</sup> suggested that the aberration constant derived from a spiral of velocity 10<sup>1</sup> km /sec. should be 20",18 instead of the usual 20",47 Borčev<sup>3</sup> shows that Perrine's deduction is erroneous. "It should be remembered, however, that aberration can only be explained on the assumption that the observer moves relative to the other. The absence of the other drift necessitates, in turn, the constant velocity of light, whatever be the velocity of the source." VAN BIESBROECK has made careful position measures of the spiral in Ursa Major which has a radial velocity of +11700 km /sec (paper read at the September, 1931, meeting of the Amer Astr Soc), and has found no evidence whatever of a different value of the aberration constant for this object Courvoisier<sup>4</sup> has lately carried through some investigations of great interest,

A N 242, p 401 (1931)
 A N 240, p 319 (1930)
 A N 241, p 343 (1931)
 L Courvoisier, Zur Frage der Mitführung des Lichtätheis durch die Erde A N 213, p 281 (1921); Bestimmung der absoluten Translation der Erde aus säkulaier Aberration, ibid, 241, p 201 (1930), G v Gleich, Bemerkungen zur absoluten Translation unseies lokalen Fixsternsystems A N 242, p 265 (1931)

which form an excellent illustration of the manifold scientific fields which contact with the high velocities of recession shown by the spirals. He holds that the observed aberration constant should be written.

$$h = k_0 \left( 1 - \frac{v}{a} \cos \psi \right)$$

where k is the observed value,  $k_0$  its "absolute" value, v the velocity of the source, c the velocity of light, and  $\psi$  the angle between the observed object and the apex of motion. One observes then not the absolute velocity of light but a velocity which is relative because of the absolute translation of the earth. This infers that the constant of annual aberration is variable with the position of the object, it is smaller in the apex-hemisphere, and larger in the celestial homisphere which is antipodal to the apex. The possibility of such an effect was noted first by Villarceau in 1872.

Courvoister investigates this effect in two ways

From observations of zodiacal stars

2 From declination observations

He gives as his final result from all observational data considered:

 $k_0 = 20^{\circ},498 \pm ^{\circ},009$   $A = 112^{\circ} \pm 20^{\circ}$   $D = +47^{\circ} \pm 20^{\circ}$  $V = 600 \pm 305$  km./sec.

These results, agreeing roughly as they do with the approximate location of the apex of galactic motion found by other methods, are of high interest. He points out that further work is urgently needed on objects of widely different celestial types.

76. Further Considerations on the Apparent Recession of the Spirals. The main difficulty which impedes a solution of the puzzle presented by the large positive values of the radial velocity of the spirals is due to the exceedingly fragmentary character of our present observational data on the score of distribution. Of the 90 velocities given in Table 14, only 30 (including the two Clouds) are below the galactic plane. Only 7 indicate a velocity of approach. The algebraic

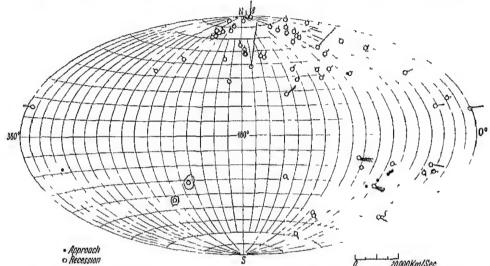
mean of all is +2470 km /sec.

It will be noted, both from Table 21 giving the galactic coordinates and from Figures 57 and 58 (Appendix No. 8), that the arrangement of spirals for which radial velocities have been determined is of such a nature that a definite solution, on any theory, is scarcely to be hoped for The region about the north galactic pole is quite well represented. Only one velocity (584; +1800 km./sec.) is known within 30° of the south galactic pole. Furthermore, in the stretch of about 240° of galactic longitude from  $l = 150^{\circ}$  to  $l = 30^{\circ}$ , there are but 4 determined velocities south of the galactic plane Because of these very serious gaps in distribution, any solution for the velocity of our system becomes highly indeterminate. Again, such a solution, with a very large K-term which seems to indicate an expansion, gives us very little information other than we already have, and leaves the puzzle of such an expansion unsolved.

It is therefore clear that the final solution of the problem may have to await the day when a considerable number of spiral velocities have been determined in the regions contiguous to the south galactic pole, and particularly in the quarter of a sphere, 180°—360°, which is now almost entirely blank. Astronomy has no more pressing observational task, nor one which would be of more service in clearing up modern cosmogonical theories. A decision between the theories treated earlier and in the following sections, must evidently await the estab-

lishment of a powerful reflector in the Southern Hemisphere!

A second uncertainty, which may eventually be turned into an advantage, tests upon the amount of random velocity, or average peculiar motion, which can be permitted a spiral or a group of galaxies. As to the variations within a group of galaxies, from the evidence of those determined at Mt. Wilson and given in Table 14, ciph 50, it would seem evident that this is 2000 km/sec, or more. If the cosmos be arranged on Charlier's scheme, in supergalactic groups, we may expect, also, an even higher variation in the velocities of such groups



Tig 57 Galactic Distribution of Spirals of Determined Radial Velocity Positive velocities are indicated by lines extending away from the center of the diagram, and negative velocities by lines toward the center. The scale of the lines is indicated on the figure

77. Earlier Values of the Motion of our Galaxy in Space. A few of these values are collected in this Section, not because they are believed in any way to be a solution of the problem of the velocities of recession, but rather to indicate the past trend of research in this line. The distance-velocity values have been added. In this tabulation, A is the right ascension of the apex, D its declination,  $V_{\rm gal}$  the galactic motion, and K the "expansion" term common to all objects treated

Table 20 Values of the Apex and Motion of the Galaxy

Author	A	D	Fgal km /sec	K km /sec	Reference	
TRUMAN ,	300°	-20°	670		Pop Asti 24, p 111 (1916)	
PADDOCK , , ,	270	+30	200土	300-	Publ A S P 28, p 109 (1916)	
Young and Harper	300	-12	600	D O	RAS Can 10, p 134 (1916)	
Dose	299	+68	765		AN 229, p 157 (1927)	
LUNDMARK	305	+75	65 i		Obs 47, p 279 (1924)	
STROMBERG	310	+60	460	660	Ap J 61, p 353 (1925), mean of	
					7 groupings of data,	
WIRTZ .	195	+89	693	887	AN 215, p 349 (1922)	
HUBBLE	286	+40	360	142/10 <sup>8</sup> 1 v	Wash Nat Ac Ploc 15, p 168	
	•			/ 3	(1929); 24 spii,	
Hubble , ,	269	+33	306	157/10 <sup>6</sup> 1 v	ibid, 9 groups	
HUBBLE .	_	-	_	170/100 l v	Ap J 74, p 43 (1931)	
OORT , ,	170	-64	360	132/1001 v	BAN 5, p 239 (1930)	
OORT ,	_		_	90/1061 v	BAN 6, P 155 (1931)	
DE SITTER ,	-		- 1	146/1001 v	BAN 5, P 157 (1930)	

See further Appendix No S

78. Moissard's Modification of the Doppies Formula. There have been several attempts to seek for other causes which might explain the recession of the spirals. Russill shows that neither radiation pressure, nor gravitational or electrical forces can reasonably account for the high velocities of the spirals, to say nothing of their predominant positive sign

W. MICHELSON® pointed out that some of the assumptions in the derivation of DOIPLER's principle are necessarily arbitrary; 1 that the period of vibration of the source is not affected by its motion along the line of sight, 2 that the

medium is at rest, and, 3 that its velocity is not changing

It is not impossible that a high "absolute" motion of our galaxy or our super-system of galaxies might contribute largely to the effect, as noted by DRUDE

" In this case (both hodies moving) the rigorous calculation shows that the actual period T and the relative period observed at B stand to each other in the relation:

$$\frac{T}{T'} = \frac{c - u}{o \pm v},$$

(characters changed from original to conform with later nomenclature. H.D.C.) in which is in the absolute velocity of B, s that of A in the direction of the ray, and c that of the light in the medium between A and B... Now we know nothing at all as to the absolute velocities of the heavenly bodies, hence in the ultimate analysis the application of the usual equation representing Doffica's principle to the determination of the relative motion in the line of sight of the heavenly bodies with respect to the earth might lead to errors. Attention was first called to this point by Mosseard."

The Moissard-Drude suggestion that the ordinary formula for the Doppler shift is not rigorously accurate has not hitherto been considered, so far as the author knows. The great interest which attaches to the puzzle exhibited by the great positive velocities of the spirals is sufficient warrant for the somewhat tentative illustration of this hypothesis given in Appendix No 8.

79. Conclusion. We must wait for many more velocities of spirals, with adequate representation near the south galactic pole and south of the galactic plane in the region from 180° to 360° galactic longitude, before any acceptable decision can be made between the various theories which have been advanced to explain the excess of velocities of recession exhibited by the spirals.

There are no theories of this very curious phenomenon which do not require the introduction of rather radical ad hoc hypotheses. In the velocity-distance correlation we need either to assume, with a considerable measure of observational support, that the vibration period of light is diminished by its passage through space, or that the universe is actually expanding, the outer parts more rapidly than the inner. If the cause is assumed a consequence of some form of expanding relativity universe, we find at once another basal assumption in the cosmological constant  $\lambda$ , which is inserted in the Einstein form of the gravitational equation:

"Finitude of space depends upon a "cosmical constant"  $\lambda$ . Except in so far as a value may be suggested by astronomical survey of the extra-galactic universe  $\lambda$  is unknown (Eddington)." "The constant  $\lambda$ , which is a measure of the inherent expanding force of the universe, is still very mysterious, and it is difficult to see what its real meaning is. It might even be one constant too many, unless we may hope that it will ultimately be found to be in some way connected with Planck's constant h. Evidently the dynamical solution of Lemaître is not

<sup>1</sup> Ap J 53, p 4 (1920). 
8 Ap J 13, p. 192 (1900)
8 Optics, English translation (1902), p 473, footnote 
4 CR 114, p, 1471 (1892)

the last word, but it can hardly be doubted that it represents an important step towards the true interpretation of nature (DE SISTER). As noted earlier, the most recent solutions of Einstein and DE Sister place  $\lambda=0$ . There is no theory yet advanced, in other words, which is free from somewhat diastic ad hoc hypotheses, all require a measure of extrapolation or speculation fat beyond the available range of observational data.

Whether one prefers to assume that light vibrations are slowed up by then passage through space (velocity-distance correlation, spiral velocities apparent), or to postulate a universe that is actually expanding (Lemaître's and other relativity universes, spiral velocities real), or to accept a universe of the CHARLIER type with the Molssard modification (spiral velocities in part real, in part apparent), is doubtless entirely a matter of individual choice and belief. The remarkably close parallelism between the structure of the suggested Charlier universe and the observed arrangement of the accessible exteno universe, is too exact and detailed to be cast lightly aside. Under assumptions which seem not more ad hoc than those which have been made for other theories tested, it would appear within the bounds of possibility to remove the excess of positive velocities which have formed the main obstacle to the acceptance of a universe of the Charlier type (see treatment in Appendix No. 8) For this and other reasons, therefore, the writer prefers, solely as a matter of personal choice and belief, to adhere, until more evidence may be gathered, to a cosmogony based on the scheme of CHARLIER, rather than to accept one or another of those which seem as yet somewhat nebulously based upon a fourdimensional frame of reference

It can not be too strongly emphasized, however, that many aspects of our present available observational evidence are so madequate and so incomplete that no final decision is possible, and that the field of speculation is still open as regards any of the theories which have been advanced in explanation of the excess of velocities of recession in the spiral class

# e) Appendices. Appendix No 1.

Finding List for Names frequently used in the older literature

Namo	NGC	Messier	Description
America nebula	7000		Enormous diffuse neb
Andromeda nebula	224	31	Largest spual
Crab nebula	1952	1	Planetary
Dumb-bell nebula	6853	27	Planetary
Hercules cluster	6295	13	Large globular cluster
Horse shoe nebula	6618	17	Bright diffuse nebula, of Omega
I agoon nebula	6523	8	Large diffuse nebula
Network nebula	6995	<u> </u>	Very large diffuse nebula
Omega nebula	6618	17	Bught diffuse nebula, of House- shoe neb
Orion nebula, Great nebula in			
Orion	1976	42	Very bright diffuse neb
Owl nebula	3587	97	Planetary
Praesepe	2632	44	Bright open cluster
Ring nebula (in Lyia)	6720	57	Planetary
Swan nobula .	6618	17	Diffuse of Omega nebula
Trifid nebula .	6514	20	Bright diffuse nebula
Whirlpool nebula	5194	51	Fine spiral

<sup>1</sup> Cf JEFFREYS' interesting and suggestive book, Scientific Inference, Cambridge (1931).

Finding List for MERSIER Numbers. (Abridged from SHAPLEY and DAVIS, Publ ASP 29, p. 178 (1917)

MEMIER	NGC No.	Description	Memma	NGC No.	Description
1	1952	Crab Nebula	51	5194	Spiral
2	7089	Globular cluster	52	7654	Cluster
3	5272	Giobular cluster	53	5024	Globular cluster
4	6121	Globular cluster	54	6715	Globular cluster
3	5904	Globular chater	55	6809	Globular cluster
Ğ	6405	Open cluster	56	6779	Globular cluster
7	6475	Open cluster	57	6720	Planetary (Ring nob biLyra
Ř	6523	Diffuso nebula	58	4579	Spiral
9	6333	Globular cluster	59	4621	Spiral
10	6254	Globular cluster	60	4649	Spiral (alliptical)
11	6705	Open cluster	61	4303	Spiral
12	6218	Globular cluster	62	6266	Globular cluster
13	6205	Heroules cluster	63	5055	Spirei
14	6402	Globular cluster	64	4826	Spiral
15	707B	Globular cluster	65	3623	Spiral
16	6611	Open cluster	66	3627	Spirel
17	6618	Diffuse nobula (Horse-shoe	67	2682	Open chaster
		or Omega neb)	68	4590	Globular cluster
18	6613	Open cluster	69	6637	Globular cluster
19	6273	Globular cluster	70	6681	Globular cluster
20	6514	Diffuso nobula (Trifid neb.)	71	6838	Open cluster
21	6531	Open cluster	72	6981	Globular cluster
22	6656	Globular clustor	73	6994	Open cluster
23	6494	Open cluster	74	628	Spiral
24	6603	Open cluster	75	6864	Globular cluster
25	I 4725	Open cluster	76	650	Planetary
26	6694	Open cluster	77	1068	Spiral
27	6853	Planetary (Dumb-bell nob.)	78	2068	Diffuse pehula
28	6626	Globular cluster	79	1904	Globular cluster
29	6913	Open aluster	80	6093	Globular cluster
30	7099	Globular cluster	81	3031	Spiral
31	224	Spiral (Andromeda neb.)	82	3034	Spiral
32	221		83	5236	Spiral
		Spiral (elliptical)	84	4374	Spiral (elliptical)
33	598		85	4382	Spiral
34	1039	Open cluster	86	4406	Spiral (elliptical)
35	2168	Open cluster		4486	
36	1960	Open cluster	87 88	4501	Spiral (olliptical)
37	2099	Open cluster			
38	1912	Open cluster	89	4552	Spiral
39 40	7092	Open cluster Two faint stars	90	4569	Spiral
-		1-11-11-11-11-11-11-11-11-11-11-11-11-1	91	-	Comet??
41	2287	Open cluster	92	6341	Globular chuster
42	1976	Diffuse nebula (Great Ne-		2447	Open cluster
		bula In Orion)	94	4736	Spiral
43	1982	Diffuse nebula	95	3351	Spiral
44	2632	Open cluster (Praesepe)	96	3368	Spiral
45	_	Plolade	97	3587	Planetary (Owl nebula)
46	2437	Open cluster	98	4192	Spiral
47	2478	Cluster	99	4254	Spiral
48	-	Very open cluster	100	4321	Spiral
49	4472	Compact spiral	101	54 27	Spiral
50	2323	Open cluster	102	5457 5866	Spiral, identification
-				,	doubtful
	ſ		103	581	Open cluster

Appendix No 2
Finding Lists for Sir W Herschel's Classes and Numbers,
Herscher's Class I, 1-288

I i to I 50	I 51 to I 100	I 101 to I 150	I 151 to I 200	I 201 to I 250	I 251 to I 288
1055	6638	779	524	3877	3945
2775	7006	1022	821	3949	4041
3166	7331	6934	908	3938	4036
3169	393	7606	949	2639	4605
3655	7479	720	1453	2841	5308
5363	2903	1309	1023	4088	5322
4472	2905	1407	672	4096	1344
4698	1395	467	1600	4157	1491
4179	2784	1201	278	4220	3923
4643	1332	7723	4546	4346	2880
		1			
4153	2974	7727	4159	4800	1931
1377	701	772	4866	4460	3682
3521	1052	2830	3115	4449	4128
4632	1084	2964	3294	5474	4250
4666	4361	3021	4151	5866	3182
4753	2781	3395	4369	2787	3206
3379	3962	3396	2782	1579	3445
3384	4856	3430	3184	2419	3458
4147	4902	4560	4145	3665	3488
3666	5634	3887	5290	3549	3610
3810	5812	4030	5739	3718	3613
4371	3254	1637	3432	3729	3332
4452	4150	4378	3941	4026	4589
4596	4245	4580	4062	4085	4648
4754	4274	4586	4203	4102	4291
3345	4314	5746	4656	3631	4319
3412	4414	5813	4657	3780	4386
4438	2985	5846	4618	3898	4144
3593	3147	4699	4618	3998	4127
4365	3348	4958	5297	5422	6217
4526	3344	3672	5383	5473	613
4570	3900	2855	5713	5485	2977
4124	4494	2742		3448	3183
5248		4781	5750		
	4725		5728	4500	3329
4216	5012	4782	5633	5585	2976
4550	3245	4783	5195	5631	3077
4551	3486	2859	5377	5678	3735
4526	3504	5061	5689	5376	2655
4697	4251	4303	5676	5379	
4941	4278	4713	5395	5389	Į.
4731	4448	4808	5394	3621	
4995	4559	4665	7008	2681	ļ
4594	4793	4900	651	4814	
6401	3813	5566	3675	3619	Į
6316	4214	5574	4111	3642	
6355	5005	5576	4138	3683	
6712	5033	6304	4485	3690	
6356	5273	5921	4490	3894	1
6522	5557	6342	3198	2742	1
6624	584	6440	2683	2768	1

HERSCHEL'S Class II, 1-150.

II 1 to II 50	II 51 to II 100	II 101 to II 150	II 151 to II 200	II 201 to 11 230	11 251 to 11 300	II 301 to 11 350
7184	3608	3489	6106	6569	7448	4984
7507	3626	3596	3692	6847	514	2481
157	3659	3800	3822	7013	660	2554
596	3691	3872	3825	6629	1134	2316
1032	4394	4168	4417	6642	7742	3110
1055	4450	4189	4442	6979	7743	5306
1580	2872	4208	4469	7217	95	5324
1587	2874	4212	4519	7741	1232	5343
1588	3070	4222	3681	214	2577	5426
7800	4124	4262	3686	315	2916	5427
4237	4294	4298	3801	972	7137	2986
4651	4299	4302	3968	7457	1371	5068
3705	4313	4419	4193	7753	1385	5084
4119	4352	4473	4200	296	2139	5134
4578	4429	4477	4206	379	2196	2592
3462	4503	4479	4267	380	2613	2371
4235	4528	4474	4387	383	1415	2372
4470	4564	4501	4388	392	3078	2608
4610	4608	4540	4413	407	3585	2619
4612	4638	4548	4425	410	718	3106
4795	4660	4458	4431	736?	741	4136
5106	4694	4461	4436	750	742	4278
4420	4733	4476	4440	777	1070	4283
4772	4754	4478	4461	404	1153	4317
5147	4762	4639	4531	890	2967	4525
4453	5970	4654	4638	7678	4045	4676
5665	3338	4659	5600	7817	4073	5089
3226	3367	4689	5953	678	955	5127
3227	5669	5020	5954	680	1507	5623
3626	2672	5936	4454	7769	2695	5653
4592	3370	3423	4684	7771	2708	5607
3645	3455	3976	4691	7798	615	5832
3640	4152	4180	4593	7332	636	3063
4412	4328	4197	4602	7339	1035	3063
4457	4340	4215	4989	7556	1208	3403
4496	4350	4224	4775	7585	1241	3516
4527	4379	4223	4786	958	1299	3562
4636	4405	4260	4951	1003	1376	3629
4664	4421	4261	4981	1161	1888	3689
2911	4450	4264	4928	7814	1357	3798
3389	4489	4326	4933	57	1421	3826
3547	4502	4333	5861	7681	1832	3912
3162	4515	4339	5077	57	3091	4555
3190	4540	4370	5548	7711	3957	4747
3193	4710	4423	6287	234	4024	4789
3301	5962	4430	5694	877	4027	4819
3437	5996	4532	6544	7177	5247	3248
2672	3041	4612	6540	7280	4727	3327
3599	3377	4623	6517	7454	4877	3701
3607	3485	5645	6528	7625	4899	3710

Herschee's Class II, 351-700

1 to 11 400	I 101 to II 450	II 451 to 11500	II 501 to II 550	II 551 to II 600	II 601 to II 650	II 651 to II 700
3728	5937	7444	682	3637	11123	5930
3772	0118	210	1172	3732	1129	6160
4162	3947	7393	1199	3892	1278	5129
4213	4032	7576	1209	2507	+ 818	5951
4455	4158	1417	2811	2889	828	5980
5010	4336	1418	2907	2935	7231	5984
5637	4561	1005	3508	2718	1175	6012
3274	3897	1440	4033	4658	1193	2691
3277	4190	1452	4050	4759	252	4627
3380	4534	1161	5037	4790	661	4625
3400	4619	521	5044	4939	670	4655
3414	4711	533	5049	3715	489	4704
3418	4956	550	5054	4825	, 855	4963
3451	5014	1550	1620	2778	2274	5023
3510	5352	1090	1635	3381	2275	5103
3512	5440	1087	1713	5078	2435	5123
3713	5444	7562	4904	[5 101	691	5145
4008	5533	7785	4227	A270	695	5289
4017	5544	7284	4229	1273	1156	5320
1104	5614	1140	2765	4277	1169	5336
1134	5656	137	3611	4281	1259	5362
173	5675	255	1636	A 300	428	5410
1185	5695	599	1646	4281	3955	5608
<b>1</b> 196 [	5347	873	1618	5668	2990	5630
1209	5990	1200	1638	5701	4348	5697
1275	6962	7310	1653	5770	3604	5784
1283	6964	7371	1682	4600	2545	5787
1310	7311	151	1684	4701	4312	5893
375	7541	191	2721	5560	4474	5183
556	7537	217	4376	5638	4468	5184
1692	7600	681	4480	5636	4506	5691
4798	7721	833	4630	5690	4595	5719
4816	337	835	5300	6010	1058	5792
4827	357	838	5364	6235	2563	5865
4840	788	839	4771	5864	3660	5327
4839	881	853	4845	6445	4597	5345
4841	883	945	4909	6426	5015	5506
4869	895	1045	5740	665	5253	5301
4872	7619	932	5806	673	3158	5198
4892	7626	2770	5831	7458	3163	6155
4889	7634	2968	5839	14	3334	5448
4911	7364	3067	\$838	1024	4156	5480
4921	7391	3413	5850	1400	4662	5481
4923	227	3424	5854	1442	4868	5602
4944	245	2906	5869	7183	4914	5660
4952	271	4233	2872	706	5112	5673
4957	1 430	4434	2874	1441	6158	5351
4961	545	4470	4129	7377	5696	5380
5958	547	4492	4818	7197	5704	1 5406
5910	7443	14535	3636	7640	5899	5698

HERSCHEL'S Class II. 701-909

Herachel's Class II, 704-909								
II 701 to II 750	11 751 to 11 500	11 801 to 11 850	Il 851 to II 900	II 901 to II 910				
6207	5857	5486	7773	6389				
7392	5859	4149	1425	6555				
259	6181	4161	29	30617				
1184	5582	4271	128	3523				
7354	5875	4290	132	3752				
7538	5820	4335	194	5949				
185	5879	5667	198	6646				
2798	5905	5687	200	2650				
3600	5907	5751	693	3063				
5311	5908	6125	196	46467				
5313	5963	6143	2320	)				
5326	5965	6338	2332					
5350	5894	4187	257					
5353	5982	4732	3904					
5354	5987	4987	4105	]				
5371	5985	5040	4106					
2998	6340	5250	4194					
3415	1569	5881	2814					
2543	2339	3571	2820					
3202	3687	2387	3259					
3205	4304	2415	3266					
3207	4626	2426	3394					
3891	4628	2693	6048					
3971	4671	3917	5928	)				
4020	3652	3924	6166	ļ				
2532	4487	5109	5492	1				
2649	4813	5430	5513					
3583	4888	2756	6824	,				
3614	4925	3669	3622					
3726	5085	3804	3654					
3769	4068	3838	3879					
3782	3656	3895	3225	}				
4013	3738	3958	3238					
2326	3756	2726	3517					
2329	3888	3043	3625					
2340	3913	3725	3674					
3811	3916	3762	3435	)				
3893	3921	3770	3470					
3896	1 3972	3796	5374					
3928	3977	3978	5491	}				
4047	3990	5216	5652					
4248	4172	5218	3001	}				
4381	4198	5370	5674					
701/	4644	5376	5679					
3320	4686	3668	5257					
5018	4695	4256	5258	)				
4144	5201	4332	7218	)				
4217	5278	4441	3107	1				
4389	5443	4524	5323	1				
, 4460	5475	4545	1247	l .				

Herscher's Class III, 1-350

III 4 to III 50	111 51 to 111 100	III 101 to III 150	III 151 to III 200	III 201 to III 250	III 251 to III 300	III 301 to III 350
1982	3020	5239	807	871	474	4495
867	3024	3833	1012	7168	488	4514
4028	3153	3876	266	7497	520	4962
2939	3299	3874	421	251	3044	4966
3342	3300	4598	420	459	3156	5004
4698	5416	4779	495	473	2555	5056
2508	5146	3356	496	794	2618	5057
2894	5463	3425	499	803	4077	5065
5208	5482	3790	507	7042	850	5074
5209	2744	5587	508	7463	863	5672
5417	2774	3535	987	7165	941	5808
5570	2802	3679	1060	7659	1239	5836
4577	2803	3915	1066	7691	1409	6011
5621	2843	4422	1240	774	2722	6091
3646	3129	5146	7186	781	755	2963
3649	3303	5885	7335	7385	731	3252
4409	3473	5076	515	7386	2076	3343
4505	4126	5079	517	7648	1781	3364
2402	4498	5111	513	6956	1993	5620
3433	4758	5605	537	7515	2089	3812
3491	5180	5597	536	7559	2283	3902
3506	5249	5595	552	7563	3052	3944
3524	б021	6267	553	171	3072	4015
3088	6073	6278	614	907	3981	4021
3177	3498	5396	679	2124	2763	4007
4529	3616	5642	735	7671	2902	4101
3605	4037	5706	925	827	2992	4146
3686	4516	5709	1167	1044	2993	4670
3768	3559	5771	697	1046	4035	4673
3802	3731	5773	7316	7469	4724	3216
4344	3773	5798	1 7550?	7778	4756	3270
5490	4752	5635	7578	7779	5073	3475
6046	4880	5735	52	7782	5677	3615
2984	5136	5523	7506	2599	3818	3618
3848	5222	5594	7566	2628	5369	3651
3852	5221	5610	7592	2764	5468	3653
4067	5230	6372	7694	7321	5476	3670
4368	3401	5898	7701	7570	2566	3808
4390 4482	3567 3914	5903 6064	7725 7832	922 1979	2983 3956	3815 3832
4491	4246	6907	352			
4497	4240	6926		2073	2750	3911
4606	4297	6717	702	2815	2604	3951
4647			748	7436	3068	3983
5174	4343 4341	6857	1266 1287	216	2679	4002
5175	4341	7052	1321	1187	2783	4003
5532	4342	7720 23	1320	1353	2796	4979
5747	4588	108	1003	1401	2893 2918	5559
2648	5210	233	1160	1439		3196
2661	5235	604	213	470	4272 4286	3265

HERSCHEL'S Class III, 351-700.

III 351	III 401	III 451	111 501 to	1II 551	III 601	III 651
III 400	Ш 450	111 500	1П 550	TII 600	111 650	III 700
3550	4986	1393	1670	5546	3060	5157
3552	5141	7156	1678	5549	4571	5187
3714	5142	1762	1729	6070	4634	5433
4004	5149	622	4591	5775	845	4985
4080	5154	1073	5252	6548	2512	5003
4131	5199	36	5356	532	2558	5214
4132	5223	864	5203	990	2562	5730
4169	5228	7252	5729	7492	2743	5731
4174	5240	686	4599	1370	3791	5888
4175	5265	723	2110	551	4705	5900
4393	5399	24	5845	687	4720	5922
4475	5401	1094	2513	703	3952	4653
I 4051	5445	268	2914	704	4843	4668
4927	5529	762	4703	705	4890	4690
4983	5579	7432	4739	706	3304	5334
5000	5589	7794	4773	797	3930	5392
5032	5590	154	4777	834	4025	5400
				1308	4774	5604
5116	5533	773	3145		5107	5017
5251 5263	5616 5654	1162 7526	2948 2863	1397 898	5243	5047
-					5305	
1000	5684	624	2979	910	6038	5716
3883	5312	977	3411	980		5173
5768	5318	7647	4682	982	6120	5256
5913	4719	924	4700	1293	6137	5500
3805	5233	1036	4770	1294	2704?	5714
3821	7685	160	4784	7426	2755	5520
3837	7750	280	2969	477	2838	5622
3842	61	3099	2980	1207	2844	5797
3926	274	2459	3591	7707	2852	5804
3940	273	II 3115	3661	1138	2853	1 6154
3954	586	4356	3667	1030	3237	1 5303
4095	600	4415	3693	1088	3468	5361
4098	790	4464	4114	780	5093	5403
4099	991	4488	4177	1056	5966	5407
3862	7623	244	4265	1609	5992	1 5515
3860	7816	867	4714	1611	5993	5732
3875	7751	1354	4748	1576	6058	5754
3884	7665	2848	4794	1643	0146	6104
3937	279	4763	5094	1659	6150	6255
4049	450	1552	2719	1954	6173	5757
4070	560	4044	2955	1242	6175	1 5791
4069	564	4418	3074	426	5185,	7171
4074	1248	4541	4688	429	5207	7180
4061	1304	4642	4765	493	5522	1343
4065	1324	4583	5019	193	5649	896
4076	1358	4737	5382	3081	6018	7139
4204	1924	3434	5386	2921	2759	4183
4685	2110	3495	4799	3509	4359	1 - 5337
4163	1114	1516	5329	2595	5025	5355
4097	1125	1779	5718	3053	5096	3319

HERSCHLL'S Class III, 701 - 981

III 701	III 751	III 801	III 851	111 901	111 951
to III 750	to III 800	to 111 850	to 111 900	to 111 950	to 111 981
,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,				22 750	
3374	2965	4364	4238	2388	6331
4253	2530	4547	4391	2578	1633
2389	2582	5255	3073	4034	1634
3192	4087	5526	7760	1120	163
3478	4403	5540	7805	3961	270
3595	4404	5777	7806	4693	1284
3985	4520	4549	1366	4749	6500
4117	4878	5113	7016	4857	6501
2500	4879	5372	7081	5034	1331
2541	4928	5402	7680	3188	1362
2552	4942	5821	39	3220	1377
2684	5478	6088	7223	3284	1482
2856	5618	6182	7248	3408	2938
2854	4462	4142	7250	3440	31747
3906	4970	4707	1985	3530	3194?
3922	4993	4801	13	3102	3197?
4100	3298	4834	7797	3286	
4218	3657	4932	12	3288	3500?
	3931	4998	125		3500?
4231			182	3407	3747?
4232	3594	5009		3543	3901?
4741	3733	5163	173	3589	3939
4708	3737	5225	192	3671	3471
3577	3794	5238	201	5328	6068
5087	3824	3497	2322	5592	6251
4242	3829	2746	2329	5118	6252
4288	3850	2780	180	5224	5789
6239	4181	2840	2525	5599	2908
6283	4675	3885	2805	5227	3057
4392	4964	2431	4384	5331	3210
6186	4977	2474	4566	7165	3212
5536	4973	2692	3392	7230	3215
5541	4974	2800	5671	7246	2629
5598	4967	3870	6071	7251	2641
5603	5164	4511	6079	3080	7810
6241	5294	5526	5760	3734	, , , , ,
5878	5368	2469	5851	7076	
5902	5447	2488	5852	4972	
5989	5461	2497	6103	4363	1
6015	5462	2505	6089	4572	1
6140	5477	2534	6177	3890	
6434	5484	2710	6129	4159	1
6742	3398	3353	6142	4331	1
6781	3499	3757	6195	5909	
6814	4054	3795	5702	5912	
7423	4141	4154	5710	6324	ł
2347	4195	2870	5737	5295	
II 2133	4199	3740	2290		
2366	4284	5007	2289	5452 5547	1
2810	4358	5342	2333		
2493	4362	4210	2385	5640 5712	1

	CHEL'R		ЗСП <b>Е</b> L'я /, 1—52	Heri		NECE VI, 4	1—42, VII 38	167,
IV t	IV 51	VΙ	V 51	VII	VIII	VII 51	VIII	VIII 51
1V 50	1V 79	لم 7 50	V 52	VI 42	VII 50	VII 67	VIII 50	VIII 88
7009	6818	253	4236	2420	1662	7062	2509	2306
2261	7635	4536	3359	2304	2244	7082	2063	2413
2245	1501	4910		2269	1498	7209	2251	6507
3662	4143	4123		3055	1817	2253	1896	6561
4517	2537	4293		2194	2236	7762	2264	6596
3423	4051	5293		2355	2356	7790	2180	6910
3507	6301	3346		5053	6520	2192	1663	7024
4567	40	3628		_	6940	2479	1647	6997
456R	3658	6526		3466	G930	6866	2234	1664
3239	3310	6514		6144	2482	1513	2678	2311
63 <b>6</b> 9	3992	6514		6284	2539	1528	2395	1778
6553	3982	6514		6293	2360	6756	6664	7708
6894	5204	6533		6451	2204	2627	6728	7234
6772	2440	6992		6802	2318	2567	6647	381
16	2346	6960		6678	2352	2401	6604	659
6905	2701	68		6839	2354	7142	6834	1027
1253	3963	598		2158	2362	2421	6938	7160
7662	2950	205		2309	6823	1	6837	2126
2170	1514	891		5897	6755		6840	7686
2185	5144	247		288	2215		6885	1582
1964	5856	2359		2266	1758		6800	2281
2467	6888	5170	ì	2548	2254		6RB2	6633
936	6826	3027	t	6645	2489		6950	6828
2023	7023	4505		7044	2112	1	2169	7031
2327	7129	246		1245	2186		2232	7243
1535	6946	3003		1605	2225		2129	6991
3242	1325	2264		2301	2349	1	2367	7380
4038	4750	2024		2259	2423		2026	225
3456	3034	4395		7245	5998	1	7826	129
4861		1977		7789	6568		2627	1444
7302		1980		663	6583		2286	6793
1700		1788		7086	752		2335	6989
1999		1908		869	1857		2343	6895
2022	1	1990		884	1883		2353	1348
2610				136	2224		2374	1545
2071	i	206		2432	2270		2396	6874
6543		7000		2506	2262		2414	2425
2182		1909	l .	6804	2324		2422	1342
2438 4804		3511 3513		2571 6171	1907 7128		2302	
6514		4244		6412	7296		1802	
676		4631		6939			1996	
1186		4258		4539	7419		1750	1
2167		2403			7510		2394	
2392		3953			436	i	2358	
5493		3556		}	654	1	2430	
4915		3079		l e	1502		2428	
3104		1097	ļ		559		2260	
5507	1	1624	1		637		2240	
6229	i	2997			7067		2252	

Appendix No 3
Finding List for General Catalogue Numbers

GC	NGC	GC	NGC	GC	NGC
100 200 300 400 500 600 700 800 900 1000 1100 1200 1300 1400 1500 1600 1700 2000 2100 2200 2400 2500 2600 2700 2800 2700 2800 2900 3000 3100 3200 3300 3400 3500 3600 3700 3800 3900 4000 4100 4200 4500 4500 4500 4500 4500 4500 45	196 376 516 676 812 1068 1320 1500 1653 1783 1892 1997 2102 2216 2436 2488 2666 2816 2969 3105 3240 3376 33519 3658 3812 3911 4077 4209 1334 4444 4556 4668 4793 4961 5095 5227 5361 5492 5634 5771 5925 6152 6362 6611 6805 6960 7127 7299 77507 7727	5057 58 59 60 5061 62 63 64 65 66 67 68 69 70 5071 72 73 74 75 76 77 78 80	7832 119 313 1251 1312 1767 1922 2189 2198 2515 3123 3229 3801 4270 4582 5200 5310 5366 5404 6634 7150 7285 7692 3	\$100 \$200 \$300 \$400 \$500 \$600 \$700 \$900 6000 6100 6200	113 751 1236 2487 2943 4031 4893 6041 6579 7085 7420 7670

Appendix No. 4

JH	NGC	J HL	NGC	JЩ	NGC	J H.	NGC
1	12	1500	4864	3000	2150	4000	7713
50	224	50	5009	50	2231	4006	7764
100	477	1600	5142	3100	2452	4007	319
50	672	50	5248	50	2788	4008	322
200	835	1700	5352	3200	3053	4009	7796
50	1043	50	5475	50	3247	4010	7812
300	1343	1800	5603	3300	3447	4011	7823
50	1857	50	5696	50	3742	4012	368
400	2262	1900	5834	3400	4553	4013	7832
50	2392	50	6103	50	4903	4014	7
500	2562	2000	6572	3500	5126	4015	10
50	2742	50	6826	50	5393	4016	1905
600	2889	2100	7010	3600	5915	4017	2658
50	3032	50	7218	50	6222	4018	2973
700	3207	2200	7458	3700	6407	4019	3244
50	3370	50	7691	50	6653	4020	6404
800	3475	2300	7817	3800	6816	4021	6708
50	3614	50	264	50	7007		
900	3697	2400	461	3900	7154		
50	3819	50	754	50	7322		
1000	3930	2500	1140				
50	4036	50	1359				
1100	4123	2600	1493				
50	4221	50	1616				
1200	4299	2700	1759				
50	4387	50	1816				
1300	4484	2800	1871				
50	4555	50	1943				
1400	4635	2900	2014				
50	4727	50	2080				

## Appendix No. 5

### Systems of Nobular Classification.

- A Classification of Sir Wm HERECHEL. This consisted of eight main classes,
  - I Bright nebules.
  - II Paint nebulae.

  - IV. Planetary nebulae Stars with burs, with milky chovelure, with short rays. romarkable shapes, etc.

V. VOLV

o extremely,

- V Vory large nebulae.
- VI Very compressed and rich clusters of stars
- VII. Protty much compressed clusters of large or small stars,
- VIII Coarsely scattered clusters of stars.

9. Small

As an amplification of those main classes, HERSCHEL used the abbreviations,

- B Bright
- F. Paint c. considerably L. Large p. protty
- the combination of which gave him sixteen available subdivisions in each class. A decen or so other casily understood abbreviations gave a further description of the object in a very compact form, as,

vBpLvgmbM = "very bright, protty large, very gradually much brighter in the middle."

B Classification of Sir J Hirschill He introduced into his father's system five categories, each with five subdivisions

2000				C. I marilan	Resolvability
Sub class	Magnitude	Brightness	Roundness	Condensation	- terminates
1 2 3 4	Great Large Middle-sized Small Minute	Lucid Bright Faint Dim Obscine	Circular Round Oval Etongate Linear	Stellate   Nuclear   Concentrated   Graduating   Discoid	Districte Resolvable Granulate Mottled Milky

The object was then described by five numerals, 32255 would indicate "Middle sized, bright, round, discoid, milky". This system, with minor modifications, was employed by Schulze, Nov Act Reg Ups 9 (1874). A somewhat similar system was employed by Bigourdan, CR 158, p. 1949 (1914), making use of nine sub classes under each of the categories, brightness, extension, form, condensation, and resolvability.

- C Bailey's Classification the merit of this classification is that the element of spectral type was included Harv Ann 60 (8), p 200 (1908)
  - A Vast, faint, irregular nebulosities, shown on photographs of long exposmo Examples, Nebula in Cygnus, Great Spiral about Orion
  - B Gaseous nebulae Objects having gaseous spectrum
    - B1 Large, diffused, irregular Examples Orion, η Carmae
    - B2 Planetary, rmg, and other small, well-defined gaseous nebulae Examples 3587 (Plan), 6720 (Ring neb), 6618
    - B3 Nebulous stars
  - Examples, 1514, 2003
    C White nebulae and globular clusters Objects having continuous spectra
    - C1 Nebulae, small, round, unresolved, of somewhat definite form, generally round or elliptical
    - C2 Spiral nebulae Examples 224 (Andromeda), 5194
    - C3 Globular clusters
      Examples 5139 (\omega Centauri), 6205 (Hercules)
  - D) Trregular clusters
    - D1 Fairly condensed, somewhat regular, stars of comparatively uniform magnitudes
      Examples 2437, 6494
    - D2 Fairly condensed, irregular, stars of different magnitudes Examples 869 and 884 (double cluster in Porseus), 4755 (x Cincis)
    - D3 Coarse, irregular, stars of different magnitudes Examples: Hyades, Pleiades
  - D Classification suggested by H Shapley [Harv Bull 849 (1928)]

Brightness,	Class A, brighter than 12 phg magn
4	,, B, 12-14 ,, ,,
	, C, 14-16 ,, ,,
	, D, 16-18 ,, ,,
	, E, 18-20 ,, ,,
Concentration,	a, least concentrated
	b,
	C,
	d,
	e,
	f, most concentrated
Degree of elonga	tion, 10 (round) to 1 (most elongated), determined from 10 · b/a, where a and b are the major and minor axes
Spiral form,	classification preceded by s
Irregular,	11 11 12 12
	Example: sAb9 = "a nearly round, bright spiral, very little

Example: sAb9 = "a nearly round, bright spiral, very little concentrated"

E Word's Classification Die Klassifizierung der kleinen Nebelflecken, mit Tafel, Heidelberg Astroph Inst 3, No 5 (1908), used also by Hunner, Yorkes Publ 4, part II (1917), with the addition of an extra type  $h_0$ 

An empirical system of classification, of 22 types indicated by the letters from a to w, with the emission of f, x, y, and s. The forms corresponding to these letters are given in a chart, to which reference must be made. See also Lundmark's allocation of Wols's types under G below

If Hunsle's Nobular Classification Mt Wilson Contr 324 (1926), of also ibld.

214 (1921) In this system it is assumed that the evolution of the spirals is from an earlier, closely arranged and compact form to an older form of more open arrangement

Chernoter	Gymtani		NGC Example
I Galactic nebulac			
A Planotaries ,	P		7662
B. Diffuse	D		
1 Predominantly luminous 2 Predominantly obscure 3 Conspicuously mixed	DL DO DLO		6619 Barnard 92 7023
II, Extra-galactic nebulac			
A. Rogular			
1 Illiptical (s, omitting the decimal point = 1, 2,	E#	Eo	3379
object)		II.2	221
		R5	4621
2 Spirals	1	E7	2117
•	s		
a) Normal spirals	Sa. Sb So		4594 2841 5457
b) Barrod spirals	SB		
1 Barly.	SBa		2859
2. Intermediate	SBb		7479
3. Late	SBc		3351
B. Irrogular	Irr		4449
Rxtra-galactic nebulae too faint to be classified	ا و		

G LUNDMARK'S Nobular Classification. Studies of Anagalactic Nobulae, First Paper, Ups Modd 30 (1927) is perhaps the most detailed classification which has appeared to date. It is given below with a few verbal changes, and with LUNDMARK's allocation of WOLF'S types.

	Character	Bymbol	Example	World
ī	Galactic Nebulac	G		
	1 Quasi-planetary nobulac	Gp		a, b, c
	a) No contral star	Gp0	6537	a, b,
	b) Hollooidal forms c) Central star and different gradations in the ratio of total light to light of	Gph	6543	•
	central star	Gp1—Gp10	40	C
	2. Irregular nebulae a) Irregular bright nebulae b) Irregular dark nebulae	GI GIb GId		
ÌΤ	Anagalactic nebulae	A		ĺ
	1. Anomalous nebulac	Aa	2537 5144	
	2. Globular, elliptical, elongated, ovate, or lentiquiar nobulae	Λο		
	a) Very little compressed toward center	OaA	4302	d, h
	b) Slightly compressed toward center	A61 A62	2233 1600	8

Character	Symbol	Frample	Wolf
d) Rather	Ae3	1382 1278	f, g, h, 1, k
f) Very much ,, ,, The letter a is added if absorpresent, e g	orption is Ae5	4486]	
3 Magellanic nebulae	Am		
a) Very little if at all compressed	l towards		
center	Am0		p? q?
b) Different degrees of compre	ssion Am1-Am5	1449	
4 Spiral nebulac	Ая		
a) Spiral structure barely seen	Aso	4 194	0
b) Different degrees of compre			
wards center	As1-As5		
Spiral arms continuous	As1c-As5c	3031	S, V
Spual arms broken	As1b—As5b	598	r, u, v
c) One-branched spirals	Aso (	5278	
d) Spual arms form a bught i		4736	t
e) Doubtful connection of 1mg w			
(Saturn-shaped)	Ass	936	
f) Barred spirals	Asp	1326	1
g) Spiral arms have an append	ıx nebula   Asa	5194 - 5	1

## Appendix No 6.

#### Published Reproductions of Nebulae

Introductory Any system of classification, however detailed, has serious limitations in the representation of objects which differ so greatly from individual to individual as do the diffuse and planetary types, and the spirals. For this purpose, there is nothing quite so satisfactory as a pictorial representation. The ideal NGC of the future would have a picture of the object at each entry!

Photographs and sketches of the various classes comprised under the term "nebulae" are for the most part widely scattered in the periodical literature. The following list is intended to give, in general, the best available representations that are available up to 1931. The list does not pretend to be complete, where there are very many representations available, as for an object like the Great Nebula in Orion, only a few of the better plates are mentioned. Reproductions in articles or books of a more popular nature are omitted, unless no other example occurs

The sketches of Rosse and Lassell have been included for their historical interest; these observers were the first to employ apertures adequate to recognize spiral character. Sketches will be indicated by asterisks\* \* It should be noted that the sketches made at Helwan and those of the planetaries made at Lick were carefully drawn from photographs and are nearly the equivalent of a photograph. The very large number of sketches in the older literature, made from visual observations, have been omitted, except as noted above.

References are given in the form Publication, volume, page preceding plate, number of figure on the plate if more than one is given, date Dates are omitted for Lick Publ 8 (1909), 11 (1913), 13 (1918), for Barnard's Atlas of Selected Regions of the Milky Way, Carnegie Institution, Washington, 1927 (abbreviated to 'Atlas').

Rosse's drawings appeared originally in Phil Trans 1850 and 1861, they are now most easily accessible in his Collected Scientific Papers, 1926. The plates retain the pagination of the Phil Trans, Plates XXXVI—XXXVIII

follow pages 112, 114, and 116 of the Collected Papers, and are from Phil Trans 1850; Plates XXV—XXXI follow page 150, and are from Phil Trans 1861. In citations of Rosse the page and date will be omitted.

LASSELL'S sketches (LAS) appeared in Mem RAS 36, pp. 82ff. (1866).

The plate only will be quoted, omitting the page and the date.

ROBERTS, Photographs of Stars, Star Clusters and Nebulae, London, 1893, 2 vols., will be referred to by ROB I and II. The dates given are those on which the respective plates were made, as for many objects the photographs of ROBERTS were the first taken. Other photographs published and discussed by Mrs. ISAAC ROBERTS in the M N are also headed ROB.

A large number of BARNARD's dark nebulae are best studied in the Atlas; entry is generally given for these objects only when taken individually. fr. = frontispiece; end = at end of volume, etc.

Most of the illustrations in the Ap J will be found also in Mt Wilson Contr

where the paper is repeated.

Number	Class	Reference
40	plan.	Lick Publ 13, p. 58, VIII, 1a and *L*; spectrum, ibld., p. 86
	L	XXVII, 4, 5, 15; p. 240, XLIV, 3, 4, 5; L, 3.
68	nob, st.?	*ROSSB, XXV, 1*; *ROB, M N 73, VI, VII (1913)*.
131	ell.	*Helw Bull No. 9, II, 1 (1912)*.
134	spir.	*Helw Bull No. 9, II, 1 (1912)*.
150	barr, sp.?	*Holw Bull No. 9, II, 2 (1912)*.
151	spir.	Helw Bull No. 22, III (1921).
169	edgew, sp.	Lick Publ 13, p. 54, III, 20.
205	spir.	Ap J 46, p. 25, IX, a (1917).
221	oll.	Ap J 64, p. 324, XIV (1926).
224	spir,	ROB II, X (1894); Yerkes Publ 2, XXIV (1903); Lick Publ
(Andr.)	Opar,	8, I; 13, p. 54, VI, 76, 77, 78; Ap J 69, p. 158, I-VI, th
(		best direct, and also with novae and variables. Spectrum
		Wolf, Szber Heidelb Akad Abh 27 (1910), 8.
246	plan,	ROB II, XVIII (1898); *M N 74, p. 712, XX (1914)*; *Hel
240	page,	Bull No. 9, II (1912)*; Lick Publ 13, p. 58, VIII, 2.
247	spir.?	*Helw Bull No. 9, II, 4 (1912)*; *ROB, M N 75, p. 191, X
24/	obir't	(1915)*.
253	no.l.	Lick Publ 8, II; *LAS I, 1*.
255	spir.	Publ A S P 43, p. 352 (1931).
	spir.	*Helw Bull No. 9, II, 6 (1912)*.
2745	diff.	
278	spir.	Ap J 46, p. 25, IX, b (1917); *ROB, M N 72, p. 408, III (1912)
281	dlff.	ROB II, XXII (1896).
300	spir.	Helw Bull No. 22, I. (1921); *ibld., No. 9, II, 5 (1912)*.
578	spir,	Helw Bull No. 22, III (1921).
598	spir.	*Rosse, XXVI; XXXVI, 5*; ROB II, X (1895); Yorkes Pu 2, XXV (1903); Lick Publ 8, III.
613	harr en	Holw Bull No. 9, I (1912).
628	barr, sp.	ROB II, XI (1893); Lick Publ 8, IV.
650-1	spir.	Lick Publ 8, V; 13, p. 58, VIII, 3.
678	plan.	
693	edgew, sp.	*Lick Publ 13, p. 54, III, 19*. *Rosse, XXV, 2*.
697	spindle	Lick Publ 13, p. 54, IV, 45.
770	spir.	*Dogge VVVVIII 10*
821		*ROSE, XXXVIII, 12*.
828	apir.	*ROB, M N 74, p. 238, X, 4 (1914)*.
891	spir.	*Lick Publ 13, p. 54, IV, 33*.
051	edgew, ap,	ROB I, VIII (1891); FRANKS, M N 65, p. 160, VIII, 1 (1904
008	anta	Lick Publ 8, VI; 13, III, 1.
908	spir.	FRANKS, M N 65, p. 228, VIII (1904).
936	barr. sp.	*Holw Bull No. 9, III, 7 (1912)*,
972	spir,	*Rosse, XXV, 3*; Ap J 46, p. 25, IX, c (1917); Lick Publ 1
4040	onto 3	p. 54, V, 66.
1012	spir.?	*Rosse, XXV, 4*.
1023	spir.?	*Rossn, XXV, 5*.

Number	Class	Reference
1068	spir	*Rosse, XXV, 6*, *LAS I, 2*, ROB I, X (1892), Lick Pub 8, VII, Ap J 46, p 25, IX, c, d (1917)
1084	spir	*I AS I, 3*
1087	Spir	Helw Bull No 22, III (1921)
1097	barr sp	Helw Bull No 22, I, III (1921), M N 85, p 1018, XX (1925)
1186	spn	Ap J 51, p 279, XIII, d (1920)
1187	bair sp	Helw Bull No 22, IV (1921), *1bid, No 9, III, 8 (1912)*
1270	spir )	Spectra taken with RAYION lens and photograph of region
1273	spir }	m Ap J 71, p 354 (1930)
1300	bari sp	Publ ASP 24, p 227 (1912), Inck Publ 13, p 13, I, 2,
1309	spir	Helw Bull No 22, IV (1921)
1316	diff?	*Helw Bull No 9, HI, 9 (1912)*
1350	spir	*Helw Bull No 9, III, 10 (1912)*
1365	ban sp?	*Helw Bull No 9, HI, 11 (1912)*
1491	ban sp	Ap J 51, p 279, XIII, c (1920)
1499	diff	ROB II, XX (1897), Ap J 2, p 350, XI (1895)
1501	plan	Ap I 46, p 25, VI, a (1917), Lick Publ 13, p 58, IX, 6a, *6
1514	plan	*Rossr, XXV, 7*, *ROB, MN 71, p 234, VIII, 1 (1914)
1714	Prices	Lick Publ 13, p 58, IX, 7
1518	ir sp	Helw Bull No 22, IV (1921)
	bari sp	Lick Publ 13, p 43, I, 2, b
1530	ell	*Helw Bull No 9, III, 12 (1912)*
1531 1532	edgew sp	*Helw Bull No 9, III, 12 (1912)*
7		*LAS, I, 4*, Ap J 46, p 25, VI, b (1917), M N 60, p 43
1535	Plan	(1900), Lick Publ 13, p 58, IX, 8a and *8*
	7777 11.55	*Prase, Ap J 45, p 89, I, 1, a (1917)*
1555	vai diff	*Rosse, XXV, 8*, Ap J 46, p 25, VIII, a (1917)
1579	diff	*Lick Publ 13, p 90, fig 7*
1714	plan	*Lick Publ 13, p 92, fig 9*
1722	plan	
1743	plan ?	*Lick Publ 43, p 92, fig 10*
1763	diff	*Lick Publ 13, p 92, fig 11*   Helw Bull No 22, II (1921)
1788	diff	*Helw Bull No 9, IV, 13 (1912)*
1792	spn	
1888	edgew sp	Lick Publ 13, p 54, IV, 29
1935	Plan	*Lick Publ 13, p 94, fig 14*  *LAS, I, 6*, ROB I, XIV (1892), ibid, II, XXVI (1892)
1952	plan?	I tek Publ 8, IX, 1bid, 13, p 58, X, 11
(Crab)	7.60	ROB I, XVI (1888), abid, II, XXVI (1896), Lick Publ
1976 (Orion)	diff	fi and XI, Pop Astr 31, p 376, XXV (1923), Yerkes Po 2 (inner), XXI, (whole) XXIII (1903) Radial velocity
		Lick Publ 13, p 98, XXVIII, 18, 19, Spectrum, 1bl
	1	XXIV, 20, 21, 22, XLIII, 4, Great outer portions a
		'loop' (II 2118), Wolr, M N 65, p 303, XI (1903), Szl
		Heidelb Akad 1, p 23 (1902), M N 65, p 528 (1925), Ap
		65, p 136, II (1927) (best)
1977	diff	Lick Publ 8, XII, Ap J 57, p 138, VI (1923)
1980	dıff	*Rossr, XXXVIII, 16*
2022	plan	*LAS, I, 8*, Ap J 46, p 25, VI, c (1917), *I ick Publ
2024	dıff	p 58, X, 12* Lick Publ 8, XIII, Ap J 53, p 392, XI, XII (1921)
2029	plan ?	*Lick Publ 13, p 108, fig 23*
2068	diff	Lick Publ 8, XIV
2070	diff	*Lick Publ 13, p 108, fig 24*
		*Lick Publ 13, p 109, fig 25*
2077	plan ?	*Lick Publ 13, p 109, fig 26*
2079	plan	*Lick Publ 13, p 109, fig 25*
2080	plan	*Lick Publ 13, p 110, fig 27*
2086	plan (2)	Lick Publ 13, p 54, III, 14, Ap J 51, p 279, XIII, f (192
2146	edgew sp	Atlas, IX
2175	diff	ROB II, XXVII (1899), Lick Publ 41, XXVI, XXVII
2237-9 2245	diff	*Rosse, XXVII, 11*

Number	Cluss	Roference
2261	var, diff,	*Rosse, XXXVII, 10*; Helw Bull No. 22, VII, VIII (1921) Pop Astr 26, p. 248, XI (1918); Hubble, Ap J 44, p. 1
22(1	1116	(1910); 45, p. 352, 1X (1917).
2264	diff.	Lick Publ 8, XV; AN 221, p. 376 (1924).
2288		\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \
2289		
2290}	spir. (5)	Ap J 51, p. 279, XIII, a (1920).
2291		1 5 5 7 1 - 177 1 - 172 1 1 (1720)
2294		
2316	3	*Rosse, XXVII, 12*.
2359	diff.	*TAC II ON. A. T. F
2371-2	plan.	*LAS, II, 9*; Ap J 51, p. 279, XVI, b (1920).
23/11-2	Patrici	*Rosse, XXXVII, 6*; *LAS I, 10*; Ap J 46, p. 25, VI,
0202	alou	(1917); Lick Publ 13, p. 58, XI, 16.
2392	plan.	*I.AS I, 11*; Ap J 46, p. 25, VI, d (1917); Lick Publ
		1. 58, X1, 17a and *17*; Spectra; ibid., 13, p. 112, XX
		28; XXXI, 29; 240, XLIII, 1; XLVII, 1.
2403	spir.	ROB 11, X1; Ap J 46, p. 25, X, c (1917); Lick Publ 8, XV
2438	plan.	ROB II, XVIII; Lick Publ 13, p. 58, XII, 18a, and *1.
2440	plan.	Lick Publ 13, p. 58, XII, 19a, and *19*.
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2782	barr, sp.	*ROB M N 74, p, 238, X, 6 (1914)*.
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7640	apir	I.lek Publ 13, p 54, V, 65
7662	plan	*Rosse, XXX, 40*, *LAS, X, 38*, Lick Publ 8, LX1\(\lambda\),
		Ap J 46, p 25, VII, f (1917), *Lick Publ 13, p 58, XXIV,
		78*, Spectrum, Ibid , 164, XL, 64, 240, XI.II, 2, XI.VI,
		3, 4, 5
7678	apir	*Rosak, XXX, 41*
7814	odgow sp	*Rossa, XXX, 42*, ROB I, LHI (1891), Lick Publ S, LXX,
,		13, p 54, III, 3
7817	spir	Lick Publ 13, p 54, IV, 49
,0.,	-1771	1 240 C 2 2 1 2 1 2 1 4 1 4 1 4 1
		Pirat Index Catalogue
I 59	difL	ROB II, XXV (1895), Lick Publ 13, p 43, II, 4
_		#Tick Dubl 42 n ce TV ce
_	plan	*Lick Publ 13, p 58, IX, 5*
	dill	Knowl 26, p. 81 (1903), Sirius 38, p. 288, XIII (1906)
I 418	plan	*Lick Publ 13, p 58, X, 10*, Spectrum, ibid, 240, XLIX, 4
I 434	dill +dark	I 431, 433, 434, near & Orlonia, ROB M N 63, p 32, I (1902)
		Ap J 53, p 392, XI (1921), Lick Publ 13, p. 42, 11, 5
_		Harv Ann 32, III, 3 (1895), Ap J 38, p 500, XX, 1 (1913)
I 1029	spir	*Lick Publ 13, p 54, IV, 30*
I 1470	qjtt	Ap J 51, p 279, XVIII, a (1920)
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Number Class	Reference
II 1747 plan II 2116 plan II 2116 plan II 2119 plan II 2165 plan II 2165 plan II 2167 spn II 3568 plan II 4406 plan II 4593 plan II 4732 plan II 4732 plan II 4776 plan II 4997 plan II 5117 plan II 5117	Second Index Catalogue  *Lick Publ 13, p 58 VIII 19  *Tick Publ 13 p 92 fig 12*  Sec 1976 Onon  *Tick Publ 13 p 58 X 1 41*  Lick Publ 13 p 58 X 1 41*  Lick Publ 13 p 58 X 1 41*  Lick Publ 13, p 58, XIII, 25*  *Iick Publ 13, p 58, XIII 27*  *Lick Publ 13, p 58 XII 27*  *Lick Publ 13, p 58 XII 27*  *Lick Publ 13, p 58 XVII, 11  *Lick Publ 13, p 58 XVII, 11  *Lick Publ 13, p 58, XVII 50*  Lick Publ 13, p 58, XVII 50*  Lick Publ 13, p 58, XVII 79  Lick Publ 13, p 58, XVII 79
JONCKHELRL  320 plan  JONCKHERRE  300 plan  249 galaxies at 12 <sup>h</sup> 55 <sup>m</sup> + 28° 30′  Cluster of galaxies in Ursa  Maj (Bande)  Christies Cluster in Leo  Large Magellanic Cloud	*Lick Publ 13, p 58, XXIII 75*  *Lick Publ 13, p 58 IX, 0*  *Lick Publ 13, p 58 XI, 15*  Lick Publ 13, p 13 I, 3  A N 233 p 71, II (1928)  Publ A S P 13, p 350 (1931)  Harv Ann 20, end, IV, 2 (1891), 60 p 108 II (1908). Mem  R A S 60, p 144 V (1903), Hary Bull No 881, II (1931)
Small Magellanic Cloud	Huy Ann 26, end, IV (1891), 60, p 108, I (1908)

The largest of the diffuse nebulae are best seen in plates taken with instruments of shorter focus. Many such, frequently combining luminous and dark nebulosity, can be found in Barnard's Atlas, passim. Others are

Very large diffuse neb in Auriga About y Carmae

Detached diff neb in Cygnus Near y Cygni

Very large, near ψ Eridani Diff, in Monoceros Bright and dark neb near ρ Ophiachi Very large diffuse near ξ Persei Large diff + dark near ρ Persei

Outer nebulosity of Pleiades

Pleiades diffuse neb

Very large diff near i Scorpu Verv large diff near i Scorpu Several diff neb in Vela Preceding 7000 Enormous diff in Taurus and Perseus 'Cave' neb in Cepheus Near I 405 Worr, M N 63, p 506 && (1903) Harv Ann 26, end, V, I, 2 3, VII 2 (1891) 60 p 229, IV (1908) (best), Mem R A S 60, p 111, VI (1910)

Franks M N 65 p 158, VI (1901)
Lick Publ 11, I XXVI, Ap J 63, p 121, VIII, 126, IX (1926),
Atlas XLIV, ROB II, XXIII (1895)
Wolf, M N 65, p 528 AV (1905)
Lick Publ 8 XVI

Atlas, XIII, Lick Publ 11 XXXVI

Lick Publ 11, XVI, XVII

Atlas III Lick Publ 8, IX, Yerkes Publ 2, XXVI (1903), ROB 1, XI (1888), II, XXV (1897) BARNARD, M N 60 p 258 IX, X (1900), Ross, Ap J 67, p 294, VIII (1928), lick Publ 11 XV Atlas, XII Atlas, XI

MELOITL M N 86, p 636 AV (1926) Ap J 63 p 122 VII (1926) Ross, Ap J 67, p 280, VI (1928)

Ross, Ap J 67, p 292, VII (1928) Worr, M N 69, p 117 VI (1908)

### Dark Nebulae

Most of the dark nebulae which BARNARD has catalogued will be found noted in the descriptive matter accompanying the plates of his Atlas, without doubt the most wonderful Milky Way photographs which have ever been made Some of the smaller spots which have been observed with instruments of greater focal length are given below

BARRARD No	a 1875,0	à 1875,0	Raterence
13	5h 34h	,6 — 2° 32′	Ар J 53, р 392, VI (1921), Lick Publ 13, р 43, II, 5
63	17 0	21 20	Ap J 49 p to, 111, a (1919)
64	17 10	-18 21	Ap J 49, p 10, IV, d (1919)
	17 10	-23 30	Ap J 49, p 10, III, b (1919), 57, p 143, VIII
75	17 18	-21 55	Ap J 49, p 8, II, b (1918)
84	17 39	20 12	Ap J 49, p 8, II, a (1919)
86	17 55	-27 52	Lick Publ 13, p. 54 VII, 80, Ap J 63, p. 122, VI (1926)
92-93	18 9	~ 18 10	Ap J 57, p 143, X, XI (1923)
98	18 25	-26 9	Ap ] 49, p 10, IV, c (1919)
127	18 55	- 5 37	Ap J 49, p. 10, IV, a (1919)
129	18 55	- 5 29	Λp ] 49, p 10, IV, a (1919)
133	19 00	- 7 5	Ap J 57, p. 144, XII (1923), 49, p 10, IV, b (1919)

## Appendix No. 7

### Abridged Nebular Bibliographical Apparatus

1 Lists of Nebulae Vimini Micrometric Positions.

W HERBERRY, Scientific Papers of, published by the Royal Society and the Royal Astronomical Society, London (1912), 2 vols. Collects his papers scattered in the Phil Trans and other media 2500 entries, J HERSCHEL, General Catalogue of Nebulae, Phil Trans (1864) 5079 entitles, Result, Phil 7 mas (1853) and (1861), observations amembied in Trans Roy Dublin Sec 2 (1880), now most easily accordible in his Collected Scientific Papers, London (1926). LABORLE, MARTIN Catalogue of (XX) objects found at Malta, Mem RAS 36 (1866), D'ARREST, Siderum nebulosorum observationes Havnionses Copenhagen (1867) 1942 entries. Micrometer, RUMKER, A N 63 to 68, New 1508, 1531, 1566, 1599, 1631 (1863 to 1866) Ring micromoter 135 objects, Schönker D. Astr Boob Mannholm 1, 2 (1862—1875) Ring micrometer 489 oblouts, Schul Tz, Nov Acta Reg Ups 9 (1874) Micrometer 500 objects, General catalogue of nebulae observed at Stressburg, by various observers, 1881 to 1910, Ann Sternw Strassb 4, 1257 NGC objects Micrometer, WINNECKE, Bearbeltot von E BECKER, Ann Stormw Strassb 3, p 1 (1909) Micrometer 406 NGC objects, Wirtz, Boobachtung von Nobelflecken, nungeführt in den Jahren 1880-1902, von H Kobold, A WINNECKE und W Schur, Micrometer 619 objects Ann Sternw Strassb 3, JAVELLE, Catalogue de nébulcuses, Ann Nico 4 (1895), 6 (1897), 11 (1908) Micromoter 1469 objects, Bigourdan, Ann Paris (1884ff.) I hour in a per volume Since published by Gauthler-Villars. Micrometer Bidoux-DAN sot out to observe every NGC object visible from the latitude of Paris, STEPHAN, Muny references in periodical literature, collected in the introduction to the NGC, p. 9, DREYER, A New General Catalogue of Nebulae and Clusters of Stars, being the Catalogue of the late Sir John I. W. Herschel, revised, corrected, and enlarged. Mem R A S Lond 49, p 1 (1888) lucludes all results known to the end of 1887 7840 entries + 88 objects found by Swift The Introduction contains references to the work of all earlier investigators. See also WIRTE' comparisons in Ann Stornw Strassi 4, Index Catalogue of Nebulae found in the Years 1888 to 1894, with Notes and Corrections to the New General Catalogue Mem R A S Lond 51, p 185 (1895) 1529 entries, Second Index Catalogue of Nobulae and Clusters of Stars, containing these found in the years 1895 to 1897, etc. Mom R A S Lond 59 (1908) 3857 entries, continuing from First Index Catalogue to No 5386, here, for the first time, photography bogins to overwhelm the entaloguer, of the 2800 Worr nebulae known at that time, the 1500 in the the future great catalogues of nebulae will certainly have to be third list are emitted " REFERENCE IN ZOMOS Of one degree " AUWERS, Verzeichnis der Orter von viersig Nebelflecken AN 58, p 369 (1862) Hollometer 40 objects, ROMBER, Beobachtungen von Alrkumpolar Nebeln

678

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No 8

3, p 87

(1908)

770

auf der Hamburger Steinwarte A N 63, p 305 (1865) of, p 289 (1865), 66, p 81 (1866), 67, p 225 (1806) 68, p 353 (1867) 437 entires Ring micrometer, Vogit, Beobachtungen von Nebelflecken Leipzig (1867) Micrometer 100 objects Publ Leipzig 1 p 3 (1882) Micrometer 132 nebulae Engry Mann, Mendian-Beobachtungen von Nebelflecken A N 101, p 193 (1883) Mendian circle 124 nebulae Klimpi, Publ Astroph Potsdam 7 p 145 (1892) Micrometer 82 objects Porti R, Publ Cine 11 (1891) Micrometer 105 nebular D'ENCLI HARDT, Observations astronomiques faites a Diesde 3, p. 96 (1895). Micrometer 590 nebulae, Breker, Ann Obs I dinb 1, p. 1 (1902) 217 objects. Mendian enele. Monnienni yer. Veröft Steinw Bonn 1 (1895). Ring micrometer. 236 objects. Spilali R. A. N. 132, p. 369. (1893) Ring micrometer 136 entites, MLRI CKI, Observations micrometriques de ni bulcuses, I, Wusaw (1903) 72 objects Micrometer, HAGIN, A preputatory catalogue for a Duich mustcing of nebulae. The zone catalogue. Spec Vat. 10 (1922-1927). I BICKIR A preparatory cat dogue for a Durchmustering of nebulae. The general catalogue. Spec Vat 13 (1928) About 4100 entries,  $\pm$  705 with designation st (stellar), and 700 unconfirmed obrects

### 2 Lists of Nebulae Photographic

Wort (and colleagues) Kongstuhl Nebel-Listen Publ Heidelb (Kongstuhl) List No 1 1, p 11 (1902)151 entires List No 9, 3, p 149 (1909) 102 entrics No 10, 6 p No 11, 6, No No 2, 1, p 17 301 1 (1909) 62 (1902)No 3, 1, p 125 (1902) 1528 2 (1909) 91 No 4 2 p 57 (1904)272 No 12, 6, No 3 (1911) 279 11 No 13 6, No 8 (1912) No 11 6 No 10 (1913) No 5 2, p 77 (1904)239 111 No 6 2, p 89 (1905)204 511 No 7. 3 p 77 (1907)310 No 15, 7, No 7 (1916) 189 No 16, 8, No 11 (1928)

WOLF and KAISLE, Positionsbestimming von 124 Nebelflecken im Perseus-Nebelhaufen Publ Heidelb 6, No. 11 (1913), JORINZ, Positionsbestimmung von 178 Nebelflecken Publ Heidelb 6 No. 1 (1911) Nearly all NGC objects. Reinmuri, Photographische Positionsbestimmung von Nebelflecken (Winnecke-Nebel). Publ Heidelb 8, No. 2 (1927) 321 entries, 111 photographische Nebelpositionen, ibid 7, No 8 (1916) 111 objects, mostly new, 1bid 8, No 14 (1929) 351 entries, Photographische Positionsbestimmung von 356 Schultzschen Nebelslecken 1bid 7 No 6 (1916) 356 entries, all NGC, Photographische Positionsbestimmung von Nebelflecken in Virgo, ibid 8, No 7 (1927) 334 entries, ibid 8 No 11 (1928) 317 entries, mostly new Die Heischel-Nebel nach Aufnahmen der Kömgstuhl-Steinwarte, Heidelb 9 (1926) This work contains 6251 NGC objects and is the largest single photographic nebular catalogue in existence. It assembles all the previous Königstuhl work by Wirtz, Rlinmuth, and others It gives a, b, L, B, the diameters along major and minor axes and brief description, Pr Ase, Photographs of nebulae with the 60 meh reflector, 1917-1919, Ap J 51, p 276 (1920) Descriptions of 330 objects, Curits, Descrip tions of 762 Nebulae and Clusters photographed with the Crossley Reflector Lick Publ 13 KNOX-SHAW, Helw Bull No 9, p 69 (1912) 112 NGC and 48 new, ibid No 15, p 129 (1915) ca 195 NGC and 31 new, ibid No 30, p 71 (1924) 70 entries Gri Gory, Helw Bull No 21, p 201 (1921) 168 NGC, 177 new, ibid No 22, p 219 (1921) 183 NGC 60 new, BAHJY Nebulae discovered at the Haivard College Observatory Harv Ann 60, p 147 (1908) 1238 new objects 1659 new nebulae, ibid 72, p 17 (1913), Shapily, Menzil, and Campbelli, Descrip tions and positions of 2829 new nebulae Haiv Ann 85 p 113 (1924), Minzii, Haiv Bull No 773 ca 2000 new objects, mostly south of -45°, Hubbil, Extra galactic nebulae Ap J 64, p 321 (1926) Classifies 400 objects of the spiral type, Duncan, Photographic studies of nebulae Ap J 51, p 4 (1920), 53 p 392 (1921) 57, p 137 (1923), Killin, 744 nebulae (small) discovered on the plates of the Crossley program Lick Publ 8, p 31 (1908). 511 BLRNAGEI, Positionsmessing von Nebelflecken AN 230, p 305, 441 (1927) 189 entries

References to other phenomena of the nebulae will be found in the separate sections.

## Appendix No 8

A lest of the Moissard Modification of the Doppier Formula in a Universe of the CHARLIER Type

The Morssann hypothesis (see ciph 78) requires that we take into account the absolute velocity of the observer's system through the medium, as well as the relative motion of source and observer in the line of sight. In applying this theory to the observed data, it does not seem at all essential that we hold to the word "absolute", for we know nothing of our absolute speed in space, and apparently must remain forever ignorant of its direction and amount. We may think, however, of various frames of reference to which our motion is relative e.g., the motion of our galaxy within the frame of reference given by the totality of members of our particular cluster of galaxies. We may even continue the analysis and consider the motion of this cluster of galaxies with regard to a reference frame composed of other similar groups of galaxies. We shall accordingly use the phrase "total motion" to describe such motions through various systems of reference, and thus avoid the anathema attending the concept of absolute motion

Relatively to such reference frames, Morsaard's modification of the customary Dopples formula, requires that the total motion of the observer be taken into account. Following Morsaard, we may make the postulate on classical grounds and replace  $e/(e \pm v)$  in the usual formula for the Dopples shift by  $(e - v)/(e \pm v)$ , where v is the velocity of the source relative to the observer in the line of sight, and v the total motion of the observer's system through the modium. This is equivalent to the assumption that our total motion through our reference frame "specks up" our own wave vibrations and standards, so that vibrations from far distant sources at rest, or moving more slowly within this frame at random, would seem to be slower than our own. An observer in a system moving more rapidly than the mean total motion of the other members of the system would than observe an apparent excess of positive velocities. That we happen to be situated in a system of higher velocity than the average may be assumed to be but a happy accident, similar to that by which the universe has not expanded sufficiently to render the beautiful spirals invisible. Like abstration, this effect would apparently not act Im kloinen

The very large scatter of our velocity data on the spirals, together with the limited number of velocities known, proclude any need for rigor in the treatment. Placing X, Y, and Z as the components of such a total motion, the assumed effect of the total motion will then be two-fold

i It will be assumed to act with its full value as expressing the amount by which the observed radial velocity of a distant object tends to appear more positive

2. In addition to the above effect, the component of such a motion in the line of sight will be manifested as the customary Doppers effect.

Then the total effect to be removed from the velocities of distant sources will be

$$X(1 + \cos \alpha \cos \delta) + Y(1 + \sin \alpha \cos \delta) + Z(1 + \sin \delta) = V$$

where Y is the observed radial velocity of the source

The scheme of Morsanan, applied as above, may be regarded as of the nature of a "directed" K-term, placing discrepancies of excess upon our own galaxy, rather than upon ALL other galaxies

The automishing degree of similarity between the Charles theory and data thus far observed has been noted above. Hunason's brilliant work at Mt. Wilson has shown electly the existence of clusters of galaxies, localized as to grouping, and with radial velocities nearly the same.

While such clusters of external galaxies are for the most part very definitely indicated, it is, as yet, considerably more difficult to select with certainty these spirals which may be assumed to be members of our own local cluster of galaxies. It was finally decided to segregate as members of our local cluster all objects with an observed velocity less than 2000 km /sec , while all objects with velocities 2000 km /sec. or greater were assumed to be members of other  $G_0$  systems. This selection may have introduced some error, though approximate tests of the available material in different ways indicated that any over-precise refinement or grouping of the limited data is superfluens. This process, in particular, allocates to our local group the 7 objects assigned by Humason to the Virgo cluster

The proceedure employed in the application of the Morasann formula was then as fol-

1 Using the formula given above, the total motion of our galaxy was first computed with reference to our assumed local reference frame, or G<sub>0</sub>, composed of 56 objects

2. The 34 remaining objects, belonging to well determined clusters of spirals, or "bolated" objects of high velocity, were formed into 13 groups, on the assumption that they represented other  $G_0$  systems in a Charler universe. The affect of the total motion of our own galaxy having been first removed, a second solution was made for the total motion of our local system of galaxies within the reference frame formed by the 13 other  $G_0$  systems. The locations of these are plotted in Figure 58.

The results of the two least square solutions are as follows

1 Total motion of our Galaxy within its local reference frame of 56 Spirals

770 
$$\pm$$
 100 km /sec , toward,  
 $\alpha = 288^{\circ}$ ,  $l = 339^{\circ}$   
 $\delta = -1^{\circ}$ ,  $b = -7^{\circ}$ 

2 Total motion of  $G_2$  cluster of 50 spirits within reference frame of  $A_3$  galactic clusters and isolated spirals of high velocity

$$5670 \pm 1500 \text{ km /sc}$$
 toward  
 $x = 507$   $I = 308$   
 $\delta = -58$   $b = 55$ 

The residual velocities obtained from these two solutions are given in the subjoured table these have been rounded off to tens of kilometers for the first solution, and to hundred s for our local  $G_2$  in  $G_3$  . The column headings in this table are self-explanatory

	1		T	
)((	Ob vel kin sec	Residud within (1	Residud, G in G	Alloration
205	- 300	- 710		Local
221	- 200	600	1	Local
224	- 220	- 640		Local
275		+ 200		
2511	+ 650   1400	- )	į	Local
381	4 500	_ }	600	Pisces Chister
354	- 4 500	<b>→</b> ]	(1.70	2 (20, 2 (112(1)
285	F 4900	-		
404	- 25	610		Local
554	F 1800	1260		Local
598	- 70	- 620		Local
936	+ 1300	580		Local
102ა	₹ 30u	- 420	_	Local
1065	+ 020	+ 150		Local
1270	+ 4800	- 1		TAR
1273	- 58uu	}	- 2800	Persons Cluster
1275	÷ 5200		2 11.17	Tersons cuisiti
1277	5200	noma		
1700	-{ 500	~ 120		Local
2562	+ 5100	}		
2563	- 4800	}	-9100	Cincer Cluster
2681	+ 700	-250		Local
2653	400	- 700	_	Local
2541	+ 600	- 310		l ocal
2859	+ 1500	+ 450		Local
2950	+ 1500	+ 660		Local
3031	- 30	~ 760	İ	Local
3034	- 290	- 130	}	local
3115	<b>∃</b> 600	- 470		l ocal
3193	+ 1300	+ 280	_	Local
3227		+ 140		
2261	$\pm 19600$		9500	Local
3368	+ 940	- 30	1 9300	Leo Cluster
3370	+ 810	- 170	_	Local
3480	GOO	- 330		Tocal Local
3521	÷ 730	- 300	1	_
3610	- 1850	+ 1130		Local
3623	4 800	- 80	-	Local
3627	4- 650	- 230	~	Local
1051	+ 650	- 40		l ocal Local
-	+-11800		-2100	
4111	-  800	+ 110	+2100	Ursa Major Cluster
1151	+ 960	+ 270		local
4192	1 150	+ +10		local
4214	+ 300	- 380	_	local? (Viigo)
		300		Local

(Continued )

		(Continuo	<u>u</u> )	
1	2		3	Allocation
NGC	Olas, vel kut/ser.	Residual within G.	Residual, O. in O.	
4258	- - 500	- 150		Local
4374	F 1050	+ 360		Locul? (Virgo)
4382	+ 5(x)	- 180	_	Local? (Virgo)
1449	2(x)	- 480	-	Local
4472	+ 850	<b> 180</b>	-	Local? (Vingo)
4486	+ HIXI	+ 130	- 1	Local? (Virgo)
4526	· + 580	- 80	~	Local? (Virgo)
4565	-   1 1(X)	+ 460	-	Local
4594	- 1140	+ 540	_	Taxel
4649	+ 1190	i 460	· –	Local? (Virgo)
4736	+ 290	- 300	i - ì	Local
4826	F 150	- 390	-	Local
4853	+ 76(X)	<b>–</b> 1		
4860	+ 79(x)			
4865	+ 5(XX)	_		
4872	6900	!		Coma Berenlees
4874	- - 71XX)	_ }	(200)	Chator
4881	- - 6900	_		Clumbot
4884	+ 67(10)	_		
4895	+ 8500	- 1	1	
L 4045	-l- 6600			
5005	900	F 360		Laxal
5055	- 450	- 80	_ 1	Local
5194	250	- 240		Lucal
5236	- 500	-  50		Local
5457	- - 3(N)	- 130	} _ }	LexenJ
5866	650	- - 330	~-	1,ocnl
6359	3000		- 32(0)	Incolutual
6658	- 4100	-	22(X)	Incluted
6661	39(x)	-	+2000	Incluted
6702	-} 2000		-1900	Incluted
6703	2000	-	-1900	Incoluted
6710	-1 5100			Incluted
6822	- 150	4 90	-	Laxal
6824	⊢ 32(K)	~	1200	Incluted
7217	F 1050	+- 1040		Local
7242	-  50mi	-	F1800	Inolated
7331	- 500	+ 400	1 - 1	Local
7611	- 3400	- )		
7617	J- 3900	~		Thursday Albert
7619	-   3.8cm)	- }	+2200	Pogenus Cluster
7623	- 3 Rux	-		
7626	+ 3700	-		
LMC	+ 280	- 390	_	Leenl
SMC	-1 170	- 310	-	Laxal

The results from both solutions may be regarded as on the whole satisfactory, and perhaps significant. These found for the motion of our own galaxy within its  $G_k$  are in general "reasonable". We know so little as to a possible upper limit to the speed of a cluster of galaxies that the larger residuals found for our  $G_k$  moving in a  $G_k$  system do not seem impossible. The total motion of our own  $G_k$  cluster, as 5700 km/sec, is of the order of the larger residuals in the second solution.

A study of the residuals from the two solutions will indicate that the excess of positive velocities has been almost completely removed. It is unnecessary to reiterate that a slightly different grouping of the objects in the two classes treated, or the acquisition of a number

of velocities of spirals in the regions adjacent to the south galactic pole, would be expected to make significant changes in the magnitudes and directions of the total motions resulting

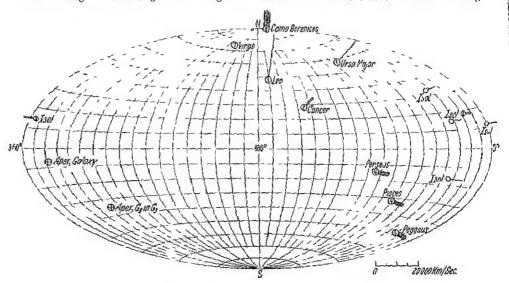


Fig 58 Distribution of Clusters of Galaxie,

from this method of treatment. The data are manifestly too limited in amount and in distribution to warrant any further refinement m the analysis

## Kapitel 7.

# Die Milchstraße.

Von

#### B. LINDBLAD-Stockholm.

Mit 28 Abbildungen und 1 Tafel.

# a) Einleitung.

1. Die Milchstraße als Objekt der Forschung. Das schwach leuchtende, diffuse und komplizierte, aber doch in einem gewissen Sinne sehr regelmäßige Gebilde unseres Nachthimmels, das den Namen Milchstraße (Voie lactée, Milky Way, griech. γαλαξίας, lat. Via lactea) trägt, ist in seiner Gesamtheit, der scheinbaren Ausdehnung nach, das gewaltigste aller Himmelsobjekte. In der Forschung haben wir zuerst die Milchstraße als scheinbares Gebilde, das "Phänomen der Milchstraße", zu betrachten. Es gilt hier, soweit möglich, persönliche Differenzen verschiedener Beobachter auszugleichen und ein mittleres Bild der Milchstraße, wie sie einem normalen menschlichen Auge erscheint, zu geben. Dieses Bild wird durch photometrische Schätzungen und Messungen in systematischer Weise ergänzt. Endlich greift hier auch die Photographie in bedeutungsvoller Weise ein. Doch muß immer daran erinnert werden, daß das visuelle und das photographische Milchstraßenbild in vielen Beziehungen prinzipiell streng zu unterscheiden sind.

Diese Festlegung des scheinbaren Phänomens hat aber nur einen Sinn, wenn sie für eine tiefer gehende Forschung die Grundlage bildet. Die Stellarastronomie sieht in der Milchstraße den Effekt einer Konzentration der Sterne unseres Systems gegen eine Fundamentalebene, die als Milchstraßenebene oder galaktische Ebene bezeichnet wird. Diese Konzentration gegen eine Ebene ist sogar in ihrer offenbaren Gesetzmäßigkeit das unmittelbarste Zeichen dafür, daß wirklich die uns umgebenden Sterne in ein gewaltiges System eingeordnet sind. In der Stellarastronomie wird das Wort Milchstraße bisweilen als ein Synonym für das Sternsystem verwendet. Es wird schließlich eine Aufgabe der Astronomie, die Erscheinung der Milchstraße in ihrer stellarastronomischen Bedeutung dynamisch zu erklären, welche Aufgabe es bedingt, eine statistische Mechanik des Sternsystems zu entwickeln. Die Methoden einer solchen statistischen Mechanik haben mehrere Berührungspunkte mit den statistisch-mechanischen Methoden der allgemeinen theoretischen Physik, wenn auch keineswegs die Theorien der kontinuierlichen Medien, der Gase und Flüssigkeiten, unmittelbar auf das Sternsystem angewandt werden können.

2. Übersichtliche Darstellungen und Monographien. Von Übersichtswerken über die Ergebnisse und Methoden der Milchstraßenforschung sollen hier nur einige erwähnt werden, welche, ohne neues Primärmaterial zu geben, durch selbständige zusammenfassende Gesichtspunkte gekennzeichnet sind. Unter

den alteren Werken dieser Art sind zu nennen F. G. W. Struye, Etudes d'Astronomic stellane<sup>1</sup>, J. Hirschill, Outlines of Astronomy<sup>2</sup>, H. J. Killin, Der Paxsteinhimmel usw<sup>3</sup>, R A Proctor, The Universe and the Coming Transits<sup>1</sup> Einer spateren Zeit gehoren z B. die Übersichtswerke von Miss CIEKKL, und 5 NI WCOMB<sup>6</sup> an 1 RISH NPARI gibt unter dem Wort "Universum" in VALIN-Handbuch<sup>7</sup> eine eingehende Bespiechung der damaligen Resultate der Milchstraßenbeobachtungen und der Stellarstatistik. Etwas spater erschemt H Kobold, Dei Bau des Einsteinsystems\* Aus der Zeit der zwei letzten Jahrzehnte sind besonders zu erwähnen A.S. Eppington, Stellar Moyements and the Structure of the Universes, and H KOBOLD, Das Sternsystem in und Stellarastronomie 11 K Graff gibt in R Henselings "Astronomisches Handbuch, herausgegeben vom Bund der Sternfreunde"12, eine Darstellung der Resultate der visuellen und photometrischen Milchstraßenbeobachtungen. I. Prassmann<sup>13</sup> hat eine sehr verdienstvolle Monographie, "Die Milchstraße" herausgegeben, die auch emen Zusatz von J. Hagin über "Die Nebelstraße" enthalt. A. Kopit gibt in MULLI R-POULLELS Tehrbuch der Physik 11 eine inhaltreiche Übersicht über den Bau des Steinsystems nach den modernen Untersuchungen. Eine zusammentassende Daistellung über den Bau des Kosmos ist von W Bernhilmir im Handbuch der Physik 15 gegeben worden

## b) Das visuelle Milchstraßenbild.

3 Die Beschreibung und zeichnerische Darstellung der Milchstraße Die Milchstraße ist schon für eine flüchtige Beobachtung ein auffalliges Phanomen des gestinnten Himmels und ist doch nicht leicht durch wissenschaftliche Vermessung quantitativ zu eifassen und daizustellen. Selbst eine genaue qualitative Beschieibung der Milchstraßenstruktur in ihren Einzelheiten und eine detaillierte zeichnerische Daistellung derselben ist erst in der Mitte des vorigen Jahrhunderts ernstlich angefangen worden. Hindernisse der exakten Beobachtung sind die mit dei Hohe über dem Horizont wechselnde atmospharische Absorption und auch allerler Trubungen durch fremdes Licht, die den Eindruck des schwach leuchtenden Gebildes verfalschen konnen. Zu bemerken ist, daß die Milchstraße nur in geringem Kontrast gegen das allgemeine schwache Himmelslicht leitchtet Die Schwierigkeiten sind naturlich mit der komplizierten Natur des Phanomens verbunden, mit der santten und doch in einem Gewebe unendlich reicher Struktur voi sich gehenden Abstufung dei Lichtstarke von den verhaltnismaßig hellen Wolken bis zu den kaum wahrnehmbaren femen Lichtschleiern, die dunklere Partien umgeben oder allmählich in den dunklen Himmelsgrund der außergalaktischen Regionen übergehen

Die Schwietigkeiten, ein einheitliches Bild des ganzen Milchstraßengurtels zu schaffen, sind weiterhin eine Folge dei Ausdehnung des Phanomens langs eines großten Kreises des Himmels, der um etwa 60 Grad gegen den Aquator geneigt erscheint. Nur in den Tropen kommt die ganze Milchstraße wahrend

<sup>1</sup> St -Petersbourg Imprim de l'Acad Impér des Sc (1847)

<sup>3</sup> Jondon Longman, Brown etc (1849, mit spateren Auflagen)

Jondon Longman,

Jondon Longman,

London Longmans, Green, and Co (1874)

London Longman, Green, and Co (1874)

London Longman, Green, and Co (1874)

London Longman, Green, and Co (1874)

London Longmans, Green, an

Kultur der Gegenwart III (Astronomie)
 S 511 Leipzig und Berlin Teubner (1912)
 Encyklopädie der math Wiss VI 2 B, Heft 2 Leipzig Leubner (1926)

 <sup>12</sup> S 183 Stuttgart Franckische Verl (1921)
 13 Probleme der Kosmischen Physik IV Hamburg Grund (1924) 11 11 Aufl , V, 2 Halfte, 5 429 (1928) 16 IV, S 577 (1929)

eines Jahreslaufs über den nächtlichen Horizont. Die gegenwärtig in den Einzelheiten genauesten Darstellungen des visuellen Milchstraßenbildes sind hauptstichlich über den nördlichen Teil der Milchstraße ausgedelint, während zur Zeit der Vollendung der Uranometria Argentina der südliche Teil der Milchstraße der durch gute Darstellung begünstigte war

Aus dem Altertum sind zwei Beschreibungen der Milchstraße aufbewahrt worden, von Aristorki est und von Prolemaus. Die letztere ist ziemlich eingehend und ist wahrscheinlich erst im 19 Jahrhundert übertroffen worden I'me deutsche Übertragung des Almagest mit der heutigen Sternbenennung gibt K MANITIUS Profestages Milchstraßenbeschreibung ist von Eastons nach Hal MAS Übersetzung mit Erklärungen wiedergegeben worden. Ein Bruchstück in freier Übersetzung mit Bemerkungen hat Pannekork in seinem unten besprochenen Werke "Die stidliche Milchstratte" gegeben. Eine nur wonig in Einzelheiten gehende Beschreibung der Milchstraße hat Thomas Wright in seinem seltenen Werke "Theory of the Universe" (London 1750) geliefert Die Sternkarten des 17 und des 18 Jahrhunderts behandeln die Milchstraße nur sehr dürftig Noch auf Books Karten ist nur eine schematische Milchstratienkontur grob gezogen worden J K HORNER hat als erster nebst einer Milchstraßenbeschreibung eine elementare Photometrie der Magkllanschen Wolken und hellerer Partien der südlichen Milchstraße mit Hilfe von farbigen Glüsern verschiedener Dicke versucht W Herschfif gibt ein kurzes Verzeichnis von hellen und dunklen Partien der Milchstraße zwischen Sagdttarius und Perseus, Emige Fortschritte in bildlicher Darstellung sind wohl in den Karten von W H WOILASTON'S, J W. LUBBOCK's und J DUNLOP'S zu registrioren

F W A ARGRIANDER fordert in Schunachers Jahrbuch, 1844, die Freunde der Astronomie zu Beobachtungen der Milchstraße auf In den 40er Jahren erschemt ] Herschels<sup>11</sup> verdienstvolle Zeichnung der südlichen Milchstraße mit eingehender Beschreibung. A v Humboldt gibt im dritten Bande des "Kosmos" hauptsächlich nach den Arbeiten von J HERSCHET eine Beschreibung des Zuges der Milchstraße unter den Sternen

Ein Bruchstück einer detailheiten wörtlichen Beschreibung wurde im Jahre 1867 von H J KIFIN in HRIS' "Wochenschrift für Astronomie" veröffentlicht, und emige Jahre später gab endlich E. Hrisis seine Zeichnungen der Milchstraße hernus. Sie gehen stidlich bis zur Deklination -35° HRIS unterscheidet fünf Lichtstufen, die als Schattierungen verschiedener Tiefe in den Zeichnungen wiedergegeben und Some Darstellung steht daher mit den isophotischen Karten späterer Beobachter in Verwandtschaft. Die felneren Einzelheiten werden in dieser Weise nicht berücksichtigt, sondern in Lichtflecken einfacherer Kontur ausgeziehen. Die medrigste Stufe bei Heis entspricht dem schwachen Schimmer, in den die Milchstraße einem Beobachter mit scharfen Augen unter guten atmosphärischen Verhältnissen eingehüllt erscheint

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Almagest, Lib VIII, Cap. 2
<sup>1</sup> Metourologica, Lib I, Cap 8
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Loipsig Tenhner (1912) La voie lactée dans l'hémisphère boréal Paris Gauthier Villars (1893) Uranographia sive astrorum descriptio Berlin (1801)

Monatilche Correspondenz 10, S 220 (1804)

Phil Trans 1817, S. 302, Coll Scient Papers II, S 586.

A Portraiture of the Heavens as they appear to the Naked Lye London (1811)

The Stars in six Maps, etc. London (1830, mit spateren Aufl.)

<sup>19</sup> Phil Trans 1828, S 152 11 Results of Astronomical Observations, etc., p 383 London Smith, Elder (1847); Beschreibung auch in Outlines of Astronomy (5 Edition, S 527)

<sup>18</sup> Atlas cocleatis novus Köln (1872)

Die sudliche Milchstraße wurde in der großartigen Uranometria Argentina von B A Gould nach Zeichnungen von W M Davis und J M I nom in genauer Weise wiedergegeben. Die Art der Reproduktion der Zeichnungen war eine photolithographische, die Wiedergabe der Einzelheiten ist weniger durch vereinfachende Ausgleichung gebunden als in den Karten von III is



Durch die Arbeiten von Heis und Gould was somit eine eingehende und wissenschaftlich einigermaßen brauchbare Darstellung des ganzen Milchstraßengurtels geschaffen worden. Die bisweilen erheblichen Unterschiede der zwei Bilder in den gemeinsamen Teilen lassen jedoch die Subjektivität der Auffassung selbst in den zeichnerischen Arbeiten hochster Klasse deutlich erkennen

Resultados del Observatorio Nacional Argentino I (1879) Mit Atlas

Inzwischen war eine Reproduktion der ganzen Milchstraße erschienen, die war eine noch schematischere Darstellung als die Hrissche bot, aber auf eine neue methodische Schützung der Lichtstufen gegründet war Dieses Werk ist in der "Uranométrio générale" von J C Houziau1 enthalten Die Beobachtungen wurden auf Jamaika angestellt Houzkau hat einen Versuch gemacht, die Linien konstanter Lichtstürke, die Isophoten, zu zeichnen Er ordnet die Helligkeiten verschiedener Partien in eine Skala von Größenklassen, die eine Art Anschluß an die Größenskala der Sterne dadurch gewinnt, daß man das Hervortreten oder Verschwinden der Lichtflecken in der Däminerung oder in der Himmelsbeleuchtung durch den Mond zur salben Zeit wie das Hervortreten oder Verschwinden benachbarter Sterne einer gewissen Größe beobachtet Houzhau gibt in omer Tabelle die Intensitäten für 33 Punkte maximaler Holligkeit Um diese Maxima sind die isophotischen Linien in menilich schomatischer Weise gozeichnet, oftmals als regelmäßig abgerundete Ovale Durch diese schematische Regelmanigkeit steht Houzeaus Darstellung in einer Sonderklasse unter den visuellen Milchstrußenbildern Die größten Intensitäten (Größen 4,5 und 5) notiert Houzeau für die Gegenden, die in Tabelle i zusammengestellt sind (Koordinaton für Aqu 1880)

In schärfstem Gegensatz zu Houzkaus Methode steht die Art der Milchstraßendarstellung, die von O BORDDICKER zu Birr Castle in Irland praktiziert wurde Die Milchstraße ist hier in eine komplizierte Struktur von felnon Stromungen mit oftmals ziem-

Taballa 4

	100	UIIO 1		
A.R	A.R DekL		Sternbild	
16 <sup>h</sup> 4 <sup>m</sup> 17 46 18 0 18 8 18 23 18 41 21 2	- 54°,3 - 34 ,7 - 28 ,5 - 18 ,7 - 14 ,4 - 7 ,0 + 45 ,5	5 5 4,5 5 4,5 5	Norma Scorplus (M7) <sup>a</sup> Sagittarius Sagittarius Scutum Scutum Cygnus	

lich scharfon Begronzungen aufgelöst. Die Subiektivität dieser schönen und technisch vollendeten Darstellung ist offenbar PANNEKOEK, der die Gelegenheit hatte, die Originalzeichnungen zu untersuchen und zu benutzen, macht jedoch die Bemerkung, daß diese Bilder viel mehr als die Reproduktionen sich dem wirklichen Anblick der Milchstraße nähern, und daß also der Ilthographische Prozeß, trotz größter Sorgfalt, viele schwache Nuancen modifiziert hat Eine Beschreibung seiner Arbeitsmethode hat BORDDICKER selbst in einer Notize gegeben

Unter den Zeichnungen dieser Zeit ist auch eine Chromolithographie von L. TROUVELOT von der Milchstraße zwischen Casslopeia und Scorpius zu nennen Die Originale besinden sich nach Easten in Meuden

Zu den schönsten Zeichnungen der Milchstraße gehören wohl die von Julius SCHMIDT, die in den Jahren 1864-1867 zu Athen hergestellt worden sind und die erst kürzlich in phototypischer Reproduktion von der Sternwarte zu Leiden\* publiziert wurden. Die Zeichnungen erstrecken sich im Süden bis zur Deklination -45° Besonders die südlichen Partien, von Scorpius bis Aquila, sind mit orstaunlicher Fülle von Einzelheiten mit größter Sorgfalt ausgearbeitet worden

<sup>&</sup>lt;sup>1</sup> Anuales de l'Observatoire de Bruxelles, N S , I (1878)

The Milky Way from the North Pole to 10° South Declination I onden (1892)
Die Größe der Gegend um M7 ist in Houzzaus Tabelle als 4, auf der Karte aber als 5 bezalahnet Die letztere Zahl ist von Baston (l c) aufgenommen worden

MN 50, S 12 (1889)
The Trouvelot Astronomical Drawings New York Scribner (1882) Annalen van de Sterrewacht to Leiden XIV. Tweede Stuk (1923)

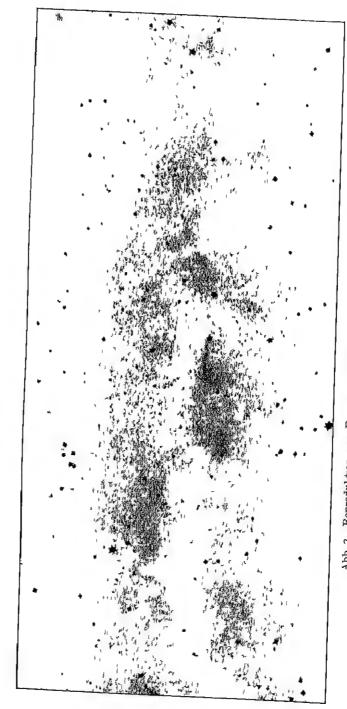
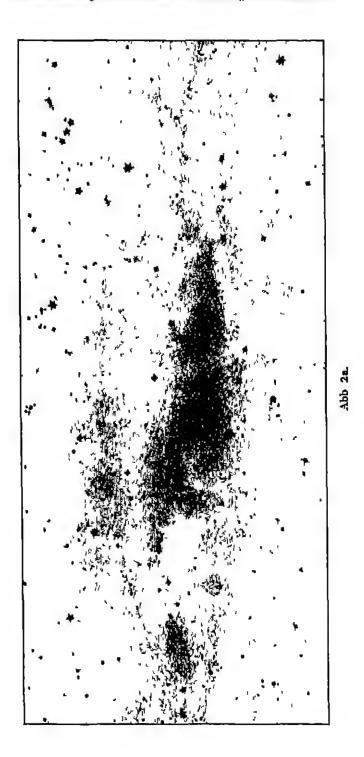


Abb 2 Reproduktion von Eastons "carte generale der nordlichen Milchstraße



Nach J Hopmann<sup>1</sup> befindet sich auf der Bonner Steinwarte im Manuskript eine Reihe von Schmidts Milchstraßenbeobachtungen, Beschreibungen und Helligkeitsschatzungen, beginnend 1859 in Athen, die nur teilweise in direktem Zusammenhang mit seiner Karte stehen

Die Milchstraße nordlich der Deklination -10° ist in sehr eingehender Weise von den zwei holkindischen Astionomen, C. Easton und A. Pannlkoik, behandelt worden Easrons vorher erwahnte, 1893 erschienene Arbeit, "La voie lactée dans l'hemisphere boréal", bildet einen sehr merklichen Fortschritt in der bildlichen Darstellung der Milchstraße. Easton hat seine Karten ganz unabhangig von anderen Daistellungen gezeichnet. Die Reproduktion ist auf lithographischem Wege ausgeführt worden, wobei der Zeichner selbst die zur Vorbereitung notige Kopierarbeit sowie eine Retusche der gedruckten Karten ausgeführt hat Easton befont besonders die großen Schwierigkeiten, durch Zeichnung ein exaktes Bild dei Milchstraße, wie sie dem Auge erscheint, wieder-Das Milchstraßenlicht ist so schwach und die Helligkeitsdifferenzen der verschiedenen Partien sind so sanft akzentuiert, daß die Wiedergabe immet em weng ubertrieben werden muß Easton gibt eine Hauptkarte (carte genérale), welche die Gradation des Milchstraßenlichts und die relative Helligkeit der Milchstiaßenpartien wiedergeben soll, wahrend dier "cartes explicatives" in etwas femere Emzelheiten gehen. Die Hauptkarte, welche ein bemerkenswertes, vorzugliches Stuck Arbeit ist, wird hier in Abb 2 ieproduziert. Der Text enthalt eine aussuhiliche geschichtliche Übersicht über das Problem der Milchstraßenbeschierbung Zuletzt gibt Easton hier eine eigene, sehr eingehende Beschreibung der nordlichen Milchstraße nebst einem Katalog, der die Randkoordinaten von 164 hellen Flecken und Stromungen und von 47 dunklen Partien enthalt. In einer spateren Arbeit? hat Easton auch eine Karte mit isophotischen Linien gegeben

PANNLKOLK scheint der eiste zu sein, der die Mahnung Argi landers in semer "Aufforderung", eine feste Skala relativer Helligkerten durch wiederholte Vergleichungen verschiedener Leile der Milchstraßenstruktur auszubilden, beherzigt hat In seinem Werke' "Die nordliche Milchstraße" gibt er die Resultate seiner umfangreichen Helligkeitsschatzungen. Die Helligkeiten wurden zuerst in einer willkurlichen Skala ausgedruckt, nachher wurde eine Zahl von Normalstellen ausgesucht, diese wiederholt aneinander angeschlossen und damit alle anderen zu beobachtenden Stellen verglichen. Die relativen Helligkeiten wurden nach der Stufenmethode Argelanders geschätzt, und die Ausgleichung für die Normalstellen in einer zusammenhangenden Skala mit der Stufe als Einheit geschah auf dem Wege wiederholter Annaherung. In dieser Skala wurden die Helligkeiten von 128 Stellen der Milchstraße ausgedruckt. Der Stufenweit wurde zunächst unter Benutzung der atmosphauschen Absorption durch Vergleichung hellei Flecken, wenn sie in geringer Hohe stehen, mit hochliegenden Stellen der Milchstraße und auch nach Houzeaus Methode aus Beobachtungen in der Dammerung bestimmt. Eine bessere Bestimmung ergab sich spater i aus einer Vergleichung mit den Helligkeitsmessungen von VAN RHIJN (Ziff 5) Der Stufenwert der Gesamthelligkeit des Himmelsgrundes ("Erdlicht" in weiterem Sinne + Milchstraßenlicht) eigibt sich hier zu 0,11 Gioßenklassen, was abei, wenn das "Eidlicht" eliminiert wird, im Mittel für das Milchstraßenlicht 0.3 Großenklassen bedeutet

<sup>1</sup> V J S 64, S 320 (1929)

<sup>&</sup>lt;sup>2</sup> Verh der K Akademie van Wetenschappen, Amsterdam, VIII, Nr 3 (1903)

Annalen van de Steirewacht te Leiden XI Derde Stuk (1920)
 AN 214, S 389 (1921)

Pannekoek gibt seine Resultate teils in einer sehr ausführlichen wörtlichen Beschreibung der Einzelheiten, teils als Zeichnungen, die auf den zahlenmäßigen Resultaten füßen und durch ein photographisches Roproduktionsversahren vervielfältigt wurden, teils endlich als Karten mit isophotischen Linien, die direkt die Zahlenergebnisse zum Ausdruck bringen. Weiter folgen der sehl eingehenden Beschreibung der nördlichen Milchstraßenstruktur ausführliche Vergleichungen mit anderen Darstellungen (Easton, Schnidt, Boeddicker, Klein, Backhouse<sup>1</sup>, Uranometria Argentina). Schließlich werden die Isophotendarstellungen von Pannekoek und von Easton mit den Zeichnungen von Schnidt und von Boeddicker in ein "mittleres Milchstraßenbild" von zuhlenmäßiger Form zusammengefäßt, das auch in Isophotenkarten wiedergegeben wird. Der mittlere Stufenwert wird für die Eckpunkte und für das Zentrum jedes Quadratgrades des galaktischen Gürtels gegeben. Dieses Zahlensystem sollte als "das beste Gesamtresultat zu betrachten sein, das sich aus den bisherigen Arbeiten über die Milchstraße ableiten läßt"

Ganz kürzlich hat Pannekoeks nach demselben Plan seine Arbeit auch über die südliche Milchstraße ausgedehnt. Die Beobachtungen wurden gelegentlich einer Expedition, die von der K Akademie der Wissenschaften in Amsterdam zur Beobachtung der am 14. Januar 1926 stattfindenden totalen Sonnenfinsternis nach Indien geschickt wurde, ausgeführt, und zwar sowohl auf der Bosscha-Sternwarte in Lembang auf Java, als auf dem Dampfer während der Reise. Die Witterungsverhältnisse waren durchgehend ziemlich ungünstig. Nichtsdestoweniger ist es dem unermüdlichen Astronomen gelungen, sein Programm durchzuführen und die südliche Milchstraße in ihren Einzelheiten auf photometrischer Grundlage darzustellen

Eine Anzahl Normalpunkte wurde ausgewühlt und durch wiederholte Vergleichungen untereinander in eine "stidliche Skala" eingeordnet, welche sowohl an der Aquilaseite als an der Monoceresseite nut der nördlichen verglichen und auf diese reduziert werden konnte Die Helligkeiten anderer Punkte wurden mit Hilfe der Normalstellen geschätzt Pannekork gibt einen Katalog über die Beobachtungsresultate für 189 Stellen der südlichen Milchstraße.

Wie für die nördliche Partie der Milchstraße hat PANNEKOEK auch in dieser Arbeit auf Grund seiner Resultate Zeichnungen und Isophotenkarten ausgearbeitet und gibt auch eine in die feinsten Einzelheiten gehende wörtliche Beschreibung, der er die Beschreibungen von PTOLEMÄUS und von J HERSCHEL folgen läßt

Der große Reichtum der südlichen Milchstraße wird besonders von Pannikkoek hervorgeholen;

"Wer nur die Teile des Sternhinmels kennt, die in den mittleren Breiten Europas sichtbar sind, kann sich keine Vorstellung von der wundervollen Schönheit der südlichen Milchstraße machen Gewiß gehört eine dunkle Augustnacht in Europa mit den großen hellen Lichtwolken im Schwan und dem anschließenden buchtigen Fleckenband im Adler und in der Cassiopela zu den schönsten Natureindrücken in unserem Welttell. Aber die Pracht des Südhimmels ist doch ganz anderer Ordnung, man möchte ihre höhere Potenz nach einer unrichtigen, aber verständlichen Gedankenassoziation mit dem üppigen Reichtum aller Tropennatur in Zusammenhang bringen Es ist zuerst die viel größere Holligkeit, die die Milchstraße in librer südlichen Hälfte erreicht. Ihr Licht wächst von dem schwachen, einförmigen Schimmer des Januarhimmels bei Orien und Sirius allmählich an und erreicht in Carina, in 250° Länge, eine Helligkeit, die schon

<sup>&</sup>lt;sup>1</sup> The Structure of the Universe Publ of West-Henden House Observatory I, II
<sup>8</sup> "Die sudliche Milchstraße", Annalen v d Bosscha-Sterrowacht Lombung (Java)
II, 1ste Gedeelte (1929)

die hellsten Stellen am Nordhimmel übertrifft. Hier wirken die Anhaufung der schonsten Steine und Steinbilder, die dichtgestieuten Gruppen im Schiff, das Sudliche Kreuz und die hellen Centaurussteine mit den unregelmaßigen Buchten der schaff begrenzten Lichtpartien des Milchstraßenbandes zusammen, um ein



eindrucksvolles Ganzes zu schaffen Etwas weiter fangt eine reichgegliederte Reihe von Stromen und Wolken an, die stets heller werden, bis sie in dem Schutzen einen Hohepunkt erreichen, von dieser Reihe erblicken wir in Europa noch das letzte Glied in dem Lichtfleck im Schild Dei Glanz dieser hellen Schutzenflecken

PANNEKOEKS Isophotenkarte für die südliche Milchstraße zwischen den galaktischen

Abb

tibertrifft weitaus alle anderen Gebilde der Milchstraße, die Eigentümlichkeit des Eindrucks wird noch gesteigert durch die Armut dieser Gegenden an für das bloße Auge sichtbaren Sternen Bei jedem Vergleich fällt der Gegensatz auf, wie die Milchstruße im Schwan und in Lacerta mit szintilherendem Sternstaub dieht besät ist, wührend die hellen Schützenwolken wie mit ruhiger Leuchtfarbe auf einen sternenleeren Himmelsgrund gemalt erscheinen"

Als ein Beispiel der Pannekoekschen Milchstrißendarstellung wird in Abb 3 die Isophotenkarte der kontrastreichen Carina-Crux-Centaurus-Region des Südhimmels wiedergegoben

4. Photometrische Eichung der Isophoten Eine wichtige Erganzung zu dem rein visuellen Milchstraßenbild, wie es nach den Beobachtungen mit bloßem Auge erschemt, hegt in den Resultaten photometrischer Messungen des Milchstraßenlichts In dem Universalphotometer von K GRAFF1 wird ein Bild der beobachteten Himmelsgegend durch ein kleines Mikroskopobjektiv in der Kontaktfläche eines Lummer-Brodhunschen Priamas erzeugt. Von der Seite her wird das Bild einer beleuchteten Milchglasscholbe nach dem Okular zu total roflektiert, so daß man den eingestellten Teil des Himmels als einen runden Fleck inmitten eines gleichmäßig erhollten Feldes sicht, das durch einen Photometerkeil vor der Milchglasscheibe auf die Lichtstärke des Fleckes abgeschwächt wird Als Anschlußheiligkeit für Graffs Messungen diente der Hintergrund in Ursa minor bei R A, 0h 0m und Dekl +85°, dem willkürlich die Größe 2m,0 beigelegt wurde. Als zweiter Anhaltspunkt diente die Cygnuswolke zwischen y und & Cygni, für die der Wert 1m,30 photometrisch erhalten wurde Graffs Beobachtungen verteilen sich auf 32 Stellen des Himinels, in Verbindung mit Stufenschätzungen wurden 47 Punkte der nördlichen Milchstraße von Sagittarius bis Canis major in ihrer relativen Helligkeit photometrisch festgelegt

J. Hopmann<sup>a</sup> hat als eine Nebenaufgabe bei der Sonnenfinsternisexpedition 1922 nach Christmas Island mit Anschluß an Grapps Messungen übnliche Beobachtungen für einige Punkte der südlichen Milchstruße ausgeführt und auch eine Menge Stufenschützungen relativer Intensitäten in dieser Gegend gemacht Unter Benutzung der Pannkkorkschen Isophoton der nördlichen Milchstraße und Zuhilfenahme von Goulds Darstellung der südlichen Milchstraße in der Uranometria Argentina zur Ergänzung sonner Stufenschützungen hat Hopmann dann eine Isophotonkarte der gunzen Milchstraße konstruiert Für Pannkkorks Stufenwert findet Hopmann aus Graffs Messungen 0<sup>m</sup>,138, für seinen eigenen findet er 0<sup>m</sup>,0996. Es sollte hervorgehoben werden, daß die Stufenmethode erheblich genauer ist als die photometrischen Messungen, deren w. F einer Beobachtung etwa 0<sup>m</sup>,1 beträgt Die im Photometer gemessene Fläche ist auch größer als die mit dem Auge vorglichenen Gebiete. Der Vorteil des Photometers besteht also wesentlich in der Einführung einer unpersönlichen Skala.

PANNEKOER® hat der Hopmannschen Darstellung einige kritische Beinerkungen gewidmet. Es scheint sehr möglich, daß infolge unzulänglicher Verbindung der zwei Hälften der südlichen Milchstraße, Centaurus- und Curinaseite, in den Stufenschätzungen Hopmanns die Gegend um 6h R A (Monocaros) zu schwach, verglichen init der Gegend um 18h (Sagittarius), ausgefallen ist Pannekoer hebt auch hervor, daß infolge variablen "Erdlichts" das Helligkeitsverhältnis zwischen Normalstelle und Milchstraßengegend veränderlich sein muß, und daß

<sup>&</sup>lt;sup>1</sup> Abhandl. der Hamburger Sternw zu Bergedorf II, Nr 5 (1920)

<sup>\*</sup> AN 219, S 189 (1923)

BAN 3, S 44 (1925), Die südliche Milchstraße (1929)

die Graftsche Methode daher kaum geeignet ist, eine ganz zuverlassige absolute Skala zu geben. In einer eingehenden Rezension der Pannekolkschen Werke über die Milchstraßenstruktin macht Hopmann<sup>1</sup> auch einige Bemerkungen zu Pannekolks Kritik. Es ware noch zu früh, mit Sicherheit über das wahre Intensitätsverhaltnis zwischen den zwei Milchstraßengebieten zu urteilen. Es scheint, als ob man vielleicht bei Pannekolk mit einer kleinen Variation der Stufe zwischen Nord- und Sudhimmel zu rechnen hat (vgl. Ziff. 5)

5 Die absolute Helligkeit des Himmelsgrundes. Zur Einsttlung der wahren Intensitätsveiteilung des Milchstraßenlichts oder des allgemeinen Sternenlichts aus den Resultaten der photometrischen Stufenschätzungen und Messungen ist es notwendig, die beobachteten Helligkeiten von dem Einfluß der allgemeinen zerstreuten Strahlung des Himmels, die als "Erdlicht" im weiteren Sinne bezeichnet werden kann, zu befreien Diese Strahlung ruhrt großenteils von Nordlichtern und vom Zodiakallicht her Die Scheidung der zwei Strahlungsarten, Steinlicht und "Erdlicht", ist daduich möglich, daß die Steinstrahlung für höhe galaktische Breiten aus den Steinzahlen mit genugender Approximation berechnet werden kann

Nach Pionierarbeiten von S Newcomb<sup>2</sup>, C J Burns<sup>3</sup>, S D Townley<sup>4</sup> und J C Kapteyn<sup>5</sup> haben besonders L Yntema<sup>6</sup> und P J van Rhijn<sup>7</sup> das Problem sehr eingehend behandelt. Das benutzte Flachenphotometer besteht im Prinzip aus einer kleinen beleuchteten Scheibe, die gegen den Himmel gerichtet wird, und deren Helligkeit durch Anderung der Beleuchtung in meßbarer Weise gleich der Helligkeit des Himmels an der betrachteten Stelle gemacht werden kann van Rhijn findet aus seinen auf Mount Wilson angestellten Beobachtungen die totale Helligkeit der direkten Steinstrahlung aquivalent mit 1440 Steinen der Große 1<sup>m</sup>,0, was in guter Übereinstimmung mit Yntemas Resultat, 1350 Steinen derselben Große, ist. Die beobachtete Steinstrahlung für miedere galaktische Breiten begt zwischen den aus den Steinzahlen in den Groninger Publikationen Ni. 18 und 27 berechneten Werten, ist aber in besserer Übereinstimmung mit den letzteren Daten

van Rhijn gibt für den mittleren Anteil der verschiedenen Strahlungsarten im der direkt gemessenen nachtlichen Strahlung folgende Weite. Die Einheit der Helligkeit ist ein Stein von der Große 1,0 im Harvardsystem per Quadratgrad. Die Steingroße 1,0 entspricht 0,94 10<sup>-6</sup> Meterkerzen (Hefner)<sup>8</sup> Die benutzte Einheit der Flächenhelligkeit des Himmelsgrundes entspricht daher etwa 0,78 10<sup>-6</sup> der Flächenhelligkeit des Vollmondes

Zodiakallicht	0,071
Ducktes Sternenhoht	0,020
Amora borealis	0.024
Gestientes Erdlicht	0,032
Gestreutes Stanenlicht	0,009

C Hoffmlister macht jedoch wahrscheinlich, daß van Rhijn den Anteil des Zodiakallichts zu hoch geschatzt hat Er findet überhaupt einen viel kleineren Betrag für das "Erdlicht", nur etwa ein Funftel von Yntemas und van Rhijns Wert

<sup>&</sup>lt;sup>1</sup> V J S 64, S 327 (1929) <sup>2</sup> Ap J 14, S 297 (1901) <sup>8</sup> Ap J 10 S 166 (1902) <sup>1</sup> Publ A S P 15 S 13 (1903) <sup>8</sup> Plan of Selected Arcas, S 11 (1906)

Publ Astron Lab Groningen Nr 22 (1909)
 Publ Astron Lab Groningen Nr 31 (1921)
 Val Astron Lab Groningen Nr 31 (1921)

Vgl Russett, Ap J 43, S 128 (1916)
 Veroff d Sternw Berlin-Babelsb 8, H 2 (1930)

VAN RHIJNA Resultate wurden von Pannekoek zur Ermittlung seines Stufenwerts benutzt (Zilf 3) In ühnlicher Weise hat Hopmann¹ seine scheinbaren Flüchenheiligkeiten der Milchstraße durch eine summarische Korrektion in wahre Intensitüten vorwandelt Das Resultat, die mittlere Intensität, pro Quadrutgrad gerechnet, für aukzessive Areale in dem galaktischen Koordinatennetze (galaktische Lünge und Breite), wird hier in Tabelle 2 wiedergegeben.

Tabelle 2 Die mittlere Verteilung des galaktischen Lichts nach Hopmann,

ì B	0" - 2	5° — 1	,	5" +!	5° +1	5° +2	5* +30*
O°	37™	404	62 <sup>R</sup>	55*	498	40 <sup>ss</sup>	36■
10	36	43	71	56	51	37	36
20	36	40	76	53	49	36	36
30	36	41	74	100	56	36	36
40	36	46	62	77	51	36	36
50	36	45	65	63	56	36	36
60	36	46	74	60	46	36	36
70	36	48	73	63	45	36	36
HO	36	45	62	62	46	36	36
90	36	45	57	49	42	36	36
100	36	45	51	51	39	36	36
110	36	41	49	46	46	36	36
120	26	43	49	45	43	36	36
130	1 00	49	46	54	47	37	36
140		45	47	59	51	39	36
150	36		53	63	51	45	36
160	36	49	51	62	51	45	36
170		1 49	51	65	56	45	36
1 HO		43	56	68	68	45	36
190	36		44	68	58	44	36
2(H)	36	42	57	83	60	48	36
210	36		57	79	66	48	37
220	36	46	71	79	73	51	40
230	36	42	64	73	66	51	39
240	36	37	57	80	61	48	36
250	36	36	50	89	62	41	36
260	36	36	44	95	51	39	36
270	36	39	94	116	90	42	36
280	36	45	106	117	105	49	36
200	36	53	108	117	116	57	39
3(8)	36	57	104	118	113	73	46
310	36	56	109	109	126	89	51
320	36	56	133	125	136	83	46
330	36	53	83	123	95	60	36
340	39	53	76	99	54	36	36
350	40	54	83	76	46	37	36
360	40)	3.4	0.7	10			

Die Einheit der Helligkeit ist so gewählt worden, daß ein Stern von der Größe 1,00 im visuellen Harvardsystem gleich 1000 gesetzt wird. Es ist klar, daß die Resultate nicht als endgültig angesehen werden können, sondern einer sorgfältigen, Prüfung durch wiederholte Messungen und Vergleichungen verschiedener Teile der Milchstraße unterworfen werden müssen. Sehr auffallend ist die relativ große Intensität des Milchstraßenlichts im Intervalle L 270°—360°, die jedoch nach Pannekoik (Ziff 4) etwas übertrieben sein kann. Hopmann gibt in einer Pigur einen Vergleich der Vorteilung des Milchstraßenlichts nach galaktischer Länge mit den in analoger Weise behandelten Sternzahlen für die Grenzgrößen 8-,25 und 11m,0 (vgl. Ziff 16). Die Maxima der Sternzahlen sind in galak-

LAN 222, S 81 (1924)

tischer Lange betrachtlich gegen die Richtung zur Sagittariusregion, wo das Milchstraßenlicht sein Maximum hat, gedicht

In C Hoffmeisters obenerwahnter Arbeit wurden auch die Pannikorkschen Normalstellen der Milchstraße mit dem Flachenphotometer, dessen Konstruktion im Prinzip mit dem von Yntema und van Rinjn benutzten analog ist, ausgemessen Labelle 3 gibt die Normalstellen mit den von Hoffmeister angenommenen Koordinaten. Die Tabelle enthalt die Stufenschatzungen von Pannekork und Hoffmann und weiter die gemessenen, auf das Zenith reduzierten

- 1	1	be:	Н	e	7

				t thene 3						
Stelle	a	δ	Sternbild	L	Punn	Норч	J,		$J_{ m abs}$	(ardße
ψ	121°	- 32	Риррія	219.5	3,1	1	0,321	0,042	0,316	3m,71
-	105	-16		195 .5		-	279		,26‡	3 ,91
$\gamma$	107	- 4	Monoccios	186,3	28	1.7	,313	,032	,306	3 ,75
2"	109	15	Canis major	197,0	2.7	3.7	300	,021	290	3 ,80
v	100	- 5	Monoccios	183 ,8	1,8		,219	,002	,189	4 ,20
$J_{c}$	117	-31	Puppis	217,6	1 1		,259	,053	,239	10, 3
T.	91	19	Lepus	193 ,0	0,5	2,3	,186	,031	,181	1 ,53
Α	166	60	Carma	257 .4	65	7.3	,868	,026	1,000	
Λ' C	178	-62	Centamus	263 ,3	5,8	_	,608	,043	0,675	2 ,80
C	114	53	Vela	213,8	3,0	-	321	,035	, 320	3 ,70
D	141	16	Vela	237 ,5	1.7	63	,233	,051	,206	1 ,18
D'	131	57	Carma	212,2	1,9	3,1	,196	,018	,160	1 ,15
$\mathbf{r}$	138	-50	Vela	238 ,3	0,9	! -	,184	023	,115	1 ,56
E'	160	44	Vela	247 ,7	10		,169	,015	,126	17, 1
F	200	63	Centaurus	271,0	1,0		.543	,077	,591	3 ,02
G	219	-63	Centamus	282 6	2.7	71	,423	,032	,441	3 ,31
Gr'	201	-58	Centaurus	275,2	2,9		,471	,037	,508	3 ,19
H	196	-51	Centaurus	273 ,5	1 5	7,9	,208	014		1 ,35
K	191	-63	Ciux	269 ,9	0,0	7,9	,233	009	,206	1 ,18
4	232	50	Noi ma	295 ,1	3,1	7,6	133		156	3 ,31
T L	270	-28	Sagittarius	330 ,3	9,8	12,2	1,367	,060	1,624	1 ,93
L	280	8	Scutum	353,0	7,2	9,5	0,845	,104		2 ,12
Nordpol		- 90					,130	,009		5 ,13
	84	+ 7					,202	,013		
-	175	+60				)	,100	,003		
		•	•			1				1

Intensitaten  $J_{\tau}$ , die auf den leeren Raum und tur Eidheht reduzierten "absoluten" Intensitaten  $J_{abs}$  und deren Aquivalente in Steingroßen per Quadratgrad. Die Einheit der Intensitaten entspricht einem Stein von der Große 2,22 per Quadratgrad und ist also im Verhaltnis 1 3,076 kleiner als die van Riijnsche Einheit Die Tabelle enthalt auch einige Stellen außerhalb der Milchstraßenstruktur

Der Vollstandigkeit halber werden hier in Tabelle 4 auch Pannekoeks Stufenwerte für die Normalstellen der nordhehen Milchstraße, wie sie in Panne-koeks erstem großen Werke angegeben worden sind, aufgeführt. Die galaktischen Koordinaten sind nach dem Marrisschen Pol ( $\alpha=12^{\rm h}$  40<sup>m</sup>,  $\delta=+30^{\circ}$ , 1880) gerechnet worden

Der Anschluß zwischen Hoffmeisters photometrisch bestimmten Intensitaten und Pannekoeks Stufenwerten in Tabelle 3 ist sehr gut und entspricht im Mittel der Gleichung

$$J_z = 0.100 + 0.086 S + 0.00045 S^3$$

wo S Pannekoeks Stufenweit ist Daß systematische Fehlei bei den Stufenschatzungen auftreten mussen, ist von vornheiem fast schstverstandlich (vgl Zift 4) Die Messungen scheinen zu zeigen, daß bei Pannekoek die Gegend von 200° bis 250° galaktischei Lange etwas zu hell, die Fortsetzung bis etwa 300° etwas zu schwach beobachtet ist, wobei die Angaben ielativ zum mittleien

Nullpunkt jenes Teils der Milchstraße bei Pannekoek zu verstehen sind Man kann dann nach Hoffmeister folgende Berichtigungen zu den Stufenwerten annehmen

(val. I,Ango	et.	Gal Lings	ed.	
200°	-0,2	260°	0.0	
220	-0.3	280	+0,8	
240	-0,3	300	+0,6	

Die systematischen I'chler bei Pannekoek sind also jedenfalls sehr klein und erreichen kaum den Betrug von 1 st. Eine der obigen ähnliche Relation gibt der Vergleich mit Hopmanns Stufenwerten. Hier sind einige größere Differenzen zu bemerken, besonders für die südlichen Normalstellen H und K, die in Hopmanns Arbeit auffallend hell geschätzt worden sind

Tabelle 4.

Stelle	Newdehrong	I	Н	Statement
I	3 II Scuti 1 1 Aquilao	353°,0	- 3°,0	6,4
ľ	& Aguilae — 110 liere	16 .1	+ 6.3	2,2
M	7 Aquilae # 110 Flore	16 .7	- 5.4	4.3
Q	6 Vulpec - 113 Herc.	23 ,6	+ 6,2	1,4
N	7 Sagittao - 12 Vulpec	26 ,6	- 3 .8	3.3
ON A B C Z D	57 Cygni J 60 Cygni	53 .1	+ 0 ,9	5,1
В	" Cuphel 3 Lacortno	69 .7	- 0 ,3	4,5
C	7 Lucortae — 2 Cam	73 .5	- 2,0	3.7
Z.	A Cophel & Cophel	74 ,2	+ 3 .7	0,4
	β Caus — 7 Androin	79 .9	- 4 ,9	2,3
K	* Androm - Cass	83 ,2	-10 ,8	1,5
v	(f) Case, to Cophel (f) Case to Cophel	83 ,9	+ 1 ,4	3,6
S	SO COURT TO COURT.	94 ,8	+10 ,1	1,6
T	B Cam - q Pornol	96 ,3	- 7 .i	1,1
T X H I'	J Cass. g Persel	97 .8	- 2 .3	2,6
H	β Tauri τ Tauri - ι Aurigno	142 .4	- 6,1	1,0
14	/ Tauri w Aurigao .	148 ,0	+ 3,3	2,6
(r	p (romin - r (romin - r (romin	158 ,3	+ 8,0	2,0

J DUFAY hat in scher eingehonden Arbeit "Recherches sur la lumière du ciol nocturne" die Intonsitäten einiger Milchstraßengegenden mit der Intensität des Himmels am Pol, wie auch mit den Intensitäten an Punkten in derselben Zanitdistunz eben außerhalb der Milchstraße verglichen. Er findet die dichtesten galaktischen Wolken etwa 2,5 mal so hell wie den Himmel am Pol, wührend für die meisten Milchstraßengegenden das Helligkeitsverhältnis den Wert 2,0 nicht erreicht Die Messungen wurden teils mit einem visuellen Photomotor, einer für die Aufgube geeigneten Form des Photometers von FARRY-Buisson, tolls photographisch ausgeführt Dufay findet, daß, nachdem die Strohlung des Himmels für die Diffusion des Lichts in der Atmosphäre korrigiert worden ist, etwa 1/10 der Strahlung von den schwachen Sternen herrührt Das Zodiakallıclıt entspricht in einer Sonnenentfernung von 60° etwa einem Sechstel der totalen Helligkeit Der Rest der Strahlung, von Nordlichtern abgesehen, stammt vielleicht aus einer Diffusion des Sonnenlichts durch Meteoriten außerhalb der Atmosphäre Die Strahlung des Nachthimmels ist nur in geringem Maßo polarisiert, erscheint auch nicht besonders reich an blauem Licht

<sup>&</sup>lt;sup>1</sup> Lyon Bull 10, Nr 9, S 70 (1928).

# c) Die Photographie der Milchstraße.

6 Die prinzipiellen Verschiedenheiten der visuellen und photographischen Beobachtungen. Wahrend schon Steine 7 Große einzeln dem normalen Auge unsichtbar bleiben, wachst die Zahl schwacherer Steine in den Milchstraßenzonen so gewaltig, daß ihr Gesamtlicht über ein kleines Areal einen merklichen Reiz auf die Stabchen der Netzhaut des Auges ausubt. In dieser Weise entsteht die optische Illusion, die wir als das Phanomen der Milchstraße wahrnehmen

Dei photographischen Platte gegenüber hegt die Sache merklich anders Die Empfindung des Auges ist vom Lichteffekt der pio Zeitemheit aufgenommenen Energiemenge abhangig, wahrend die Platte in der Expositionszeit Belichtungsenergie akkumuliert. Die Steine sehr geringer Helligkeit drangen sich /war auf der Platte so dicht anemander, daß ihre Scheibehen nicht mehr als distinkt anzusehen sind, aber Steine, die noch viel schwacher als die visuelle Sichtbarkeitsgienze (Große etwa 6m,5) sind, werden wesentlich unabhangig voneinander als mit dei Belichtungsdauer wachsende runde Flecke abgebildet. Die Flache eines Scheibehens wachst jedoch nicht proportional zu der totalen wirksamen Belichtungseneigie, sondern langsamer Der Einfluß der helleren Sterne wird somit in der Photographie relativ zurückgehalten, wenn wir mit den Verhaltnissen bei dei visuellen Beobachtung vergleichen Pannekolk<sup>2</sup>, der diese Tatsachen besonders auseinandergesetzt hat, hebt hervor, daß die visuellen Beobachtungen und die photographischen Aufnahmen zwei verschiedenartige Darstellungen der Milchstiaße bieten "Die Photographie zeigt die kleinsten Emzelheiten und Umegelmaßigkeiten, abei hauptsachlich in Steinpunktehen aufgelöst, nur mitunter von einer Flachentonung erganzt, und daher ist die richtige Gesamthelligkeit nur schwierig zu ermitteln. Das visuelle Bild erfaßt sofort die Gesamthelligkeit als solche, abei es gibt nur die grobere Struktur des Milchstraßenlichts wieder, in subjektiv abgerundeten Formen"

Eine andere Grundverschiedenheit der zwei Beobachtungsmethoden liegt in dei Beweglichkeit des Auges, die es gestattet, in kurzei Zeit ein großes Areal zu uberblicken und weit entfernte Punkte des Himmels unmittelbar nacheinander zu betrachten Das bedeutet zwai in eister Linic eine Überlegenheit gegenüber der photographischen Kamera und ein notwendiges Mittel zur Überwindung der Unvollkommenheiten des Auges als optischen Instruments, aber es hegt doch in dei schnellen Diehung des Auges eine Quelle zur subjektiven Umformung des wahigenommenen diffusen Objektes Pannekoek schieibt über diesen Umstand folgendes "In ausgedehnten Gebieten mit schwachen oder gleichmaßigen Lichtfluktuationen sucht das Auge Anhaltspunkte, um überhaupt etwas zeichnen und beschreiben zu konnen es sucht helle und dunkle Gebilde zu erkennen und findet sie oft in vollig zufalliger und personlicher Weise Reihen schwacher Sterne 5 und 6 Große, die bei dem irrenden Herumtasten des Blickes die vorhandenen Lichteindrucke verstarken, rufen immer wieder das Bild deutlicher Lichtstreifen hervor, wo sich vielleicht gar keine großere Lichtmasse der wirklich teleskopischen Steine befindet Lichtstreifen, die Reihen sichtbarei Sterne folgen, finden sich ber allen Beobachtern, ohne daß es deshalb sicher ist, daß dem etwas Reales der Milchstraße selbst entspricht "Die photometrischen Messungen aber, die mit einem visuellen Flachenphotometer gemacht werden, sind naturlich fiel von Fehlein dieser Alt Die Vergleichung verschiedenei Gegenden geschieht hier duich Anschluß an eine kunstliche Lichtquelle, die in

<sup>2</sup> Die nördliche Milchstraße, S 110

Ygl J Plassmann, Die Milchstraße als Gegenstand der Sinneswahrnehmung Z f Psychol (I) 88, S 120 (1921)

meßbarer Weise abgeschwächt oder verstärkt wird. Wir haben hier ein Mittel, ein objektives visuelles Bild der Milchstraße zu erhalten, das außerdem auf quantitativen Messungen der Helligkeit beruht. Wie vorher hervorgehoben ist, besteht jedoch noch die Schwierigkeit, den Euffuß der von Zeit zu Zeit variablen allgemeinen Himnelsbeleuchtung zu ehminieren

Wenn wir die Gesamtleistung der visuellen Methoden betrachten, müssen wir anerkennen, daß es schwer ist, auf photographischem Wege etwas Ähnliches zu erreichen Wir haben oben von der Tendenz der photographischen Abbildung, die Struktur in Sternscheibehen aufzulösen, gesprochen Schon die Körnigkeit der lichtempfindlichen Substanz der Platten mull abei bewirken, dall bei genügend kleiner Fokaldistanz und also genügend kleiner Skala des Bildes die schwachen Sterne einer Milchstrußenregion in derselben Weise wie eine kontinuierlich leuchtende Flüche auf die Platte wirken. Um eine Schwärzung auf der Platte hervorzurufen, muß dann die gesammelte Intensität pro Flächeneinheit der Platte einen Minimumwert erreichen, was durch ein großes Offnungsverhältnis des Objektivs befördert wird. Der in Winkelmaß ausgedrückte Durchmesser der Sternschelbehen, welcher bei vollkommener Abhildung dem Objektivdurchmesser umgekehrt proportional sein sollte, wiichst in der Regel mit dem Öffnungsverhaltnis als one Folge der unvermeidlichen Abbildungsfahler, die wesentlich Form und Größe der einzelnen Bilder bestimmen Eine große Objektivöffnung bei kleiner Fokaldustanz bewirkt daher auch ein vollständigeres Zusammenfließen der Sternscheibehen einer gewissen Größenklasse, so daß man den Verhültnissen einer wirklichen Flächenabbildung nahekomint. Das Gebiet kontinuierlicher Schwärzung, welches durch das Zusammenwirken der Sterne entsteht, und seine Umgebung auf der Platte sind aber immer von uner mehr oder weniger lockeren Ansammlung von einzelnen oder in kleinen Gruppen zusammenfließenden Sternscheibehen besitt. Die Begrenzung der kontinuierlichen Schwärzung wird daher wesentlich von der Optik des Linsensystems und von der Expositionszeit abhängig. Natürlich soll das Objektiv außer einem großen Öffnungsverhältnis auch ein großes nutzbares Bildfeld haben, um gleichzeitige Abhildung eines großen Areals des Himmels auf der Platte zu geben. Die optischen Abbildungsfehler des Linsensystems und die Vignettierung für schräg gegen die Achse verlaufende Strahlenbändel, deren Einfluß mit dem Abstande vom Plattenzentrum varnort, lasson aber eine Beartellung der relativon Intensitäten nur für ein ziemlich kleines Gebiet auf ein und derselben Platte zu

Nichtsdestoweniger ist die Photographie für ein Studium der Einzelheiten des Milchstraßenbildes unentbehrlich. Durch des Zusammenfließen der Schelbchen an den dichten Stellen wird gegenüber den leeren eine starke Kontrastwirkung erzeugt. Wo das Auge nur strukturlese Lichtflecke wahrnimmt, enthüllt die Photographie oftmals ein reiches, unendlich kompliziertes Spiel von Sternanhäufungen, leuchtenden Nebelmussen, wirklichen oder durch absorbierende Materie hervorgerufenen scheinbaren Sternleeren. Unsere jetzige Auffassung von der Struktur des Milchstraßenphilnomens berüht daher in stärkstem Grade auf den photographischen Aufnahmen.

7. Die photographischen Arbeiten einzelner Forscher. Der Beginn der photographischen Milchstraßenforschung erfolgte durch E E Barnards erste Versuche im Jahre 1889 mit der "Willard Lense", einem Petzvalobjektiv von 15 cm Öffnung und 78 cm Pokullänge, das später nach Umschleifung von Brashrar am "Crocker-Teleskop" der Lieksternwarte montiert wurde Einige der früheren von Barnard aufgenommenen Bilder sind in den ersten Bänden der

<sup>1</sup> MN 50, 5 310 (1890); Publ A S 1 2, S, 240 (1890)

Zeitschritten "Astrophysical Journal" und "Populai Astronomy" reproduziert worden. In dei letztgenannten Zeitschrift hat auch II C. Wilson¹ seine frühen Milchstraßenphotographien, die hauptsachlich mit einer der Barnardschen ahnlichen Linse aufgenommen sind, wiedergegeben. Eine großere Sammlung ausgezeichneter Reproduktionen hat Barnard erst im Jahre 1913 als eine Publikation der Licksteinwarte² herausgegeben. Die Reproduktion der Negative geschah nach der "Photogelatin"-Methode. Von hervorragender Schonheit sind besonders die Aufnahmen der steinreichen Sagittatus-Ophruchus-Scorpius-Regionen. Die Bilder sind von Erlauterungen begleitet, die auf einer Analyse

dei Originalnegative berühen

Als em Beispiel soll die folgende sehr interessante Bemerkung zur Tafel N1 42, cine Partie des westlichen Astes der Milchstraße um den Stern 58 Ophrucht fgalaktische Lange 334°, Bieite +5°), mitgeteilt werden "The very singular mass of aregular clouds that occupies the middle of the plate looks strange or out of place. It is quite unique in the milky way and does not give the impression of being clouds either of stars or of nebulous matter in its general makeup. In some respects these clouds have the appearance of being quite separate from the background of small stars, as if the masses were nearer to us. One would hesitate in passing on these as to their being nebulous, and yet the appearance does not suggest star masses. It, however, we examine the two small tufts at the left of the general mass, it will be seen that they are clearly made up of small stars which spread out in a scattering manner to the southeast from both masses, almost like coarse dust" In seinem untenerwahnten neuen photographischen Atlas sagt Barnard von denselben Wolkenbildungen (Tafel 23) , They are probably entirely stellar, though this does not seem altogether certain. If stellar they probably are relatively very far away, though from their brightness this does not seem to be the case. Between us and these stars is a generous sprinkling of considerably larger stars , they are doubtless much nearer to us than the clouds "Die Lage dieser Wolke in einer Gegend, die wahrscheinlich nahezu einer Richtung gegen das Zentrum des Milchstraßensystems entspricht, macht es moglich, anzunehmen, daß diese Wolke ein sehr entferntes Gebilde ist, dessen Platz im Raume vielleicht nahe am Zentrum oder vielleicht sogar in einer noch weiteren Entfeinung gelegen ist

Nach seiner Übersiedlung an die Yerkes-Sternwarte setzte Barnard mit dem 10zölligen Bruce-Teleskop, das er auf einige Zeit (1905) auch nach Mount Wilson brachte, seine Michstraßenaufnahmen fort. Seine Arbeit findet ihren Abschluß in der großartigen posthumen Publikation "A Photographic Atlas of Selected Regions of the Milky Way", die im Jahre 1927 von der Carnegie-Instrution unter Redaktion der Yerkes-Sternwarte herausgegeben wurde. Die Karten sind photographische Kopien von sekundaren Negativen, die besonder hergestellt wurden, um einen größeren Kontrast oder größere Starke als die Originalnegative zu geben. Ein zweiter Teil des Werkes dient als Schlussel um enthält für jede Karte ein gleich großes Blatt, wo die helleren Steine der Bonner oder Cordobaer Durchmusterung eingezeichnet und alle bemerkenswerten. Ob jekte aufgenommen und numeriert sind. Jedes Blatt enthalt auch die Eckpunkte

eines aquatorialen Koordinatennetzes

Die Einleitung zum eisten Teil gibt eine ausführliche Bibliographie übe die Arbeiten von Barnard, die in irgendeiner Weise die Photographie von Michstraßenobjekten berühren

Ungefahr gleichzeitig mit BARNARDs ersten Versuchen hat H C RUSSELJ auf der Sidney-Sternwarte mit einem Dallmeyerschen Objektiv von 6 Zol

<sup>&</sup>lt;sup>1</sup> Pop Astr 3, S 58 (1895) <sup>2</sup> Publ Lick Obs 41 (1913) <sup>3</sup> M N 51, S 39 (1890

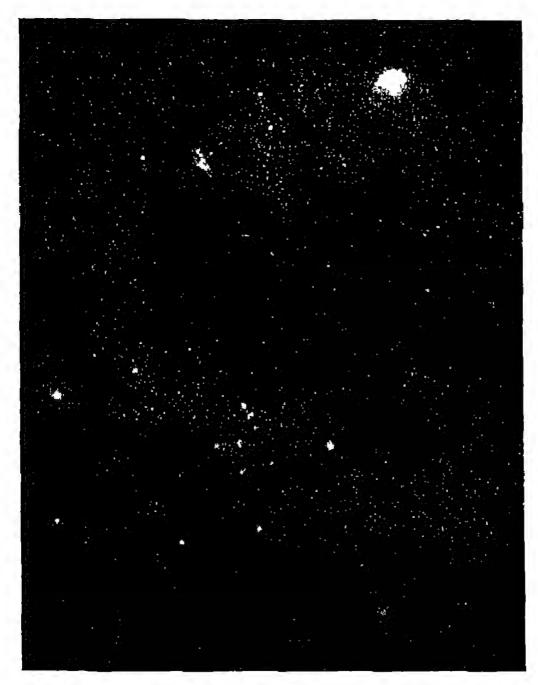


Abb 4 Milchstraße in Taurus, Auriga und Persous. Aufnahme von M Wolv mit Zokstressar (31/145 mm) Belichtung 5 Stunden 2 Minuten

Öffnung Aufnahmen der sudlichen Milchstraße und der Magellanschen Wolken gemacht. Unter den interessanten Bemerkungen, die er an seine Aufnahmen



Abb 5 Umgebung von 8 Monocerotis Aufnahme von M Wolf mit dem 162bligen Bruce-Refraktor (40/202 cm) Belichtung 5 Stunden 18 Minuten

knupft, kann ei wahnt weiden, daß er als erstei eine vei wischte Spiialstiuktui in der Nubecula Major zu schen behauptet

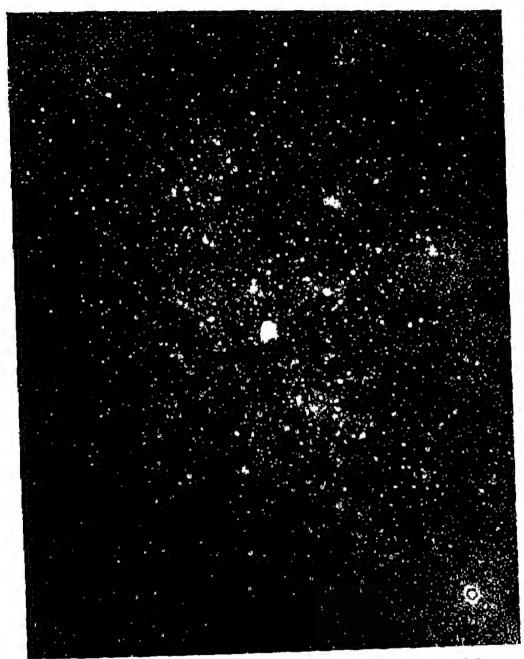


Abb 6. Umgobung von y Cygni Aufnahme von M Woly mit dem Bruce-Refraktor Bellehtung 6 Standen 50 Minuten

M Wolk ist nebst Barnard einer der erfolgreichsten auf dem Gebiete der Milchstrußenphotographie. Auf der Sternwarte Königstuhl, Heidelberg, hat Wolk mit dem 16kbilligen "Bruce-Refraktor" und auch mit kurzhrennweitigen Objektiven (besonders zwei Zeiss-Lessaten von 31 mm Offnung und 145 mm Biennweite) in großem Umfang verschiedene, und zwai meistens nordliche Gegenden der Milchstraße photographisch aufgenommen. Mehrere der Wolfschen Aufnahmen sind oft in Lehrbuchern und Monographien als Illustrationsmaterial reproduziert worden. Vollständigere Sammlungen hat Wolf in den Werken "Die Milchstraße" (Leipzig 1908) und "Die Milchstraße und die Kosmischen Nebel" (Verlag Die Steine, Potsdam 1925) herausgegeben. Das letzteie Werk enthalt 16 ausgezeichnete Lichtdrucke von Milchstraßenpartien und Nebeln

Einige Piachtstucke dei Wolfschen Aufnahmen beziehen sich auf die Milchstraße im Sternbilde (ygnus, speziell auf die große (ygnuswolke, die viele Einzelheiten von großem Interesse zeigt. Einige bemeikenswerte Erschemungen, z. B. der "Amerikanebel" und der "Kokonnebel", sind besonders durch Wolfs Aufnahmen in ihren Einzelheiten klargelegt worden. Im ganzen hat Wolfbewundernswerte Aufnahmen aller Gegenden der Milchstraße von Scutum bis Monoceros gemacht. Durch Geheimfat Wolfs freundliches Entgegenkommen werden hier einige von seinen Aufnahmen in Abb 4 bis 6 reproduziert.

Die Milchstraßenzeichnung von Goos, die nach Works Aufnahmen hergestellt ist, wird unten in Ziff 8 besprochen

Unter den wichtigsten Milchstraßenaufnahmen sind weiter die sehr schonen Photographien der sudlichen Milchstraße zu nennen, die von S. I. Baili x<sup>1</sup> zu Hanover in der Kapkolonie mit einem Cooke-Objektiv von 1<sup>1</sup>/<sub>2</sub> Zoll Öffnung und 13 Zoll Breinweite aufgenommen worden sind. Diese Aufnahmen bilden eine wertvolle Erganzung zu den Barnardschen und Worfschen Aufnahmen der nordlicheren Gegenden. Die strukturreiche Zeisplitterung der Milchstraße von a Centaum aus nach wachsender galaktischer Lange hin und die große Machtigkeit der Wolkenbildungen in den Langen 300° bis 360° freten hier in imposanter Weise hervor

Die Arbeit wurde spater in der nordlichen Milchstraße<sup>2</sup> fortgesetzt die zur Umspannung des ganzen Milchstraßengurtels erforderlichen Photographien wurden von W-II Pickering auf Jamaika und von Bauer in Cambridge, Massachusetts, hergestellt

Ein interessanter Versuch, aus einem Material von Harvard-Platten ein photographisches Bild der Milchstraße in den Regionen zwischen Crux und Aquila zusammenzusetzen, ist von H Sitapier gemacht worden und wird hier durch Herrn Sitapiers Entgegenkommen in Abb 7 reproduziert. Interessant ist ein Vergleich zwischen diesem Bild und der Herscherschen Zeichnung in Abb. 1

Von großtei Bedeutung als photogiaphische Daistellung dei Milchstiaße, besonders in ihrem sudhchen Verlauf, ist die über den ganzen Himmel sich eistieckende Franklin-Adams-Kaite³ Die Aufnahmen wurden von J Franklin-Adams mit einem Taylor-Objektiv von 10 Zoll Öffnung und 45 Zoll Breinwette zu Mei vel Hill, Godalming, in England in den Jahren 1905 bis 1909 und spater zu Johannesburg in Sudafrika gemacht. Da die Fokallange bedeutend großer ist als bei Baileys Instrument, erscheinen die Steinwolken hier weit inehr aufgelost. Viele Gegenden der sudlichen Milchstraße, in Ciux und Sagittarius, zeigen jedoch die komplizierte Struktur der ungeheuer dichten Steinwolken in außerordentlich auffalligem Kontrast gegen die benachbarten Steinlegen und gegen die gleichförmigeren steinarmeren Gegenden hoherer galaktischer

Harv Ann 72, Ni 3 (1913)
 Harv Ann 80, Ni 4 (1917)
 Franklin-Adams-Chart, R Astronomical Soc (London 1921)



Abb 7 Zusammengesutztes Blid der zentralen Milehstraßengegend swischen Crux und Aquila nach mit einem Ross-Tesser-Objektiv zu Arequipa aufgenommenen Platten

Breite Die Reproduktionen (Franklin-Adams-Karten) wie die Originalplatten selbst, die zu Greenwich aufbewahrt werden, sind schon von großer Bedeutung für mehrere Arbeiten in der Stellarastronomie gewesen

Unter neueren Milchstraßenaufnahmen sind / B die von E II Collinson<sup>1</sup> mit einem Anastigmaten 1 3, mit 6 Zoll Brennweite, gemachten zu erwahnen

Eine hohe Entwicklung der photographischen Technik ist aber besonders in den Aufnahmen von F. E. Ross<sup>2</sup> erreicht worden. Mit einem Objektiv seiner eigenen Konstruktion (3 Zoll Offnung, 21 Zoll Brennweite) hat er mit vielstundigen Expositionszeiten überaus schwache Nebelschleier in Orion, Monoceros, Laurus und Perseus photographiert. Bei solchen Objekten hangt der Erfolg, außer von der Empfindlichkeit der Platten, sehr stark von einer kontrastierichen Reproduktion der Originalnegative ab. In dem Reproduktionsprozeß benutzt Ross panchromatische Platten mit Rotfilter. Er macht auch wichtige Bemerkungen über die Grenzgrößen verschiedener Instrumente, wenn es sich um die Aufnahme von Sternen handelt. Es zeigt sich, daß für schwache Sterne gewissermaßen ein langbrennweitiger Refraktor einem Reflektor gegenüber an Wirksamkeit gewinnt infolge der kleineren Dimensionen der Sternscheibehen und der größeren Reduktion der Himmelshelligkeit

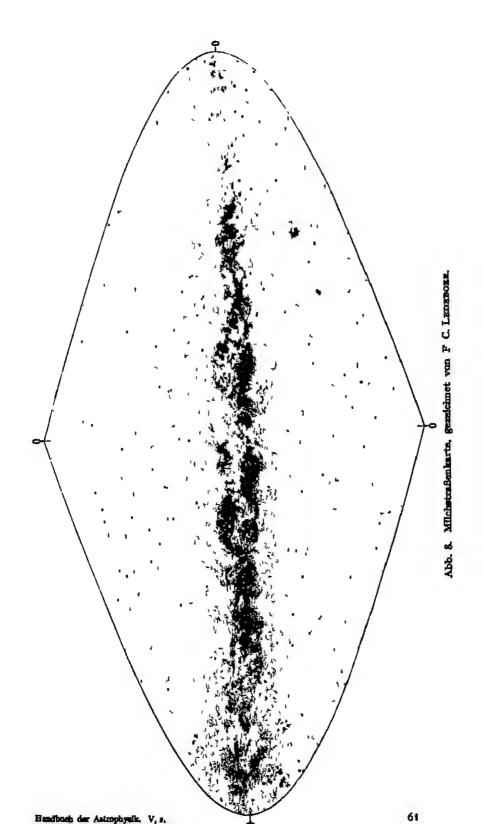
8 Milchstraßenzeichnungen auf Grund photographischer Aufnahmen. Photographische Photometrie der Milchstraße Eine Zeichnung dei Milchstraße auf Grund photographischer Reproduktionen ist zuerst von Easron³ publiziert worden Sein Material war eine Kompilation der Aufnahmen verschiedener Milchstraßemegionen von Barnard, Wolf, Pickering, Russell, Balley und anderen Die Zeichnung gibt in einer "zirkularen" Projektion die Milchstraße zwischen den galaktischen Breiten +20° und -20° In einer spateren Arbeit hat er eine in außerst feine Emzelheiten ausgearbeitete Karte der nordlichen Milchstraße gegeben

Die Worrsche Sammlung von Milchstraßenaufnahmen ist im besonders genauer Weise von F. Goos<sup>5</sup> zu einer zeichnerischen Konstruktion des nördlichen Milchstraßenverlaufs benutzt worden. Die mit den Zeiss-Tessaren aufgenommenen Milchstraßenbilder wurden in ein einheitliches Kartennetz eingezeichnet. Die vielen Steinhaufen, Nebel und Kanale wurden mit großter Sorgfalt wiedergegeben, wober der Zeichner sich bemuht hat, alles subjektive Vorunteil auszuschalten, und nur zu zeichnen, was die photographische Platte zeigt. Die Helligkeitsverhaltnisse im großen wurden durch direkte Beobachtung am Himmel und durch Anlehnung an altere direkte Zeichnungen, besonders die von Easton, moglichst wahrheitsgetien wiedergegeben. So ist eine Zeichnung entstanden, mit der an Darstellung der Einzelheiten keine durch direkte Augenbeobachtung erhaltene verglichen werden kann.

Goos hat auch in verdienstvoller Weise die Zeichnungen von Heis, der Uranometria Argentina, von Easton, Boeddicker und Houzeau in dieselbe Kartenprojektion umgezeichnet, was für die Kenntnis der zur Zeit teilweise schwer zuganglichen alteren Zeichnungen von Bedeutung ist

Eine sehr bemerkenswerte Zeichnung der ganzen Milchstraße auf Grund von Reproduktionen der Baileyschen Platten und von erganzendem photographischen Material hat kurzlich K. Lundmark unter technischer Mithilfe von O Jahnke hergestellt und in Druck vervielfaltigt. Durch Heirn Lundmarks Entgegenkommen und diese Karte hier in einer Tafel reproduziert. Sie findet sich auch in Reproduktion in Lundmarks Neubearbeitung eines Werkes von Arrhenius und im Handbuch der Physik?

<sup>&</sup>lt;sup>5</sup> Die Milchstraße, mit einem Geleitwort von Professor Max Wori Hamburg 1921 <sup>6</sup> Varldarnas utveckling Stockholm 1929 <sup>7</sup> IV (1929), Tafel



Auf der Stockholmei Steinwalte hat F.C. Lldebolk eine Zeichnung über den Veilauf der Milchstiaße in Flamstelds Piojektion nach galaktischen Kooldinaten ausgeführt (Abb. 8). Von dieser Kaite ist auch eine kleine Auflage im Dluck helausgegeben wolden. Als Volbild dienten zum Teil die Zeichnung von Goos, besondels aber Reproduktionen der Bahleyschen und anderen Halvard-Photographien, die von Heiln Shapley wohlwollend zur Veifugung gestellt wolden sind, weiter auch für die Beurteilung der lelativen Intensitaten verschiedener Partien die Karten von Pannekopk

Unseie durch die Photographie erlangte Kenntnis der allgemeinen Lichtverteilung im Milchstraßengebilde ist bisher wesentlich nur von qualitativer Ait geblieben Eine wichtige Aibeit, in der eine quantitative photographische Photometrie dei nordlichen Milchstraße begründet wird, hat abei Panni kopk. ausgeführt, unter Benutzung eines von M Wolf auf der Sternwarte Heidelbeig angesammelten Plattenmaterials Die Platten wurden mit einem klemen Tessarobjektiv von 33 mm Öffnung und 145 mm Biennweite extratokal aufgenommen, und die Ausmessung geschah mit einem Hartmannschen Mikrophotometer de-Astronomischen Institutes zu Amsteidam Die Gradation der Platten für schwäche Intensitäten wurde aus den extrafokalen Sternscheiben dadurch ermittelt, daß die Differenz zwischen der Schwätzung eines Scheibehens und der kontinuterlichen Schwärzung der unmittelbaren Umgebung auf der Platte als Funktion der bekannten Helligkeit des Steins angesetzt wurde, wobei Koriektionen fur wechselnde Größe der Scheibehen auf der Platte, Unregelmäßigkeiten in der Lichtverteilung ın den Scheibchen usw angebracht wurden Die photographische Himmelhelligkeit eines Punktes winde dann aus der Differenz zwischen der Schwärzung im betreffenden Punkt auf dei Platte und im unbelichteten Teil dei Platte berechnet Nach Berucksichtigung von Mittelpunktskorrektion und Nullpunktskonektion für die einander in großem Umfange überdeckenden Platten sind endlich die Intensitaten, wie sie auf jeder der 35 Platten für die Eckpunkte eines engmaschigen Netzes gefunden worden sind, auf 35 Kaiten wiedergegeben Emhert der Intensität ist die Helligkeit eines Steins 10 Große pio Quadratgrad Die Kaiten sind auch in einem Gesamtbilde zusammengefugt worden -- Die Beseitigung der systematischen Fehlerquellen hat in der Arbeit viel Schwierigkeit gemacht, und unerklärte Differenzen zwischen einander teilweise überdeckenden Platten treten auf Sie entstehen teils durch unberechenbare Einflüsse von Extinktion und von fremdei Erhellung des Himmelsgrundes Es ist auch nicht möglich, exakt anzugeben, für welche Große die Sterne auf den Platten noch einzeln als Scheiben sichtbar sind. Eine ähnliche Unbestimmtheit besteht abei auch, wie wir oben geschen haben, für visuelle Beobachtungen — Auf dei Bosscha-Sternwarte zu Lembang werden gegenwartig extiafokale Aufnahmen dei südlichen Milchstraße für eine ahnliche Arbeit gemacht

## d) Das allgemeine Bild der Milchstraße nach den visuellen und photographischen Beobachtungen.

9. Der Verlauf der Milchstraße am Himmel in großen Zugen. Als hellste Flecke der Milchstraße können zwei in Sagittatius und Scutum gelegene I ezeichnet werden. Der erste und großere erstreckt sich südlich von  $\mu$  Sagittatiti gegen  $\gamma$ ,  $\delta$  und  $\lambda$  desselben Sternbildes. An diesen Fleck schließt sich im Süc en eine nur wenig schwächere Masse gegen  $\varepsilon$  und  $\eta$  Sagittatit und gegen die charakte-

<sup>&</sup>lt;sup>1</sup> Eine Reproduktion dieses Druckes findet sich in K Svenska Vetenskapsakademiens Årsbok 1930.

<sup>&</sup>lt;sup>2</sup> Publ Astr Inst Univ Amst, Nr 3 (1932)

ristische Sterngruppe in der Schwanzspitze des Skorpions (G, i, x, i Scorpii) an, sie erscheint besonders hell um den Sternhaufen M7 herum. Diese ganze Partie der Milchstraße ist als die große Sagittariuswolke wohlbekannt und bildet den hervorragendsten Teil des östlichen Milchstraßenastes oder Hauptastes. Das Intensitätsmaximum der Wolke, wenn wir vom hollen Fleck um M7 herum abselien, liegt nördlich von y Sagittarii und südlich von dem Nebel M8 und dem Triffdnelxel, die als helle Knoten am Rande des dunklen Zentralgebiets, das hler die Milchstralle in zwei gewaltige Aste teilt, erscheinen Gegen dieses Zentralgebiet füllt die Intensität der Wolke sehr schnell und in einer sehr verwickelten Struktur ab

Vom südlichsten Gebiet der Wolke bei M7 geht über den Sternhaufen M6 eine schwuche Lichtbrücke gerade bls zum westlichen Ast hinfiber, der sich hier in der weitgestreckten hellen Lichtmasse zwischen a Scorpii, a Scorpii und Ophluchi ausbreitet. Nördlich von dieser Masse wird der westliche Ast durch einen dunklen Kanal durchquert, der von dem e Ophluchi-Nebel ausgeht und der sich über die Milchstraße närdlich und östlich von Ophinchi in der Farm eines gewaltigen Ankers ausbreitet. In der Nähe von Ophiuchi sind in dieser Formation einige sehr dunkle Partien zu finden Auf der anderen Seite des Kanuls, von Ø Ophinchi aus, finden wir einige weniger helle, aber doch machtig erscheinende Wolken, die zum Teil ihrer "Feinköringkeit" wegen sehr merkwirdig sind (vgl BARNARI), Ziff 7), und die ihrerselts gegen Norden hin von einem müchtigen dunklen Gebiet begrenzt und, das wie ein etwas gebogener Keil von Südwest her in die Milchstraße einsetzt, seine Spitze ungefähr in der galaktischen Länge von Altuir hat und den westlichen Ast in Ophiuchus in zwei weit getrennte Partien tellt. Die Spitze des Keils bildet auch die stellenweise schr dunkle Trennungsregion zwischen dem östlichen und dem westlichen Ast der Milchstrate in den Sternbildern Serpens und Aquila. Die Trennung ist hier welt stärker murklert als in den Regionen von Sagittarius und Scorpius, wo die Trennung der zwei Aste überhaupt sehr irregulär und oft von hellen Brücken unterbrochen erscheint.

In dem östlichen Ast ist die helle Verbindung zwischen Sagittarius- und Scutumwolke durch mehrere durchquerendo dunkle Kanale gestärt, vor allem durch den zwischen d und y Scuti gelegenen, der an einigen Stellen sehr dunkle Geblete aufweist. Sehr helle Flecken finden sich nördlich von  $\mu$  Sagittarii, ziemlich in der Zentrullinie der Milchstraße (kleine Sagittarluswolke) und um y Scuti herum. Die große Wolke in Scutum ist nach BARNARD "the gem of the Milky Way, the finest of the ster clouds" Der hellste Fleck befindet sich sudlich von B Scutl In östlicher Richtung verbreitert sich die Wolke und nummt das Licht sanft ab; das schwächste Milchstraßenlicht ist hier weit in südliche galaktische Breite zu verfolgen Die Welke zeigt nach BARNARD eine gleichformigere Flache, als die Milchetraßenweiken im allgemeinen Eine Anzahl sehr dunkler Flecke zeichnet sich außerordentlich scharf gegen die nördliche Partie der Wolke ab, besonders unmittelbar nördlich vom Sternhaufen M11

Nördlich von der Scutumwolke wird der östliche Ast durch das Sternbild Aquila hindurch fortgesetzt. Von der dunklen Durchquerung bei 1 Aquilae an der Grenze der Scutumwolke aus geht der Lichtstrom weiter gegen Norden und bildet nach einer dunklen Durchquerung bei d Aquilae den hellen Fleck unmittelbar westlich von γ Aquilae, der sich welter nördlich in der hellen Partie im kleinen Sternbild Sogitta fortsetzt.

Der woniger ausgeprägte westliche Ast geht der nördlichen Seite des dunklen Gebletes in Ophluchus entlang in nordestlicher Richtung und bildet zwischen B Ophluchi und & Aquilae eine langliche Wolke Dann folgt wieder eine weite dunkle Region Schwache Verbindungsstiome gehen von der eben genannten Wolke nach Sagitta und in einem Bogen gegen die sudwestlichen Auslaufer der großen Cygnuswolke. Die dunkle Trennungsregion zwischen dieser westlichen Ophruchus-Aquilawolke und der Cygnuswolke setzt in ahnlicher Weise wie das sudlichere dunkle Gebiet in Ophruchus in die Milchstraße ein. In der Form eines gebeugten Armes geht sie von den Sternbildern Lyra und Hercules gegen Sagitta, wo sie umbiegt, und von hier aus der Zentrallinie der Milchstraße entlang zwischen e und  $\gamma$  Cygni gegen  $\alpha$  Cygni. Die Region zwischen  $\alpha$ ,  $\gamma$  und  $\lambda$  Cygni, welche die geballte Hand des "Armes" darstellt, ist sehr dunkel. Dieses Gebiet ist zum Teil von den machtigen unregelmaßigen Nebeln nahe  $\gamma$  Cygni und  $\alpha$  Cygni ("Amerikanebel") begrenzt. Von hier aus geht weiter ein bierter dunkler Kanal in westlicher Richtung, der die nordliche Begrenzung der großen Cygnuswolke bildet

Die große Cygnuswolke steht mit der Paitie des östlichen Astes in Sagitta mittels einer schwachen Lichtbrucke zwischen  $\gamma$  Sagittae und  $\beta$  Cygni in Verbindung. Diese Wolke hat einen fast ellipsenformigen Umiiß, mit der größeren Achse zwischen den Steinen  $\beta$  und  $\gamma$  Cygni, und bildet unzweifelhaft mit ihrei nachsten Umgebung eine der interessantesten Partien der ganzen Milchstraße Gegen die dunkle Trennungsregion im Osten fallt die Intensität ziemlich steil ab, wahrend gegen das Sternbild Lyra hin die Lichtstarke in sanfter Weise abnimmt. In der Mitte der Wolke, um  $\eta$  Cygni herum, liegt eine dunklere Region

Vom Sternbilde Sagitta geht als eine Fortsetzung des ostlichen Astes ein schwacher Lichtstrom gegen s und & Cygni, der nördlich von diesen Steinen an Intensitat gewinnt und dann in stetiger Konvergenz gegen die zentiale Milchstraßenlinie über o und r Cygni duich die Sternbilder Lacerta und Cassiopeia lauft, um in der dunklen Region um  $\gamma$  Persei herum seinen Endpunkt zu finden Diesei Strom kann als Hauptstrom bezeichnet werden. Am nördlichen Rande dieses Stromes eischeinen einige Wolkenbildungen, die vielleicht als eine Foitsetzung des westlichen Milchstraßenastes angesehen werden konnen So erscheint ostlich von a Cygni die helle und sehr konzentiierte kleine Cygnuswolke, die ın einem Bogen über  $\alpha$ ,  $o_1$ ,  $o_2$  und  $\delta$  Cygni mit der großen Cygnuswolke in schwacher Verbindung steht Nordlich von der kleinen Wolke liegt das tiefdunkle Gebiet, das als "nordlicher Kohlensack" bezeichnet wird. Von diesem erstreckt sich in sudostlicher Richtung ein dunklei Kanal, der schließlich nahe den Sternen A und o Cygni den Hauptstrom durchquert und damit die kleine Cygnuswolke von dem kleinen hellen Gebiet um  $\pi_1$ ,  $\pi_2$  und g Cygni trennt Ziemlich weit nach Norden hin vom Hauptstrome aus erstieckt sich die schwache Cepheuswolke zwischen  $\alpha$ ,  $\delta$  und  $\iota$  Cephei Gegen Cassiopeia hin teilt sich dei Hauptstrom gewissermaßen in Lichtstreifen, die von dunklen Gebieten ( $\delta$  Cephei bis 4 Cassiopeiae, 1 H bis  $\beta$  Cassiopeiae) getiennt sind. Nordlich von einer Verbindungslinie zwischen  $\beta$  und  $\varkappa$  Cassiopeiae liegt ein Lichtmaximum, das sich in sudlicher Richtung über α Cassiopeiae in schwächeren Lichtmassen fortsetzt. Die Gegend bei  $\delta$  Cassiopeiae vereint sich mit den Perseushaufen h und  $\chi$  in einem langgestreckten hellen Fleck auf der Zentrallinie, der sich schließlich in das weitgestreckte Dunkelgebiet um y Persei herum verliert. Eine schwache, bogenformige Lichtblucke über 9 Persei vereint die erwähnte helle Partic mit einem kleinen Lichtmaximum unmittelbar sudlich von  $\alpha$  Persei Auf der Nordseite geht ein mit der Zentrallinie paralleler Lichtstreifen über & Cassiopeiae zum Dunkelgebiet in Perseus

In der Perseus-Camelopardalis-Region ist die Milchstraße nur sehr schwach markiert, gewinnt aber in Auriga wieder an Intensität. In der Gegend um  $\eta$  Geminorum herum hat die Milchstraße eine eigentumliche Struktur, von hier

aus gehen nach allen Seiten helle und dunkle Streifen wie von einem Zentrum<sup>1</sup> BARNARD macht die wichtige Bemerkung, daß in dieser Himmelsregion auf der nördlichen Seite der Milchstraße ein allgemeiner schwacher Lichtschimmer viel walter zu verfolgen ist als auf der südlichen, gegen Orion hin, während in der diametral antgegengesetzten Sagittarmsregion der Lichtschimmer auf der Südseite der Milchstraße weiter ausgedehnt als auf der Nordseite erscheint. Von dem genannten Punkto in Gemini weiter südlich verläuft die Milchstraße als ein memlich emholtliches, schwaches, aber an Intensität wachsendes Lichtband durch die Stornbilder Monocoros und Canis major hindurch, um im Sternbilde Puppis eine etwas verwickeltere Natur zu zeigen. In stidestlicher Richtung von m Puppis, mit & Puppis nahe auf der Westseite, zieht ein langgestrecktes, von der Zontrallinie gegon Süden divergierendes dunkles Gebiet. Dieses wird von einer hellen Partie östlich von y Velorum im wesentlichen überbrückt und geschlossen Bol a-b Velorum zeigt diese Partie ein kleines Gebiet von beträchtlicher Halligkeit Stidlich von dieser Stelle erweitert auch aber eine dunkle Region gegen beide Selten der Milchstraße, so daß zwischen y und d Volorum eine breite dunkle Durchquerung, auf die wohl zuerst J HERSCHEL aufmerksom gemacht hat, zustande kommt Von hier aus wächst die allgemeine Intensität der Milchstraße sehr schnell und verjüngt sich gleichzeitig der Lichtstrom, um in die schmale, aber sehr helle Milchstraßenpartie in Carina überzugehen

Die Carinawolke zeigt gegen den Südpol hin einen sehr schnellen Intensitätsabfall: nach einem sehr konzentrierten Helligkeitsinnzimum um  $\eta$  Carinae herum bildot sich gegen A Centauri eine sehr merkierte dunkle Einbiegung in der intensiv leuchtenden Masso. In Crux wird der Strom breiter und umschließt den großen, dunklen, zentral gelegenen "Kohlensack" östlich von & Crucis. Diesos birnenförmige Oval hat eine größte Länge von etwa 8° und eine größte Breite von etwa 5° Dor holle Lichtstrom wird dann immer breiter, bel & Centauri wird durch eine langgestreckte, im Sternbilde Norma gegen Norden hin umgebeugte dunkle Masse ein westlicher Ast abgesondert, der in wachsendom Abstand von der Zentrallinie der Milchstraße und mit abnehmender Intensität sich schließlich mit der hellen Partie des westlichen Milchstraßenastes in Scorpius vereint,

Der östliche Hauptstrom hat ein starkes Intensitätsmaximum in Norma und sondert dort noch einen Strom gegen die westliche Scorpluspartie ab. Der hier abgesonderte Strom wird jedoch in mohreren Punkten, bei y Normae, bei & Scorpil und zwischen μ und s Scorpii, durch dunkle Risse durchquert. Der östliche Hauptstrom wird durch die Spaltung nach Süden gedrückt und verliert zuerst bedoutend an Intensität, gewinnt aber in Scot plus und Sagittarius wieder an Stärke und trifft endlich über die Schwanzsterne des Skorpions mit der großen Sagittariuswolke zusammen. Bei den eben grwähnten Sternen erwoltort sich die Lichtmasse gegen den westlichen Ast hin, so daß hier von & bis \u03c4 Scorpii eine weite Überbrückung zwischen den zwei Hauptästen entsteht Zwischen dieser Lichtbrücke und der vorher erwähnten, über die Sternhaufen M7 und M6 gehenden liegt bel 2 und v Scorpii eine welte dunkle Höhle.

10. Die Magellanschen Wolken. Die zwei Gebilde des Stidhimmels, die als die Magellanschen Wolken (auch die Kapwolken oder die zwei Nubeculae, (N major and N. minor) bezeichnet werden, sind oftmals als "versprengte Stücke der Milchstraße" bezeichnet worden, wenngleich ihre vollkommene Abgeschlossenhelt von der Milchstraße selbst schon von J Herschel ausdrücklich betont

<sup>&</sup>lt;sup>1</sup> PANNEROEK, Die nördliche Milchetraße, S. 76.

Photographic Atlas I, S. 10.

Results of Astronomical Observations, S. 384 und Pl XIII (in Abb 1 oben reprodu-

wurde Nach Herschelb Beschreibung eireicht man die kleinere Wolke an allen Seiten "durch eine Wuste"

Die größere Wolke befindet sich in der Position  $\alpha=5^{\rm h}$  20<sup>m</sup>,  $\delta=-69^{\rm o}$  (1900) Die galaktischen Koordinaten sind  $L=247^{\rm o}$ ,  $B=-32^{\rm o}$  Der zentrale Teil der Wolke ist ein langgestrecktes, fast elliptisches, auf den photographischen Aufnahmen ziemlich amorph erscheinendes Gebilde, das speziell gegen Suden hin von einem weiten, schwachen Lichtschleier umgeben ist. Um und über diese zentrale Partie ist außerdem eine Menge kleinerer Gebilde von grobkörnigerer Struktur in umegelmäßiger Weise gestreut. In dieser Weise erstreckt sich die Wolke im ganzen über ein fast kreisförmiges Areal von ungefahr 6° Durchmesser. Die Wolke enthalt zahlreiche Sternhaufen und Nebel

Die kleinere Wolke hat die Koordinaten  $\alpha = 0^{\rm h}$  40<sup>m</sup>,  $\delta = -74^{\circ}$ ,  $L = 270^{\circ}$ ,  $B = -43^{\circ}$  Die Struktur dieser Wolke erscheint durchaus armer als die der

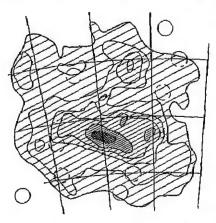


Abb 9 Die Isophoten der größeren Magellanschen Wolke

großeien, wenngleich im ganzen große Ahnlichkeiten bestehen. Der großte Duichmesser des Gebildes ist etwa 3°. In einer Entfeinung von nur 2° von der Wolke, aber sonst ohne figendem Zeichen einer physischen Verbindung mit der Wolke, liegt auf der nordwestlichen Seite der schone Kugelhaufen NGC 404, § Tucanae

Nach den Messungen von Hopmann (Ziff 4) eiteicht die Flachenhelligkeit der großeien Wolke nahe die maximale Helligkeit der großen Sagittariuswolke Die Flächenhelligkeit der kleinen Wolke ist bedeutend geringer, aber kommt doch nach Hopmann vielen dei helleren Milchstraßenwolken gleich Nach E Hertzsprung wurde, wenn die Flachenhelligkeit dei kleineren Wolke über dem ganzen Himmel vorheitschen sollte, die entspiechende Strahlungsintensität an einem

Punkt der Erdoberflache derjenigen eines Sterns im Zenit von dei Giöße —6,6 aquivalent sein Für ein gleichmaßig helles kreisrundes Objekt vom Radius  $\varrho$  und von der integrieiten Größe m bekommt man den Aus-

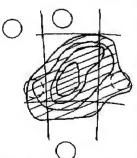


Abb 10 Die Isophoten der kleineren Magellanschen Wolke

von der integrieiten Größe m bekommt man den Ausdruck für die Flachenhelligkeit durch die aquivalente Größe eines Zenitsterns im oben definieiten Sinne einfach gleich  $m + 5 \log \sin \rho$ 

Eine photographische Photometrie der Wolken hat kurzlich G van Herk<sup>2</sup> ausgeführt. Die Platten sind auf der Sternwarte zu Lembang aufgenommen worden und die Methode, die früher von Pannekoek in einer Photometrie der Scutumwolke (Ziff 17) verwendet wurde, was die folgende Die Platten weiden ein wenig extrafokal exponiert und mikrophotometrisch ausgemessen. Die Schwarzungsskala wird aus den extrafokalen Scheibehen der Sterne von bekannter Große ermittelt. Die in dieser Weise bestimmten isophotischen Linien der größeren und kleineren Wolke sind hier in Abb 9 und 10

gegeben Die Linien sind für die Helligkeiten 20, 40, 70, 100, 140 und 200 gegeben, wo die Einheit einem Stern von 10 Größe pro Quadratgrad entspricht.

<sup>1</sup> BAN 2, S 209 (1925)

<sup>2</sup> BAN 6, S 61 (1930)

VAN HERK findet durch Vergleich mit PANNEKOEKS Resultaten, daß die hellste Partie der Scutumwolke erheblich heller als die hellsten Stellen der Magellanschen Wolken ist. Für die integrierte photographische Gräße in der gewähnlichen Skula findet er für zwei Platten

> Großere Wolke · +1m,2, 十1四,2 Kleinere Wolke .  $+2^{m}.8.$ +2m,9

Pür die kleinere Wolke hat Shapley eine photographische Größe zwischen 4-2m und | 3m und J S PARASKEVOPOULOS +1m,8 angegeben Hertzsprungs obenerwähnte visuelle Flächenholligkeit entspricht 424 Sternen der Größe 10m pro Quadratgrad Man muß wohl hier aber bei dem Vergleich mit van Heres kleinerem Wert in Betracht ziehen, daß wir wahrscheinlich mit einem Farbenindex

der Wolken von etwa +0m,5 zu rechnen haben

11. Die Lage der Milchstraße. Die zentrale Linie des Milchstraßengürtels folgt sehr nahe einem größten Krais am Himmel Für den Pol dieses Kreises sind mehrere Bestimmungen gemacht worden W HERSCHEL® gibt die Koordinaten RA - 186°, Dekl = +32° für das Aquinoktium 1785 Die Werte von ARGKLANDER<sup>4</sup>, mus Bodes Darstellung der Milchstraße in seinem Atlas bestimmt, und von F W. STRUVE haben nur historisches Interesse, sind aber schon mit den houtigen Werten naho thereinstimmend Houzeau benutzte die Koordinaten seiner 33 Punkte maximaler Helligkeit und berechnete, von Stroves Pol ausgehend, in einer Ausgleichung nach der Methode der kleinsten Quadrate den Pol des größten Kreises, der sich diesen Punkten am besten anschmiegt Einmal reclinet or mit glolchem Gowichte für alle Punkte, ein zweites Mal mit Gewichten nach den Helligkeiten. Eine Ausgleichung desselben Materials unter Einführung der Nordpoldistanz  $\sigma$  des Kreises als unbakannte Größe in die Gleichungen haben RISTRIPART und KOROLD unternommen Das Resultat von Korold ist in der ersten Zeile der Tabelle 5 aufgeführt. Die Tabelle gibt auf das Äquinoktium 1900 reduzierte Werte (außer für Newcomb, der sein Aquinoktium nicht angibt) der zur Zeit besten Bestimmungen, die auf Zeichnungen und photometrischen Beobachtungen der Milchstraße beruhen

Huis lint eine Bestimmung aus seinen Milchstraßenzeichnungen im Atlas Corleatis Novus gemacht, die nicht sehr von Goulds und Newcomes<sup>10</sup> Resultaten abwelcht, die aus Bearbeitungen der Milchstraßenzelchnungen im Atlas Coelestis Novus und in der Urunometria Argentina herrühren Besonders Gouldes Resultat

lst sehr viel benutzt worden

Eine Bestimmung auf Grund der Goosschen Darstellung der nördlichen Milchstralio ist von C. Wirtz<sup>11</sup> gemacht worden Diese Bestimmung behandelt aber die beiden Arme der Milchstraße getrennt (vgl wenter unten). GRAFF18 und HOPMANN 18 haben weiter ihre photometrischen Messungen zur Lösung der Aufgabe benutzt

Hinsichtlich der Daten, die man zur Bestimmung der Symmetrieebene hernnzichen kann, sind in Anschluß an Pannekoeks Ausführungen die folgenden

Typun zu unterscheiden.

<sup>5</sup> Harv Bull 840 (1926).

Harv Circ 260 (1924)

Harv Bull 840 (1926).

Phil Trans 75, S. 253 (1785), Collected Scientific Papers I, S. 251

Bonner Boobschtungen V. 3 (1862).

Rtudes d'Astronomic Stellaire, S. 62 (1847)

Untermohungen über die Constants der Pracession, S 63 Karlsruhe 1892

Dor Bau dos Firsternsystems, S 184 (1906).
Vorrodo sum Atlas, vgl HAGEN, AN 217, S. 291 (1922).
Uranometria Argentina, S. 371.

16 Publications of the Carnogle Inst. of Washington, No 10 (1904)
11 V J S 57, 8, 22 (1922)
12 A N 213, S. 27 (1921).
13 A N 222, S. 92 (1924) 11 V J S 57, S. 22 (1922)

a) Man kann von den Randern ausgehen und überall die Mittellime möglichst

an die Mitte zwischen Nord- und Sudrand anschmiegen

Eine größere Sicherheit gewinnt man, wenn man die helleren Gebilde der Milchstraße als ihre Hauptobjekte ansicht und hellere isophotische I mich als Begrenzung ihres wesentlichen Teiles betrachtet. Dies führt zum entgegengesetzten Gienzfall

b) Man sucht alle hervortretenden hellsten Stellen Zentren der Lichtwolken und Maxima der Strome auf und legt die Mittellinie durch sie hundurch Willkurlichkeiten in der Auswahl solcher Stellen lassen sich dann schwer vermeiden

Die Festlegung der Helligkeitsveiteilung in Zahlen bietet die Möglichkeit,

diese Willkurlichkeiten zu vermeiden, indem man entweder

c) fur jeden Querschnitt die Lage des Lichtschweipunktes bestimmt, also  $\sum h \ b(N)$  gleich  $\sum h \ b(S)$  macht, wo h Helligkeit, b Breite im Koordmatensystem der Karte ist,

d) oder es wird für jeden Querschintt die "Lichtmitte", also  $\sum h(N) = \sum h(S)$ .

berechnet

In der Tabelle 5 sind die Bestimmungen nach diesem Schema klassifiziett worden Nach Hopmann kann man konstatieren, daß die Ansatze a) und c), die Wert auf die mittlere Helligkeitsverteilung legen, die Milchstraße als genau in einem Großkreis verlaufend hinstellen Dagegen hegt dei Zug dei hellen Wolken [Ansatz b) und d] in einem Kleinkreise, dessen Pol nordöstlich von dem der anderen Methoden hegt Newcombs Behandlungsweise muß als ein Kompromiß zwischen a) und b) bezeichnet werden, da ei 42 Punkte teils auf dei Mittellime, teils an Stellen maximalei Intensitat, in ziemlich gleichmäßiger Verteilung nach galaktischer Lange, benutzt hat Das in die Tabelle aufgenommene Resultat von Wirtz ist in ahnlicher Weise zu bezeichnen, bezieht sich aber auf den "Hauptzweig" der Milchstraße

Besonders großes Vertrauen verdient ohne Zweifel Pannekofks Bestimmung der Mittellinie der Milehstraße und die daraus folgende Lage des Pols in seiner oben (Ziff 3) erwähnten Arbeit über die sudliche Milehstraße. Für jeden (nach der galaktischen Lange am Nord- und Sudhimmel wurde die Summe der Helligkeiten in dem entsprechenden Querschnitt der Milehstraße gebildet, und die Breite der Mitte, welche die Totalhelligkeit in zwei gleiche Hallften teilt, bestimmt Die schwachsten Helligkeiten wurden vor der Summenbildung ausgeschlossen (die gegebenen Helligkeitszahlen wurden um eine Einheit vermindert und negative Zahlen durch 0 ersetzt). Die erhaltenen Werte sind in einer Tabelle in der erwähnten Arbeit aufgeführt. Pannekoek hebt hervor, daß eine sich an die erhaltene Mittellinie schmiegende Ebene vielleicht noch nicht die wahre Symmetrieebene des galaktischen Systems darstellt, da die absorbierenden Nebelmassen in Taurus die Mittellinie nach Norden und in Ophiuchus nach Süden drangen und daher der Pol scheinbar in der Richtung nach 330° Länge verschoben wird, seine R.A. hierdurch zu groß und seine Deklination ein wenig zu klein wird.

Die Gesamthelligkeit als Funktion der galaktischen Lange zeigt nach PANNE-KOEKS Zahlen ein hohes, schaifes Maximum in Sagittarius Die Daistellung der Helligkeit durch eine einfache gomometrische Formel ergab

$$h = 319 + 179 \cos(L - 323^\circ)$$

Die Abweichungen gegen diese Formel zeigen noch vier Maxima bei 325° in Sagiftarius, 50° in Cygnus-Lacerta, 170° in Gemini, 260° in Carina Minima dazwischen bei 10° in Aquila, 110° in Perseus, 230° in Vela, 290° in Circuius-Lupus

Tabella 5

Viriodit	Autorität			
HOURRAU-KOHOLD LOULD. NEWCOMB LOUN-WIRTZ LIRAFF HOPMANN PANNERORK	(b)	191 ° 26′	+27° 56′	91° 14',5 ± 50' (m F)
	(a)	190 38	27 13	90 0 ± 6'
	(a, b)	191 6	26 48	90 59
	(n, b)	195 8	29 8	90 31 ± 23'
	(c)	192 16	26 48	90 0
	(c)	189 44	26 0	90 14,2 ± 6'
	(d)	194 0	27 43	91 5

Aus den Zahlenangaben für  $\sigma$  ersicht man, daß die Sonne wahrscheinlich ein wenig nördlich vom der zentralen Ebene der Milchstraße gelegen ist. Der Botrug der Abweichung ist jedenfalls nach diesen Resultaten sehr gering, aber noch ziemlich unsicher bestimmt

Rine Neuberechnung des Pols der photographischen Milchstraße (Goos-Wolf) von Wirtz unter Berücksichtigung von Haupt- und Nebenzweig zusammen gibt  $A=191^{\circ},9$ ,  $D=+31^{\circ},0$  (1900),  $\sigma=87^{\circ},9$  Eine Auflösung für die photographische Milchstraße nach Barnards Atlas gibt  $A=194^{\circ},2$ ,  $D=+28^{\circ},7$  (1900),  $\sigma=88^{\circ},0$ . Die Sonne stände also etwas südlich von der Hauptebene der "aktinischen" Milchstraße Die wahre Bedeutung dieses Phänomens ist wohl aber noch ganz unklar

Über die zur Bestimmung des Pols benutzten mathematischen Methoden

mag folgendes gesagt werden.

1. Houzeau berechnet den sphärischen Radius der Milchstraßenpunkte von Struves Pol aus Die Abweichung von 90° für einen Punkt wird als eine kleine Verschiebung des wahren Pols gedeutet Ristenpart und Kobold geben der etwas verüligemeinerten Methode von Houzeau die folgende Form. Seien  $\alpha$ ,  $\delta$  die Koordinaten einzelner beobachteter Punkte (etwa Punkte größter Dichtigkeit), A, D die Koordinaten des Pols, für welche man die Näherungswerte  $A_0$ ,  $D_0$  luit. Von diesem genäherten Pol aus berechnet man den Abstand  $\sigma_0$  eines beobachteten Maximums folgendermaßen.

$$\cos \sigma_0 = \sin \delta \sin D_0 + \cos \delta \cos D_0 \cos (\alpha - A_0)$$

$$\sin \sigma_0 \sin P = \cos \delta \sin (\alpha - A_0)$$

$$\sin \sigma_0 \cos P = \sin \delta \cos D_0 - \cos \delta \sin D_0 \cos (\alpha - A_0)$$
(1)

Die Hedingungsgleichungen zur Bestimmung der Korrektionen dA und dD des provisorischen Poles und der Größe  $\sigma$  sind dann von der Form

$$\sin P \cos D_0 \cdot dA + \cos P \cdot dD + \sigma = \sigma_0. \tag{2}$$

2. Wenn wir die beobachteten Punkte des Milchstraßengürtels in einem provisorischen galaktischen System mit l,b bezeichnen und die Koordinaten des wahren Pols in demselben System mit L,B, so haben wir unmittelbar die Relation

$$\cos b \cos l \cos B \cos L + \cos b \sin l \cos B \sin L + \sin b \sin B + \cos \sigma = 0$$
 (3)

Da wir voraussetzen können, daß der provisorische Pol nahe dem richtigen liegt, so kann sin B=1 gesetzt werden, und wir können eine direkte Auflösung nach der Methode der kleinsten Quadrate mit den Unbekannten  $\cos B\cos L$ ,  $\cos B\sin L$ ,  $\sigma$  vornehmen Für  $\sigma$  kann man  $90^{\circ}+p$ , wo p die Tiefe ("dip") der Milchstraßenlinie bedeutet, einführen.

3. Newcomb sucht die Ebene durch unseren Beobachtungsort zu bestimmen, für welche die Summe S der Quadrate  $\phi^a$  ein Minimum ist, wo  $\phi$  den Sinus

<sup>1</sup> Hauptrweig der Milchstraße,

der Winkeldistanz der Objekte von der Ebene bezeichnet Wenn wir die folgenden Bezeichnungen für die Richtungskosinusse einfuhren

$$a = \cos \delta \cos \alpha$$
,  $b = \cos \delta \sin \alpha$ ,  $c = \sin \delta$ ,  
 $v = \cos D \cos A$ ,  $y = \cos D \sin A$ ,  $z = \sin D$ ,

so ergibt sich

$$p = ax + by + cz$$

Wir bekommen dann die Summenformel

$$S = [aa] x^2 + 2[ab] xy + [bb] y^2 + 2[ac] xz + 2[bc] yz + [cc] z^2$$

Außerdem haben wir

$$x^2 + y^2 + z^2 = 1$$

Die Differentiation dieser Ausdrucke gibt, wenn wir die Bedingung dS = 0 einfuhren, für v, y, z die Gleichungen

$$\begin{aligned} &([aa] - \lambda)x + [ab]y + [ac]z = 0, \\ &[ab]x + ([bb] - \lambda)y + [ba]z = 0, \\ &[ac]x + [bc]y + ([cc] - \lambda)z = 0, \end{aligned}$$

wo I also durch die folgende Gleichung bestimmt weiden muß

$$\begin{vmatrix} [aa] - \lambda & [ab] & [ac] \\ [ab] & [bb] - \lambda & [bc] \\ [ac] & [bc] & [cc] - \lambda \end{vmatrix} = 0$$
(4)

Die Wurzeln dieser Gleichung sind reell und positiv. Sie bestimmen die dier Hauptebenen des Systems. Newcomb zeigt, daß die Kondensationsebene durch die kleinste Wurzel  $\lambda$  definiert wird. Eine ausführliche Darstellung der Newcombschen Methode hat Philippot<sup>1</sup> gegeben.

Da die Milchstraße als der Kreis maximalei scheinbaiei Steindichtigkeit am Himmel definiert werden kann, so ist es klai, daß auch die Resultate dei Sternzahlungen zur Bestimmung der Lage dieses Kieises benutzt werden können Die frühen Sternzahlungen berühten im wesentlichen auf dem Material der Bonner Durchmusterung und ihrer stidlichen Fortsetzung Nach den Arbeiten von Ristenpart<sup>2</sup> und Prey<sup>3</sup> folgen die Dichtigkeitsmaxima der Steine heller als 9<sup>m</sup>,5 zwei etwas gegeneinander geneigten Ebenen. Die Lage der weniger ausgepragten sekundaren Ebene fällt jedoch für die beiden Autoren sehr verschieden aus

Aus der Verteilung der Sterne bis zur photographischen Größe 11,0 (Statistik der Zahlungen von H Henie¹ nach der "Harvard Map") hat H Nori⁵ unter der Annahme A=491°, D=+27° für die Lage des Pols die Tiese p=+1°38°  $\pm 70°$  (m F) erhalten

Die die schwachsten Sterne beiucksichtigenden Bestimmungen dei Symmetrieebene sind erst kurzlich von F H Seares und P J van Riijn? gemacht worden Seares Resultate wurden aus einer Statistik der Selected Aleas bis zur 18 photographischen Größe, zusammen mit einigen Zonen dei photographischen Himmelskarte, erhalten Er untersucht die systematischen Ab-

7 Groningen Publications, Nr 43 (1930)

Annuaire de l'Observatoire Royal de Belgique, 1923, S 195
 Unters über die Konstante der Präzession (1892)

Denkschriften der math -naturw Klasse der K Akad der Wiss, Wien, Bd 43 (1896).
 Lund Medd, Serie II, Nr 40 (1913)

Recherches astron de l'Observatoire d'Utrecht VII, S 115 (1917)
 Mt Wilson Contr 347, S 19, Ap J 67, S 141 (1928)

weichungen A der Logarithmen der Sternzahlen von einem rotationssymmetrischen Verlauf in gulaktischer Länge und bestimmt die Konstanten a, b und L' der Formel  $\Delta = a + b \cos(L - L')$ 

sowold für verschiedene Größen als auch für verschiedene Zonen der galaktischen Breite Die Abhängigkeit von der galaktischen Länge wird als Folge dieser Verschiebung des galaktischen Pols wie auch einer exzentrischen Lage der Sonne Im System gedeutet (Zulf 18) Aus den Werten von a, b und L' für verschiedene Zonen werden also der Betrag der Polverschiebung und die Länge des Zentrums ermittelt.

VAN RIIIINS Material sind für schwächere Sterne die Selected Areas (Harvard Durchmusterung und Mount Wilson-Katalog, wie oben bei Seares) zur Gronzgröße 14 verwendet er die Franklin-Adams-Karten, bis zur Größe 10 die Bonner und Cordoba Durchmusterungen und für Sterne heller als 6m die Harvard Revised Photometry Beide Verfasser gehen von dem Gouldschen Pol aus und bestlinmen Lange und Breite des wahren Pols für die in Frage kommenden Sterne. Die Resultate sind in Tabelle 6 zusammengefaßt worden L und B sind die galaktischen Koordinaten des wahren Pols in Goulds System Die Gronzgrößen m sind photographisch van Renju gibt auch den "dip" p des Symmetriekreises

Tabelle 6

	Searce			Van Reije			T
<b>J</b>	L	H		L	В	•	
9 11 13.5 16 18	275° 296 319 357 350	81°,9 83 ,2 82 ,0 85 ,9 87 ,3	4 5 6 8 10 14 14 16	152° 166 213 290 293 347 354 359	69°,0 88 ,4 87 ,3 88 ,7 87 ,2 85 ,0 87 ,6 86 ,1	-0°.7 +2 .1 1 .2 1 .8 1 .6 3 .0 0 .5	(Franklin-Adams-K ) (Selected Areas)

Den wahrscheinlichen Fehler in B. L con B und p schätzt van Rhijn zu etwa i°

Für die Storne zwischen 9m und 14m zeigen die Resultate der zwei Verfasser sehr erhebliche Differenzen in der Breite B Es ist bemerkenswert, daß nach van Rhijn für Sterne schwächer als 8m praktisch dieselbe Lage des Pols für alle Klassen wiedergefunden wird Die große Bedeutung diesbezüglicher Fragen wird In den folgenden Abschnitten ersichtlich.

Für die Größen 8 bis 16 geben van Rhijns Resultate im Mittel  $L=330^{\circ}$ ,  $B = 86^{\circ}, 6, p = +1^{\circ}, 9$ , und in aquatorialen Koordinaten für das Aquinoktium A = 193°54', D = +25°29', 1900.  $\sigma = 91^{\circ},9$ 

Wenn wir mit diesem Pol als Grundlage galaktische Koordinaten berechnen und diese mit L1, B1 bezeichnen, bekommt man nach van Rhijn für sukzessive Grenzgrößen die Werte in Tabelle7.

Die Verschlebung des Pols für die helisten Grenzgrößen ist ein Phänomen,

 $B_1$ L • 00,0 150°,2 65°,6 +1 .5 84 .7 167 ,2 5-6 87 ,3 167 ,2 90,0

Tabelle 7

das schon in großen Zügen von J Herschell und von Gould's beobachtet wurde. Gould fand, daß von den 527 Sternen bis zur 4 Größe 306 sich der

Proc Amer Assoc for Adv Science, S 115 (1874), Uranometria Argentina, S. 354 1 Results of Observations, etc., p 385

Milchstraße, aber 330 sich einer anderen Symmetrieebene (dem "Gournschen Kreise") innerhalb 30° anlehnen Fui den Pol seines Kieises land Gouid etwa  $A=171^{\circ}$ ,  $D=+30^{\circ}$ , oder im galaktischen System der Tabelle 7  $L_1=162^{\circ}$ ,  $B_1 = 69^{\circ}$  Dieselbe Verschiebung erscheint auch in Newcombs<sup>1</sup> Resultaten über die Lage des Pols fur verschiedene hellere Großenklassen, verglichen mit dem Milchstraßenpol Nach van Rhijns Resultaten ist das Phanomen noch bis au 7 Große schwach zu spuren VAN DE LINDE2 findet fur Sterne heller als 6m,25 den Pol  $A = 183^{\circ}$ ,  $D = +28^{\circ}$  Über die Bedeutung dieser Erschemung zu sprechen weiden wit im folgenden mehrfach die Gelegenheit haben. Unter anderem wird es hervortreten, daß die Eischemung auch besonders ausgepragt für die Heliumsterne und die Gasnebel in unserei nachsten Umgebung 1st (Ziff 13 und 19)

Zu erwahnen ist noch, daß J BAILLAUD<sup>3</sup> für die Zone -1-22° der photographischen Himmelskarte, Grenzgroße etwa 12,5, eine sehr erhebliche galaktische Konzentiation gefunden hat, eine Lage des Pols  $A = 200^{\circ}, 5$ ,  $D = +27^{\circ}, 2$  (1900) und eine Tiefe von 3° Spater hat er' aus Seares' Beobachtungsmaterial, aber nach einer allgemeineren und einfacheren Methode als der von SFARES benutzten, fui die Polkooidinaten  $A = 193^{\circ}.7$ ,  $D = +27^{\circ}.1$ 

berechnet, mit einer Unsicherheit von etwa 2° Diese Lage des Pols stimmt seln

wohl mit dem Pannekoekschen Weit in Tabelle 5 und ist auch mit van Riijns oben angefuhrten, aus analogem Material bestimmten in leidlicher Übereinstim-

Von großem Interesse ist die galaktische Verteilung für Objekte von großer absoluter Leuchtkraft und dahei großer mittlerer Entsernung, da wir hier heurteilen können, in welcher Weise die raumliche Anordnung dieser Objekte sich der galaktischen Ebene anschmiegt Diesbezugliche Fragen werden in Ziff 19 und 20 naher diskutiert

12. Galaktische Koordinaten. Die Fundamentalebene der galaktischen Koordinaten wird durch den zum Milchstraßenpol gehörigen großten Kreis festgelegt Die galaktische Lange wird langs diesem gioßten Kiels, gewöhnlich vom aufsteigenden Knoten des Kreises auf dem Aquator, gezählt Die galaktische Breite ist das Komplement der Distanz vom Nordpol dei Milchstraße Die Formeln zur Übertragung der aquatorealen Koordinaten α, δ in galaktische sind dann, wenn wir wie vorhei galaktische Lange und Bierte mit L und B, R  $\Lambda$ und Dekl des galaktischen Pols mit A und D bezeichnen

$$\cos B \cos L = \cos \delta \sin(\alpha - A)$$

$$\cos B \sin L = \sin \delta \cos D - \cos \delta \sin D \cos(\alpha - A)$$

$$\sin B = \sin \delta \sin D + \cos \delta \cos D \cos(\alpha - A)$$
(5)

Nach der gegebenen Definition hegt die galaktische Länge 0° auf dem galaktischen großten Kreis im Sternbilde Aquila, die Lange 90° in Cassiopeia, 180° in Monoceros, 270° in Crux. Die über ein großeres Areal hellsten Partien der Milchstraße befinden sich in den galaktischen Langen 315° bis 335°, in den Steinbildern Sagittarius, Scorpius und Ophiuchus

Andere Vorschlage zur Annahme des Anfangspunktes in galaktischei Lange sind gemacht worden Man hat zuweilen als Nullpunkt den Sonnenapex benutzt (vgl unten) oder einen hellen Stern mit sehr kleiner Eigenbewegung wie α Cygni<sup>5</sup> Keine von diesen Zahlungen ist bisher allgemein angenommen woi den

<sup>1</sup> Publ of the Carnegie Inst, No 10 (1904)
2 De Verdeeling der heldere Sterren, S 59 Rotterdam Wyt & Zonen 1921
3 CR 188, S 377 (1929),

Von dieser Willkürlichkeit des Anfangspunktes der galaktischen Länge abgesehen, gibt es ebenso viele Systeme galaktischer Koordinaten wie Bestimmungen der Lage des Milchstraßenpols. Da vurschiedene Bestimmungen oft ziemlich stark voneinander abweichen und es überdies nie darauf ankommt, eine galaktische Position mit äußerster Genaugkeit anzugeben, so wäre es natürlich am zweckniäßigsten, durch eine allgemeine Konvention unter Berticksichtigung der besten Bestimmungen eine gewisse Lage des Pols für allgemeine Zwecke zu fixieren. Hier herrscht gegenwärtig noch eine gewisse Verwirrung. Oft werden abgerundete Ziffern, wie z B  $\Lambda=190^\circ$ ,  $D=+30^\circ$ , benutzt, in anderen Fällen z B der Gouldsche Pol

A MARTH¹ hat zur Benutzung bei Milchstraßenbeobachtungen die galaktischen Koordinaten für die sichtbaren Sterne innerhalb der galaktischen Breiten  $\pm 20^{\circ}$  gegeben. Für den Pol der Milchstraße wurde dabei  $A=190^{\circ}, D=\pm 30^{\circ}$  (Äqu 1880) angenommen Der Marthsche Katalog ist speziell als Hilfe für die Konstruktion einer Karte aufgestellt und ist auch in dieser Weise vielfach benutzt worden. Pannekoek, Easton und Plassmann haben z B. Reproduktionen solcher Karten unter Astronomen und Liebhabern verteilt, um die Praxis des Milchstraßenzeichnens allgemeiner zu verbreiten.

J C. KAPTEYN<sup>5</sup> hat eine Tafel für Berechnung der galaktischen Breite unter Benutzung des Gouldschen Pols ausgearbeitet. Die Intervalle der Argumente sind 1<sup>h</sup> in α und 1° in δ. Eine Spezialtabelle für die Umgebung des galak-

tuschen Pols wird auch gegeben

E. C. Pickering<sup>4</sup> gibt nach A. Searle oine Tafel für galaktische Länge und Breite gemäß der Lage des Pols  $A=490^\circ$ ,  $D=+28^\circ$  (1900) Die Intervalle sind  $40^{\rm m}$  in  $\alpha$  und  $10^\circ$  in  $\delta$ 

O. R WALKEY hat cine Tafel für die Lage des Pols A = 12h 47m, D = +27°

und mit den Intervallen 1h und 10° gegeben

E. L. Johnson<sup>6</sup> hat unter Verwendung des Newcombschen Pols,  $A = 191^{\circ}, 1$ ,  $D = +26^{\circ}, 8$ , eine Tafel mit Intervallen 20<sup>m</sup> in  $\alpha$  und 5° in  $\delta$  berechnet.

A PANNEKORK gibt in seinem oben reierlerten Werke "Die nördliche Milchstraße" eine Tafel gemäß dem MARTHSchen Pol und mit denselben Intervallen

wie in Johnsons Arbeit.

J. Plassmann gibt in seinem Werke "Die Milchstraße" Tafeln mit den Argumenten  $\alpha - \Omega$  und  $\delta$  in Intervallen von  $6^\circ$ , wo  $\Omega$  die  $\Lambda$  R. des aufstelgenden Knotens der Milchstraße ist Ein paar Differentlaltafeln lassen die Korrektionen in L und B für eine andere Deklination des Pols als die zur Konstruktion der

Haupttafeln gewählte +27° 26' berechnen.

7 Lund Obs Ann 3 (1932).

Eine Tafel, die nach Intervallen von 1° in  $\alpha$  und  $\delta$  fortschreitet, ist von C. V. L. Charlier auf der Sternwarte Lund ausgearbeitet worden. Die angenommene Lage des Pols ist hier  $A=190^{\circ}$ ,  $D=+28^{\circ}$  (1900) Die gonauesten gegenwärtig existierenden Tafeln sind später von derselben Sternwarte veröffentlicht worden. Die Arbeit geschah unter Leitung von J. Ohlsson, der auch ein Vorwort zu den Tafeln geschrieben hat. Für jeden ganzen Grad in  $\alpha$  und  $\delta$  werden L und B auf ein Hundertstel des Grades gegeben. Außerdem wird der Winkel  $\varphi$  zwischen Doklinationskreis und galaktischem Breitenkreis gageben, um die Berechnung der Eigenbewegungskomponente längs der galaktischen Koordinatenkreise zu erleichtern. Die Lage des Pols ist die eben er

<sup>1</sup> MN 33, S. 1 u. 517 (1872), 34, S. 77 (1873), 53, S. 74 u 384 (1893)

Vgl. PANNEKOER, Pop Astr 5, 8, 395, 485 u 524 (1898)
Groningon Publ Nr 18 (1908)
Harv Ann 56, S. 5 (1912)
MN 74, B. 201 (1913)
Union Circ 29, S. 226 (1915)

wahnte, aber ausführliche Reduktionstafeln zur Erleichterung des Übergangs

auf einen anderen Pol werden auch gegeben

P EMANUELLI hat ausfuhrliche Tafeln mit Angabe der Zehntelgrade m L und B gegeben Die Tafel schneitet nach Intervallen von 10m in a und 1° in  $\delta$  fort und 1st gemaß dem Newcombschen Pol  $A=12^{\rm h}$  44m,  $D=126^{\circ}$ ,8 (fur das Jahr 1900 gultig angenommen) konstruiert worden. Die galaktische Lange wird hier vom Sonnenaper ( $\alpha = 270^{\circ}$ ,  $\delta = +30^{\circ}$ ) gerechnet Der Vertasser gibt in der Emleitung eine ausführliche Bibliographie über Tafeln zur Berechnung galaktischer Koordinaten und über die verschiedenen Bestimmungen der Lage des Milchstraßenpols

P J van Rhijn² gibt fin jede Stunde in a und jeden Grad in δ die galaktischen Koordinaten in einem System, dessen Pol mit dem Pol der schwachen Sterne (m > 8),  $A = 194^{\circ}$ ,  $D = +25^{\circ}$ ,5 (1900), ubereinstimmt Eine Spezialtabelle gilt fur die Umgebung des galaktischen Pols Außerdem werden Differentialtafeln entspiechend Verschiebungen des Pols in Übereinstimmung mit den Resultaten fur die helleren Steine (heller als m = 4, 5, 6, 7 resp.) gegeben

Graphische Verwandlungstafeln sind von II Selliger, P Stroobant, H NORTS, J. A PEARCE und S N HILLS publiziert worden Zu diesen kommen auch em paar Karten von O SEYDL, "Maps of the Boundaries of the Constellations

in the Galactic System of Coordinates "7, gerechnet werden

R INNES<sup>8</sup> und nach ihm H Philippor<sup>8</sup> entwickeln die Vorteile, an Stelle der "mittleren" Örter der Gestiene die galaktischen einzustühren. Innis gibi Formeln und Tafeln zur genauen Übertragung mittlerer Orter der Jahresanfange zwischen 1750 und 1950 in galaktische Kooldinaten unter Zugrundelegung de-Newcombschen Pols der Milchstraße Die galaktischen Längen werden vom Sonnenaper  $\alpha = 270^{\circ}$ ,  $\delta = +30^{\circ}$  (1900) getablt. Et gibt auch eine Specialtafel zur duekten Verwandlung der schembaren Orter für das Jahr 1913 in "mittlere" galaktische Mehrere Beispiele, unter anderem fur Polaris und Polarissima, sind gerechnet worden Eine neue Bezeichnung der Steine schlägt Inni s auch voi Es sollten also an Stelle etwa der Benennung nach BD die helleren Sterne in den Vierecken sukzessiver Grade der galaktischen Lange und Biette nach der Lange numeriert weiden Eine Bezeichnung

## 325°8°8 oder 325, 8, 8

bezeichnet also den achten Stern im Viereck zwischen Lange 325° und 326°, Breite +8° und +9° Negative Breiten sollten etwa durch Kursivstil aus-

gezeichnet werden

Eine Konsequenz der Benutzung galaktischer Kooldinaten ist natuigemäll. daß auch die Bewegungskomponenten der Sterne im galaktischen Koordinatensystem Ausdruck finden Formeln und Tafeln zur Beiechnung von galaktischen rechtwinkligen Bewegungskoordinaten, wenn Parallaxe, Eigenbewegung in RA und Dekl samt Geschwindigkeit im Visionsradius gegeben sind, hat kürzlich A Kohlschütter<sup>10</sup> veroffentlicht Die Lage des Pols wurde zu R A 190°. Dekl +27° angenommen In einer Spezialtafel weiden aber auch Verbesserungen

<sup>2</sup> Groningen Publ Nr 43 (1929) Sitzber d K Bayer Akad d Wiss, Math-Phys Kl 16, S 220 (1886)

<sup>4</sup> Annales Obs Roy de Belg 11, S 97 (1908) 5 Recherches astron de l'Observatoire d'Utrecht VII (1917)

10 Veröff Univ-Sternw Bonn Nr 22 (1930)

Pubblicazioni della Specola Vaticana, Ni XIV, Appendice prima (1929)

Publ Astroph Obs Victoria 4, Nr. 4 (1927)
 Publ Obs Nat de Prague Ni 5 (1928)
 Union Circ 2 (1912)
 5, 6 (1913)
 Annuaire de l'Obs Roy de Belg 1923
 5 155

zu den neun Übertrugungskoeilizienten der Geschwindigkeitskomponente bei Übergang zu einem anderen galaktischen Pol gegeben. Eine Sterntafel enthält die Koeffizienten für alle Sterne, deren Radialgeschwindigkeit zur Zeit bekannt wur

## e) Der Einfluß der diffusen Nebel auf das Milchstraßenbild.

18. Die galaktischen Nebelfelder. Die Photographie hat uns in unverkennbarer Welse gezeigt, daß der Milchstraßengürtel nicht nur eine von Sternen byvorzugte Region des Himmels ist, sondern auch reichlich leuchtende und dunkle, unregelmälig begrenzte Nebelmassen enthält. Die Felder der leuchtenden Nobel sind in der Rogel als Gebieto eigenartiger Struktur der Milchstraße ausgezeichnet. Die helle Nebelmasse selbst ist oft dicht mit Sternen, bisweilen von beträchtlicher Holligkeit, besät. Gebiete auffallend kleiner Sternanzahl eratrecken sich gewöhnlich in unregelmäßiger Weise um die hallen Partien herum Lis ist offenbur, dall mun diese Reduktion der Sternfülle am emfachsten als einen Absorptionseffekt dunkler nobliger oder staubförmiger Massen auf das Licht entfernterer Sterne erklären kann, da wir andernfalls sehr langgestreckte, von uns aus radial gerichtete Lücken durch das Sternsystem hindurch in der Umgebung der hellen Nebel annehmen müßten, und das würde eine sehr unwahrschemliche Anordnung bedeuten1 Damit haben wir auf die Existenz mächtiger, nichtleuchtender Mussen geschlossen, die imstande sind, allgemeine Absorption oder Diffusion des Lichtes auszuüben. Solche Massen sind aber nicht notwendig nur in Verbindung mit leuchtenden Nobeln vorhanden, sondern verraten oft ihre Existenz nur durch ihre Absorptionswirkung als dunkle, an Sternen auffallend urme Gebiete, die gegen den hellen Hintergrund der Milchstraße kontrastieren

In diesem Zusammenhang mag erwähnt werden, daß die Luminiszenz der hellen Nebelpartien wahrschemhelt von der Einstrahlung naheltegender Sterne lucilingt ist. V. M SLIPHER fand, daß für Merope, Mala, Q Ophiuchi, NGC 2068 und 7023 das Spektrum der Nebelmasse wenigstens ungefähr mit den Spektren der hellsten eingehüllten Sterne übereinstimmt E HERTZSPRUNG hat die Theorie einer partiellen Reflexion oder Streuung durch Photometrierung der Plejadenneled zu prüfen gesucht; er findet, daß die Flächenhelligkeit der Nebal an ihren hellsten Stellen um etwa 4 his 5 Sterngrößen schwächer ist, als sie bei vollständiger Strouung des Lichtes des Zentralsterns an den betreffenden Punkten sein würde II N Russkl.L4 hat die Reflexionstheorie für die galaktischen Nebel aufgenommen und weiter die Hypothese aufgestellt, daß auch die Nebel mit Linlenspektren durch das Licht von nahehegenden Sternen zur Strahlung erregt worden. R. Hunnand hat diese Theorien auf Grund eines größeren Materials geprüft und im allgemeinen Durchschnitt gute Bestätigung gefunden. Er hebt horvor, daß in den hellen diffuson Nebeln fast immer Sterne zu finden sind, die mit der Nebelmasse in deutlicher Verbindung stehen. Wenn das Sternspektrum vom Typus O-130 ist, strahlt der Nebel mit Linienspektrum, aber wenn der Spektraltypus des Sterns ein späterer ist, erscheint das Nebelspektrum kontinuierlich

HUBBLE findet auch einige interessante, aber weniger klar ausgesprochens Verschiedenheiten zwischen Nebela mit Linienspektrum und Nebela mit kontinuierlichem Spektrum. Die Netzwerknebel haben gewähnlich Linienspektrum,

<sup>1</sup> Vgl. Ziff. 22. ■ Lowell Obe Bull Nr 55 (1912), Nr 75 (1916); Publ ASP 30, S 63 (1918); 31, S. 212

<sup>(1919)</sup>A N 195, S 449 (1913)

Wash Nat Ac Proo 8, S. 115 (1922), Obs. 44, S 72 (1921)

Wash Nat Ac Proo 8, S. 115 (1922), Obs. 44, S 72 (1921)

Mt Wilson Contr 241 = Ap J 56, S. 162 (1922), 250 = Ap J 56, S 400 (1922)

und die mehr regelmaßigen, wolkenartigen ein kontinuierliches. Die kontinuierlich strahlenden sind mit großeier Verdunklung verbunden, obgleich schwei-wiegende Ausnahmen von dieser Regel in dem Orionnebel und in NGC 7000 (Amerikanebel) gefunden werden. Die hellsten Nebel haben Linicnspektrum, die ausgedehntesten kontinuierliches Spektrum. Die letztere Klasse hat die starkere Tendenz zu einer Konzentration um in den Nebel eingehullte Sterne

Auch die allgemeine Verteilung der hellen dissusen Nebel am Himmel ist von Hubble diskutiert worden. Diese Verteilung ist nicht einsach eine Konzentration gegen die galaktische Ebene. Zwei verschiedene Guitel sind zu unterscheiden, die Milchstraße und ein Gurtel, der gegen den galaktischen Kreis um ungefahr 20° geneigt ist. Die Knoten sallen ziemlich genau mit denen der hellen Heliumsterne zusammen, aber die Neigung der Nebelschicht ist eineblich großei. Die Verbindung zwischen Nebeln und Heliumsteinen wird jedoch durch diese Verteilung sehr augenscheinlich. Wir wollen im solgenden einige hei vorragende Nebelselder, die für die scheinbare Milchstraßenstruktur von Bedeutung sind, kurz erwähnen.

Em heller Nebelschleier, der auf Milchstraßenaufnahmen der Perseusgegend (Abb 4) in markanter Weise hervortritt, ist NGC 1499 Dieser Nebel befindet sich am sudlichen Rande der Milchstraße etwas nordlich vom Stein  $\xi$  Perser (Spektraltypus Oe5), der wahrscheinlich der erleuchtende Stein ist. Der Nebel liegt nahe der weitgestreckten dunklen Masse zwischen i Tauri und  $\varepsilon$  Perser Diese Masse ist in nordlicher Richtung durch einen feinen Kanal mit einer dunklen Höhle einige Grade westlich von  $\alpha$  Aurigae, ziemlich auf der Zentrallmie der Milchstraße, verbunden und hat in sudlicher Richtung Verbindung mit einer sehr dunklen Partie nordlich von  $\tau$  Tauri, die sowohl in östlicher Richtung gegen  $\beta$  Tauri als in westlicher Richtung gegen die Nebelpartien um o Perser her um schmale Kanale aussendet. Wir sind hier schon in betrachtlich sudliche galaktische Breite geführt. In der Nahe erscheint die in Nebel eingehullte Plejadengruppe

Eine Fortsetzung der eben genannten Nebelpartien, die augenscheinlich der gegen die Milchstraße um 20° geneigten Nebelschicht angehören, bilden die

Nebel in der Oriongegend

Ziemlich in dei Zentrallinie der Milchstraße finden sich in dieser Gegend die interessanten Nebel um S Monocerotis (Abb 5) und um 12 Monocerotis herum Der letztere Nebel erscheint am Rande einei Dunkelregion, die gegen Orion hinzieht

Im sudlichsten Verlaufe der Milchstraße ist von allem zu erwähnen die mächtige und sehr helle Nebelmasse NGC 3372 um  $\eta$  Cannac herum², die nahe zentral in der Milchstraße gelegen ist, wo diese sich zu einem schmalen hellen Lichtstrom verjungt. Die scharfe Einbuchtung der Milchstraße sudöstlich von diesem Nebel ist wohl mit großter Wahrscheinlichkeit einer nebularen Absorption zuzuschreiben. Nach der Franklin-Adams-Karte scheinen  $\lambda$  Contaun und naheliegende Steine am Rande der hellen Partie in helle Nebel eingehullt zu sein. Von dunklen Gebieten ist aber in dieser Himmelsgegend vor allem zu bemei ken der "Kohlensack" ostlich von  $\alpha$  und  $\beta$  Crucis. Nahe an  $\alpha$  und im nördlichsten Teil unweit von  $\beta$  ist das dunkle Gebiet sehr arm an Sternen, in sudwestlicher Richtung erstreckt sich vom Dunkelgebiet aus ein schmaler Kanal, der sich auf mehrere Grade hin verfolgen laßt

In den Sternbildern Norma, Ara und Scorpius wird die sich erweiternde Milchstraße in sehr komplizierter Weise von dunklen Flecken und Kanalen

<sup>1</sup> Vgl auch Aufnahmen von Ross, Ap J 67, S 281 (1928)

<sup>&</sup>lt;sup>2</sup> Vgl Franklin Adams Karte oder Harv Ann 80, Pl IV (1908)

zerrissen Es ist sehr wahrscheinlich, daß die sukzessive Abspultung der zwei westlichen Milchstraßenäste in dieser Gegend auf Absorption durch dunkle Massen zurückzuführen ist. Von deutlichem Nebelcharakter erscheint eine komplizierte. vielfach in Kanale aufgelöste, langgestrechte dunkle Region, die vom Schwanze des Skorplons nördlich von 1 und v Scorpli in westlicher Richtung den westlichen Milchstraßenast durchquert, um in der Gegend von n und O Luri ein ziemlich weitgestrecktes dunkles Gebiet zu bilden, an dessen stidlichem Rando der Sternhaufen NGC 6124 golegen ist Von diesem Gebiete gehen schmale Kanale weiter nach Westen Im ganzen zeigt die Nebelpartie eine gewisse Ähnlichkeit mit den waiter nordlich gelegenen Nobeln, die mit dem hellen Nebel um p Ophlucht m Verbindung stehen.

Die hellen Nebel in Scorpius und Ophluchus bilden gewissermaßen ein Gegenstück zu den Nebeln in Orlon, da sie in beinahe entgegengesetzter Richtung am Himmel erscheinen und also im ganzen eine erhebliche westliche Abweichung von der zentralen Milchstraßenlinie zeigen. Von außerordentlichem Interesse ist die Nebelmasse um o Ophinchi und 22 Scorpii herum, die vielleicht auch in ciniger Verbindung mit den Nebeln um o und > Scorpii herum steht. Von diesem Nobel gehen nach Oston hin mehrere dunkle Kanale. Einer von diesen geht auf den westlichen Ast der Milchstraße in Ophiuchus zu, teilt sich dort in einen nördlichen und einen südlichen Ast, so daß das ganze Gebilde fast die Form eines gewaltigen Ankers orhalt (vgl Ziff 9). Der südliche Ast enthält die außerordentlich dunkle Partie südöstlich von O Ophiuchi. Der nördliche Ast spaltet einen Zweig in östlicher Richtung ab, der gegen den Sternhaufen M23 hinkuft, aber von diesem Haufen in südlicher Richtung umbiegt und sich dann in der großen dunklen Mittelpartie zwischen den Milchstraßenasten verliert.

Die dunkle Region zwischen den Milchstraßenästen in Sagittarius enthält am östlichen Rande die zwei schönen Nebel M81 und M20 (NGC 6523 und 6514); der letztere ist der berühmte Trifidnebel\*. Sie stehen an der Spitze einer Reihe von kleineren Sternweiken, die von der Scutumgegend über # Sagittaril hin laufen, und die von einer "grobkörnigeren" Struktur als die umgebenden großen Wolken in Sagittarius und Ophiuchus zu sein scheinen. An die helle kleine Wolke in der Nahe von "Sagittarii schließt sich im Süden ein dunkles Gebiet, das die Nebel NGC 6589 und 6590 anthalt. Im nordlichen Teil derselben Walke erscheinen die bekannten dunklen Nebel BARNARD 92 und 93. An die genannte Wolkenreihe schließen sich auch der Nebel M17 (NGC 6618) und der neblige Haufen M16 (NGC 6611) an, aber vor allem welter nordlich der Nobel IC 1287 (um den Stern Boss 4687), der auf allen Selten in weite Sternleeren übergelit, zu demen die großen, die Milchstraße durchquerenden Kanäle sädlich von der Scutumwolke gehören.

Es ist wohl kaum zu bezweifeln, daß der große, in Ziff, 9 besprochens dunkle "Keil", der in die Milchstraße in Ophluchus von Westen her einsetzt und die Aufspaltung der Milchstraße in Ophluchus und Aquila bewirkt, in der Lichtabsorption dunkler Massen seinen Ursprung hat. Eine Verbindung der absorblerenden Massen mit dem o Ophluchi-Nebel scheint nicht ausgeschlossen. Dieselbe Erklärung folgt dann mit großer Wahrscheinlichkeit für den dunklen "gebeugten Arm" der Cygnusgegend, der in seinem oberen Teil den "Nord-

amerika-Nebel" und die hellen Nebel um y Cygni herum enthält.

Es liegt nahe zu bemerken, daß die zwel letztgenannten dunklen Gebiete von nördlicher galaktischer Breite her in der Richtung wachsender galaktischer Lange in die Milchstraße hineinreichen, während die entsprechenden dunklen

Vgl. Aninehme von DUNCAR, Mt Wilson Contr 177 - Ap J 51, 8. 4 (1920).

Trennungsmassen der Milchstiaßenaste in Scorpius und Norma von überwickend nordlicher Breite gegen abnehmende Lange hinzichen. Man kann aus dieser Tatsache allem Veranlassung haben, den Schluß zu ziehen, daß die neblige Materie unserer nachsten Umgebung in großerer Haufigkeit in einer Ebene betrachtlicher Neigung gegen die Milchstraße verteilt ist, und daß diese Islame thre größte galaktische Breite in der Scorpius-Ophiuchus-Gegend erreicht Es scheint, daß ein wesentlicher Teil der dunklen Nebelmassen, die die Miklistinßezwischen α Centauri und α Cygni zeistuckeln, als Ausläufer einer solchen Schicht anzusehen ist, und daß besonders der westliche Ast in dieser Milchstraßengegend durch die Nahe an dei Absorptionsebene in seiner mittleren Lichtstäuke reduziert worden ist Wenn wir die Knoten der Ebene in Crux und Cassiopeia annehmen, scheint es moglich, viele der großten verdunkelten Gebiete anderer Gegenden als zur genannten Nebelschicht gehorig anzusehen. Es ist abei auch deutlich ersichtlich, daß die Zweiteilung der Milchstraße in Scorpius, Sagittarius und Ophiuchus zum Teil auch auf in der zentralen Milchstraßenebene orientierte dunkle Massen zuruckzufuhren ist, und wir haben somit eine doppelte Verteilung der dunklen Massen gefunden, die der vorher besprochenen Verteilung der hellen diffusen Nebel durchaus ahnelt

Der nordlichste Verlauf der Milchstraße ist reich an umegelmäßigen dunklen Gebilden, die bis in die Perseusgegend hauptsachlich auf der Nordseite der zentralen Milchstraßenlinie gelegen sind So haben wir den "Kohlensack" nörd» lich von der klemen Cygnuswolke mit seinem in südlicher Richtung den "Haupt» strom" der Milchstraße durchquerenden schmalen Kanal, den dunklen Fleck östlich von  $\delta$  Cepher und das langgestreckte dunkle Gebiet westlich von  $\beta$  Cassioperae

In der ostlichen Milchstraßenpartie in Cygnus eischeinen A. B. die zwei wahrscheinlich zusammengehorigen Netzweiknebel NGC 6960 und 6992 Daß die Nebelschlinge 6960 auf der Außenseite, von 6992 aus gerechnet, von dunklen Nebeln begleitet ist, die eine merkliche Absorption austiben, ist besonders auf J C Duncans<sup>1</sup> Aufnahme mit dem Hooker-Teleskop deutlich zu erkennen

(vgl M Wolf, Ziff 22)

Östlich von der in unserer allgemeinen Beschichbung dei Milchstraße er wähnten Durchquerung des Hauptstromes bei A Cygni haben wit eine schwächtte bei  $\pi_1$  und  $\pi_2$  Cygni Dieser Kanal steht mit einem eigenatigen Nebel in Verbindung Aus einer ziemlich großen dunklen Höhle geht in sudöstlicher Richtung ein ziemlich langer, kanalartiger, sternarmer Streifen heivor. In dessen öst lichem Ende liegt ein heller, rundlicher Nebelfleck2, der sog "Kokon-Nebel" (IIC 5146) Wir sehen hier in einem kleinen Maßstab, abei in sehi deutlicher Weise, eine Art Verbindung zwischen leuchtender und dunkler Nebelmaterie. die wir schon mehrmals, nur in etwas verschiedenei Form, gefunden haben. 128 scheint, als ob die helle Nebelpartie sich fortbewege, einen Schweif von allmählich sich weit verbreitender dunkler Materie hinterlassend. Die oben genannte Durchquerung besteht aus einem fast geradlinigen, zei hackten Zug von dunklen Stellen, der in nordlicher Richtung hinzieht und bei dem Stein 14 Cephei in einen sehr dunklen eirunden Fleck, BARNARD 169, ausmundet Diesei Fleck liegt am stidlichen Rande der Cepheuswolke

Westlich vom eben genannten Fleck und sudlich von  $\mu$  Cephei liegt ein  $\mathbf{m}$ ausgedehnte schwache Nebel gehullter Sternhaufen um den Stern 13 H Cepher (Oe5) herum Diese Gegend zeigt eine Menge schmaler, tiesdunklei Kanäle und Flecke und wird ringsum von großeren dunklen Partien umgeben (vgl BARNARD. "A Photographic Atlas etc ", Pl 49)

<sup>&</sup>lt;sup>1</sup> Mt.Wilson Contr 256 = Ap J 57, S 137 (1923) Wolf, Die Milchstraße und die kosmischen Nebel, Pl III

14. Dunkle, wohl marklerte Flecke im Sternstratum Manchmal schr scharf begrenzte, tiefdunkle Flecke treten oft in außerordentlich auffälliger Weise gegen den Hintergrund einer sternreichen Gegend hervor Schon A. Secchi hat auf tiefschwarze Höhlen in den Sternwolken in Sagittarius aufmerksam gemacht, und G F Chambers zählt solche Flecke auch in Scorpius auf. Eine kleine schwarze Höhle von nur 2' Durchmesser in der Sagittariuswolke (B 86) wurde von Barnard im Jahre 1883 durch visuelle Beobachtung entdeckt Diese Höhle hat den kleinen Stornhaufen NGC 6520 unmittelbar auf der östlichen Selte und erscheint daher in besonders starkem Kontrast gegen ihre Umgebung Barnard hat sich dann besonders einem Studium der dunklen Flecke auf photographischem Wege gewidmet und schließlich einen Katalog und eine Beschreibung für 182 Objekte dieser Art gegeben Sein photographischer Atlas der Milchstraße enthält auch reichlich Bemerkungen tiber diese Objekte Es ist selbstverständlich, daß für die Erklärung dieser Flecke nur die Absorptionshypothese ernstlich in Frage kommen kann

Ein systematisches Aufsuchen dunkler Flecke des Himmels ist kürzlich mit Hilfe der Franklin-Adams-Platten von K. Lundmark und P J Melotte ausgeführt worden Eine Karto, welche die Verteilung der 1550 gefundenom Objekte zolgt, hat Lundmarks gegeben. Er schätzt das ganze Arenl der dunklen Flecke auf ungefähr 850 Quadratgrade, was etwa 1.50 des ganzen Himmels ontspricht

Man muß bei der Deutung dieses Resultats die Bemerkungen vorausschicken, erstens, daß nicht alle Flecke notwendigerweise durch Absorption in dunklen Massen hervorgerufen sein müssen, sondern biswellen wurklichen sternleuren Regionen im Raume entsprechen können, was auch von Lundmark hervorgehoben wird, zweltens aber, daß eben die größten verdunkelten Gebiete des Himmels, deren Gronzen verwaschen oder mehr unregelmäßig definiert erscheinen, z. B das große Absorptionsgebiet in Ophfuchus, mituater nur durch ihre dunkelsten Gebiete repräsentiert werden.

Die Verteilung der dunklen Mecke zeigt eine große Frequenz in der südlichen Milchstraße zwischen Carina und Aquila, wie auch eine große Häufigkeit in der Orlongegend (südliche galaktische Breite) und in der Copheus-Cassiopeia-Gegend (nördliche galaktische Breite) Das Auftreten von Flocken auch in sehr beträchtlicher galaktischer Breite hat H. Shapling veranlaßt, für 50 Regionen hoher galaktischer Breite die Verteilung schwacher Sterne auf Harvard-Platten zu untersuchen Nur für eines der untersuchten Gebiete (östlich von  $\mu$  und b Serpentis) wird eine Absorption durch Dunkelwolken bestätigt; die Sterne, die schwächer sind, als es der Gronzgröße der Franktin-Adams-Platten entspricht, zeigen für andere Regionen eine wesentlich gleichförmige Verteilung. Shapling hat vorher ein ähnliches Resultat für eine sternarme Region auf den Karten der Pariser Astrographischen Zone, auf die von E Öpik und M. Lukks hingewiesen worden war, gefunden.

15. Hagges dunkle Nebel. Auf die Existenz dunkler Nebelwolken, die wesentlich außerhalb der Milchstraße auftroten und dort ein zusammenhängendes

<sup>1</sup> A N 41, S. 238 (1855).

Descriptivo Astronomy, 3rd ed. Oxford 1877.

A N 108, S. 369 (1884)

Ap J 49, S. 1 (1919).

Pop Astr Tidakr 7, S. 18 (1926) — Upsala Medd 12; Studies of Anagalnotic Nebulac,
N Acts Rog Soc. Scientiarum Upsal, Volumon extra ordinem editum (1927), Upsala

Medd 30, Pl. I,

Harv Bull 844 (1927).

Harv Circ 281 (1925).

Publ Ohe Univ de Tartu (Dorpat) 26, Nr 2 (1924)

Gewebe ahnlich den Gestaltungen irdischer Wolken bilden, hat J G Hagen<sup>1</sup> aus umfangreichen visuellen Beobachtungen mit dem 16zolligen Refraktor der Vatikan-Steinwarte geschlossen Schon W Herschel's hatte 52 weit ausgedehnte milchige Nebelgebilde angegeben, die in allen galaktischen Breiten aufticten, und die zusammen sieher wert mehr als 150 Quadratgrade des Ilmmels bedecken In neuerer Zeit ist aber für diese Felder nur im Ausnahmefallen auf photographischem Wege die Anwesenheit von Nebelmaterie nachgewiesen worden3 Hagens Nebel umfassen auch die Herschelschen. Sie haben eine graue neutrale Farbung und fur die Dichte oder Trubung der Nebel hat HAGEN eine Skala von fünf Stufen eingefuhrt, deren Nummern mit dem Trübungsgrad wachsen Stufe V entspricht also den dichtesten, "fast alle Steine verdunkelnden" Partien In der Durchmusterung der Nebel wurde das Fermohr auf volle Grade in R A eingestellt und in Dekl, bewegt Das Gesichtsfeld hatte 25' Durchmesser Die Beobachtungsmethode besteht in einem Überfahren ("sweeping") eines Streifens benachbaiter Gebiete.

Das Hauptresultat der Hagenschen Untersuchungen ist, daß die dunklen Nebel ein zusammenhangendes Netzwerk bilden, das aber von kanal- und ovalformigen Lichtungen vielfach durchbrochen ist. Sie bevorzugen die außeigalaktischen Regionen des Himmels, kommen aber auch in der Milchstraße vol. Da der geschatzte Trubungsgrad augenscheinlich auf der Sternfulle beruht, so ist es von voinheiein klar, daß eine negative Koirclation zwischen Dichte des Nebels und Sternanzahl zu erwaiten ist

Die hellen Nebelflecke der außergalaktischen Regionen finden sich selten ınnerhalb großer Wolkenkontmente, sondern meist an derem Rande oder wo die Dichte sich schnell verandert. Große Wolkengebiete eischeinen oft von Sternketten umsaumt

HAGEN schließt, daß unser Milchstraßensystem von einem dunklen Nebelmeer eingehullt ist, das auch die hellen außergalaktischen Nebelflecke umfaßt Er sucht auch in weitgehender Weise die kosmogonische Stellung der dunklen Nebel aufzuklaren, nach ihm waren die dunklen Nebel der Uistoff der ursprünghch kalten und dunklen Riesensterne, die sich in dem Lockyer-Hertzsprung-Russellschen Schema weiterentwickeln

Die Resultate von Hagen sind von F Becker und J Stein daigelegt und verteidigt worden J Hellerich und V Cerulli7 haben zusammenfassende Übersichten gegeben

<sup>&</sup>lt;sup>1</sup> Mem SAIt 1 (1920), MN 81, S 449 (1921), AN, Jubil-Nr (1921), 213, S 351 (1921), 214, S 449 (1921), Naturwiss 9, S 935 (1921), Scientia 31, S 185 (1922), Publ A S P 34, S 320 (1922), Atti Pontif Accad Sci 75, S 71 u 83 (1922), 76, S 31, 89 u 200 (1923). 77. S 131 (1924) (Durchmusterung und kleinere Notizen), Specola Astronomica Vaticana, Miscellanea Astronomica 1, parto 3 (1924) (Neudruck älterer Abhandlungen), A N 224, S 421 (1925), 225, S 129 u 383 (1925), Specola Vaticana X (1922, 1925 u 1927) (Katalog), M N 86, S 144, 146, 349, 439, 548 u 642 (1926), A N 227, S 391 (1926), B Z 23 (1927), Atti Pontif Accad Sci 80, S 51 u 94 (1927), A N 229, S 303 (1927), 230, S 325 (1927), M N 87, S 106 (1926), Publ A S P 39, S 167 (1927), Attı Pontif Accad Sci 81, S 343 (1928), 82, S 263 (1929), B Z 16 (1929), Pop Astr 37, S 284 u 395 (1929), A N 235, S 313 (1929), M N 90. S 331 (1930), außerdem "Die Nebelstraße", Anhang zu der Monographie "Die Milchstraße" von Plassmann (1924), "Das photographische Problem der Nebelwolken", Festschrift Stella Matutina II (1931), Miscellanea Astronomica 6, No 93 (1931)

Phil Trans S 269 (1811), Coll Scientific Papers II, S 459 8 Vgl besonders Mrs I Roberts, I Roberts' Atlas of 52 Regions A Guide to Herschel's Fields Preface by J G HAGEN Paris 1928

<sup>4</sup> A N 223, S 303 (1925), 224, S 113 u 235 (1925), 225, S 129 (1925), Die Sterne, S 97 (1926), Specola Astronomica Vaticana XIII (1928), Dunkelwolken in der Umgebung von NGC-Objekten <sup>5</sup> V J S 61, S 250 (1926)

<sup>&</sup>lt;sup>6</sup> Naturwiss 14, S. 107 (1926) <sup>7</sup> Scientia 40, S 133 (1926)

Es hut aber auch nicht an Einwänden gegen Hagens Deutung seiner Beobachtungen gefehlt. So besteht die Schwierigkeit, daß auf langexponierten Platten unter Verwendung von lichtstarken Instrumenten keine den Nebeln entsprechende Struktur hervortritt. Dieser Schlaß kann aus den ausgedehnten photographischen Arbeiten, z B von BARNARD, WOLF und HUBBLE, gezogen werden, da diese keine diffusen Nebel in hohen galaktischen Breiten nachgewiesen haben. N Iva-NOVI konstatierto kürzlich dassalbe Sachverhältnis für die Hagenschen Nebelwolken bei V und UW Draconis und bei R und S Tauri LUNDMARK hebt unter anderent herver, daß Fehlerquellen wie Tierkreislicht, Erdlicht, physiologische Effekte, Farbengleichung des Instrumentes einwirken können Er schlägt vor. daß Hagens Beobachtungen von anderen Beobachtern, in einem anderen Khma, mit Teleskopen von größerem Öffnungsverhältnis und größerem Feld wiederholt werden sollten

Angosichts der großen Schwierigkeiten, die eine Einpassung des "Nebelmeors" in unser Weltbild verursacht, ware es wohl jedenfalls angemessen, eine weniger revolutionierende Erklärung des beobachteten Phänomens zu suchen. WIETZ sloht in den Beobachtungen der Hagenschen Nebel Stufenschätzungen der scheinbaren Heiligkeit des Himmelsgrundes. Der negative Korrelationskooffizient r zwischen Dunkelstufen und Sterndichtigkeit wird numerisch um so größer, je schwächer die Sterne der verglichenen Sternzählungen sind Bei der Grenzgrille 11,0 ist r = -0,16, bel 14,5 ist r = -0,64. Es hert also in Hagens Resultaten ein engmaschiges Netz grober schematischer Sterneichungen vor Praktisch denselben Schluß hat auch Shapley aus ahnlichen Überlegungen gezogen. HAGEN und Bucker lehnen jedoch diese Auffassung ab auf Grund von dem unmittelbaren subjektiven Eindruck, der direkt die unzweidentige Existenz der Wolken gewährleisten soll

Es scheint jedoch wohl noch die Möglichkeit zu bestehen, daß der schwache graue "Nobelschein", der keine Struktur auf den photographischen Platten glbt, als "lerdlicht" im weiteren Sinne (Ziff 5) erklärt werden kann, daß er nach HAGENS Angaben mit großer Stornftille im Felde zu verschwinden scheint, ware als ein physiologischer Kontrasteffekt zu deuten Es ist schon oben der Schluß gezogen worden, daß Sternanzahl und Trübungsgrad korreliert sein mitssen, da offenbar die Sternleere des Foldes als Maß der Trübung benutzt wird. Auf die Gefahr einer Selbsttäuschung bei der Einordnung benachbarter Sterne im Gesichtsfelde in "Ketten" sollte wohl auch hingewiesen werden,

Wenngleich eine "einfachere" Erklärung dieser Art gegenwärtig vielleicht vorzuziehen ware, verdienen doch ohne Zweifel die scharfen und kühnen Beobachtungen Hagens mit größtem Interesse aufgenommen zu werden, was besonders durch die zahlreichen Kommentare und Erklärungsversuche, z. B in neuester Zeit von H. Osthoffs, J. Hartmanns und J Hopmann, bewiesen wird.

## f) Die astrophysikalisch-statistischen Ergebnisse über die Natur der Milchstraße.

16. Die galaktische Konzentration der Sterne und die effektive Sterngröße des Milchetraßenlichts. Es ist seit drei Jahrhunderten eine wohlbekannte Tatsache, daß das Milchstraßenphänomen auf einem scheinbaren Zusammendrängen der Sterne gegen einen gewissen Gürtel des Himmels beruht Durch die

AN 239, S. G1 (1930).

<sup>&</sup>lt;sup>1</sup> Bulletin of the Observing Corp of the Soc. of Amateur Astronomers of Moscow <sup>8</sup> Publ ASP 34, S 191 (1922).

Nr 8, 8, 57 (1927)

A N 223, S 123 (1924); 224, S. 267 (1925), 225, S. 299 (1925)

A N 238, S. 233 (1930) AN 238, 8, 233 (1930) 4 Hary Ciro 281 (1925). 1 AN 238, S. 285 (1930)

Arbeiten von Houzeau, Seeliger, Schaparelli, Pickering, Straionoff u a wurde es auch klaigelegt, daß diese "galaktische Konzentiation" der Steine in allen Großenklassen zu finden ist, wenn auch die Steine der hellsten Großen sich eher gegen den Gouldschen Kreis (Ziff 11), als gegen die zentiale Milchstraßenlinie konzentrieren Jedenfalls wurden wir, wenn wir den ganzen Himmel betrachten, eine positive Korrelation zwischen Milchstraßenlicht und Steinanzahl finden, und zwar für alle Großenklassen, auch die hellsten. In diesem Sinne kann man sagen, daß das Phanomen der Milchstraße in allen Großenklassen widergespiegelt wird, wenn auch in weit höherem Maße für die sehr schwachen Größen als für die helleren.

HOUZEAU vergleicht nach der Uranométrie Générale die Sterndichtigkeit in verschiedenen galaktischen Zonen mitemander. Wenn man die Zonen —30° bis +30°, um die Milchstraße herum, mit den übrigbleibenden Kalotten des Himmels vergleicht, findet man nach Houzeau für die so definierte galaktische Konzentration den Wert 1,38 für die Größen 1 bis 3 und 1,22 für die Größen 4 bis 6

Pickering¹ hat aus den Milchstiaßenzeichnungen von IILis und Gouid eine rohe Intensitatstabelle tur das Milchstiaßenlicht hergestellt. Er gibt in einer Skala von zehn Stufen die mittleren Intensitaten für Intervalle von 1<sup>h</sup> in RA und 5° in Dekl. Wenn er die Sternzahlen, auf gleiche Fläche reduziert, in der Milchstiaßenzone (10999 Quadratgrade) und in den außergalaktischen Partien (25641 Quadratgrade) vergleicht, findet er bis zur Größe 7 eine nahe konstante galaktische Konzentration vom Betrage 1,85. Die Konzentration ist sogar für die hellsten Größen ein wenig starker

Kapteyn und van Rhijn definieren die galaktische Kondensation fur die Größe m als das Verhältnis zwischen der Anzahl der Steine von den hellsten bis zur Größe m pro Quadratgrad  $(N_m)$  in der Zone 0 bis 20° und der entsprechenden Anzahl fur die Zone 40° bis 90° Nach Searfs und van Rhijn² ergeben sich für sukzessive photographische Größen die Werte in Tabelle 8 Die Kondensation ist nahezu konstant bis zur Größe 10,0 und steigt dann allmählich, um für die schwachsten Größen sehr erhebliche Werte anzunehmen

Tabelle 8

111	Kond	211	Kond	3))	Kond
4,0	2,5	10,0	2,6	16,0	5,8
5,0	2,5	11,0	2,9	17.0	7,1
6,0	2,5	12,0	3,1	18,0	8,5
7,0	2,5	13,0	3,5	19,0	10,7
8,0	2,5	14,0	4,1	20,0	13,2
9,0	2,5	15,0	4,8	21,0	16,2

Im Raume betrachtet sehen wir den unmittelbaren Grund des Milchstraßenphanomens und des damit verbundenen, zum Teil aquivalenten Phänomens der
galaktischen Konzentration der Steine in einem Zusammendrängen der Steine
gegen eine gewisse Ebene, die galaktische Ebene, welche durch die Zentrallime
der Milchstraße definiert wird. Wenn aber die Milchstraße etwa einer gleichförmigen Verteilung der Steine in einem zweidimensional unendlichen Stratum
entspräche und keine Absorption des Lichtes in diesem Stratum vorauszusetzen
ware, so ist es leicht einzusehen, daß die effektive Steingröße oder die Größe,
welche der maximalen Gesamthelligkeit für Steine innerhalb einer Größenklasse

<sup>&</sup>lt;sup>1</sup> Haiv Ann 48, S 149 (1903)

<sup>&</sup>lt;sup>2</sup> Iransactions of the International Astronomical Union II, S 96 (1925)

entspricht, nach der Zentrallinie der Milchstraße hin eich gegen eine unendlich lichtschwache Größe verschieben würde, und daß gleichzeitig die Intensität gegen diese Zentrallinie anwachsen würde, so daß in der unmittelbaren Umgebung der genannten Linie selbst, wo die Sterne unendlich dicht gegeneinander gedrängt orscheinen würden, die Helligkeit sogar die photosphärische Helligkeit der Sterne erreichen sollte Die unmittelbare Beobachtung zeigt uns. daß die genannten Annahmen nicht zutreffend aud, was auf eine Begrenzung des Sternstratums oder auf Schwankungen der räumlichen Dichte hinweisen, aber auch durch eine Absorption des Lichts im interstellaren Raume bedingt sein kann. Mit größter Wahrscheinlichkeit sind alle drei Ursachen verhanden. Ohne Zweifel können wir jedoch a priori voraussetzen, daß die effektive Sterngröße der verschiedenen Partien der visuellen Milchstraße nicht überall dieselbe sein kann.

Wenn wir die Anzahl von Sternen zwischen den scheinbaren Größen 193 und m + dm mit a(m) dm bezeichnen, so ist offenbar  $a(m) \cdot 10^{-0.4}$  m sin Ausdruck für die Gesamthalligkeit dieser Sterne. Wenn wir also genügend genaue Sternzählungen zur Verftigung haben, so ist es leicht, den Anteil verschiedener

Größenklassen an der Gesamtlichtwirkung zu bestimmen

Für einen Quadratgrad der großen Sagittariuswolke hat S BAILEY1 eine Sternzählung bis zur 19 photographischen Größe vorgenommen Tabelle 9 gibt die Große /(m) gemäß der Formel

$$\log/(m) = \log a(m) - 0.4 m + 3$$

für sukzessive Größenklassen nach diesen Zählungen, a(m) ist hier die Anzahl Sterno zwiechen m-1 und m+1.

Man ersieht aus der Tabelle, daß nach Baileys Resultaten die in dieser Gegend wirksamsten Storne von der Große 15 und 16 sind, abor auch daß die Funktion f(m) sich ziemlich lang-

/(=) / (m) A 15 /(=) # 10,0 1,5 13,0 1,4 16,0 5,1

Tabelle 9

29 11,0 1,5 140 17,0 12,0 | 1,0 | 15,0 | sam mit der Größe andert. Der Antoll

der helleren Storne an dem Gesamtlicht ist daher auch nicht unerhoblich Für Größen heller als 10 wird jedoch die Anzahl Sterne so klein, daß es fraglich erscheint, ob die entsprechende Lichtmenge wirklich im wahrgenommenen kontinuierlichen Milchstraßenschein mitwirkt. Die effektive Größe des Milchstraßenlichts liegt daher hier wahrscheinlich nahe der Größe 15.

PANNEKOKK macht aber zu Balleys Stornzählung die Bemerkung, daß die daraus resultierende Totalhelligkeit (0,024 Sterne der Größe 0,0 pro Quadratgrad) viel kleiner ist als die ans dem Glanz der Wolke in Verbindung mit van Ruijns Messungen (Ziff. 5) ermittelte. Es ist deher möglich, deß Bailings Zahlen von der Große 17 ab zu klein sind, wahrscheinlich infolge des Zusammendrängens der Sterne auf der Platte, oder vielleicht, daß die Größenskala nicht ganz in Ordnung ist. Nach der ersten Alternative ware die effektive Größe noch schwächer als die oben golundene.

Es mag in diesem Zusammenhang von Interesse sein, die am meisten effektive Sterngröße verschiedener galaktischer Zonen gemäß den über alle Längen. gemittelten Sternzahlen, wie sie den Untersachungen über das "typische System" zugrunde liegen, zu ermitteln. In Tabelle 10 ist f(m) für die galaktische Breite 0° und 90° gemäß F H. Seares's Sternzahlen berochnet worden. Die effektive Sterngröße liegt offenbar nahe der Größe 13,0 für die galaktische Zone und nahe 8,5 für den galaktischen Pol.

BAN 4, S 39 (1927). 1 Hary Circ 242 (1922). Mt Wilson Contr 346 - Ap J 67, S. 67 (1928)

Die Beziehung der mittleren Sternzahlen zu der beobachteten Strahlung des allgemeinen Himmelsgrundes ist schon in Ziff 5 besprochen worden

HOPMANN¹ hat aus seiner Isophotenkarte unter Heranziehung der von H Henie<sup>2</sup> und H Nort<sup>3</sup> ausgearbeiteten Verteilung der Steine heller als 44<sup>m</sup>

Tabelle 40

5 0,49 0,14 13 0,90 0 6 ,55 ,16 14 ,88 7 ,62 ,17 15 ,82 8 ,68 ,18 16 ,72 9 ,75 ,18 17 ,60			-				
6 ,55 ,16 14 ,88 ,82 ,68 ,18 16 ,72 ,60 ,75 ,18 17 ,60	121					121	
11   85   15   19   36   12   89   13   20   26	6 7 8 9 10	,88 ,00 ,82 ,00 ,72 ,00 ,60 ,00 ,48 ,0 ,36 ,0	6   14 7   15 8   16 8   17 7   18 5   19	,16 ,17 ,18 ,18 ,17	36	6 7 8 9 10	-

den Anteil am Milchstraßenlicht der Steine heller und schwachei als 11<sup>m</sup> fur verschiedene Regionen zu bestim-Fui die Sagittainismen versucht wolke stimmt sein Resultat qualitativ mit dem oben gegebenen überein. Für andere Regionen ergibt sich ein relativ größerer Anteil der helleren Sterne als fui die Sagittariuswolke

Ohne sehr wertgehende genaue Sternzahlungen bis zu außer ordentlich

schwachen Gibßenklassen fur verschiedene Gegenden der Milchstraße konnen wir die Frage nach der effektiven Sterngröße nicht streng beantworten, und genugende Zahlungen dieser Art hegen noch kaum vor Da abei die Photographie weit mehr als die diickte Beobachtung die Umisse dei Milchstiaßenstruktur in isoliei te Steine auflöst, so liegt in der Milchstraßenphotographie wenigstens ein Mittel vor, eine obei e Gienze dei mittleien Helligkeit dei Steine in den Grenzgebieten der visuellen Milchstraße zu finden. Wenn wir auf den Photographien feststellen, fur welche Gienzgröße eine Struktur der Verteilung, den Umissen der visuellen Milchstraße entsprechend, zuerst hervortritt, konnen wir wenigstens den Schluß ziehen, daß die effektive Steingröße nicht meiklich heller als diese Gienzgioße sein kann Nach K Graff kann man annehmen, daß eist Steine von der Größe 13 abwarts die klare Begrenzung der Milchstraßenwolken hervor-1ufen Trotz des Umstandes, daß einige Einzelheiten der Milchstraßenstruktur schon bei helleren Größen hervortreten, können wir mit großer Sicherheit annehmen, daß die effektive Größe des Milchstraßenlichts, gemäß der oben gegebenen Definition, in den helleren Partien der eben erwahnten oder sogar einer noch schwächeren Größe entspricht

Für eine Deutung dei Wolkenstruktur der Milchstraße ist es übrigens von Bedeutung, festzustellen, für welche Sterngröße die scheinbare Verteilung der Sterne inneihalb der Milchstiaßenzone eine deutliche Kouelation mit dei Lichtverteilung der Milchstraße selbst zeigt. Sehr ausführlich ist dieses Problem von EASION<sup>5</sup> behandelt worden Er untersucht zuerst helle und dunklere Partien der Milchstraße in Aquila und Cygnus Fin die Steinzählungen lieseite sin hellere Sterne die BD das Material, und fur schwachere Sterne wurden die Sternzählungen von Herschel, Cei oria, Epstein und Wolf inneihalb dei betieffenden Regionen benutzt. Die sehr klaie Korrelation zwischen Steinzahl und Milchstraßenhelligkeit für die schwachen Steine bleibt in geringerem Maße auch für die BD-Steine schwacher als 9m bestehen, wahrend für hellere Sterne jede deutliche Korrelation verschwindet. In seiner spateren Arbeit vergleicht Easton den Dichtigkeitsgrad der BD-Steine nach der ausführlichen Bearbeitung dieser Sterne von W. STRATONOFF<sup>6</sup> mit dem Helligkeitsgrad der Milchstraße und erstreckt seine Untersuchung über den ganzen nördlichen Milchstraßenverlauf.

<sup>&</sup>lt;sup>1</sup> A N 222, S 86 (1924) <sup>2</sup> Lund Medd Ser II, Nr 10 (1913)

a Recherches astron de l'Obs d'Utrecht VII (1917)

<sup>&</sup>lt;sup>1</sup> Grundriß der Astrophysik, S 715 (1928)
<sup>5</sup> A N 137, S 81 (1894), Ap J 1, S 216 (1895), A N 159, S 169 (1902), Proc Acad Lerdam 8, Nr 3 (1903)
<sup>6</sup> Publ Obs Taschkent 2 (1900) Amsterdam 8, Nr 3 (1903)

Es stellt sich hier horaus, daß eine kleine mit steigender Helligkeit abnehmende Korrelation im ganzen auch für die helleren Klassen der Argelanderschen Sterne besteht Noch für die hellste Klasse, welche die Größen 0 bis 6,5 umfaßte, ist eine Spur davon vorhanden. Eine erheblich größere Korrelation für diese hellste Klasse ist aber von NEWCOMB1 hergeleitet worden, was wohl auch mit I C VAN DE LINDER Resultaten übereinstimmt

Easton zieht aus der Übereinstimmung der Konzentrationspunkte für verschiedene Größen den Schluß, daß die schwachen Sterne der Milchstraße von uns nicht viel weiter entfernt sein können als etwa die Sterne 9. oder 10. Größe, und daß die scheinbaren Sternweiken auch wirklichen reellen Anhäufungen un Raumo entsprechen. Von unserem jetzigen Standpunkt aus müssen wir aber diese Auffassung als einen Fehlschluß betrachten. Daß eine Korrelation zwischen Sternverteilung und Milchstraßenhelligkeit auch für helle Größenklassen besteht. kann auch bedouten, daß die Ursachen der Wolkenstruktur wenigstens zum Teil in unserer Naho llegen und wesentlich in einer Absorption des Lichts in dunklon Wolken von nebliger oder staubförmiger Materie zu suchen sind. Wir werden im folgenden sehen, daß diese Auffassung in der lotzten Zolt mehr und mehr Platz greift. Le ist jedoch jedenfalls ein bleibendes Verdienst von Easton, die Bedeutung der großen Streuung in absoluter Größe unter den Sternen für das Milchstraßenproblem erkannt zu haben.

NORT hat in seiner eben erwähnten Arbeit die Untersuchung von Easton auf Grund der Sternzählungen bis zur 11. Größe erweitert. Unter Verwendung einer von Easton hergestellten Isophotonkarte für den Südhimmel, die auf GOULDS. HOUZEAUS und BACKHOUSES Arbeiten beruht, hat er die Untersuchung auch auf die südliche Milchstraße ausgedehnt. Er gibt in Tabellen und Figuren einen Vergleich zwischen Lichtintensität und Sterndichte für Gebiete der galaktischen Zone in Intervallen von 15° in L und 4° in B Er zieht den Schluß, daß das Phänomen der Milchstraße im ganzen noch nicht in der Verteilung der Sterno zwischen 9m,0 und 11m,0 widergespiegelt wird. Dieser Schluß ist in Übereinstimmung mit Pannerores Resultaten, daß kelne organische Verbindung zwischen der großen Masse der Sterne von der 9. bis vielleicht zu der 11. Größe und den Wolken, welche die Milchstraße bilden, besteht, widerspricht jedoch wohl in einem gowissen Grade den oben referierten Resultaten von Hopmann, nach denen in violen Fällen die Sterne heller als von der Größe 11 sogar in der Gesamtlichtwirkung dominieren sollen.

Daß eine ausgeprägte Korrelation zwischen dem Verlauf der Milchstraße und der Vertellung der Sterne bis etwa zur Größe 14 (visuell) besteht, ist z. B aus den umfangreichen Zählungen auf der Franklin-Adams-Karte, die von Charlier und solnen Mitarbeitern in Lund ausgeführt worden sind, ersichtlich. Eine Tafel, welche die Resultate bildlich wiedergibt, ist in Charliers "California Lectures" gegebon.

17. Das Integralspektrum der Milchstraße. Effektive Entfernung der Milchstraßensterne. Das integrierte Spektrum von einigen galaktischen Wolken wurde zuerst von E. A. FATH auf dem Mount Wilson mit Expositionszeiten von 30, 67 und 74 Stunden erhalten. Das Ergebnis war ein Spektrum approximativ vom Sonnentypus. Da nach van Rhijns oben (Ziff 5) besprochener Arbeit ein beträchtlicher Teil der Strahlung des Himmelsgrundes auch für heile galak-

<sup>&</sup>lt;sup>1</sup> The Stars, S 273 (1902)

Do Verdeeling der heldere Sterren, S. 63 Rotterdam. Wyt & Zonen 1921.

Versl Akad Amsterdam 19, S. 243 (1910); Proc Acad Amsterdam 13, S. 239 (1910).

Lund Medd Sar II, 31 (1923)

Mem Univ Calif. 7 (1926). 4 Lund Modd Sar II, 31 (1923)

Mt Wilson Contr 63 - Ap J 36, 8 362 (1912)

-1-0.77 findet

tische Regionen wahrscheinlich dem Zodiakallicht zuzuschieiben ist, so ist es

möglich, daß diese Lichtquelle in dem Resultat etwas mitspielt

E A Kreiken hat fur 4000 Steine der Scutumwolke bis zur Große 14,9 die photographisch effektiven Wellenlangen bestimmt. Das Plattenmaterial hatte E Herrzsprung mit dem 60 zölligen Reflektor auf dem Mount Wilson gesammelt Im Mittel eigibt sich ein Farbentypus, der eine Spektralklasse etwas futher als GO andoutet Nach unseien Übeilegungen in Ziff 16 ist es wahrscheinlich, daß Kreikens Untersuchung die effektive Große des Milchstraßenlichts erreicht, und daß also die berechnete mittlere Farbe der Steine fur dieses Gesamtlicht einigermaßen reprasentativ sein sollte. Das gewonnene Resultat ist naturlich von jedem Erdlicht oder Zodiakallicht fier und stutzt daher die Gultigkeit der von Fath eihaltenen Spektialklasse

In einer spateren Arbeit<sup>2</sup> hat Kreiken unter Heranziehung anderen Materials die Farben der Milchstraßensteine bis zu noch schwacheren Großen studiert (vgl Ziff 22) Im Mittel eigibt sich fut die Scutumwolke bis zur Größe 17.3 em Fai benindex +0.38, wahrend Shapleys fur 310 Steine zwischen den Größen 12 und 15 in deiselben Wolke in dei Umgebung des Sternhaufens M11 im Mittel

Eine direkte Bestimmung des Faibenindex derselben Wolke hat Pannekoek<sup>1</sup> volgenommen Die Platten wurden von Wolf mit einem kleinen Zeiss-Tessal aufgenommen und extrafokal eingestellt, so daß die helleren Sterne als isolierte Scheibehen eischeinen. Die Schwärzung auf der Platte ruhrt außerdem vom galaktischen Licht und vom "Eidlicht" her, letzteies kann als über das Feld konstant angesehen werden Die Variation der Schwarzung mit einer Variation der photographischen Helligkeit (in Sternen der Große 0 per Quadratgrad ausgedruckt) wurde aus den Steinscheibehen hellei Steine ermittelt. Der Zusammenhang zwischen Schwaizung und visuellei Helligkeit des Milchstraßenlichts in einer entsprechenden Einheit wurde aus den Pannekoekschen Isophoten nach ihrei Eichung gemäß van Rhijns Messungen bestimmt. Aus dem Veihaltnis dei Koeffizienten dei zwei Ausdrücke zieht Pannekofk den Schluß, daß die photographische Lichtstarke der Milchstraßenwolke 57/85 der visuellen betragt Dieses Verhaltnis entspricht einem Faibenindex von 4-0,43 und einer Spektralklasse F5.

Kurzheh haben W S Adams, M Humason und A. II. Joy<sup>5</sup> mit einem kleinen Spektrographen in Veibindung mit dem 10zölligen Cooke-Refiaktor auf dem Mount Wilson Spektrogramme der Milchstraßenwolken in Sagittarius und Cygnus aufgenommen Die Expositionszeiten waren 93 und 141 Stunden. Die Spektralklassen wurden in beiden Fallen fruher als vom Sonnentypus, nämlich F5 für die Sagittanuswolke und F3 für die Cygnuswolke, gefunden. Infolge der kleinen Dispersion des Spektrographen laßt sich natürlich eine genauere Bestimmung dei Radialgeschwindigkeit dei Wolken nicht durchführen Von Bedeutung ist abei die Bemerkung, daß die Radialgeschwindigkeiten beider Wolken klein gefunden werden,

Wenn wir also für das Integralspektrum der Milchstraße die Klasse F5 annehmen, so ist es klai, daß wir es in diesem Falle mit einei Art von Mischspektrum zu tun haben, zu dem verschiedene Sterntypen mehr oder weniger ihren Beitrag liefern Da aber die Klasse F5 und die diese Klasse in der Spektralieihe unmittelbar umgebenden Typen unter den schwachen Steinen sehr zahlieich vertieten

<sup>&</sup>lt;sup>1</sup> On the Colour of Faint Stars in the Milky Way, and the Distance of the Scutum Group Dissert Groning

M N 87, S 196 (1927)

B A N 2, S 19 (1923) Dissert Groningen 1923

<sup>&</sup>lt;sup>8</sup> Mt Wilson Contr 133 = Ap J 46, S 64 (1917) <sup>5</sup> Publ ASP 39, S 368 (1927)

sind, so können wir mit einiger Wahrscheinlichkeit schließen, daß wir es in der Näho der "effoktiven" schembaren Größe im Durchschnitt mit Sternen dieser Spektralklasse zu tun haben, und zwar mit gewöhnlichen "Zwergsternen", da die "Riesen" dieser Klasse sehr selten im Raume sind und wir für die Sterne der schwachen Größenklassen keine sehr extreme Salektion nach großer absoluter Leuchtkraft vorauszusetzen haben. Wir können also für die mittlere absolute Größe der Sterne etwa +3 annehmen Die effektive Entfernung der Milchstraßensterne konnen wir als die Entfernung definieren, in der die effektive absolute Größe auf die effektive scheinbare Größe des Milchstraßenlichts reduziert wird Wenn wir für die letztere die Größe 14 fixleren, bekommen wir für die effektive Entfornung der Milchstraßensterne 1600 Parsec Für die Sagittariuswolke beträgt die effektive Entfernung etwa 2500 Parsec Der eingeführte Begriff der effektiven Entfernung ist natürlich ganz unabhängig von der Frage, ob die Sterne Mitglieder einer reellen Wolkenstruktur sind oder m einem sehr ausgedahnten Stratum zlemlich gleichmäßig gestreut vorkommen Man ersieht ohne Schwierigkeit aus dem symmetrischen Verlauf von /(m) um die effektive Größe herum in Tabelle 9, daß diese Entfernung approximativ so abgemessen ist, daß eine Hülfte des galaktischen Lichts aus größerer, eine Hälfte aus kürzerer Entfernung stammt.

Eine wenn auch nur sehr grobe Kontrolle dieser Schätzung der effektiven Entfernung gibt uns das Phänomen der Tiefe oder des "dip" der Milchstraße Nach Tabelle 5, Ziff 11, bekommen wir im Mittel für die Tiefe  $p=\sigma-90^\circ$  den Wert 26' Andererseits finden wir in Ziff 21, daß die Sonne wahrscheinlich etwa 34 Parsee nördlich von der mittleren galaktischen Ebena gelegen ist. Wenn wir diese zwei Daten zusammenstellen, ergibt sich für die "affektive Entfernung" rein geometrisch etwa 4500 Parsee, was wenigstens der Größenordnung nach mit dem obigen photometrischen Resultat stimmt. Wenn wir z B PANNERORES Wert der Tiefe, p=65', angenommen hätten, wäre die Übereinstimmung viel besser.

18. Übersicht der allgemeinen statistischen Untersuchungen über die Vertellung der Sterne im Raume. Daß die Milchstraße als Phänomen durch eine Zusammenwirkung des Lichts von unzähligen Sternen, die in einer Schicht großer Sternhäufigkeit vertellt sind, entsteht, ist eine Ansicht, die im Altertum von DEMOKETT, in der Neuzeit von Kepler und Galilki, und auf mehr naturphilosophischer Grundlage von Swedenborg, Wright, Kant und Lambert ausgesprochen wurde. Als Begründer der Stellarastronomie als empirischer Wissenschaft ist aber W. HERSCHEL anzuschen. Die empirische Grundlage der Feststollungen Herschels sind in den vielerwähnten Sternelchungen1 enthalten. Er zahlte für verschiedene Punkte des Himmels die Anzahl Sterne, die im Felde seines Reflektors sichtber weren. Der Bearbeitung des Materials lag die Annahme olner bis zu olner gowissen Grenzfläche gleichförmigen Dichte im Sternsystem zugrunde Die verschiedene Fülle sichtbarer Sterne in verschiedenen Gegenden des Himmels mußte dann auf eine Erschöpfung aller Sterne bis zur Grenze des Systems zurückgeführt werden, und der Abstand der Grenze in einer gewissen Richtung wurde durch eine einfache Formel direkt aus der Sternzahl berechnet So gelangte Herschel zu der wohlbekannten Darstellung des Systems in Form eines linsenförmigen Gebildes, dessen größter und kleinster Durchmesser 860 und 220 "Sirlusabstände" betragen. In seinen späteren Jahren wurden allerdings die Ansichten Herschells etwas modifiziert; die Tiefe der Milchetraße erscheint ihm in gewissen Gogonden unermeßlich.

Phil Trans 74, S 437 (1784), 75, S 213 (1785), Collected Scientific Papers I, B. 157 ff., 223ff

Die Weiterentwicklung der Stellarstatistik im 19 Jahrhundert ist an eine Reihe von Namen geknupft, von denen wir is G. W. Struve, G. V. Schlaparflit, II Gylden erwahnen können. Ihre vollstandigste Entwicklung und gewissermaßen einen vorlaufigen Abschluß finden die neuen Methoden in den Arbeiten II. v. Speligers<sup>1</sup>

An Stelle der Annahme, daß die Steine alle ungefahr dieselbe absolute Leuchtkraft besitzen, tritt die Annahme einer statistischen Verteilung der wichlichen Helligkeiten, die durch eine Luminositatsfunktion ausgedruckt wird. Die absolute Leuchtkraft i wird als die auf die Entfernung i reduzierte scheinbare Helligkeit verstanden, und die Proportion der Steine in einer Volumeneinheit, die zwischen i und i+di liegen, wird durch den Ausdruck  $\varphi(i)di$  definiert, wo  $\varphi(i)$  die Luminositatsfunktion darstellt. Die Anzahl aller Steine in der Volumeneinheit für die Distanz r innerhalb der betreffenden Region des Himmels ist eine Funktion D(r) von r. Wenn wir das Problem der Verteilung in aller Allgemeinheit angreifen, mussen wir die Moglichkeit offen lassen, daß  $\varphi(i)$  von Ort zu Ort wechseln kann, m a W daß das Mischungsverhaltnis verschiedener absoluter Größen mit der Entfernung wechseln kann. Die Leuchtkraftsfunktion sollte also  $\varphi(i,r)$  geschrieben werden

Die schembare Helligkeit h ist mit i durch die Relation

$$\iota = \frac{h \, r^a}{\psi \, (r)} \tag{1}$$

verbunden, wo  $\psi(r)$  die Einwirkung einer etwaigen Absorption des Lichtes im

Raume Rechnung tragt

Die Anzahl A allei Sterne, die auf ein Flachenstück des Himmels von der Größe  $\omega$  projiziert und die heller als von der scheinbaren Lichtstärke h erscheinen, kann jetzt in der Form eines Doppelintegrals aus den Funktionen  $\varphi$ , D und  $\psi$  ausgedruckt werden. Wenn wir zuerst die Anzahl dA der Sterne im scheinbaren Heligkeitsbereiche zwischen h und h+dh ins Auge fassen, bekommen wir fast unmittelbar die folgende Integrahelation

$$\frac{dA}{dh} = -\omega \int_{0}^{\sigma} D(r) \frac{r^{1}}{\psi(r)} \varphi\left(\frac{h r^{2}}{\psi(r)}, r\right) dr, \qquad (2)$$

wo  $\sigma$  die obere Integrationsgrenze in r angibt. Fur die mittlere Parallaxe  $\pi(h)$  der in Betracht genommenen Sterne von der scheinbaren Helligkeit h oder von der scheinbaren Größe m, wo

$$m = -2.5 \log h,$$

haben wir dann auch, wenn r in Paisec ausgedruckt wird,

$$\pi(h) \frac{dA}{dh} = -\omega \int_{0}^{\sigma} D(r) \frac{r^{3}}{\psi(r)} \varphi\left(\frac{hr^{2}}{\psi(r)}, r\right) dr$$
 (3)

Fur Stellgers Analyse besonders charakteristisch sind die folgenden Annahmen, erstens, daß für die absolute Leuchtkraft i eine obere Grenze II angegeben werden kann, welche allerdings vom Orte im System abhängen kann, und zweitens, daß eine Entfernung  $r_1$  gefunden werden kann, außerhalb welcher die Sterndichtigkert so schnell abnimmt, daß wir von einer wirklichen Begrenzung des Systems bei  $r = r_1$  reden können. Diese Annahmen sind natürlich von Be-

Ausführliche Bibliographie und zusammenfassende Darstellung von G. Di Urschland, V.J.S. 54, S. 25 (1919) Eine spätere Arbeit ist "Untersuchungen über das Sternsystem" Sitzber d. Bayer Akad d. Wiss, Math-phys. KI (1920)

deutung für die obere Integrationsgrenze  $\sigma$  Wenn wir Sterne von so großer scheinbarer Helligkeit in Betrucht ziehen, daß auch Sterne der absoluten Leuchtkraft H noch innerhalb der Grenze  $r_1$  stehen müssen, um der gewählten scheinbaren Helligkeit zu entsprechen, ergibt sich  $\sigma$  aus der Relation

$$k = \frac{H(\sigma)\,\psi(\sigma)}{\sigma^2}$$

Wenn aber die Entfernung, in der die absolut hellsten Sterne die scheinbare Helligkeit h besitzen, die Grenze  $r_1$  überschreitet, haben wir als obere Integrationsgrenze  $\sigma = r_1$  zu setzen. In dieser Welse bekommt man zwei verschiedene Ausdrücke für die theoretischen Sternzahlen und mittleren Parallaxen für hellere

und schwichere Sterngrößen.

Eine Folge dieser Aufspaltung der Formeln für die theoretischen Sternzahlen bei einer gewissen Sterngröße m=n, welche einen Stern der absoluten Helligkeit H an der Grenze  $r=r_1$  kennzeichnen würde, ist eine Unstetigkeit in den zweiten Differenzen der Sternzahlen A. Wenn wir also in üblicher Weise die Sternzahlen A durch eine Interpolationsformel  $\log A(m) = \alpha + \beta m + \gamma m^2$  darstellen wollen, so gentigt diese Formel nicht in dem genzen Bereich von Größenklassen, sondern wir müssen mit Sekliger annehmen

$$\log A(m) = \alpha + \beta (m-n) - \gamma (m-n)^{n}, \quad \text{für} \quad m < n,$$

$$\log A(m) = \alpha + \beta (m-n) - \gamma_{1} (m-n)^{n}, \quad \text{für} \quad m > n$$

Um aber aus den beobachtoten Stornzahlen zu einer praktischen Bestimmung der Dichte- und Luminositätsverteilung zu gelangen, müssen wir die vereinfachende Annahme einführen, daß die Luminositätsfunktion und auch die maximale Helligkeit unabhängig vom Orte sind, d. h. das Mischungsverhältnis der absoluten Helligkeiten sell überall dasselbe seln. Die Frage, ob eine Absorption im Raume vorhanden ist, kann dadurch vorläufig umgangen werden, daß wir die "scheinbare" Entfernung  $\varrho$  und Dichte  $A(\varrho)$  in folgender Weise einführen,

$$\varrho^{\mathbf{a}} = \frac{r^{\mathbf{a}}}{\Psi(r)}, \quad A(\varrho) = D(r)\Psi(r)\frac{dr}{d\varrho}.$$
(4)

Wir bekommen dann aus (2) für die Sternzahlen verschiedener Grenzgrößen m

$$A(m) = \omega \int_{0}^{\pi} A(\varrho) \, \varrho^{\mathbf{a}} \, d\varrho \int_{\mathbf{a}}^{\Pi} \varphi(\mathbf{z}) \, d\mathbf{z} \,, \tag{5}$$

WO

$$\sigma = \begin{cases} \sqrt{\frac{H}{h_m}}, & \text{für } m < n, \\ \sqrt{\frac{H}{h_n}}, & \text{für } m > n. \end{cases}$$

 $h_m$  und  $h_n$  sind die den Größen m und n entsprechenden Helligkeiten. Für die mittleren Parallaxen haben wir dann die Formel

$$\pi(m)\frac{dA}{dh_m} = -\omega \int_0^\pi \Delta(\varrho) \frac{q^2}{\sqrt{\psi(r)}} \varphi(h_m \varrho^4) d\varrho , \qquad (6)$$

we also die Absorptionsfunktion  $\psi(r)$  explicit auftritt.

Die Sternzahlen der helleren Größenklassen folgen nahezu dem Gesetz

$$A = oh^{\frac{1-3}{2}},\tag{7}$$

wo  $\lambda$  mit der galaktischen Breite zunimmt. Seeliger weist nach, daß eine solche Form der Funktion  $\Lambda$  unabhängig von der Luminositätsfunktion einem Dichtegesetz

 $\Delta = \gamma \varrho^{-\lambda} \tag{8}$ 

entsprechen muß. Die Integralgleichung (5) für hellere Größenklassen gibt somit Aufschluß über die "scheinbare" Dichteverteilung, während die entsprechende Gleichung für schwächere Klassen die Eigenschaften der Luminositätsfunktion bestimmen kann. Die Gleichung der mittleren Parallaxen kann dann zur Bestimmung der Absorptionsfunktion  $\psi(r)$  benutzt werden, wodurch die wahre Dichtefunktion D aus  $\Delta$  hergeleitet wird; praktisch muß jedoch eine solche Verwendung dieser Gleichung für eine Verbesserung der "scheinbaren" Dichtefunktion  $\Delta$  zurücktreten. Bei zu vernachlässigender Absorption ergibt nämlich die Dichtefunktion (8)

 $\pi(m) = c \left(\frac{h_m}{H}\right)^{\frac{1}{2}} \tag{9}$ 

unabhängig von der Luminositätsfunktion, eine Formel, die mit den Kapteynschen mittleren Parallaxen in Widerspruch steht. Zur Erzielung einer Übereinstimmung muß die Dichtefunktion (8) modifiziert werden, da nur eine Einführung der Absorptionsfunktion nicht genügt.

Die veränderte Form des Dichtigkeitsgesetzes lautet

$$\Delta(\varrho) = \gamma(\varrho^{-\lambda} - a\varrho^{-\lambda_1}), \qquad (10)$$

wo der zweite Term in der Klammer nur für unsere nähere Umgebung von Bedeutung ist (allernächste Umgebung,  $\varrho=0$ , ist ausgeschlossen). Ifür die Luminositätsfunktion nimmt Seeliger an

 $\varphi(i) = I'\{x^{-r} e^{-h^{2}[(\log x)^{2} + b \log x + c]} - x e^{-h^{2}c}\}, \tag{11}$ 

wo x = i/H ist.

Bei der Konstantenbestimmung aus den empirischen Daten vereinfacht sich jedoch dieser Ausdruck praktisch auf  $\varphi(i) = I'e^{-a(\log r)^2 - b\log x}$ . Die maximale Leuchtkraft H wird aus den mittleren Parallaxen der hellsten scheinbaren Größen gemäß (9) bestimmt. Die Grenzentfernung  $r_1$  ist durch einen Sprung in den Differentialquotienten  $\frac{d^2\log A}{dm^2}$  und  $\frac{d\log \pi}{dm}$  bei einer gewissen Größe m=n bedingt, und kann direkt durch die Beträge dieser Sprünge berechnet werden, aber auch durch die Beziehung  $\varrho_1 = H^{\frac{1}{2}}h_n^{-\frac{1}{2}}$ .

Die Beobachtungsdaten für Seeligers Untersuchungen waren in den ersten Arbeiten die BD und deren stidliche Fortsetzung bis zur Dekl. --23°. Für die helleren Sterne dienten die Harvard-Photometry und die Potsdamer Durchmusterung, und für die schwächeren Größenklassen wurden die Eichungen von den beiden Herschel ausgewertet. Für spätere Arbeiten spielte das in Groningen von Kapteyn und van Rhijn zusammengestellte Material die größte Rolle. Die Werte der mittleren Parallaxen waren die von Kapteyn aus den parallaktischen Eigenbewegungen hergeleiteten.

Die Ermittlung der räumlichen Verteilung geschah teils für das schematische Sternsystem, bei welchem die Abhängigkeit der Sternzahlen von dem scheinbaren Ort völlig vernachlässigt wird, und teils für das typische Sternsystem, für welches die Abhängigkeit von der galaktischen Breite berücksichtigt wird. Das Phänomen der Milchstraße äußert sich in Smeligens Resultaten wie in den Herschelschen in einer beträchtlich größeren Ausdehnung des Systems in der Ebene der Milchstraße als in anderen Richtungen. Für die Grenze in der Milchstraßenzone gibt Seeliger in seiner letzten Arbeit den Abstand 725 Sirius-

weiten (3625 Parsec) und für die Grenze in der Richtung des galaktischen Pols den Abstand 180 Sirlusweiten (900 Parsec). W. Sametinger hat später in einer neuen Durchrechnung für die Grenzentfernung in den zwei Richtungen 2820 und

1260 Parsec gefunden

Die Schnelligkeit, mit der die Sterndichtigkeit gegen die Grenzfläche des Systems abnimmt, und auch die Entfarnung der Grenze selbst in verschiedenen Richtungen hängt natürlich von einer Schätzung der Absorption des Lichts im Raume, d h von der Funktion  $\psi(t)$ , ab. Die eben gegebenen Entfernungen der Granze setzten vornus, daß die Absorption zu vernachlässigen ist, also daß w(t) = 1zu setzen ist, womit A und D identisch werden. Wenn man mit SEKLIGER vom Gesetze  $d(p) = \gamma p^{-1}$  ausgeht und voraussetzt, daß die wahre Sterndichtigkeit D(r) nicht gegen die Grenzfläche hin wachsen darf, so bekommt man einen Höchstbetrag für die Absorption durch vorgelagerte Massen wie auch für eine allgemeine Absorption des Lichtes im Raume, der in beiden Fällen sehr klein ausfällt, und zwar so klein, daß der Einfluß auf die räumliche Ausdehnung des Systems als gering anzusehen ist. Im letzteren Falle hat man  $\psi(r) = e^{-rr}$  zu setzen und bekommt dann nach (4) die wahre Dichtigkeit durch die Formal

$$D(r) = \Delta (r e^{\frac{1}{4}rr}) (1 + \frac{1}{4}rr) e^{\frac{1}{4}rr}$$
 (12)

Für den maximalen Absorptionskoeffizienten (per Parsec gerechnet) in diesem Falle findet SEELIGER 0.0000617.

Mit dieser Überlegung ist aber sicher nicht die Frage einer merklichen Absorption des Lichtes definitiv criedigt. Das vorausgesetzte "scheinbare" Dichtigkeitsgesetz, einschließlich der scharfen Grenze bei  $r=r_1$ , ist für die großen Entfernungen eine sehr schematische Annahme über die Dichtefunktion und kann keine strengere Gültigkeit beanspruchen. Es scheint schon aus diesem Grunde sehr fraglich, ob ingendeine zuverlässige Abschätzung der Absorption

nach dem genannten Prinzip gemacht worden kann

Les ist auch aus anderen Gründen ersichtlich, daß die Maschen des "typischen" Sternsystems viel zu grob sind, um die Verteilung der Sterne für größere Entfernungen in dem dinnen galaktischen Stratum mit einiger Zuverlässigkeit zu fangen. Die Struktur der Milchstraße zeigt in mehreren Zügen unzweldeutige Einflüsse einer mit dem scheinbaren Orte wechselnden Absorption durch neblige oder staubfürmige Materie. Im "typischen Sternsystem" werden Einzelhelten dieser Art, die Ahhängigkeit von der galaktischen Breite innerhalb einer Zone sowie jedo Abhängigkeit von der galaktischen Länge in einer allgemeinen Mittelbildung ausgeglichen Wir werden auf die diesbezüglichen Fragen in späteren Abschnitten zurückkommen.

Die Methode, die von J. C. KAPTEYN' und solnem Mitarbeiter und Nachfolger P. J. van Rhijns befolgt wurde, um aus beobachteten Sternzahlen und statistischen Parallaxon die Dichtigkeitsfunktion und die Leuchtkraftsfunktion zu bestimmen, ist nicht an mathematisch definierte Näherungsausdrücke gebunden, sondern besteht in einer Im Prinzip voraussetzungafreieren tabellarischen Behandlung des empirisch gegebenen Materials. Die Anzahl No. a der Sterne zwischen sukzessiven Intervallen in schelnbarer Größe m und Eigenbewegung  $\mu$ wird unter Benutzung der empirisch bestimmten Funktionen n. (mittlere Parallaxo für gegebene Werte von m und  $\mu$ ) und  $\chi_{\pi,m,\mu}$  (die Verteilungsfunktion der wahren Parallaxen um diesen Mittelwort horum) über sukzessive Intervalle in

Groningen Publ Nr. 34 (1923), Nr. 36 (1925), Nr. 38 (1925)

<sup>1</sup> SEELIGER-Festschr S. 276 (1924) Groningen Publ Nr. 11 (1902); A J 566 (1904); Groningen Publ Nr. 29 (1918), Nr. 30 (1920); Mt Wilson Contr 188 — Ap J 52, S. 23 (1920).

Groningen Publ Nr. 34 (1021), Nr. 36 (1021), Nr. 38 (1021)

 $\pi$  verteilt. Aus der resultierenden Tabelle mit doppeltem Eingang nach m und  $\pi$ können Luminositätsfunktion und Dichtigkeitsfunktion direkt abgelesen werden, und zwar wird die erstere für sukzessive Parallaxenintervalle wiederholt bestimmt. Die Methode ist im grundlegenden Prinzip frei von einer Hypothese über die Absorption des Lichtes im Raume. Die Verschiebung der Luminositätskurye zwischen sukzessiven Parallaxenintervallen ist aber durch das Vorhandensein einer Absorption bedingt; wenn man dieselbe Luminositätsfunktion für verschiedene Distanzen postuliert, kann der Absorptionsbetrag gewissermaßen beurteilt werden. Da aber keine deutliche Spur einer Absorption vorhanden ist, kann nur ein Höchstbetrag derselben geschätzt werden. Für die Luminositätsfunktion wurde in den früheren Arbeiten sehr nahe eine normale Verteilung in absoluter Größe (der Gaussschen Fehlerkurve analog) gefunden, was auch mit SEELIGERS Resultaten übereinstimmt. In der späteren Arbeit von VAN RHIJN wird jedoch dieses Ergebnis für die schwächsten absoluten Größen erheblich modifiziert, indem die Häufigkeit der schwächsten absoluten Größen keine Abnahme zeigt, sondern einen weiteren schwachen Anstieg. Für die Herleitung der Luminositätsfunktion ist hier auch eine andere Methode, welche nur gemessene trigonometrische Parallaxen benutzt, herangezogen worden.

In Analogie mit Seeligers typischem Sternsystem wird in der Kapteynschen Statistik angenommen, daß die Dichtigkeitsverteilung Rotationssymmetrie

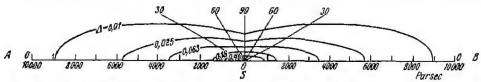


Abb. 11. Die Dichtigkeitsverteilung im typischen System nach Kaptryn und van Rhijn.

um eine Achse durch die Sonne senkrecht zur Milchstraße hat. Die ermittelte Dichtigkeitsverteilung ist in Abb. 11 illustriert. Die Abbildung stellt einen Schnitt durch das Sternsystem senkrecht zur Milchstraße dar. Die Kurven entsprechen Flächen konstanter Dichtigkeit und sind nur auf der einen Seite der Symmetricebene ausgezogen worden.

Eine ausführliche Darlegung der Kapteynschen Methoden in einer allgemeinen Behandlung der stellarstatistischen Probleme hat W. J. A. Schouten<sup>1</sup> gegeben.

In Seeligers Theorie sind die Annahmen einer maximalen Grenze der absoluten Leuchtkraft und einer Begrenzungsfläche, außerhalb der die Sterndichtigkeit als verschwindend klein angesehen werden kann, miteinander eng verknüpft. Die Erfahrungstatsachen, auf denen diese Annahmen beruhen, d. h. die Sprünge in den Werten gewisser Differentialquotienten, sind, wenn auch wahrscheinlich vorhanden, doch verhältnismäßig sehr geringe Effekte. Die speziellen Ansätze der eben genannten Art sind daher für eine statistische Analyse nicht als notwendig zu betrachten. Ohne irgendeine vorausgesetzte Beschränkung der absoluten Leuchtkraft i oder der oberen Integrationsgrenze in r hat Schwarzschild eine allgemeine Lösung der zwei Integralgleichungen der Sternzahlen und mittleren Parallaxen gegeben.

Von großer praktischer Bedeutung ist eine Lösung von Schwarzschild, bei der für die Sternanzahl einer Größenklasse und für die mittleren Parallaxen

On the Determination of the Principal Laws of Statistical Astronomy. Diss. Amsterdam 1918.

<sup>&</sup>lt;sup>8</sup> A N 185, S. 81 (1910).

gewisse geeignete Näherungsausdrücke gewählt werden Wir bezeichnen mit  $a(m) \, dm$  die Anzahl der Storne zwischen den Größen m und m + dm und mit  $\pi(m)$  die mittlere Parallaxe derselben Storne. Wenn die absolute Größe

$$M = -2.5 \log i$$

eingeführt wird und die Verteilung der absoluten Größen durch eine Funktion  $\varphi_1(M)$  gegeben wird, so daß

$$\varphi(i)\,di = -\varphi_1(M)\,dM\,,$$

und wenn die Absorptionsfunktion  $\psi(r)=1$  gesetzt wird, so können die Integralausdrücke für a(m) und  $\pi(m)$  in folgender Form geschrieben werden

$$a(m) = \omega \int_{0}^{\infty} D(r) \varphi_{1}(m - 5 \log r) r^{2} dr,$$

$$\pi(m) a(m) = \omega \int_{0}^{\infty} D(r) \varphi_{1}(m - 5 \log r) r dr.$$
(13)

Jetzt wird vorausgesetzt

$$\log a(m) = \kappa_0 - \kappa_1 m - \kappa_2 m^2, \log \kappa(m) = P_0 - P_1 m,$$
 (14)

wo  $\varkappa_0$ ,  $\varkappa_1$ ,  $\varkappa_2$ ,  $P_0$ ,  $P_1$  Konstanton sind. Diese Annahmen führen auf die folgende Form der Funktionen D(r) und  $\varphi_1(M)$ , wenn wir  $\tau = -5\log r$  einführen,

$$\log D(r) = a_0 - a_1 r - a_2 r^2, 
\log \varphi_1(M) = b_0 - b_1 M - b_2 M^2,$$
(15)

was direkt durch Einsetzung in die Gleichungen (13) und Ausführung der Integration verifiziert werden kann.

Die Funktion  $\varphi_1(M)$  ist eine Gaussche Fehlerkurve mit der Streuung

$$\sigma = \sqrt{\frac{\log \theta}{2b_0}}$$

und dem Mittelwert

$$M_0 = -\frac{1}{2} \frac{b_1}{b_1}$$

Der Ansatz (14) entspricht im Durchschmitt sehr wehl den empirischen Resultaten von Kapteyn, und die Ausdrücke (15) für D und  $\varphi_1$  geben auch die analytische Form der Hauptresultate der Kapteynschen Analyse wieder.

K Schwarzschild hat auch gezeigt, daß man unter der Annahme einer normalen Verteilung der Logarithmen der räumlichen Geschwindigkeiten der Sterne in bezug auf die Sonne die Kapthynschen Resultate für die Funktionen  $\pi_{m,n}$  und  $\chi_{m,n,n}$  reproduzieren kann.

Wenn  $\varphi_1(M)$  und a(m) bekannt sind, bekommt man die Koeffizienten  $a_1$  und  $a_2$  von D nach den Formeln

$$a_{1} = -0.6 + \frac{b_{1} \kappa_{0} - b_{0} \kappa_{1}}{b_{0} - \kappa_{0}},$$

$$a_{0} = \frac{b_{0} \kappa_{0}}{b_{0} - \kappa_{0}},$$
(16)

<sup>1</sup> AN 190, S. 361 (1912).

Aus den numerischen Werten von Kapteyn und van Rhijn<sup>1</sup> erhält man z. B. die folgenden Resultate, wo a(m) pro Quadratgrad gerechnet wird:

log 
$$a(m) = -4.542 + 0.724 \ m - 0.0141 \ m^2$$
 (Gal. Breite 0°)  
log  $a(m) = -4.903 + 0.774 \ m - 0.0221 \ m^2$  (Gal. Breite 90°)  
log  $\varphi_1(M) = -2.394 + 0.1858M - 0.03450M^2$   
log  $D(r) = -2.532 + 2.478 \ \log r - 0.593 \ (\log r)^2$  (Gal. Breite 0°)  
log  $D(r) = -6.219 + 6.120 \ \log r - 1.538 \ (\log r)^2$  (Gal. Breite 90°)

Die Konstanten  $a_0$  und  $b_0$  sind hier so angepaßt, daß die Dichte in der Umgebung der Sonne als Einheit für D benutzt wird, während  $\varphi_1(M)$  die Anzahl Sterne pro Kubikparsec nahe der Sonne für verschiedene absolute Größen glbt.

Die hier gegebene Funktion  $\varphi_1(M)$  entspricht

$$M_0 = +2.7, \qquad \sigma = 2.5.$$

Zu bemerken ist, daß die gegenwärtig am meisten gebrauchte Skala der absoluten Größen um fünf Einheiten größer ist als die oben benutzte. In dieser Skala, in der die absolute Größe als die auf die Entfernung 10 Parsec reduzierte scheinbare Größe definiert wird, ist daher  $M_0=+7.7$ . Die Formel für D(r) hat natürlich keine Gültigkeit in unserer unmittelbaren Umgebung, da offenbar für r=0 die Formel D=0 gibt. Es soll schließlich betont werden, daß die eben gegebenen einfachen Ausdrücke für  $\varphi_1(M)$  und D(r) durch neuere Untersuchungen, besonders durch van Riijns Arbeit in Groningen Publ. 38, wo auch die einzelnen Spektraltypen separat behandelt werden, in mehrfacher Weise modifiziert worden sind.

Wichtige Beiträge zu der statistischen Behandlung der Dichtigkeitsverteilung sind in C. V. L. Charliers<sup>2</sup> Arbeit "Studies in Stellar Statistics" enthalten. Unter anderem wird von Charlier bemerkt, daß, wenn man die Stellerrschen Annahmen der oberen Begrenzungen in Leuchtkraft und Entfernung fallen läßt, die Gleichung

$$\frac{dA}{dh} = -\omega \int_{0}^{\infty} D(r) \varphi(hr^{2}) r^{4} dr,$$

in Verbindung mit dem Sternzahlgesetz (7) der helleren Größen

$$\frac{dA}{dh} = ch^{-\kappa},$$

nicht mit Notwendigkeit auf die Lösung  $D(r) = \gamma r^{-1}$  und eine arbiträre Leuchtkraftsfunktion führt, sondern daß ihr auch durch den Ansatz

$$\varphi(x) = \frac{1}{x^{\kappa}} \tag{17}$$

bei beliebiger Dichteverteilung Genüge geleistet wird, und zwar ist es möglich,

daß sogar unendlich viele Lösungen existieren.

CHARLIER nimmt für die Funktionen a(m) und  $g_1(M)$  normale Frequenzkurven vom "Typus A" an, wo jedoch nur die generierende Funktion selbst gebraucht wird. Die Ausätze sind also mit denen der oben besprochenen gleichzeitig publizierten Arbeit von Schwarzschild identisch. Die Dichtigkeitsfunktion D(r) wird dann auch eine normale Frequenzkurve in  $\log r$ . Die mittleren Parallaxen werden in der Form

$$\pi(m) = K e^{-\lambda m} \tag{18}$$

<sup>&</sup>lt;sup>1</sup> Mt Wilson Contr 188 = Ap J 52, S. 23 (1920).

<sup>&</sup>lt;sup>2</sup> Lund Medd Ser II, 8 (1912).

ausgedrückt,  $\lambda$  wird aus den mittleren Eigenbewegungen verschiedener scheinbarer Größen bestimmt, die einem analogen Gesetz mit demselben Werte von  $\lambda$  gehorchen Die Konstanten der Leuchtkrafts- und Dichtigkeitsfunktionen

werden gemäß diesem Resultat ermittelt.

CHARLIER verläßt die Approximation des "typischen Systems" und teilt den Himmel in 48 gleich große Flächen nach galaktischer Länge und Breite, innerhalb deren die Statistik unabhängig ausgeführt wird, was unzweifelhaft eine prinzipiell welt richtigere Problemstellung bedeutet. Eine ausführliche Übersicht der mathematisch-statistischen Grundlagen zur Analyse der Dichtigkeitsverteilung ist in Charliers vorher (Ziff 17) erwähnten "Califorma Lectures"

gegoben

Einige für die Stellarstatistik besonders wichtige Rolationen sind von K G. Malmouist<sup>1</sup> hergeleitet worden. Wenn die Leuchtkraftfunktion eines Volumens im Raume einem normalen Verteilungsgesetz gehorcht, so ist unter gewöhnlichen Bedingungen auch die scheinbare Leuchtkraftsfunktion, d. h. die Verteilung der Sterne von der scheinbaren Größe m nach absoluter Größe M, sehr nahe eine normale Frequenzkurve. Wenn die wahre Leuchtkraftsfunktion durch den Mittelwert  $M_0$  und die Dispersion  $\sigma$  bestimmt wird und wenn wir die scheinbare Leuchtkraftsfunktion durch eine Entwicklung vom Typus A,

$$F(M) = \varphi_{\mathbf{m}}(M) + A_{\mathbf{n}} \varphi_{\mathbf{m}}^{II}(M) + A_{\mathbf{n}} \varphi_{\mathbf{n}}^{IV}(M) + \cdots, \tag{19}$$

ausdrücken, wo

$$\varphi_{\mathbf{m}}(\mathbf{M}) = \frac{1}{\sigma_{\mathbf{m}} \sqrt{2\pi}} \sigma^{\frac{(\mathbf{M} - \mathbf{M}_{\mathbf{m}})^2}{2\sigma_{\mathbf{m}}^2}} \tag{20}$$

die genorierende Funktion und  $\varphi^{III}$ ,  $\varphi^{IV}$ , die dritten und vierten Ableitungen nach M darstellen, so hat man

$$M_{m} = M_{0} - \sigma^{4} \frac{d/}{dm},$$

$$\sigma^{3}_{m} = \sigma^{4} + \sigma^{4} \frac{d^{3}/}{dm^{4}},$$

$$\left[\frac{3}{4}A_{4} = \sigma^{4} \frac{d^{4}/}{dm^{4}},\right]$$

$$\left[\frac{4}{4}A_{4} = \sigma^{4} \frac{d^{4}/}{dm^{4}},\right]$$
(21)

WO

$$f(m) = \log \operatorname{nat} a(m) \tag{22}$$

Ähnliche Beziehungen gelten auch für die Leuchtkraftsfunktion der Sterne heller als eine gewisse Größe m. Wenn  $M_0$  und  $\sigma$  für eine besondere Klasse von Sternen bekannt sind, kann die scheinbare Leuchtkraftsfunktion, durch die Ableitungen von  $\log a(m)$  in der oben gegebenen Welse gebildet, für eine Ermittlung der Dichtigkeitsverteilung der betreffenden Sterne im Raume gebraucht werden, da diese mit einfacher Rechnung durch die doppelte Verteilung der Sterne nach scheinbarer und wirklicher Größe gegeben sein muß. Von besonderer Bedeutung and diese Relationen, wenn  $\sigma$  klein ist, so daß die höheren Potenzen dieser Größe vernachlässigt werden können.

Wenn aber die Dispersion der absoluten Größen für irgendeine Klasse von Sternen klein ist, können wir auch folgendermaßen vorgehen. Wenn die Dispersion Null ware und alle Sterne dieselbe absolute Größe Me besäßen, so hätte

Lund Modd 100 - Ark Mat Astr Fys 16, Nr. 23 (1922).

man offenbar zwischen der Dichtigkeitsfunktion D(r) und der Sternzahlfunktion a<sub>1</sub>(m) die Relation

 $\omega r^2 D(r) dr = a_1 (M_0 + 5 \log r) d(5 \log r),$  $D(r) = \frac{5\log\sigma}{mr^3} a_1(M_0 + 5\log r).$ (23)

also

Die Variation von M, der Dispersion  $\sigma$  entsprechend, kann jetzt als eine Abweichung von einem idealen Zustande betrachtet werden und ihr Einfluß auf a(m) dem eines gleich großen Beobachtungsfehlers in m gleichgesetzt werden. Wir suchen daher die ideale Funktion a<sub>1</sub>(m) aus der beobachteten a(m) zu bestimmen. Nach einer Formel von Eddington haben wir in der Tat

$$a_1(m) = a(m) - \frac{\sigma^8}{2} \frac{d^3a}{dm^2} + \frac{\sigma^4}{8} \frac{d^4a}{dm^4} - \cdots$$
 (24)

Wenn a(m) tabuliert mit dem Intervalle  $\alpha$  in m vorliegt, haben wir approximativ die zweite Differenz

$$a(m + \alpha) - a(m - \alpha) - 2a(m) = \alpha^2 \frac{d^3a}{dm^3},$$
 (25)

woraus  $d^2a/dm^2$  bestimmt wird. Der Term in  $\sigma^4$  wird für kleines  $\sigma$  vernachlässigt.

Ernster Zweifel an der Gültigkeit der Annahme einer approximativ rotationssymmetrischen Verteilung der Sterne um die Sonne herum wurde wohl zuerst durch H. Shapleys? Studien tiber die Lagen der kugelförmigen Sternhaufen im Raume erregt. Auf die eigentümliche scheinbare Verteilung der Haufen scheint zuerst K. Bohlin<sup>3</sup> in einer bemerkenswerten Arbeit aufmerksam gemacht zu haben; er hat auch eine Anordnung dieser Haufen um den Zentralpunkt des Sternsystems herum für wahrscheinlich gehalten. Für diesen Punkt ergeben sich nach seinen Resultaten die Koordinaten  $L = 321^{\circ}34'$ ,  $B = -2^{\circ}56'$ . Die scheinbare Verteilung wurde weiter von A. R. Hinks4 und von E. Hertzsprungs untersucht. Gleichzeitig mit Shapley hat Charlier die Verteilung im Raume ermittelt auf Grund der Annahme, daß der wahre Durchmesser für alle Haufen derselbe ist. Die absolute Skala der Entfernungen wurde jedoch hier viel zu klein angenommen. In Shapleys Arbeit wurde die Stellung der Haufen als trotz der gewaltigen Entfernungen zum Sternsystem gehörige Gebilde sehr wahrscheinlich gemacht. Der Zentralpunkt des Sternhaufensystems liegt nach Shap-LEY in der Richtung  $L=327^{\circ}$ ,  $B=0^{\circ}$ , in einer Entfernung von etwa 16000 Parsec. Das "System der Haufen" ist jedoch in Hinsicht auf die Dichtigkeitsverteilung so unregelmäßig definiert, daß die Schätzung der Entfernung des Zentralpunktes unsicher bleibt. (Über den Einfluß der Absorption vgl. Ziff. 33.)

Außer durch die regelmäßige Verteilung der Haufen in bezug auf die galaktische Ebene wird die Zugehörigkeit dieser Objekte zum Milchstraßensystem durch den Umstand gestützt, daß die allgemeine Intensität und Mächtigkeit der Milchstraßenwolken in der Gegend des scheinbaren Zentralpunktes ihr Maximum erreicht. Der Beweis, daß die Stellung der Sonne im Sternsystem in der Tat eine ausgeprägt exzentrische ist, und daß das Zentrum in einer Richtung nahe  $L=327^{\circ}$  zu suchen ist, wurde jedoch erst kürzlich durch die Sternzählungen schwacher Sterne in den Kapteynschen Selected Areas gegeben. Die Harvard-Groningen Durchmusterung wurde von Kreiken? zu einer Statistik der Dichte-

<sup>1</sup> M N 73, S. 359 (1913).

Mt Wllson Contr 151—157, 160, 161, 175, 176, 190 u. 195; Ap J 48—52 (1918—1920).

K Svenska Vet Akad Handi 43, Nr. 10 (1909).

M N 71, S. 693 (1911).

A N 192, S. 261 (1912).

Lund Medd Ser II, 19 (1918).

M N 85, S. 499 (1925); 86, S. 665 (1926).

verteilung ausgenutzt, und endlich das vorzügliche, auf exakten photometrischen Messungen gegründete Mount Wilson-Material von Seares¹ diskutlert. Für hellore Größen wurden auch die Kataloge der photographischen Himmelskarte benutzt. Die Abweichungen  $\Delta$  der Zahlen  $\log N_m(N_m = \text{Zahl}$  der Sterne pro Quadratgrad heller als die Größe m in der internationalen photographischen Skala) von einer mittleren rotationssymmetrischen Verteilung werden von Seares versuchsweise in der Form

$$\Delta = a + b\cos(L - L') \tag{26}$$

dargestellt Die Länge L' wurde für verschiedene Grenzgrößen zwischen m=9 und m=18 und für verschiedene galaktische Breiten ermittelt.

Eine etwas exzentrische Stellung der Sonne in einem sphäroldischen System von konstanter Dichtigkeit gibt als theoretischen Ausdruck für 🗸

$$s + F\cos(L - L_0) \tag{27}$$

 $L_0$  ist dann die Richtung gegen des Zentrum des Systems $^{\bullet}$  Aus einer systematischen Verschiedenheit für nördliche und südliche Breiten schließt Seares auf

eine mit der Sterngröße wechselnde Konrektion des Gouldschen Milchstraßenpols. Er führt daher in den theoretischen Ausdruck für  $\Delta$  auch die Terme

$$\pm G \mp k \cos(L - L_1) \tag{28}$$

ein, wo obere und untere Vorzeichen für närdliche bzw. südliche Breite gelten. Der wahre Pol, durch die Sterne einer gewissen Breite B ermittelt, ist um den Betrag p in der Länge  $L_1$  vom Gould-schen Pol entfernt, wo

$$p = \frac{h}{D}$$
,  $D = \frac{d \log N}{dB}$ . (29)

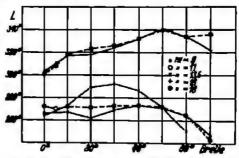


Abb 12. Die Länge des Zentrums (Ordinato) für verschiedene galaktische Zenen (Abssisse) und verschiedene Grenzgrößen

Durch Zusammensetzung von (27) und (28) bekommt man offenbar eine Form (26), wo aber L', a, b für nördliche und südliche Breiten verschieden ausfallen. Aus den empirischen Werten für L', a, b für nördliche und südliche Breiten berechnet man dann leicht die wahre Länge  $L_0$  der tiefsten Richtung im System und die wahre Amplitude der logarithmischen Sternzahlen, wie auch die Werte  $L_1$  und  $\phi$ . In dieser Weise bekommt Seares die Lagen des Pols für verschiedene Grenzgrößen, die in Zaff. 11 gegeben und diskutiert worden sind, und die folgenden Werte für die Länge des Zentrums

Die Werto  $L=L_0$  für verschiedene Zonen und Grenzgrößen werden in Abb. 12 dargestellt.

Shares findet eine markante parallele Verschlebung in  $L_0$ ,  $L_1$  und  $\phi$  mit der Sterngröße m. Da aber die Werte für  $L_1$  und  $\phi$  für hellere Größen erhebliche Differenzen gegen die in direkter Weise von van Rhijn ermittelten zolgen, so dürfte wohl die mehr indirekte Methode von Seares hier nicht als ganz einwandfrei zu bezeichnen sein.

Für die schwächsten Größen m=16 und 18 findet Seares  $L_0=319^\circ$ , was sehr wohl mit Shapleys Zentralpunkt für die Kugelhaufen,  $L=327^\circ$ ,

<sup>&</sup>lt;sup>1</sup> Mt Wilson Contr 346-347 = Ap J 67 (1928)

L baw L eind bei SEARES mit L baw L bezoichnet.

harmoniert. Kreiken hatte für die Grenzgröße 17 in seiner Arbeit  $L_0=314^\circ$  gefunden. Man kann diese Werte mit Hopmanns und Pannekoeks Resultaten für die Verteilung des galaktischen Lichts vergleichen (Ziff. 5 und 11). Hopmann fand ein sehr ausgeprägtes Maximum um  $L=315^\circ$  herum, während Pannekoek für die Länge des allgemeinen Lichtmaximums 323 $^\circ$  herleitete.

Die Verschiebung in  $L_0$  von 267° für m=9 bis 319° für die schwächsten Größen schreibt Seares, in Übereinstimmung mit den Ansichten vieler anderer Forscher, z. B. mit Hopmanns Ausführungen in seiner eben besprochenen Arbeit, dem Einfluß eines weit ausgedehnten "lokalen Systems" zu, das hauptsächlich die Verteilung der helleren Sterne bestimmt, während die Verteilung der schwächsten Größen dem großen System entspricht. Die Ausdehnung des lokalen Systems in der galaktischen Ebene schätzt er auf ungefähr 6000 Parsec. Da die Verschiebung des Pols für die helleren Größen gegen den Pol der hellen Heliumsterne vor sich geht und gleichzeitig die Länge des Konzentrationspunktes gegen die Länge der größten Häufigkeit dieser Sterne verschoben erscheint, schließt er auf eine Zusammengehörigkeit, und daß also der Haufen der nahen Heliumsterne den Kern des großen lokalen Systems bildet (vgl. Ziff. 19). Nach van Rhijns Resultaten scheint jedoch die Verschiebung des Pols für die Größen 9 bis 13,5 sehr zweifelhaft, was die Argumentation von Seares einigermaßen abschwächt.

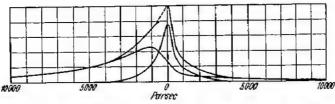


Abb. 13. Die Dichtefunktion nach Seares (obere Kurve) in zwei Telle, dem lokalen System und dem großen System entsprechend, zerlegt.

Um die Sachlage noch mehr zu beleuchten, berechnet Seares aus den Sternzahlen für die Längen  $L_0$  und  $180^\circ + L_0$  in der galaktischen Ebene mit Hilfe einer Gaussschen Luminositätskurve die entsprechende Dichtigkeitsverteilung nach

der Schwarzschildschen Methode. Für die Sterndichte D(r) findet er die Resultate der Tabelle 11.

Tabelle 11.

	D (7)		_ 1	D(r)	
r	$L_1$	180° + L,	,	L,	180° + L
1	1,00	1,00	6310	0,15	0,03
100	0,98	0,93	7943	,11	,02
200	,95	79	10000	,08	,014
316	,90 ,84 ,70	,63	12590	,06	,01
500	,84	,47	15850	,04	-
1000	,70	,28	19950	,03	
2000	,49	17	25120	,02	
3162	,33	,08			
3981	,33 ,27 ,20	,06			
5012	.20	,04			1

Die räumliche Sterndichtigkeit nimmt also viel schneller gegen das Antizentrum als gegen das Zentrum ab. Trotzdem ist ein großer Überschuß in unserer unmittelbaren Nähe ersichtlich. Seares versucht (Abb. 13) die Frequenz in zwei Kurven zu zerlegen, von denen die eine das lokale System, die andere das große System repräsentieren soll. Den totalen Durchmesser des großen Systems schätzt Seares zu 60000 bis 90000 Parsec. Daß die letztere Kurve asymmetrisch erscheint, deutet Seares als einen Einfluß der großen Absorptionsgebiete der Milchstraße in der zentralen Himmelsgegend.

Außer diesem Hinweis auf eine mögliche Absorption des Lichtes in gewissen Gegenden des Systems hat aber Srares die Möglichkeit der Erklärung der größeren Sterndichtigkeit in unserer Nähe durch eine allgemeine Absorption des Lichtes in den galaktischen Regionen nicht berücksichtigt Wir werden später Gelegenheit haben, ein wenig auf diese Frage einzugehen,

Unter früheren wichtigen Arbeiten anderer in diesem Zusammenhang nicht erwähnter Autoren, die mit weniger Vollständigkeit des zur Verfügung stehenden Materials Abweichungen von einer rotationssymmetrischen Verteilung studiert haben, sind zu nennen die von H Nort, H. C. Plummer und H H Turner.

J. HALM's stellt ornstlich in Frage, ob die gewöhnliche Annahme einer vom Orto im System unabhängigen Leuchtkraftsfunktion wirklich als annähernd zutreffend anzuschen ist. Es scheint nach seiner Ansicht vielmehr, daß die Heterogenität der scheinbaren Verteilung eher durch Schwankungen der Leuchtkraftsfunktion als durch Variationen der räumhehen Dichte erklärt werden kann. Es scheint sogar möglich, daß die Sterne in der Milchstraße scheinbar zahlreicher vorkommen, nicht weil sie räumlich zusammengedrängt sind, sondern weil sie eine größere absolute Leuchtkraft besitzen.

Von großer Bedeutung ist auch die Untersuchung Panneroers über die Dichtigkeitsvertellung in unserer näheren Umgebung auf Grund einer erneuten sorgfältigen Analyse der Durchmusterungskataloge Er verläßt vollkommen die schematischen Annahmen des "typischen Systems" und sucht m unserer Umgebung die wahren Kondensationen zu bestimmen. Er vertritt auch die Ansicht, daß ein lokales System als eine selbständige geschlossene Einheit, eine "Wolke", nicht existiert, sondern sich in eine Mange kleinerer Gruppen, die als Indi-

viduen in das große System eingehen, auflösen läßt,

19. Die Vertellungsgesetze verschiedener Spektraltypen. Die große Streuung der allgemeinen Louchtkraftsfunktion der Sterne und die wahrscheinlich bedoutendo Abweichung dieser Funktion von einer Gaussschen Fehlerkurve für die schwachen absoluten Helligkeiten macht es sehr schwierig oder sogar unmöglich, ohne eine Aufspaltung des Materials in Klassen von kleinerer Dispersion alchere Resultate über die Dichtigkeitsverteilung im Sternsystem zu bekommen. Rine partielle Aufspaltung der genannten Art bietet schon die Klassifizierung in die Harvard-Spektraltypen und auch die in großen Zügen mit dieser Klassifizierung aquivalenten Bestimmungen der Sternfarbe, Für die "frühen", heißen Spaktraltypen bedeutet nämlich die Klassifizierung oder Ferbenbestimmung eine Grupplerung nach absoluter Größe mit verhältnismäßig kleiner Streuung innerhalb der Gruppen. Da weiter die spezielleren Methoden zur spektrographischen Bestimmung absoluter Größen gegenwärtig auch für schwache Sterne, wenn auch in mehr summarischer Form, verwendbar sind, so eröffnet sich hier ein Weg zu einer genaueren Analyse der Sternverteilung in den verschiedenen Richtungen von unserem Ort im System aus. Wir sind jedoch auf diesem Geblote noch kaum über die Pionierarbeit hinausgekommen. Wir wollen hier die Hauptergubnisso der Spektraldurchmusterungen in bezug auf die allgemeine Dichtigkeitsverteilung unserer näheren Umgebung im Starnsystem kurz erwähnen und später (Ziff. 22) die spezielleren Untersuchungen der Milchstraßenregionen behandoln.

Das gegonwärtig wichtigste statistisch ausgenutzte Material ist in dem Draffir-Katalog der Harvard-Stornwarte enthalten. Die scheinbare Verteilung

<sup>&</sup>lt;sup>1</sup> Rocherches astronomiques de l'Obs d'Utrocht VII (1917)

<sup>8</sup> M N 78, S, 668 (1918).

<sup>8</sup> M N 85, B, 610 (1925).

MN 78, S. 668 (1918). MN 80, S. 162 (1919).

Publ Astr Inst Univ Amsterdam Nr. 1 (1924); Nr. 2 (1929)

verschiedener Spektraltypen am Himmel ist ausstihrlich von G. ZAPPA1. H. Shapley<sup>2</sup>, C. V. L. Charlier<sup>8</sup>, A. Pannekoek<sup>4</sup> und O. Seydl<sup>5</sup> statistisch untersucht worden. SEYDL gibt im zweiten Teil seiner Arbeit für Sterne heller als 7<sup>m</sup>,0 die scheinbare Dichtigkeitsverteilung der verschiedenen Spektraltypen in galaktischen Koordinaten in einer Serie von Karten wieder. Die zuerst von E. C. Pickering nachgewiesene Variation der scheinbaren galaktischen Konzentration mit der Spektralklasse kommt in diesen Untersuchungen sehr schön zum Vorschein. Die viel kleinere galaktische Konzentration der Spektralklassen. von F bis M, mit den Klassen B und A verglichen, wurde oft als ein im wesentlichen scheinbarer Effekt gedeutet, der als eine Folge einer mit der Spektralklasse sich ändernden mittleren absoluten Leuchtkraft der Sterne auftritt. Eine Vergrößerung der absoluten Leuchtkraft bedeutet nämlich einen Zuwachs der mittleren Entfernung für eine und dieselbe scheinbare Größe, was infolge der allgemeinen Konzentration der Sterne gegen die galaktische Ebene eine vergrößerte scheinbare Konzentration gegen die Milchstraße mit sich bringt. Wenn auch dieser Erklärungsgrund für das Intervall B-F einigermaßen zutrifft, ist es doch wegen der ziemlich großen absoluten Helligkeiten der großen Mehrzahl der K- und M-Sterne des Katalogs, die kaum der mittleren Helligkeit der A-Sterne nachstehen, durchaus klar, daß das Phänomen auch auf reelle Verschiedenheiten in der Anhäufung gegen die Milchstraßenebene zurtickzuführen ist. Einen direkten Nachweis in dieser Richtung hat P. J. van Rhijn gegeben, der eine Trennung verschiedener Spektraltypen bei Bestimmung der Leuchtkrafts- und Dichtigkeitsverteilung nach der Kapteyn-Methode unternommen hat. Die Abnahme der absoluten Dichtigkeit der A-Sterne und der Riesensterne späterer Spektraltypen mit wachsender Entfernung von der galaktischen Ebene ist auch von B. LINDBLAD<sup>8</sup> und H. Petersson<sup>9</sup> bestimmt worden. Die kleinere Konzentration der späten Riesen tritt hier sehr deutlich hervor und wird als eine Folgeder für diese Sterne größeren Dispersion der Geschwindigkeitskomponente senkrecht zur Milchstraße gedeutet (vgl. Ziff. 28).

Die Dichtigkeitsverteilung der A-Sterne in der Richtung gegen den galaktischen Pol ist von K. G. Malmouist10 ermittelt worden auf Grund einer Bestimmung der Farbenäquivalente nach der Methode von Seares für 3700 Sterno innerhalb 10° Distanz von dem galaktischen Pol, von denen jedoch nur eine kleine Prozentzahl A-Sterne sind.

Zu den bedeutendsten aus dem Harvard-Material der helleren Sterne gewonnenen stellarstatistischen Resultaten gehört dasjenige fiber die Verteilung der Sterne der Spektralklasse B, der Heliumsterne, in unserer Umgebung. Wichtige Untersuchungen sind hier von Kapteyn<sup>11</sup>, Charlier<sup>12</sup>, Shapley<sup>18</sup>, B.P.Gerasimo-

<sup>&</sup>lt;sup>1</sup> Publ R Specola di Collurania (A) 1, S. 59 (1921). <sup>2</sup> Harv Circ 240 (1922); 248 (1923).

<sup>8</sup> Lund Medd Scr II, 36 = K Svenska Vot Akad Handl 4, Nr. 3 (1927).

<sup>4</sup> Publ Astr Inst Univ Amsterdam Nr. 2 (1929). <sup>5</sup> Publ Obs Nat Prague 6 (1929).

<sup>5</sup> Harv Ann 26, S. 152 (1891); 56, S. 1 (1912). <sup>7</sup> Groningen Publ 38, Tab. 27, 45 (1925).

<sup>8</sup> Nova Acta Reg. Soc. Scient. Upsallensis, Volumen extra ordinem 1927 = Upsala Medd 11; Ark Mat Astr Fys 19 B, Nr. 15 (1926) = Upsala Medd 14.

<sup>9</sup> The Distribution of Distances and Velocities of Stars in the Carrington Zone on the Bosis of Spacesophetematric Application Distances and Velocities of Stars in the Carrington Zone on the Bosis of Spacesophetematric Application Distances and Velocities of Stars in the Carrington Zone on the Bosis of Spacesophetematric Application Distances and Velocities of Stars in the Carrington Zone on the Bosis of Spacesophetematric Application Distances and Velocities of Stars in the Carrington Zone on the Bosis of Spacesophetematric Application Distances and Velocities of Stars in the Carrington Zone on the Bosis of Spacesophetematric Application Distances and Velocities of Stars in the Carrington Zone on the Bosis of Spacesophetematric Application Distances and Velocities of Stars in the Carrington Zone on the Bosis of Spacesophetematric Application Distances and Velocities of Stars in the Carrington Zone on the Spacesophetematric Application Distances and Velocities of Stars in the Carrington Zone on the Spacesophetematric Application Distances and Velocities of Stars in the Carrington Zone on the Spacesophetematric Application Distances and Velocities of Stars in the Carrington Zone on the Spacesophetematric Application Distances and Velocities of Stars in the Carrington Zone on the Spacesophetematric Application Distances and Velocities of Stars in the Carrington Zone on the Spacesophetematric Application Distances and Velocities of Stars in the Carrington Zone on the Spacesophetematric Application Distances and Velocities and Velocities

Basis of Spectrophotometric Analysis. Diss. Upsala 1927 = Upsala Medd 29.

<sup>10</sup> Lund Medd Ser II Nr. 37 und 46 (1927).

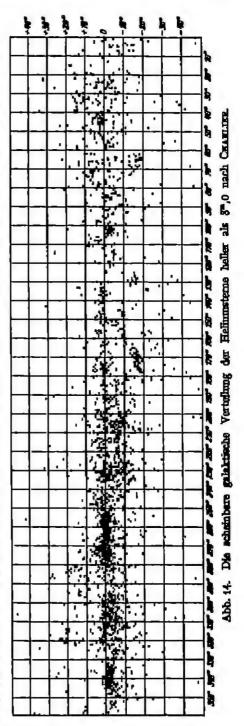
<sup>11</sup> Mt Wilson Contr 82 = Ap J 40, S. 43 (1914); Mt Wilson Contr 147 = Ap J 47, S. 104, 146 u. 255 (1918).

Nova Acta Reg. Soc, Scient, Upsaliensis (IV) 4, Nr. 7 (1916); Ibid., Volumen extra. ordinem 1927; Lund Modd Ser II, 14 und 34.

<sup>&</sup>lt;sup>18</sup> Mt Wilson Contr 157 = Ap J 49, S. 311 (1918); Mt Wilson Comm 54 (1918); 64 (1919); Scientia, Marz 1920; A N Jub.-Nr. S. 25 (1921); Harv Circ 239 (1922); Harv Bull 846, S. 12 (1927).

VIČ1 und PANNEKOEK® nusgoführt worden Die Hellumsterne zeigen eine sehr starke scheinbare Konzentration gegen die Milchstraße hin, aber wie oben (Ziff. 13) crwähnt wurde, hat die Symmetricebene der helleren B-Sterne emo beträchtliche Neigung gegen den aus den Milchstraßenwolken ermittelten größten Kreis Charlier gibt für den Pol der helleren B-Sterne seiner ersten Arbeit R.A. 183°,34, Dekl +28°,74, was bel Annahme des Gouldschen Milchstraßenpoles den galaktischen Koordinaten  $L = 165^{\circ}$ ,  $B = +83^{\circ}$ , 4 enterprish und ım System der Tabelle 7, Ziff 11,  $L = 158^{\circ}$ ,  $B = +80^{\circ}$ , 0 gibt. Die Neigung der Symmotrieebene gegen die Gouldscho Milchstraßenlinie ist also 6°,6, mit dem aufsteigenden Knoten in L = 255°; dle Nelgung gegen die mittlere Ebene der schwachen Sterne beträgt 10°,0. SHAPLEY zelgt, daß diese Noigung mit abnohmender Helligkelt abnimmt und schon zwischen den Größen 7 und 8 fast vollständig verschwindet Dasselhe Verhältnis wiederholt sich in geringerem Maße für die A-Sterne Die Verteilung der helleren Sterne zeigt auch hier eine gewisse Neigung der Symmetricebeno gegon die Milchatraßo, welche Neigung für schwächere Größen vorschwindet.

Die scheinbare Verteilung der Heliamstorno heller als 8m,0 am Himmel wird nach CHARLIER in Abb. 14 illustriert. Le ist offenbar, in welchem hohen Grade diese Storne in getrennten Flocken von beträchtlicher Konzentration auftroton, was in KAPTEYNS Arbeit eine große Rolle spielt und neuerdings von Pannekoek besonders hervorgehohen wird. Ein Maximum der Anhäufung findet sich in der Carinagegend, um L = 260° herum. Die Projektion der raumlichen Verteilung auf die Milchstraßenebene wird in Abb, 15 nach CHAR-LIER wiedergegeben. Die Entfernungen der individuellen Sterne sind unter der Annahme konstanter absoluter Leuchtkraft innerhalb der Untergruppen Bo,



<sup>1</sup> V J S 61, S 219 (1926). 1 L. 0 SHAPLEY and CANNON, Harv Circ 229 (1922).

B1 usw. ermittelt worden. Man bekommt hier den Eindruck, daß diese Sterne eine gewisse Einheit bilden. Die Aufspaltung in kleinere Gruppen, die in der scheinbaren Verteilung so deutlich hervortritt, ist aber auch hier zu spüren. Die äußere Begrenzung des Haufens ist von der Grenzgröße des Materials (m=8,0) bedingt. Für das Zentrum des Haufens findet Charlier eine Entfernung von 63 Parsec (13 Siriometer) in der Richtung  $L=243\,^{\circ},90$ ,  $B=-13\,^{\circ},80$ .

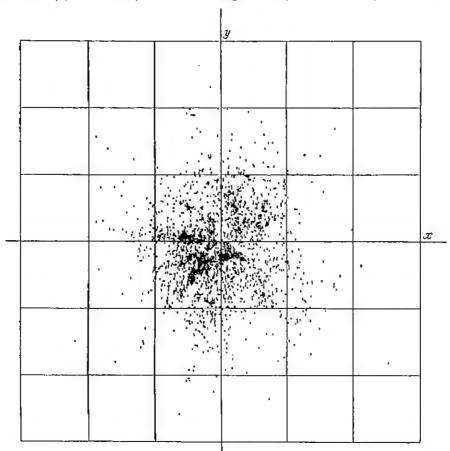


Abb. 15. Die Verteilung der Hellumsterne (Bo bis B5) heller als  $8^m$ ,0 in der galaktischen Ebene (X-Achse gegen  $L = 0^\circ$  gerichtet).

Gerasimovič teilt die Sterne in zwei Gruppen, heller und schwächer als die Größe 6,7, und findet für das Zentrum dieser Gruppen

$$m < 6.7$$
:  $L = 225$ °,5,  $B = -12$ °,0,  $R = 77$  Parsec,  $m > 6.7$ :  $L = 268$ °,5,  $B = -9$ °,0,  $R = 204$  Parsec.

Dieses Resultat stimmt mit den Ansichten Shapleys überein, nach denen wir hauptsächlich in der helleren Gruppe die Mitglieder eines lokalen Haufens vor uns haben, während wir für schwächere Helligkeiten es mit einer Mischung zwischen Haufensternen und Sternen des allgemeinen Milchstraßenstratums zu tun haben. Gerasimovič hat auch die allgemeinen Dichtigkeitsflächen der B-Sterne ermittelt. Die Abplattung der Flächen vermindert sich je nach der

Entfernung von der Sonne. Der Halbmesser des ganzen lokalen Haufens sollte wenigstens 1000 Parsec betragen. Nach Pannekoek löst sich aber der "lokale Haufen" der B-Sterne in eine Menge kleinerer, voneinander unabhängiger Haufen oder Ströme auf

Die Kurven gleicher Dichtigkeit in der Umgebung der Sonne hat KREIKEN<sup>1</sup>

für B- und A-Sterne zu ziehen versucht,

G. Shajn<sup>®</sup> hat einen Versuch gemacht, die Hauptzüge der räumlichen Dichtigkeitsverteilung für B-, A-, F-, K- und M-Sterne aus dem Material des Harvard-Katalogs zu ermitteln. Die Abhängigkeit der scheinbaren galaktischen Konzentration vom Spektraltypus in der Serie O bis F wird als eine Folge der Veränderung in mittlerer absoluter Größe gedeutet; die verhältnismäßig kleine galaktische Konzentration der K-Sterne ist nach Shajn auf eine Inhomogenität dieser Sterne in bezug auf ihre absolute Größe zurückzuführen, insbesondere auf eine Beimischung von Sternen, die intermediär zwischen "Riesen" und "Zwergen" sind, unter die Sterne in den schwächeren Größenklassen. Für die M-Sterne muß er aber eine reelle Abweichung der räumhehen Dichtigkeitsverteilung von ihrem gewähnlichen Charakter annehmen. Die Schneihgkeit der Dichtigkeitsabnahme mit der Entfernung ist für fast alle Klassen beträchtlich größer als die von Kapthyn und van Rhijn für Sterne im allgemeinen gefundene.

Was die räumliche Dichtigkeitsverteilung in der Nähe der galaktischen Ebene bis zu größeren Entfernungen betrifft, so führen die weiteren Untersuchungen auf diesem Gebiet, angesichts der sehr erheblichen lokalen Verschiedenheiten in dem galaktischen Gürtel, mit Notwendigkeit auf detaillierte Untersuchungen der hellen und dunklen Partien der Milchstraße, die wir in Ziff. 22

näher besprechen werden.

Zur Beurteilung der allgemeineren Fragen über die galaktische Konzentration für verschiedene Spektraltypen wird in der Zukunft ein vorzügliches Material in den Spektraluntersuchungen der Solected Areas vorliegen. Ein wichtiger Beitrag liegt hier schon in F Beckers Spektraldurchmusterung der Kapteyn-Eichfelder des Südhimmels vor Dieso Arbeit enthält auch eine vorläufige Statistik über die Verteilung der Spektralklassen nach galaktischer Breite und nach der scheinbaren Helligkeit sowie über die räumliche Verteilung der Sterne. Weitere Beiträge werden hier in der Zukunft die Sternwarten Mount Wilson und Hamburg gebon, wo die Sterne der Kapteynschen Felder bis zu etwa der Größe 12 klassifiziert werden.

Eine auf ausgewählte Partien des Himmels sich beziehende Spektraluntersuchung, die in gewissen Gegenden bis zur Größe 11,5 bis 12 reicht, wird von Miss Cannon an der Harvard-Sternwalte in der "Henry Draphe-Extension"

ausgeführt.

Auf der Stornwarte Stockholm ist gegenwärtig eine allgemeine Untersuchung der Spektra in gewissen Milchstraßenregionen bis zu etwa der Größe 13 begonnen worden. Es wird hier besonders eine Berlicksichtigung der spektralphotometrischen Kriterien, die zur Beurteilung der absoluten Größen der Sterne dienen können, beabsichtigt.

20. Die galaktische Verteilung spezieller Objekte von großer absoluter Leuchtkraft. Die Objekte von sehr großer absoluter Helligkeit zeigen in der Regel eine außerordentlich markante scheinbare Konzentration gegen die Milch-

<sup>&</sup>lt;sup>1</sup> M N 85, S. 985 (1925). 
<sup>8</sup> A N 232, S. 17 (1928).
<sup>8</sup> Publ Astrophys Obs Potsdam Nr. 88, 89, 90 (1929—1931).

Publi Astrophys One Potential Rr. 88, 89, 90 (1949-1931).
 Über den Fortschritt dieser Arbeit a. besonders Snapley, "Sidereal Explorations".
 The Rice Institute Pamphlet 18, Nr. 2 - Harv Reprint 68 (1931).

straße. Wahrscheinlich haben wir hier eine Kombination von zwei verschiedenen Ursachen, teils einen scheinbaren Effekt der größeren mittleren Entfernung, teils aber eine allgemeine Vergrößerung der absoluten galaktischen Konzentration mit steigender absoluter Helligkeit (vgl. Ziff. 19). Um zwischen diesen beiden Effekten zu unterscheiden, müssen wir aus der scheinbaren Verteilung die wahre Verteilung im Raume herleiten. Bei unserer oft mangelhaften Kenntnis der Entfernungen ist dies in vielen Fällen nur in unvollständiger Weise möglich.

Eine Folge der großen scheinbaren galaktischen Konzentration einer bestimmten Gruppe ist es zunächst, daß auch mit einer geringen Anzahl von Objekten die Feststellung der Lage der Symmetrieebene möglich wird. E. HERTZsprung1 hat (Tab. 12) eine Zusammenstellung der Lagen des Poles für ver-

schiedene Klassen von Objekten gegeben.

Tabelle 12.

Klasse	Pol der Konz	Anzahl der	
Kiase	А	D	Objekto
Holiumsterne (Oc5 bis B9). Spektraltypus N Oa bis Oc	182°,1 194 ,2 190 ,7	- -27°,9 27 ,4 26 ,9	1402 228 87
Bedeckungsveränderl	188 ,2 195 ,9 189 ,1	25 ,8 26 ,8 26 ,3	150 60 98
Gasnobel	192 .7	28 ,1	130

Für 97 Sterne vom Typus Oa-Oc5 findet W. GYLLENBERG<sup>2</sup> unter der Annahme einer ellipsoidischen Verteilung für die kürzeste Achse die Richtung  $A = 191^{\circ},28, D = +27^{\circ},13.$ 

B. P. Gerasimovič<sup>3</sup> findet für 144 O-Sterne des Draper-Katalogs

$$A = 189^{\circ} 13', D = +27^{\circ} 22',$$

und für 78 planetarische Nebel

$$A = 192^{\circ} 13', D = +28^{\circ} 28',$$

unter Verwendung der Newcombschen Berechnungsmethode,

J. Schilt findet für 340 c-Sterne eine sehr gute Übereinstimmung mit der galaktischen Ebene nach Pickering (Lage des Pols  $A = 190^{\circ}$ ,  $D = +28^{\circ}$ ).

Es ist übrigens augenscheinlich, daß alle Klassen außer der ersten in Tabelle 12, welche die B-Sterne umfaßt, eine Lage des Pols in sehr guter Übereinstimmung mit dem allgemeinen Milchstraßenpol (Ziff. 11) ergeben.

Außer den verschiedenen Graden von galaktischer Konzentration ist es auch von großer Bedeutung, daß in vielen Fällen die galaktische Länge einen sehr merklichen Einfluß auf die scheinbare Verteilung zeigt. Allerdings muß man hier vorsichtig sein, da eine Selektion auf Grund einer mehr oder weniger intensiven Beobachtung gewisser Himmelsregionen vorliegen kann.

N. C. Dunka hatte auf die große galaktische Konzentration der Sterne von Secchis Typus IV (Harvard-Typus N und R) aufmerksam gemacht. Diese Erscheinung wurde von T. E. Espine und J. A. Parkhurst näher untersucht und bestätigt. Später hat Espin<sup>8</sup> die galaktische Verteilung verschiedener Objekte von pekuliaren Spektraltypen untersucht. Die größte Konzentration zeigen

<sup>1</sup> A N 192, S. 261 (1912).

<sup>\*</sup> Lund Medd 75 (1917).

<sup>&</sup>lt;sup>a</sup> AN 226, S. 327 (1926). 
<sup>b</sup> BAN 2, S. 47 (1924).
<sup>c</sup> Sur les étoiles à spectres de la troisième classe. K Svenska Vet Akad Handi 21, Nr. 2. S. 126 (1885). Yerkes Publ 2, S. 127 (1903). <sup>6</sup> Ap J 10, S. 169 (1899).

<sup>6</sup> J Can RAS 7, S. 79 (1913).

nach ihm die Wolf-Rayet-Sterno (Typus O), von denen etwa 98% zwischen galaktuscher Breite 0° und ±10° lægen Dann folgen in der Reihe abnehmender Konzentration die nouen Sterne, die Sterne mit hellen Wasserstofflinien, die Gasnebel und die N-Sterne Auffallend ist, daß z B die R-Sterne eine sehr viel kleinere Konzentration als die N-Sterne aufweisen Espin findet auch die mittlere galaktische Breite in den einzelnen Gruppen antschieden negativ, was auf eine Lage der Sonne nördlich in bozug auf die galaktische Symmetricebene hinweist Er untersucht auch die Verteilung nach der galaktischen Länge. Für Gasnebel und noue Sterne findet er eine Konzentration gegen L = 395° bzw 325°

Auf die Anhäufung schwacher Novae im Sagittariusgebiet hat besonders K. LUNDMARK<sup>1</sup> animarksam gemacht. Es bestätigt sich hier, dom ummittelbaren Eindruck nach, die Vermutung, welche wir schon vorher mehrfach besprochen haben und welche wir später (Ziff, 28) auf Grund neuer Evidenz von ganz anderer Natur nochmals aufnehmen werden, daß die Partien der Milchstraße, welche die Sternbilder Sagittarius, Scorpius und Ophluchus berühren, im wesentlichen einem gewaltigen Zentralkern unseres Sternsystoms entsprechen. Ein Vergleich mit der Verteilung der Novae in der Zentralregion des großen Andromedanebels ist in vieler Hinsicht sohr bestechend Diese Tatsachen sind aber schon ausführlich an anderer Stelle in diesem Handbuch behandelt worden. P Doig. hat die Verteilung in galaktischer Länge für verschiedene Objekte dargelegt; er zeigt besonders eine Verschiebung des Konzentrationspunktes vom Monoceros-Argo-Gebiet zum Centaurus-Sagittarius-Gebiet, wenn wir von dem B-Typus und den offenen Sternhaufen zu den O-Sternen, planetarischen Nebeln, langperiodischen Veränderlichen, Novne und Kugelsternhaufen übergehen

GYLLENBERG' gibt die raumliche Verteilung der O-Sterne gemäß der Methode. walche CHARLIER für die B-Sterne benutzt hat. Den Zentralpunkt für 97 Sterne findet or in der Entfernung 263 Parsec in der Richtung  $L = 328^{\circ}, B = -4^{\circ}$ . Eine sehr eingehende Untersuchung fiber die scheinbare und räumliche Verteilung der c-Sterne hat Schilt in einer obenerwähnten Arbeit gegeben. Wenn drei spezielle Gruppen ausgeschlossen werden, findet Schult eine Anordnung dieser Sterne im Raume, welche der von CHARLIER für die B-Sterne gefundenen Verteilung ähnelt. Wie oben erwähnt, fällt aber die Symmetrieebene der e-Sterne mit der allgemeinen "galaktischen" zusammen. P. Doigs untersucht die Verteilung der "Pseudo-Cephelden" und Übergiganten der Spektraltypen F bis M. Das Material ist jedoch für stidliche Deklination sehr unvollständig C. LUPLAU-JANSSEN und G. HAARH® haben die räumliche Verteilung der N- und R-Sterne studiert und auf die obenerwähnte große Verschiedenheit der Konzentration

gegen die galaktische Ebene für diese zwei Klassen hingewiesen

Eine sehr wichtige Aufgabe für die Kenntnis unseres Systems besteht im systematischen Aufsuchen von 6 Cephel-Veründerlichen, de die Relation zwischen Periode und absoluter Größe eine ziemlich genaue Ermittlung der räumlichen Vertellung erlaubt, wenn wir von Absorptionserscheinungen im interstellaren Raumo abschon Hentzsprung untersucht die raumliche Verteilung der & Cephol-Sterne und der Sterne vom Typus Oes. Shapley hat in Verbindung mit seinen Untersuchungen über die Kugelhaufen (Zilf 18) die Verteilung der galaktischen & Caphel-Sterne ausführlich studiert. Eine sehr eingehende Untersuchung über die galaktische Verteilung der d Cephel-Sterne gibt M Güssow. Wehlbekannt

Publ A S P 33, S 219 u 225 (1921), Pop Astr Tidskr 4, S, 127 (1923).

Da Handb VI, S, 257 (1928)

J B A A 33, S 238 (1923)

L. c.

J B A A 36, S, 292 (1926).

A N 214, S 383 (1921).

Kritischo Zusammenstellung sämtlicher Beobschtungsorgebnisse der Veränderlichen vom d Cophel-Typus und Kritik der Eddingronschen Pulsationatheorie, Inaug.-Diss. Borlin 1924

ist der auffällige Unterschied in galaktischer Konzentration zwischen den langperiodischen und kurzperiodischen Sternen dieser Art¹. Die Häufigkeit der langperiodischen  $\delta$  Cephei-Sterne zeigt nach M. Güssow Maxima in den Längen 250° bis 260° und 330° bis 360°. J. Schilt² hat die Häufigkeit der Perioden für verschiedene Milchstraßengegenden untersucht. In der Sagittarius-Aquila-Region zeigt die Häufigkeit ein Maximum für  $\log P = 0.84$ , während für andere Regionen das Maximum für entschieden kürzere Perioden eintritt.

Eine der großartigsten Arbeiten für die Erforschung der Milchstraßenstruktur wird gegenwärtig auf der Harvard-Sternwarte und ihrer südlichen Filiale ausgeführt, wo in mehr als 200 Feldern, welche die ganze Zentralzone der Milchstraße bis  $\pm 20^{\circ}$  Breite bedecken, durch wiederholte Aufnahmen alle Veränderlichen systematisch aufgesucht und in ihrem Lichtwechsel ver-

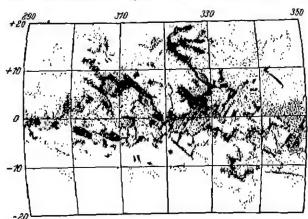


Abb. 16. Vordunklungsgebiete in der Zentralgegend der Milchstraße,

folgt werden3. Die ersten Früchte dieses Planes sind schon erschienen in mehreren Aufsätzen von H. SHAPLEY und H. W. SWOPE unter dem Titel "Studies of the Galactic Center4". Besondere Aufmerksamkeit wird nämlich darauf verwandt, die Lage, Entfernung und Dichte des galaktischen Zentrums, welches, wie oben erwähnt, großer Wahrscheinlichkeit in der Sagittariusregion der Milchstraße gelegen ist, zu untersuchen. Es werden kurz- und lang-

periodische & Cephei-Sterne, langperiodische Veränderliche, Novae und Bedeckungs-Veränderliche studiert.

In einem Feld von 70 Quadratgrad um das vermutete Zentrum herum wurden unter 450 Veränderlichen 78 kurzperiodische & Cephei-Sterne oder "Sternhaufenveränderliche" gefunden. Die scheinbaren Helligkeiten dieser Sterne sind größtenteils zwischen 15<sup>m</sup>,1 und 16<sup>m</sup>,2 verteilt, mit einem Maximum bei 15<sup>m</sup>,7. Shapley schließt, daß diese Sterne zu einer Art von System gehören, dessen mittlere Entfernung er zu 14400 Parsec schätzt. Da dieser Wert gut mit der früher von Shapley gefundenen Entfernung zum Zentrum im System der Kugelhaufen übereinstimmt, so ist es sehr wahrscheinlich, daß dieses System mit dem Kern unseres Milchstraßensystems identifiziert werden kann.

Auch die Verteilung der langperiodischen δ Cephei-Veränderlichen nach scheinbarer Größe, die ein sehr starkes Maximum bei 14<sup>m</sup>,8 aufweist, spricht für die Existenz eines scharf ausgeprägten Kerns im galaktischen System.

Die erwähnten Studien von Shapley und seinen Mitarbeitern umfassen auch eine wichtige Untersuchung der Verdunklungsgebiete in der betreffenden

<sup>1</sup> Vgl. Ludendorff, Handb. der Astrophys. VI, Kap. 2, Ziff. 63.

Mt Wilson Contr 315 = Ap J 64, S. 149 (1926).
 Siche besonders "Sidereal Explorations". The Rice Institute Pamphlet 18, Nr. 2
 Harv Repr 68 (1931).

<sup>4</sup> Wash Nat Ac Proc 14, S. 825, 830 u. 958 (1928), 15, S. 174 (1929) = Harv Repr 51, 52, 53, 58.

Himmelsgegend und Erwägungen über die Durchsichtigkeitsverhältnisse des interstelluren Raumes Shapley hat die auf den Photographien erkennbaren Verdunklungsgebiete der Zentralgegend in einer Zeichnung durch Schrafflerung von verschiedener Stärke zu markieren versucht (Abb. 16) Das Gebiet am Himmel entspricht dem des zusammengesetzten Bildes in Abb. 7. Er hat dann auch die Verteilung der extragalaktischen Nebel in demselben Gebiet untersucht, um daraus weitere Schlüsse über die Durchsichtigkeitsverhältnisse dieser Gegend ziehen zu können (Abb 17).

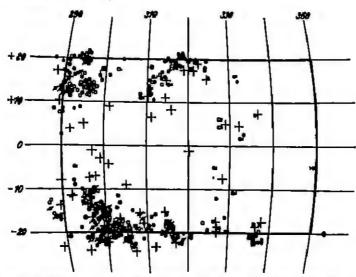


Abb 17. Die Verteilung der extragalaktischen Nebel in der Zontralgegend. In der Abbildung repräsentieren große Punkte NGC-Objekte, kleine Punkte IC-Objekte oder Nebel in publisierten Harvard-Katalogen, die kleinen Kreise neue auf dem Harvard-Observatorium entdeckte Nebel. Die durch eine Linie gekrenzten Punkte sind dentlich spiralförmige Objekte. Die Kreuze geben die Zentra der langezponierten Platten an.

Sharley zieht den Schluß, daß, wenngleich leicht festzustellendes absorbierendes Material einige galaktische Wolken in der Zentralregion und auch das Zentrum selbst verbirgt, die Milchstraße an den Grenzen dieser Dunkelnebel vollkommen durchsichtig ist und demnach die Beobachtung der entferntesten Sterne unseres Systems wie auch der außeren, wahrscheinlich Millionen Lichtjahre von uns entfernten "Milchstraßen" zuläßt

P. TEN BRUGGENCATE<sup>1</sup> hat in Verbindung mit einer Untersuchung über die räumliche Verteilung von neuentdeckten & Cephei-Variabela mit Perioden von mehr als einem Tage einige Bomerkungen über Shapleys größeres galaktisches System gemacht. Die Veränderlichen der betreffenden Klasse kommen im Ranme unter die offenen Sternhaufen gemischt vor. Es sollen alle offenen Sternhaufen und mehrere Kugelhaufen in den Sternweiken der Milchstraße selbet liegen

Die Eigenschaften der Sternhaufen werden an anderem Orte in diesem Handbuch ausführlich behandelt. Hier sollen nur der Vollständigkeit wegen einige fundamentale Tatsachen betroffs der Verteilung der Haufen im Raume Erwähnung finden.

Die offenen Sternhaufen sind Objekte von außerordentlich starker galaktischer Konzentration. Vorsuche, ihre Verteilung im Raume zu bestimmen,

<sup>1</sup> BAN 4, S 195 (1928).

sind von C. V. L. CHARLIER<sup>1</sup>, H. SHAPLEY<sup>2</sup>, S. RAAB<sup>3</sup>, P. COLLINDER<sup>4</sup> und R. TRÜMPLER<sup>5</sup> gemacht worden. Die Verteilung der zur Zeit bekaunten Haufen, wie sie besonders in den zwei letztgenannten Arbeiten zutage tritt, kann folgendermaßen kurz charakterisiert werden. Die Symmetricebene des Systems erscheint ein wenig schief gegenüber der gewöhnlich angenommenen galaktischen Ebene. TRÜMPLER findet für den Pol des Haufensystems

$$A = 192^{\circ}, 6, D = +27^{\circ}, 7 (1900).$$

Wenn wir vom Gouldschen Pol ausgehen und die entsprechenden galaktischen Koordinaten des Haufenpols suchen, bekommen wir nach TRÜMPLER

$$L = 10^{\circ}, B = +88^{\circ}, 3.$$

Es ist sehr bemerkenswert, daß diese Lage des Pols in derselben Richtung von Goulds Pol abweicht wie die Lage des Pols für die schwachen Größenklassen in Tabelle 6 (Ziff, 11) gemäß den Untersuchungen von Seares und van Rhijn. Die Abweichung ist jedoch für die Haufen von einem kleineren Betrag, was nach TRUMPLER andeutet, daß das System der Haufen weiter in den Raum hinausreicht als im Durchschnitt die Sterne 18. Größe. Das System der bekannten Haufen bildet eine sehr flache, nahe kreisförmige Scheibe von etwa 8000 Parsec Durchmesser und mit einem beträchtlichen Zuwachs an Dichtigkeit gegen das Zentrum hin, Dieses Zentrum befindet sich ziemlich nahe der Sonne. Wenn wir die zwei galaktischen Koordinatenachsen so ziehen, daß gleich viele Haufen auf beiden Seiten jeder Achse liegen, so bekommen wir nach Trümpler den Schnittpunkt in der Entfernung 350 Parsec in der galaktischen Länge 247°. Dies deutet an, daß die dichte Zentralregion des Haufensystems dem Phänomen des "lokalen Systems" entspricht. Diese Zentralregion geht aber allmählich in die allgemeinen Milchstraßenregionen über, und wir haben oben gesehen, daß die Symmetrieebene der Haufen im ganzen gar nicht im Sinne des Gouldschen Kreises oder der Symmetrieebene der helleren B-Sterne von der allgemeinen Milchstraßenebene abweicht, sondern in ihrer Lage mit der Tendenz der Sterne von sehr schwachen Größenklassen übereinstimmt.

Wenn wir zu den Kugelhaufen übergehen, so spricht für ihre Zugehörigkeit zum Milchstraßensystem, außer ihrer nahezu symmetrischen Anordnung in bezug auf die galaktische Ebene und ihrer größten Häufigkeit in der Gegend der hellsten Milchstraßenwolken, unter anderem der Umstand, daß es auch Objekte großer individueller Leuchtkraft gibt, die in ihrer Verteilung gewissermaßen eine Zwischenstellung zwischen den Kugelhaufen und den Klassen von großer galaktischer Konzentration einnehmen. Eine solche Klasse bilden die planetarischen Nebel, deren Verteilung von A. R. Hinks<sup>6</sup>, C. V. L. Charlier<sup>7</sup> und H. D. Curtis<sup>8</sup> diskutiert worden ist. Diese Nebel kommen mit ziemlich großer Häufigkeit in der Sagittariusregion vor (besonders die Nebel von kleinem scheinbaren Durchmesser), zeigen aber sonst keine sehr ausgeprägte galaktische Konzentration.

Eine auffallend kleine galaktische Konzentration zeigen auch trotz hoher absoluter Leuchtkraft die R-Sterne und die helleren kurzperiodischen δ Cephei-Veränderlichen. Für ein Studium über die Verteilung dieser Sterne nach galaktischer Länge liegt aber kaum genügend homogenes Material in den verschiedenen Himmelsgegenden vor. Shapley<sup>9</sup> hat die räumliche Verteilung der letztgenannten

Lund Medd Ser II, Nr. 19 (1918).
 Lund Medd Ser, II, Nr. 28 (1922).
 Mt Wilson Comm 62 (1919).

Pop Astr Tidskr 8, S. 36 (1927); On Structural Properties of Open Galactic Clusters and their Spatial Distribution, Inaug. Diss. Lund 1931.

Lick Bull 14, S. 154 (1930).
 Lund Medd Ser II, Nr. 19, Plate IV.
 M N 71, S. 693 (1911).
 Publ Lick Obs 13, S. 60 (1918).
 Mt Wilson Contr 153 = Ap J 48, S. 279 (1918).

Sterne aus Entfernungsbestimmungen auf Grund der Relation zwischen Porlode und absoluter Größe studiert. Die kleine galaktische Konzentration wird von Shapley als eine Folge der größen Streuung der räumlichen Geschwindigkeiten gedeutet. Wenn wir das obenerwähnte Vorkommen in der "zentralen" Milchstraßengegend im Sagitturius mitrechnen, so scheint in vieler Hinsicht eine ausgeprägte Analogie zwischen der Verteilung dieser Sterne im Raume und der Verteilung der Kugelhaufen zu bestehen

Inwiewelt die hergeleitete Vertellung einer Klasse von Objekten großer absoluter Louchtkraft das wahre Vertellungsgesotz der betreffenden Objekte um Sternsystem wiedergibt, hängt natürlich in erster Linie von der Vollständigkeit ab, mit welcher diese Obiekte in unserem statistischen Material vorkommen. Eine der größten Schwierigkeiten der direkten stellarstatistischen Untersuchungsmethode liegt ohne Zwelfel in der Absorption des Lichts in ausgedehnten Anhäufungen von Materio im interstellaren Raume Eine solche Absorption beeinträchtigt nicht nur die Vollständigkeit des Materials, sondern verfälscht auch, wenn unberücksichtigt, die nach photometrischer Methode ermittelten Entfernungen und damit die aus diesen berechnete räumliche Dichtigkeit. Es wird durch beide Ursachen eine falsche "anthropozentrische" Verteilung vorgetäuscht. Mit großer Wahrscheinlichkeit sehen wir z. B einen Absorptionseffekt in dem scheinbaren Vermeiden einer zontralen Milchstraßenzone, welches die Kugelhaufen zeigen Trümpler rechnet in seiner obenerwähnten Arbeit mit einer allgemeinen Extinktion von 0m,67 (photographisch) per 1000 Parsec innerhalb einer dünnen Schicht um die galaktische Zentralebene herum. Inweweit diese und andere mehr unregelmäßige Absorptionserschelnungen auf die von TRÜMPLER gefundene Verteilung der offenen Haufen in "anthropozentrischer" Richtung cinwirken, bleibt wohl noch unnulgeklärt (vgl Ziff. 24 und 33).

21. Die Entfernung der Sonne von der Symmetrieebene der Milchstraße. In Ziff 14 haben wir für den sphärischen Radius des zentralen Milchstraßenlinie im Mittel einen gewissen Überschuß über 90° gefunden, was als "dip" der Milchstraße bezeichnet wird Eine genauere Abschätzung der entsprechenden Entfernung der Sonne von der Symmetricebene gegen den nördlichen galaktischen Pol hin kann durch eine Statistik gewisser Klassen von Objekten ermittelt werden

CHABLIER findet in seiner ersten Arbeit über die helleren B-Sterne eine Stellung der Sonne nördlich von der Symmetrieebene um 20 Parsec (4 Skriometer) und in seiner späteren Arbeit für die B-Sterne heller als 8<sup>m</sup>,0 eine Entfernung von 15,5 Parsec, was sehr nahe mit einer Schätzung von SHAPLEY und CANNON¹ für die Sterne vom Typus B0 bis B5 im Größenintervall 7<sup>m</sup>,26 bis 8<sup>m</sup>,25 übereinstimmt.

Gerasikovič findet für B-Sterne heller als 6<sup>m</sup>,7 eine Distanz von 16 Parsec und für Sterne schwächer als 6<sup>m</sup>,7 den Wert 34 Parsec. Derselbe Verfasser<sup>a</sup> hat aus den O-Sternen eine Sonnenerhöhung über die Milchstraßenebane von 31 Parsec hergeleitet

SCHILT findet in seiner in Ziff. 20 besprochenen Arbeit für die e-Sterne mit der scheinbaren Größe ziemlich varlierende Werte, die jedoch im Mittel gut mit den Resultaten für andere Klassen übereinstimmen.

Aus den & Cephel-Stornen fand Hertzsprung 40 Parsec und Shapley 60 Parsec, während kürzlich Gheastmovic und Luyten aus verbessertem Material 34 ± 11 Parsec gafunden haben, was mit den Resultaten für Miss

Harv Circ 239 (1922)
 A N 226, S. 327 (1926).
 A N 196, S. 207 (1913).
 Mt Wilson Contr. 157 — Ap J 49, S 311 (1919)

Wash Nat Ac Proc 13, S. 387 (1927).

Maurys c- und ac-Sterne und für die Spektralklassen O und B in bester Übereinstimmung steht. Das letztgenannte Resultat ist daher ohne Zweifel das zur Zeit zuverlässigste. Nach Trumpler1 liegt die Sonne 10 Parsec nördlich von der

Zentralebene der offenen Sternhaufen.

22. Spezielle Untersuchungen der Sternleeren und Sternwolken der Milchstraße. Der unmittelbare Anblick zeigt uns die Milchstraße in eine Art von Wolkenstruktur aufgelöst, die zweifellos zum großen Teil eine scheinbare, durch Absorption des Lichts in dunklen Massen hervorgerufene Zerstückelung bedeutet (vgl. Ziff. 13). Wenn wir sogar die Vermutung hegen können, daß die meisten auffälligen Risse des Milchstraßengebildes Absorptionsgebiete darstellen, so bedarf diese Behauptung doch eines direkten Nachweises, den uns in erster Linie eine statistische Analyse der Sternzahlen sukzessiver Größenklassen, soweit möglich unter Hinzufügung spektralanalytischer Daten, zu geben hat. Die Anzahl Sterne verschiedener Helligkeiten in den Dunkelgebieten wird mit den Sternzahlen benachbarter "normaler" Gebiete verglichen. Es wird dann untersucht, ob die Abweichungen durch die Einwirkung einer Absorptionsschicht in einer gewissen anzugebenden Entfernung und mit einem gewissen Absorptionsvermögen erklärt werden können.

Es ist von vornherein klar, daß eine vollständigere Analyse, die auch die Sternbewegungen berücksichtigt, für eine Beurteilung diesbezüglicher Fragen von großer Bedeutung sein würde, da ja aus den Eigenbewegungen der Sterne des Dunkelgebiets die mittleren Entfernungen hergeleitet werden können. Unsere Kenntnis der Bewegungen ist jedoch noch viel zu mangelhaft, um im allgemeinen.

eine solche Analyse erfolgreich zu machen.

Schon aus einer direkten Analyse der Kurven, welche die Sternzählungen. nach scheinbarer Größe wiedergeben, können wichtige Eigenschaften des Nebels, wie Entfernung und Absorptionsgrad, wenigstens grob geschätzt werden. Für genügend schwache Größen sollten die Kurven für das freie und das verdunkelto Feld einander parallel laufen, mit einer Differenz in m gleich der Absorption & der verdunkelnden Nebelschicht für hinter dieser Schicht liegende Sterne.

Eine mathematisch-statistische Methode zur Abschätzung der Entfernung und der Absorption ist von A. PANNEKOEK<sup>8</sup> entwickelt worden. Für die Sternzahlen pro Größenklasse im freien und im verdunkelten Gebiet, a(m) und  $a_1(m)$ , setzen wir  $a_1(m) = \gamma_1 a(m) + \gamma_2 a(m - \varepsilon)$ . Wenn wir für die Dichtigkeitsfunktion die Seeligersche oder die Schwarzschildsche Approximation annehmen, so werden γ<sub>1</sub> und γ<sub>2</sub> durch die Konstanten dieser Funktionen und durch die Entfernung r der Nebelschicht bestimmt. Durch Variation der zwei Parameter & und r wird die bestmögliche Darstellung der beobachteten Zahlen  $a_1(m)$  angestrebt. W. GYLLENBERG3 hat eine ähnliche Methode entwickelt, welche aber die Unbekannten in mehr direkter Weise ergibt. Die Entfernung des Nebels kann auf drei Wegen ermittelt werden, durch die mittlere scheinbare Größe, durch die Größe maximaler Frequenz oder durch die Totalsumme der Sterne des Vordergrundes. Lundmark hat verschiedene Methoden zur Entfernungsbestimmung für helle und dunkle Nebel skizziert.

Wie vorher auseinandergesetzt wurde, scheint in unserer Nähe eine Nebelschicht von beträchtlicher Neigung (etwa 20°) gegen die Milchstraße zu existieren, deren ausgedehnteste Absorptionsgebiete in Taurus-Orion und in Ophiuchus zu finden sind.

Das große Dunkelgebiet in Taurus zwischen R.A. 3h bis 5h 30m und nördl. Dekl. 20° bis 25° ist in einer detaillierten Abzählung auf den Franklin-Adams-

<sup>1</sup> L. c. Ziff, 20.

Amsterdam Proc 23, Nr. 5 (1920).
 Yubl A S P 34, S, 40 (1922). <sup>8</sup> Lund Medd Ser II, Nr. 52 (1929).

Platten von F W Dyson und P J MELOTTE1 behandelt worden Die Abzählung zeigt drei Regionen starker Verdunklung im genannten Gebiet, um 3h 20m. +30° herum (SW von & Persei und nahe o Persei), um 4h 30m, +26° herum (zwischen den Plejaden und & Tauri) und um 5h 20m, +25° herum (S.W. von B Tauri) Dieses Gebiet war früher von BARNARD beinerkt worden, der auf die Existenz absorbierender Materie geschlossen hatte, was durch die Anwesenheit von hallen Nobeln um so mehr wahrscheinlich wird (Zuff 13) Es wird auf der Wolfschen Aufnahme (Abb 4) wiedergegeben Dyson und MELOTTE schließen, daß die Entfornung der dunklen Materie nicht 300 Parsec fiberschreiten kann

PANNEKOEK findet aus den Zählungen im Taurusgebiet ause Entfernung des dunklen Nebels von 140 Parsec und einen Absorptionsgrad in den dunkleren Partien von etwa zwei Größenklassen Eine Bestätigung dieses Resultats ist kürzlich von C Schalen geliefert worden, der speziell die B- und A-Storne in der betraffenden Region untersucht und diese in "Lummositätsklassen" von wahrscheinlich sehr geringer Streuung in absoluter Größe aufgeteilt hat. Die Methode von Pannekork wurde für jede einzelne Klasse befolgt Schaltn findet als Mittel aus vier Luminositätsklassen, die mitemander wohl übereinstimmende Resultate geben,

$$r = 126$$
 Parsec,  $s = 1^m, 8$ 

Aus den Zahlen der A- und K-Sterne des Draper-Katalogs hatte Shapley als Maximalwort der Distanz 250 Parsec angegeben. Wenn die gefundene Absorption durch RAYLEIGH-Diffusion in Wasserstoff erklärt wurden soll, wird die Masse des Taurusnebels nach Panneroek von der Größenordnung 4 · 10 Sonnenmassen Eine solche Masse in einer Entfernung von nur 126 Parsec führt indessen auf bedenkliche dynamische Konsequenzen der Sternströmung gegenüber, weshalb es nach Pannerork wahrscheinlicher ist, daß wir es mit einer Diffusion durch freie Elektronen oder mit einer Absorption durch kosmischen Staub zu tun haben. in wolchem Falle sehr viel kleinere Massen zur Erklärung gentigen. Dann haben wir auch keine mit der Wellenlänge sich verändernde Absorption zu erwarten, was mit der bisherigen Erfahrung über die Absorption in den ausgedehnten dunklen Nebeln übereinzustimmen scheint. Dagegen ist für Sterne, die mit heller Nebulosität verbunden sind, oftmals ein großer Farbenexzeß beobachtet worden.

A. EDDINGTON weist nach, daß die Annahme einer Diffusion durch freie Elektronen für den Taurusnebel eine wahrscheinlich noch zu hohe Masse gibt (12 · 107 Sonnenmassen). Es scheint daher, daß nur die Hypothese einer "soliden Obstruktion" durch kleine Partikaln stichhaltig ist.

Die Extinktion einer solchen Wolke ist bei gegebener Masse und Dichte ein Maximum, wonn der Durchmesser einer Partikel gleich der Weilenlange des Lichtes wird. Für diese Partikelgröße geht auch der Übergang von nichtselcktiver zu selektiver Extinktion vor sich Nach H. N. Russell, ist es also wahrscheinlich, daß die Extinktion des Lichts im Raume hauptsächlich von feston Partikeln von einigen zehntausendsteln Millimeter ausgeübt wird

Für die Umgebung des Orionnebels hat A Koppre eine umfangreiche Sternzählung auf einer Aufnahme mit dem 16zölligen Bruce-Teleakop der Sternwarte

M N 80, S. 3 (1919)
 Ap J 25, S. 218 (1907).
 K Syenska Votonsk Handi (III) 6, Nr 6 (1928) — Upsala Modd 37

Harv Circ 240 (1922).
F. H. Seares u. E. Hunhle, Mt Wilson Contr 187 - Ap J 52, S. 8 (1920).

The Internal Constitution of the Stars, S. 388 (1926) Wash Nat Ac Proc 8, 8, 115 (1922) - Mt Wilson Comm 77 Publ Astrophys Obs Konignstuhl-Heidelberg 1, S. 177 (1902).

Königstuhl, Belichtungsdauer  $6^h$   $45^m$ , durchgeführt. Die scheinbare Sterndichtigkeit ist in einer bildlichen Darstellung durch Schraffierung verschiedener Stärke wiedergegeben worden. Es zeigt sich, daß der Nebel von einer sternarmen Region umgeben ist. Diese verbreitert sich auffallend in südöstlicher Richtung, so daß der Nebel fast an der Spitze eines langgestreckten sehr dunklen Kanals gelegen ist. Ein feiner dunkler Arm geht jedoch auch in nordwestlicher Richtung vom Nebel aus; in nordöstlicher Richtung steht die leere Region mit den Nebelmassen um  $\zeta$  Orionis in Verbindung. S. Asklöf hat eine Abzählung derselben Gegend für sukzessive Größenklassen bis zur Größe 13,0 unternommen. Für die Entfernung des dunklen Nebels erhält er im Mittel 290 Parsec, was mit den Entfernungsbestimmungen für die Heliumsterne im Orion und für Doppelsterne dieser Gegend, die wahrscheinlich mit den Heliumsternen und dem hellen Nebel verbunden sind, wohl übereinstimmt.

PANNEKOEK<sup>2</sup> hat für eine Partie der Milchstraße in Aquila Sternzählungen ausgeführt, aus welchen er schließt, daß das hier auftretende Dunkelgebiet durch

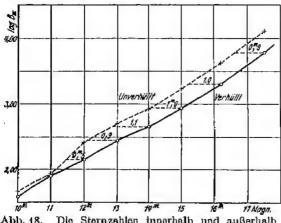


Abb. 18. Die Sternzahlen innerhalb und außerhalb des Nebels NGC 6960 nach Wolf.

eine absorbierende Nebelmasse verursacht wird, die schon für Sterne der Größen 10 und 11 sehr bemerkbar wird,

Für den großen dunklen Ophiuchusnebel gibt PanneKOEK in seiner vorher erwähnten Arbeit über das "lokale Sternsystem" eine Entfernung zwischen 100 und 200 Parsec, also von derselben Größenordnung wie die Entfernung des Taurusnebels. Shapley<sup>3</sup> schätzt für die dunklen Nebel der Ophiuchus-Scorpius-Region die Entfernung zu 200 bis 300 Parsec.

Eine Menge Sternzählungen für Absorptionsgebiete sind in den letzten Jahren von M. Wolf gemacht worden. Die erste unten aufgeführte Arbeit bezieht sich auf den Nebel NGC 6960, der sich in langem Bande fast genau durch den Stern 52 Cygni (R.A. 20<sup>h</sup> 41<sup>m</sup>, Dekl. +30° 21') hindurchzieht. Der helle Nebel ist offenbar der westliche Teil einer sehr ausgedehnten Nebelmasse, die bis zu dem ebenfalls langgestreckten Netzwerknebel NGC 6992 hinüberreicht. Wir haben schon vorher (Ziff. 1 u. 13) den großen Unterschied in den Sternzahlen auf beiden Seiten des Nebels NGC 6960 besprochen. Diese Erscheinung hat Wolf durch Sternzählungen bis zur Größe 17,5 verfolgt. Das Resultat ist in Abb. 18 wiedergegeben.

Aus der Verschiebung der Sternzahlenkurve für die Absorptionsregion kann man die Extinktion des dunklen Nebels östlich von der hellen Randpartie zu einer Größenklasse schätzen. Die Entfernung schätzt Wolf zu rund 450 Parsec. Er findet keine Spur von einem Farbenexzeß im verdunkelten Teil,

Nordisk Astr Tideskr 5, Nr. 1 (1924); Ark Mat Astr Fys 22 A, Nr. 14 (1930) = Upsala Medd 51.
Versl Akad Amsterdam 27, S. 1327 (1919); Amsterdam Proc 21, Nr. 10 (1919).

<sup>\*</sup> Harv Circ 239 (1922).

\* A N 219, S. 109 (1923); 223, S. 89 (1924); 229, S. 1 (1926); Seeliger-Festschr S. 312 (1924); V J S 61, S. 263 (1926).

Ähnliche Untersuchungen von Wolf beziehen sich auf den "Amerikanebel", auf die Sternleeren bei S Monocerotis und auf die Sternleere neben der dichtesten Gegend der Scutumwolke Bei dem Amerikanebel und der Scutumlecre beträgt die Absorption 3,5 Grüßenklassen

Schr interessant ist Wolfs Vergleichung der Sternzahlen für die vier eben genannten Regionen der Milchstraße mit den Sternzahlen am gelaktischen Pol. Die letztere Gegond erscheint sternärmer als die Leeren des Milchstraßengürtels. Wichtig ist auch, daß der Gang der Sternzehlen für den galaktischen Pol von der Größe 9 bis zur Größe 16,5 wenigstens keine stärkere Absorptionswirkung durch irgendeine Dunkelwolke andeutet.

Für den Amerikanebel liegen außer Wolfs obenerwähnter Arbeit mehrere Untersuchungen vor. So hat A Koppr<sup>1</sup> eine umfangreiche Sternzählung in derselben Welse wie für den großen Orionnebel ausgeführt E. Buch-Andersen fundet aus Sternzählungen die Entfernung des Nebels gleich der mittleren Entfernung der Sterne der Größe 8,5 in der betreffenden Region. B. Okunev<sup>8</sup> untersucht die Spektra von 743 Sternen zwischen R.A 20h 4m und 24h 13m und Dekl +40° bis +47° und findet in ziemlich guter Übereinstimmung die der Entfernung des Nebels entsprechende Sterngröße zu 9.0

W. GYLLENBURG, findet für die Parallaxo dieses Nebels nach seiner oben besprochenen Methode, aber in zwei etwas verschiedenen Durchführungen  $\pi = 0'',0064$  bzw. 0'',0074. Für den Nebel um S Monocerotis findet er  $\pi = 0'',013$ . K LUNDMARK hat in seiner oben besprochenen Arbeit für diese und andere Nebel nach verschiedenen Methoden genäherte Parallaxen gegeben.

O. STRUVE hat in Verbindung mit seiner Arbeit über das interstellare Kalzum (Ziff 25) einen Dunkelnebel im Cepheus behandelt und aus Sternzählungen eine Entfernung von 350 Parsec erhalten.

A UNSÖLD hat nach Wolfs Mothodo den südlichen "Kohlensack" in Crux untersucht. Er findet eine Entfernung von ungefähr 150 Parsec und eine Extinktion von einer Größenklasse, Zu der Unsöldschen Arbeit hat E. von DER PAHLEN<sup>6</sup> cinige bestätigende theoretisch-statustische Bemerkungen hinzugefügt

In selner oben besprochenen Arbeit hat Schaum für einige dunkle Gebiete der nördlichen Milchstraße durch eine sorgfältige Analyse der Sternzahlen der B- und A-Sterne unter Eintellung derselben in spezialle Sonderklassen, die wesentlich von der Intonsität der Wasserstofflinien im Spektrum abhängen, die Entfernung und den Absorptionsgrad der Dunkelwolken bestimmt Die Ergebnisse sind nuch Schalen in Tabelle 19 aufgeführt. Die Existenz des Nebels in der Cassionslagegend ist nach ihm unsicher In einer späteren Arbeit' hat er in der Cephousrogion unter Heranziehung von Daton für andere Spektralklassen. Andoutungen von zwei Nobeln in den Entfernungen 250 und 410 Parsec und mit der Absorption 0,3 bzw. 0,6 Größenklassen gefunden.

Tabello 13

To-loc	Ka	ord.	Rationage	Extinition
Ragion	ă	ð	in Pareso	
Cygnus , , ,	20 <sup>h</sup> 25 <sup>m</sup>	+35°	800	2**
Cophous	21 50	+35° +58	370	0,9
Copheus	21 45	+57	800	1,5
Camiopola	1 50 1 30	+57 +63 +56 +36	900	1
Auriga-Taurus	4 45	+ 36	126	1,8

<sup>&</sup>lt;sup>1</sup> Ap J 38, 8. 275 (1913)

Bulletin de l'observatoire central de Russie à Poulkovo 10, S 594 (1927).

Wir haben oben vielfach die Sternleeren der Milchstraße als im großen ganzen durch absorbierende Dunkelwolken hervorgerufen angesehen. Diese Auffassung war jedoch nicht immer die geläufige. Barnard und Wolf waren beide zuerst geneigt, in den dunklen kontrastierenden Gebieten wirkliche Sternleeren zu sehen; Wolf wollte z. B. früher in den Höhlennebeln eine Art Wegfegung von Sternen durch den hellen Nebel sehen, wodurch die sternleeren Kanäle entstehen sollten. Beide wurden aber später zu entschiedenen Vertretern der Absorptionshypothese bekehrt. In den meisten Fällen ist auch sicher diese Hypothese vorzuziehen, wenn auch hervorgehoben werden muß, daß nicht alle gegen ihre Umgebungen kontrastierenden dunklen Gebiete des Himmels notwendig als durch Absorption des Lichtes entstanden zu betrachten sind, wenigstens nicht in höheren galaktischen Breiten (vgl. Ziff. 14).

Trotz dieses Ergebnisses besteht noch immer die Vorstellung, daß das System der Milchstraße räumlich in eine Menge gegeneinander isolierter Wolken aufzulösen sei. Inwieweit dieser Vorstellung etwas Reales zukommt, läßt sich zwar noch kaum völlig entscheiden, doch muß nach dem Durchbruch der Absorptionshypothese für die Deutung der Dunkelgebiete der Milchstraße die ältere Auffassung betreffs der hellen Regionen jedenfalls sehr erheblich modifiziert werden.

Die Vorstellung einer Wolkenstruktur der Milchstraße wurde aber auch zum Teil aus einer Statistik der Sternzahlen hellerer Sterne abgeleitet. W. Stratonoff¹ fand für die Argelanderschen Sterne gewisse Kondensationsregionen, von denen die wichtigsten in Cygnus, Auriga, Monoceros und Argo gelegen sind. Stratonoff hält die Sonne für ein Glied eines Haufens, dessen Mitte wir ein wenig südlich von α Cygni wahrnehmen. F. Ristenpart³ suchte die räumliche Dichtigkeit für verschiedene Regionen zu ermitteln und kam zu dem Ergebnis, daß die Sonne sich in einem Sternhaufen befindet, dessen Zentrum etwa in der galaktischen Länge 290° im Sternbilde Norma liegt. Eine zweite deutlich hervortretende Wolke ist die in Cygnus. Wie vorher erwähnt, hat auch Pannekoek kürzlich unsere nähere Umgebung in eine Serie von Wolken aufzulösen versucht, von denen die mächtigsten in Cygnus und Monoceros liegen.

Diese Ergebnisse scheinen jedoch in einem gewissen Gegensatz zu anderen vielleicht augenblicklich allgemeiner angenommenen Ansichten zu stehen, nach denen die helleren Sterne unserer Umgebung überwiegend einem großen "lokalen System" angehören, dessen Kern von dem "lokalen Haufen" der Heliumsterne gebildet wird. Dieses "lokale System" wäre aber auch als eine einheitliche Sternwolke neben anderen zu betrachten. Diese Auffassung wird vor allem durch die nach allen Seiten abnehmende Sterndichtigkeit, wie sie aus den Sternzahlen ohne Berticksichtigung einer allgemeinen Absorption ermittelt wird, gestützt. Über die Natur und Mächtigkeit dieses hypothetischen "lokalen Systems" bestehen jedoch sehr auseinandergehende Meinungen (vgl. Ziff. 18, 19, 33). Nach einer neueren Auffassung auf Grund der differentiellen Rotationseffekte (Ziff. 30) besteht wenigstens kein beständiges, in dynamischer Hinsicht gegen andere "Wolken" abgeschlossenes lokales System.

Nicht weniger gehen die Ansichten über die Entfernungen und Eigenschaften der äußeren galaktischen Wolken auseinander. Nach einer Arbeit von Pannekoek (Ziff. 16) sollte keine Verbindung zwischen den Sternen von den Größen 9 bis 14 und den wirklichen Milchstraßenwolken bestehen. Später berechnete er³ aus Sternzählungen für die Cygnuswolke und die Aquilawolke Entfernungen von 40000 bis 60000 Parsec. Für die Sternzahlen wurden die der BD, die Eichungen von Herschel und Epstein und außerdem einige Zonen der photographischen

Publ Obs Taschkent Nr. 2 u. 3 (1900, 1901).

<sup>&</sup>lt;sup>9</sup> V J S 37, S. 375 (1902). <sup>8</sup> M N 79, S. 500 (1919).

Himmelskarte benutzt Der Gradient dlog N/den zeigte ein Minimum und ein Maximum, wenn wir gegen schwache Größen fortschreiten, was PANNEKOEK als einen typischen Wolkeneffekt deutete Unter Zugrundolegung der KAPTEYNschen Luminositätskurve und mit Vernachlässigung der räumlichen Tiefe der Wolke berechnete er für verschiedene Wolkenontfornungen theoretische Starnzuhlen, wober für die Sterne des Vordergrundes die Zahlen für den galaktischen Pol angenommen wurden Eine Konstante, die von der räumlichen Sterndichtigkeit der Wolke abhängt, wurde in Übereinstimmung mit der grob geschätzten Flächenhelligkeit der Wolke angenommen Der schwache Punkt dieser Entfernungsbestimmung lag in der relativen Unzuverlässigkeit und in der Inhomogenität der Quellen für die Sternzehlen, Gegen Pannekoeks Resultate hat Easton' ornsto Einwände auf Grund einer neuen Ermittlung der Korrelation zwischen Sternzahlen und Milchstraßenhelligkeit erhoben. Er leitet auch die Prozentzahl der B- und A-Sterne her und berechnet die mittleren Eigenbewegungen für dunkle und helle Regionen, wobei sich zeigt, daß die Eigenbewegungen im Mittel etwas größer für die dunkleren als für die helleren Easton schließt aus den Resultaten auf die Zugehörigkeit eines Teils der holleren Sterne zu den Wolken Man muß jedoch hierzu die Bemerkung machen, daß Eastons Resultate wohl oher durch die kleinen Entfernungen der Dunkelwolken, welche die hellen Milchstraßenpartien trennen, als durch kleine Entfernungen der etwalgen Sternwolken erklärt werden können (vgl. Ziff. 16)

In einem späteren Aufsatz tiber das Cygnusgeblet findet PANNEROBE, daß wir hier in der Nähe von  $\gamma$  Cygni zuerst eine Anhäufung von Sternen in einer Entfernung von nur 200 bis 600 Parsec vor uns haben, ein Haufen, der aber nichts mit der wirklichen Cygnuswelke zu tun hat. Für die Entfernung der letzteren ergibt eine Revision der Annahmen in der obenerwähnten Arbeit 18000 Parsec. Easton<sup>a</sup> macht zu diesen Resultaten einige kritische Bemerkungen und verdentlicht mit neuem Material seine Resultate für die Wolke zwischen & und  $\pi$  Cygni. Er lehnt auch eine weitgehende Erklärung der Milchstraßenstruktur durch Absorption in Dunkelwolken ab

Für die Cygnuswolke liegen noch viele Untersuchungen verschiedener Autoren vor. Ö Bergstrand hat photographisch effektive Wellenlängen für Sterne bis zu einer photographischen Größe zwischen 13 und 14 in der Gegend R.A. 19<sup>h</sup> 49<sup>m</sup> bis 59<sup>m</sup>, Dekl. + 35° 10′ bis 37° 10′, bestimmt. In einer plötzlichen Erhöhung des Mittelwerts der effektiven Wellenlängen für die Größe 12 sieht er die Einwirkung der Begrenzung des lokalen Systems und schätzt die Entfernung der Grenze zu 2500 Parsec. Die eigentliche, zwischen  $\beta$  und  $\gamma$  Cygni sich erstreckende Wolke liegt wahrscheinlich in einer noch größeren Entfernung.

A Koppe will zeigen, daß die Annahme der Gültigkeit der Kappenschen Luminositätskurve für die Wolke auf einen zu hohen Wert der Flächenheiligkeit führt. Wenn man an Stelle dessen annimmt, daß die Wolkensterne hauptsächlich A- und F-Sterne sind, so wird man unter Zugrundelegung der Abzählungsergebnisse von Pannekoek auf eine Entfernung von nur 4000 bis 6000 Parsee geführt. Pannekoek selbst kommt später zu einem ähnlichen Resultat. Die gegebenen Daten sind jedoch nicht zuverlässig genug, um exakte Schlüsse auf die Luminositätsfunktion zu erlauben.

<sup>1</sup> MN 81, S. 215 (1921)

BAN 1, 9.54 (1922).
AN Jub.-Nr. (1921)

BAN 1, S. 157 (1922)
AN 216, S. 325 (1922)

BAN 2, 8, 11 (1923).

H. Shapley hat die Verteilung von 11000 Sternen in den Milchstraßenregionen studiert und bemerkt, daß die "relativ naheliegenden" Wolken in Cygnus nur die Spektralklasse A zu beeinflussen scheinen, während im vorhandenen

Material nur die B-Sterne den Reichtum der Carinagegend andeuten.

O. STRUYE hat die Korrelation zwischen den O- und B-Sternen des DRAPER-Katalogs und dessen "Extension" und der galaktischen Helligkeit studiert. Er findet eine wahrscheinliche Entfernung der Cygnuswolke von 780 Parsec. Schalen hat in seiner obenerwähnten Arbeit eine Andeutung einer Verdichtung in der Entfernung 1000 Parsec gefunden, aber sonst eine ganz kontinuierlich abnehmende Dichtigkeitskurve bis zu 4000 Parsec.

Für mehrere andere Wolkenformationen liegen astrophysikalisch-statistische Resultate vor, die dazu beitragen können, die wahre Natur der Wolkenerschei-

nungen zu enthüllen.

Shapley<sup>8</sup> hat die Farbenindizes für 310 Sterne der Scutumwolke nahe M11 bestimmt. Er findet zwischen den Größen 12 und 15 eine Abnahme des mittleren Farbenindex von +0,98 auf +0,60. Ein analoges Phänomen sollte nach einer vorläufigen Mitteilung von Seares auch für schwache Sterno anderer Milchstraßenregionen auftreten. Soweit eine genügend ausführliche Statistik möglich ist, besteht jedoch sicher im allgemeinen eine Zunahme der Farbe mit steigender Größe. Nach F. H. Seares gilt für den Farbenindex C im Mittel für den ganzen Himmel bis zur Größe 17

$$C = +0.50 + 0.029 m_v,$$
  

$$C = -0.18 + 0.071 m_p,$$

für eine Gruppierung nach visueller bzw. photographischer Größe. Gegen die Milchstraße nimmt die mittlere Farbe schon für helle Größen merklich ab. Für die galaktische Breite +5° ermittelt Seares im wesentlichen aus Kreikens Farbenbestimmungen für schwache Milchstraßensterne (Ziff. 17)

$$C = +0.38 + 0.024 m_o,$$
  

$$C = -0.10 + 0.048 m_p,$$

während Kreiken<sup>o</sup> für die Milchstraße in Cepheus

$$C = -0.587 + 0.0678 m_p$$

und in Scutum-Aquila

$$C = -1,120 + 0,1051 m_p$$

herleitet.

K. Grapp hat eine photometrische Sternfolge von 73 Sternen bis zur Größe 11,5 für eine kleine Wolke am Rande der Scutumwolke zwischen R.A. 18h 29m und 18h 36m, Dekl. -4°,1 und -5°,1 (1855) hergestellt und auch visuell die Farben geschätzt. Er findet als bemerkenswert, daß nicht weniger als 29 Sterne die Farbenstuse 3 oder tiefer zeigen, die darauf schließen läßt, daß es sich dabei um die Spektraltypen G und K handelt. Um den Stern BD -4° 4525 herum gruppiert sich ein ganzes Nest solcher gelber bzw. rotgelber Sterne.

S. BAILEYS Sternzählung in der großen Sagittariuswolke ist an anderem

Orte (Ziff, 16) besprochen worden.

E. A. Kreiken schätzt in seiner obenerwähnten Arbeit über die Farben schwacher Milchstraßensterne aus denjenigen Sternen der Scutumwolke, die wahrscheinlich dem Typus B angehören, nach Kapteyns<sup>8</sup> Methode die Entfernung dieser Wolke zu 1500 Parsec.

<sup>&</sup>lt;sup>1</sup> Harv Circ 240 (1922).

A N 231, S. 17 (1927).
S. 64 (1917). Mt Wilson Rep. 1921.

Mt Wilson Contr 133 = Ap J 46, S. 64 (1917).
 Mt Wilson Rep 1921.
 Mt Wilson Contr 287 = Ap J 61, S. 114 (1925).
 M N 87, S. 196 (1927).
 A N 218, S. 109 (1923).
 Mt Wilson Contr 82, S. 63 = Ap J 40, S. 103 (1914).

Dieselbe Entfernung fand H Petresson<sup>1</sup> für die Aquilawolke westlich von y Aquilac aus einer Bestimmung effektiver Wellenlangen von Sternen bis zur photographischen Größe 11,5 Eine etwas kleinere Entlernung wurde von C SCHALÉN<sup>a</sup> auf Grund einer Spektralklassifizierung ermittelt

Aus den nach ihrer Farbe wahrscheinlich zum Typus B gehörenden Sternen in der Umgebung von M37 bestimmten H von Zeipel und J Lindgebn<sup>3</sup> die

Entfernung der Aurigawolke zu 2300 Parsec.

F. H SEARES leitet aus den schwachen B-Sternen einiger Milchstraßengebiete (Selected Areas) in Taurus, Perseus, Scutum und Aquila vorlänfig Entfernungen zwischen 7000 und 14000 Parsec ab

P. Doigs berechnet für die Milchstruße in Aquila aus langperiodischen

Veränderlichen die Entfernung 3000 Parsec, aus Copheiden 10000 Parsec

Eine mathematisch-statistisch wohl ausgeorbeitete Methode zur Bestimmung der Entfernungen und relativen Dichtigkeiten der Sternwolken ist zuerst von K G. Malmouiste angegeben worden Für die Dichtigkeitsverteilung einer gewissen Klasso von Stornen innerhalb einer Sternwolke setzt Maluquist nach CHARLIER

$$D(r) = D_0 e^{-\frac{(r-r_0)^4}{2\sigma^4}}, \tag{30}$$

wo also die Dichtigkeit des Mittelpunktes  $D_0$ , die mittlere Entfernung  $\tau_0$  und die Dispersion q zu bestimmen sind Für die Leuchtkraftsfunktion und die Verteilung der scheinbaren Größen werden keine bestimmten Funktionsformen eingeführt. Die erstere wird nur durch den Mittelwert  $M_0$  und die Dispersion  $\sigma$ charakterisiert und die letztere durch den Mittelwert mo, die Dispersion a und die totale Sternanzahl N.

Für das "lokale System" bekommt man nach CHARLIER, wenn 7. = 0 gesetzt und mit N die Anzahl Sterne in dem raumlichen Winkel w definiert wird,

$$\begin{cases}
\log \varrho = m_0 - M_0 - 0.792, \\
N_0 = \omega \sqrt{\frac{\pi}{2}} D_0 \varrho^6.
\end{cases}$$
(31)

(Die absolute Größe M wird als die scheinbare Größe für die Elnbeit der Entfernung definiert ) MALMQUIST zeigt, daß für eine entfernte Sternwolke die Unbekannten aus den als bekannt vorausgesetzten Größen nach dem folgenden Schema berechnet worden können.

$$\Phi_{\mathbf{a}}\left(\frac{q}{r_0}\right) \approx \sqrt{\alpha^2 - \sigma^2},$$

$$5\log r_0 = m_0 - M_0 - \Phi_1\left(\frac{q}{r_0}\right),$$

$$D_0 = \frac{N}{\omega \sqrt{2\pi q} \left(g^2 + r_0^2\right)}$$
(32)

Die Funktionen Ø, und Ø, sind in Tabelle 14 in Abkürzung nach MALHQUIST wiedergegeben. Für die Grenze einer Wolke kann  $|r-r_0|=3 \varrho$  gewählt werden, de die Dichtigkeit für diese Entfernung vom Zentrum der Wolke nur 0,01  $D_0$ beträgt.

Ark Mat Astr Fys 18, Nr. 36 (1925).

<sup>1</sup> Ark Mat Astr Fys 19A, Nr 3 (1925) Ark Mat Astr Fys K Symska Vot Akad Handl 61, Nr 15, S. 106 (1921)

1 J B B A 35, S. 128 (1925)

1 J B B A 35, S. 128 (1925) Mt Wilson Rep (1921)
 I B B A 35, S. 128 (1925)
 K Svenska Vet Akad Handl (III) 4, Nr 2 — Lund Modd Ser II, 46 (1927)

Tabolle 14.

e/re	$\Phi_1(\varrho/r_{\bullet})$	$\Phi_{2}\left(\varrho/r_{0}\right)$	e/r∎	$\Phi_1(\varrho/r_0)$	$\Phi_{\bullet}\left(\varrho/r_{\bullet}\right)$
1,00	1,470	0,907	0,40	0,435	0,671
0,90	1,317	,891	,30	,264	,560
,80	1,153	,867	,20	,124	,404
.70	0,981	,836	,10	,032	,213
,60	,801	.797	,00	,000	000
.50	,618	,745			

Für die Anwendung seiner Berechnungsmethode wählt Malmquist die Sterne im Farbenindexintervall 0,00 bis 0,24, was nahe der Harvard-Spektralklasse A entspricht. Die Leuchtkraftsfunktion dieser Sterne setzt sich aus zwei Frequenzfunktionen zusammen, die ein wenig voneinander verschiedene Werte von  $M_0$  (Differenz etwa 1,6 Größenklassen) haben und von denen jede eine sehr kleine Dispersion zeigt.

Aus von Zeipels und Lindgrens Farbenbestimmungen in der Nähe von M37 findet Malmouist für die Aurigawolke, daß diese in einer Entfernung von ungefähr 1450 Parsec beginnt, ihre maximale Dichtigkeit bei 2900 Parsec aufweist und sich bis zu 4350 Parsec erstreckt. Für die maximale Dichtigkeit, pro Kubiksiriometer gerechnet, bekommt er

$$D_0 = 0.023 \pm 0.004$$
.

Aus Kreikens Farbenbestimmungen in der Scutumwolke findet er die entsprechenden Zahlen 1800, 3400 und 5000 Parsec und

$$D_0 = 0.055 \pm 0.011$$
.

Aus eigenen Farbenbestimmungen<sup>1</sup> in der Umgebung des galaktischen Pols findet er für die Ausdehnung des "lokalen Systems" in dieser Richtung 1090±130 Parsec und eine Dichtigkeit der A-Sterne unserer Umgebung von

$$D_0 = 0.024 \pm 0.009$$
.

Die Dichtigkeit der Wolken wäre also von derselben Größenordnung wie die Dichtigkeit des "lokalen Systems".

Kreiken<sup>2</sup> hat die Hess-Diagramme für die Aurigawolke und die Scutumwolke studiert. Er findet, daß die Verteilung der Sterne nach absoluter Größe und Spektraltypus dieselbe wie in der Sonnenumgebung zu sein scheint. In den absoluten Luminositätskurven der Wolken findet er ein sekundäres Maximum, das mit einem entsprechenden, von Shapley gefundenen Maximum für die Kugelhaufen zusammenfällt. Die Entfernungen der Wolken ergeben sich zu r=2200 bzw. 2400 Parsec, in ziemlich guter Übereinstimmung mit Malmouists aus demselben Material hergeleiteten Werten.

Ein sehr brauchbares Verfahren zur Ermittlung der räumlichen Dichte für Klassen von kleiner Streuung in den absoluten Größen bedient sich der Relationen MALMQUISTS [Gl. (19) bis (22), Ziff. 18], um aus der "scheinbaren Leuchtkraftsfunktion", nach Voraussetzung einer normalen Frequenzkurve und den beobachteten Sternzahlen in sehr direkter Weise die räumliche Verteilung numerisch zu berechnen, ohne jede Voraussetzung über die Dichtigkeitsfunktion. Die Voraussetzung einer normalen Fehlerkurve für die Leuchtkraftsfunktion scheint wegen der kleinen Streuung wenig bedenklich. Diese zuerst von MALMQUIST<sup>8</sup> benutzte Methode ist von Lindblad und Petersson (l. c. Ziff. 19) auf A-Sterne und Riesen der späteren Spektralklassen in einigen Gebieten hoher galaktischer Breite an-

Lund Medd Sor II, 37 (1927).

Lund Medd 106 (1925). 3 BAN 5, S. 61 (1929).

gewendet worden, und auch von Schalen in seiner eben behandelten Arbeit fiber die B- und A-Sterne in gewissen Milchstraßengebleten Für die hellsten Milchstraßenpertien in Cygnus, Cepheus, Cassiopela und Auriga findet Schalen eine langsame kontinulerliche Abnahme der Sterndichtigkeit mit der Entfernung, im allgemeinen ohne deutlichen "Wolkeneffekt" Dies ist besonders bemorkenswort, da die Korrelation zwischen Milchstraßenheiligkeit und der Zahl der Sterne pro Quadratgrad in Schalens Arbeit sehr ausgeprägt ist Daß die hier gefundene scheinbare Abnahme der Sterndichtigkeit von einer Absorption im Raume verursacht sein kann, wird in Ziff 24 näher besprochen.

Ahnliche Ergebnisse, die auf eine prinzpielle Einheitlichkoit der Milchstraßenstruktur hindeuten, sind auch von A D Maxwell¹ hergeleitet worden Er hat mit einem spaltlesen Spektrographen in Verbindung mit dem Crossley-Reflektor der Licksternwarte eine Spektralklassifikation für Sterne in sechs Selected Areas in der Milchstraße bis zu einer Grenzgröße zwischen 13,5 und 14,0 ausgeführt Dabei worden Riesen und Zwerge der späten Spektraltypen durch das Zyankriterium und durch die verschiedene allgemeine Intensitätsabinnime gegen kleine Wellenlängen (verschiedene Farbe) voneinander geirennt. Die Zentralpunkte der untersuchten Areale sind in Tabelle 15 aufgeführt.

Tabello 15

Beleated Area No.	R.A.	Dekt.	Deki. Saleoted Area R.A		Dekl,
64 40 18	19 <sup>k</sup> 58 <sup>m</sup> 20 47 21 24	+30° 0′  -45 0  +60 10	19 8	23 <sup>3</sup> 23 <sup>14</sup> 1 0	+60° 0′ +60 10 +60 20

Für die Statistik wurde auch Material aus dem Draffer-Katalog und dessen Extension herangezogen. Die verschiedenen Spektruklassen zeigen im ganzen einander ähnliche Dichtigkeitsverteilungen. Die Dichtigkeit ist zuerst konstant bis zu Entfernungen zwischen 400 und 600 Parsec und erleidet von hier aus eine langsame Abnuhme. Keine Andeutungen sekundärer Dichtigkeitsmaxima in großen Entfernungen sind vorhanden. Die Anzahl der schwachen Sterne verträgt alch gut mit Dimensionen des galaktischen Systems von der Größenordnung 40000 Parsec. Die Frequenz der Zwerge von spätem Typus in Vergleich mit den Riesen erscheint größer, als verher für unsere nähere Umgebung angenommen worden ist, weshalb auch die Luminositätskurve einen stelleren Anstieg als van Riijns Kurve für die absolut schwachen Größen zeigt.

Für die mittlere Farbe C als eine Funktion der photographischen Größe ergibt sich C = -0.16 + 0.054 m,

in ziemlich guter Übereinstimmung mit den oben gegebenen Resultaten von Seares und Kreiken.

Der Koeffizient von m stimmt auch mit dem theoretischen, von G. Shajn hergeleiteten Wert +0,05 tiberein. Shajn geht von der Dichtefunktion nach Kapteyn und van Rhijn aus und berechnet aus der Luminositätskurve aller Sterntypen zusammen (Kapteyn und van Rhijn) und aus einer angenommenen Luminositätsfunktion für die Bo- bis A5-Sterne separat des Verhältnis der Anzahl der Bo- bis A5-Sterne zu der Anzahl der F-, G-, K-, M-Sterne für sukzessive scheinbare Größen und für verschiedene gelaktische Regionen Aus diesen Daten berechnet er für C

$$C = +0.48 + 0.05 (m - 7.0)$$
, Milchstraße,  $B = 0^{\circ}$ ,  $C = +0.74 + 0.05 (m - 7.0)$ ,  $B = \pm (40^{\circ} \text{ bis } 90^{\circ})$ 

Lick Bull 13, S 68 (1927)

MN 86, S. 382 (1926).

Eine der Maxwellschen ähnliche Untersuchung hat C. J. Krieger¹ für die Scutumwolke ausgeführt. Die Arbeit umfaßt Sterne zwischen den Größen 5 und 18. Bis zu etwa der Größe 13 hat Krieger die Spektra der Sterne mit dem spaktlosen Spektrographen photographiert, und für schwächere Sterne hat er die Farbenindizes bestimmt. Es wurden in dieser Weise alle erreichbaren Sterne innerhalb gewisser kleiner Gebiete der Wolke untersucht. Wenn man die Häufig-

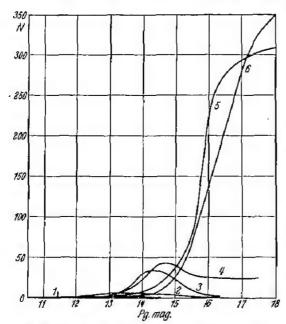


Abb. 19. Die Häufigkeit vorschiedener Farbenklassen als Funktion der photographischen Größe in der Scutumwolke nach C. J. Krieger. Die in der Figur augegebenen Nummern haben folgende Bedeutung:

Nr.	Farbenindex	Nr.	Parbonindex
2 3	-0,60 bis -0,10	4	+0,40 bls +0,65
	-0,10 ,, +0,15	5	+0,65 ,, +0,90
	+0,15 ,, +0,40	6	+0,90 ,, +1,15

keit verschiedener Farbenklassen gegen die photographische Größe in einem Diagramm darstellt (Abb. 19), sieht man unmittelbar, in welch hohem Grade die Farbe der schwächsten Sterne (Größen 15 bis 18) mit zunehmender Größe (abnehmender Leuchtkraft) wächst.

Die Dichtefunktion hat Krue-GER für verschiedene Spektralgruppen unter Berücksichtigung der Dispersion in absoluter Größe innerhalb der Gruppen gemäß der in Gleichungen (23) bis (25), Ziff. 18, skizzierten Methode bestimmt. Alle Spektralklassen geben eine ausgeprägte Tremung zwischen dem lokalen System und der Sternwolke (Abb. 20 bis 22). Für die Entfernung der Wolkenmitte von uns bekommt Krie-GER 2800 Parsec, was sich wohl mit Malmouists oben zitiertem Wert von 3400 Parsec verträgt, wie auch mit Kreikens letztein Wert von 2400 Parsec. Die Entfernung ist fast identisch mit den in ähnlicher Weise bestimmten Entfernungen der Sternhaufen M11 und M26, die am Himmel auf die Scutumwolke projiziert

erscheinen und also jetzt gemäß den Entfernungsbestimmungen als mit der Wolke verbunden angesehen werden können. Lindblad<sup>2</sup> hat für M44 die Distanz 2500 Parsec gefunden und TRÜMPLER<sup>3</sup> (ohne Berücksichtigung der interstellaren Absorption) 2200 Parsec für M44 und 2750 Parsec für M26.

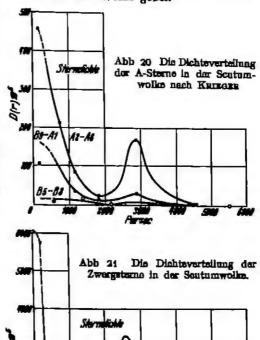
Wenn wir Vergleiche mit den Verhältnissen in der Umgebung der Sonne nach van Riijns und Maxwells Resultaten anstellen, so erscheint die Scutumwolke ungefähr gleich reich an A-, F-, G-Sternen und an K-Sternen von der Riesenklasse und entschieden reicher an G-Sternen vom Zwergtypus, während die B-Sterne in der Wolke wahrscheinlich seltener als in unserer Umgebung sind. Krieger zieht den Schluß, daß für alle Klassen zusammen die Dichte der Wolke etwa die Hälfte der Dichte unserer Umgebung sein wird. Die Berücksichtigung

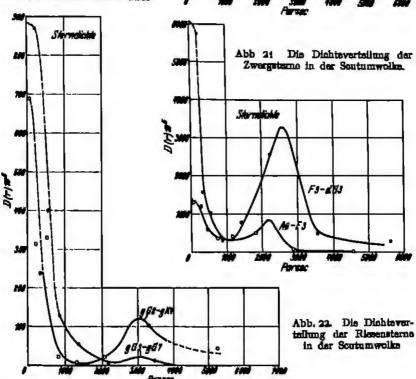
<sup>1</sup> Lick Bull 14, S. 95 (1929).

Mt Wilson Contr 228 = Ap J 55, S. 85 (Corr. S. 413) (1922).
 Lick Bull 14, S. 154 (1930).

einer oventuellen Absorption des Lichts im interstellaren Raume würde aber, gleichzeltig mit einer Reduktion der Entfernungen, eine sehr erhebliche Korrektion zu jeder Schätzung der absoluten Dichte der Wolke geben

Miss L. SLOCUM1 lint ganz kürzlich durch Farbanindaxbestimmungen für 1500 Sterne zwischen den Größen 12 und 18,5 in den Kapteynschen Feldern 8. o. 18, 19, 64 die Maxwellsche Arbeit fortgesetzt Die Dichtevertoilung im Raumo wird unter Beritcksichtigung einer allgemeinen Absorption im TRUMPLERSchen Sinne (Ziff. 24) hergeleitet Für die selektive Absorption ergibt sich aus 53 Sternen mit bekannten Spektren und Farbenindizes der mit TRUMPLER nahe über-





einstimmende Wert +0m,00034 per Parsec, und es wird angenommen, daß dies etwa 0,4 der allgemeinen Absorption entspricht. Für die Dichte  $\delta$  des absorblerenden Mediums wird ein Ausdruck  $\delta = o' e^{-r/\epsilon}$ , wo c' = 2,4,  $\varrho = 3000$ , angesetzt; die Absorption nimmt also ziemlich schnell mit wachsender Entfernung ab. Die nach diesem Prinzip ermittelte Sterndichte nimmt mit stelgender Ent-

<sup>1</sup> Link Bull 15, S 123 (1931).

fernung ab, am schnellsten in unserer Nähe, zeigt aber eine Andeutung eines sekundären Maximums für r=2000 bis 2500 Parsec, und in der Cygnusregion (Area 64) auch für r = 6000 Parsec. Das letztere Ergebnis stimmt mit den obenerwähnten Entfernungsbestimmungen von Kopff und Pannekoek für die

Cygnuswolke überein.

28. Spezielle Untersuchungen über die Natur der Magellanschen Wolken. Wie schon in Ziff. 10 erwähnt, ist die Stellung der Magellanschen Wolken eine ganz besondere. Die große Bedeutung dieser Gebilde in der gegenwärtigen Forschung können wir mit H. Shapley etwa folgendermaßen formulieren. Sie sind uns nahe genug gelegen, um vollständig in Millionen von Sternen aufgelöst zu werden, und doch entfernt genug, um ganz von außen her gesehen und untersucht zu werden. Sie dienen als Schlüssel zur Kenntnis entfernter Milchstraßen und eröffnen hierdurch den Weg aus lokalen Regionen in ein äußeres Universum hinaus. Die Spezialforschungen auf diesem Gebiete werden in anderen Teilen dieses Handbuchs ausführlich behandelt, und wir können hier nur in einer kurzen Übersicht die wichtigeren Punkte erwähnen.

Der große Reichtum der zwei Wolken an Nebeln und Sternhaufen wurde schon von J. Herschel entdeckt, aber eine eigentliche astrophysikalische Untersuchung beginnt erst mit dem Anfang unseres Jahrhunderts durch die photographisch-photometrische Arbeit der Harvard-Sternwarte mit einem zu Arequipa aufgenommenen Plattenmaterial. Die ersten Früchte dieser Arbeit waren Miss H. Leavitts<sup>2</sup> Kataloge über die in den Wolken beobachteten veränderlichen Sterne, 808 in der großen, 969 in der kleinen Wolke. Die von Miss Leavitt für 25 & Cephei-Veränderliche in der kleinen Wolke gefundene Relation zwischen Periode und Helligkeit wurde zuerst von E. HERTZSPRUNG<sup>8</sup> zu einer Entfernungsbestimmung dieser Wolke benutzt. Shapleys Festlegung der Relation zwischen Periode und absoluter Größe für die & Cephei-Sterne hat dann aber eine neue Bestimmung der Entfernungen der zwei Wolken herbeigeführt. Nach seiner letzten Revision der "Period-Luminosity Curve" findet er aus 107 & Cephei-Veränderlichen in der kleineren Wolke und 50 in der großen folgende Werte4:

> Kleine Wolke  $\pi = 0'',0000345$ Entfernung = 29 Kiloparsee = 95000 Lichtjahre Durchmesser = 6000 Lichtiahre

Große Wolke  $\pi = 0'',000038$ Entferning = 26,2 Kiloparsec = 86000 Lichtiahre Durchmesser = 10800 Lichtjahre

Die zur Zeit bekannten zehn Kugelhaufen in den Wolken haben scheinbare Durchmesser von 1 bis 2 Bogenminuten. Eine hierauf begründete Entfernungsbestimmung liefert mit den oben gegebenen sehr nahe identische Werte.

K. Lundmarks hat für die große Wolke zur Entfernungsbestimmung außer den Kugelhaufen auch die Wolf-Rayet-Sterne und die offenen Haufen benutzt und findet im Mittel den Wert  $\pi = 0^{\prime\prime},000036$ , der offenbar sehr gut mit dem

oben gegebenen übereinstimmt.

Die Magellanschen Wolken geben uns eine wichtige Gelegenheit, den Verlauf der Leuchtkraftsfunktion im Gebiet der allerhellsten Sterne zu untersuchen, und sie geben uns auch Aufschluß über die absoluten Größen verschiedener Objekte von sehr großer Leuchtkraft, wie Nebel, Haufen und Sterne von gewissen abnormen Typen. Besonders die Untersuchungen von Shapley und seinen Mitarbeitern sind hier erfolgreich gewesen. Zu erwähnen ist, daß einzelne

Star Clusters, Harvard Monograph No. 2, S. 183 (1930).
 Harv Ann 60, S. 87 (1908).
 A N 196, S. 201 (1913). 4 L. c. S. 189.

<sup>&</sup>lt;sup>5</sup> Obs 47, S. 276 (1924); Pop Astr Tidskr 5, S. 146 (1924). Harv Circ 255, 260, 268, 271, 275, 276, 280, 288 (1924-1925).

Sterne die überaus hellen absoluten Größen —5 und —6 erreichen Einige rote Veränderliche der Spektralklassen K bis Mc und fünf Sterne vom P Cygni-Typus gehören zu den hellsten Sternen der großen Wolke<sup>1</sup>. Die Nebel sind im allgemeinen von einem diffusen, irregulären Typus, unter ihnen ist der Riesennebel 30 Doradus, mit einer absoluten Größe wahrscheinlich heller als —13 und einem Durchmesser von etwa 30 Parsec, besonders auffallend LUNDMARK bemerkt, daß dieser Nobel eine Anzahl von dunklen Mecken in der Nobelfläche zeigt, in genau derselban Wolse, wie wir sie in vielen von den hellen Milchstraßennebeln schen. Überhaupt sind in der großen Wolke dunkle Risse von verwickelter Natur vorhanden, die sehr an Erscheinungen in der Milchstraßenstruktur erhnern.

Die Spektra der Gasnebel\* geben für die große Wolke eine Radialgeschwindigkert von +276 km/sec und für die kleine +168 km/sec. Hertzsprungs hat die Hypothese aufgestellt, daß gewisse Differenzen in den Radialgeschwindigkeiten für die 17 beobachteten Nebel der großen Wolke sich im wesentlichen als eine Folge einer parallelen und gleich großen Bewegung dieser Nebel im Raume erklären. Es zeigt sich dabei, daß die Radialgeschwindigkeit der kleinen Wolke sich in diese Reihe einordnen läßt, so daß die zwei Wolken in der Tat eine gemeinsame Bewegung haben konnen. Als Konvergenzpunkt ergibt sich  $\alpha = 4^h 94^m$ ,  $\delta = -5^{\circ},5$  and für die Geschwindigkeit relativ zur Sonne 625 km/sec

Die Rotationstheorie der Milchstruße läßt uns aber das Problem der Bewegung der Wolkon aus einem anderen Gesichtspankt betrachten J H Ookr bemerkt, daß mit einer Geschwindigkeit der Sonne von 286 km/sec gegen einen Punkt  $L = 55^{\circ}$ ,  $B = 0^{\circ}$  (vgl, Ziff. 30) die Residuen der Radialgeschwindigkeiten die Werte +41 km/sec und -9 km/sec annehmen Es ist also recht wahrscheinlich, daß die Wolken nur kleine Geschwindigkeit relativ zum Schwerpunkt des Systems besitzen.

W J. LUYTENS hat, wesentlich auf dem Boden der Hertzsprungschen Hypothese, die möglichen Bahnformen der Wolken relativ zum Zentrum der Milchstraße unter verschiedenen Annahmen über die Masse des Milchstraßensystems diskutiont. Das Resultat ist ansorst unsicher, zelgt aber, daß auch mit einer verhältnismäßig hohen totalen Geschwindigkeit der Wolken relativ zum

erwähnten Zentrum elliptische Bahnen nicht ausgeschlossen sind.

Gegen die Annahme einer direkten Zusammengehörigkeit der zwei MAGELLANschen Wolken mit den Milchstraßenwolken hat eine andere Auffassung behauptet, daß sie oher zu den extragalaktischen Nobeln gerechnet worden sollten, also Objekte sind, die zufälligerweise in die Nähe des Milchstraßensystems gekommen sind. Die letztere Meinung ist woll zuerst von Clevriand Abbe klar ausgesprochen worden. Später hat LUNDMARK' die Ähnlichkeit der großen Wolke mit dem Nebel NGC 4449 nachgewiesen und dann auch die tiberaus wichtige Beobachtung gemacht, daß die Wolken sogar als Typen für eine gewisse Klasse von Nebeln dienen können. Zu den auffallenderen Objekten von dieser Klasse gehört der Nobel NGC 6822, der eingehend von E. Hubble untersucht worden ist. In der neuesten Zeit steht man zwar ganz auf dem Boden der letzteren Auffassung, ist aber geneigt anzunehmen, daß die Wolken doch etwa als "ferne Begleiter" dem Milchstraßensystem angehören (vgl Ziff. 34).

Zuictzt sei hier erwähnt, daß D. WATTENBERG eine eingehende Besprechung der neueren Resultate über die Natur der Magellanschen Wolken gegeben hat.

Lick Obe Publ 13, S. 168 n. 187 (1918).

Miss Cannow, Harv Bull 754 ti 801 (1921, 1924).

M N 80, S 782 (1920); Nordisk Astr Tidaskr 1, S. 133 (1920)
B A N 4, S. 79 (1927). Wash Nat Ac Proc 14, S. 241 (1 Wesh Nat Ac Proc 14, S. 241 (1928) - Harv Rope 44.

MN 27, 6. 262 (1867) K Svenska Vot Akad Handl 60, Nr 8 (1920) Mt Wilson Contr 304 - Ap J 62, 8, 409 (1925)

Naturwise 18, S. 696 (1930); A N 237, S. 401 (1930).

24. Die Absorption des Lichts im interstellaren Raume. Wir haben schon oben in Ziff 18 und 20 die große Bedeutung der Frage, ob eine allgemeine Absorption im interstellaren Raume existiert, für die Erforschung der raumlichen Dichteverteilung im Milchstraßensystem hei vorgehoben Selliger und Kapilyn hatten beide einen Höchstbetrag dei Absorption beiechnet unter der plausiblen Annahme, daß die wahre raumliche Dichte für große Entfernungen nicht erheblich anwachsen kann Kapteyn<sup>1</sup> hat z B aus dieser Erwägung einen Höchstbetrag von ein paar tausendstel einer Großenklasse pro Parsec angegeben, walnend SEELIGER nach dem in Ziff 18 eiwähnten Prinzip, welches eine bestimmte Funktionsform fur die "scheinbare" Dichteverteilung einschließt, nur einen noch erheblich kleineren Absorptionskoeffizient zugeben wollte. Da eine Absorption der genannten Art sehr wahrscheinlich mit dei Wellenlange veranderlich sein wind, wunde das Interesse zumächst auf die Frage nach der Existenz einer selektiven Absorption gefuhrt Man hat so wiederholt versucht, eine direkte Abhangigkeit der Fai be der Steine von ihrer Entfernung festzustellen. Anscheinend positive Resultate in dieser Hinsicht wurden von Kaptlyn, Jones, King, van Rillin u.a. hergeleitet Diese Versuche gelangten aber zu einem gewissen Abschluß daduich, daß das Problem durch eine deutliche Abhängigkeit der Farbe von der absoluten Giöße innei halb gewisser Spektialtypen kompliziert wurde, und vor allem dadurch. daß die Evidenz aus den Faibenbestimmungen in den Kugelhaufen und für extragalaktische Nebel entschieden gegen die Existenz einer allgemeinen selektiven Absorption sprach Eine Untersuchung von K LUNDMARK<sup>3</sup> über die Variation der Flächenhelligkeit der extragalaktischen Nebel mit der Entfernung und von II Shapley und A Ames4 über den Zusammenhang zwischen Durchmesser, photometrischer Größe und Entfernung für Nebel im Coma-Virgo-Gebiet setzten eine ungeheuer enge obeie Gienze auch für eine nichtselektive allgemeine Absorption In derselben Richtung geht auch van Rhijns<sup>5</sup> Resultat aus einem Studium des Zusammenhanges zwischen Durchmessei und photometrisch bestimmter Entferning für die Kugelhaufen wie auch Shapleys in Ziff 20 ei wähnte Folgerung betreffs der Umgebung des zentralen Verdunklungsgebietes in Sagittarus-Ophruchus

Die Idee, daß die "anthropozentrische" Anordnung der Steine, welche die nach allen Seiten abnehmende Steindichte unserer Umgebung anzeigt, nur scheinbar sei und den Effekt einer Absorption darstelle, eine Idee, die wohl am konsequentesten von J. IIalm durchgeführt worden ist, ist jedoch niemals ganz aufgegeben worden Ganz kürzlich hat C Schalen  $^{\dagger}$  die Frage auf Grund seiner oben (Ziff 22) besprochenen Arbeit über B- und A-Steine in ausgewählten galaktischen Regionen aufgenommen Für die Spezialgruppen höchster Luminosität ( $\tau$  und  $\tau$ — genannt) hat er untersucht, welcher Absorptionskoeffizient  $\nu$  für konstante räumliche Dichte in der Milchstraßenebene vorauszusetzen wäre Wenn wir die Absorption in Größenklassen per Parsec rechnen und diesen Koeffizienten mit  $\alpha$  bezeichnen, so hat man  $\alpha=2,5\log e\cdot \nu=1,09\nu$  Für die als normal betrachteten Regionen in Cepheus und Cassiopera findet Schalen

 $\alpha = 0,0005 \text{ mag/Parsec}$ 

Für die Autigaregion mag dei größei gefundene Weit vielleicht auf eine wirkliche Abnahme der Dichte in der Richtung vom Zentrum des Milchstraßensystems (in

<sup>&</sup>lt;sup>1</sup> A J 24, S 115 (1904)

<sup>&</sup>lt;sup>2</sup> Für die historische Entwicklung des Problems siehe besonders II Kienle, Die Absorption des Lichtes im interstellaren Raume Jahrbuch der Radioaktivität und Elektronik 20, II 1 (1922)

<sup>&</sup>lt;sup>8</sup> M N 85, S 865 (1925) 
<sup>4</sup> Harv Bull 864 (1929) 
<sup>5</sup> B A N 4, S 123 (1928) 
<sup>6</sup> M N 77, S 243 (1917), 80, S 162 (1919). 
<sup>7</sup> A N 236, S 249 (1929)

der gelaktischen Länge 330°) zurückgeführt werden Auch in Cygnus findet ei einen größeren Wert Wenn die letztgenannten zwei Regionen mitgerechnet werden, kann man nach Schalan als obere Grenze  $\alpha < 0.0020$  mag/Parsec setzen.

SCHALRINS Resultat wurde dann in sehr bemerkonswerter Weise durch R TRUMPLERS Untersuchung über die offenen Sternhaufen (Ziff. 20) bestätigt und erganzt. Wenn wir die photometrisch ohne Berücksichtigung der Absorption bestimmte Entfernung eines Haufens mit r', die wahre Entfernung mit r bezeichnen, so haben wir

$$m - M = 5 \log r' - 5$$
$$= 5 \log r + \alpha r - 5$$

Wenn welter d der scheinbare Durchmesser in Begenminuten, D' und D die mit 7' baw 7 gerechneten linearen Durchmesser in Parsec sind, haben wir

$$\log D' = -3.536 + \log d + \log r'$$

$$\log D = -3.536 + \log d + \log r$$

$$\log D' - \log D = \frac{\alpha}{5} r,$$

Wir bekommen also

und im Mittel

$$\overline{\log D'} - \overline{\log D} = \frac{\alpha}{5} \overline{r}$$

Wenn wir jetzt eine Unterabteilung von Haufen mit kleiner Streuung in log D betrachten, so können wir  $\log D = \log D$  setzen und für die direkt aus den scheinbaren Durchmessern gebildeten Differenzen

$$v' = \log D' - \widetilde{\log} \overline{D}'$$

bekommen wir dann direkt

$$v'=\frac{\alpha}{5}\left(r-\tilde{r}\right),$$

oder

$$v' = a + br$$

WU

$$a = \frac{\alpha}{5}\bar{r}, \quad b = \frac{\alpha}{5}$$

r wird in sukzessiven Annäherungen aus der Relation

$$\log r + br = \log r'$$

ermittelt Trümpler hat für verschiedene galaktische Längen die Werte von a. für 1000 Parsec gerechnet, zusammengestellt (Tab 16)

Ea bestoht offenbar eine sehr gute Übereinstimmung zwischen Schalens und TRUMPLERS Resultaten TRUMPLER macht jetzt die Annahme, daß diese Absorption nur in einer verhältnismäßig dünnen Schicht um die Zentralebono der Milchstraße herum besteht Vielleicht ist diese Schicht nur etwa 200 bis 300 Parsec dick, in der Milch-

Tabelle 16.					
Galaktische Länge	σ	w, F			
330°- 45° 45 -110 110 -195 195 -330	0°,79 ,59 ,87 (,37)	士0 <sup>3</sup> ,09 士 ,08 士 ,17 士 ,16			
Alle	.67	士 ,07			

atraßenebene selbat aber wahrscheinlich schi weltgestreckt und geht vielleicht als eine Trannungsfläche durch das ganze System hindurch

<sup>1</sup> Llok Bull 14, S 154 (1930).

Auch die von Shapiev, Herrzsprung, Searls und Wallenguist konstatierten Farbenenzesse in gewissen offenen Haufen werden von Trümpler als Absorptionseffekte gedeutet. Wenn wir für den Enzeß E im Farbenindex

$$E = \iota r$$

ansetzen, bekommt Trumpler fur den Koeffizienten

$$c = +0^{\text{m}},32 \pm 0,^{\text{m}}03 \text{ (per 1000 Parsec)}$$

Da auch dieser Effekt nach Trümplers Annahme an die dunne absorbierende Zentralschicht gebunden ist, erklart sich ungezwungen, warum kein Farbeneffekt für Kugelhaufen und extragalaktische Nebel konstatiert worden ist

Der Farbeneffekt für den Hausen NGC 663 und sun Steine, die auf diesen Hausen projiziert eischeinen, ist nach Beobachtungen von Å Wallenguist und C Schalen von letzterem¹ diskutieit worden. Ei sindet sur den Koessienten c den Weit 0<sup>m</sup>,26±0<sup>m</sup>,03. Die Faibenessekte für entseinte Milchstraßensterne von siuhem Typus haben P van de Kamp² und Y Öhman³ behandelt. Der erstere sindet ein Resultat in enger Übereinstimmung mit Trumpific und leitet als besten Weit ab

$$c = +0^{\text{m}},331 \pm 0^{\text{m}},022 \text{ (per 1000 Parsec)}$$

Ei sucht auch einen Einfluß der galaktischen Bieite auf die Absorption zu finden, um daraus die Dieke der absorbierenden Schicht zu bestimmen. Er findet im Mittel aus dem Absorptionseffekt für verschiedene Klassen von entfernten Objekten (Haufen, B-Sterne, Nebel) eine Dieke dieser Schicht von 175 ± 50 Parsec Dieser Wert muß aber noch als sehr unsicher betrachtet werden

Ohman deutet den oft ausgeplägten Farbenevzeß fur schwache B-Steine als einen Entierungsefiekt und findet aus seinem Material den Koeffizienten 0,19 mag per 1000 Parsec fur ein Farbenaquivalent, welches aus dem Intensitätsverhaltnis fur die Wellenlangen  $\lambda$  3912 A und  $\lambda$  4415 A im Spektrum gebildet ist. Dieses Resultat läßt sich gut mit Trümplers und van de Kamps Farbenkoeffizienten vereinen, welcher fur die Wellenlangen  $\lambda$  4300 A und  $\lambda$  5600 A gilt. Ein mit den obigen Eigebnissen sehr nahe übereinstimmendes Resultat  $c = +0^{\rm m}$ ,34  $\pm$  0 $^{\rm m}$ ,03 hat kürzlich Miss L. Slocum<sup>4</sup> (vgl. Ziff. 22) ermittelt

K F Bottlinger und H Schneller<sup>5</sup> haben endlich auf einen anderen Effekt der absoidierenden Schicht hingewiesen. Es wird die Absorption in einer derartigen Zentralschicht zur Folge haben, daß eine Klasse von Objekten, die eine einebliche Konzentration gegen die Milchstraßenebene zeigen, für größere Entfernungen scheinbar eine zu kleine Konzentration aufweisen wird. Denn berechnet man die Entfernungen ohne Berucksichtigung der Absorption, so daß diese für schwache Sterne zu groß ausfallen, so wird der Abstand von der Mittelebene  $Z=R\sin b$  entsprechend zu groß. Je weiter also die Sterne entfernt sind, desto größer wird ihr mittlerer Abstand von der galaktischen Ebene sich eirechnen. In der Tabelle 17 sind die mittleren Z-Koordinaten, eistens ohne Berücksichtigung der Absorption, zweitens (Z') mit der Trömplerschen Absorption  $\alpha=0^{m},67$  und zuletzt (Z'') mit einer Absorption  $\alpha=2^{m}$  pro 1000 Parsec gerechnet. Für diesen größeren Wert der Absorption finden Bottlinger und Schneller einige Stütze in Schalens Resultaten für die Cygnus- und Aufgaregionen

Ark Mat Astr Fys 22A, Ni 15 (1930) = Upsala Medd 49

<sup>&</sup>lt;sup>a</sup> A J 40, S 145 (1930)

Spectrophotometric Studies of B-, A- and F-Type Stars N Acta Reg Soc Sc Upsahensis
 (IV) 7, Nr 3 (1930) = Upsala Medd 48
 Lick Bull 15, S 123 (1931)

<sup>&</sup>lt;sup>5</sup> Z f Astrophys 1, S 339 (1930)

Tabelle 17

Batterrungsbereich in Kilopanies	Amenial der Sterne	Ē	E	R	[2"]	Pr	E"
0 1	38	597	71	491	59	394	48
1-2	33	1 524	111	1066	77	747	54
2- 3	26	2442	139	1482	85	991	55
3- 4	26	3 508	148	1862	79	1174	48
4- 6	22	4908	144	2282	66	1386	37
6-12	10	8 486	438	2975	163	1723	94
12-25	16	16385	448	4062	108	2162	57

Die stellarastronomische Bedeutung der Absorption liegt vor allem darin, daß die empirische Grundlage, auf welche die um die Sonne rotationssymmetrische Anordnung des "typischen" Sternsystems und später des "lokalen" Systems gegrundet wurde, sich aufzulösen beginnt. Es wird hier mehr und mehr offenbar, daß die Verteilung der Materie in der Milchstraßenebene bis zu sehr großen Entfernungen von uns als wesentlich gleichförmig anzusehen ist, und daß wir berechtigt sind, jeder ausgeprägt "anthropozentrischen" Anordnung der Materie im System mit Mißtranen zu begegnen

Die physikalische Erklärung der Absorption steht noch im wesentlichen offen 25. Die Kalziumwolken in der Milchstraße. Ein Phänomen, das violleicht mit der oben behandelten Extinktion in einer mittleren Milchstraßenschicht in Beziehung steht, haben wir in dem im Jahre 1904 von HARTMANN¹ entdeckten Absorptionseffekt der sog. "ruhenden" Kalzinmlinlen. J. HARTMANN fand, daß im Spektrum des spektroskopischen Doppelstorns & Orionis die K-Linie die periodische Verschiebung der Linien nicht zeigte und schloß daraus, daß irgendwo auf der Verbindungslinie zwischen uns und dem Stern eine Wolke existiert, die eine Absorption in der erwähnten Linie hervorruft. Er machte auch die Beobachtung, daß im Spektrum von Nova Persel die H- und K-Linion wie auch die D-Linien als scharfe Absorptionslinien, die einer kleinen konstanten Radialgeschwindigkeit (+7 km/sec) entsprechen, vorhanden waren. Scharfe Kalziumlinien and bald darant von E B FROST und W. S. ADAMS im spektroskopischen Doppelstern 9 Camelopardalis beobachtet worden und Frost machte einige Jahre später Mittellungen über scharfe Kalziumlinien in den Spektren von 25 Sternen. Die Linien sind dann oftmals in den Spektren der spektreskopischen Doppelsterne identifiziert worden. Das Auftreten der H- und K-Linien in den Novae hat auch J. EVERSUED' diskutiert. Die aus diesen Linien ermittelten Radialgeschwindigkeiten für Nova Persel, Nova Geminorum Nr 2 und Nova Aquilae wie auch für sechs spektroskopische Doppelsterne deuten an, daß die Bewegungen dieser Sterne fast gans der Sonnenbewegung entsprechen, und daß also das Kalzium sich sehr nahe in Ruho relativ zum Zentrold der uns umgebenden Sterne hofindet. R. H Curriss hat allerdings eine langsame Veränderung der Geschwindigkeit aus den H- und K-Linien für die Nova Geminorum 1912 konstatieren wollen, während für Nova Aquilae 1918 und die Nova Cygni 1920 die Linien stationär erscheinen,

Die stationaren D-Linien wurden von Miss Heger studiert. Eine Zusammenfassung des Beobachtungsmaterials und eine eingehende Diskussion des ganzen Problems wurde zuerst von R. K. Young' ausgeführt. H Ludendoepp

Sitzber K Akad Wiss Berl (1904), S 527, Ap J 19, S. 268 (1904)
 Ap J 19, S. 350 (1904)
 Ap J 29, S. 234 (1909)
 Obs 42, S 85 (1919).
 Pop Astr 33, S. 167 (1925)
 Lick Bull 10, S 59 (1919); 10, S. 141 (1921).
 Publ Astrophys Obs Victoria 1, S. 219 (1920), J Can R A S 14, S. 389 (1920)

AN 211, S. 118 (1920), 212, S 11 (1921)

hat gefunden, daß die schaifen Linien speziell für die Heliumsteine mit besonders großen Massen auftreten und betont die Schwierigkeiten der verschiedenen Eiklarungshypothesen Die Theorie, daß die K-Linie in einer zu dem betreffenden Stern gehörigen Atmosphare entsteht, erscheint nicht befriedigend, und die Annahme einer kosmischen Wolke reicht auch nicht aus, da bei einigen Systemen die K-Linie Verschiebungen in derselben Periode wie die übrigen Linien zeigt, wenn auch mit kleineiei Amplitude Einen sehr erheblichen Schritt vorwarts bedeutet dann die Untersuchung der betreffenden Linien für die O-Sterne durch J S PLASKETT1 Das Volkommen der Linien in allen Typen fluher als B3 und der wahrscheinlich interstellare Ursprung der Limen wird hier besonders betont Eine partielle Oszillation dei Linien in gewissen spektioskopischen Doppelsternen vom B-Typus kann durch eine Kombination der stationaren interstellaren Linien mit den schwachen Kalziumlinien der Steinatmospharen selbst eiklart werden, da nach R H FOWLERS und E A MILNES theoretischer Arbeit die H- und K-Linien eist bei dem Typus B0 oder früher vollkommen verschwinden Unter anderen, die sich mit dem Problem beschaftigt haben, befinden sich F HENROTEAU<sup>2</sup> und H KIENLE<sup>3</sup>, der eine eingehende Behandlung der Geschwindigkeitsdifferenzen Stein-Wolke in ihrer Abhangigkeit vom Spektialtypus gegeben hat Auflösungen fur die Sonnenbewegung haben A B IIENROTEAU' und G Strombleg gegeben J Wolijer ji 6 hat dei Ansicht Plaskerts eine weitere theoretische Begrundung gegeben

Em weiterer Fortschritt zur Deutung der stationaren Linien war insbesondere A S Epdingtons' theoretische Behandlung des Pioblems Plaskeit und Woltjer hatten den Gedanken ausgesprochen, daß die Kalziumatome vorzugsweise in der Nahe der heißeren Sterne die fur das Auttreten der Ca+-Linien notwendige Ionisation eileiden Gegen diese Ansicht hebt Eddington heiver, daß die relative Konzentiation dei Ca+-Atome in dei Nahe dei heißeren Steine als eine Folge einer zweimaligen Ionisation abnehmen muß, und er zieht den Schluß, daß die Absorption gleichmaßig langs dem Visionsiadius von sich geht. Eine außerordentlich dunne, allgemein ausgebreitete Mateire aus Kalzium und anderen Elementen kann in genugend großer Menge vorkommen, ohne in meßbarer Weise die scheinbare Leuchtkraft oder die Farbe der Steine zu andern

Die Temperatui dei interstellaren Materie in einem gewissen Punkte ist nach Eddington auf Grund der Geschwindigkeiten der durch Strahlungserregung aus den Atomen gelösten Elektronen von derselben Größenordnung wie die Temperatur, die der spektialen Energieverteilung der Strahlung in dem betieffenden Punkte entspricht Für diese Temperatur T kann abei die Temperatur der umgebenden Steine, etwa 10000°, gesetzt werden Wenn wir mit I(v, T) dvdie Strahlungsdichte bei thermodynamischem Gleichgewicht für ein Frequenzintervall zwischen  $\nu$  und  $\nu + d\nu$  und für die Temperatur T bezeichnen, so setzt Eddingson für die Dichte der Strahlung im interstellaren Raume

$$I(v,T) dv/\delta$$
,

wo  $\delta$  als "factor of dilution" auftitt. Man hat dann die Regel, daß die Ionisationsverhältnisse der interstellaren Materie von der Dichte o dieselben sind wie in Materie von der Dichte  $\varrho \delta$  in thermodynamischem Gleichgewicht bei dei Tem-

Cambridge 1926

Publ Astrophys Obs Victoria 2, S 335 (1924), M N 84, S 80 (1924)

J Can R A S 15, S 62 (1921)
 SEELIGER-Festschr, S 38 (1924), M N 84, S 583 (1924) 4 J Can R A S 14, S 234 (1920)

<sup>&</sup>lt;sup>5</sup> Mt Wilson Conti 243 = Ap J 61, S 372 (1925) 6 BAN 2, S 125 (1925) 7 London R S Proc 111 A, S 424 (1926), The Internal Constitution of the Stars, S 377

peratur T Der Ionisationsgrad wird nämlich durch Gleichsetzung der Anzahl eingefungener Elektronen mit der Anzahl durch Ionisation ausgelöster erhalten Die erstere Anzahl ist proportional der Elektronendichte, die letztere der Strahlungsdichte Eine Multiplikation von beiden mit einem Faktor  $\delta$  ändert das Gleichgewicht nicht Der Faktor  $\delta$  kann aus dem Gesamtbetrag des Sternenlichts berechnet werden; für  $\varrho$  nimmt Eddington gemäß einer isothermen Gleichgewichtstheorie für die diffusen Nebel, die als Kondensationen in der interstellaren Materie angeschen werden können, die Größenordnung  $10^{-26}$  g/cm². Er erhält dann nach der Ionisationstheorie für die relativen Konzentrationen der verschiedenen Ca- und Na-Atome folgonde Werte

$$\frac{Ca}{Ca^{+}} = \frac{1}{300000}, \qquad \frac{Ca^{+}}{Ca^{++}} = \frac{1}{400}, \qquad \frac{Na}{Na^{+}} = \frac{1}{1000000}.$$

Für Ca wäre also der weit überwiegende Teil der Atome zweimal ionisiert und domnach zur Absorption in H und K unfähig. Ein analoges Verhältnis ergibt sich für die D-Linien des neutralen Natriums. Nur ein sehr kleiner Teil der interstellaren Materie von der angenommenen Dichte wäre also bei der Absorption in den erwähnten Linien wirksam, was auch mit den schwachen Intensitäten

der Linien in den Sternspektren in Übereinstlimmung steht

In O. STRUVES1 Arbeiten wurde das Problem auch empirisch von einer nouen Selte her angegriffen. Vorzagsweise für Sterne vom Spektraltypus O bis B3 hat er auf Spektrogrammon die Intensität der interstelleren K-Linie geschützt Das Arbeitsmaterial bildeten zuerst für 321 Sterne vom Typus O bis B3 Spaltspektrogramme, die auf den Sternwarten Mount Wilson, Victoria, Lick und Yerkes aufgenommen warden sind, dann für 1718 Sterne vom Typus O bis B3 und für 338 Sterne von spätoren Typen Objektivprismenplatten aus cler großen Sammlung der Harverd-Sternwarte Die Intensitäten wurden in einer Gedächtnisskale geschätzt, wo jede sukzessive Stufe einer eben bemerkbaren Zunahme der Intonsität entspricht Für die Spaltspektrogramme ist die Intenuität der K-Linie im Spektrum der Vega auf 10 fixlert worden, später wurde der Stern 9 Cephel (a = 21h 35m,2, b = +61° 38', B2p; 4m,7) als Standard mit derselben Intensität benutzt Der wahrschelnliche Fehler einer Schätzung war 0,5 Stufen für die Platten der ersteren Art und etwa 1,0 für die Harvard-Platten Nach einer genüherten Kalibrierung der Skale entspricht jede Stufe einer Größendifferenz von etwa 0m,1 in dem Intensitätsverhältnis zwischen Limenmitte und ningebondem kontinuierlichen Spektrum.

Mit seinem vollständigen Material hat Struve ausführlich die Relation zwischen Intensität, Spektraltypus und schembarer Größe untersucht. Tabelle 18 zeigt das Resultat für die Spektraltypen O bis B3. Für die späteren Unterabteilungen des B-Typus tibt schon die Absorption des Kalziums in der Sternutmosphäre einen merklichen Einfluß auf die Intensität der K-Linie aus.

Man sicht aus der Tabeile unmittelbar, daß für alle Untertypen die Intensität in derselben Welse mit abnehmender scheinbarer Helligkeit wächst, und auch daß für eine und dieselbe scheinbare Größe die früheren Typen in der Regel die größere Intensität aufwelsen. Diese Erscheinungen können am emischsten dadurch erklärt werden, daß die Intensität einfach eine Funktion der Entfernung der Sterne ist. Daß der Gang mit der scheinbaren Größe nicht auf irgendelnen systematischen Fehler zurückzufähren ist, beweist Struve durch Schätzungen der Linie 2 1924 (Sl++). Die mittlere Intensität dieser Linie zeigt keine Abhängigkeit von der scheinbaren Größe

Pop Astr 33, S 639 (1925), 34, S, 158 (1926), A N 227, S, 377 (1926), Publ A S P 38, S 211 (1926); Mt Wilson Contr 331 — Ap J 65, S, 163 (1927), Ap J 67, S, 353 (1928)

Tabelle 18

Scheinb		0	]	В0		Bı		B2	1	33
Große	n	I	n	1	n	I	u	I	n	I
0 1	0	_	0	-	1	1,0	0	-	0	
1-2	0	-	2	2,0	4	0,7	3	0,9	1	(),4
2-3	3	0,9	6	1,2	5	1,8	7	1,4	11	1,4
3-4	1	5,1	2	2,6	5	1,4	10	1,7	24	1.8
4- 5	6	3,9	9	2,6	11	3,0	18	3,0	97	2,1
5- 6	12	4,1	21	4,2	8	4.0	23	3,3	141	2,5
6- 7	17	4,2	45	3,4	11	4,2	42	3,2	201	2,9
7-8	24	5,0	66	3,8	17	3,8	85	3,9	197	3,2
8- 9	19	4,8	94	3,9	4	3,0	87	3,9	168	3,1
9-10	9	3,8	55	3.7	0		44	4,3	74	4,0
10-11	3	3.7	2	4.8	0	-	7	4,4	15	4,6
11-12	1	11,0	0		0		0	-	0	
7114	95	4,40	302	3.71	66	3,13	326	3,65	929	2,97

Die mittleren Intensitaten für verschiedene Milchstraßemegionen werden nach Struve in Abb 23 dargestellt

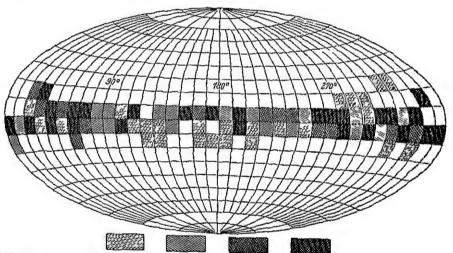


Abb 23 Galaktische Verteilung der Kalzumintensitäten Die vier Schattlerungen entsprechen der Reihe nach I < 2.8;  $2.8 \le I < 3.2$ ,  $3.2 \le I < 3.7$ ,  $3.7 \le I$  Die galaktischen Koordinaten der wichtigeren Regionen sind

Perseus Orion Monoceros Carina Crux Scorpius Sagittarius Cygnus Cepheus	$L = 100^{\circ} - 120^{\circ},$ $160 - 180$ $170 - 180$ $250 - 260$ $260 - 280$ $300 - 320$ $330 - 340$ $30 - 50$ $60 - 80$	$B = -10^{\circ} \text{ bis}$ $-10$ 0 -10 -10 -10 -10 -10 0	-20 +10 +10 +10 +10 +10	(solu schwach)
---	--	---	--	----------------

Es besteht eine Andeutung, daß im Intervall zwischen den galaktischen Langen 80° und 250° die Intensitaten durchschnittlich schwacher sind als in der gegenuberliegenden Hemisphare

Struye bemerkt, daß bei zusammengehörenden Doppelsteinkomponenten die Linien mit derselben Intensitat auftreten, und auch daß die Variation mit

der scheinbaren Größe innerhalb physisch zusammengehörender Sterngruppen, die ja bei dem B-Typus allgemein and, aufhört Für eine Milchstraßenregion in Cephens wurde die Beziehung der Kalzumabsorption zu einer absorbierenden Dunkelwolke, deren Entfernung Struvk auf Grund von Sternzählungen zu 350 Parsee schätzt, untersucht Es stellt sich heraus, daß keine Spur einer direkten Verbindung zwischen den zwei Erscheinungen besteht, wenngleich die "Kalziumwolken" und die Dunkelwolken violleicht teilweise einander räumlich berühren und durchdringen

Das eben beschriebene empirische Material haben B P Germemovič und O Struve<sup>1</sup> von theoretischem Gesichtspunkte aus eingehend behandelt. Mit den von Germenovič (vgl. Zilf 19) angegebenen mittleren Parallaxen der Untertypen der Hellumsterne und unter plansiblen Annahmen über die Streuung in  $\log n$  für Sterne von derselben scheinbaren Größe berechnen die Verfasser den Absorptionskooffizienten der interstellaren K-Linie Im Falle der B3-Sterne wird für die wahrscheinliche Abweichung r in  $\log n$ , vom wahrscheinlichsten Wert  $\log n$  gerechnet, nach Germenovič der Wert 0,094 angenommen, während im Falle B0 bis B2 für r alternativ mit den zwei Werten 0,32 und 0,16 gerechnet wird Für den Absorptionskooffizienten  $\beta$ , per Parsec gerechnet, ergeben sich somit die Werte in Tabelle 19 Die Tabelle zelgt eine sehr gute Übereinstimmung

Tabelle 19	ror Absorptionskooffixient ollare K-Ling per Parsec.	lür	dio
	 Do Bo	Ti s	

Mittiers scholnbare	D0 -	Do - Ba		
Grtiße	r = 0,32	r = 0,16	r = 0,094	
2,5	1,1 10-4	2,8 10-4	1,3 10-4	
3,5	1,1	2,8	3.0	
4.5 5.5 6.5	1,7	4,2	3.6	
5.5	2,0	5,0	4,2	
6,5	1,6	4,0	4,4	
7.5	1,6	4,0	4,4	
8,5	1,4	3.5	3,6	
9.5	1.3	3,2	2,9	
10,5	1.3 - 10-4	3,2 · 10-4	3.7 • 10-1	
Mittol	1,4 10-4	3,6 10-4	3,4 · 10-4	

der  $\beta$ -Worte für die verschiedenen scheinbaren Größen einerseits und für die B0- bis B2-Sterne (r=0.16) und die B3-Sterne andererseits. Man schließt aus diesen Resultaten, daß  $\beta$  bis zur Grenze der Boobachtungen konstant ist. Im Mittel ergibt sich  $\beta=3.4\cdot 10^{-4}$  oder per ein gerechnet,

Die Theorie für die Absorption in der K-Linie gibt, wenn der Einsteinsche Koaffizient  $A_{\rm BI}$  nach Millers Resultat für die Kalziumchromosphäre angenommen wird, die Anzahl  $N^+$  der einmal ionisierten Kalziumatome per cm³ in ihrer Beziehung zur totalen Absorption in der Linie. Für die letztere Größe wird gesetzt  $\beta\Delta\lambda$ , wo  $\Delta\lambda$  die Breite der Linie, etwa 0,3 A, ist. Wenn die Masse des Kalziumatoms in Rochnung gezogen wird, ergibt sich dann für die Dichte des einmal ionisierten Kalziums der Wert

Mit einer Strahlungstemperatur  $T=15300^\circ$  und einem "factor of dilution"  $W=2.2\cdot 10^{-17}$  ergibt die Ionisationstheorie, daß der weit überwiegende Teil

<sup>1</sup> Ap J 69, 8 7 (1929)

dei Kalzumatome im zweisch ionisierten Zustande (Ca<sup>++</sup>) sem muß. Die totale Dichte des interstellaren Mediums ist naturlich außeidem dadurch bestimmt, in welcher Proportion das Kalzum überhaupt im Medium vorhanden ist Gerasimovič und Struve rechnen hier mit zwei alternativen Annahmen Erstens wird die partielle Konzentiation  $\phi$  der Kalzumatome gleich 1, zweitensgleich dem entsprechenden Wert für die Erdkruste, 1,5–10<sup>-2</sup>, augenommen In den zwei Fallen ergibt sich für die Totaldichte

Werte, die sicher als extreme angeschen werden konnen. Da die interstellaren Wolken wahrscheinlich durch einen standigen Ausfuß von Atomen aus den Sternatmospharen durch die Wirkung eines selektiven Strahlungsdruckes bedingt sind, so ist die Konzentiation des Kalziums wahrscheinlich großer als in der Erdrinde

Da nur dei Biuchteil  $10^{-11}$  von den Kalziumatomen im neutralen Zustande ist, so konnen wir gewiß nicht ein meikbares Auftreten der Linien des neutralen Kalziums in den Sternspektren erwarten. Außei den Linien H und K des (al-Atoms sollte aber auch die infraiote Doppellinie sichtbai sein. Von besonderem Interesse sind die Prinzipallinien vom Typus  $1\sigma-1\delta$ , die vom Korrespondenzprinzip "verboten" sind. Diese Übergange sollten die zwei Linien im Rot  $\lambda$  7293,43 A und  $\lambda$  7325,91 A geben

Y Öhman<sup>1</sup> hat die Moglichkeit für das Auftreten der Ca<sup>1</sup>-Linien in Ermision im Spektrum des Nachthimmels diskutiert. Er kommt zu dem Schluß, daß die H- und K-Linien kaum zu erwarten sind, daß aber gewisse Möglichkeiten für die eben erwahnten "verbotenen" Linien bestehen. Er betont, daß uns eventuelle Emissionslinien des interstellaren Kalziums Auskunft über die Dichte des Stratums und über die Dimensionen des Milchstraßensystems geben konnten

Gerasimovič und Struve diskutieren auch das interstellare Natrium, für welches jedoch gegenwartig weit weniger Beobachtungsmaterial vorliegt. Sie gehen schließlich zu einer Diskussion der mittleren Radialgeschwindigkeiten des Kalziums für sukzessive Intervalle in galaktischer Lange über. Die Doppelwelle der Oortschen differentiellen Rotation der zentralen Milchstraßenschicht ist hier besonders deutlich ausgepragt. Eine Auflösung nach der Formel

$$K + rA \sin 2(L - 325^{\circ}) = \bar{\rho}$$

wo  $\bar{\varrho}$  die mittlere Radialgeschwindigkeit für die Lange L ist, gibt

$$rA = +5.3 \text{ km/sec} \pm 1.0 \text{ (w F)},$$
  
 $K = -0.6 \text{ km/sec} \pm 0.7 \text{ (w F)}$ 

Eine weitere Diskussion der diesbezuglichen Fragen wird in Ziff 31 folgen Zuletzt sei hier noch erwähnt, daß O Struve im Verdunkelungsveranderlichen U Ophiucht vom Typus B8 (nach Struve etwa B5) nahe dem Zeitpunkt dei maximalen Trennung der stellaren K-Linien zwischen diesen Linien die interstellare K-Linie beobachtet hat Dei Stern zeigt auch interstellare Natitumlinien Diese geben in guter Übereinstimmung mit der erwähnten K-Linie eine Radialgeschwindigkeit von -21 km/sec Nach Abzug der parallaktischen Bewegung gibt dies für die Restgeschwindigkeit der interstellaren Linien -3,5 km/sec Die Erklarung des Verschwindens der interstellaren K-Linie für Typen später als B3 durch ein Überdecken der interstellaren Linie durch die stellare oder wenigstens durch eine in gewohnlichen Fällen zu nahe Nachbarschaft der be-

<sup>&</sup>lt;sup>1</sup> Nature, Aug 3 (1929) <sup>2</sup> Ap J 72, S 199 (1930)

treffenden Linien im Spektrum gewinnt durch STRUVES Beobachtung sehr an Wahrscheinlichkeit.

Nach Gerasimovič und Struve ist das interstellare Gas in seiner Gesamtmasse von nur geringer dynamischer Bedeutung. Die Totalmasse kann kaum <sup>1</sup>/<sub>100</sub> der totalen Masse der Sterne betragen, und der Widerstandseffekt auf die Bewegungen der Sterne in ihren Bahnen muß verschwindend sein.

Andererseits ergibt sich die interstellare Materie als mögliche Quelle der harten kosmischen Strahlung. Wenn diese nach Millikans Hypothese aus einer Transmutation von H in He herrührt, wäre mit der gegebenen Energiedichte der kosmischen Strahlung, 4·40<sup>-16</sup> erg/cm³, eine Transmutation eines gewissen Atomes einmal während 10<sup>50</sup> Jahren zu erwarten. Das interstellare Gas ist aber als für die kosmische Strahlung fast vollkommen durchsichtig zu betrachten. Die monochromatische Absorption und eine Absorption für kurze Wellenlängen außerhalb der Seriengrenze ausgenommen, besteht die Durchsichtigkeit für alle Wellenlängen. Ein eventueller Zusammenhang mit dem absorbierenden Medium in der zentralen Milchstraßenzone kann daher wenigstens kein direkter sein.

## g) Die Dynamik der Milchstraße.

26. Milchstraße und Gastheorie. Rotation der Milchstraße. Lord KELVIN und H. Poincaré<sup>1</sup> haben auf die Analogie zwischen den Sternen in der Milchstraße und den Molekeln eines Gases hingewiesen. Wenn wir das Gesamtsystem der Milchstraße ins Auge fassen, können wir die Sterne als eine große Menge materieller Punkte betrachten, die einander nach dem Newtonschen Gesetze anzichen und die gegeneinander in jedem Augenblicke translatorische Bewegungen in allerlei Richtungen haben. Bei starken Annaherungen zwischen zwei Sternen werden die Bahnen nach den Gesetzen der hyperbolischen Bewegung geknickt. Die Repulsionskraft zwischen Gasmolekeln, die sehr schnell mit dem Abstande zwischen den Molekeln abnimmt, wird also hier durch eine NEWTONsche Attraktion ersetzt, die für ein einzelnes Sternpaar mit wachsender Entfernung unmerkbar wird. Wir haben also eine ziemlich bestechende Analogie. Das "Sterngas" der Milchstraße muß aber als extrem verdünnt angesehen werden. Wenn wir den Aktionsradius eines Sterns so groß annehmen, daß ein Vorübergang eines anderen Sternes in dieser Entfernung eine Ablenkung der Bahnen von nur einem Bruchteil eines Grades verursacht, werden wir doch auf eine freie Weglänge geführt, die die wahrscheinlichen Dimensionen des Systems weit übertrifft.

Eine naheliegende Erklärung der augenscheinlich großen Abplattung des Sternsystems wäre, was wohl zuerst von J. Herschel ausgesprochen wurde, die, daß das System als Ganzes eine allgemeine Rotationsbewegung besitzt und daß die Abplattung aus dem Gleichgewicht der Zentrifugalkraft mit der Newtonschen Attraktionskraft folgt. Poincaré hat gezeigt, daß für ein kontinuierliches Medium der Dichte  $\varrho$  eine obere Grenze der Winkelgeschwindigkeit  $\omega$  durch die Relation

 $\frac{\omega^8}{2\pi G\varrho} < 1$ 

gegeben ist, wo G die Gravitationskonstante bedeutet. Da im Sternsystem  $\varrho$  sehr klein ist, wird  $\omega$  auch sehr klein, und die minimale Rotationszeit T lang, von der Größenordnung 10<sup>7</sup> Jahre. (Diese Schätzung nach einem neueren Wert von  $\varrho$  ergibt eine beträchtlich kleinere Grenze von T als Poincarés Wert von  $5 \cdot 10^8$  Jahren.)

Leçons sur les hypothèses cosmogoniques, S. 257. Paris 1911.
 BA 2, S. 109 (1885).

Da das astronomische Koordinatensystem ein Inertialsystem ist und die Lagebestimmungen, wie C V L CHARLIER hervorhebt, auf die invariable Ebene des Planetensystems ubergefuhrt werden können, so wäre es möglich, in den Eigenbewegungen der Sterne einen solchen Rotationseffekt zu finden Unter den ersten Versuchen, in den Eigenbewegungen einen Rotationseffekt aufzuspuren, ist voi allem derjenige von II Gyldén in einer unten (Ziff 31) naher besprochenen Arbeit aus dem Jahre 1871 zu nennen Andere Untersuchungen ruhren von E Schonfeld<sup>1</sup>, F Bolte<sup>2</sup> und F RANCKEN<sup>3</sup> her J. Struvi I fuhrte Rotationsterme in die Gleichungen zur Bestimmung der Prazessionskonstante ein Charlier scheint der erste zu sein, der einen ziemlich zuverlassigen Wert hergeleitet hat Die letzte von ihm ausgefuhrte Bestimmungs gibt eine mittlere Eigenbewegung in galaktischei Lange von -0",0024, pio Jahi gerechnet Charlier macht die Bemerkung, daß eine retrograde Prazession der invariablen Ebene infolge einer dynamischen Einwirkung des umgebenden Sternsystems auf unser Planetensystem diesen Weit bedeutend erhöhen kann Wir werden unten auf andere Bestimmungen eingehen und dabei auch bemeiken, daß die mittlere Bewegung in galaktischer Lange (mit B bezeichnet) durch einen anderen Rotationseffekt, der auf einer in der Milchstraßenebene mit dem Abstande vom Zentrum varuerenden Winkelgeschwindigkeit bezuht, wahrscheinlich vermindert wird und also nicht unmittelbar der Winkelgeschwindigkeit av entspricht

Eine Rotationsbewegung wurde weiter mit negativem Zeichen in die durch Anschluß an umgebende Sterne bestimmten Eigenbewegungen der "anagalaktischen" Nebel eingehen, wenn diese, was gegenwärtig als gesichert angesehen werden kann, außeihalb des Sternsystems gelegen sind. Diesen Weg hat kurzlich K. Lundmarke eingeschlagen. Die Resultate geben wenigstens eine Andeutung von einem Effekt der oben genannten Ait, abei das Material ist noch nicht für eine sichere Bestimmung hinreichend. Es gilt aber auch hier, daß nicht unmittelbar die Winkelgeschwindigkeit ω, sondern die Größe B gemessen wird.

27. Allgemeine statistische Mechanik des Sternsystems. Grund der Analogie zwischen Sterndynamik und Gastheorie aus der letzteren Konsequenzen fur die ersteie zu ziehen, können wir von vornheiem die Eigenschaften der Steine als Massenpunkte einführen und eine statistische Mechanik auf Grund des Newtonschen Gesetzes aufbauen Un begegnen hier sogleich einer großen Verschiedenheit zwischen Stern- und Gasdynamik In dem Steinsystem ist namlich die das System zusammenhaltende "reguldre" Kraft nur eine Summe derjenigen Krafte, die auch als Passage- oder Stoßkrafte auftieten, wenn die Sterne einander paarweise gegenübergestellt werden. Es läßt sich also nicht ohne weiteres um einen Stern ein Stoßbereich, der klein ist gegen die mittleie Distanz zwischen den Sternen und außerhalb dessen die Passagekräfte ignorieit werden konnen, absondern Mit wachsender Entfernung vom betrachteten Stein aus haben wir es aber mit einem mehr und mehr komplizierten Zustand vielfacher Passagen zu tun, und die Passagekrafte gehen allmahlich durch Summierung ın die regularen Krafte uber Wir konnen daher mehr oder weniger willkiulich eine obere Grenze fur die Distanz der Passagen fixieien und nur den Einfluß der individuellen Vorubergänge innerhalb einer gewissen Sphare in Rechnung

<sup>&</sup>lt;sup>1</sup> V J S 17, S 255 (1882) <sup>2</sup> Diss Bonn (1883) <sup>3</sup> A N 104, S 149 (1883), auch Diss Helsingfors

Mémoires de l'Academie Impériale de St Pétersbourg (VII) 35, Nr 3 (1887)
 The Motion and the Distribution of the Stars Mem Univ Calif 7, S 32 (1926)
 Studies of Anagalactic Nebulae, S 38 Nova Acta Reg Soc Sc Upsala, Volumen extra

ziehen. Die Kräfte der außerhalb dieser Sphäre gelegenen Massen werden dann

in eine reguläre Kräfteresultante zusammengesetzt.

J H Jeans<sup>1</sup> hat besonders den Einfluß der nahen Passagen auf die reguläre Bahn eines Sterns untersucht Wenn wir mit  $\sigma$  den kleinsten Abstand zwischen zwei Sternen von den Massen M und M' bei einem Vorübergang, dem eine kleine Defiektion  $\psi$  der relativen Bahn entspricht, bezeichnen, so haben wir

$$\sigma = \frac{2G(M+M')}{\psi v^4},$$

wo v die relative Geschwindigkeit ist Nehmen wir  $\psi=1^\circ$  und mit Jeans  $M+M'=6.8\cdot 10^{10}$  g (= 3.4 Sonnenmassan),  $v=4\cdot 10^4$  cm/sec (40 km/sec), so finden wir  $\sigma=3.2\cdot 10^{10}$  cm, einen Wert, der ungefähr siebenmal größer als der Durchmesser der Neptunbahn ist Die mittlere Zeit t zwischen Passagen in Distanzen  $\leq \sigma$  kann aus der gustheoretischen Formel  $t=\frac{1}{\kappa\tau\sigma^2v}$  berechnet werden, wo v die Anzahl Sterne pro Volumeneinheit ist. Die mittlere Zeit zwischen den Passagen wird von der Größenordnung  $10^{11}$  Jahre Für Kollisionen innerhalb einer Distanz gleich dem Radius der Neptunbahn ergibt sich die mittlere Zwischenzeit zu  $4\cdot 10^{10}$  Jahre. Während sehr langer Zeiten können wir daher die sehr nahen Passagen ignorderen.

Für den kumulativen Effekt der Passagen zwischen den Distanzen  $\sigma_1$  und  $\sigma_2$ 

während der Zelt i leitet JRANS die Formel ab

$$\sigma_{\eta}^{1} = t \cdot \frac{6\pi r G^{1} M^{\prime 1}}{\overline{\sigma}} \log \frac{a_{0}}{\sigma_{1}}, \qquad (1)$$

wo  $v_a$  die gagen die ursprüngliche Bewegungsrichtung senkrechte Geschwindigkeltskomponente eines Sterns ist. Wenn wir für  $\sigma_1$  den obigen Wert von  $\sigma$  für  $\psi = 1^\circ$  annehmen und nur die Passagen ziemlich nahellegender Sterne, innerhalb 20 Parsec, berücksichtigen, bekommen wir

$$v_{\bullet} = \frac{1}{4}\sqrt{\ell}, \tag{2}$$

also ome transversale Goschwindigkeitserhöhung von ½ cm/sec in einem Jahre und 1 km/sec nach 40000 Millionen Jahre. In dieser Weise hat JEANS bewiesen, daß der Einfluß der Passagen naheliegender Sterne in der ersten Approximation zu vernachlässigen ist, und daß die Sterndynamik in erster Linie das Problem

der Bowegung unter den regulären Kräften des Systems enthält.

CHARLIER<sup>2</sup> hat nach dem Vorbild der kinetischen Gastheorie eine statistische Mechanik auf Grund des Newtonschen Gesetzes entwickelt. Die Anzahl Storne innerhalb des Volumenelementes dxdydz um den Punkt x, y, z herum, welche Geschwindigkeitskomponenten innerhalb dudvdw um den Punkt u, v, w im Geschwindigkeitsraume herum haben, sei mit f(x, y, z, u, v, w, t) bezeichnet. Die fundamentale Differentialgleichung der Verteilungsfunktion kann man in der Boltzmannschen Form

$$\frac{\partial f}{\partial t} + u \frac{\partial f}{\partial w} + v \frac{\partial f}{\partial y} + w \frac{\partial f}{\partial z} + X \frac{\partial f}{\partial u} + Y \frac{\partial f}{\partial v} + Z \frac{\partial f}{\partial w} = P(f) + \Box (f)$$
 (3)

ausdrücken, wo X, Y, Z die Komponenten der regulären Kraft im Punkte x, y, x sind. P(f) ist die "Passagefunktion" und  $\square(f)$  die "Kollisionsfunktion" P(f) wird wie in der kinetischen Gastheorie gemäß der Dynamik der Passagen als ein mehrfaches Integral ausgedrückt Die Funktion  $\square(f)$ , die wirklichen Zusammenstößen der Sterne Rechnung trägt, wird im Hauptteil der Charlierschen Arbeit

Lund Modd Sor II, 16 (1917).



<sup>1</sup> Problems of Cosmogony and Stellar Dynamics, S. 224. Cambridge 1919

weggelassen, da sie wahrend absebbaiei Zeitiaume keine Rolle spielt. CHARLII R entwickelt die Funktion / in eine Frequenzfunktion vom Typus A und leitet aus der Bolizmannschen Gleichung für die Koeffizienten Differentialgleichungen ab. Für die obere Gienze der Distanz, innerhalb welcher eine Passage gerechnet wird, nimmt Charlier die halbe mittlere Entfernung zwischen den Steinen unserer Umgebung an

Aus den Differentialgleichungen der Koeffizienten zweiter Ordnung leitet Charlier ab, daß eine ursprunglich ellipsoidische Verteilung der Geschwindigkeiten u, v, w mit der Zeit nach Gleichheit der Dispersion in verschiedenen Richtungen strebt. Die Zeit, in der ein Überschuß des Quadrates der Dispersion in einer Richtung auf 1/e seines Betrages reduziert wird, die "Relaxationszeit", wird von Charlier zu 3,6 10<sup>16</sup> Jahren geschatzt. Die Langsamkeit der Wirkung der Steinpassagen ist also hier bestatigt worden

C F LUNDAHL<sup>1</sup> hat CHARLIERS Ausemandersetzungen unter spezieller Be-

rucksichtigung der Kollisionsfunktion fortgesetzt

Da offenbar  $\Gamma(f)$  und  $\Gamma(f)$  nur eine sehr langsame Veranderung der Prequenzfunktion / herbeifuhren konnen, mussen wir zuerst in der Boltzmannschen
Gleichung Passagefunktion und Kollisionsfunktion außer acht lassen und den
Bewegungszustand des Systems unter der alleinigen Wirkung der regularen
Systemkrafte X, Y, Z studieren Wir haben also

$$\frac{\partial f}{\partial t} + u \frac{\partial f}{\partial v} + v \frac{\partial f}{\partial y} + w \frac{\partial f}{\partial z} + X \frac{\partial f}{\partial u} + Y \frac{\partial f}{\partial v} + Z \frac{\partial f}{\partial w} = 0 \tag{4}$$

zn setzen, wo 
$$X = \frac{du}{dt}, \quad Y = \frac{dv}{dt}, \quad Z = \frac{dw}{dt}$$
 (5)

$$\varrho = \iiint_{-\infty}^{+\infty} m / du \, dv \, dw \,. \tag{6}$$

Diffuse gasformige Materie im Raume denken wir uns über die Partikeln verteilt und im m eingerechnet. Wenn wir die Verteilung von  $\varrho$  nach  $\lambda$ ,  $\gamma$ , z für einen gewissen Augenblick festhalten, so können wir gemaß dieser Dichtigkeitsverteilung und gemaß den augenblicklichen Lagen und Geschwindigkeiten der Partikeln ihre Bahnen im sechsdimensionalen Raume berechnen. Das Gravitationspotential V wird nach Poissons Gleichung bestimmt

$$\frac{\partial^2 V}{\partial x^2} + \frac{\partial^3 V}{\partial y^2} + \frac{\partial^3 V}{\partial z^2} = -4\pi G\varrho \tag{7}$$

In der wirklichen Bewegung wird aber im allgemeinen Falle die Dichtefunktion  $\varrho$  stetig modifiziert, wir wollen sagen durch eine Funktion  $\Delta\varrho$ , welche von den Koordinaten x, y, z und der Zeit  $\Delta t$  abhangt. Wenn wir eine kontinuierliche Variation der Dichtigkeit  $\varrho$  und der mittleien Geschwindigkeiten u, v, w mit x, y, z voraussetzen, so kann gemaß der Kontinuitatsgleichung

$$\frac{\partial \varrho}{\partial t} + \frac{\partial (\varrho \, \overline{u})}{\partial v} + \frac{\partial (\varrho \, \overline{v})}{\partial y} + \frac{\partial (\varrho \, \overline{w})}{\partial z} = 0 \tag{8}$$

<sup>1</sup> Lund Medd Ser II, 45 (1926)

 $\partial \varrho/\partial t$  nie ins Unendliche wachsen. Wenn wir demgemäß während des Zeitelements  $\Delta t$  erster Ordnung das Integral  $\int \int |\Delta \varrho| dx dy dz$ , über das ganze System erstreckt, als eine kleine Größe von der ersten oder von höherer Ordnung betrachten, so erscheinen "Störungskräfte" erster oder höherer Ordnung mit Komponenten von der Form  $\int \int \frac{\Delta \varrho}{r^2} x dx dy dz$ , wo r die Distanz von dem betrachteten Ort (Origo) bis zum Punkte x, y, z ist. In der Bewegung einer Partikel während des Zeitelements  $\Delta t$  erleiden daher die Geschwindigkeitskomponenten u, v, w "Störungen"  $\Delta u$ ,  $\Delta v$ ,  $\Delta v$  zweiter oder höherer Ordnung, während jedoch die entsprechenden  $\Delta x, \Delta y, \Delta z$  von höherer Ordnung als der zweiten sind. Für die Berechnung der Dichtigkeitsverteilung nach einem kleinen Zeitintervall  $\Delta t$  von dem betrachteten Zeitpunkt an können wir daher bis auf Größen höherer Ordnung als der zweiten die wahre Bewegung der Partikeln durch die Bewegung in den augenblicklichen sechsdimensionalen Bahnen ersetzen. Wir können diese Bahnen auch als Stromlinien in der sechsdimensionalen Mannigfaltigkeit bezeichnen.

Wenn wir aber auf die Verhältnisse für längere Zeiten Rücksicht nehmen, werden infolge der Veränderungen des Kraftfeldes die Partikeln längs einer gewissen augenblicklichen Bahn über eine Serie verschiedener, mehr oder weniger benachbarter Bahnen eines späteren Zeitmoments gestreut. Dieser Umstand, wie auch die verschiedenen angulären Geschwindigkeiten in den Bahnen um den Schwerpunkt herum bewirken eine fortschreitende Mischung der Materie des Systems und eine stetige Ausgleichung der Frequenz zwischen einander benachbarten sechsdimensionalen Bahnen.

Wir nehmen jetzt an, daß eine weitgehende Mischung und Ausgleichung in der Materie des Systems stattgefunden hat. Wir teilen die Materie in eine Unzahl von augenblicklichen, sechsdimensionalen Bahnen, jede Bahn mit einer gewissen mittleren Dichtigkeit /, auf und setzen infolge der Mischung eine im wesentlichen regellose Verteilung der Partikeln längs einer Bahn voraus. Da die räumliche Dichtigkeit  $\varrho$  aus einer Integration in u,v,w bestimmt wird, also aus einer Summierung über unendlich viele Bahnen, die den betrachteten Punkt durchkreuzen, so ist sie also, von kleinen Schwankungen abgesehen, als wahrscheinlich von der Zeit unabhängig zu betrachten. Die sechsdimensionalen Partikelbahnen werden dann stationär, und da wir die Verteilung in diesen Bahnen als regellos betrachten, so ist die a priori zu erwartende Frequenz / in einer

solchen Bahn als von der Zeit unabhängig anzuschen, was mit der Gleichung

$$\frac{\partial f}{\partial t} = 0, \tag{9}$$

oder der daraus gemäß der Gleichung (4) folgenden

$$\frac{\partial f}{\partial w}dx + \frac{\partial f}{\partial u}dy + \frac{\partial f}{\partial z}dz + \frac{\partial f}{\partial u}du + \frac{\partial f}{\partial v}dv + \frac{\partial f}{\partial w}dw = 0$$
 (10)

äquivalent ist. Dieses Resultat stimmt mit einem Satz von Poincaré überein, nach welchem in einem stationären Zustande die Dichtigkeit der Partikeln im generalisierten Raume der kanonischen Variabeln  $q_1, q_2, \ldots, q_n, p_1, p_2, \ldots, p_n$  längs der Bahn einer Partikel in diesem Raume konstant ist. Wenn die Bewegungsgleichungen k erste Integrale

$$I_1 = \text{konst.}, \quad I_2 = \text{konst.}, \quad \dots, \quad I_k = \text{konst.}$$
 (11)

haben, so kann die Verteilungsfunktion

$$f(I_1, I_2, \ldots, I_k) \tag{12}$$

<sup>1</sup> Leçons sur les hypothèses cosmogoniques, S. 100 (1911).

geschrieben werden, vorausgesetzt, daß die Bahn einer Partikel das Gebiet von 2n - k Dimensionen, welches durch die Gleichungen (11) definiert wird, ausfullt.

Im aktuellen Falle betrachten wir jetzt sowohl die Lagen als die Geschwindigkeiten in bezug auf den Schwei punkt des Systems Fui eine allgemeine Dichtigkeitsverteilung haben wir nur ein eistes Integral, das Energieintegral

$$I_1 = u^2 + v^2 + w^2 - 2V = \text{konst}$$
 (13)

Eine Verteilung  $f(I_1)$  wird aber ein endliches Rotationsmoment der Masse ausschließen

Fur einen stationalen Zustand bei endlichem Rotationsmoment muß dahei eine rotationssymmetrische Verfeilung um eine gegen die fundamentale Rotationsachse senkrechte Achse vorausgesetzt werden. Die Frequenzfunktion kann dann geschrieben werden.

 $/(I_1, I_2), \tag{14}$ 

wo

$$I_2 = vv - uy, \tag{15}$$

wenn die vy-Ebene die Ebene maximaler Flachengeschwindigkeit des Systems ist. In dieser Form ist Poincarés Theorem speziell von Jeans¹ und von Charlier² aufgenommen und diskutiert worden. Die Existenz eines Gleichgewichtszustandes, welcher durch eine gewählte Funktion  $f(I_1, I_2)$  bestimmt wird, unterliegt naturlich der Bedingung, daß Poissons Gleichung Genuge geleistet wird, d. h. daß V gemäß einer aus (14), (6) und (7) resultierenden Gleichung  $\Delta V = \Psi(V, R)$  bestimmt werden kann, wo  $R^2 = v^2 + y^2$ 

In dem eben zitieiten Werke hat Poincaré auch das wichtige Theorem von Jacobi, welches im Virialtheorem von Clausius enthalten ist, in die theoretische Behandlung der astronomischen Partikelsysteme eingeführt. Eine Anwendung dieses Theorems auf den Bewegungszustand in Sternhaufen ist spater von Eddingfon<sup>3</sup> gemacht worden. Wenn J das Tragheitsmoment in bezug auf den Koordinatenanfangspunkt, T die kinetische und W die potentielle Energië (W = 0 für unendliche Verdunnung des Systems) ist, so haben wir

$$\frac{1}{2}\frac{d^{2}J}{dt^{2}} = 2T + W \tag{16}$$

Im stationaren Zustande ist also

$$2T + W = 0 \tag{17}$$

Jeans<sup>4</sup> hat dieses Theorem auf die Frage nach dem Ursprung des galaktischen Systems angewandt. Konnen wir uns z. B. denken, daß unser System aus einem Zusammenfließen von einzelnen kleineren Sternhaufen entstanden ist? Wenn  $T_1$  und  $W_1$  die kinetische und die potentielle Energie eines einzelnen Haufens von dem Zusammenstoß mit anderen Haufen,  $U_1$  die Translationsenergie des Haufens in bezug auf den gemeinsamen Schweipunkt aller Haufen,  $T_0$  und  $W_0$  die kinetische und die potentielle Energie des resultierenden Systems sind, so gilt  $T_0 + W_0 = \sum (T_1 + W_1 + U_1)$ 

Wenn jeder Haufen vor dem Zusammenstoß in einem stationaren Zustand sich befunden hat, so haben wir außerdem

$$2T_1 + W_1 = 0$$

und auch, sobald das große System stationar wird,

$$2T_0 + W_0 = 0$$

M N 76, S 70 (1915)
 Lund Medd Ser I, 82 (1917)
 M N 76, S 525 (1916)
 M N 82, S 138 (1922), Astronomy and Cosmogony, S 377 (1929)

Man bekommt nach diesen Voraussetzungen sofort

$$W_{\bullet} = \sum W_1 + 2 \sum U_1 \tag{18}$$

Die Translationsenergie der Haufen wird also in potentielle Energie verwandelt. und in der Regel muß also eine gewaltige Expansion auf ein Zusammenfließen von der genannten Art folgen Die große Ausdehnung des galaktischen Systems steht also durchaus nicht in Widerspruch zu einem eventuellen Ursprung in einer Kombination einer Anzahl viel kleinerer Systome, die sich allmählich durch gegenseitige Einwirkungen auflösen

Eine ausstihrliche geschichtliche Übersicht der hier behandelten Probleme und eine Weiterführung der Theorie des stationaren Zustandes hat J. Ohlsson<sup>1</sup> gegeben In Analogie mit einem Resultat der Ohlssonschen Arbeit beweist U WEGNER durch eine exakte Lösung der Boltzmannschen Gleichung für den Fall einer zweidimensionalen achsensymmetrischen Verteilungsfunktion von CHARLIERS Typus A, daß diese Funktion sich notwendig auf die MAXWELLsche Form C . 02 V-10-10 reduziert

28. Theorie der Sternströmung im typischen Sternsystem. Die kapitale Entdeckung von Kapteyn, daß die pekullaren Bewegungen der Sterne nicht regellos verteilt sind, sondern eine gewase Richtung im Raume bevorzugen, die sehr nahe in der Milchstraßenebene gelegen ist, weckte die Hoffnung, dieses Phanomen als eine Eigenschaft eines stationaren Zustandes deuten zu können. um damit über den Aufbau des Milchstraßensystems wichtige Schlüsse zu siehen Die erste Deutung des Phanomens im Sinne der Kapteynschen Zweistromtheorie sagt ja schon etwas in der Richtung einer dynamischen Erklärung aus, aber nichts zu der Frage, ob diese Bewegungsert eine stationäre Erscheinung an unserem Orte im System sein kann. H H. TURNERS stellte die Hypothese auf, daß die Sternströmung der ein- und ausgehenden Bewegung in Bahnen, die mit großer Exzentrizität um den Schwerpunkt des Systems verlaufen, ontsprochen könne Da der Vertex der Sternströmung ungefähr in der galaktischen Länge 340° llegt, also in der Gegend der hellsten Milchstraßenwolken, hatte diese Hypothese an sich eine nicht unerhebliche Wahrscheinlichkeit, würde aber eine sehr erhebliche zentrale Kondensation der Materie voraussetzen. Nach einer strengen Theorie gemäß den oben (Ziff. 27) gegebenen Aussinandersetzungen ist weiter in einem abgeplatteten System nur cine gegon den Radiusvoctor transversale Sternströmung möglich (vgl unten JEANS) und kann eine radiale stationare Sternströmung nur in Systemen von sphärischer Massenvertellung vonkommen

Daß bel sphärischer Symmetrie eine radiale, überall ellipsoidische Sternströmung möglich ist, wurde zuerst von Ennington nachgewiesen. Die außerdem einzige Möglichkeit einer überall streng allipsoldischen Geschwindigkeitsverteilung (and zwar in einer nahe radialen Richtung) besteht nach Eddiscrons für ein abgeplattetes System, wenn das System ein Untersystem ist und die Gravitationskraft von einer vorherrschenden sphärischen Masse konstanter Dichte bestimmt wird

Die Hypothese einer radialen Sternströmung wurde später praktisch außerhalb der Diskussion gelassen. JEANS suchte die Frequenzfunktion im stationären rotationssymmetrischen Zustande auf die Behandlung des Problems anzuwenden In diesem Falle ist die Frequenzfunktion in der Form  $I(I_1, I_2)$  zu schreiben, wo I1 das Energieintegral und I2 das Plächenintegral für die Symmetriechene ist. Jeans führt zylindrische Koordinaten R,  $\theta$ , s ein, wobel die ontsprechenden

Lund Medd Ser II, Nr 48 (1927)
 MN 72, S 387 (1912).
 MN 75, S. 366 (1915).
 MN 76, S. 37 (1915); Obs 41, S. 132 (1918) \* Zf Phys 45, 8 539 (1927).

hnearen Geschwindigkeiten mit  $\Pi$ ,  $\Theta$ , Z bezeichnet werden. Das Flachenintegral ist dann  $R\Theta$ , und die Frequenzfunktion schreibt sich

$$f(\Pi^2 + \Theta^2 + Z^2 - 2V, R\Theta) \tag{19}$$

Die Geschwindigkeitsverteilung ist somit symmetrisch in II und Z, eine preferentielle Strömung ist nur in Ø möglich, also in der Richtung senkt er lit zum Radiusvector Aus diesem Umstand schloß Jeans zueist, daß die Sternströmung nicht als eine stetige Bewegung im Steinsystem gedeutet werden kann

Cherlier wies abei auf die Tatsache hin, daß die Hehumsteine in unserei Nahe um ein Zentrum in der galaktischen Lange 240° herum verteilt sind und daß die Richtung gegen dieses Zentrum nahezu senkrecht gegen die Verteitstichtung der Sternströmung ist. Da weiter die stellarstatistisch gefunderen Geschwindigkeitsellipsoide nahezu eine verlangerte, rotationssymmetrische Form haben, wird auch sehr nahe die Bedingung erfullt, daß im stationären Zustande die Verteilung in den Komponenten II und Z rotationssymmetrisch um die O-Komponente sein soll, wenn wir eine stationare Bewegung um den Zentralpunkt der Hehumsterne annehmen. Diese Theorie kann mit der Anschauung eing versbunden werden, nach der die Heliumsteine den Kein eines "lokalen Systems", einer Sternwolke innerhalb des größeren Milchstraßensystems, bilden. Eine obenerwahnte Arbeit von Eddington zeigt jedoch, daß die Geschwindigkeits verteilung bei transversaler Sternströmung micht überall im System streng ellipsoidisch sein kann.

Auf einem ganz anderen Wege hat Kapteyn' einen großartigen Versie b gemacht, eine Dynamik des Sternsystems zu begrunden. Er ging daber von der empirisch gegebenen Sternverteilung im typischen Sternsystem aus, berechnete unter einigen vereinfachenden Annahmen die Gravitationskraft (zunächst in einer willkurlichen Einheit) in verschiedenen Punkten des Systems und suchte dann die empirischen Ergebnisse der Geschwindigkeitsveileilung in diesen Rahmen hmemzupassen Fur die Abhangigkeit dei Dichte von der Höhe über der galak tischen Ebene und die barometrische Gleichung angewandt; es eigibt sich daber, daß die mittlere Masse der Sterne, die den Absolutwert der Gravitationskraft bestimmt, von 2,2 Sonnenmassen in unserer Nahe auf 1,4 fur die außerste herucksichtigte Dichtigkeitsschale abnummt. Für das Gleichgewicht in der galaktischen Ebene ist eine Rotationsbewegung notwendig, die für größere Distanzen nahezu konstant und gleich 19,5 km/sec wird. Die Steinströmung wird durch zwei einander entgegengesetzte Rotationsbewegungen eikläit, die also eine relative Geschwindigkeit von rund 40 km/sec, in Übereinstimmung mit dem emphisch gefundenen Wert, gibt Das Zentrum soll in einer gegen die Steinströmung senkrechten Richtung, in einem Abstande von ca 650 Paisce, gesucht werden

Die Kapteynschen Resultate veranlaßten Jeans² zu einer mathematisch sehr eleganten Behandlung des Problems Von der oben gegebenen Form der Frequenzfunktion im rotationssymmetrischen Falle ausgehend, bildet Jeans die quadratischen Momente der Geschwindigkeitskomponenten, d h die Mittelwerte  $\widehat{HO}$  nsw Wenn  $\nu$  die Anzahl Sterne pro Volumeneinheit bedeutet, eihält man

$$\nu \overline{HO} = 0$$
,  $\nu \overline{HZ} = 0$ ,  $\nu \overline{\ThetaZ} = 0$ ,  $\nu \overline{H}^2 = \nu Z^2$ .

JEANS schreibt

$$\nu \overline{II^2} = \nu \overline{Z^2} = p , \qquad \nu \overline{O^2} = q$$
 (20)

<sup>&</sup>lt;sup>1</sup> Mt Wilson Contr 230 = Ap J 55, S 302 (1922)
<sup>2</sup> M N 82, S 122 (1922)

und zieht dann zur weiteren Behandlung des Problems die Gleichungen der Massenbewegung in einem System materieller Punkte heran, die unter Verwendung rechtwinkliger Koordinaten von der folgenden Form sind

$$\frac{d}{dt}(\nu\bar{u}) + \frac{\partial}{\partial w}(\nu\bar{u}^{\bar{u}}) + \frac{\partial}{\partial y}(\nu\bar{u}^{\bar{u}}) + \frac{\partial}{\partial z}(\nu\bar{u}\bar{w}) = \nu\frac{\partial V}{\partial w}.$$
 (21)

Im stationaren Zustande verschwindet der erste Term. Wichtig ist zu bemerken, daß in diesem Falle die Erfüllung der "Druckgleichungen" (21) die Folge einer Frequenzfunktion vom Typus (19) ist, wovon man sich durch Berechnung der linken Seite in (21) unter Voranssetzung einer Frequenz nach (19) überzeugt. Wir bekommen nach Einführung zylindrischer Koordinaten

$$\frac{\partial p}{\partial s} = v \frac{\partial V}{\partial s}, 
\frac{\partial p}{\partial R} + \frac{p - q}{R} = v \frac{\partial V}{\partial R}.$$
(22)

Diese Gleichungen golten für jeden einzelnen physikalisch definierten Sterntypus für sich, nur ist V immer des Gravitationspotential, das von allen Sternen und aller dunklen Materie zusammengenommen herrührt

Wenn  $\nu$  und dann V, in einer von der mittleren Masse der Sterne abhängigen Einheit, als bekannte Größen angenommen werden, kann  $\phi$  für einen Punkt des Systems aus

 $\dot{p} = -\int \gamma \frac{\partial V}{\partial x} dx \tag{23}$ 

berechnet werden, wo die Integration vom betrachteten Punkt sich der s-Achse parallel bis in eine Region, wo r zu vernachlässigen ist, erstreckt.  $\frac{P}{r} = \overline{H^2} = \overline{Z^2}$  kann in dieser Weise für jeden Punkt des Systems in einer später zu bestimmenden Einhelt berechnet werden. Dann ergibt sich aus der Gleichung die Größe  $\frac{P-q}{R}$ , woraus  $\frac{q-p}{r}$  für jeden Punkt erhalten werden kann.

Wenn  $h_1, h_2$  die Halbachsen des Geschwindigkeitsellipsoids sind, haben wir

$$\frac{h!}{h!} = \frac{\sum G^0}{\sum Z^1} = \frac{g}{b} \,. \tag{24}$$

In der Nähe der Sonne nimmt JEANS  $h_1/h_2 = 0,577$  an, und daraus folgt

$$\frac{q-p}{r} = 2,00 \cdot \frac{p}{r} \,. \tag{25}$$

Aus dieser Bedingung kann die Distanz R der Sonne von der Rotationsachse mit Hilfe einer berechneten Tabelle zusammengehöriger Werte von  $\frac{q-p}{r}$  und  $\frac{p}{r}$  bestimmt werden. Jeans findet R=1090 Parsec Der Wert von  $\frac{q-p}{r}$  in der angenommenen willkürlichen Einheit wird dementsprechend aus der Tabelle entnommen. Die Absolutwerte von q/r und p/r sind aber durch die gegebenen Werte von  $h_1$  und  $h_2$  bestimmt, oder man hat, wenn man nach der Zweistromtheorie die Strömungsgeschwindigkeiten U' und U'' annimmt, wie leicht zu ersehen ist,

 $\underline{q-p} = U'U^p. \tag{26}$ 

Durch Vergleich der zwei Werte von 2-2 erhält man den Wert der früher unbestimmten Einheit des Potentials V, und daraus die mittlere Sternmasse.

 $i \neq j$ 

Diese ergibt sich zu 6,34 · 10<sup>38</sup> g oder 3,2 Sonnenmassen. Dieser Wert ist aber als derjenige Mittelwert der Masse anzusehen, der erhalten wird, wenn die ganze Masse des Systems auf die leuchtenden Sterne verteilt wird. Die dunkle und

neblige Materie ist also in diesem Mittelwert eingerechnet.

Da Kapteyns typisches System Rotationssymmetrie um die Soume besitzt, die Sternströmungstheorie nach den soeben angewendeten Prinzipen aber eine exzentrische Stellung der Sonne fordert, muß dem Kapteynschen System eine gewisse Retusche gegeben werden, damit die obigen Auseinandersetzungen logisch miteinander vereinbar sind. Diese Retusche spielt dann eine gewisse Rolle für die Schätzung des Abstandes der Sonne von der Rotationsachse und auch für die Schätzung der mittleren Sternmasse. Jeans erhält in dieser Weise zuletzt

$$R = 700 \text{ Parsec}, M = 2.4 \text{ Sonnenmassen},$$

in offenbarer Übereinstimmung mit KAPTEYNS Werten.

Sehr interessant ist Jeans' Anwendung der Methode auf Charliers System der Heliumsterne. Er zeigt hier, daß die beobachtete Verteilung der Heliumsterne im Raume als notwendige Bedingung sehr kleine Geschwindigkeiten dieser Sterne voraussetzt. Die theoretischen Geschwindigkeiten Z und II im Zentrum sind von der Größenordnung 4 km/sec und die Sternströmung für eine Distanz von 90 Parsec (die Entfernung der Sonne) vom Zentrum ist nur 2,2 km/sec.

Es ist aber klar, daß die Ansichten von Charlier und von Kapteyn und Jeans, wenn auch miteinander verwandt, doch nicht zusammenfallen. Die oben geforderte Distanz von 700 Parsec vom Zentrum ist nicht mit dem Abstande des Zentrums im System der Heliumsterne vereinbar. Jeans nimmt daher an, daß Charliers System der B-Sterne den Charakter eines "moving cluster" hat.

Man kann aber wohl die Frage stellen, ob wirklich dem Kaptreynschen typischen System eine dynamische Realität zukommt. Die Zeugnisse der letzten Zeit deuten auf sehr erhebliche Abweichungen von der Rotationssymmetrie um die Sonne, die es sehr fraglich erscheinen lassen, ob dem typischen System eine wirkliche Annäherung an die wahre Sternverteilung im Raume zuzuschreiben ist. Besonders aber sind wir auf dem Gebiete der Sterngeschwindigkeiten auf neue Phänomene gekommen, die innerhalb des typischen Systems nicht genügend Raum finden. Man kann sich jetzt fragen, ob es möglich sei, die genannten Züge der Sternverteilung im Raume und der Geschwindigkeitsverteilung in irgendeine Theorie zusammenzufassen, die aber auch den vorher besprochenen empirischen Resultaten Genüge leistet.

29. Einheitliche Theorie des Milchstraßensystems. Wir haben schon vorher (Ziff. 26) hervorgehoben, daß die große Abplattung des Milchstraßengebildes als Ganzes wahrscheinlich auf eine Rotationsbewegung des großen Systems zurückgeführt werden kann. In der Theorie des typischen Systems wird aber die Abplattung des Systems nicht als Folge einer einheitlichen Rotationsbewegung, sondern durch eine in beiden Richtungen um das Zentrum herum vor sich gehende Bewegung oder Strömung erklärt. Da aber das typische Sternsystem offenbar nicht die ganze Struktur des Sternsystems darstellen kann, so könnte man sich einen Kompromiß derart denken, daß das typische Sternsystem wesentlich die Rolle eines lokalen Systems spielt, während das große System als ein System von Wolken oder lokalen Systemen einheitlich rotiert.

Man kann aber, wie oben gesagt, ernstlich in Frage stellen, ob wirklich dem typischen System irgendeine geschlossene Einheit, wenn auch nur als lokales System, zukommt. Zwei Phänomene, denen auf dieser Grundlage eine genügende Erklärung zu geben aussichtslos erscheint, sind die asymmetrische Verschiebung der Geschwindigkeitsellipsoide verschiedener Sterngruppen mit steigender Streu-

1.54 14. Gas ung der Geschwindigkeiten (Bd. VI, Chap. 1, Ziff. 18) und die unten (Ziff. 30) besprochenen "differentiellen" Rotationseffekte in den mittleren Sternbewegungen. Die Tatsache, daß Gruppen von großer Streuung und großer asymmetrischer Verschiebung des Geschwindigkeitsmittelpunktes, welche offenbar nicht in einem lokalen System gebunden sein können, eine ellipsoidische Verteilung von ungefähr demselben Charakter wie für Gruppen kleinerer Streuung aufweisen, deutet auch an, daß der Grund der ellipsoidischen Verteilung oder der Kapteynschen Sternströmung nicht im lokalen System, sondern in den Eigenschaften des großen Systems selbst zu suchen ist. Von diesen Ausgangspunkten aus haben B. LINDBLAD1 und J. H. Oort2 das Problem behandelt.

Es wird in LINDBLADS Arbeit zunächst einem Zusammenhang zwischen dem Phänomen der Asymmetrie der Geschwindigkeiten, wie sie besonders in G. Ström-BERGS<sup>8</sup> Arbeit hervortritt, und allgemein anerkannten Tatsachen betreffs der räumlichen Verteilung der Materie im Sternsystem nachgeforscht. Wir können hier besonders die folgenden hauptsächlichen Gesichtspunkte in Betracht ziehen.

1. Wenn auch die auffallenden Unterschiede in scheinbarer galaktischer Konzentration zwischen verschiedenen Arten von Objekten gewissermaßen auf verschiedene mittlere Entfernung der Individuen der betreffenden Gruppen zurückgeführt werden können, so ist es doch in vielen Fällen offenbar, daß es für verschiedene Gruppen von Objekten auch eine wirkliche Variation in der "absoluten" räumlichen Konzentration gegen die Milchstraßenebene gibt. So besteht wahrscheinlich eine wirkliche Verschiedenheit in galaktischer Konzentration zwischen den A-Sternen und den Riesensternen von späterem Spektraltypus. Wir können auch extreme Gruppen wie O-Sterne und langperiodische & Cephei-Sterne auf der einen Seite mit planetarischen Nebeln, kurzperiodischen δ Cephei-Sternen, Kugelhaufen auf der anderen Seite einander gegenüberstellen.

2. Es werden diese Verschiedenheiten in der wahren galaktischen Konzentration von einer Variation der inneren Streuung in den Geschwindigkeiten relativ zum Zentroid begleitet und zwar in direktester Weise von dieser Varlation aus erklärt. Zufolge einer größeren allgemeinen Streuung der zentroidalen Geschwindigkeiten wird die Bindung der betreffenden Objekte an die Milchstraßencbene weniger stark, die Amplituden in der Bewegung senkrecht zu dieser Ebene im Durchschnitt größer und die galaktische Konzentration weniger ausgeprägt.

3. Die fundamentale Einstellung zum Problem hängt jetzt wesentlich davon ab, daß wir zur Erklärung des Phänomens der "asymmetrischen Geschwindigkeitsverteilung" die Hypothese einführen, daß die Streuung der Geschwindigkeiten relativ zum Zentroid klein ist gegen die systematische Bewegung des Zentroides selbst relativ zum Schwerpunkt des Systems als Ganzem. Wir werden gleich unten diese systematische Bewegung mit einer allgemeinen Rotationsbewegung identifizieren.

4. Gemäß unsren Resultaten über die allgemeine Verteilung des Milchstraßenlichts (Ziff, 9, 11), über die räumliche Verteilung der Kugelhaufen, der schwachen Sterne (Ziff. 18) und der Objekte hoher absoluter Leuchtkraft (Ziff. 20) suchen wir den Schwerpunkt des Systems in der Sagittariusgegond,

etwa in den galaktischen Längen 325°-330°.

5. Wir führen hier weiter die Annahme ein, daß das System sich wenigstens in groben Zügen in einen dynamisch stationären Zustand angeordnet hat. Eine

<sup>&</sup>lt;sup>1</sup> Ark Mat Astr Fys 19A, Nr. 21, 27 u. 35; 19B, Nr. 7; 20A, Nr. 17; 21A, Nr. 3 u. 15 (1925-1929); A N 236, S. 481 (1929); M N 87, S. 553 (1927); 90, S. 503 (1930); Upsala Medd 3, 4, 6, 13, 24, 26, Stockholm Medd 1, 2, 4, 5.

<sup>2</sup> BAN 3, S. 275 (1927); 4, S. 79 und S. 91 (1927); 4, S. 269 (1928).

<sup>3</sup> Mt Wilson Contr 275 → Ap J 59, S. 228 (1924); Mt Wilson Contr 293 → Ap J 61,

S. 363 (1925).

ziemlich weitgehende Mischung der Materie von verschiedenen Bahnkom im System wird in der Tat schon nach wenigen Umläufen in der Rote bewegung erfolgen, und wir müssen von vornherein nicht mehr in den ]

des stationären Zustandes hincinlegen (vgl. Ziff. 27).

6. Um hier noch einen Schritt weiter tun zu können, ziehen wir zue eine Erfahrungstatsache den Umstand heran, daß für die Objektgruppe kleinster Streuung in den Geschwindigkeiten (z. B. die Gruppen der langpschen  $\delta$  Cephei-Sterne) wir in der galaktischen Ebene wenigstens keine ill auffallenden systematischen Veränderungen in der räumlichen Dichteverte und auch nicht in der Geschwindigkeitsstreuung, beobachtet haben, wenn hier oftmals die beobachteten Objekte wegen ihrer großen absoluten Leuch innerhalb eines ziemlich weiten Kreises um uns herum gestreut vorkor Wenn wir dann auf das System als Ganzes eine Theorie analog derjenige vorigen Ziffer, Gleichungen (19) bis (22), anwenden und die entsprech Bezeichnungen einführen (die Richtung gegen den Schwerpunkt aber  $\xi$  den obigen Auseinandersetzungen in einer anderen Himmelsgegend anneh so folgt für eine solche Gruppe aus der Kleinheit von  $\widehat{H}^{\mathfrak{s}}$  und  $\partial \widehat{H}^{\mathfrak{s}}/\partial R$  (vgl. Zi und aus der Endlichkeit von  $\partial r/\partial R$ 

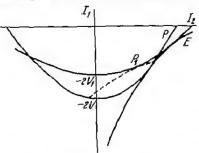


Abb. 24. Diagramm zur Erklärung der Eigenschaften einer Frequenzfunktion  $f(I_1, I_2)$ .

$$\frac{\partial p}{\partial R} = 0,$$

und demnach aus der zweiten Gleichung wenn wir p an der Seite von q ver lässigen,

 $\frac{q}{r} = -R \frac{\partial V}{\partial R}$ 

oder  $\overline{\Theta^{\underline{p}}} = -R \frac{\partial V}{\partial R}$ .

Wir können hier  $\overline{\Theta}^2$  mit  $\Theta_0^3$  vertauscher  $\Theta_0$  die mittlere Geschwindigkeit in der g tischen Ebene senkrecht zur Richtung  $\xi$  den Schwerpunkt des Systems bezeic

Dies zeigt uns, daß  $\Theta_0$  mit der Geschwindigkeit der zirkularen Beweg um den Schwerpunkt herum identisch ist. Mit verschwindender Streuung Bewegungen innerhalb einer Gruppe von Objekten geht also die Bewegungt in eine Kreisbewegung um den Schwerpunkt herum über, während glzeitig die galaktische Konzentration der betreffenden Objekte außerordlich stark ausgeprägt wird. Für diesen Satz werden wir unten (Ziff. 31 Anschluß an eine Diskussion des interstellaren Kalziums eine wichtige Stinden.

Wir wenden uns aber zunächst zur unmittelbaren theoretischen Bedcu und Begründung des Satzes. Wenn wir einen stationären Zustand ge Poincarés Theorem annehmen wollen, so scheint zwar die einzige Möglich der zuerst von Jeans und Charlier angegebene Spezialfall zu sein, wo die quenzfunktion von den zwei Integralen, Energieintegral und Flächeninte abhängt, was eine rotationssymmetrische Anordnung des Systems im Ra einschließt (Ziff, 27). Wir haben dann für die Frequenzfunktion einen Ausd

wo 
$$I_1 = II^2 + \Theta^2 + Z^2 - 2V$$
,  $I_2 = R\Theta$ .

R ist wie vorher die Projektion des Radiusvektors vom Schwerpunkt auf Milchstraßenebene, H die entsprechende Geschwindigkeit,  $\Theta$  die Geschwindigkeit,

in der galaktischen Ebene senkrecht zu R, Z die Geschwindigkeit senkrecht zur galaktischen Ebene. V ist das Gravitationspotential. — Wir können jetzt die Funktion  $f(I_1, I_2)$  in der Weise studieren, daß wir in ein Diagramm (Abb 24)  $I_2$  als Abszisse und  $I_1$  als Ordinate eintragen und das Flächenelement  $dI_1 dI_2$  das sechsdumensionale Element  $RdRd\theta dId\theta dZ$  formal repräsentieren lassen.

Die Grenzgeschwindigkeit im stationären Zustande an irgendemem Punkte

des Systems wird durch die Bedingung

$$I_1 < 0 \tag{30}$$

ausgedrückt Man muß nämlich erwarten, daß ein Stern mit größerer Geschwindigkeit in seiner weiteren Bahn definitiv aus dem System entweicht. Wir können also eine endliche Frequenz / nur unterhalb der Achso  $I_1=0$  habon. Eine weitere Grenzlinie im Diagramm ergibt sich aus der selbstverständlichen Bedingung

 $I_1^* \le R^*(I_1 + 2V)$ , (31)

welche für einen Punkt R, s im System gilt. Die Parabellinie  $I_s^* = R^*(I_1 + 2V)$  nonnen wir die charakteristische Parabel des betreffenden Punktes. Auf dieser Parabel ist offenbar

$$II = Z = 0$$

Da für ein und denselben Radius R das Potential V mit der Entfernung s von der galaktischen Symmetrieebene abnehmen muß, wir also für einen gegebenen Wert von V umgekehrt  $R = \max$  für s = 0 haben, so entspricht die Linie s = 0 auf der Potentialfläche  $V = \max$  dinem maximalen Parameter  $\frac{1}{4}R^3$  der charaktonstischen Parabel mit beibehaltenem Vertexpunkt  $(I_1 = 0, I_1 = -2V)$  im Diagramm Das Gebiet des Diagramms, welches für das System als Ganzes in Frage kommen kann, wird also von der Enveloppe (E) der charakteristischen Parabel für Punkte in der galaktischen Ebene (s = 0) begrenzt. Wie man sich leicht überzeugt, wird diese Enveloppe durch die Relation

$$I_{\bullet}^{\bullet} = -R^{\bullet} \frac{\partial V}{\partial R} \tag{32}$$

charakterisiert, woraus folgt

$$G^{a} = -R \frac{\partial V}{\partial R}$$

Da außerdem H=Z=0, so bedeutet diese Bewegung eine zirkulare Bewegung um das Zentrum herum. Umgekehrt bedeutet also eine Konzentration gegen zirkulare Bewegungen in der galaktischen Ebene eine Konzentration der Frequenz f gegen die betrachtete Grenzlinie E im Diagramm. Da wir aber eine allgemeine Rotationsbewegung nur in einer Richtung voraussetzen, wird nur der eine von den zwei Enveloppenzweigen von Bedeutung

Die Sache liegt demnach so, daß wir für einen gegebenen Punkt (R, s) im System mögliche Kombinationen von  $I_1$  und  $I_2$  im Diagramm nur zwischen der Achse  $I_1 = 0$  und der dem Punkt entsprechenden charakteristischen Parabel haben, während für das System als Ganzes das in Frage kommende Gebiet zwischen der Achse  $I_1 = 0$  und der Enveloppe (E), welche zirkularen Bewegungen

in der galaktischen Ebene entspricht, liegt

Die individuellen Partikeln, deren  $I_1$ ,  $I_2$ -Punkte im Diagramm innerhalb einer gewissen charakteristischen Parabel liegen, können wir aber als Partikeln die in dem betreffenden Punkte (R, s) des Systems gegeneinander stoßen, betrachten. Mit dem Begriff "Stoß" meinen wir dann natürlich eine nahe Passage von zwei oder mehreren Partikeln in ihren Bahnen. Es ist unzweifelhaft, daß

in diesem Vorgang wenigstens eine Tendenz zu einer Gleichverteilung der Ernergie der Partikeln vorhanden sein muß. Wenn wir nur das Gebiet einer und derselben charakteristischen Parabel in Betracht zichen, so würden wir, wenn die Masse einer Partikel mit m und die Geschwindigkeitsdispersion für Partikeln der Masse imit  $\sigma$  bezeichnet wird, eine Frequenzfunktion

$$I = C e^{-\frac{m}{2\sigma^2}(I_1 - 2\sigma I_1)} \tag{33}$$

erwarten.  $\omega$  ist die mittlere Winkelgeschwindigkeit der Rotationsbewegung. Die Linien konstanter Frequenz in dem  $I_1$ ,  $I_2$ -Diagramm wären somit gerade Linien mit einem Winkelkoeffizienten gleich  $2\omega$ . Wenn wir aber in Betracht ziehen, daß alle Punkte des betrachteten Gebietes im Diagramm, außer den Punkten auf der Enveloppe (E) selbst, gleichzeitig verschiedenen charakteristischen Parabeln angehören, so müssen wir doch für die Frequenzlinien Kurven von allgemeinerer Natur voraussetzen. Der Prozeß der Gleichverteilung ist so langsam, daß wir eine vollkommene Ausgleichung als einen niemals erreichten Grenzfall betrachten können.

Es ist durchaus möglich, daß in der Nähe der Enveloppe die für eine kurze Strecke als die Geraden

$$I_1 - 2\omega I_2 = \text{konst.} \tag{34}$$

angenommenen Frequenzlinien mit der Tangente der charakteristischen Parabel in ihrem Kontaktpunkte mit der Enveloppe (E) parallel werden. Dies bedeutet, daß die mittlere Winkelgeschwindigkeit  $\omega$  mit der Winkelgeschwindigkeit der zirkularen Bahn identisch wird. In diesem Falle werden wir eine starke Konzentration gegen die Enveloppe (E) im Diagramm und, räumlich interpretiert, gegen die zirkularen Bewegungen in der Ebene zu erwarten haben. Es ist bemerkenswert, daß (34) das Jacobische Integral für die Bewegung um eine lokale Kondensation, welche einer zirkularen Bewegung mit der Winkelgeschwindigkeit  $\omega$  folgt, darstellt. Es ist in der Tat möglich, daß in dem allgemeinen Ausgleichungsprozeß auch höhere Einheiten als einzelne Sterne, d. h. mehr oder weniger lockere Anhäufungen von Sternen, mitspielen, was besonders für die Ausgleichung der Frequenz nahe der Enveloppe von Bedeutung sein wird, da die Sterne sich hier mit kleinen relativen Geschwindigkeiten bewegen.

Nach den obigen Auseinandersetzungen ist also die charakteristische Verteilung der Geschwindigkeiten in unserem Punkte des Systems wie auch die räumliche Konzentration gegen eine gewisse Ebene (Milchstraßenphänomen) durch eine Konzentration gegen die Enveloppe der charakteristischen Parabel und gleichzeitig durch eine gegen  $I_1 = 0$  kontinuierlich gegen

Null abnehmende Frequenz bedingt.

HALM¹, CHARLIER² und SEARES® haben die Gleichverteilung der Energie für Sterne verschiedener Massen in unserer näheren Umgebung diskutiert. Zweifellos ist in den Geschwindigkeiten relativ zum Zentroid eine deutliche Tendenz zu einer Gleichverteilung vorhanden. Es ist aber offenbar, wenn wir das System als Ganzes betrachten, daß wichtige Ausnahmen verzeichnet werden müssen. Eine Erklärung dieser Verhältnisse muß offenbar eng mit einer Kosmogonie des Systems zusammenhängen.

Wir haben oben stillschweigend vorausgesetzt, daß ein stationärer Zustand mit einer Frequenzfunktion vom Typus  $f(I_1, I_2)$  wirklich existiert, d.h. daß man mit einer solchen Funktion der Poissonschen Gleichung Genüge leisten kann (vgl. Ziff. 27). Die Existenz des stationären Zustandes für spezielle ana-

M N 71, S. 610 (1911).
 Lund Medd Nr. 76 und 81 (1917).
 Mt Wilson Contr 226 - Ap J 55, S. 165 (1922).

lytisch definierte Funktionen  $I(I_1,I_2)$  wird in den oben zitierten Arbeiten von Ohlsson und Wigner behandelt. Wir können aber hier besonders auf die Existonz des Grenzfalles hinweisen, wo eine endliche Frequenz I nur an der Enveloppe I im  $I_1,I_2$  Diagramm vorhanden ist, was offenbar bedeutet, daß die Materie des Systems in zirkularen Bahnen in der Ebene um den Schwerpunkt schwingt, in Analogie mit den Bewegungen im Sonnensystem. Nach der hier behandelten Theorie wird das System, als Ganzes betrachtet, sich nicht sehr viel von diesem Zustand unterscheiden, und es scheint offenbar, daß auch in der Nähe vom "Sonnensystemtypus" Lösungen existeren mitsen

Die "Druckgloichungen" (21), deren zwei letzte Terme auf der linken Seite wir gewissermaßen als "Viskositätsterme" bezeichnen können, sand, wie schon obon in Ziff, 28 bemorkt worden ist, bei der hier angenommenen Frequenzfunktion  $f(I_1, I_2)$  von solbst critilit. Wenn wir den Effekt der nahen Passagen in Botracht zichen, würde zwar die lange freie Weglänge einer Partikel außerdem elnen großen Viskositätskooffizienten, nach abstrakter Analogie mit der Gastheorie gerechnet, herbeiffihren. Die unmittelbare Analogie mit den Gasen versagt aber offenbar, da der Weg eines Sterns zwischen den Stößen gar nicht als geradlinig vorauszusetzen ist, sondern die ganze gekrümmte Bahnbewegung einer Partikel im System innerhalb der freien Weglänge fällt (vgl. Ziff, 27) Wenn wir im System cine geschlossene Rotationsfläche mit dem Schwerpunkt als Mittelpunkt betrachten, so worden die Sterne, die etwa in einem gewissen Augenblicke über diese Fläche nach außen ziehen, im allgemeinen zwischen zwei Passagen in ihrer Bahnbewegung mohrmals über diese Plache hin und her ziehen Der Bereich um die Flüche herum, innerhalb der die betrachteten Sterne einen Austausch von Moment vormitteln können, wird im allgemeinen wegen der Bahnbewegung ziemlich eng begrenzt. Der wirkliche Transport von Moment über die Fläche infolge der l'assagen wird daher sehr langsam.

Es soil außerdem hier betont werden, daß es durchaus nicht notwendig ist, einen stationären Zustand in dem vollen abstrakten Sinne dieses Wortes anzunehmen. Was vorausgesetzt wird, ist, daß eine ziemlich vollständige Mischung der Materie des Systems, wie in Ziff. 27 auseinandergesetzt, stattgefunden hat. Es kann verkommen, daß gewisse Eigenschaften eines stationären Systems nur so laugsam eintreten, daß sie in der tatsächlichen Entwicklung des Systems noch nicht erreicht worden sind. Da das System offenbar gegen eine Symmetriesbene sehr abgeplattet ist, und die Bewegung in der Nähe dieser Ebene von nahe zweidimensionaler Natur ist, so besteht z. B. eine sehr schwache statistische Verbindung zwischen der Bewegung parallel zur Ebene und der Bewegung senkrecht dazu. Da die Kraftkomponente in der s-Richtung sich nur langsam mit R ändarn wird, so können wir in der Tat die Abhängigkeit der vertikalen Kraftkomponente von s als eine konstante Funktion längs der ganzen Bahn eines Sterns anschen, wedurch die Bewegung in s unabhängig von der Bewegung parallel zur galaktischen Ebene wird. Um diesen Verhältnissen Rechnung zu tragen, schreiben

wir das Energiointegral

$$I_1 = \Pi^0 + \Theta^0 + Z_0^0 - 2V_0(R), \quad Z_0^0 = Z^0 - 2(V(R, s) - V_0(R)), \quad (35)$$

wo  $V_0$  die in der Ebene herrschende Potentialfunktion ist,  $Z_0$  der Z-Wert für n=0, und wo vorausgesetzt wird, daß die Differenz  $V(R,s)-V_0(R)$  sich nur langsam mit R ändert. Diese Differenz kann gewissermaßen als ein Mittel für die Potentialdifferenzen zwischen den Höhen s und 0 in verschiedenen, alch in der Höhe s mit demselben Wert von Z kreuzenden Bahnen betrachtet werden,  $Z_0$  wird dann als eine Konstante in der Bewegung eines einzelnen Sterns vorausgesetzt. In der unmittelbaren Umgebung der galaktischen Ebene haben wir

 $A_0^{\prime\prime}$ 

dann nach (28) für jedes Intervall  $dZ_0$  die zweidimensionale Verteilung

$$dZ_0 \cdot \varphi_0(R, \Pi, \Theta, Z_0) R dR dz d\Pi d\Theta,$$

$$\varphi_0(R, \Pi, \Theta, Z_0) = f(I_1, I_0). \tag{36}$$

wo  $\varphi_0(R,\Pi,\Theta,Z_0)=f(I_1,I_2)\,, \tag{36}$  und wo  $I_1$  gemäß (35) ausgedrückt wird. Eine allgemeinere stationäre Verteilung

und wo $I_1$  gemäß (35) ausgedrückt wird. Eine allgemeinere stationäre Verteilung für beliebige Entfernung s von der galaktischen Ebene können wir dann folgendermaßen definieren

 $\varphi(R, z, \Pi, \Theta, Z) R dR dz d\Pi d\Theta dZ = \varphi_0(R, \Pi, \Theta, Z_0) R dR dz d\Pi d\Theta \cdot F(Z_0^2) dZ_0$ 

wo  $F(Z_0^2)$  eine a priori unbekannte, beliebige Funktion ist. Wir haben auf der rechten Seite  $dZ_0$  durch dZ ersetzt, weil in der Bewegung dz dZ invariant ist. Es ergibt sich also

 $\varphi = \varphi_0 \cdot F(Z_0^3) , \qquad (37)$ 

wo der Ausdruck für  $Z_0$  gemäß (35) eingesetzt wird. Für z=0,  $Z=Z_0=0$ , ist  $\varphi=\varphi_0$ , also gilt F(0)=1.

Was sonst die Funktion F angeht, so ist es jedenfalls sehr wahrscheinlich, daß für jeden Wert von R die Streuungen in den Komponenten H und Z in enger Beziehung zueinander stehen. Es ist aber nicht notwendig, daß sie gleich sind, wie man unter strenger Rechnung nach (28) fordern müßte. In unserer Umgebung gilt, daß  $\overline{Z^2}$  etwas kleiner als  $\overline{H^2}$  ausfällt. Wenn wir im folgenden der Einfachheit wegen mit (28) rechnen, setzen wir voraus, daß für Fragen, die mit der Verteilung senkrecht zur Milchstraßenebene von Bedeutung sind, eine Transformation zu machen ist, wobei die allgemeinere Verteilungsfunktion  $\varphi$  gemäß (37) zu bilden ist.  $F(Z_0^2)$  ist gemäß dem empirisch ermittelten Geschwindigkeitskörper zu wählen, unter Beachtung der Relation (38).

30. Die asymmetrische Geschwindigkeitsverteilung in ihrer Beziehung zur Rotation. Wir wollen eine gewisse Klasse von Objekten ins Auge fassen und im

1, I2-Diagramm (Abb. 24) eine Linie konstanter Frequenz

$$I(I_1, I_2) = \text{konst.},$$

lir diese Klasse ziehen. Der innerhalb einer charakteristischen Parabel eineschlossene Teil der Frequenzlinie entspricht einer geschlossenen Fläche im Feschwindigkeitsraume. Nehmen wir an, daß die Frequenzlinie (gestrichelte inie in der Abbildung) durch eine Parabellinie

$$I_1 + \frac{1}{2p}(I_2 - M)^2 = N \tag{39}$$

pproximiert werden kann, wo M, N,  $\phi$  zur Verfügung stehende Konstanten nd. Die Differenz  $\Delta I_1$  in den Ordinaten zwischen einem Punkte auf der Freuenzlinie und der charakteristischen Parabel

$$I_2^2 = R^2(I_1 + 2V) \tag{40}$$

t gleich  $H^2 + Z^2$ , da auf der letzteren Kurve H = Z = 0 ist, während die tangenelle Geschwindigkeitskomponente durch die Relation  $\Theta = \frac{1}{R} I_2$  gegeben ist. an findet dann nach einigen einfachen Reduktionen für die Geschwindigkeitsiche, welche der Frequenzlinie (39) entspricht, folgenden Ausdruck:

$$\frac{II^3 + Z^3}{a^3} + \frac{(\Theta - \Theta_0)^3}{b^2} = 1, \tag{41}$$

$$\Theta_0 = \frac{MR}{R^4 + 2p}, \quad a^2 = 2V + N - \frac{M^2}{R^4 + 2p}, \quad \frac{b^2}{a^4} = \frac{2p}{R^4 + 2p}$$
 (42)

Die Geschwindigkeitafläche ist also für p > 0 ein in der  $\theta$ -Richtung abgeplattetes Sphäroid Bezeichnen wir mit  $\alpha$  und  $\beta$  die Halbachsen des sog Geschwindigkeitsellipsoids für einen gegebenen Ort, so haben wir also gemäß der obigen Approximation (39)

$$t = t_0 \theta^{-\frac{1}{2} \left( \frac{H^0 + Z^0}{a^2} + \frac{(\theta - \theta_0)^2}{\beta^2} \right)} \tag{43}$$

wo

$$\alpha^2 = \frac{\sigma^4}{m}, \quad \frac{\beta^4}{\alpha^4} = \frac{2b}{R^4 + 2b}. \tag{44}$$

Soweit eine ellipsoidische Approximation gilt, ist also  $\alpha$  konstant für verschiedene Punkte des Systems, während  $\beta$  mit R (aber nicht mit s) variiert Da offenbar  $\alpha^{\bullet} = \overline{H}^{\bullet}$ , so kann man also auf Grundlage der Theorie eines stationären Zustandes wenigstens keine schneile Variation von  $\overline{H}^{\bullet}$  mit der Lage (R,s) des betrachteten Punktes im System voraussetzen. Dies ist in Übereinstimmung mit unserer oben für die Sterne mit kleinem  $\overline{H}^{\bullet}$  getroffenen Annahme der Kleinheit von  $\partial \overline{H}^{\bullet}/\partial R$ .

Die beobachtete Asymmetrie der Geschwindigkeitsverteilung müssen wir von unserem Standpunkte aus als eine Variation der mittleren Rotationsgeschwindigkeit  $\Theta_0$  mit der Streuung der individuellen Geschwindigkeiten deuten. Die Richtung der asymmetrischen Verschiebung der Geschwindigkeitsmittelpunkte soll dann offenbar senkrecht zur Richtung gegen das Zentrum des Systems stehen. Nach Strömbergs Arbeit über die Asymmetrie ist dies auch sehr nahe erfüllt. Wir erhalten nach seinen Resultaten für die galaktische Länge des Zentrums 331°,5 ± 5°, was sehr wohl mit Shapleys aus der Verteilung der Kugelhaufen hargeleitetem Wert 327° übereinstimmt

Wir wollen jetzt eine gewisse Klasse von Sternen auswählen, die wir auch mit dem Wort "Untersystem" kennzeichnen können. Wir führen für ein solches Untersystem den Begriff "effektive Grenzfläche" ein, deren Radius in der galaktischen Ebene wir mit  $R_1$  bezeichnen. Wir definieren die "effektive" Begrenzungsfläche siemlich willkürlich derart, daß an dieser Fläche der Frequenziaktor /. der Gleichung (43) im Verhältnis 1/o, mit dem Werte an unserem Orte im Raume verglichen, abgenommen haben soll Die Bedeutung des eingeführten Begriffs folgt aus der folgenden Überlegung Betrachten wir im Geschwindigkeitsraume unseres Ortes eine ellipsoldische Schale (42), wo  $a^3=2\alpha^4$ ,  $b^3=2\beta^3$  An dieser Schale wird offenbar gemäß (43) die Frequenz 1/0 herrschen Die Geschwindigkeiteschale entspricht einer gewissen Frequenzlinie im  $I_1$ ,  $I_2$ -Diagramm, und es 1st klar, daß wir einen neuen Ort  $(R_1,0)$  so wählen können, daß die charakteristische Parabel für diesen Punkt die genannte Frequenzlinie tangiert Wir haben dann für diesen Ort eine Frequenz  $\frac{1}{a} f_{\bullet}$  für  $\Pi = Z = \Theta - \Theta_{\bullet} = 0$ . Der Wert von  $a^2$  für  $R = R_1$  muß daher verschwinden Wir haben also gemäß (42) zu setzen, den zwei betrachteten Ortern im System entsprechend,

$$2\alpha^{3} = 2V + N - \frac{M^{3}}{R^{3} + 2p},$$

$$0 = 2V_{1} + N - \frac{M^{3}}{R^{3}_{1} + 2p}.$$
(45)

Wenn wir aus diesen Relationen und den Gleichungen (42, 44) die Parameter M, N und p eliminieren, bekommen wir

$$\Theta_0^3 + 2\alpha^2 \left( \frac{R_1^4}{R_1^2 - R^2} - \frac{\beta^2}{\alpha^2} \right) = 2(V - V_1) \left( \frac{R_1^3}{R_1^2 - R^2} - \frac{\beta^2}{\alpha^2} \right). \tag{46}$$

Für  $\beta/\alpha$  ist nahe 0,7 zu setzen. Wenn wir aber annehmen, daß  $R_1 - R$  klein gegenüber R selbst ist, die Sonne also sehr exzentrisch im System liegt, so vereinfacht sich diese Gleichung mit sehr guter Approximation auf die folgende:

$$\Theta_0^2 + \alpha^2 \frac{R_1}{R_1 - R} = -R \frac{\partial V}{\partial R}. \tag{47}$$

Wir können jetzt auch, wenn wir verschiedene Untersysteme betrachten, annehmen, daß  $R_1-R$  nicht gleichzeitig mit  $\alpha$  verschwindet, und dies ist damit gleichbedeutend, daß mit verschwindender Streuung  $\alpha$  die mittlere tangentiale Bewegung  $\Theta_0$  einer Gruppe sich der zirkularen Bewegung  $\Theta_0$  um das Zentrum herum nähert. Wir haben somit  $\Theta_0=\max_{\alpha}=\Theta_0$  für  $\alpha=0$ , und demnach

$$(\Theta_0)_{\text{max}}^{\text{s}} = \Theta_{0,}^{\text{s}} = -R \frac{\partial V}{\partial R}.$$
 (48)

Die asymmetrische Geschwindigkeitsverschiebung wird als

$$S = \Theta_{o} - \Theta_{0} \tag{49}$$

definiert. Wir haben jetzt dieses Verschiebungsgesetz mit der von Strömberg¹ durch ein Studium der Radialgeschwindigkeiten hergeleiteten Relation zwischen Geschwindigkeitsstreuung und "asymmetrical drift" zu vergleichen. Strömberg leitet eine parabolische Relation ab, die aber auch eine langgestreckte elliptische sein kann, der Gleichung (46) entsprechend, wenn wir in diese  $R_1 =$  konst. einsetzen.

Wenn wir annehmen, daß das Untersystem der Kugelsternhausen im Mittel keine merkliche Rotationsbewegung besitzt, können wir eine rohe Abschätzung von  $\Theta_{\bullet}$  machen. Nach Lundmarks und Strömbergs Resultaten für die Sonnengeschwindigkeit in bezug auf die Hausen ergibt sich  $\Theta_{\bullet}$  zu rund 300 km/sec. Wir nehmen hier nach Strömberg (vgl. Tabelle 20, Kugelhausen)  $\Theta_{\bullet} = 275 \text{ km/sec}$ 

Tabelle 20.

Klasse	Н	os	S	$\frac{R_1-R}{R_1}$	Klasse	Н	α	S	$\frac{R_1-R}{R_1}$
M0-M9 K4-K9 " G9-K3	$ \begin{array}{l} -1,9 \text{ bis } + 3,0 \\ \leq -2,0 \\ -1,9 \text{ bis } +3,0 \\ \geq +3,1 \\ \leq -3,0 \\ -2,9 \text{ bis } -2,0 \\ -1,9 ,, -1,0 \\ -0,9 ,, 0,0 \\ +0,1 ,, +1,0 \end{array} $	20,4 29,6 52,2 16,7 19,6 23,2 26,0	+14,6 + 7,4 +15,5 + 3,7 + 6,7 + 1,9	0,33 0,19 0,10 0,11 (1,35) 0,08 0,37 0,39 0,12	F0-F9  " " " " " " " " " " " " " " " " " "			+ 5,4 + 7,2 + 1,7 + 6,8 + 95,0 + 0,9 + 8,5 + 9,4	0,13 0,15 (0,90) 0,63 0,34 0,54 (0,01)
Go-G8	$ \begin{vmatrix} +1,1 & + 3.0 \\ +3,1 & + 12.0 \end{vmatrix} $ $ \leq -2,0 $ $ -1,9 \text{ bis } + 1,0 $ $ +1,1 & + 5,0 $ $ +5,1 & + 10,0 $	41,9	+25,2 +14,5 + 3,4 + 6,9 + 9,7 +21,2	0,13 0,15 0,17 0,18 0,37	Per. < 0,7 d. 05-09 c-Sterne P M1e-M6e M2e-M5e Kugelhaufen		74 19,6 12,9 64,7 52 88 117	+ 97 + 23,5 + 9,4 + 15,6 + 50,5 +151 +275	0,12 0,03 0,33 0,50 0,11 0,13 0,18

<sup>&</sup>lt;sup>1</sup> L. c. <sup>2</sup> Publ ASP 35, S. 318 (1923).

Mt Wilson Contr 292 = Ap J 61, S. 353 (1925).

an. Die Entfernung der Sonne von der effektiven Grenze des Systems, wenn wir als Einheit den Radius selbst nehmen, berechnen wir aus

$$\frac{R_1 - R}{R_1} = \frac{\alpha^4}{S(2\theta_4 - S)}. \tag{50}$$

Tabelle 20 gibt  $\alpha$ , S und  $\frac{R_1-R}{R_1}$  für die verschiedenen Gruppen in Strömbergs Arbeit S wird vom "limiting center", d. h. dem Vertex der Parabal, längs deren Achse, gerechnet.  $\alpha$  ist mit der größeren Achse des Geschwindigkeitsellipsoids in der galaktischen Ebene identisch genommen. H ist die Quantität  $m+5\log\mu$ 

Es ist aus der Tabolle ersichtlich, daß die meisten Gruppen eine bemerkenswerte Übereinstimmung zeigen. Wenn wir einige extreme Werte ausschließen (zwei extrem große und die sehr kleinen Werte der frühen B-Sterne), so bekom-

men wir im Mittel für 27 Gruppen

$$\frac{R_1-R}{R_1}=0.23\pm0.03$$
 (m. F.).

Die Sonne ist also um 23 % des Radius innerhalb der "effektiven" Grenze

des Systems, also sohr exzentrisch, gelegen

Für die räumliche Dichtigkeit  $\nu$  eines Untersystems ergibt sich durch Integration von (43)  $\nu=(2\pi)^{3/2}\alpha^2\beta/c$ . Man bekommt dann gemäß (44) und nach der Definition der "effektiven Grenze" für die Dichtigkeit  $\nu_1$  an dieser Grenze

$$\frac{r_1}{r} = \frac{\beta_1}{\beta} \frac{1}{s} ,$$

und welter gamaß (39)

$$\left(\frac{\beta_1}{\beta}\right)^2 = \frac{R^2 + 2p}{R_1^2 + 2p}, \quad \left(\frac{\beta}{\alpha}\right)^2 = \frac{2p}{R^2 + 2p}.$$

Nach Elimination von p ergibt alch

$$\frac{r_1}{r} = \left(\frac{\alpha^4 R^6}{\beta^4 R^6 + (\alpha^5 - \beta^5) R^4}\right)^{\frac{1}{6}} \cdot \frac{1}{a} \,. \tag{51}$$

Numerisch erhält man gemäß den oben für  $\beta/\alpha$  und  $R/R_1$  gegebenen Worten  $\nu_1/\nu = 0.32$ . Die räumliche Dichtigkeit an der "Grenze" ist also 0.32 der Dichtig-

kelt in unserer Umgebung.

Die allgemeine Dichtigkeitsverteilung in der galaktischen Ebene gemäß der ellipsoidischen Approximation ergibt sich aus (43) und dem Diagramm Abb. 24 unter Benutzung einer Methode, welche zu Gleichungen, die mit (45) und (46) analog sind, führt. Wir bezeichnen jetzt mit  $R_0$ ,  $\nu_0$  und  $V_0$  für unseren Punkt im System geltende Werte, und mit R die laufende Koordinate. Wenn die Geschwindigkeitsverteilung an unserem Punkte wie vorher durch  $\Theta_0$ ,  $\alpha$ ,  $\beta$  charakterislert ist, so haben wir für das betreffende Untersystem

$$\log \frac{r}{r_0} = \frac{1}{2} \log \frac{\alpha^3 R_0^3}{\beta^3 R_0^3 + (\alpha^3 - \beta^3) R^3} + \frac{1}{\alpha^4} \left( V - V_0 + \frac{1}{2} \Theta_0^3 \frac{\alpha^3 (R^3 - R_0^3)}{\beta^3 R_0^3 + (\alpha^4 - \beta^3) R^3} \right) \log \sigma. (52)$$

Der erste Term auf der rechten Selte ist klein Wir können mittels dieser Gleichung den Radiusvektor R für beliebige Werte von  $r/r_0$  berechnen, sobald wir in genügender Weise die Kraftfunktion für sukzessive Werte von R, woraus  $V - V_0$  berechnet wird, kennen. Durch Differentiation der Gleichung können wir  $\partial \log r/\partial R$  in Relation zu  $\theta_0$ ,  $\alpha$  und  $\partial V/\partial R$  bringen, woraus, wie wir unten sehen werden, eine alternative, aber im Prinzip mit dem obigen identische Behandlung des Phänomens der Asymmetrie sich ergibt.

Eine Erklärung der approximativen Konstanz von  $R_1$  kann uns eine Betrachtung der Abb. 24 geben. Mit wachsendem R nähert sich die charakteristische Parabel des betrachteten Systempunktes mehr und mehr der  $I_2$ -Achse, um im Limes mit dieser Achse zusammenzufallen. Wenn wir annehmen, daß die Geschwindigkeit der zirkularen Bewegung an unserem Orte nicht sehr weit von der Grenzgeschwindigkeit, welche  $I_1=0$  entspricht, liegt, so ist der Berührungspunkt zwischen der charakteristischen Parabel und der Enveloppe nicht weit von der  $I_2$ -Achse entfernt, und die charakteristische Parabel unseres Ortes verläuft in der Nähe dieser Achse. Da für alle Untersysteme die Frequenz  $I(I_1,I_2)$  gegen die Achse  $I_1=0$  sukzessiv gegen Null abnimmt, so ist es a priori

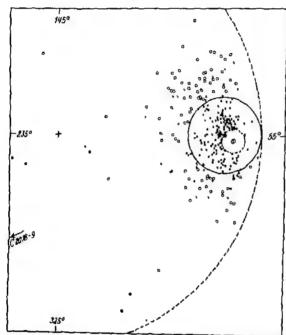


Abb. 25. Die Verteilung in der galaktischen Ebene für große Geschwindigkeiten relativ zur Sonne (nach Oort). Die schwarzen Punkte entsprechen einem homogenen Material für Geschwindigkeitsdifferenzen gegen die Sonne größer als 19,5 km/sec. Der größere (voll gezogene) Kreis entspricht Geschwindigkeiten von 65 km/sec relativ zum Zentroid. Das Kreuz soll die Schwerpunktsgeschwindigkeit des Systems repräsentieren, und der große (unterbrochene) Kreis mit dem Kreuz als Zentrum hat einen Radius von 365 km/sec.

wahrscheinlich, wenigstens für die Gruppen von großer Asymmetrie, daß in der Figur eine einzige charakteristische Parabel, welche approximativdereffektiven Grenze  $R = R_1$  verschiedener Untersysteme entspricht, gezogen werden kann. Die Abnahme der räumlichen Dichtigkeit gegen eine "effektive Grenzfläche", wie auch das ganze Phänomen der Asymmetrie der Geschwindigkeitsverteilung erscheint also als eine Folge der Bedingung, daß die Partikeln des Systems der Relation  $I_1 < 0$ genügen müssen, mit einer kontinuierlichen Abnahme der Frequenz gegen dieso Grenze im  $I_1$ ,  $I_2$ -Diagramm.

Daß die zirkulare Geschwindigkeit an unserem Orte in der Tat nicht sehr weit von der "velocity of escape" entfernt ist, wird angedeutet durch die volkommene Abwesenheit von großen Geschwindigkeiten relativ zum Zentroid in

einer Richtung, welche eine gerade Fortsetzung des Geschwindigkeitsvektors  $\Theta_{\bullet}$  bildet. Dieses Phänomen wird sehr gut durch ein Dlagramm von J. H. OORT<sup>2</sup> veranschaulicht (Abb. 25), wo die absoluten Geschwindigkeiten für Sterne, welche große zentroidale Bewegungen zeigen, innerhalb eines Geschwindigkeitskreises vom Radius 365 km/sec gelegen erscheinen.

Oort hat eine in der Form beträchtlich verschiedene, aber der obigen prinzipiell ähnliche Behandlung des Phänomens der Asymmetrie ausgeführt,

<sup>&</sup>lt;sup>1</sup> Lindblad, VJS 61, S. 265 (1926). <sup>2</sup> BAN 4, S. 269 (1928).

Die Behandlung des stationären Zustandes in der Umgebung der Sonne ist rein analytisch, wobei eine ellipsoidische Verteilung der Geschwindigkeiten für jede Untergruppe vorausgesetzt wird. Obgleich die Oortsche Methode durch diese Annahme im ganzen etwas weniger generell als die oben gegebene wird, ist sie für unsere Umgebung gerechtfertigt, wo wir wissen, daß die ellipsoidische Verteilung als Approximation im ganzen zulässig ist, von welchem Sachverhältnis wir auch oben Gebrauch gemacht haben. Die Gleichung, welche (46) und (47) oben entspricht, ergibt sich aus (52) und schreibt sich nach Oort

$$\Theta_0^2 = -R \frac{\partial V}{\partial R} + \alpha^2 \left( \frac{R}{\nu} \frac{\partial \nu}{\partial R} + 1 - \frac{\beta^2}{\alpha^2} \right), \tag{53}$$

woraus, wenn wir mit Oort  $\Theta_0/R = 0.043$  km/sec Parsec annehmen, für die asymmetrische Drift  $S = \Theta_0 - \Theta_0$  gilt

$$S = -11.6 \,\alpha^2 \left( \frac{1}{\text{Mod.}} \, \frac{\partial \log r}{\partial R} + \frac{1}{R} \left( 1 - \frac{\beta^2}{\alpha^2} \right) \right). \tag{54}$$

Der Gradient  $\partial \log r/\partial R$  ergibt sich als von derselben Größenordnung für verschiedene Gruppen und entspricht etwa einem Faktor 2 in der Dichtigkeit für

eine Distanz von 1000 Parsec. Für die gewöhnlichen Spektraltypen in Ström-BERGS Tabelle ergibt sich im Mittel

 $\partial \log v / \partial R = -0,00019 \pm 0,00005$  (m. F.).

Im vereinfachten Falle einer ebenen Bewegung der Sterne um ein Massenzentrum können wir mit K. F. Bott-LINGER1 die Abhängigkeit der Asymmetrie von der parabolischen Grenzgeschwindigkeit und von der Konzentration der Sterne gegen das Zentrum hin anschaulich machen. Die Bahnen durch unseren Ort im System können, wie Abb. 26 zeigt, nach Exzentrizität & a = 1/2 0 und Halbachsenlänge klassifiziert werden, was offenbar einer Aufteilung nach  $I_1$  und  $I_2$  entspricht, da  $I_1$  die Halbachsenlänge a, und die Flächengeschwindigkeit I2 bei gegebenem a die Exzentrizität e bestimmt. Linic von O nach einem beliebigen Punkt in der Abbildung entspricht einer Geschwindigkeit in bezug auf den Schwerpunkt des Systems, und man kann sogleich die entsprechenden Werte von a und e ablesen. Der Punkt P markiert die Kreisbewegung, S die Sonnenbewegung. Die Asymmetrie der Geschwindigkeitsverteilung, von P oder S aus gerechnet, wird um so größer, je stärker die inneren Bahnen, a < 1, im

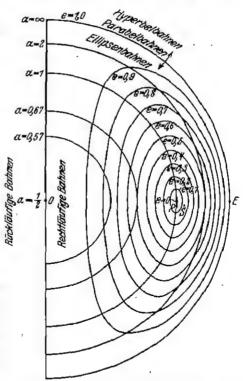


Abb. 26. Geschwindigkeitsstrenung der Bahnen durch einen gewissen Ort des Systems im Falle ebener Bewegung um ein Massenzentrum.

Vergleich mit den äußeren, a > 1, besetzt sind. Von diesem Gesichtspunkte aus

<sup>&</sup>lt;sup>1</sup> Naturwiss 19, S. 297 (1931); Berlin-Babelsberg Veröffentl 8, H. 5 (1931).

wären also die Sterne mit großer asymmetrischer Bewegung solche, die vorzugsweise in den inneren Partien des Systems vorkommen.

Es ist wohlbekannt, daß die Geschwindigkeitsellipsoide in den meisten Fällen nicht sphäroidisch mit der kürzesten Achse in der galaktischen Ebene, sondern beträchtlich gegen die galaktische Ebene abgeplattet gefunden werden. Wie oben (Ziff. 29) erwähnt, hängt dies damit zusammen, daß die Bewegung in der Ebene von zweidimensionaler Natur ist, und daß eine Ausgleichung zwischen dieser Bewegung und der allgemeineren dreidimensionalen nur sehr langsam vor sich geht. Eine starke Korrelation zwischen den Streuungen in  $\Pi$  und Z müssen wir jedenfalls voraussetzen, was auch der empirischen Erfahrung entspricht. Es ist dann aber klar, daß Gruppen von verschiedener Rotationsgeschwindigkeit und verschiedener Streuung, also verschiedene Untersysteme, auch ver-

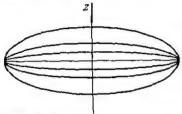


Abb. 27. Schematischer Meridionalschnitt durch das Sternsystem. Die Grenzsiächen repräsentieren verschiedene Untersysteme.

schiedene Konzentration gegen die galaktische Ebene zeigen müssen. Wenn wir einen Meridionalschnitt durch die "effektiven Begrenzungsflächen" ziehen, so bekommen wir also die schematische Darstellung der Untersysteme, welche in Abb. 27 gegeben ist.

Wir können jedenfalls auf die Bewegung in z senkrecht zur Milchstraßenebene das Massenbewegungsgesetz

$$\frac{\partial (\nu \overline{Z^*})}{\partial x} = \nu \frac{\partial V}{\partial x} \tag{55}$$

anwenden. Eine unmittelbare Verwendung kann diese Formel für die A-Sterne erhalten, da diese praktisch in einem so dünnen Stratum enthalten sind, daß wir annehmen können

$$\frac{\partial V}{\partial z} = -4\pi G \varrho z, \tag{56}$$

wo  $\varrho$  die Dichtigkeit des zentralen galaktischen Stratums ist. Wenn  $\nu_0$ ,  $z_0$ ,  $Z_0$  die für die A-Sterne nahe unserem Punkte im System geltenden Werte der Dichtigkeit, Distanz von der Symmetrieebene und Geschwindigkeitsstreuung in Z sind, so haben wir

in Z sind, so haben wir
$$Z_0^2 = -\int_{z_0}^{\infty} \frac{\partial V}{\partial z} dz = 4\pi G \varrho \int_{z_0}^{\infty} \frac{\partial V}{\partial z} z dz. \tag{57}$$

Wir können für  $z_0$  den Wert 30 Parsec annehmen und für  $v/v_0$  z. B. die von Petersson und Lindblad (Ziff. 19) hergeleitete Veränderung der Dichtigkeit mit der Entfernung von der Milchstraßenebene. Für  $Z_0$  hat Strömberg 9,1 km/sec gefunden. Nach Ausführung einer numerischen Integration finden wir dann für  $\varrho$ , in Sonnenmassen per Kubikparsec ausgedrückt, den Wert

$$\rho = 0.11,$$

was mit anderen Schätzungen der Dichtigkeit in unserer Umgebung ziemlich übereinstimmt.

Eine ähnliche Untersuchung hat Bottlinger¹ für die Sterne von großer absoluter Leuchtkraft ausgeführt. Aus dem durchschnittlichen Abstand der hellen Sterne von der Milchstraßenebene (etwa 40 Parsec) läßt sich mit Hilfe der Masse und der Dimensionen des großen Systems (vgl. Ziff. 33) eine Geschwindigkeitsstreuung von 3,6 km/sec berechnen. Eine sorgfältige Diskussion der Radialgeschwindigkeiten ergibt das Resultat, daß die Streuung der O- und

<sup>1</sup> L, c.

B-Sterne im Rahmen dessen liegt, was man nach der Rotationstheorie erwarten muß.

Eine sehr ausführliche Arbeit über diesbezügliche Fragen ist ganz kürzlich von Oort 1 veröffentlicht worden. Wenn wir die senkrecht zur Milchstraßenebene wirkende Kraftkomponente  $\partial V/\partial z$  mit K(z) bezeichnen und diese als im wesentlichen in der Bewegung eines Sterns von R unabhängig betrachten, so haben wir fitr die Bewegung in Z, gemäß dem zweiten Teil unserer Gleichung (35) oben,

 $Z_0^2 = Z^2 - 2 \int_z^z K(z) \, dz \,,$ (58)

und es ist leicht einzuschen, z. B. durch unsere Gleichung (37) oben, daß im Falle einer stationären Verteilungsfunktion  $\varphi(z, Z)$  diese einfach eine Funktion von  $Z_0$ sein wird. Im Falle einer Gaussschen Verteilung der Geschwindigkeiten für z = 0 haben wir

$$\varphi(0, Z) = \nu_0 \frac{l}{\sqrt{\pi}} e^{-PZ\delta}, \tag{59}$$

und also für beliebige z-Werte

$$\varphi(z,Z) = \nu_0 e^{\frac{2P\int_0^z K(z)dz}{L}} \cdot \frac{l}{\sqrt{\pi}} e^{-l^2Z^2}, \tag{60}$$

woraus wir ableiten

$$v(z) = v_0 e^{2v \int_0^z K(s) ds}.$$
 (61)

Diese Formel ist identisch mit der von Kapteyn für einen analogen Zweck benutzten (Ziff. 28). Wenn wir die empirische Geschwindigkeitsverteilung als eine Summe von Gaussschen Verteilungen approximieren, welche je die Bruchteile  $\theta_1, \theta_2, \ldots$ , der Sterne in unserer Nähe umfassen, so bekommen wir

$$\nu(s) = \nu_0 \left\{ \theta_1 s \left( \theta_1 s \right)^{\frac{1}{2}} K(s) ds + \theta_2 s \left( \theta_1 s \right)^{\frac{1}{2}} K(s) ds + \cdots \right\}. \tag{62}$$

Durch die statistisch ermittelten  $\nu(z)$  und gegebene Werte der  $\theta$  und l können wir die Funktion K(z) in sukzessiver Approximation ermitteln.

Oort bestimmt aus den Radialgeschwindigkeiten für verschiedene Sterntypen die Streuung in den vertikalen Geschwindigkeitskomponenten Z, woraus die Werte von I sich ergeben. Hauptsächlich unter Benutzung der van Rhijnschen Resultate für die Dichtefunktion in hohen galaktischen Breiten (für A-Sterne

und Riesensterne von spätem Typus werden auch die oben erwähnten Resultate von LINDBLAD und PETERSSON zum Vergleich herangezogen) berechnet Oort die Funktion K(z) für z zwischen 0 und 600 Parsec. Das Hauptresultat wird in Tabelle 21 wiedergegeben, wo K in cm/scc2 ausgedrückt ist. Der numerische Wert von K(z) wächst linear bis ungefähr in der Höhe von 200 Parsec, der Gang mit z wird dann beträchtlich langsamer. Wenn umgekehrt für die Dichtefunktion der Ausdruck (62) angenommen wird, kann man aus ihm und aus der als bekannt vorausgesetzten Leuchtkraftsfunktion die Sternzahlen für verschiedene scheinbare Größen berechnen, und als Kontrolle werden von Oort weitläufige Rech-

Tabelle 21.					
g	K(s)·10 <sup>2</sup>				
50	-0,77				
100	1,55				
150	2,59				
200	3,52				
250	3,78				
300	3,86				
400	3,68				
600	4,44				

nungen dieser Art ausgeführt. Da eine Berechnung der Sternzahlen der schwächsten Größen Kenntnis von K(z) bis zu etwa 5000 Parsec voraussetzt, so kann

<sup>&</sup>lt;sup>1</sup> B A N 6, S. 249 (1932).

man aus diesen Sternzahlen eine grobe Kontrolle etwaiger Extrapolationen von K(z) für große Höhen bekommen, eine Möglichkeit, die auch von Oort ausgenutzt wird, doch vorläufig ohne definitive Resultate. Den Verlauf der Stornzahlen mit galaktischer Länge nach Seares benutzt Oort, um den Gradienten  $\partial \log r/\partial R$  zu berechnen, welchen Wert er im Mittel zu -0,0003, in gutor Ulwreinstimmung mit dem oben besprochenen Resultat aus der asymmetrischen Drift, berechnet. Ein Schnitt der Dichtigkeitsflächen senkrecht zur Milchstraße in der Richtung  $L = 320^{\circ}$  gibt für hohe galaktische Breiten Kurven, die sehr wohl als Ellipsen mit Zentrum in der Milchstraßenebene in der Entfernung 10000 Parsec angesehen werden können. Die Ellipse, bei der die Dichte des photographischen Lichts 1/95 der entsprechenden Dichte in der Nähe der Sonne ist, hat die Achsen a = 12200, b = 1310, und die Ellipse für die Dichte  $\frac{1}{100}$ die Achsen a = 14300, b = 2240, in Parsec ausgedrückt. Oorr berechnet aus K(z) unter verschiedenen schematischen Annahmen über die Massenverteilung im System die Totaldichte e der Materie in der Umgebung der Sonne. Er findel Werte zwischen 0,079 und 0,108 Sonnenmassen per Kubikparsec, womit offenbar LINDBLADS oben gegebener Wert gut übereinstimmt. KAPTEYN hatte den Wert 0,099 gefunden, Jeans aus der Sternströmungstheorie (Ziff. 28) 0,143. Durch Vergleich mit der wahrscheinlichen Anzahl von Sternen per Volumeneinheit zieht Oort den Schluß, daß Nebel und Meteore zusammen zu der Totalmasse weniger als die Sterne beitragen, möglicherweise sogar viel weniger.

81. Differentielle Rotationseffekte in den beobachteten Geschwindigkeiten. Nach der eben besprochenen Theorie liegt die Richtung der asymmetrischen Verschiebung der Geschwindigkeitsmittelpunkte senkrecht zur Richtung von uns nach dem Zentrum des Systems. Die asymmetrische Verschiebung ist eine differentielle Rotation verschiedener Gruppen von Objekten relativ gegeneinander. Vom Nordpol der Milchstraße gesehen, geht die Rotation in retrograder Richtung.

von links nach rechts.

Es ist aber J. H. Oort¹ gelungen, auf anderem Wege eine Bestimmung der Lage des dynamischen Zentrums zu gewinnen. Die mittleren Geschwindigkeiten  $\Theta_0$  sind überall senkrecht zum Radiusvektor gerichtet, werden ja aber nicht unmittelbar beobachtet. Was in der Beobachtung gemessen wird, ist die vektorielle Differenz zwischen  $\Theta_0$  und der Geschwindigkeit der Sonne. Wir betrachten jetzt Sterne in der galaktischen Ebene in der Entfernung r von uns. Die eben erwähnte vektorielle Differenz zerlegen wir in ihre Komponente längs r, die Radialgeschwindigkeit, und ihre Komponente senkrecht zu r, die transversale Geschwindigkeit. Durch Abziehen der Komponenten der Sonnenbewegung in bezug auf die umgebenden Sterne der betreffenden Klasse bekommen wir Residuen, welche die vektorielle Differenz zwischen den ringsherum im Abstande r geltenden  $\Theta_0$ -Werten und dem  $\Theta_0$ -Wert des Sonnenorts darstellen. Wenn r gegen R klein ist, bekommen wir dann für die Radialgeschwindigkeiten eine Abhängigkeit von der galaktischen Länge der beobachteten Objekte von der Form

$$rA\sin 2(L-L_0), \tag{63}$$

wo  $L_{\mathbf{0}}$  die galaktische Länge des Zentrums ist, und für die transversalen Geschwindigkeiten

$$rA\cos 2(L-L_0)+rB, \tag{64}$$

WO

$$A = \frac{1}{2} \left( \frac{\Theta_0}{R} - \frac{\partial \Theta_0}{\partial R} \right), \quad B = \frac{1}{2} \left( -\frac{\Theta_0}{R} - \frac{\partial \Theta_0}{\partial R} \right). \tag{65}$$

<sup>&</sup>lt;sup>1</sup> BAN 3, S. 275; 4, S. 79 u. S. 91 (1927).

Wir haben also  $B = A - \omega$ , wo  $\omega = \frac{1}{R} \Theta_0$  die Winkelgeschwindigkeit der Rotationsbewegung ist. In dem speziellen Falle, wo  $\Theta_0$  die Geschwindigkeit der zirkularen Bewegung ist, also wenn die Dispersion  $\alpha$  sehr klein ist, haben wir

$$A = \frac{1}{4} \left( \omega + \frac{1}{\omega} \frac{\partial^2 V}{\partial R^2} \right). \tag{66}$$

In Übereinstimmung mit den Ergebnissen aus dem Phänomen der Asymmetrie setzen wir voraus, daß  $\omega$  eine retrograde Bewegung ist, also eine Rotation von links nach rechts, wenn sie von einem Punkte nördlich von der galaktischen Ebene betrachtet wird. Die transversale Geschwindigkeit wird im Sinne wachsender galaktischer Länge gezählt. Für die mittleren Eigenbewegungen in galaktischer Länge bekommen wir, wenn A und B in Kilometern per Sekunde für die Entfernung von einem Parsec und die Eigenbewegungen in Bogensekunden ausgedrückt werden,

$$4.74 \,\mu_L = A\cos 2 \left( L - L_0 \right) + B. \tag{67}$$

Die oben gemachten Ansätze haben viel gemeinsam mit den Gedanken, welche zuerst Gylden in einer Arbeit entwickelte, in der die Sternbewegungen mit den geozentrischen Bewegungen der kleinen Planeten verglichen wurden. GYLDEN entwickelt die mittleren Eigenbewegungen in Rektaszension (a) für verschiedene α innerhalb einer Deklinationszone in eine Fouriersche Reihe, deren einzelne Glieder von den sin und cos für sukzessive Vielfache von a abhängig sind. Als Terme von reeller Bedeutung behandelt er besonders den konstanten Term und die Terme in  $\alpha$  und  $2\alpha$ . Die Terme in  $\alpha$  geben den Reflex der Sonnenbewegung in bezug auf die betrachteten Sterne (sind aber zum Teil auch von galaktischen Rotationseffekten oben beschriebener Art bedingt); für den Apex findet Gylden hieraus  $\alpha = 270^{\circ}$ . Die tibrigen Terme deuten aber nach ihm auf eine allgemeine Umlaufsbewegung der Sterne um ein gemeinsames Zentrum hin. Zwar bekommt Gyldén aus seinem Material, speziell nach einer Korrektion der Präzession von Nyren, einen konstanten Term, der einer direkten Rotationsbewegung entspricht, Aus der qualitativen Übereinstimmung der Koeffizienten der Entwicklung mit denen der geozentrischen Bewegungen der kleinen Planeten am 21. März 1868 zieht er weiter den Schluß, daß das Zentrum des Sternsystems in einer Richtung liegt, deren R.A. mit der R.A. der Sonne in der späteren Hälfte des März zusammenfällt, also in der Himmelsregion zwischen Auriga und Cygnus. Wenn man aber eine retrograde Bewegung voraussetzt, bekommt man aus GYLDENS Koeffizienten für cos 2 a und sin 2a die Werte -1",21 und -0",40 pro 100 Jahre und für das Zentrum zwei um 180° verschiedene alternative Werte, von denen der eine einer galaktischen Länge des Zentrums von 359° entspricht, was in ziemlich guter Übereinstimmung mit unseren jetzigen Ansichten steht.

In besonders interessanter Weise hat S. Oppenheim die Gyldenschen Ideen weiter zu entwickeln gesucht und für die spezielle Klasse der B-Sterne die harmonische Analyse auch auf die Radialgeschwindigkeiten ausgedehnt. Sein Ziel war zuerst, unter Voraussetzung einer Analogie mit den kleinen Planeten, die Bahnebene der Bewegungen zu ermitteln und durch harmonische Analyse der Bewegungen parallel dieser Ebene die Lage des Bewegungszentrums zu finden. Er führt später, im Anschluß an die Bessel-Koboldsche Methode zur Apexbestimmung in Harzers Ausführung, ein "Momentenellipsoid" ein (das

Overs K Vetenskapsakad Förhandl 28, S. 956 (1871).

AN 188, S. 137 (1911); Wien Denkechr Math Nat Kl 87, S. 297 (1912); Astron Kal 1913, S. 126; Wien Denkschr Math Nat Kl 92; AN 201, S. 241 u. 417 (1915); Wien Denkschr Math Nat Kl 93; AN 202, S. 89 (1916); 204, S. 447 (1917); Seeliger-Featschr S. 131 (1924);

von dem Momentenellipsoide in Charlier-Wicksells statistischer Theorie der zentroidalen Bewegungen zu unterscheiden ist) von der Form

$$Ax^{2} + By^{2} + Cz^{2} + 2Dyz + 2Ezx + 2Fxy = 1,$$
 (68)

WO

$$A = \Sigma(ll),$$
  $C = \Sigma(nn),$   $E = \Sigma(nl),$   
 $B = \Sigma(mm),$   $D = \Sigma(mn),$   $F = \Sigma(lm),$   
 $l = \sin i \sin \Omega,$   $m = -\sin i \cos \Omega,$   $n = \cos i.$  (69)

 $\Omega$  und i sind die R.A. des aufsteigenden Knotens und die Neigung des Bewegungskreises eines Sterns. Die größte Achse dieses Ellipsoids soll gegen den Apex der Sonnenbewegung, die mittlere Achse gegen das Zentrum der Bewegung und die kleinste Achse gegen den Pol der Bewegungsebene zeigen. Aus den Eigenbewegungen der Sterne ergeben sich aber zwei Bestimmungen dieses Ellipsoids, da die Werte von  $\Omega$  (nach einer einheitlichen Regel bestimmt) zwei voneinander sehr verschiedene Gruppen andeuten, die auch räumlich voneinander getrennt sind. Nach Vertauschung der zwei kleineren Achsen in dem sekundären Ellipsoid, das sonst keine verständliche Beziehung zur Milchstraßenebene zeigt, werden die Achsenrichtungen jedoch fast identisch und ein Mittel kann gebildet werden. Die Theorie ergibt, auf die Bewegungen der kleinen Planeten und der Kometen angewandt, sehr interessante und zum Teil leicht interpretierbare Resultate.

Für die Sterne des Boss-Kataloges findet Oppenheim als Mittel für die Hauptrichtungen der zwei Ellipsoide in der oben gegebenen Ordnung

$$\alpha_1 = 271^\circ, 5 
\delta_1 = +32^\circ, 3$$
 $\alpha_8 = 31^\circ, 4 
\delta_2 = +38^\circ, 1$ 
 $\alpha_8 = 155^\circ, 1 
\delta_3 = +35^\circ, 2$ 

Die erste Richtung ist in guter Übereinstimmung mit dem allgemein angenommenen Apexwert, die letzte zeigt gegen eine hohe galaktische Breite ( $+60^{\circ}$ ). Die der zweiten Richtung gerade entgegengesetzte am Himmel, die ebensogut die Richtung gegen das Zentrum andeuten kann, entspricht den galaktischen Koordinaten  $L=288^{\circ}$ ,  $B=+21^{\circ}$ , also einem Punkte, der nicht allzu weit von Shapleys Anhäufungspunkt der Kugelhaufen entfernt ist.

Oorr hat in erster Linie die Radialgeschwindigkeiten für Objekte von großer Entfernung in niedrigen galaktischen Breiten untersucht, um die Existenz des Rotationstermes (63) nachzuweisen. Es stellte sich bei dieser Untersuchung heraus, daß entfernte Objekte von verschiedener physikalischer Natur im ganzen miteinander wohl übereinstimmende Werte von  $L_0$  und A ergaben. Für die

Tabelle 22.

Grupps	L,	m.F,				
В3-В5	322°	± 5°				
$A - G \left\{ \begin{array}{l} \mu < 0'',020 \\ 4,0 < m \le 5,8 \end{array} \right\}$	345	士 9				
B0-B2	322	± 5 ± 8				
c-Sterne $m < 5.0$ $A-G \begin{Bmatrix} \mu < 0'',020 \\ m > 5.8 \end{Bmatrix}$	330 337	± 8				
$Oo5 \qquad m > 5.8 $	308					
c-Sterne m ≥ 5.0	321	土 7 土 4				
Planet, Nebel	333	土10				

Länge des Attraktionszentrums erhielt Oort die Werte in Tabelle 22, wo die Gruppen grob nach mittlerer Entfernung (von 300 bis etwa 1200 Parsec) angeordnet worden sind. Das unter Berücksichtigung der Gewichte berechnete Mittel für L<sub>0</sub> wird 324°±2° (m. F.), was offenbar sehr gut mit Shapleys Konzentrationspunkt für die Kugelhaufen übereinstimmt und sich

auch mit der Länge des Zentrums, wie sie aus der Asymmetrie der Geschwindigkeitsverteilung (Ziff. 30) hervorgeht, gut verträgt.

Für den Koeffizienten A ergab sich im Mittel +0,019 km/sec per Parsec ±0,003 (m.F.). Da A die Abweichung von einer gleichförmigen angulären Rotations-

geschwindigkeit mißt, so ist also gemäß diesen Resultaten die vektorielle Differenz der Rotation im oben angegebenen Sinne oder die "differentielle Rotation", innerhalb unserer Umgebung des Sternstratums nachweisbar. Es deutet dies a.n., daß das Gravitationsfeld an unserem Ort im System nicht etwa dem Felde eines homogonen Rotationsellipsolds in seiner Äquatorebene entspricht, sondern, mit diesem Fall verglichen, auf eine merkliche Verdichtung der Materie gegen die zentralen Regionen des Systems schließen läßt

Um aber eine entscheidende Evidenz für die Realität der differentiellen Rotation zu bekommen, mitsen auch die Effekte (67) in den Eigenbewegungen untersucht wurden. Ookt hat die Eigenbewegungen des Preliminary General Catalogue von Boss behandelt Korrektionen für die Bewegung des Frühlings-Dunktes und für die Prazessionakonstante wurden aus den Bewegungskompomenten in galaktischer Breite bestimmt. Als Korrektionen der Newconnschen Werte für die zwei erwähnten Größen findet Oort +0",0137 ± 0",0020 (m F) lozw. +0",0113 ± 0",0020 (m.F). Als Wert der Lumsolarprezession ergibt sich also 50",3821 (1900) Die korrigierten Eigenbewegungen in galaktischer Länge wurden zur Bestimmung von  $L_0$ ,  $\Lambda$  und B benutzt Die Werte von  $L_0$  etimmen gut mit den oben gegebenen, aus den Radialgeschwindigkeiten ermittelten überein, während A nicht unerheblich kleiner als der oben gegebene Wert ausfällt, was aber nach Oort sehr wohl durch Fehler in den Eigenbewegungen, speziell für Sterne in der südlichen Milchstraße, verursacht sein kann. Für die mittlere Bewegung B/4,74 langs der Milchstraße gibt Oort, gemäß den Resultaten für drei Gruppen von sehr entfernten Sternen, als wahrscheinlich besten Wert -0",0050 oder B = -0.024 km/suc per Parsec +0.005 (m,F) (vgl Ziff, 26 und 32)

Zur weiteren Beleuchtung des überaus wichtigen Effektes der differentiellen Rotation in den Radialbewegungen konnte J S Plaskett¹ ein vorzügliches neues Material von Goschwindigkeiten für Wolf-Rayet- und Helium-Sterne ausnutzen, die auf dem Observatorium in Victoria gemessen worden sind Für die Rotationsgrößen  $L_0$  und tA und den K-Term hat er die in Tabelle 23 aufgeführten Werte mit den angegebenen wahrscheinlichen Fehlern gefunden Im Mittel bekommt Plaskett hier  $L_0 = 324^\circ, 5 \pm 1^\circ, 8$ ,  $A = +0.0155 \pm 0.0007$  km/sec per Parsec.

Tabollo 23

Kles	se und Größe		ī	L,	K km/ma	r.d. km/ma
B0-B2 B0-B2 B3-B5 B3-B5	<6,21	66 66 181 175 65	5,00 6,94 5,16 6,79 6,43	332°.7±9.8 328.5±3.0 308.5±2.6 325.0±2.1 322.3±7.2	+3.2 ± 1.0 -0.4 ± 0.9 +0.9 ± 0.3 -1.2 ± 0.3 +5.8 ± 2.9	+ 5.9 ± 0.9 +16.7 ± 1.1 + 4.8 ± 0.5 + 5.9 ± 0.3 +17.1 ± 4.0

Eine sehr große Bedeutung hat gegenwärtig die Theorie der differentiellen Rotation für die Erscheinung der "stationären" Kalziumlinien (Ziff. 25) gewonnen. Oort berechnete den Rotationskoeffizient für 40 Ca<sup>+</sup>-Geschwindigkeiten zu +5,6 km/sec ± 2,2 (m F.). Gerabinovič und O. Struve haben dann die galaktische Rotation des interstellaren Kalziums aus den Ca<sup>+</sup>-Geschwindigkeiten für 103 Sterne vom Typus O-B2 studiert. Der Koeffizient 7A für die "Wolken" ergibt sich zu +5,3 km, während für die Sterne selbst +12,0 km aus Plasketts obenerwähnten Werten berechnet wurde Das Verhältnis 1 2,3 zwischen den mittleren Entfernungen wurde als Zeugnis für eine approximativ gleichförmige Verteilung des Kalziums gemäß Eddingtons Hypothese betrachtet.

<sup>1</sup> M N 88, S. 395 (1928)

Ap J 69, S 9 (1929)

Einen ungemein großen Fortschritt zur Aufklärung der diesbeztiglichen Verhältnisse bedeutet aber vor allem die Arbeit von J. S. Plaskett und J. A. Pearce1, die im wesentlichen auf dem umfangreichen Material von Geschwindigkeiten für Bo-B5-Sterne heller als 7m,5 visuell und nördlich von der Dekl. -11° beruht, welches in den letzten Jahren auf dem Observatorium in Victoria gesammelt worden ist, Für 261 Sterne, deren galaktische Verteilung in Abb. 28 dargestellt wird, sind Ca+-Geschwindigkeiten vorhanden. Mit einer angenommenen Sonnengeschwindigkeit von +20.0 km gegen den Apex  $L = 21^{\circ}.8$ ,  $B = +20^{\circ}$  ergaben sich für den K-Term und die Rotationsgrößen die Resultate  $K=-0.61\pm0.57$  km,  $\bar{r}A=+7.90\pm0.79$  km,  $L_0=331^{\circ}.7\pm5^{\circ}.7$ . Der Rotationskoeffizient kommt also hier mit einem Werte heraus, der zehnmal größer als sein wahrscheinlicher Fehler ist. Die Länge Lo erscheint fast exakt um 90° gegen Strömbergs Asymmetrielinie gedreht,

Die 235 Sterne, für welche sowohl "stellare" als "interstellare" Geschwindigkeiten vorliegen, wurden zuerst in Gruppen nach scheinbarer Größe geteilt und

Tabelle 24. Gruppierung nach Größe,

ī.	п	r.A				,	Υ
		Sterne	Wolken	Steme	Wolken		
4,41 5,60 6,03 7,08 7,34	37 45 79 119 69	$\begin{array}{c} + 1.81 \pm 2.83 \\ + 10.26 \pm 2.12 \\ + 13.86 \pm 1.75 \\ + 16.58 \pm 2.20 \\ + 20.49 \pm 2.32 \end{array}$	+ 3,85 ± 1,22 + 5,02 ± 1,24 + 7,66 ± 0,90 + 8,31 ± 1,36 +10,08 ± 1,57	+7.12 ± 1.42 +3.99 ± 0.96 +1.67 ± 0.77 +1.39 ± 1.46 +2.34 ± 0.86	+0.02 ± 0.61 +0.97 ± 0.56 +0.09 ± 0.40 -0.69 ± 0.90 +0.23 ± 0.56		

innerhalb jeder Gruppe ist dann der Rotationskoeffizient rA und der K-Term sowohl für Sterne als für Wolken bestimmt worden. Für  $L_0$  wurde hier immer der Wert 325° angenommen. Die Resultate sind in Tabelle 24 aufgeführt.

Für die vier letzten Gruppen, in mittleren Entfernungen von etwa 600. 800, 1000 und 1200 Parsec, ist das Verhältnis der Rotationskoeffizienten 7d für Sterne und Wolken der Reihe nach 2,04, 1,81, 1,99, 2,03 oder im Mittel 1,97. Die Eddingtonsche Hypothese, daß die interstellare Materie gleichförmig verteilt ist, wird also hier in außerordentlich deutlicher Weise bestätigt.

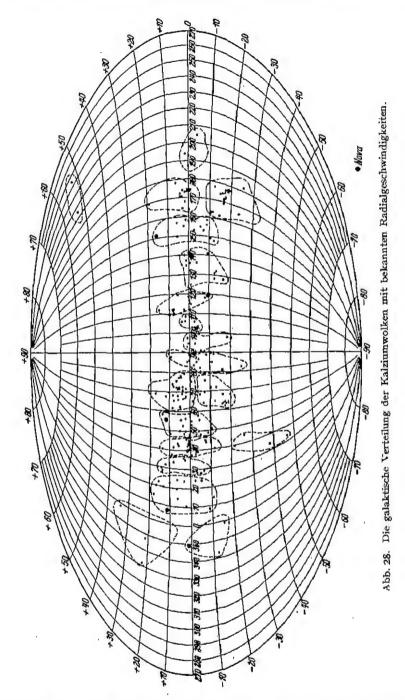
Ähnliche Resultate gibt eine Einteilung des Materials nach der Intensität der interstellaren K-Linie, wie Tabelle 25 zeigt. Die erste Kolumne gibt die benutzten Intervalle in Intensität in einer konventionellen Skala,

Tabelle 25. Gruppierung nach Intensität der interstellaren Linion.

Inten	uust	Ī.	4	· K	
Intervall	Mittel	Sterne	Wolken	Sterne	Wolken
0 -5,9 6,0-6,9 4,4-6,9 7,0-7,9 8,0-9,5	4,72 6,50 6,08 7,46 8,42	+ 3.64 ± 3.25 +12.12 ± 1.88 +10.22 ± 1.72 +14.53 ± 2.93 +27.52 ± 2.46	+ 4.93 ± 0.92	+6,12 ± 2,14 +4,66 ± 1,27 +5,24 ± 1,17 -0,14 ± 1,95 +3,18 ± 1,74	+1,15 ± 0,50 +0,10 ± 0,62 +0,10 ± 0,58 -0,21 ± 0,70 -1,17 ± 0,82

Es stellt sich heraus, daß die Intensität der interstellaren Linie ein besseres Entfernungskriterium als die scheinbare Große ist. Aus den Werten von 71 für die letzte Gruppe der Tabelle kann man die mittlere Entfernung zu etwa 1600 Parsec berechnen. In wie hohem Maße der Rotationsterm  $rA\sin 2(L-325)$ die Geschwindigkeiten innerhalb der einzelnen Längengruppen wiedergibt, zeigt

<sup>1</sup> M N 90, S. 243 (1930).



uns die Tabelle 26, wo für die letzte Intensitätsgruppe die beobachteten und die berechneten Geschwindigkeiten relativ zum Zentroid für verschiedene galaktische Längen gegeben worden sind.

Tabelle 26.

Mittlere		Ste	rns	Wolken		
Länge	п	Beob.	Bor,	Beob.	Ber.	
358°	2	+35,7	+24,3	+ 8,2	4- 9.4	
17	2	+12,2	+29,5	+ 6,1	4-11.5	
34	6	+21.5	+21,3	+ 7.5	+ 7.9	
47	2	+11,8	+10,4	+ 6,6	+ 2,4	
70	12	- 3,4	10,4	<b></b> 5.4	- 8,0	
97	4	-26.8	-23,4	-15,5	-14,3	
107	9	-28,4	-23,5	-17,7	14,5	
141	4	- 4,1	- 0,9	+ 1,2	3.2	
169	2	+13,6	+16,0	+ 1,9	- - 5,3	

OORT1 hat eine Auflösung für diese Gruppe allein mit Lo, rA und K als Unbekannten gemacht, wobei die Bestimmung von  $L_0$  beträchtliches Gewicht hat. Er bekommt als Resultat die folgenden Werte:

Sterne	Wolken
$L_0 = 330^{\circ}, 1 \pm 2^{\circ}, 6 \text{ (w.F.)}$ $\vec{r}A = 26, 0 \pm 2, 2 \text{ km/sec}$	$L_0 = 329^{\circ}, 3 \pm 4^{\circ}, 3 \text{ (w.F.)}$ $\vec{r}A = 12, 4 \pm 1, 7 \text{ km/sec}$
K = +0.9 + 1.6	K = -2, 2 + 1, 2,

Es ist ohne weiteres augenscheinlich, in welch hohem Grade die Resultate von Plaskett und Pearce unsere Vorstellungen über die allgemeinen Eigenschaften des rotierenden Sternsystems stützen, erstens durch die Bestütigung des Rotationseffektes selbst und zweitens durch den Schluß auf eine gleichförmige Verteilung der interstellaren Materie in der galaktischen Ebene innerhalb eines sehr weiten Kreises um uns herum. Keines von diesen Ergebulssen läßt sich wohl mit der Existenz eines lokalen Systems vereinigen, wenn mit diesem Ausdruck irgendeine dynamisch abgeschlossene Einheit gemeint wird.

Eddington's hat auch hervorgehoben, daß die Existenz einer derartigen Schicht von dünnem Gase, die sich gegen das Zentroid der in ihr eingelagerten Sterne in Ruhe befindet, die beste Stütze dafür ist, daß die Bewegung des Zentroids relativ zum Schwerpunkt des Systems eine Kreisbahn beschreibt. Denn da das interstellare Gas zu gleichförmig verteilt erscheint, um wesentlich von irgendeinem hydrodynamischen Druckgradienten gegen die Attraktion des Systems getragen zu sein, so muß das Gleichgewicht durch die Zentrifugalkraft allein bewirkt werden und demnach die mittlere Bewegung innerhalb eines Elementarvolumens des Gases mit der Kreisbewegung übereinstimmen. In dieser Weise können wir mit Eddington behaupten, daß schon die Existenz der kosmischen Wolken ein Beweis für die Existenz der Rotation ist. Der Beweis für die Kreisbewegung ist übrigens analog mit unserem oben (Ziff. 29) für die Sterne von kleiner Geschwindigkeitsdispersion gegebenen.

Es ist aber an sich sehr bemerkenswert, wie Eddington und Oort hervorheben, daß die Bewegung der Wolken so exakt mit dem Zentroide der Sternbewegungen zusammenfällt (nach Oort innerhalb 1 km/sec), wenn wir bedenken, daß die Rotationsgeschwindigkeit auf ungefähr 300 km/sec zu schätzen ist.

In den ohen referierten Arbeiten von Oort und von Plaskett und Pearce sind besonders Gruppen von Objekten mit großer mittlerer Entfernung und mit kleiner Streuung in den zentroidalen Geschwindigkeiten behandelt worden. Es sind aber auch Versuche gemacht worden, die Rotationsgrößen für ein mehr normales Material zu bestimmen. Es ist klar, daß die Schwierigkeiten, ein zu-

<sup>1</sup> BAN 5, S. 192 (1930).
2 The Rotation of the Galaxy. Halley Lecture. Oxford: Clarendon Press (1930).

verlässiges Resultat zu bekommen, mit abnehmender mittlerer Entfernung (wolche direkt auf die Amplitude  $\bar{r}A$  einwirkt) und mit einer steigenden Streuung der Geschwindigkeiten (wolche den Ausgloich der partikularen Bewogungen herabsetzt) erheblich wachsen. Im Falle der Elgenbewogungen bleibt zwar die Rotationsgröße dieselbe, wird aber mit abnehmender Entfernung unmer kleiner im Verhältnis zur mittleren Eigenbewegung der Sterne Eine Tatsache betreffs der Rotationseffekte für die gewöhnlichen Riesensterne der Spektralklassen A bis K scheint jedoch ziemlich wohl begründet. Es stellt sich hernus, daß die Länge  $L_0$  des Rotationszentrums ein wenig höhere Worte als für die entfernteren Objekte von kleinerer Streuung in den Geschwindigkeiten annimmt Dieses Phanomen ist schon durch Corrs Resultate in Tabelle 22 angedeutet worden, wo für die A bis G-Sterno  $L_0=345^\circ$  bzw 337° gefunden wurde Lindblad findet für die Sterno vom Typus P bis K und  $\mu<0'',040$  den Wert  $L_0=346^\circ$  Rednan findet für 425 K-Sterne im Größenintervall 7,0 bls 7,5 und größtenteils innenhalb ±10° galaktischer Breite, deren Radialgeschwindigkeiten von ihm selbst in Victoria bestimmt worden and, die differentielle Rotation  $7A = 1.9 \pm 1.3$  km/soc,  $L_0 = 17^{\circ} \pm 18^{\circ}$  (w F) Die Sterne in diesem Material zeigen aber eine ziemlich große Streuung in den Geschwindigkeiten, und nach gewissen Eigenschaften der Frequenzkurve der Geschwindigkeiten in verschiedenen Gegenden des Himmels scheint es sehr wohl möglich, daß spezielle Strömungen unter den Sternen auf das Resultat ungünstig eingewirkt haben H Nordström hat deshalb, anstatt das arithmetische Mittel der Geschwindigkeiten verschiedener Gegenden zu benutzen, in einem Ausgleichungsverfahren die Geschwindigkeit maximaler Frequonz ffir jedes Arcal bestimmt und in die Gleichungen für die differentielle Rotation olugesetzt. Er findet dann aus REDMANS Material im Mittel  $\bar{r}A = 3.0$ .  $L_{\bullet} = 333^{\circ}$ , was als ganz normal anzuschon ist und auch sehr wohl mit seinen Resultaten für K- und M-Sterne heller als 6m,0 übereinstimmt

Es lat von großem Interesse, die eben erwähnten Resultate mit den aus omer Behandlung der Eigenbewegungen gewonnenen zu vergleichen. Für eine gesammelte Gruppe von B-, c-, O-, N- und & Cephel-Sternen (also sehr entfernten Objekten) hat OORT gefunden  $A = +0'',0024 \pm 0'',0016$  (m F.),  $B = -0'',0050 \pm 0'',0014 \text{ (m F)}, L_0 = 326^{\circ} \pm 17^{\circ} \text{ (m F)}, \text{ withrend Dyson's für}$ B0- bis A0-Sterne die fast identischen Werte A = +0'',0025, B = -0'',0046,  $L_0 = 326^{\circ}$  erhält. J. Schult, der spoziell die Eigenbewegungen verschiedener AG-Zonen auf die diesbezitglichen Effekte hin analysiert hat, findet aber fol-

gende Worte GYLLEWINERO (35°-40° nordi. Doki ) +0",0106 340° • +0",0081 337° • +0",0080 ± 28(m F) 351° ± 9(m F) PRACER (31°-40° nordi Dekl) . . . Boss PGC . . . . .

J. E MERRILL findet aus dem Yale-Katalog für nördl Dekl 50° bis 55°,  $A = +0^{\circ},0073, L_0 = 0^{\circ}$ 

Da unter den von Schilt und Merrill untersuchten Zonensternen die Mehrheit normale Riesensterne vom Typus A bis K sein werden, so können die eben gegebenen Resultate an die Seite der aus den Radialgeschwindigkeiten für diese Typen hergeleiteten gestellt werden. Es ergibt sich also ein höherer Wert der gelaktischen Länge des Zentrums  $L_0$ ; außerdem geben offenbar die

\* A J 39, S. 90 (1929)

M N 90, S 503 (1930) — Stockholm Medd 5

MN 90, S 690 (1930), 92, S 107 (1931), Publ Astrophys Obs Victoria (IV) Nr. 20 (1930) Lund Modd 131 (1933)
MN 90, S, 239 (1930).

Lund Modd 131 (1933) Wash Nat Ac Proc 13, S 642 (1927), A J 38, S. 149 (1928); 39, 5 17 (1928).

Daten aus den Eigenbewegungen der Zonensterne einen ziemlich hohen Wert für den Amplitudenfaktor A. Zum Vergleich mag erwähnt werden, daß der Wert A = +0.0155 km/sec per Parsec aus den Radialgeschwindigkeiten, durch Division mit 4,74, dem Werte  $A = +0^{\circ\prime},0033$  im Eigenbewegungsessekt entspricht. Es liegt nahe zu bemerken, daß die Länge Lo für die normalen Riesensterne besser mit dem beobachteten Vertex des Geschwindigkeitsellipsolds als

mit der Länge L, für die entfernten Sterngruppen übereinstimmt.

Es sind schon verschiedene Erklärungen für das eben geschilderte Phänomen vorgeschlagen worden. H. MINEUR1 macht darauf aufmerksam, daß wir die Länge Loum 90° ändern können, wenn wir gleichzeitig das Vorzeichen von A ändern. Er sucht dann das Material in zwei Gruppen zu trennen, eine Klasse von sehr entfernten Objekten, die sich um ein Zentrum in der Länge 325° hewegen und eine Klasse von nahen Sternen, die sich um ein lokales Zentrum etwa in der Länge 240° drehen; die letztere Länge stimmt mit dem Zentrum des lokalen Haufens nach Charlier und Shapley überein. Es können jedoch wohl ernste Einwände gegen Mineurs Auffassung erhoben werden. Vor allem ist die Entfernung zum Zentrum des "lokalen Haufens" zu klein, um die Theorie der differentiellen Rotation in der Oortschen Form hier anzuwenden. Es scheint auch, daß der spezielle Rotationseffekt in MINEURS Analyse, den er zur Scheldung zwischen den zwei Rotationsarten heranzieht, von grundsätzlich anderem Charak-

ter als der oben diskutierte Effekt ist (Ziff. 34).

S. S. Hough und J. Halm? haben schon in ihren wichtigen Arbeiten über die Sternbewegungen die harmonischen Terme von zweiter Ordnung in den Radialgeschwindigkeiten und in den Eigenbewegungen gefunden und studiert. Sie sehen aber die Ursache der Erscheinung in einem verschiedenen Mischungsverhältnis der drei großen Sterntriften (KAPTEYNS Triften I, II und HALMS o-Trift) in verschiedenen Gegenden des Himmels. In neuercr Zeit ist auch J. Schill's geneigt, die Theorie der differentiellen Rotation zur Erklärung der harmonischen Terme zweiter Ordnung in den Sternbewegungen ganz aufzugeben. Er bildet eine Größe U, welche die Form der Frequenzkurve für die Eigenbewegungen repräsentiert und zeigt, daß ähnliche harmonische Terme in dieser Große auftreten. Er zieht hieraus den Schluß, daß die harmonischen Terme zweiter Ordnung einem verschiedenen Mischungsverhältnis von Sternströmen in verschiedenen Gegenden des Himmels zuzuschreiben sind. Daß die erwähnte Verschiebung in  $\check{L}_0$  wahrscheinlich im Phänomen der Sternströmung ihren Grund hat, wird auch von REDMAN und LINDBLAD behauptet. Es ist aber nicht notwendig, deshalb die Rotationstheorie aufzugeben, was besonders nach den Ergebnissen von Oort, Plaskett und Pearce kaum möglich ist. Ein enger Zusammenhang zwischen dem Geschwindigkeitsellipsoid oder der Sternströmung überhaupt und der differentiellen Rotation ist übrigens durchaus in Einklang mit der Theorie, wie wir im folgenden in Ziff, 32 näher auseinandersetzen werden. Nach der Rotationstheorie hängen nämlich sowohl der Effekt der differentiellen Rotation wie die Richtung und das Größenverhältnis der Achsen des Geschwindigkeitsellipsolds in der Milchstraßenebene unmittelbar von dem Scherungsessekt einer gegenseitigen Translation der Geschwindigkeitsmittelpunkte für einander benachbarte Orter im System ab. Diese Translation soll der Richtung der Kreisbewegung folgen und ihre Größe nur auf der Differenz der Entfernung vom Zentrum zwischen den betreffenden Ortern beruhen. Es ist aber durchaus nicht

<sup>1</sup> CR 188, S. 236, 1086 p. 1378 (1929); 190, S. 1050 (1930); BA 5, S. 505 (1929); MN 90, S. 516 (1930).

3 M N 70, S. 85 und 568 (1909, 1910); 71, S. 610 (1911).

befremdend, daß eine Abweichung der Vertexrichtung oder andere Anomalien der allgemeinen Sternströmung, die etwa in einzelnen ausgeprägten Sternströmen ihren Grund haben, von entsprechenden Effekten in den ermittelten Rotationsquantitäten begleitet sein können.

32. Die Beziehung zwischen dem Geschwindigkeitsellipsoid und der Rotation. Nach der abstrakten Theorie sollte das Geschwindigkeitsellipsoid ein Sphäroid sein, dessen Äquatorebene auf der galaktischen Ebene senkrecht steht und mit der Ebene, welche die Rotationsachse des Systems enthält, zusammenfällt. Das Verhältnis der Achsen  $\alpha$  und  $\beta$  soll aber auch in einer gewissen Beziehung zu der Größe  $\Lambda$  und zu der Winkelgeschwindigkeit  $\omega$  der Rotation stehen. Wir haben gemäß den Gleichungen (65), (42), (44)

$$A = \frac{1}{2} \left( \frac{\theta_0}{R} - \frac{\partial \theta_0}{\partial R} \right), \qquad \theta_0 = \frac{MR}{R^2 + 2p}, \qquad \left( \frac{\beta}{\alpha} \right)^2 = \frac{2p}{R^2 + 2p}$$

und bekommen dann die Relation

$$A = \omega \left[ 1 - \left( \frac{\beta}{\alpha} \right)^2 \right]. \tag{70}$$

 $\omega$  wird positiv in retrograder Richtung gerechnet.  $\alpha$  ist die Achse, welche in der Milchstraßenebene gegen das Zentrum des Systems zeigt. In Ziff. 30 haben wir weiter aus der Theorie ermittelt, daß, wenn die ellipsoidische Approximation streng wäre, die Achse  $\alpha$  für alle Punkte des Systems konstant sein sollte, während  $\beta$  mit R (aber nicht mit z) variiert.

Die Bedeutung der Gleichung (70) ist eine zweifache: Erstens, da es sehr wohl möglich ist, daß A und  $\beta/\alpha$  für verschiedene Gruppen von Sternen verschiedene Werte annehmen, können wir hoffen, durch Koordination der gemessenen Werte von A und  $\beta/\alpha$  im Vergleich mit der Gleichung eine wertvolle Kontrolle der Theorie selbst zu bekommen. Zweitens können wir in dieser Weise die Größe  $\omega$  bestimmen, was sonst durch direkte Analyse der Eigenbewegungen geschehen muß. Die mittlere Eigenbewegung B in galaktischer Länge ist mit A und  $\omega$  durch die Relation  $B = A - \omega$  verbunden. Der Wert von B aus den Eigenbewegungen muß mit dem aus dieser Relation ermittelten verglichen werden.

Gemäß den oblgen Auseinandersetzungen und unserer Deutung der empirischen Daten in der vorigen Ziff. 31 betrachten wir A und  $\omega$  als positive Größen. Die Achse  $\alpha$  soll also die größere sein und die Vertexlinie der Sternströmung

soll gegen das Zentrum hin zeigen.

Eine quantitative Vergleichung zwischen differentieller Rotation und Geschwindigkeitsellipsoid hat B. Lindblad unter Benutzung des zur Zeit zugänglichen Materials von Radialgeschwindigkeiten für gewöhnliche Spektraltypen versucht. Die Resultate sind in Tabelle 27 aufgeführt. Für die Typen A bis K sind die Sterne in Gruppen nach Eigenbewegung aufgeteilt worden. Die Bestimmung von A und  $L_0$  ist nur für die entfernteste Gruppe möglich gewesen.

Tabolle 27.

Gruppa	A	$L_{\bullet}$	Vertex	& km/sea	// km/see	km/sec	21
B0-B7	+0,006 +,013 +,033 +,021	324° 334 319 346 —	289° 275 21 335 356 342 349	10,9 12,4 18,6 17,5 19,1 27,7 36,3	9,8 10,5 12,4 13,6 8,4 19,4 21,4	4.5 11.4 3.9 16.5 10.0 16.9 25.5	445 250 304 714 391 857 825

<sup>&</sup>lt;sup>1</sup> M N 90, S. 503 (1930) = Stockholm Medd 5.

Die Sterne vom Typus B zeigen nur geringe Spuren einer Vorzugsrichtung der relativen Bewegungen in der Milchstraßenebene, was wohl in der kleinen Streuung der Geschwindigkeiten und dem Zusammengehen dieser Sterne in mehr oder weniger losen Haufen seinen Grund hat. Im A-Typus setzt der Ursa Major-Strom ein, und dies führt eine sehr merkliche Distorsion der Geschwindigkeitsfläche mit sich. Die späteren Typen zeigen ziemlich hohe Werte von  $L_0$  und der Länge des Vertex, ein Phänomen, das wir schon in der vorigen Ziff. 31 besprochen haben. Im ganzen scheint es sehr wohl möglich, daß die Abweichungen des Ellipsoids von den idealen Verhältnissen der Theorie wenigstens großenteils auf den Einfluß irregulärer Strömungen in unserer näheren Umgebung zurückgeführt werden können.

Zur Erklärung des Umstandes, daß die dritte Achse gewöhnlich viel kleiner als die größte Achse in der Vertexrichtung herauskommt, haben wir schon in Ziff. 29 und 30 angeführt, daß die Bewegung parallel zur Milchstraßenebene in der unmittelbaren Nachbarschaft von dieser Ebene von nahe zweidimensionaler Natur ist, und daß demnach die statistische Ausgleichung zwischen den galaktischen Bewegungskomponenten und der dritten Bewegungskomponente senkrecht zur Milchstraßenebene eine außerordentlich langsame sein muß. Spezielle Strömungen in der Milchstraßenebene werden daher auch nur sehr langsam auf die Streuung in Z einwirken.

Nur für die erste Gruppe F bis K in Tabelle 27 ist ein direkter Vergleich zwischen dem Ellipsoid und den Größen der differentiellen Rotation möglich. Der Wert von A ist jedoch hier mit einem ziemlich großen mittleren Fehler behaftet. Wenn wir an Stelle dessen Plasketts Wert A = 0.0455 annehmen und

für  $\beta/\alpha$  als normalen Wert 0,78, so bekommen wir aus der Formel

$$\omega = +0.040$$
,  $B = -0.024$ .

Durch Division mit dem Faktor 4,74 ergibt sich

$$\omega = +0'',0084$$
,  $B = -0'',0051$ ,

ein Resultat, das sich im ganzen wohl mit den direkt aus den Eigenbewegungen ermittelten Werten verträgt (vgl. Ziff. 31).

H. RAYMOND und R. E. WILSON¹ haben in einer Untersuchung über die Raumgeschwindigkeiten von 4233 Sternen die diesbezüglichen Fragen einer eingehenden Besprechung unterzogen. Die beiden Verfasser haben nach neuen Methoden eine Analyse der Asymmetrie der Geschwindigkeitsverteilung ausgeführt, welche für die Asymmetrierichtung  $L=62^{\circ}$ ,  $B=+6^{\circ}$  gibt, in wesentlicher Übereinstimmung mit Strömbergs Resultaten, und sie haben die offenbare Verbindung zwischen dieser Asymmetrie und den nahe senkrecht dazu vor sich gehenden allgemeinen Vertexbewegungen untersucht. Zuletzt haben sie sehr ausführlich die Relation zwischen den Rotationsgrößen und den Eigenschaften der Geschwindigkeitsellipsoide diskutiert. Als mittleren Wert für das Achsenverhältnis  $\beta/\alpha$  erhalten sie 0,72, woraus für A=+0.015

$$\omega = +0.031$$
,  $B = -0.016$ 

folgt, oder in Bogensekunden

$$\omega = +0'',0065$$
,  $B = -0'',0034$ .

Unser oben hergeleiteter Wert B=-0'',0054 stimmt mit dem von Oort aus den Eigenbewegungen sehr entfernter Sterne bestimmten überein. Nach Raymond und Wilson steht jedoch der kleinere Wert B=-0'',0034 in besserer. Übereinstimmung mit der mittleren Eigenbewegung in galaktischer Länge für

<sup>1</sup> A J 40, S. 121 (1930).

die Sterne im allgemeinen. Die Verfasser haben auch aus ihrem Material die Konstanten der differentiellen Rotation sowohl für Radialgeschwindigkeiten wie für Eigenbewegungen bestimmt. Die ersteren, in zwei Gruppen nach der mittleren Parallaxe der Sterne geordnet, gaben folgendes Resultat:

$$\vec{\pi}$$
 L<sub>4</sub>  $\vec{r}A$  A  
0,0121 329° +1,29 ± 0,34 +0,0155  
0,0046 355 +3,05 ± 0,40 +0,0140

Die Resultate sind in guter Übereinstimmung mit den in der vorigen Ziff. 31 referierten. Der hohe Wert von  $L_0$  für die zweite Gruppe ist auffallend.

In den Eigenbewegungen wird ein Term vom Typus  $C\cos 3(L-L_I)$  eingeführt, dessen Koeffizient  $C=+0'',0022\pm0,0003$  gefunden wird, und wo sich für  $L_1$  der Wert +10° ergibt. F. W. Dyson hatte einen ähnlichen Term für die B-Sterne eingeführt. Wahrscheinlich liegt der Grund dieses Termes in speziellen Strombewegungen, möglicherweise sogar im Ursa Major-Strom und im Taurus-Strom. Der erstere geht nahe gegen die Länge 0°, wo  $\cos 3L$  und  $\cos L$  Maxima haben, während der letztere gegen  $L=450^\circ$  zeigt, wo  $\sin 3L$  ein Maximum hat. Für A und B ergeben sich die sehr kleinen Werte

$$A = -1-0'',0013, B = -0'',0005.$$

Der Übersicht wegen stellen wir in Tabelle 28 einige repräsentative Bestimmungen der wichtigen Konstanten B zusammen. Die als theoretisch bezeichneten Werte sind die aus dem Achsenverhältnis des Geschwindigkeitsellipsoids berechneten.

Tabelle 28.

	В	Autoritāt
-0",0024 -0 ,0015 -0 ,0023 -0 ,0005 -0 ,0050 -0 ,0051 -0 ,0034	13-, c-, O-, N-, & CophSterne Theoretisch	CHARLIER <sup>1</sup> FOTHERINGHAM <sup>2</sup> OORT RAYMOND UND WILSON OORT LINDBLAD RAYMOND UND WILSON

Ein einfaches Mittel aus diesen Werten gibt  $B=-0^{\prime\prime}$ ,0029, und dieser Wert

kann vorläufig als der beste für diese Größe gelten.

88. Die Dimensionen, die Masse und die Rotationszeit der Milchstraße. Wenn wir gemäß Tabelle 28 für die Konstante B im Mittel -0",0029 annehmen und für A den Wert +0",0033, so gibt uns die Relation  $\omega=A-B$  für die Winkelgeschwindigkeit der Rotation  $\omega=0$ ",0062. Nachdem wir den Wert von  $\omega$  bestimmt haben, gibt uns eine Ermittlung der linearen Rotationsgeschwindigkeit  $\Theta_0$  unmittelbar unsere Entfernung R vom Zentrum des Systems. Aus den Apexbestimmungen für die Kugelhaufen haben wir oben  $\Theta_0$  für Gruppen kleiner Geschwindigkeitsstreuung zu 275 km/sec angenommen. Der entsprechende Wert der Zentrumsentfernung ist R=9400 Parsec.

Die Rotationsdauer an unserem Orte wird etwa

483

$$P = 200$$
 Millionen Jahre.

Für die Zentralkraft an unserem Orte haben wir offenbar, da für kleine Geschwindigkeitsstreuung  $\Theta_0$  die Geschwindigkeit der Kreisbewegung ist,

$$\frac{\partial V}{\partial R} = -\frac{1}{R} \Theta_0^2 = -R \omega^2. \tag{71}$$

<sup>&</sup>lt;sup>1</sup> Mom Univ Calif 7 (1926). <sup>8</sup> M N 86, S. 424 (1926).

Wit konnen eine "effektive Masse" des Systems in der Weise einstteln, daß wit diese Kraft als durch ein schematisches System eizeugt denken, welches aus einer spharischen Zentialmasse  $M_1$  und einer sehr abgeplatteten, homogenen, spharoidischen Verteilung von der Gesamtmasse  $M_2$  mit dem galaktischen Radius  $R_1$  besteht Das Verhältnis zwischen  $M_1$  und  $M_2$  soll so angepaßt weiden, daß es für zirkulare Bewegungen einen differentiellen Rotationseffekt A gibt Wir haben dann also gemäß (71)

$$\frac{\partial V}{\partial R} = -G\left(\frac{M_1}{R^2} + \frac{3\pi}{4R^2}RM_2\right) = -R\omega^2 \tag{72}$$

Wii konnen weiter schreiben

$$A = \frac{1}{4\omega} \left( -\frac{1}{R} \frac{\partial V}{\partial R} + \frac{\partial^2 V}{\partial R^2} \right) = \frac{3}{4} G \frac{M_1}{\omega R^3} , \tag{73}$$

und bekommen dann nach einigen Reduktionen

$$M_1 = \frac{4R^3}{3G}\omega A$$
,  $M_2 = \frac{4R_1^3}{3\pi G}\omega(\omega - \frac{4}{3}A)$  (74)

Wenn w<br/>nRın Parsec und  $\Theta_0$ ın km/sec ausdrücken, bekommen w<br/>ın nach Ausrechnung des Zahlenfaktors

$$M_1 = 0.617 \cdot 10^{88} \frac{A}{\omega} R \Theta_o^3 g,$$
 (75)

$$\frac{M_3}{M_1} = \frac{1}{\pi} \left( \frac{R_1}{R} \right)^3 \left( \frac{\omega}{A} - \frac{4}{3} \right). \tag{76}$$

Mit den obigen Werten von A,  $\omega$  und R bekommen wit, wenn wit übrigens  $R_1$  mit dem "effektiven Radius" in Ziff 30 identifizieren,

$$M_1 = 233 \cdot 10^{12} \,\mathrm{g}, \quad M_2 = 89 \cdot 10^{42} \,\mathrm{g}$$

und also fur die Totalmasse

$$M_1 + M_2 = 322 \cdot 10^{42} \,\mathrm{g} = 16 \cdot 10^{10} \,\mathrm{Sonnenmassen}$$

Die Masse des Systems ergibt sich also von der Großenordnung 10<sup>11</sup> Sonnenmassen. Die anderen hier gewonnenen Resultate konnen verschieden interpretiert werden Trotz des Umstandes, daß die galaktische Länge des Zentiums gemäß dem Phanomen der differentiellen Rotation in die Gegend der hellsten Milchstraßenwolken fallt, zeigt Pannekoeki, daß die Lichtstaike der Wolken keine Ansammlung von Steinen, die einer Masse von der Größenordnung von M<sub>1</sub> entspricht, zuläßt, auch wenn wir mit ziemlich erheblichen Absorptionseffekten rechnen. Er weist darauf hin, daß die gasförmige interstellare Materie moglicher weise ausreichend ist, um eine gegen das Zentrum konzentrierte Masse von der angeführten Größe zu geben. Andererseits ist in Shapley's obenei wähnten Resultaten die Anwesenheit einer wirklichen zentralen Kondensation angedeutet Der große Wert von  $M_1/M_2$  in unserem schematischen System ist ja doch nur von der Natur des Kraftfeldes in unserer Umgebung bedingt und kann nach Oort<sup>2</sup> sowohl auf eine wirkliche zentrale Kondensation wie auf einen ziemlich schnellen Zuwachs der Dichtigkeit gegen das Zentrum hin in unserer unmittelbaren Umgebung zuruckgefuhrt werden

Zwischen der oben angenommenen Zentrumdistanz von 9400 Parsec und den aus der Verteilung von Kugelhaufen (Shapley, Ziff 18) und von Veranderlichen in einem Milchstraßenfelde (Shapley und Swope, Ziff 20) ermittelten Weiten, 16400 bzw. 14400 Parsec, besteht offenbai eine Inkongruitat Die neuen Resultate, die auf die mögliche Existenz eines absorbierenden Stratums

<sup>&</sup>lt;sup>1</sup> BAN 4, S 39 (1927) <sup>2</sup> BAN 4, S 92 (1927)

nahe der Milchstraßenebene hindeuten (Ziff, 24), stellen aber eine Revision der aus den photometrischen Daten berechneten Entfernungen in Aussicht, van der Kamp¹ hat kürzlich dieses Problem zur Behandlung aufgenommen. Nach dieser Untersuchung stellt sich gegenwärtig die Sache so, wie Tabelle 29 angibt. Van der Kamp hat sowohl mit Trümplers Absorptionskoeffizienten wie mit dem von Bottlinger und Schneller, unter Annahme einer Dieke der absorbierenden Schicht von 175 Parsec, die Entfernungen der betraffenden Objekte neu ausgerechnet.

Tabelle 29

		Absorpt ion		
Material	Keine Absorption	011,67per 1000 Parson	2m per tono Parses	
Geometrisches Zentrum des Systems der Kugelhaufen	16700 Parsec	13700 Parsoo	9700 Parrecc	
Veranderliche in Harvard Milky Way Field 185 [Pol nach Pickerine (a) baw van Rhijn (b)]	14400	(a) 11 600 (b) 12 500	(a) 7400 (b) 9400	
Galaktische Rotation		7000-11	000 Рапос	

Es scheint nach diesen Resultaten nicht ausgeschlossen, daß die Werte der verschiedenen Methoden sich in dieser Weise miteinander in leidlichen Einklang bringen lassen.

34. Übersicht verschiedener Anschauungen über die Natur des Milchstraßensystems. Wenngleich die eben besprochene Theorie eine beträchtliche nnere Einheitlichkeit besitzt und in der Tat auf einem Minimum von Hypothesen beruht, so treten neben ihr andere, mehr oder weniger grundverschiedene Auffassungen hervor. Wir haben schon vorher mehrfach die Theorie erwähnt, die ein im wesentlichen dynamisch geschlossenes "lokales System" voraussetzt Die dynamischen Eigenschaften dieses Systems werden wohl im allgemeinen im Sinne des Kapteyn-Jeansschen Systems in Ziff. 28 angenommen. Von diesem Gesichtspunkte aus erscheint sogar die Existenz eines allgemeinen, alle als galaktisch erkannten Objekte zusammenhaltenden Kraftfeldes fraglich. So hat früher G. Strömberg in dem Phänomen der Asymmetrie der Geschwindigkeitsverteilung den direkten Einfluß der Eigenschaft eines fundamentalen Raumos, die Größe der m ihm gemessenen Geschwindigkeiten zu beschränken, in Verbindung mit einer Tendans der Materie in unserer Umgebung zu einem lokalen Zusammengehen gesucht.

Eine Thoorie, welche in vielen Zügen Berührungspunkte mit der oben referierten Rotationstheorie hat, in anderen aber eine grundvorschiedene Einstellung nimmt, haben kürzlich E. von den R-Rifekt der Radlalgeschwindigkeiten vorgelegt. Diese Verfasser gehen von dem K-Rifekt der Radlalgeschwindigkeiten der Hellumsterne und dessen Variation mit der galaktischen Länge aus. Hier aber wird der ganze K-Rifekt als ein Dilatationseifekt der uns umgebenden Gruppe von B-Sternen infolge einer Bahnbewegung dieser Gruppe im großen System erklärt. Die Bewegung kann als ein "Fallen" der Sterngruppe im Gravitationsielde des großen Systems beschrieben werden Unter der Annahme, daß wir uns mit der Sterngruppe dem Zentrum nähern, beobachten wir, daß die uns in der Bahn voraneilenden Sterne sich relativ zu uns entfernen, da ale bereits dem Zentrum näher sind, während in der entgegengesetzten Richtung

A J 44, S. 84 (1931).

L. c. Siehe such "Conference on Michalson-Morley-Experiment". Mt Wilson Contr

<sup>373,</sup> S 61 = Ap J 68, S. 401 (1928)
Publ Astrophys Obs Potsd 26, H. 3, Nr. 86 (1928).

die Sterne mit kleinerer Geschwindigkeit zuruckbleiben. Die Richtung, in der die Bewegung von sich geht, wird aus den galaktischen Langen der Maxima des K-Effektes zu etwa  $L=10^{\circ}$  gefunden, eine Richtung, welche einen Winkel von etwa 45° mit der Richtung gegen das Shapleysche Zentrum einschheßt Aus den folgenden Daten. Maximalbetrag des Effektes, Ausdehnung des betrachteten Haufens von B-Steinen in der galaktischen Ebene, Entfernung vom Zentrum des großen Systems, werden die Elemente der Bahnbewegung bestimmt, unter der Voraussetzung, daß das Gravitationsfeld als von einer Punktmasse im eben genannten Zentrum herruhrend angesehen werden kann

Unter Berucksichtigung der Radialgeschwindigkeiten der Kugelhaufen wird die Geschwindigkeit in der Bahn zu 70 km/sec geschatzt. Wenn die Entfeinung vom Zentrum zu 12000 Paisce geschatzt wird, ergibt sich eine Masse im Zentrum von der Glößenoldnung 10<sup>11</sup> Sonnenmassen und eine Umlaufszeit von 10<sup>8</sup> Jahren, Die Eigenschaften der schnellbewegten Steine und die Kaptrynschen Steinstrome werden dann diskutiert. Als Zusammenfassung gilt nach dieser Ansicht, daß die Steine im Raumgebiet um unseien Punkt im System herum in ihrei uberwiegenden Mehrzahl sehr langgestreckte elliptische Bahnen im Gravitationsfelde der großen Masse im zentralen Teil des von den Kugelsternhaufen definierten galaktischen Systems, an dessen Rande sich unsei lokales Steinsystem befindet, beschreiben. Die Steine dieses lokalen Systems zerfallen im wesentlichen in zwei Wolken, die zwai sehi ahnliche, jedoch schon meiklich verschiedene Bahnen beschreiben, wobei die Gruppen der helleren B-Sterne der einen Wolke, die Sonne abei dei zweiten Wolke mit etwas kleinerer Exzentrizitat (etwa 0,90) und augenblicklich größeiei Bahngeschwindigkeit (etwa 90 bis 100 km/sec) angehören Der Unterschied der Bahnen und der augenblicklichen Geschwindigkeiten bedingt das Phanomen der beiden Steinstrome Das Sternsystem befindet sich also noch sehr wert von einem stationaren Zustande, und die erhaltenen Bahnen sind nui "momentane" Wie ein deraitiges momentanes Zusammenballen von Sternen in dei Wolke des "lokalen Systems", dessen eigene Gravitationski aft keinen mei klichen storenden Einfluß auf die Bewegungen im System, insbesondere keine nierkliche zusammenhaltende Kraft auf seine eigenen Mitglieder ausüben soll, zustande kommt, bleibt wohl aber gänzlich unerklärt. Die Streuung in den relativen Geschwindigkeiten innerhalb des lokalen Systems ist ja in der Tat viel gioßei als die Amplitude des K-Effekts, auf den die Eigengravitation des lokalen Systems keine merkliche Einwirkung haben soll. Das lokale System gemäß dieser Theorie könnte also nicht etwa durch allmähliche Auflockerung eines ursprunglich geschlossenen Systems entwickelt worden sein und kann überhaupt nicht mit dem lokalen System der geläufigen Vorstellung identifiziert werden

J Rosenhagen<sup>1</sup> hat eine allgemeine Untersuchung über den K-Effekt für die normalen Spektraltypen unter Ausnutzung des gesamten Materials der zur Zeit bestimmten Radialgeschwindigkeiten ausgeführt. Er untersucht den Gang des K-Teimes mit einer Langenkoordinate sowohl in der Milchstraßenebene wie in zwei senkrecht zu ihr und zueinander stehenden "orthogalaktischen" Ebenen und findet auch für die letzteren eine ausgeprägte Variation, die durch eine zweigipfelige Smuskurve approximiert werden kann. Die Maxima eischeinen ziemlich nahe an den Polen dei Milchstraße gelegen. Ei sucht seine Ergebnisse sowohl nach der Theorie von von der Pahlen und Freundlich wie nach einer Erweiterung der Oortschen Ansatze zu deuten, ohne ein entscheidendes Argument für diese oder jene zu bekommen. Im letzteren Falle muß er zur

<sup>1</sup> A N 242, 5 401 (1931)

Deutung der "orthogalaktischen" Kurven eine Variation der Geschwindigkeitsmittelpunkte in unserer Umgebung nicht pur mit der Zentrumsentfernung R, sondern auch mit der s-Koordinate annehmen. Die Rotationsgeschwindigkeit Go soll also  $\Theta_0(R,s)$  geschrieben werden. Die nördlichen Schichten der Milchstraße sollten eine höhere Rotationsgeschwindigkeit als die südlichen haben Der K-Effekt in der Milchstraße gibt in Übereinstimmung mit den oben in Ziff. 32 diskutierten Resultaten für die gewöhnlichen Spektraltypen eine Zentrumslänge L<sub>a</sub> = 350° Eine Variation der Geschwindigkeitsmittelpunkte mit der z-Koordinate ist früher von H MINEUR1 eingeführt worden, der eine allgemeine Analyse des K-Effektes nach Kugelfunktionen entwickelt hat. MINEUR findet emen Effekt, aus dem er eine Rotation um ein lokales Zentrum in der galaktischen Lange 240° herlettet Die angulare Geschwindigkeit dieser Rotation soll nur wenig von der Entfernung zum Rotationszontrum abhängen, dagegen aber mit der Höhe über der galaktischen Ebene beträchtlich veränderlich sein. Der genannte Effekt läßt sich folgendermaßen beschreiben. Wenn wir die Achsen x, y, s im Raume in die folgenden Richtungen legen

$$x \begin{cases} L = 232^{\circ} \\ B = 0^{\circ} \end{cases}$$
  $y \begin{cases} L = 322^{\circ} \\ B = -10^{\circ} \end{cases}$   $x \begin{cases} L = 320^{\circ} \\ B = +80^{\circ} \end{cases}$ 

so existiert ein Term  $\varphi$  in den Radialgeschwindigkeiten von der Form

$$\varphi = -0.058 \text{ yz}$$

Es scheint, daß dieser Effekt auch quantitativ mit Roseneagens K-Variation in einer mit der verlibene nahe zusammenfallenden orthogalaktischen Ebene (G"-Ebeno genannt) ziemlich übereinstimmt.

Es ist wohl nach den geschilderten Verhältnissen klar, daß, wenn wir auf dem Boden der Rotationstheorie blelben, wir sichere Auskunft über die Rotationsbewegungen im großen System am besten aus den sehr entfernten Objekten in der Milchstraßenebene, in der Weise, wie es besonders Oort sowie PLASKETT und Prance gemacht haben, bekommen, daß aber, wenn wir zur großen Masse der uns verhältnismäßig nahellegenden Sterne mit größerer Geschwindigkeitsdispersion übergeben, der differentielle Rotationseffekt teilweise durch Störungen überlagert wird, über deren wahre Natur wir noch in Unklarheit sind. Es ist jedenfalls von Interesse, zu konstatieren, daß diese Störungen den Vertexpunkt des Geschwindigkeitsellipsoids und die Lange La um denselben Betrag verschieben.

Von größter Bedeutung für die kosmologischen Ideen während der letzten zwei Jahrhunderte ist die Frage nach einer möglichen Analogie zwischen unserem Milchstraßensystem und den "außergelaktischen" oder "anagalaktischen" Nebalflecken gewesen Die "Weltinseltheorie" wurde wohl zuerst in HERSCHELS Arbeit "On the Construction of the Heavens" (1785) ausgebildet, doch macht HERSCHEL hier noch keinen prinzipiellen Unterschied zwischen wirklichen und acheinbaren Nebeln, sondern nimmt an, daß die Nebel überhaupt von der letzteren Art sind und demnach nichts anderes als entfernte Sternansammlungen darstellen In selnen späteren Arbeiten hat er die zwol Nebelarten erkannt, nelgte aber allmählich mehr und mehr zu der Ansicht, daß die Milchstraße in ihrer eigenen Ebene eine ungeheure Ausdehnung besitze, und daß sie wahrscheinlich in ihrem System alle für uns wahrnehmbaren Objekte einschließe. Bls in die letzten Julire haben in der Tat die Ansichten über die wahre Natur der Milchstraße zwischen

B A 5, S, 505 (1929).
 Vgl. goschichtliche Übersicht von K. Lummark, Studies of Anagalactic Nebulac.
 Nova Acta Reg Soc Sc Upsal, Volumen extra ordinem 1927

den beiden Extremen der Weltinseltheorie einerseits und der Theorie eines praktisch allumfassenden Milchstraßensystems andererseits geschwankt.

Nach Lord Rosses Entdeckung der Spiralform einiger Nebel (1845) ist die Weltinseltheorie in interessanter Weise von Stephen Alexander<sup>1</sup> und von Cleveland Abbe<sup>2</sup> entwickelt worden. Der erstere kann, wie Lundmark bemerkt, durch seine Theorie über die Nebel als sternproduzierende Mechanismen als ein Vorgänger von Jeans betrachtet werden.

Die spektroskopische und spektrographische Scheidung der galaktischen Gasnebel von den Nebeln mit typischem Absorptionsspektrum hat dann in besonderer Weise die Diskussion gefördert. Da im letzteren Falle Spektra von angenähertem Sonnentypus sich ergeben, hat man hier gleich eine schwer-

wiegende Bestätigung der Weltinseltheorie gesehen.

Unter den Verfassern, die sich in neuerer Zeit mit den diesbezüglichen Fragen beschäftigt haben, ist besonders Easton<sup>a</sup> zu nennen, der auf Grund seiner eigenen Forschungen aus dem verwickelten Verlauf der Milchstraße am Himmel die Gestalt eines gewaltigen Spiralnebels mit dem Kern in der Cygnus-

region herauszulesen versuchte.

Nach Shapleys grundlegenden Untersuchungen über das größere galaktische System, die eine unerwartete Erweiterung unserer Vorstellungen über den Umfang des Milchstraßensystems als Ganzem mit sich führten, neigte die Auffassung wohl zugunsten der Theorie einer praktisch allumfassenden Milchstraße, um so mehr, da die van Maanenschen direkt gemessenen Rotationsgeschwindigkeiten der Spiralnebel gegen genügend große, der Weltinseltheorie entsprechende Entfernungen für diese Objekte sprachen. Besonders durch die Studien von Curtis, Lundmark, Hubble u. a. über die Natur der außergalaktischen Nebel hat aber die Weltinseltheorie ihre alte Stellung als bevorzugte Theorie wiedererobert. Die gegenwärtigen Grundlagen der Entfernungsbestimmungen für die Spiralnebel und die verwandten Objekte haben schon einen bemerkenswerten Grad von Zuverlässigkeit gewonnen, und die Distanzen kommen genügend groß heraus, um in genereller Weise der Weltinseltheorie zu entsprechen,

Mit dieser wahrscheinlich endgültigen Entscheidung einer alten Streitfrage sind aber keineswegs die Fragen über die Natur und Stellung des Milchstraßensystems erledigt worden. Es scheint zwar an sich wahrscheinlich, daß unter den verschiedenen Typen von Nebeln ein "Modell" zu unserem eigenen System gefunden werden könnte, jedoch ist von vornherein klar, daß das Material für elne rein morphologische Klassifizierung unseres Milchstraßensystems noch nicht vorliegt, und daß hier besonders große Schwierigkeiten, vor allem die mehr oder weniger regelmäßigen Absorptionserscheinungen, zu überwinden sind. SEARES hat der Lösung der Frage auf dem Wege der Flächenhelligkeiten näherzukommen versucht. Er berechnet aus KAPTEYNS und VAN RHINS Dichtefunktion die Flächenhelligkeit des von einem sehr entfernten Punkt in der Richtung des galaktischen Pols aus gesehenen galaktischen Systems, Er findet, daß diese Helligkeit etwa der visuellen Größe 23 per Bogensekundenquadrat entspricht, etwa 100 mal kleiner als die Flächenhelligkeit der helleren Partien in typischen Spiralnebeln. Daß wir so verhältnismäßig leicht die galaktischen Wolken wahrnehmen, beruht nach Seares einfach auf dem großen Areal dieser Gebilde am Himmel, Dieses Resultat, das auf eine vom galaktischen System verschiedene Konstitution der Spiralnebel deutet, verliert wohl aber erheblich an Beweiskraft, wenn wir nicht länger das Zentrum des galaktischen Systems in unserer unmittelbaren Nachbarschaft suchen. In einer späteren, oben in

<sup>&</sup>lt;sup>1</sup> A J 2 (1852). <sup>2</sup> M N 27, S. 262 (1867). <sup>3</sup> Ap J 12, S. 136 (1900). <sup>4</sup> Mt Wilson Contr. 191 = Ap J 52, S. 162 (1920).

in den außeren Teilen unseres Systems nach der eben erwähnten Theorie wohl möglich, wenngleich die wahrscheinlich erhebliche zentrale Kondensation der Materie im System eine sahr mächtige Entwicklung der Spiralstruktur verhindern mag. Es soll aber hier zuletzt erwähnt werden, daß H. Voor1 die Bedeutung der neuen Ergebnisse über die Expansion der Welt zur Erklärung der Spiralform herangezogen hat, und es ist möglich, daß dieses Phanomen auch für unser eigenes System wichtige Konsequenzen mit sich geführt haben kann

Von den oben referierten Gesichtspunkten wesentlich verschiedene, aber namiteunder verwandte Hypothesen über die Natur des Milchstraßensystems haben gleichzeitig Lundmarks, Shapleys und Trümplers aufgestellt. Nach den Ansichten der zwei ersteren Verfasser ist das Milchstraßensystem kein emheitliches Objekt, das mit irgendeinem einzigen außergalaktischen Nebel verglichen werden kann Shapley sicht eher in den Nebelhaufen, z. B. in der Coma-Virgo-Gruppe oder noch mehr in der dichteren Centaurusgruppe, unserem Mikhstraßensystem ähnliche Formationen Die einzelnen Glieder unseres Systems, die mit den Nebeln einer Gruppe vergleichbar wären, sind die Sternwolken der Milchstraße, unter die ein lokales System gerechnet wird, ferner die MAGELIANschen Wolken und die Kugelhaufen. LUNDMARK teilt die eigentliche Milchstraße in wesentlich zwei Tellsysteme, das lokale System und das zum großen Tell durch Absorption in Dunkelnebeln verborgene Sagittariussystem Er betont besonders eine mögliche Verwandtschaft zwischen den Kugelhaufen und den elliptischen außergalaktischen Nebeln TRUMPLER deutet sein System von offenen Sternhaufen, das ziemlich Rotationssymmetrie um die Sonne besitzt, als gewissermaßen einen Grundriß zur eigentlichen Milchstraßenstruktur. Dieses um die Sonne zentrierte System wird dann in der Tat die Hauptmasse des Systems enthalten, und die Existenz des verborgenen Sagitterlussystems schelnt in Frage gestellt. TRUMPLER deutet das System als einen Spiralnebel mit gegen rechts gewundenen Armen, vom Nordpol der Milchstraße aus gesehen. Die Kugelhaufen sind nicht organisch in dieses System singegliedert. Es mag erwähnt werden, daß TRUMP-LEES System sich nicht mit dem Shapleyschen lokalen System oder lokalen Haufen deckt, sondern ein viel weiter gestrecktes Gebilde darstellt. Der lokale Haufen nach Shaprey könnte aber als die Zentralregion des Milchstraßennebels anigefaßt werden.

Wenigstens gegen welt getriebene Hypothesen in der Richtung einer Aufteilung des Milchstraßensystems in isolierte Teilsysteme kann wohl mit Recht hervorgehoben werden, daß es als ein merkwürdiger Zufall zu bezeichnen würe, daß die Teilsysteme, die nach dieser Annahme die eigentliche Milchstraße aufbauen, alle so nahe in einer und derselben Ebene orientiert liegen. Man darf auch sagen, daß die Anwesenheit der Kugelhaufen, welches ihr Ursprung auch sein mag, keineswegs an und für sich unserem Milchstraßensystem die Würde einer Organisation von höherer Ordnung als die gewöhnlichen Nebel verleihen kann. Ähnliche Phänomene treten wahrscheinlich auch bei Systemen von verhåltnismäßig bescheidener Größe auf. Objekte, die als Kugelhaufen zu bezeichnen sind, sind ja z B, in der unmittelbaren Umgebung der großen MAGELLANschen Wolke vorhanden, in der Weise, daß sie offenbar mit der Wolke in Verbindung stehen. Die Angliederung der Magellanschen Wolken als "ferne Begleiter" unseres Systems crinnert ja auch an die zwei elliptischen Nebel NGC 205 und 221 bei M31. Wenn wir diese zwei Satellitennebel zum System des Andromeda-

A N 242, S. 181 (1931), 245, S. 281 (1932).
 Publ A S P 42, S 23 (1930), Pop Astr Tidskr 11, S. 85 (1930).

Hary Circ 350 (1930) 4 Lick Bull 14, S 154 (1930).

nebels rechnen wollen, so bekommen wir zwar ein mehrfaches System, der Haupt-

körper selbst erscheint jedoch vollkommen einheitlich

Gegen Trumplers Auffassung seines Haufensystemes macht Bottlingeriden Einwurf, daß jenei die Einwirkung der Absorption des Lichtes im System nicht genugend berucksichtigt hat Trumpler ist nicht daraut gekommen, daß die von ihm gefundene Absorption in einer eingen Milchstraßenschicht vielleicht die Ursache sei, die uns eine Dichteabnahme langs der Milchstraßenschicht vielleicht die Ursache sei, die uns eine Dichteabnahme langs der Milchstraßenschicht vielleicht die Ursache Es ist in der Tat sehr wohl möglich, daß die Extinktion in gewissen Richtungen, z. B. gegen das Zentrum des Systems in Sagittarius, so intensiv sein kann, daß sie die Vollstandigkeit des Haufenmaterials in sehr höhem Grade herabsetzt. Die Neigung des Haufensystems gegen die Milchstraßenebene mag durch eine etwas nördliche Absorptionszone in der Sagittariusrichtung erklart werden. Trümplers Haufensystem stellt dann einen schrägen Schnitt durch das System dar

Die Existenz eines "lokalen Systems" in dem gelaufigen Sinne dieses Wortes ist nach der Rotationstheorie nicht möglich, da die Materie in unserer Umgebung durch die beobachteten Effekte dei differentiellen Rotation stetig zeigliedert werden muß Es wären also, wenn das ortliche System etwas Geschlossenes und Beständiges 1st, diese Effekte in anderei Weise zu deuten Bei dei inneren Einheithehkeit der erwähnten Theorie, die quantitativ eine Reihe Phänomene imitemander verknüpft, die sonst als isolierte Tatsachen auftreten und besonders nach der Bestätigung der differentiellen Rotation für die Sterne mit interstellaren Ca-Limen durch die Aibeit von Plaskell und Plarce, muß man wohl doch von anderen Theorien fordern, daß sie in ebenso direkter Weise und ohne komplizierte Hilfshypothesen etwas Abnliches leisten. Es fehlt ja auch nicht an Tatsachen, die auf eine weitgehende Heterogenität des "lokalen Systems" deuten Es ist in dei Tat wohl möglich, daß der beobachtete Überschuß an Dichtigkeit in unserer Nähe, sowert er sich nicht durch Absorption des Lichts in der Milchstraßenebene erklärt, eine Folge der machtigen Stromungen ist, die sich hier zufälligerweise raumlich überemanderlagern. Wir können unter solchen Strömungen den Tautus-Strom, den Ursa major-Strom und die großen Triften der Heliumsterne nennen. Das Phänomen des "lokalen Systems" wäre dann mit den beobachteten kleineren Abweichungen von regulären Verhältnissen in der Geschwindigkeitsveiteilung in Veibindung zu setzen (vgl. Ziff 31 u. 32), hätte aber an sich nichts, was mit den großen Linien der einheitlichen Theorie in Widerspruch steht. Es mag hiei dei Klaiheit wegen bemeikt weiden, daß nach diesei Theorie die Bahnen der erwähnten großen Stromungen nur wenig von der zukularen Bewegung um das Zentium heium abweichen. Was wit unmittelbai beobachten, sind natürlich nur ihre relativen Geschwindigkeiten.

Wenn wir auf dem Boden der Rotationstheorie etwa nach dem Ursprung der beobachteten Sedimentation verschiedener Gruppen von Objekten in "Untersysteme" von verschiedenen dynamischen Eigenschaften fragen, so ist es möglich, wie in Ziff. 29 auseinandergesetzt, daß Effekte einer langsamen Gleichverteilung der Energie durch "Passage" hier mitspielen können, wenn wir nur eine genügend lange, nach der Formation des Systems verflossene Zeit voraussetzen dürfen Andere Gesichtspunkte lassen sich auch finden. So ist es vielleicht möglich, daß im Untersystem von größter Rotationsgeschwindigkeit, wo die Materie sich in nahe relativer Ruhe bewegt, sich vorzugsweise Steine mit großer Masse und verhältnismäßig großer Dichte gebildet haben<sup>2</sup>, was die große relative Häufigkeit der Steine von frühem Spektraltypus in diesem Untersysteme erklären

<sup>1</sup> Beilin-Babelsb Veröff 8, II 5 (1931)

<sup>&</sup>lt;sup>9</sup> Lindblad, Ark Mat Astr Fys 21 A, Nr 3 = Stockholm Medd 1, S 24 (1928)

könnte. Die Häufigkeit gewisser Arten von Veränderlichen, wie kurzperiodische d-Cepheisterne und Me-Sterne, in den Untersystemen von großen relativen Geschwindigkeiten und von geringer Abplattung gegen die Milchstrußenebene kann vielleicht damit in Verhindung gebracht werden, daß die Mitglieder dieser Untersysteme individuell genommen in radialer Richtung sehr langgestreckto Bahnen beschreiben, welche die betreffenden Sterne ziemlich oft in die dichten Gegenden des Zentrums führen Es besteht wenigstens die Möglichkeit, daß ein Auftreten gewisser singulärer Typen von Sternen in diesen Gegenden leichter vor sich gehen wird als in anderen. Welcher Wert derartigen Gedanken zukommt, läßt sich allerdings gegenwärtig kaum entscheiden. Ohne Zwolfel kann man jedoch sagen, daß überhaupt die allgemeinen Fragen über die Entwicklung der Sterntypen wichtige Berührungspunkte mit den Fragen nach der Struktur und der Entwicklungsgeschichte des Sternsystems haben

Es ist jedoch ohne weiteres klar, daß man bei dem jetzigen Stande der Milchstraßenforschung jeden Schluß nur mit der größten Vorsicht zu ziehen hat Für die direkten Untersuchungen der Dichteverteilung im System scheint gegenwärtig das Problem der Absorption des Lichtes in der Milchstraßenschicht das wichtigste zu sein. Erst wenn wir einen zuverlässigen Weg zur Beseitigung der aus diesem Phänomen herkommenden Schwierigkeiten gefunden haben, können wir eine volle Einigung der rein empirischen Morphologie des Systems

mit irgendeiner dynamischen Theorie erwarten.

## Appendices to Chapter 4.

# Luminosities, Colours, Diameters, Densities, Masses of the Stars.

By
KNUT LUNDMARK-Lund
(Continued)

## I. Catalogue of Stars Brighter than 5<sup>m</sup>,00.

Contents Col 1 contains the number in the PGC by L Boss (upper line) and the RHP number (lower line). This number also corresponds to the number in Schresinger's work, "Catalogue of Bright Stars", New Haven 1930. The catalogue of Schresinger was not accessible to me when I compiled the present catalogue but it has been used for check work during the proof-reading of this chapter.

Col 2 contains the name of the stars in the usual nomenclature together with the BD number, when in italics this refers to the nearest whole degree according to the wellknown rules concurring the course of the precession

Col 3 and 4 contain the  $\alpha$  and  $\delta$  for 1900,0

Col 5 contains the spectral type

Col 6 contains the colour in Osthoff's scale and the estimates according to Franks (Specola Astronomica Vaticana VIII, IX and XV.) Only in a few cases the estimates of the present writer have been added. These estimates are given in the Osthoff Scale.

Col. 7 contains the apparent magnitudes according to RIIP and to Zinner's work, "Helligkeitsverzeichnis von 2373 Steinen bis zur Große 5,50". The latter magnitudes are based upon an extensive discussion of practically all available determinations of stellar magnitude and they follow very closely the scale defined

by PD (See ciph 40.)

Col. 8 and 9 contain on the upper line the total proper motion (unit is 0",001), or the quantity  $\mu = [(\mu_{\alpha}\cos\delta)^2 + \mu_{\delta}^2]^4$  and the direction  $\psi$  of the proper motion (unit is 1°), counted in the same way as the position angles and defined as tg  $\psi = \mu_{\alpha}\cos\delta/\mu_{\delta}$ , and on the lower line the  $\tau$ - and  $\nu$ -components, which according to Kapifyn's definition are  $\tau = \mu\sin(\chi - \psi)$  and  $\nu = \mu\cos(\chi - \psi)$ , where  $\chi$  is the angle of the great circle through the Apex with the declination circle, counted in the same way as the position angles. The quantities  $\mu$ ,  $\psi$ ,  $\tau$ , and  $\nu$ , given in columns 8 and 9 have in most cases been taken over from an unpublished determination carried out under the supervision of Kapifyn by Dutch prisoners. The results of this extensive work of computation has been distributed earlier in typewritten manuscript to several observatories. I am under much obligation to Kapifyn's family as well as to P. J. van Rhijn, Director of the Kapifyn Laboratory for kind permission to include the mentioned data in the present catalogue.

Col 10 gives the iadial velocity of the star, expressed in kilometer per second. The work of J. H. Moore, "A General Catalogue of the Radial Velocities of Stars, Nebulae and Clusters", was not accessible to me, when the present catalogue was compiled but has been used for a general check when reading the proofs. When a velocity is indicated by "Var." there are no conclusive evidences as to the nature of variation of the radial velocity. When the velocity is indicated by "Var." and a number, this number in most cases refers to the velocity of the system, derived from the variation in radial velocities interpreted

as caused by orbital motion in binary systems.

Col. 11 contains on the upper line the arithmetic mean of existing parallax determinations (trigonometric or spectrographic, or in a few cases theoretic values), on the lower line the geometric mean of the same determinations, provided that they are positive. In both cases the unit is 0",001.

Col 12 gives the number of parallax determinations used when forming the mean values in col. 11. When in column 12, instead of a number, an (a) is given, the parallax value in the preceding column has been inserted from additional sources, being available since the catalogue was compiled in 1927 to 1928.

Col. 13 contains on the upper line the absolute magnitude M in the RHP system and on the lower the absolute proper motion magnitude  $H=m+5+5\log\mu$ . In cases of variable stars the M- and H-values correspond to the magnitude at maximum.

Col. 14 and 15 contain the galactic longitude and latitude computed with aid of the tables computed at the Observatory in Lund and distributed in mimeograph form. When more accurate values for these coordinates are needed the extensive tables, "Lund Observatory Tables for the Conversion of Equatorial Coordinates into Galactic Coordinates" (Ann. Obs. Lund No. 3), should be consulted.

dinates into Galactic Coordinates" (Ann. Obs. Lund No. 3), should be consulted.

A few remarks as to binaries, variable stars etc. have been added to the table. In these remarks ADS refers to R G. ATTERNS work, "Now General Catalogue of Double Stars within 120° of the North Pole I—II" [Wash Carnegie Inst Publ No. 417 (1932)].

						Or.								_
1	2	3	4	5	6	7	8	9	10	11	12	13	14	
1 3	33 Placinm 6357	0=,2	- 6°16′	K0	5°.7	4",68 4 ,85	92 + 67		- 6,3	23 23	(2)	1,5 4,5	67*	-
10 15	a Andromedae	3 ,2	+28 32	A0p	1°.7	2 ,15 2 ,39	213 - 77		-13,0	48	(5)	0,5	81	F
12	# Camiopelao 3	3 ,8	+58 36	P5	3°,1	2,42	559		+11,8	71 71	(4)	6.2	85	-
16 25	# Phoenicle 16	4 ,3	-46 18	K <sub>0</sub>		3 ,94	- 131	1480	- 9,2	25 25	(2)		290	-
27 39	7 Pognal 14	8 ,1	+14 38	B2	2°,2 W	3 ,87	13		+ 4,9	6	(4)	-3,2 -1,6	79	F
91 45	Z Pegnal 27	9 ,4	+19 39	Ma	7',3 Y	4 ,94	94 + 37	97 + 86	-45,3	5	(4)	-1,2 4,8	80	1
33 48	7 Cett	9 ,6	-19 30	Ma	7',0 OY	4 ,68	68		-22,7	13	(3)	0,2 3,8	52	Ħ
43 63	o Andromedas 84		+38 8	A2	34,0 Y1	4 ,44 4 ,65	- 52 - 40	247	+ 4,7	23 22	(4)	1,1	84	1-1
50 68	o Andromedas 44	13 ,1	+36 14	Δ2	21,9 Y1	4 ,51 4 ,70	- 81 - 70	237	Var.	15	(4)	0,2	84	Ħ
53 74	4 Cett	14 ,3	- 9 23	Ko	5'.9 Y	3 .75	37		+18,2	20 19	(3)	0,1	71	F
55 77	Tucanas 13	14 ,9	-65 28	F8		4 ,34 4 ,46	2058		+ 9,3	146 146	(1)		274	F
92	B Cambopelae	19 ,2	+63 36	Mb?	Ver	-5 ,0 to		-	-	1	(1)	-157	88	1
95	47 Tuonnao 35	19 ,6	-72 39	G 5		[4 ,5]	-		-	0,2	(1)	-8,8	272	≓
74 98	# Hydrl 16	20 ,5	-77 49	Go	44,7	2 ,90 3 ,02	2240 ± 384	82° +2195	+23,0	160	(2)		271	1
78 99	a Phoenicis	21 ,3	-42 51	Ko	5°.7	2 ,44	445		+74,2		(3)		284	
77 100	n Phoenicia 101	21 ,3	-44 14	A3		3 .90	107		+ 9	12	(4)	5.7 -0.7 4.1	283	1=

His 92. Nove H Consequence of 1572. Permiter from the spectral properties of the 13m,8 star presumed to be the Move. — HR 95. Of the MOVE. — HR 95. Of the Move. — HR 95.

Oh, 11 15 13 6 7 8 9 10 11 12 1 298° 82° 4m,96 56 210°+11,2 22m,9 -33° 34' Mb n Sculptons 83 4,96 55 6 3.7 152 105 1°,9 105°--10 0.9 88 - 8 7 (a) **B8** 4 ,88 48 26 2 +53 59 97 / Cassiopeiae 8 -1-48 3,3 5 ,02 82 123 83° Vai 25 (1) 1,9 275 4,88 128 -69 11 Phoenicis 26 ,6 -49 22 A2 99 25 5.4 4 ,97 52 116 125 115 103 122° -- 10 34 (4) 1,2 272 -54 Bo 4,52 B1 Tucanac 27,0-63 31 100 4.6 ,61 40 95 126 50 (a) 1,1 272 B2 Tucanae A2 4,48 108 1259-1 9,9 34 -54 27.0 - 6331 101 4,6 4,59 48 97 127 50 3°,5 Y1 85  $(\overline{3})$ 11 3 3,4 89 Bo 4,21 « Cassiopeiae 27,3 + 62 23 103 4,41 3 0,6 5 10 102 130 1139 - 2.0 0 (4)-3.3 20,6 23 9 ¿ Cassiopeiae 31 ,4 -- 53 133 3 ,72 122 YG1 3,98 1 23 4 0,5 153 105 23 113° -- 8,8 (3)20.5 3 -2,6 88 -29 **B**3 4,44 123 π Andromedae 31 ,5 -- 33 10 W 23 1,3 4,58 101 154 222° -83.4 30 (4) 1,8 88 336 -33 & Andromedae 40,7 4,52 33,3 + 2846 G5 130  $\mathbf{Y}^2$ 28 7,2 4,60 329 64 163 103 **(4)** 60,0 162 122 - 7,2 29 0,9 88 -32 3,49 & Andromedae 34 ,0 - 30 K2 132 YS 30 4,5 3,49 162 3 --165 91 (4) Ko 50,0 2,47 60 121° - 4.1 21 0.9 89 6 135 с Сачнорогае 34 ,8 -1-55 59  $OY^3$ 2,53 6-1-59 21 1,4 168 139 2°,7 Y¹ б (2)-1,3 89 36 ,5 -1-49  $B_3$ 4 ,85 21 109 - 9,4 -12 141 & Cassioperae 58 ,07 б 1,5 3 -+-21 5 164 179 2270 +16.5 14 (2)0.4 272 4 ,65 38 -- 71 n Phoenicis 36,6-46Ko 142 2,6 4 .73 33 19 14 180 180 0,003 (3)- 18, 89 -21 30,2 -300[4,90]33 Andromedae 37 ,2 +40 43 G4 182 148 5°,8 Y<sup>8</sup> 80° +13,3 (2) 0,3 90 -81 230 41 B Ceti 38 , 6 - 18Ko 2,21 32 147 41 4,0 2,30 143-1 182 188 115 315 +10 270 -60 38,8 - 5810  $A_0$ 4 ,53 148 n Phoenicis 8 -0.54,62 6 42 191 (2)-1,8 B2 30,0 4,70 22 103° 7,5 5 90 -14 152 o Cassiopeiae 39 ,2 -1-47 44 5  $\mathbf{Y}^{\mathbf{1}}$ 4 ,88 6 -1-21 1,4 193 183 5°,2 Y<sup>2</sup> (1) 183° + 0.6 15 0,8 90 -73m1 Ceti 9 Kο ,93 110 39 ,2 -- 11 151 48 15 5,1 4 ,94 99:-1 194 128 Vai 129 (4)1.2 -38 5°,5 4 ,30 231° 25 164 ¿ Andromedae 42 ,0 -1-23 0MYβ 4.8 4 123 43 -25,9 24 ,31 215 106 ,64 115° + 9.9 148 (9)4,4 4°,5 1242 91 -- 5 43 ,0 +57 17 F8 3 168 n Cassiopeiae Y 145 9, 1 3 ,74 25 -1-1242 219 150 1180 (4) 0,4 -55 +31,9 16 92 60,9 93 & Piscium 43.5 + 72 IX 5 4 ,55 173 4,4  $O^2$ 7 93 15 107 4 ,59 224 ,42 28 138° Vai 7 (3) 1,3 91 -21 20,2 32 **B**3 175 y Andromedae 44 ,3 +40 27 - 24,0 98° - 9,4 8 -1 1,7 7 W 4 ,71 171 226 IC 5 ,96 134 270 -43 45 ,1 -75 28 182 2 Hydu ,08 5,6 21 -133 5 236 64 338° -- 21.3 (4) 3,7 91 2 ,93 56 47 ,1 +60 F8 40,5 4 188 34 189 Cassiopoiae 56 6,3  $\Lambda_{8}$ 5 ,04 126 - 139 124 244 200°+15,5 (4) 0,1 94 -- 64 б°,5 17 12 20 Cell 47 ,9 - 1 Ko ,92 191 1,1 Y ,88 11 4 17 3 248 114 214° 0,8 -23.115 (3)91 Ko 60,0 4 ,95 53 193 v1 Cassioneiae 49 ,1 +58 26 3,6  $\mathbf{Y}^{\mathbf{a}}$ 4 ,94 52 6 1.5 134 253 940 (3)2 30 Vai 17 2,2 92 Bop 20,1 2 y Cassiopeine 50 ,7 +60 11 ,25 199 ,48 0,4 12 28 - 6,8 13 W 2 144 264 ,83 100 29 1,7 92 3 50.4 245 -47,0 (5)Ko 4 v2 Cassiopeiae 50.7 + 5838 200 YO 24 4,8 4 ,82 79 62 138 265

33 Andr The Great Andromeda Nebula The parallax of 0",000003 is determined on basis of 1 Cepheld stars, 2 Novae, 3 Non variable stars observed in this object

Oh to 1h

					$O^{h}$	to 1h.								
1	2	. 3	4	5	6	7	8	9	10	11	12	13	14	15
203 269	μ Andromedae	51 <sup>m</sup> ,2	+37°	57' A2	2°,6 W	3 <sup>11</sup> ,94 4 ,08	153 + 103		+ 8	33 32	(4)	1,5	93°	-24°
206 271	η Andromedae 153	51 ,9	+22	52 G 5	5°,0 Y2	4 ,62 4 ,63	60 - 59	225	-10:	12 12	(5)	-0,2 3,5	94	-39
212 280	α Sculptoris 297	53 ,8	-29 5	34 B5		4 ,39 4 ,55	7	82°	+ 10,5				216	-85
218 285	Cephei 19	55 .0	+85 4	13 Ko	6°,2 OY <sup>2</sup>	4 .52	86 + 21	93°	+ 8,5	15	(3)	0,4	90	+24
226 294	ε Piscium 153	57 ,8	+ 7 2	21 Ko	5°,4 Y <sup>2</sup>	4 ,45	85 - 20		+ 6,9	19	(5)	0,8	98	-55
235 310	ψ <sup>1</sup> Piscium	0 ,4	+20 5	6 A2	2°,0 Y¹	5 .55	58 + 14	108° 十 56	- 3,1			1,0	96	-41
236 311	ψ <sup>1</sup> Piscium	0 ,4	+20 5	6 A0	1°,9 W	5 .82 5 .95	47 + 11	120° + 47	- 4	12	(u)	1,2	96	-41
245 322	β Phoenicis 324	1 ,6	-47 1	5 Ko	4°,3	3 ,35 3 ,57	45 - 22	252° - 39	- 1,3	24	(4)		258	70
255 334	η Coti 240	3 ,6	-10 4	з Ко	6°,0 Y <sup>8</sup>	3 ,60 3 ,62	246 - 17	123°	+11,3	33	(2)		109	-72
257 335	φ Andromedae 275	3 ,7	+46 4	2 B8	3°,0 Y1	4 .28	10	135° + 10	- 2:	10	(5)	0,7 0,7	94	-15
259 337	β Andromedae	4 ,1	+35	5 Ma	6°,2 OY3	2 .37 2 ,27	216	122°	+ 0,5	41 41	(5)	0,4 4,0	96	27
260 338	ζ Phoenicis 241	4 ,2	-55 4	7 B8		4 .13	27 + 27	15°	Var.				263	61
264 343	θ Cassiopelae 236	5 ,0	+54 3	7 A5	3°,7	4,52	230 + 101	95°	+11	24	(4)	0,8	93	- 7
270 351	χ Piscium 172	6 ,1	+20 3	0 K0	5°,6 Ya	4 ,89	21	73°	+15,7	26 12	(4)	0,3	98	-42
271 352	7 Piscium	6 ,2	+29 3	4 Ko	5°,7	4 ,70 4 ,64	+ 17 81 + 10		+30,5	16	(4)	0,7	96	-32
281 360	q Pisclum 158	8 ,3	+24	3 Ko	5°,5	4 ,64 4 ,73	47 - 21		+ 5,1	16	(6)	4,2 0,4	98	-38
288 370	" Phoenicis 346	10 ,6	-46	4 G0		4 ,88 5 ,17	687 + 309	74°	+11,5	10			252	<u>-71</u>
294 377	x <sup>4</sup> Tucanae 45	12 ,4	-69 <sub>2</sub>	4 F8		4 ,96 5 ,09	4:13	74°	+ 9,2		(1)	9,0 6,0	266	-49
300 383	v Pisclum 220	14 ,0	+26 4	4 A2	2°,1 Y1	4 ,67 4 ,92	26	+ 405 118° + <b>2</b> 6	Var.	160 21	(3)		100	-34
304 390	E Andromedae	16 ,4	+45	o Ko	5°,4 Y2	4 ,99	41	84 °	+ 5: -11,7	17	(3)	1,8	97	-17
310 399	ψ Cassiopelae	18 ,9	+67 3	6 Ko	6°,4 OY8	4 ,96 4 ,94	+ 27 86 + 69	67°	- 12,0	17	<u>(4)</u>	3,0 0,5	94	<del>-</del>
313 402	# Ceti 244	19 ,0	- 8 4	2 Ko	5°,6	3 ,83 3 ,82	228 - 226	201°	+17,5	13 27	(4)	4,6 0,9	119	-69
314 403	d Casslopeiae 248	19 ,3			3°,0 Y1	2,80	306		+ 9	26 55	(5)	5,6 1,2	95	- 2
321 417	ω Andromedae 307	21 ,7	+-44 5	3 F5	4°,1 Y1	4 ,96 5 ,05	356	+ 278 106°	+10	34	(4)	2,5	98	-16
325 424	α Ursae Minor 8	22 ,6	+88 4	6 F8	3°,8 Y1,6	2,12	44	+ 335 89°		12	(5)		90	+27
329 429	γ Phoenicis 449	24 ,0	-43 5	0 K5	6°.7	3 ,40 3 ,49	221	188°	-17,4 Var.	24	(2)	0,3	243	-71
335 437	η Piscium 231	26 ,1	+- 14 5	0 G5	5°,4 Y*	3 ,72 3 ,91	- 221 31	109°	+25.7 $+15.3$	15	(4)	5,1 -0,6	106	<del>-46</del>
336 440	o Phoenicis 425	<b>27,</b> 0	<b>-49</b> 3	5 Ko		3,96	+ 9 194 + 161	40°	<b>– б,</b> 5	31	(2)	1,4	251	-66
Bos	8 218. Abo 2 Urs. M	ìn. – F	Sors 314.	i Is variable	with on o	wallings of	+ 161	+ 109	1700	301		5,4		

Bots 218. Also 2 Urs. Min. — Boss 314. Is variable with an amplitude of Co.1. — Boss 325. ADS 1477. Copbold variable: 2m,3—2m,4; period 4 days; has a companion F0, 8m,79, 18",3,217°. The radial velocity varies in two periods viz. 4,0 days and 30 years. The range in magnitude is only 0,08 according to photoelectric measurements.

						1 <sup>n</sup>								
1	2	3	1	5	6	7	8	9	10	11	12	13	14	15
338 442	/ Cassiopeiae 260	27 <sup>m</sup> ,4	58° 44′	Kο	Ха 1г,9	4 <sup>m</sup> ,88 4 ,83	38 - 33		+ 6,8	14 13	(5)	0,4 2,8	96°	- 2°
350 458	v Andromedac 332	30 ,9	+40 54	GO	1°,4	4 ,18 4 ,28	418	205°	-28,6	79 78	(4)	3,6 7,3	100	-20
357 464	51 Andromedae	31 ,9	18 7	$\overline{K_0}$	6',0 Ya	3 .77	127	151°	1 15,9	21	(4)	0,7	99	-13
363	a landam	34 ,0	- 57 45	В5	_2°,0 -	3 ,78 0 ,60	94		19	24 45	(2)	4,3 -1,1	257	58
$-\frac{472}{369}$	7 Andromedae	34 ,7	<del>-</del> 40 4	-B8	2°,3	0 _89_ 4 _90	- 32 29	151°	- 15	45 8	_(1)	-0,5 0,6	101	-21
477 378	378 v Piscium	<u>3</u> 6 ,2	<del>+</del> 4 59	Ko	-W 6ª,6	5,15	ii	+ 27 273°	+ 0,1	21	(4)	1,2	ĪĦ	54
<u>489</u> 384	293 p Persei		+50 11	Bop	Y3 2°,7	4,66	11 33	- 18		20 14	(2)	1,3 -0,6	99	-11
496 391	#44 r Ceti	39 ,4		Ko	W 5°,5	3,65	+ 2	-  33	1,4	13 312	(5)	_ 1,8	142	<del>-71</del>
509	295 o Piscium			,	$\lambda_3$	3,68	- 38	-1922		310		10,0		-50
393 510	273	40 ,1		K0	5°,3 Y <sup>2</sup>	1,50 4,49		+ 25		14	(4)	4,2		
411 531	7 Ceti 352	44 ,7		Fo	4°,0 Y1	4 .77 4 .89	178 - 148	- 100		35 35	(1)	2,5 5,8		67
416 539	ζ Cetı 359	46 ,5	-10 50	Ko	6°,2 Y³	3,92	- 49 - 9	48		39	(2)	1,5 2,4	135	-67
419 542	8 Cassiopeiae 320	47 ,2	+63 11	B3	2°,7 W	3,44	43		7.9	11	(5)	1,2 1,6	98	F 2
421 544	α Trianguli 312	47 ,4	129 6	1.5	4º, 1 Y <sup>2</sup>	3,58	23° - 168		Vat - 12,6	40	(4)	1,6	107	-31
422 545	y Arietis N 243	48 ,0	-1 18 48	- **	2 <sup>1</sup> ,2 W	4 ,83 4 ,99	138			16 16	(2)		111	-40
423 546	y Arietis S	48 ,0	1-18 49	ЛОР	2 <sup>ι</sup> ,2 W	4 .75	13	143	- 1	14	(1)		111	-40
426	ξ Piscium	48",4	-1 2 42	ΤKO	5°,8	4 ,91	33	41	- <del> -</del> 30	18	(4)	1,1	121	-55
_549_ 428	290 β Arietis	49 ,1	+20 19	A 5	2°,6	4 .85	147		Vai ?	65	(5)		111	-39
553 429	306 ψ Phoenicis	49,0	-46 48	Mb	W	2 ,96 4 ,41	- 25 13	225	0,6 ° ⊹ 6,8		Ì	_3,6	239	-66
<u>555</u> 433	φ Phoenicis	50,2	43 0	139	1	4,40	98 52		-Vai	_		5,0	230	69
558 438	583 y Eridani	52 ,0	-52 7	G 5		5 ,20	72		+12 6,2	78	(2)	3.2	247	-61
566	241			-	20.#	3 ,87	+ 269	- 676		78	1	8,0		-36
441 569	λ A11et15 288	52 ,4		Λ5	3°,5 Y1	4 ,83 5 ,03	- 7	5 - 60		26 26		4,7		_
442 570	η <sup>2</sup> Hyd11 101	52 ,4	-68 9	Ko		4 ,72 4 ,83	+ 7		° - 16,2	30 28		4,9	261	-49
445 574	Phoenicis 597	53 ,2	<b>−47</b> 53	G 5		4 ,74 4 ,86	+ 13	4 85 2 - 104		36		2,5		-65
446 575	A Cassiopeiae	53,8	F-70 25	A 3	3°,6 Y1	4 ,61 4 ,77	- 6 3:	1 276	1	31	(7)	2,0	96	+ 9
449	50 Cassiopeiae	54 ,9	+71 56	Λ2	30,1	4,06	4.	5 301	Vai ?	25	(4)	1,0	96	- 11
580 453	υ Ceti	55 ,3	3 - 21 34	Ma	7°,2 O²	4 ,18	13	4 45	9-1-17,S	16	(3)		165	-71
<u>585</u> 459	g Poisei	55 ,0	5 + 54 1	.38	20,9	4 ,17	4			16		- 4,8 0,0	101	- 6
590 458	430		6 - 62  3		YG1 4°,1	5 ,21		8 + 30	1,9	10	)	3,0		_
591	162	33 ,	02	1		3,16		5 + 254		"	(00)	5,	1	

Boss 146 Visual binary ADS 1598 5m,0, 7m,5, period 63 years

					11	to 2h.								
1	1	1	4	3	6	7	8	9	10	11	12	13	14	15
463	α Piscium	_	+ 2°1	7' A3P	20,4	5*,23			Var.				124°	<b>−55</b> °
595	317	30 19	,	,	H'				+ 9.9				.=-	55
463	α Piecium	56 .9	+ 2 1	7 A2P	3°, 1	4 ,33	42		Var.	20	(3)	2,0	124	~ 33
596	317				W	4 ,12		+ 37	+ 93	20			232	-67
467	7 Phoenida	57 .7	-45 1	2 K0		4 ,96	56		- 30,6			3,6	-3-	
602	659			777		5 ,05	- 48 70		-11,1	30	(7)	5,0=	105	-18
468	I*	57, B	+41 5	1 Ko	5°,4 Y0	2 ,28	- 7		-11,1	26	(//	1,5		
603	395		144 5	1 A0	3.	2,40	72		-12"	-		-0,6	105	-18
469 604	7*Andromedae 395	57 .0	+41 3	AU	BGs	5,20	- 10					1,6		
474	* Fornacie	0.0	-29 4	7 AOP		4 .74	12		+18	$\Box$			191	-72
612	706	1 0 %	,	1100		4 ,90	+ 5	+ 11				0,1		
477	a Arlette	1 .5	+22 5	9 K2	5°,4	2 ,23	239	127	-14,1	53	(6)	0,8	113	-35
617	306				Y.	2,12	+ 17			51		4,1		-22
480	58 Andromedae	2 .5	+37 2	3 A2	20,8	4 .77	157		Var	24	(3)		107	-22
620	486				W	4 ,95	+ 71			24	121	5.7	100	-24
482	/ Trianguli	3 ,6	+34 3	1 A5	3*.3	3 ,08	160		+10,4		(6)		109	-24
622	381				Yı	3 ,29	+ 70		4.0	36	(0)	4,1 -0,2	406	-15
499	b Andromedae	6 ,9	+43 4	5 Kop	64,9	5,08	17		7-44,0	9	(2)	1,3	100	
643	447		-			5,00	- 10		Var	7	(2)	-1.2	124	-48
505	£1 Cetil	7 .7	+ 8 2	13 G5	5°,5	4 ,54	- 2		- 4,0		1-4	1.6		
649	7 Trianguli	44 .4	+33 2	13 AO	20,7	4 ,07	60			21	(2)		111	-25
517 664	397	112 14	T 33 4	L AU	Yi	4 26		+ 65	۱, ۴	21	,-,	3.2		
524	φ Rridani	12 .5	-51	59 B8	<del>-</del> -	3 ,78	8		+10	15	(1)	-0.3	241	-60
674	885	1		,,		3 ,92	- 3	6 + 73	1	15		3.3		
530	o Ceti	14 .3	- 3 2	26 Mdp	7°,0	2,00	23	7 181	1+622	13	(1)	-2,4	136	56
681	353				Og_	2,00	- 19	9 + 128				3.9		
545	65 Andromedae	18 .5	+49	50 K 5	5°,9	4 ,86	3		- 4,6		(4)		106	- 9
699	656		-		O <sub>2</sub>	4 ,82		7 + 30		7	1	2,3	-	-46
548	ð Hydri	20 .0	-69	7 42		4 ,26	5		+11	144	(4)	3,0	257	-+0
705	113				70.0	4 ,37	+ 3		Var	144	11		100	+ 7
550	¿ Casalopeiso	20 ,8	+66	57 ASP	3°,9	4 ,59	+ 1	5 344 8 - 13	+ 3,3	27	(4)	0,5		T ,
707 551	213 ρ Coti	24 4	-12	44 A0	2,6	4 .90	2			14	(2)		152	-62
708	451	21 1	-12	TT AU	W	5,08	- 2		\- ··	14	1-1	2,1		-
560	E Cott	22 .	+ 8	1 A0	20,5	4 ,34	3		Var.	16	(3)	_	129	-46
718	388	- "	]' ~		W	4 .49		2+ 32		17	(-,	2,3		
563	a Rriden	23	3 -48	9 B5		4,44	1	8 137	Var,				232	-61
721	637					4 .53	- 1	4+ 12	+29			0,7		1
575	o Cett	27 .	3 - 15	41 P5	3°,5	4 ,82	14	1			(2)		160	-62
740	449	_	-		Yı	4 ,91	- 14			34	-	5,0		
580	e Fornacia	29 .	5 -28	40 B9		4 ,95	1		Var	1	1	1 00	189	-66
749	819	-	-	7 80	r	5 ,12	-	3 - 16		+	101	2,2		51
604	8 Cett 406	34 ,	4-0	6 B2	2°,4 W	4 ,04		0 84 7 + 7		1 4	(2)	-1,0	139	-31
779 610	12 Perse	25	0 1 20	46 Go				$\frac{7+7}{194}$	Var.		(1)		113	-17
788	610	33 .	9 +39	TO   GO	4 ,5 Y	4 ,99 5 ,15		8 + 132		29		6,4		1 .,
611	s Bridani	36 -	0 -43	20 A2	1-	4 ,53			+20.		-	-	220	-62
789	814	"	1			4 ,67		18 + 82				4,3		
614	. Bridani	36 .	7 -40	17 KO	1	4 ,06		104	- 9,	2 31	(2)		215	-63
794	689					4 ,12		11 + 122		31		4,!	5	
617	# Persol	37 .	4 +48	48 F8		4 ,22	3:	10	+25,	1 85	(7)		109	- 9
799	746				Y	4 ,32	+ 19	7 + 291	1	81		6,9	2	
620	35 Arletis	37	6 +27	17 B3	2.1	4 ,58	4	14 163	+23	5	(1)	-1,9	119	-28
801	424	1			Y1	4 ,85	1—	6 + 13		5	1	0,	3	

Boss 463. Bleary ADS 16151 2",7, 307" Rach component is a spectroscopic binary No orbit determined for either just — Boss 468. Binary ADS 1630; period 55 years. — Boss 530. Variable: 18,7 to 58,5 in 332 days. Prototype for the Mint class; has a 10% composion 0",78, 428.9 (1926) evidently physically competed with a Cati.

2h to 3h.

					4	10 8",								
1	2	3	4	5	6	7	8	9	10	11	12	13	11	15
622 804	y Ceti 422	38 <sup>m</sup> ,1	+ 2°49	A2	2°,9 Y <sup>2</sup>	3 <sup>m</sup> ,58	210 210	- 19		36 36	(5)	1,4 5,2	137°	-48°
621 806	ε IIydrı 161	38 ,1	-68 42	В9		4 ,26 4 ,36	92 - 27	80°	+ 6			4,1	256	-45
627 811	л Сеіл 519	39 ,4	-14 17	В5	2°,7 W	4 ,39 4 ,55	16		+ 15,0	11	(1)	-0,4 0,4	160	-59
629	μCelı	39 .5	+ 9 42	~Fo	4º,0 Y¹	4 ,36	282 + 169	95°	+29,7	32 32	(2)		132	-42
- 813 631	359 7 <sup>1</sup> Eridani	40 ,5	-19 0	F5	4°,5 Y2	4 ,61	327	82°	+26,2	57	(i)	3,4	169	-61
634	39 Arietis	42 ,0	- -28 50	Ko	60,4	4 ,62	190	130°	-15,8	19	(5)		119	26
639	462 η Persei	43 ,4	+55 29	Ko	-6°,8	3 ,93	- 27 30	123°	- 1,8	18	(6)	$\frac{6,1}{-1,8}$	107	- 3
834 642	714 ζ Hydrae	44 ,0	68 3	A2	O <sub>8</sub>	3 .92 4 .90	70	47°	+ 4	9	(1)	1,3	254	-46
$-\frac{837}{643}$	169 41 Ariotis	44 ,1	+26 51	138	2°,6	4 ,99 3 ,68	132			9 22	(3)		121	-27
838 644	471 16 Persei	44 ,2	+37 55	Fo	W 3°,8	3 .75	-28	119	+ 14	21 32	(4)		115	-18
645	– 646 β Fornacis	44 ,5	- 32 50	Ko	Y1	4 ,45	190	+ 199 32°	+17,2	30 27	(2)		198	-63
646	1025 17 Perser	45 ,4	+34 39	K 5	7ª, 1	4 ,52	177   77	165	+ 13,9	27 13	(5)		117	-20
$-\frac{843}{650}$	527 τ <sup>2</sup> Eridani	46 ,5	-21 25	Ko		4 ,64	53		- 8,6	16	(4)		173	Ē1
850 653	509 τ Poisoi	47 ,2	+52 21	ĢσŢ	Y <sup>0</sup> ,9	4 ,80		140	Vai -	16	(5)	6,2	109	<del> 5</del>
854	641 R Hoiol	50~,6	5 - 50 18	A5 Md	~ X3	4,13 4,0—10,2		8	-1-60	-17		1,4	232	58
663	- 860 v Hydri	51 ,1	-75 29	K2	-	4 ,70	6:	2 271	4.7	15	(2)		259	-40
872 665	204 η Eildani	51 ,	5 - 9 18	-ICO	50,8	4 ,82	229	160	- 20,4	15	(2)		155	-53
874 668	- <u>553</u> π Perser	52 ,4	+39 16	A2	2º,5	4,05	$-\frac{13}{6}$	7 ± 183 143	+18	19	(2)		116	-16
879 670	681 24 Person		0 +34 47	Ko	W 6°,1	4 ,85	- : 6	$\frac{2}{3} + \frac{63}{281}$	- 36,0	19	(2)	3,6	119	~ 20
882 674	550 & Arietis		5 -1-20 56	   A2	OY2 3°,2	5 ,02	- 4	The same of the sa	-81	12		0,2	127	-32
887-888 679	484 λ Ceti		1 - 8 31	B 5	W, Y'	4 ,80	- 1		- 6} +11	13		-0.2	136	-42
896 680	#55_ O1 Endani		5 -40 42	A2	3°,8	4 ,91	+ 6	2 - 11		22		-0,1 0,1		-60
- 897 681	774 V <sup>9</sup> Eridanı		5 -40 42		30,8	3 ,63	+ 3	5 58	11,9		-	_2,6		
898 691	771 & Celi		1 + 3 42		6°,7	4 ,63	+ 2	0 - 75	-25,3	24	(5)	3,8	141	
911	419				O8 4°,5	2 ,85	- 6	6 + 41		22		2,3		
694 915	γ Persei			A3 J	X <sub>3</sub>	3,19		2 + 10		21		1,9		
697 918	k Persei 767		0 +56 19		5°,5 Y2	5 ,08 4 ,98	+ 4	0 - 58		19		4.		
696 919	τ <sup>3</sup> Eridani 1387		0 -24 1		4º Y1	4,16	15 9	0 - 120		28		5,0	)	
698 921	Q Persei 630	58 ,	8 + 38 27	МЬ	6°,6	3,4-4,3		3 128 2 169	+28,2	18		4,0		-16

Boss 674 The components of this binary, ADS 2251, are in the RHP system 5,55 and 5,25 - Boss 698 Tregular variable

1084 Appendices to Chap 4 K.Lundhark . Luminosities, Colours, Diameters, etc. of the Stars

3h.

1	2	3	4	3	6	7	8	9	10	11	12	13	14	15
705 932	Camiopeine 168	1º,0	+74° 1		2°,4 Y¹	4 <sup>10</sup> ,89 5 ,10	88 32	+ 82	+24 '	15 15	(2)	0,8 4,6		+15°
708 936	# Persei 673	1 .7	+40 34	B8	1°.9	2 ,1 2 ,47	- 9 - 5	+ 7	Var + 5,7	34 33	(3)	-0,3 3,1	116	-14
710	Persol	1 ,8	+49 1	Go	4°,1 Y <sup>3</sup>	4 ,17	1269	94		104	(4)		112	<b>- 7</b>
713	857 n Persol	2 .7	+44 29	Ko	5*,8	4 ,25	240	+ 838	+29	101	(6)	0,7	116	-11
941	631				Y	3 ,99		+ 233		21		5.9	4.10	
717 947	ω Persei 724	4 ,8	+39 14		5°,4 Y	4 ,82 ; 4 ,75	— <u>16</u>		+ 6,1	13	(4)	1,5	118	-15
718 951	d Ariotis	5 .9	+19 2	Ko	5°,9	4 ,53 4 ,56	152 + 111	92° + 103	+24,6	19	(5)	0,9 5,4	131	-31
723	a Pornacia	7 .8	-29 2	F8	5°,6	3 ,95	726	26°	-20,7	82 82	(3)	3.5 8.3	191	-57
963 730	4177 ¿ Arletis	9 ,2	+20 40	AO	20,6	4 ,95	79	198	+15	15	(5)	0,8	130	-29
972 739	527 ( Bridani	44 .0	- 9 1·	A3	3ª,8	5 ,13	- 66 45	+ 43 355°	Ver	15		4,4	159	-49
984	624				$\mathbf{Y}^{1}$	5 ,08	+ 35	- 29			14	3,2		+ 8
741 985	Camelopardalis 340	_			2°,3 W	4 ,76 5 ,00	+ 6	+ 10	Var. + 2,2		(1)	-0,7 0,2		
746 991	Persel 619	12 ,5	+33 5	Ко	7°,2 Y*	4 ,92 4 ,91	13	157°	+ 1.7	10 10	(4)	-0,1 0,5	123	18
752	n Ceti 818	14 ,1	+ 3	G 5	5°,0 Y1	4 ,96 5 ,08	282 + 254	70°	+19,3		(3)		146	-42
996 755	Arietie	14 ,3	+28 4	K5	6.6	4 ,72	27	186	- 2,1	13	(3)	0,3	126	-22
999 757	1 Person -	14 ,7	+42 5	3 A2	OY 2',9	4 ,61	- 18 58	+ 20 260°	Ver	13	(2)	-1,9 -0,9	118	-10
1002	750				W	5 ,19	- 50	- 24	- 6,6	15	(3)	3,8	179	<b>- 54</b>
759 1003	584	15 ,1			6*,9	3 ,95 3 ,94		+ 31		13		3,0		
764 1008	e Eridani 1028	15 ,9	-43 2	7 G5		4 ,30 4 ,38	3168 + 317	+3136	+86,8	219	(1)	11,8	216	<b>-55</b>
772 1017	α Poraci 917	17 ,2	+49 3	F 5	3°,4 Y1	1,90	+ 39	136	- 2,1	23	(4)	-1,4 -0,1	114	- 5
778	o Tanri	19 ,4	+84	1 G5	4,9	3 ,80	10	3 221	Var	17	(5)	-0,3		- 36
1030 780	511 Persel	20 ,9	+48 4	3 B5	Y* 2*,1	3 ,85	3	2 129	Var	15	(5)	3,9 -0,5	115	- 5
1034 781	920 Camalopardalla		+59 3		W 3°,8	5 ,18	+ 10	4 104	+11	8	(2)	2.5	109	+ 4
1035	660				Ă,	4 ,54	_	3 + 3		7		-2,6		
784 1038	£ Tauri 439	21 ,7	+ 9 2	3 B8	2',3 YG1	3 ,75 3 ,95	+ 1	2 125 6+ 70	Var	17	(1)	3,0		-36
786 1040	Camelopardalia 607	21 ,	+58 3	2 Aop	4°.5	4 ,76 4 ,86	1		Var - 8,4	2	(1)	-3,7 0,0	110	+ 3
790	34 Persol	22 ,	+49 1	0 B5	2',0 Y1	4 ,67	4	4 139		9	(6)	-0.6	116	- 5
791	945 Camalopardalla	22 ,	+ 55	7 A2	20,1	4 ,89	3	6+ 44 3 266		14			112	0
1046 795	o Persei	23	5 +47 3	9 Ko	₩ 6°,4	5 ,21 4 ,55		9 — 16 3 15	+14,9	14		0.1	116	- 6
1052	843				0	4 ,51	+ 1	7- 15		13		1,4		
1057	Persed		+43 3	Nova		0,0-13,	- 1	3+ 10	+ 6	7		-3,7	'	
804 1066	f Tauri 486	25 ,	+12 :	6 Ko	5°.3	4 ,28		1 + 14	+14	19		0,0	140	
806 1070	17 Erideni	25 .	6 - 5 2	15 B9	24,4 W	4 ,80	1		4 9	10		T 0,4	157	-45
10/0		<b>.</b>			. **	כלו ד	1 T 1	J		<u>.                                    </u>	, ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	. 01.		•

Boss 708. Algal or Algol. A triple spectroscopic system with pseiods of 29 days and 1,37 years, respectively

3հ.

3	ı	5	6	7	8	9	10	11	12	13	11	15
27 <sup>m</sup> ,6	-63° 18	S' F5		4 <sup>m</sup> ,80	519		+12,0				14°	-46°
28 ,2	- 9 48	· Ko	5°,8 Y <sup>3</sup>	3 ,81	972	271	+16,0	290	(5)	6,1 1	64	-47
29 ,4	1-47 5	В5р	2º,8 YG1	3 ,81	<u>- 573</u>	127	° <del> - 3</del> -	10	(3)	$\frac{8,8}{-1,0}$	17	- 5
29 ,4	-21 5	3 38	30,6	4 ,52	44		+15,0	13	(1)	$\begin{array}{c c} 2,5 \\ \hline -0,1 \\ 1 \end{array}$	81	-51
31 ,8	+ 0	G 5	- W 4°,4	4,49	536	206	°- -28,3	71	(4)	3,7 1	53	-40
33 .5	-40 3	5 Ko	Y2	- 4 .43 4 .58	- 509 44	191	° + 9,9	73	(2)	$-\frac{8,0}{0,9}$	12	<del>-53</del>
35 ,8	+47 2	B 5	20,5	4 .61 _	40	136	+13	18	(6)	$\frac{2,8}{-1,3}$	18	- 5
s 37 ,	+63	2 1.5, Ac		3 ,31	+ _11	163		13	(2)	0,4 1	09	+ 7
38 ,0	+31 5	B <sub>1</sub>	Y <sup>2</sup> 2°,7	5,00	20	3 + 14 5 157		12	(3)	0,7 $-1,5$ 1	28	-17
38 ,	3 -32 1	B5	Y(r1	3 ,99 4 ,93	- 4	+ 26 324	Var	8			97	<u>-52</u>
38 ,4	1 + 42 1	5 I 5	3°,8	3 ,93		7 — 6 276	+ 2,6 -13,1	19	(4)	0,3 1	22	- 9
38 ,	5 - 10	6 Ko	- Y1 5°,7	4,02	749	$\frac{7}{2}$ $\frac{-}{353}$	°(- 6,1	110	(4)	3,9,1	66	45
39 ,0	0, -1 23 4	8   B5p	3",0	3 ,71	+ 53°			110	(6)	-0.7 $-0.5$ 1	34	-22
39,	1 -37 3	8 K2	- W	4,64	- 1 11;			14	(2)	0,5 2	207	-51
	3 +24 1		2°,9	4 ,65	- 7		+ 6	15	(5)	4,8 -0,4 1	134	$\frac{ }{ -22 }$
39 ,	│ 8,	1 A0	W 2",6	4 ,59	4	7 + 16 6 141		11	(1)	2,8	104	+14
		4 135	W 20,9	4 ,84	- 5	7 <u>+ 46</u> 1 147	+10	19	(5)	-0.6	134	-22
ıs 40 ,	4   65 1	3 Ma	W 7°,1	4,16	-[	0 <del> - 54</del> 4 <b>28</b> 4		12	(3)	2,7 -0,5	108	+ 9
40 ,	4 - 23 3	9 B5	O <sup>3</sup>	4 ,58		$\frac{3}{9} - \frac{3}{157}$		12	(4)	-2,3 $-0,5$	134	-22
41 ,	1 -12 2	5 Ma	- W	4 ,42	- 1	0 + 58 9 30	]    - -45,7	11	(1)	3,1	168	-45
41		8 B5p	OX5	4 ,60		8 - 7		- 12 20	(6)	3,8	134	-22
42		3 1.8	G1 5	3 ,13 4 ,33	<u>- 1</u>	8 197	7°+ 7.1	17	(3)	3,2	185	-49
42	***************************************	7 Ko	Yı.	4 ,42	- 54 30	$\frac{8+38}{7}$	3 5° Vai	60 24	(2)	0,7	245	-43
- <del>4</del> 3	2 -23	5 B8	30,1	3 ,96		3 159		4	(4)	$\frac{6,3}{-2,0}$	135	-22
44		5 Ao	YG1	3 ,96		0 52		7 25	(a)	1,4	207	50
	9 - 37		-	5 ,56 4 ,86		$\frac{20+7}{32}$	7 3° +16	-	-		207	-50
- 45		30 K0		5,00		24 + 7°	9 6°+ 2,		1 ' '	0,3	205	-50
47		35 B1	2°,8	4 ,27	<u> </u>		3° +19,		(3)	3.5	130	<del>-15</del>
1''			Y¹	3 ,12		3 + 2		3		-0,5		1

Boss 856 Paygeta — Boss 860 Maia — Boss 869 Aleyone — Boss 877 Atlas A difficult binary 0" 43, 39°,4 1881, 885 Doubtless a physical pair,

8" to 4"

					8	to 4h.								
1	2	3	4	3	6	7	8	9	10	11	12	13	14	15
896 1204	Cemelopardalis 628	48=,6	+62°4	7' B9	2'.5 Y1	4 <sup>n</sup> ,87 5 ,12	+ 5	68° + 1	+ 6:	13 13	(3)	-1,6		+ 8*
899 1208	7 Hydrl 276	48 ,8	<b>-74</b> 3	3 Ma	6.0	3 ,17 3 ,36	124 + 38	+ 118	+15.7	17 17	(1)	2.7	256	<b>-38</b>
901 1211	32 Rridani   631	49 ,2	- 3 1	4 A	G <sup>2</sup>	6,33	160 + 22	+ 158				- 0,6 5,7	159	-39
901 1213	32 Kridani 631	49 ,2	- 3 1	4 G5	6,0 Y	4 ,95 4 ,73	+ 34 + 27	- 83° - 20	+26,9	12	(5)	0,4 2,5	159	- 39
902	r Brideni 1945	49 ,5	-24 5	5 B5	4 Y1	4 ,76	34	+ 33	Ver +23			2,5	187	-48
910	Persei 895	51 ,1	+39 4	3 B1	2°,2 W	2 ,96 3 ,14	+ 9	138° + 38	Ver - 6	5	(6)	-3,2 0,9	125	- 9
913	F Perseil 775	52 ,5	+35 3	0 005	5',2 Y1	4 ,05	20	142° + 20	Var. +67,4	1 2	(2)	-4,4 0,3	129	-12
915	7 Eridani 781	53 ,4	-13 4	B K5	7.0 Y	3 ,19 3 ,25	130	151° + 117	+61,5	23 23	(4)	0,0 3,8	173	<b>-43</b>
920 1239	2 Tauri 539	55 ,1	+12 1	a B3	2*,3 W	3,4-4,2 3,7-4,2	- 13 - 13	203° + 8	Var. 13,0	3	(2)		147	-28
923 1240	r <sup>0</sup> Eridani 2022	55 .7	-24 1	AOp	2 W	4 ,69 4 ,85	+ 3	+ 63	Ver +23,2	12	(1)	0,1 0,4	187	-46
930 1247	8 Reticuli 290	57 .2	-61 4	1 Ma		4 ,41 4 ,53	- 18	- 9	- 0,8			0,9		<b>-43</b>
932 1251	r Tauri 581	57 .8	+ 5 4	3 A0	YG1	3 ,94 4 ,15	- 3	+ 6	- 6	23	(4)	-1,8		-32
936 1256	A <sup>1</sup> Tauri 585	58 ,8	+21 4	9 Ko	5°,4 Y°	4 ,50 4 ,48	+ 47	+ 103	+ 9,9	19 18	(4)	4,8		-21
938 1261	1 Persol 1101			5 A0	3°,0	4 ,33 4 ,52	_	+ 32	+ 5.	16 16	(2)	0,4 2,2	_	0
940 1264	7 Reticuli 312		-62 2			4 ,46 4 ,58	+ 17	+ 14	- 5.9			1,2		-43
941 1266	r Reticuli 293		<b>-61 2</b>			4 ,81 4 ,92	+ 34	+ 104	+60,5		7.0	5,0		-43
947 1273	c Persel 939		+47 2		AG <sub>7</sub>	4 ,03	+ 10	+ 41	Ver + 4	11	(4)	2,2		- 3
963 1298	of Erkiani 764	7 ,0		6 F2	4*,3 Y¹	4 ,14 4 ,24	+ 60	<b>—</b> 52	+14	22 21	(3)	3.7		-37
966 1302	6 Horologii 1400		-42 1			4 ,85	<del></del>	+ 203	+37:		7=5	6,4		-45
967 1303	μ Persol 1063			9 Go	5°,5	4 ,28 4 ,33		1 + 30	Ver. + 7.8		(3)	1,7	_	- 1
970 1306	f Person 912		+40 1		6°,1	4 ,89		4+ 31	Ver. + 3	3	(2)	2,4		- 7 -28
972 1311	47 Tenri 659		+ 9	1 G5	X.	4 ,98 5 ,02		7 + 24	- 6,4	10	(2)	2,8		-28
981 1320	A Tenri 657		+ 8 3		2°,6 Y1	4 ,32		3 + 32	+17	10	(4)	-0,7 2,0		
986 1324	1156			3 A2	3°,0	4 ,57		8 + 71	Var,	16	(3)	4,0	121	+ 1
1325	780		7 - 7		Y1	4 ,48 4 ,52	408 396	2 + 899	-42,1	207		12,5	167	1
985 1326	1425		7 -42 : 4 +20 :			3 ,83 3 ,94	- 21 - 21 6	7- 31	+21,4	35 35 28	(2)	5,5		-45 -20
989 1329 994	724		1 -62		W	4 ,80 5 ,08	<u> </u>	4 + 38	+16	28		3.9	143	-41
1336		13,	-04	,3   65	4*,4	3 ,36 3 ,51	+ 1	0 32°	+35.5	22		2,6		-41

Blue 901 ADS 1939. 6",98, 347",2 (1922.5). The dynamic parallex is 0",002. Probably a physical system although the proper motions of the combinably — Ross 920. Refinalog bluary Feriod 3,933 days.

4h.

<del></del>		3	4	5	6	7	8	9	10	11	12	13	14	15
1	2						1						20.0	
995	y Doradus	1314	-51°44'	F 5		4 <sup>m</sup> ,36	202		+27	- 1	- 1	5,9	227°	-44
1338	1066		146 02	021	FC 4	4 ,48 3 ,86	+ 89   120	- <del></del>	+ 38,5	25	$(7)^{-}$		147	-23
1000	y lauri	14 ,1	+15 23	120	Y2 Y2	3 ,90	1	+ 77	7 30,5	25	(//	4,3	- ','	
1001	612 v <sup>4</sup> Eridani	14 ,1	-34 3	139		3,59	58		Vai				202	-44
1347	1614	17 11	34 3		1	3,77	- 4	+ 58	+17,6			2,4		
1003	d Persei	14 ,3	+46 16	B3	2°,8	4 ,89	45	148	1	7	(4)		124	- 2
1350	872				W	5 ,07	1 .	+ 44		_ 7	4.53	3,2	- = -	
1005	& Reticuli	14 ,7	-59 32	K2		4,12	177		+28,8	31	(2)		237	-42
1355	324				40 M	4,54	- 65		0 1 20 C	29	(7)	~ 5.7	146	-21
1017	di oi d Lauii	17 ,2	+17 18	KO	5°,5	3 ,93	+ 83	1	° - - 38,5	25 25	(//	4,2	140	2.
1373	712	To	147 42	- A5-	20,5	$-\frac{1}{4}\frac{.00}{.84}$	124		Vai	25	(5)		146	-21
1022	δ <sup>2</sup> or 64 Tauri 714	10 ,4	+17 13	A5	YG1	5,09		+ 89	-1-36,6	24	12/	5,3		
1026	z1 Tauli	19 ,4	+-22 4	A3	30,1	4 ,36	112			26	(5)		143	17
1387	642	1.,			YG1	4 ,57	+ 7	1 87		26		4,6		-
1027	28 01 67 Taul1	197!	+21 58	Fo	20,9	5,42	132			22	(1)		143	17
1388	643 J				Y¹			106	-	22	/ Je\_	6,0		
1029	δ <sup>8</sup> 01 68 Lauri	19 .	1-17 42	A2	20,4	4 ,24	109	-		29	(5)	1,5	146	-20
1389	719				YG1	4 ,48	12:			25	(4)	1.4		- 16
1033	ν <sup>1</sup> or 69 Ιαυιι 696	20 ,	3 十22 35	A 5	3°,6 Y1,5	4 ,40 4 ,56	- - 7	-		25	(-1)	4,8		
1392	d Endam	20 3	3 - 34 15	IX 5		4,06	7	-		15	(1)	-0,1	202	-43
1393	1664	20 1	_ Jil 13			4,11		3 + 58		15	, ,	3,0		
1034	71 Laui	20 ,	6 15 23	A.5	_3°,0	4,60	11	8 102		20	(6)		148	-21
1394	625				Y <sup>1</sup>	4 ,89	9:	1 .	-	15		5,0		
1036	# Tauti	20	9  -11 29	021	5°.3	4 ,91	3			10	(1)		148	-21
1396	697			1 750	Ya	4 195		6 31	°- -39,1	32	(5)	2,7	*******	i=18
1044	8 Janu	22 ,	8 +18 58	Ko	5°,4	3,63	12	9+ 80		31	(2)	4.0		.*
1409	640 gr Fauri	22	8 -1-15 44	KO	50,6	4 ,04	10	8 104	°-1-37.7	28	(6)		148	-20
1045	631	24 ,	0 7-13 44	120	OX3	3 ,99	+ 8			29	'	4,2		
1046	Da Tauii	22 .	9 + 15 39	Fo	20,9	3,62	10	7 104	Vai	33	(6)		148	-20
1412	632	,			W	3,73	- - 8	0 71	-1			3,8		-   -0
1054	lauri	24 ,	8 +15 59	A5	3°,0	4 ,84	11			27			148	-20
1427	637				Y1		8	7 + _ 77				5,5	163	-29
1063	45 Eridani	26 ,	8 - 0 16	KO	5°,3 OY2	4 ,97		3 180 2 - 3	)° ++ 16,2 3	1		-2,	_	27
1437	713			A.S	3°,3	4 ,97	10	- '		24	(5)		5 150	-20
1067	g Tauri 720	28	2 +14 38	1.5	yı	4 ,92		0 + 6		23		4,		
1444	v1 Eridani	20	6 - 29 57	Ko	40,4	4 ,59		100	1°- -20,	36	(1)	2,	4 197	-41
1453	1883	25	20 27		1	4 ,59				36		6,		
1074	c Perser	29	7 4-41 4	KO	60,2	4 ,46		19		. 9		1,	· . I	- 3
1454	1000			A 3	OX	4,41		4 2		~	-	1,	5 149	-19
1077	a Lauri	30	,2 -1-16 19	IX 5	60,3	1,06				70		2,		, , , ,
1457	629				OYa	1 ,08	ww	18 + 20 56 13		21			9 154	1 -23
1076	d faum	30	,2 + 9 57	A 3	3°,2 Y1	4 ,38 4 ,51			4 28,	. 1		3,		
1458		- 21	$\frac{1}{3} - 3^{-3}$	B2	20,7	4 ,12		2 18	0° Vai	-	(3)		4 16	8 -30
1079 1463		31	12 - 2 23	22	w	4 28		1	2 -+15,	4 !	5	-4	4	
1080		31	7 -30 46	Ko	5°.7	3 ,88		59 26	6° - 3,	8 18			2 19	8 40
1464						3 .93		10 - 5	8	13	3	2	7	_
1081		31	,8 -55 15	AOp	3º,8	3 ,47	,		2°-+25,	6			23	0 -41
1465	663			-		3 ,62			6° Vai	⊥ 1 3	1 (5)		8 15	3 -21
1087		32	,6 +12 19	A3	2°,9 W	4 ,30			5 -1-54		1 (3)		.4	-
1473	618 058 1026, 1027 Pro	-	1								•	•		•
13	ass 4026, 4027 Pro	bably a	physical pair	Also inc	minde of	run Tuntas	ettiatat.	- Tanap )	of a mill					

Boss 1026, 1027 Probably a physical pair Also member of the Taurus cluster - Boss 1076 Eclipsing binary

## 4088 Appendices to Chap 4 K LUNDMARK' Luminosities, Colours, Diameters, etc of the Stars

4b,

1	2	3	4	Т	5	6	7		1	9	10	11	12	13	14	15
1090 1479	o⁴ Tauri 666	33-,5	+15°	43'	A3	2°,9 Y1	4 <sup>th</sup> ,85 5 ,00		56 +	104°	Var +22	24 23	(4)	1,7	149°	19°
1091 1481	Eridani 933	33 .6	-14	30	Ko	5°,6 OY <sup>2</sup>	3 ,98 4 ,01	17		205	Var +41,8	36 36	(2)	1,8 5,2	179	<b>-35</b>
1101 1492	R Doradus		-62		Мо		Var 4,8-6,8	+ 2	28 —	226°	+26,1			5.3-7.3	239	<b>-39</b>
1105 1496	54 Eridani 988 z Tauri			52	Ma Bs	6',8 O'	4 ,54 4 ,53 4 ,33	- 6	)4 52 +		-33.5	13	(2)	4,4	185	-36
1107 1497 1110	739	37 .3	+21	3	1/2	W	4 ,33 4 ,50 4 ,52		13 2+ 59		+ 9.6	9 9 27	(4)	-0,9 1,1	213	-14 -41
1502	1587			26	B5	20,5	4 ,63		12 - 22	169	- 1,3 Var,	27	(4)	5.7	168	<del>28</del>
1520	876 a Camelopard		+66		Во	W 3°,0	4 ,34	_	9		+16 Var	10 -6	(3)	0,9		+15
1542	358 st Orlonia		+ 6		F8	₩ 4°,0	4 ,56 3 ,31		9-	87°	+ 6,0 +25,0	125	(4)	-0,8 3,7		<del>-21</del>
1543	762	45 ,1	+ 8	44	Λo	3º,0	3 ,45 4 ,35		38 <del>+</del>	191	Var	123	(1)		157	<del>-20</del> -
1544	2 Aurigno	45 ,9	+36	33	K2	₩ 6º,6	4 ,60 5 ,04 4 06	- :	19+ 26	211	-16.7	14	(1)	-0,8	134	<del>-</del> 3
1551 1147 1552	952 n* Orionia 745	45 .9	+ 5	26	В3	2º,5 W	4 ,96 3 ,78 3 ,98		7 0+	214	Var. +23.3	14	(5)	-3,1 -3,2 -2,0	161	-23
1149 1556	o¹ Orlonia 1777	46 ,9	+14	5	Ma	7°,6	5 ,19 4 ,98		59 21 →	180		10	(a)		153	-17
1153 1560	o Erldani 1068			37	Fo	4°,6 Y1	4 ,45 4 ,59		27 6-	315° - 26		30 30	(1)	1,7	172	-27
1159 1567	π Orionia 810		+ 2		B3	2°,1 W	3 ,87 4 ,04		4+	225°	+23,4	5	(6)	-2,6 -3,1		-23
1161	7 Camelopard 829 n <sup>1</sup> Orionia		+53		A2	2°,7 Y¹ 3°,2	4 ,44		12	305	一 7.9	21	(2)	-0,2	122	+ 8
1163 1570 1167	683		+10	0	K2	60,1	4 ,74 4 ,94 2 ,90		45 0⊣ 28	158	+ 4	17 17 25	(3)	5,6	157	-19 - 5
1577	886		+13	21	Ko	Y* 5°,9	2 ,89	+	1   02	- 28 233		25 19	(3)	0,1	155	- 16
1580	740 4 Aurigao		+37	44	Ao	2º,5	4 .25	_	98- 15		Var	19	(1)	4,3	135	- 1
1592	n Orlonda		+ 1	33	Ko	7.0	5 .16	+	6	211	+ 6	32	(3)		165	-23
		54 .5	+60	18	Gop	5°,1	4 ,66	-	13	171	- 1,6		(5)	-1,4 -2,3	117	+12
1603 1187 1605	856 s Aurigne 1166	54 ,8	+43	41	F5p	4°,3	3,31-4,0	+	14	159 159	Ver - 1,0	7 7	(3)	-0,2	132	+ 2
1189	S Eridani 1047	55 .3	-12	41	Fo	4° Y1	4 ,85 4 ,99	1	07	155 - 105	-15	22 22	(1)	1,6 5,0	180	-29
1190 1612	( Aurigae 1142	55 .5	+40	56	K0,B1	6°,6	3 ,94 3 ,90	+_	32 3-	160 + 32	Var	24	(3)	-0,9 1,5	133	+ 1
1192 1617	y Eridani 948		- 7		Bs	2',9 W	4 ,81 4 ,98	+	10 5-	- 9		5 5		-1.7 -0.2		-26
1194 1620	751		+21		A5	3*,1 W	4 ,70 4 ,90	+	82 52-			16 14		0,4 4,3		-11
1193 1621	Leporis 990	57 .	-20	12	В9	2°,4	4 ,99 5 ,16	+	41 14		424			3,1	-	-32 Prob

Boss 1901. Long period variable, period 345 days. — Boss 1187. Long period solipsing binary, period 27,1 years. — Boss 1189. Probably not a variable.

4h to 5h.

					4"	to 5".									
i	2	3	4	5	6	7	8		9	10	11	12	13	11	15
198 628	Lepous 1975	58 <sup>m</sup> ,1		K0	O2	5",01 5 ,00	- 12: - 4	1+	113	- -27,8			5,4	194°	-34°
202 637	9 Aurigae 1024	58 ,8	+51 29	1.0	3°,9 Y1	4 ,99 5 ,15	17	8 5 l-	185° 169	- 1,4	47	(3)	3,2 6,2	125	+ 8
203	11 Orionis	58 ,9	+ 15 16	B9	2°,3	4 ,65 4 ,95	4	AM CT	152°	Vai +15,8	14	(1)	0,4	154	14
638 204	η Aurigae	59 ,5	+41 6	B3	10,8	3 ,28	-8	1	158°		14	(5)		133	+ 2
$\frac{641}{208}$		8, 0	-35 37	Īςō	B <sub>1</sub>	3 ,48 4 ,62	12			<u>+</u> 11,0	18	(2)	0,9	206 -	<del>-</del> 35
6 <u>52</u> 211	2089 ε Lepo115	1,2	-22 30	IC 5	6°,2	4 ,64		32 <u>+</u>	99 _159°	4-0,9	18 28	(4)		191	-32
654 218	1000	2,3	<del>-49</del> <del>13</del>	"K5"	OX3	3,34		19¦-( 15	— <u>ში</u> 78°	+36,0	28	(a)	-2,6	  223	-36
663	1662		1		20.0	5 ,02		24 +	26 228°		46	(6)	$-\frac{2,6}{1.2}$	173	-23
220 666	β Isridani 1162	2,9		A3	3°,2 V1	2 ,92 3 ,12	- 11	13 -	33		45		_3.3		
225 671	ζ Doradus 735	3 ,8	57 37	1 8		4 ,76 4 ,89	I1  -  8	13  34 +					5,0	233	<b>-36</b>
227 676	15 Orionis 752	4 ,0	F15 28	10	40, 1 Y1 5	4 ,86 5 ,08	+ 1	1 1	158	+31,4	13	(1)	0,1	155	-13
231 679	7 Fridam 1040	1 ,4	- 8 53	B2	2 <sup>d</sup> ,6 Y(,1	4,31 1,54		9	160°	Va1	7 7	(3)	-1,4 0,7	177	25
236	μ Amigae -	6,0	+38 22	Λ3	3°,0 Y1	4 ,78 4 ,99		76 33 +	1916	-	40	(3)	2,5	136	+ 1
689 239	1063 t Lepous	7 .:	11 59	138	20,7	4,54		32	116		10	(2)	-0,5 3,1		-20
696 <b>2</b> 40	1095 Θ Oπonis	8,	- 2 45	Ko	_W 6°,3	4 ,69	- [ -	17		Vat	19	(2)	0,1		-19
698 241	888 μ Lepons	8,4	- 16 19	Aop	OY'	3 ,30	-	7] <u> </u> 49	125	1十38,8 十27,7	19	(1)	$-\frac{0.5}{0.4}$	184	-27
702 242	1072 x 1 epons S	8 ,		138	W 2°,8	3 ,48	-l '	16 <u> </u> 22	47 236	- -27	26 6	(2)	1,8		-26
705	1092		1		W 3°,3	4 ,60	-	22 - 37	1	-1-30,2	87	(4)	1,2 -0,1		-i- 6
246 708	& Aurigne	9,		GO	A <sub>3</sub>	0,33	+_"	() -	437		85	1	3,4	-	
250 713	β Orionia 1063	9,	7 - 8 19	138p	1º,2 W	0 ,34		() -		+23,6			-9.7	-	
258 726	16 Aurigae 1000	11 ,	6 +33 17	Ko	6°,3	4 ,81		89 32	159	Vai 29,4	20 19	1 '- '	6,2	2	
259	λ Aurigae	12	1 + 40 1	60	4°,6 Y2	4 ,85	8	43 196 -	141	4-66,6	74		9,1		+ 3
729 262	1248	12	8 ~ 6 57	35	3°,1	3,68		17	246	0 1 18	10	(3)	I,: O,:	176	-23
735 270	o Columbae	13	-35 υ	Ko	6°,5	3 ,84	3	355	0 167	0   21,2	32	(2)	2,4	1 200	-33
743 269	2214 Doradus	13	9 - 67 18	Ko	-	4 ,92		48	= 57 353	o Van	32	(2)		1 244	-34
744	404	1	0 -13 17		2°,6	4 ,90		2	F 44				3.3	2 182	24
277 756	1127				W	4 ,45	_ <del>-</del>  -	20	<b>→</b> 3		12		3,		
281 762			,2 -21 20		2°,8	4 ,73 4 ,90		20	- 0	) }	12	2	1,	2	
284 765	o Orionis	16	,7 - 0 29	.133	2°,5	4 ,81		5	+ 2		1 :	5) _	-1,	9 170	
289	m Orionia	17	,6 + 3 27	133	2°,5	4 ,99 5 ,20		7 2		)° +-18	1	5   (2) 5	O,		
770 299	e Ortonis	19	~ 7 53	Ko	6°,3			42	207			(1)		7 178	3 -21
784	1064 loss 1220 Member o	f Uran N	I Infor Cluster?	- Boss 1:						ents ns c		1		dotern	ination

Boss 1220 Member of Ursa Major Cluster? — Boss 1216 Capella Interferometer measurements as compared with the determination of orbit on basis of variable radial velocity lead to a parallax of 0",0632 which probably is the most accurate parallax value so far determined any star

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1	П	•

						Dn							
1	1	3	4	5	6	7	8	9	10	11	12	13	24   15
1301 1788	7 Orionis 1235	19 <sup>m</sup> ,4	- 2° 29′	Bı	2*,3 W	3 <sup>3</sup> ,44 3 ,64	+ 6	80° + 1	Var +19,5	10	(5)	-2.7	172  - 19
1302 1789	25 Orionia 1005	19 ,6	+ 1 45	Взр	2*,6 W	4 ,73 5 ,04	21 -14	209° + 15	+18,9	8	(2)	-0.7 1 3	_
1303 1790	y Orlonia 919	19 ,8	+ 6 16	B2	1',7 W	1 ,70 2 ,01	20 -11	200° + 17	+18,7	14 13	(6)	-0,2 -1,8	165 -15
1304 1791	<i>β</i> Тенті 795	20 ,0	+28 31	B8	1',6 W	1 ,78	180 + 4	169° 十180	+11	33 32	(4)	-0.7 -3.1	145 2
1315 1810	o Teurl 847	21 ,6	+21 51	Вз	1",8 W	4 ,83 5 ,05	17 + 8	140° + 15	+15,8	7	(4)	10	
1314 1811	9 Orlania 982		+ 3 0	В2	2°,2 Y1	4 ,66 4 ,87	+ 7	197° + 12	Var +12,0	4 5	(7)	0,4	108 , 10
1323 1829	# Leports 1096	24 ,0		Go	A. 6.	2,96 3,07	94 -50	176° + 80	~13,8	14	(3)	-1,8 2,8	101 26
1327 1834	31 Orionis 913		- 1 11	K5	7.2	4 ,97	28 + 3	159° + 28	+ 7.9		-	2,2	172 17
1331 1839	A Orionia 939		+ 5 52	В3	2.7 W	4 ,32 4 ,50	38 + 4	169° + 38	+15	14 14	(4)	2,3	165   14
1841	T Aurigae 923 a		+30 2	Pec Nova	Ver	4,4-14,7	- 2	+ 2	-2187	0,5	(1)	-7.1 -3.0	~~~
1333 1843	χ Aurigne 1024		+32 7	B1	3°.5 Y1	4 ,88	+ 4	160	- 0,2	3	(2)	1,0	1
1335 1845	119 Tauri 875		+18 32	Ha	7',8	4 .73	+ 8	132	+22,3	3	(3)	-2,9 0,3 -3,6	154 - 7
1339 1852 1340	ð Orlonis 983 v Orlonis		- 0 22	Bo B3	1,9	2,48	+ 1	146° 4 166°	+19.9	6	(7)	-4.5 -1.9	178 - 19
1855	1106		- 7 23 -35 33	Ko	2°,1 W	4 ,64 4 ,81 3 ,92	12 - 1 56	+ 12 151°	+16,6	5	(4)	0,0	208 - 30
1862	2348 & Leporle		-35 33	Fo	3*,0	3,96	55 3	- 6 18 <sup>8</sup>	- 3,8 +24.5	17 17	(4)	2,7	189 24
1865	1166		+ 9 25	Во	Y1 20,5	2 ,87	+ 2	- 2 187°	Var	17	(5)	-4.8 -2.5	163 - 11
1876	877		+ 9 52	20	YG 2.6	4 ,70	- 2 12	+ 8	+33,2 +33	4	(5)	-10	162 - 11
1879	879 A <sup>1</sup> Orlonia		+ 9 52	005	W 20	3 ,69	+ 2	+ 12	+35	7	(3)	-1,1	162 - 11
1880	879 Orlonis		- 6 5	Bi	V*	5 ,58	4	146	+29				177 - 19
1886 1362	1233 Orlonia	30 ,1		<b>B</b> 1	B1 2.3	4 ,67	+ 2	~ 3	+28		_	-1,4	177 - 19
1887	1234 c <sup>1</sup> Orienta		4 54	B3	YG 1	4 ,87	+ 5	- 5 153°	Ver	5	(3)	-9.3	176 - 18
1892	1185 Drionis	30 ,4			W 3°,0	6 ,84	+ 0	+ 2	+28	3		-3.9 -1.9	176  - 18
1893 1363	1315 Orlonis				OR1	7 .93	+ 7	- 2	Var	3	`	-0,8	
1894	1315		- 5 27	Oo 5	Υı	5 ,36	-		-24 Var				176 -18
1895	1315 Orlonia		- 5 27			6 ,85	-		+23 Var	-			176 -18
1896 1366	1315 4 Orlonia	<u> </u>	- 5 59	Oo 5	20,8	2 ,87	7	1240	+27	5	(2)	-3,6	
1899	194   1304, Also wayne	1 - 4	lan Bar	1222 1	W	3 .09		+ 2	1	5		-3.6	, ,

Hom 1304. Also moved y Arrigan. — Hom 1327 Variable star = CJ Orlonia. — Bozz 1339. Has a comparison 53" dist. 6m,87 — Bozz 1337 Leading star in an open cluster — Rosz 1364, 1362. No doubt a physical pair — Bozz 1363. The Traparism A sociétée systems or rafter part of an open stellar chaster. Bent value for the parallax seems to be 0",0018. Express makes the total magnitude 4,96 which corresponds to the total magnitude of 5,18 according to Harvard determinations. The total magnitude of the actual is 2m,9.

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 $5^{h}$ .

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1370 1903	ε Orionis 969	31 <sup>m</sup> ,1	- 1° 16′	Во	1°,6	1 <sup>m</sup> ,75 2 ,03	2 - 0	180° + 2	+25,4	9	(5)	-3.7 -6.7	173°	-15°
1373	φ* Orlonis 898	31 ,4	+ 9 15	ĪζΟ	6°,0 Ya	4, 39 4, 30	321 + 45	$\frac{1}{163}$ ° $+318$	+99.3	28 28	(4)		164	-10
1375 1910	L'Tauri 908	31 ,7	+21 5	Взр	1°,9 W	3 ,00	28	174° + 28	Var. +16,4	10 7	(4)	-2,8 0,2	153	- 4
1384 1922	# Doradus 487	32 ,8	-62 33	F5p	ნ°,3	3 ,81 3 ,94	16 + 10	330° + 12	- <del>-</del> 7,4			1	239	-32
1388 1928	125 Tauri 902	33 ,5	+25 50	133	1°,5 W	5 ,00 5 ,33	+ 44 + 28	135° +- 34	Var. 14,8	5	(3)	-	149	- 1
1389 1931	σ Orionia 1326		- 2 39	Во	2°.7 W	3 ,78 3 ,97	+ 0	— 1	Var. +28,4	3	(6)	-3,2 -6,2	175	-16
1391 1934	ω Orionis 1002		+ 4 4	Взр	2°,8 W	4 ,54 4 ,74	+ 6	72° - 1	Var. - -22,0	5	(3)	-2,0 -1,6	168	-12
1392 1937	d Orionis 1142		- 7 16	A 3	3°,7 Y¹	4 ,88 5 ,04	50 - 26	199° + 42	Var.	17 17	(2)	1,0 3,4		t8
1396 1946	126 Tauri 841	1	+16 29	В3	2°,1 W	4 ,87 5 ,09	+ 10	155° 十 29	- -28:	8 7	(5)	-(1,9) 2,3		- 6
1398 1948	ζ Orionis 1338	35 ,7		Во	1°,6 W	2 ,05 2 ,14	+ 7	131° 4- 9	- <del></del>	5 6	(7)	-4,1 $-2,9$		<b>— 15</b>
1398	COrionis 1338		<b>- 2</b> 0		YG1	4 ,21			+13		-5:, -	— 1,3 — 0,6		15
1399 1952 1401	Orionis 1004		- 1 11	B3	1",8 W	5 ,00 5 ,17	14 - 13	236° + 5	+26,1	ი ი	(3)	- 1,1		-15
1956	α Columbae		-34 8	B5p	3°.5	2 ,75 2 ,96	- 35 - 32	173° - 15	39	25 24	(2)	-0,4 (),5		-28
1982	y Leporis 1210 y Leporis		-22   27 $-22   29$	G 5	6°,2	6 ,41	451 365	218° +275	- 9,2		(2)		195	-23
1983	1211 J	40 ,3		IÇO -	4°,6 Yª	3 ,80	468 412	216° +220 223°	9,2	115	(3)	_7,2	195	23
1995	1418 & Leporis		+39 9 -14 52	Λ2	5°,0 Y <sup>8</sup> 3°,4	4 ,64 4 ,64 3 ,67	- 35 - 26		19,5	14 14 46	(5)	-2.4		-1- 7
1998	1232 132 Tauri		+24 32	K <sub>0</sub>	YG1 6°,0	3 ,84	- 16 36	- 6 174°	+13	46	(1)	-0,1 2,1	187	-20
2002 1435	970 * Orionis		- 9 42	B0	Y <sup>3</sup>	5,00	+ 1	-J- 36 149°	+15,0	27 26	(5)	2,8 -2,8		-17
2004	1235 134 Tauri		+12 37	В9	W 2°,3	2,44	+ 2	- - 6 207°		10	(2)	-3.8	162	- 6
2010 1439	912 v Aurigac		+37 16	Ma	6°,9	5 .11	- 15 52	+ 25 137°	+37.9	10	(3)	2,2	141	+ 6
2011	1336		+39 7	Ko	0 Y <sup>0</sup>	4 ,90	$+\frac{33}{8}$	+ 40 320°	- <del> -</del>  - - - - - - - - - - - - - - - - -	10	(6)	3,6	139	+ 7
2012	d Dorndus		-65 46		Ya	4 ,18	- 5	G 285"	- 3:	17		-1.3	243	-31
2015 1446	496 β Pictoris		-51 6	Λ3		4 ,62	+ 38	+ 7 4°		58	(ຄ)	2,5	225	<del>-30</del>
2020 1453	1620 £ Aurigao		+55 41	Λ2	2°,9	4 ,07		+ 90 326°	-12	10	(4)	3.7		+16
2029	1027 136 Tauri		+27 35	Λ0	W 20,3	5 ,14	- 7 22	- 12 146°	Var,	9	(2)	0.7	149	+ 2
2034 1456	899 ð Leporis		<u>20 53</u>	Ko	Y1 6°	4 ,76	+ 11	+ 19 160°	$\frac{-16,1}{+99,6}$	14 66	(7)	1.3	193	-21
2035	1211 56 Orionis		1 50	IX ()	Y <sup>9</sup> 6°,2	3 ,92 5 ,01		+696 180°	+10,3	55	- (1)	8,1	_	-10
2037	1151	1			Ya	4 ,99		+ 11		6	, ,,,	0,2		

Boss 1384. Cephold variable 4m,2 to 5m,6; period 9,8 days. — Boss 1398; H.R. 1948, 1949. Λ visual binary, 2",5, — Boss 1419, 420. Α wide pair 95", 350°.

6h.

						6ª.								
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1459 2040	β Columbae 2546	47 <sup>m</sup> ,4	-35°4		4",3	3",22 3 ,30	397 +131	7° +377	+89,1	29 29	(3)	0,5 6,2	209°	
1460 2042	7 Plotoris 946	48 ,0	56 ·	12 Ko		4 ,38 4 ,50	96 - 75	135° - 60	+17.0	17 17	(2)	0,5 4,3	231	<del>- 30</del>
1461 2047	z <sup>1</sup> Orlonia 1162	48 ,5	+20	16 F8	5',0 Y	4,62	208 189	243° + 85	-14,1	87 89	(5)	4,2 6,2	156	- 1
1462	Plotoris 794	48 .7	<b>- 52</b>	8 Ko		4 ,98 5 ,08	90		+ 1,2			4,8	227	-29
1467 2056	A Columbae 2599	49 .5	-33	50 B5		4 ,89 5 ,04	28 + 15	2° + 24	+30	14	(1)		207	-25
1468	a Orionia 1055	49 ,8	+ 7 :	23 Ma	6,5	0 ,92	29 + 28	74°	+20,8	12	(5)	-3.7 -1.8	168	- 8
1472	& Aurigae 970	51 ,3	+54	17 Ko	_	3 ,88	153 + 83	145° +129	+ 7.7	25 23	(4)		127	+16
2077 1475 2084	139 Tauri 1052	51 ,8	+25	57 B2		4 ,90 5 ,07	- 4	194° + 3	+ 8,5	3 7	(5)	-2,7 -2,1	152	+ 2
1476 2085	η Leparle 1286	51 ,9	14	11 Fo		3 .77	138	343° -135	- 1,6	49 48	(3)		187	-17
1478 2088	# Aurigao 1328	52 ,2	+44	56 A01		2,07	47	264° + 4	- 18,7	41 38	(6)			+12
1479	Aurigae	52 .5	+45	56 Ma		4 ,59	+ 8		+ 0,9	6	(3)		134	-12
1482	Ø Aurigno 1380	52 ,9	+37	12 A0		2 ,71 2 ,90	105	149°	+29	34 32	(6)	_	142	+ 8
1486	Doradus 498	53 ,4	-63	8 Kc		4 ,53	562 - 118	14° +551	+24.7	21	(1)		239	-30
1490	γ Columbao 2612	54 ,0	-35	18 B3		4 ,36	+ 4	297°	+24,2	7	(1)		208	-25
1494 2113	Orionia 1256	55 ,1	- 3	5 K	5°,5	4 ,68 4 ,67	84 + 13	169° + 83	+25.9	27 28	(2)		177	-11
1497	n Columbae 2266	56 ,1	-42	49 K		4 ,03	33	140° - 23	+17.9	13	(2)		217	-26
1501	μ Orlonia 1064	56 ,9	+ 9	39 A2	3°,6	4 ,19	34 + 18	148*	+42	33 32	(3)		166	- 5
1503 2128	3 Monocerotis 1349	57 .1	-10	36 138		4 ,97	+ 1	- 9°	Var +39	6	(2)		185	-15
1508 2134	1 Geminorum	58 ,0	+23	16 G		4 ,30	108	184° +108	Var +20	32 31	(5)	_	155	+ 2
1507 2135	z <sup>a</sup> Orlonis 1233	58 ,0	+20	8 B2	_	4 .71	+ 8	148° + 13	Var +18	6	(3)		157	0
1522 2155	J Leporis	1,6	-14	56 A		4 ,67	24	343° 23	+32	19	(1)		189	-15
1525 2159	+ Orionis 1152	1 ,5	+14	47 B:		4 ,40	37 + 10	166° + 36	Var. +22,1	7 7	(3)		163	- 1
1550	f <sup>1</sup> Orlonia 1035	6 ,2	+16	9 B		4 ,92	+ 7	165° + 23	Var. +28	8	(2)	_	162	0
1548	& Orlonia 1187	6 ,:	+14	14 B;		4 .35	35	165° + 34	+24,1		(3)	-0,9	163	- 1
1556	Camelopardalis	7 ,	+69	21 A		4 ,73	109	174 0	Var.	13	(1)		1113	+23
1558 2212	8 Pictoria	8 ,	- 54	56 B		4 ,84	24	250	Var,	1.3		1,7	230	-27
1561	7 Geminorum 1241	8 ,	+23	32 M	6.9 OY	Var	65	255°	+19,4	13			1 156	+ 4
1565	M Aurigao 1154	9 ,	+29	33 K			274		+20,5		(5)		150	+ 7
,		•	•		. ~						-			,

, Boss 1468. Beinigsum. Variables (m.,co-om,20. The variations in the light seem to be committed with the variations in the Chamete, as derived on books of interferometer measurements. On basis of that sammption a pulsation persident of 0",007 has been derived. — Boss 1472 Mesuher of Ursa Major Clusies. Religating binary — Boss 1561. Long period variables. Period 231,4 days.

6h.

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1570	y Monocerotis		- 6°11'	Кo	6°,5 Y <sup>8</sup>	4 <sup>10</sup> ,09 4 ,14	21 - 2		- 5,2	16	(2)	0,1 0,7	182°	-10°
2227 1575 2238	1469 2 f yncis 959	<u>10</u> ,8	+59 3	AO	2°,1	4 ,42 4 ,63		347°	-4	24	(4)		123	- <del> -2</del> 0
1580 2244	Canis maj	Ī1,1	-13 41	B9	2', 1 W	4 ,99 5 15	7 - 7	- 08°	<del>-</del> 33		-	-0,7	189	-13
1579	_η² Doradus	11 ,1	65 34	Mb	~	4 ,88	112 + 18	+111	-34,5	6	(a)	1,0 1.5	243	-28
1587 2256	и Columbae 2800	13 ,0	-35 6	Ko		4 ,51 4 ,53	76 36	+ 66	<b>⊢24,5</b>	13	(2)	0,1 5,1	210	-21
1601 2282	ζ Canis maj 3038		- 30 1	В3	3°,0 W	3 ,10 3 ,30	+_ 1		34	6	(1)	-2,4	205	-18
1601 2286	μ Gemmorum 1304		+22 34	Ma	73 00'0	3,19	128 + 72	106	+ 54,4	16	(5)	-0.8	157	+ 0 -13
1609 2294	β Cams maj 1467		3 -17 51	B1	2°,1	2 ,21	- 7	- 2	+34,1 - 2,4	10 10 22	(5) (1)	-3.0 -3.6 -0.7	208	_ 13  19_
1610 2296	δ Columbae 2927		-33 23	(+5		3 ,98 4 ,05 4 ,48	+ 6	<del> </del>   6		22 22 19	(2)	8,1	173	<u> </u>
1611 2298 1611	8 Monocerotis 1236 8 Monocerotis		$5 + 4 \overline{39}$ $5 + 4 \overline{39}$	Λ5	V1 V1 4°,0	4 54		1 + _4	+15,8	19	(-)	-0,1	173	~-3
2299	1236 BL Orionis		3 -1-14 17	N6		4,7-6,6							164	  - 3
2308 1622	1283 & Catmao	21 ,	7 -52 38	1:0		,86 <sup>-</sup>	1	8 56°	+ 20,7	21	(2)	-5,1	229	-25
2326_ 1629	R1 Auugae	22,	+30 33	Go -		-0 ,67 Vai	- 1 2	195	· 1-21,4	3 3	(1)	- 2,8	Ĩ50 <sup>°</sup>	10
1635	p Geminorum	23 ,	0 +20 17	B5	2°,9 W	5,24-5,97 4,06 4,32	2:		+ 38,4	10	(3)	- 0,9 0,8	100	<b>+</b> 6
2343 1634 2344	1441 10 Monocerotis 1526	23 ,	0 - 4 42	B3	2°,3	4,98	1.		F21	5	(2)	- 1,5 0,7	183	- 6
1639 2356	111 Monocerotis	24 ,	0 - 6 58		3°,0	4 ,73	- 3 3	7 270° 6 - 8		12 12	(2)	0,1 2,5	184	- 7
1640 2357	118 Monocerolis	24 ,	0 - 6 58	B2p	M A1	5 ,22	3 - 3	7 273° 6+ 6			_	3.0	184	)
1640 2358	11º Monocerotis 1574		1		W	5 ,60			23			1,0 3,4	184	
1641 2361	λ Can19 maj 3066		5 -32 31	B5	20.4	4 ,48 4 ,64		$\frac{2}{8} + \frac{31}{63}$		13 13 13	(1) (1)	0,1 2,0 0,1	172	-18  -  -  -
1657 2385	13 Monocciolis		5 + 7 24	Aop	3°,1 W 3	4 ,50 4 ,70 4 ,35	j-t-	4 + 9 8 83°		13		-0,5 -1,8	199	_
1660 2387 1682	51 Canis maj 3991 52 Canis maj	-	$\begin{vmatrix} 6 & -23 & 21 \\ 9 & -22 & 53 \end{vmatrix}$		Y1 2	4 ,51	+	6 6 4 - 25	- 26,7			-1,2	200	
2414 1690	1458		9 +16 29		Y1 10,9	$-\frac{4}{1},70$	1- 6	4 - 13 5 136		25 54	(4)	0,2	105	+ 0
2421 1695	1223		3 - 19 10		W 5°,4	2 ,25	-1-5	32  - 39 07   136°		54	(a)	1,0 3,0	196	-10
2429 1696	1502		8 - 52 53		_ Y2	4 ,16	1	7 237	·  - -23	-	-	1.1	229	-23
2435 1698		33	.5 -18 9	KO	5°, i			243	1,	5	-	0,6	195	- 10
2443	Pictoris	34	,2 -62 33	Nova	-	1,0-12,7	15 4	9 <u>+ 13</u> 15 245 14 – 10		2	2 (1)		240	-25
1703 2450		34	.7 -14	-Ko	6°,5			11 175 6 + 10	·	1 -2	(a)		192	7
4730	Tana 1811 Dishahlu l		. Bose 1620	Tion hoos	1	ed because			mlindo ma	av fall	Very	close to	the lis	nit 5.0

Boss 1611 Probably binary - Boss 1629 Has been included because its maximum magnitude may fall very close to the limit 5,0 - Boss 1639-40 A triple system, the total magnitude of which is 3m,91 in the Harvard system and im,14 in Linnar's system

## 1094 Appendices to Chap.4 K Luminosities, Colours, Diameters, etc of the Stars

						er.								
1	3	3	4	5	6	7	8	9	iO	11	12	13	14	15
1702 2451	* Pupple 2576	34=.7	−43° 6′			3 <sup>-18</sup> ,18	+ 10		+28	25 25	(1)	0,2	219	-19°
1706 2456	S Monocerotis 1890	35 .5		Oe 5	2º,5	4 ,68	+ 7		+28,8		(5)		171	+ 4
1711 2462	Puppla 2417		<b>-48</b> 8	Ko		5 ,00 5 ,10	+ 7	304°	+27.7			0,7	224	-21
1716 2470	12 Lyncis 1015	37 ,4		A2	2'.5 W	4 ,89 5 ,05	15 - 15		+ 7	24 24	(2)		123	+24
2472	Gominorum	37 ,8		Poc Nova	Var	5,0-16,3	- 7 - 7	240°				-0,8	153	+13
1717 2473	#Geminorum 1406		+25 14	G 5	5°,9	3 ,18 3 ,22	20 + 3	180° + 20	+ 9,6	10 10	(4)	-1,8 -0,3	157	+11
1721 2478	30 Garalnarum 1390		+33 20	Ko	6°,1 Yº	4 .65	76 + 18	178° + 74	+13,0	19	(1)	1,1	168	+ 5
1725 2484	E Geminorum 1396	39 ,7		175	3°,9	3 ,40 3 ,57	231 - 72	210° + 219	+ 24	49 48	(5)		168	+ 6
1732 2491	a Canis maj		-16 35	Αo	0°.7 W	-1,58 -1,30	1316 + 184	204°	- 7.5	375 355	(7)		195	- 8
1737 2503	17 Monocerotis 1496			Кo		5,00	<b>20</b> 15	+ 13	+47	12	(B)			+ 3
1740 2506	18 Monocerotta 1397			Ko	6°,1	4 .70	26 + 2	193° + 26	+11	15 15	(4)			+ 2
1758 2527	Camelopard 266	45 ,5		K5	6",4 OY"	4 .75	85 + 85	100°	-29,4		(2)			+27
1761 2538	n Cards maj 3404		-32 23	Вар		3 ,78	10	276° + 10	+14	7	(1)		209	-14
1763 2540	# Geminorum 1481	46 ,2		A2	2*,5 W	3 ,64 3 ,83	54 + 16	174	+14 Var	24 24	(3)		150	+16
1769 2550	α Pictoria 720		- G1 50	A 5	40,0	3 ,3() 3 ,44	272 - 14	343 5	+21			5.5	239	-24
1772 2553	r Puppia 2415		-50 30	Ko		2 ,83 3 ,04	90 + 22	164° - 87	+36	31 31	(3)	0,3	228	-20
1773 2554	A Carinae 1168		-53 31	G5		4 ,38	- 13	5 4	+26,0	15 15	(1)		231	-21
	Geminorum		+32 16	Poc Nova		3.7-14.5	- 12	225°				0,3	150	+13
1776 2560	15 Lynas 982		+58 33	Go	5 4 Y	4 ,54 4 ,58	+ 29		+ 8.6	15 14	(5)		124	+25
1778 2564	o Gaminorum 1462		+13 18	Fo	4°,0	4 ,70 4 ,81	112 + 93	139	+21	40 38	(6)		169	+ 8
1781 2571	15 Canis maj 1616	49 ,2		Bt	3" W	4 ,66	- 8 - 3	- 8	+30	5	(2)	-1,9 -0,8	199	- 8
1783 2574	# Canis maj 1681		-11 55	K2	6°,6	4 .25 4 ,22	138 112	+ 81	+96,5	21	(3)		192	- 4
1785 2580	of Canis maj 4567	49 ,9		K2p	6.7 OY	4,12	- 14 - 13	306 °	+36,8	2	(B)	-3,9 -0,1	202	- 9
1786 2585	ψ <sup>16</sup> Aurigae 1367		+45 14	A2	2*,4 W	4 ,80 5 ,07	25 - 24		-22 :	22 22	(1)		139	+21
1789 2590	1810	51 ,3		F5	4°	4 ,62 4 ,71	67 + 14		+ 8.				199	- 7
1793 2596	4 Cants maj 1661		-16 55	B5	2',8 Y1	4 ,39 4 ,58	- 11 - 7	- 8	+40,6	7	(1)	-1,4 -0,4	196	- 5
1800 2608	2601		-48 35	Ма		4 ,88	+ 4	297° + 8	+22,1				226	19
1804 2618	Canla maj 3666		-28 50	B1	2º,3 G1	1 ,63	+ 1		+28,3	8	(3)	-3,9 -8,4	208	-10
1810 2646	o Cania maj 3544	57 .7	-27 47	K5	7° OR³	3 ,68 3 ,73	- 4		+21,8	11	(2)		207	-10

19 Monocerotie 57 ,9

6h to 7h.

			<del></del>			" to 7".							·	
	2	3	1	5	6	7	8	9	10	11	12	13	11	15
1815 2650	ζ Gemmorum 1687	58 <sup>m</sup> ,2			4°,6 ¥2	3 <sup>m</sup> ,6 -4 <sup>m</sup> ,5 3 ,7-1 ,3	()	196° - <del> -</del> 15	+ 6,7	4	(2)		163°	+13°
1817 2653	o <sup>2</sup> Canis maj 4797	58 8	-23 11	B5p	30 Y(1	3,12	9 + 1	229"	+48,4	6	(2)	-9,0 $-2,1$	204	- 7
1819	y Canis maj	59 ,2	$-15^{-}29^{-}$	135	2°,8	4 ,07	14	184°	+276	- 8	(2)	-1.4	196	3
2657	1625		06	1.00	- W -	4 ,23	F_ 8	-  11   292°		8	(2)	-02	200	
1839 2693	δ Canis maj 3916	4 ,3	26 14	1.8p	Y2	1 98	- 5 - 3	F 4	+31,5	10	(2)	$\begin{bmatrix} -3.0 \\ -4.5 \end{bmatrix}$	200	- 7
1841	63 Aurigat	4.8	1 39 29	J\ 2	()2 ()2	5 ,07	48	94°	-27,0	15	(I)		146	+22
2696 1840	r Geminorum	4 ,8	F30 25	Ĭζο	-6.3	4,98	53	208°	+22,1	18	(3)	3,11   1-0,8	155	+18
2697	1439				$\mathbf{Y}_{3}$	4 ,50	- 11	+ 52		18	_	3,1		
1844	20 Monocerotis 1840	5 ,2	- 4 5	KO	2°,0	5 ,02 4 ,96	217 102	-191	+785			5.7	186	+ 3
1845	A Puppis	5 ,5	39 29	В3		4 .85	13	_ 283°	÷19,5	22	(1)	1,6	218	-13
2702 1853	3105 δ Monocerotis	-6-,8	~ () 2()	~A0	-3° 0	5 ,01 1 ,09	11	+ 13 15°	- <del>-</del> -14	19	(2)	0,1	184	+ 6
2714	1636			110	w	4 ,25	- 2	11		19	(2)	-0.7		
1866 2735	γ¹ Volantis ) 600	9,6	-70 20	(1()		5 ,81 5 ,98	90 30	15°  - - 85	Vai - 3			3,3 5,8	248	24
1867	y <sup>2</sup> Volantis	96	-70 20	TK0		3 ,87	97	150	7 2.7	3 Ī	(2)	+1.3	248	-24
2736 1869	600 J		46 35	60		4 ,01	- 61	- 76   302°	- 14	_31	_	3,8	225	16
27 10	I Puppis 2977	9 ,7	40 33	1.(1		4 ,47	172	4 169				5.7		
1872 2715	27 Canis maj	10 ,2	26 10	B5p	2' W	4 ,66	- 8	311	Vai - -25	8	(i)	-0,9	206	- 6°
1875	4057 1 <sup>2</sup> Puppis	10 -5	- 44 29	Md	_ VV	- 4 ,82 - Vai	332	180	-1-23				223	- 14
2748	3227			11.2		3, 3 -5,2	159	-293	_		1.0	5,9		- 6
1877 2710	ω Canis maj 4073	10 ,7	26 35	133p	3° W	3 ,83 4 ,01	+ 6	207°	→ 29	5	(1)	-1,4	208	~ 0
1870	lyncis	10 19	149 38	A2	10,8	4 ,80	9	212°	- 8	11	(1)		135	-  26
2751 1884	Puppis	119	-48 0	-B8	VV	5 ,09 4 ,88	- 3 16	-  9   38°	<u> - 14</u>	11	-	-0.4	227	-15
2762	2807			-,		4,98	- 16	2	37		4.1	(),9	700	
1886 2763	7 Gemmorum 1443	12 ,3	+16 43	Ã2	3°,0 Y(x1	65, E 18, E	68 - 29	225°	Vai 13,8	37	(4)	2,8	168	1-15
1888	Canis maj	12 ,4	~23 8	K5		4 ,82	61	314	1 27.9	4	(41)	-2,2	201	- 4
_ 2764_ 1889	5189 Canis maj	12 .6	27 42	Mb	7"	1.77	- <u>59</u>	1 18 333°	-1 10,6	10	(1)	3.8	208	- 6
2766	3852				$O_{1}$	4 ,76	44	F 9		10		3,0		
1896 2773	π Puppis 3489	13 ,6	36 55	IC 5	60,3	2,74	8 - <del>j-</del> 4	256°	+15.5	17	(2)	-15	216	11
1898	& Gemmorum	14 ,2	+ 22 10	10	34.7	3 ,51	25	227°	Vai	49	(5)	1,9	164	+18
27 <u>7</u> 7 1899	1615 29 Canis maj	14 ,5	-24 23	Oō-	Y1 20	3 ,67	F 11	1-22 233°	- 2 -12,1	48	(2)	- 1,6	205	5
2781	5173				Y'à	5 ,08	- 7	+ 9		5	, ,	0,3		
1901		14 ,5	-24 47	Oe 5	3° Y1	4 ,40	8 - 6	330° - 6	Va1 - -40,4	8	(1)	-1,1 $-1,1$	206	5
2782 1907	_ <sub>v<sup>i</sup> ը՞սթըու</sub>	14 ,8	-36 33	133		4 ,68	15	208°	+19	11	~(i)~	- 0,1	217	-10
2787	3512			T. 6		- 4 ,83 -	1_15	+ 4	1.00.6	11		0.6	246	-23
1917 2803	d Volantis 730	16 19	-67 46	I. 5		4 ,02	+ 21	253° + 4	+22,6			0,6		41
1924	Canis maj	17 ,8	-18 50	138		4 ,87	- 8	2100	+26	7	(2)	- 0,9		- 1
1928	1806 21 Lyncis	19 ,2	F49 25	-A0	20,6	5 ,07	1 49	+ 8 187°	+25.9	18	(3)	-0,6 0,7	137	+27
2818	1623	l . ′ ′ ′ ′ ′ ′ ′ ′ ′ ′ ′ ′ ′ ′ ′ ′ ′ ′	1		W	4 .71	8	F 48		18	,-,	2,9		

Boss 1815 Cepheld variable 3m,7 to 4m,3, period 10,2 days this star has often been considered as prototype for a certain class of Caphelds but there seems to be few if any reasons nowadays to divide the Cephelds according to the shape of their light curve — Boss 1839 A complex system

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						7º.								
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1931 2821	Geminorum 1385	197,5	+28° 0′	Ko	54.3 Ya	3*,89 3 .93	- 145 - 77	+ 123		23 23	(3)	4,7		+21°
1934 2827	n Canla maj 4328	20 ,1	-29 6	B5p	4° Y1	2 ,43 2 ,65	6		+39	7	(1)	-3,3 -2,6	210	<b>- 5</b>
1944 2845	β Canle min 1774	21 ,7	+ 8 29	B8	7,2 W	3 ,09 3 ,25	- 66 - 26		Var +23	24 24	(4)	0,0	178	+13
1952 2852	g Geminorum 1582	22 .7	+31 59	Fo	3°,7 Y¹	4 ,18 4 ,36	+ 78		- 4	40 39	(6)	2,1	155	+23
1953 2854	y Canie min 1660	22,8	+98	Ko	6°,6	4 ,60 4 ,44	65		Ver +47	12	(2)		177	+14
1962	6 Cants min 1567	24 ,2	+12 13	Ko	6',2 Y	4 ,85	19		-15,4	13	(4)		174	+15
1968 2874	Pupple 1897	25 ,6	-22 49	A3		4 ,80 4 ,96	+ 11		+36,9	28 28	(1)		205	- 2
1972	o Puppia 3260	26 ,1	-43 6	K5		3 ,27 3 ,38	19		+87.3	23 22	(3)		223	-11
1973	Puppls 4620	26 ,9	-30 45	Go		4 .77	3:		+14,4			2,5	213	- 5
1979	« Gaminorum	28 ,2	+32 6		5° G1	2 ,85	203		- 1,2	79 78	(3)		155	+24
1979 2890	or Geminorum	28 ,2	+32 6	A0	1°,9	1 ,99	20	237 0 + 164	+ 6,0		(3)		155	+24
1987 2905	# Geminorum 1424	29 ,8	+27 7	K5	6,5	4 ,22	111		-20,9	16	(5)		160	+22
1988	Pupple 2007	29 ,8	-22 5	F8		4 ,52	8		+60,9		-	4,1	205	± 0
1994	p Pupple 4566	31 ,4	<b>-28</b> 9	B8	4º YG1	4 ,55	7	4 249	+13 :				211	- 2
2001 2930	o Geminorum 1649	32 ,6	+34 49	Fo	3°,4 Y1	4 ,71	12		+ 8	20	(5)		152	+26
2003	Q Carinae	33 ,2	-52 19	K5	1.	5 ,08	2		+61,1	20		5,4	232	-14
2934 2004	f231	33 ,6	-34 44	B8		5 ,03	+ 3		9+24	13	(2)		217	- 6
2008	3755 a Canla min	34 ,1	+ 5 29	175	20,7	0 ,48	124			13 317	(5)		182	+14
2943	m Pupple	34 ,1	-25 8	Вв	Y1 44-54	0 ,64	1	6 + 1242	+41	320	(1)		208	-1
2010	4828 24 Lyncia	34 ,5	+ 58 57	A2	2º.7	4 ,80	+ 6	3+ 16 8 206	+ 5:	16	(2)		125	1 30
2011	1108	34 ,7	-26 34	Bs	W	5 ,17		6+ 68			(2)		210	- 1
2012	# Pupple	34 .:	7 -26 34	B3	A,	4 ,71	3	16 + 4 12 290	+33	10	(2)		210	- 1
2949	d Pupps	36 ,0	0 - 38 4	B3	Y	4 ,83	2	23 25		12	_	1,0	220	- 7
2021	3531 α Monocarotts	36 ,	5 - 9 19	Ro	6°,2	5,08	7	11 + 20	+11,3	22	1	1.7		+ 8
2023	c Gominorum		0 +29 7	Ko	Y8 6*,1	4 ,10	1- 3	18 + 69		17 33		3,0		
2973	1590 w Geminorum		4 +24 38		OY	4 ,32	+ 1!	16+ 19	+45,8	32		6,2		
2985			2 +28 16		4°.7 Y	3 ,74	+	6+ 6		23		2,8	3	+25
2990	1463		5-28 10		Y 7°	1 ,34	- 5	14 + 31:		120	1 1-1	5,3	2	- 1
2203	4767	""	7	at least	OR*	4 116	-	13+	į   T31,,		١.	0,	5	

1979. Complex system consisting of at least the members. The bright stars at end of are spectroscopic binaries of periods 2,9 "spectively Castor C is a star of 90 at 75" distance which share the p, m, of the bright stars and which list! Is a spectroscopic Furthermore a seventh member of the system close to H.R. 2890 has been suspected from perturbations in the visual orbit. — Binary 10", 3:18"

7h to 8h.

	····				7		-							
1	2	3	1	. 5	6	7	8	9	10	11	12	13	11	15
2035 2996	18 Puppis 4774		-28° 43′	A2p	4 <sup>4</sup> Y <sup>1</sup>	f <sup>m</sup> ,10 4 ,26	10 ± 9	+ 5	+23,6			- 0,9	212°	
2040 3003	g Gemmorum	40 ,3	18 45	K2	6°,5	5 ,02 4 ,99	97	225°	Vu +-80,4	11	(i)	0,2 5 0	169	22
3003	Puppis ]	41 .5	-37 39	В3		6,45		7 94	+21,0		-	_ 20	220	- 6
3016	3861 -	44 5	25 11	- K 5		2 50	06	252°	1.02	-			000	
2052 3017	c Puppis 3863	41 ,7	- 37 44	17.2		3 ,72 3 ,80	120	23	18,3			0,8	220	0
2056	ζ Volantis	43 ,0	-72 22	Ko	_	3,89	- 8		- -48,7	32	(2)	1,4	251	-22
3024 2061	627 o Рирріъ	43 ,9	-25 42	B2	-50	4 ,04 1 ,59	- 0		only	$-\frac{32}{6}$	(1)	1,5	210	+ 1
3034	5081		_	( 0.7	161	4 .78		- 11	L lines	_ 6	(0)	5,1		-
2065 3045	ξ Puppis 6030	45 ,1	-24 37	Gop	ου.7 Υ3	47, 3 3,57	_ 7		+ 3.9	3	(2)	-4,1 -2,2	209	- 1
2067	Q Puppis	45 ,3	-46 50	Ko		4,64	128		- 0,5	20	(1)		228	-10
3046 2070	3451 P Puppis	46 .2	-16 8	B0-		4 ,80	1122	and the same of th	-24,0	20	(ī)	5,2 -1,2		- 10
3055	3458					4,30	1 —	+ 6		8		0,0		100
2078 3067	η Gemmorum 1499	47 ,4	+27 1	Λ2	2°,5 Y1	4 ,99 5 ,21	- 10		Vai 3	17	(2)	3,3	162	+-26
2087	a Puppis	48 ,8	- 40 19	G 5		3 ,76	20			21	(i)		223	- 6
3080 2089	3579 b Puppis	49 ,1	-38 36	13 3		3 <u>1</u> 86 4 153	+_ 1		- -24,5   Var	21	(1)	0,3	222y	- 5
3084	3769		10.01	13-3		4 ,62	+ 15		5 , 0	9		~ 0,5		-11
2094 3089	Puppis 3137	50 ,2	-49 21	12.2		4,83 4,92	1	293° 2 - - 15	+ 8	14	(1)	0,0	230	
2095	J Puppis	50 ,3	-47 51	Bi		4 ,32	1	186	-1-41			0,6	230	10
3090 2099	3396 e or 1 Puppis	52 ,0	- 22 37	1 · 8	50 60	4 ,43	+ 1:		- -14,3	28	(1)	0,0	209	4 4
3102	2087		20 4	Λ2	72 30	4 ,45	→ 3°			28	(a)	2,4	215	+ 1
2108 3113	Puppis 5236		-30   4	11.2	Y1	4 ,85 5 ,01	- 10	0 1- 9	1	44	(4)	0,5		
2111	χ Carmac	54 ,2	2 -52 43	133		3,60	3.		19,1	30	(1)	1,0	234	-12
3117 2119	V Puppis	55 ,	3 -48 58	Bip	-	4 ,50	-  -  3	5 <del> 38</del> 0 <b>258</b>	Vai	21	(1)		231	-10
3129	3349				00 0	4 ,86	+ 2			21	(1)	1,9	205	+ 7
2120 3131	Puppis 2118	55 ,4	1 18 7	A2	2°,8 Y¹	4,64	+ 3	4 + 31	13	17	(1)	2,9		7
2126	28 Monocerotis	56 ,	2 - 1 7	KO	6°,1 OY <sup>a</sup>	4 ,88	9	7 145	- 26,7		(1)	0,0	190	1-16
3141 2130	1882 13 Canis min	57 ,	1 1 2 36	Ko	6°,3	4 ,52	+ 9	4 - 25 6 338	2,174	14	(4)		186	- 18
3145	1854			73.57	Y3	4 ,55	- 9	000		19		4,0	5	16
2136 3159	D Carmae 866	59 .	1 63 17	133		4 ,96	_ 2	1 - 20		12		1,5	244	10
2141	ζ Puppis	0,	1 - 39 43	Od	3°,0	2 ,27	3		° - 20	27		-0,0	224	- 4
<u>3165</u> 2145	3939 27 Lyncis	- o .	9 +51 48	A2	2ª,7	4 ,87	- 5	5 32 5 262	4	27		1 - 1		1-34
3173	1391	1		i	W	5,05	4	6   31		7	1	3,0	5	
2153 3185	<i>θ</i> Puppis 6828	3 ,	3 -24 1	F 5	Y2	2 ,88 2 ,97	- 7	4-1- 67	°-1-45,9	16		2,9	211	+ 6
2154	Velorum	3 ,	5 -44 58	Ko		5,02	- i	4 214	°-1-25,3	3		_	228	- 6
3187 2155	4051	3.	6 - 2 41	GO	5°,7	4 ,99	87	4 - 4 25 253	°- -29,5	i 11	(3)	0,	/   7   193	+17
3188	2450				X3	4 .51	_ 1	3 - 32		6		1,	4	
2158 3192		1 4 ,	5 - 18 57	133	2° W	4,34		[6] 240 0]+- 16	23	7	(2)	0,	4 207 3	17 0
_					*** 1									

Boss 2119 Relipsing binary Relative velocity is 610 km/sec Varies from 4m,1 to 1m,8 in 1,5 days

8ª.

						8-,								
1	2	3	4	- 5	6	7	. 8	9	10	11	12	13	14	15
2166 3206	y¹ Valorum ) 8846	6 ,4	-47° 3	3' B3		4*,79 5 ,03	17 + 17	+ 1	Var			0.7	230°	– 7°
2167 3207	7 Velorum 3847	6 ,5	<b>−47</b>	3 Овр		2 ,22 2 ,09	0		+35	15 15	(2)	-1,9	230	- 7
2168 2169	Cancri Cancri	6 ,5	+17 5	7 Go	4°,9 3°,0 Y	5 ,56 6 ,26	155	155°	-10,6 - 5,6	44	(1)	2,9	173	+26
3208 to 3210	1867				YG1	6 ,02	+132	+ 82		44		5.7		
2170 3211	19 Pupple 2385		-12 3		5 4 Y	4 ,68 4 ,66	- 23	+ 13	+36,3	36	(a)	1,9	202	+12
2177 3220	B Carinae 1074	7 .3	-60 59	9 F5		4 ,80	326 +319		+25,0	53	(a)	3.4 7.4	242	15
2179 3223	Voluntia 736	7 ,6	68 1	9 B5		4 ,46	28 - 3		+ 9,6			1.7	249	-18
2180 3225	h <sup>1</sup> Pupple 4084	7 ,8	-39 19	9 K5		4 ,43 4 ,46	20 + 20	180°	Var +15.9			0,9	224	- 2
2181 3226	Рирры 3979	8 ,0	-42 4			4 ,87 5 ,02	+ 5		+19,2	2	(a)	-3,6 -1,6	227	- ś
2187 3237	r Puppls 4349	9 .7	<b>-35</b> 3:			4 .77	+ 13	0	+34	5	(1)	-1,7 0,4	221	- 1
2188 3240	Puppla 4358	10 ,2	<b>−36</b>	1 B3		5 .12 5 .27	+ 5		+18			0,0	221	- 1
2189 3241	Puppla	10 ,2	2 - 36	2 B8		5 .95	- 18	1350				2.7	221	- 1
2192 3243	ha Puppla	10 ,5	-40	2 Ko		4 ,43 4 ,46	+ 61	143°	Var	15	(2)		225	- 3
2195 3249	# Cancri 1917	11 ,1	+ 9 30	0 K2	6',3 OY	3 ,76	75	2240	+22,4	13	(4)			1 25
2207 3270	q Puppls	14 ,8	-36 2	1 A5		4 ,43 4 ,60	144 85	307 b	+ 5	42	( <u>a</u> )	5,2	222	1 1
2208 3275	31 Lynchs 1815		+43 3		7'.0 OY1	4 .43 4 .33	107	185° + 97	+24,3	16 16	(4)	<del></del>	144	+ 36
2214 3280	Voluntia 907		-65 1			4 ,98 5 ,09	31 - 29	21°	0,0			0,7	246	<b>– 16</b>
2216 3282	w Puppla 5185		-32 4			4 .94 4 .95	+ 3	248° + 11	+33.2			0,1	22()	<b>+</b> 3
2226 3294	B Volorum 3734	19 ,5				4 ,90 4 ,99	+ 8	+ 15	+26	11	(1)	1,1	233	- 6
2233 3307	a Carinae 1032		-59 1		G*,4	1 ,74 2 ,03	32 + 4	296° + 32	+11,9	10 10	(1)	-3,3 -0,8		-12
2237 3314	30 Monocerotta 2339				3°,0	3 ,95 4 ,11		249° + 66	+ 7	19 18	(4)	0,2 3,2		+20
3318	a Chamaeleont.					4 ,08 4 ,21	146 143	38° 3 + 25	-13.7			4.9		-22
2247 3323	o Ursae maj 1054	22 ,0	+61	3 G0	4.6 Y	3 .47 3 .54	160	226° 5+152	+19,2	6	(2)	-3,5 4,6		+36
2255 3340		23 ,6	-77 1	o Ko		4 ,26 4 ,39	151	279° +118	+22,4	17	(2)		257	-22
2258 3347	# Volantia 933	24 ,6	65 4			3 ,65 3 ,82	171 +154	193	+27,0	25 25	(1)		248	-16
2290. 3403	s Urano maj 698	31 ,5	5 +64 4		A.	4 ,76	52		+14,7	17	(4)		118	+37
2291 3407	C Volorum 3646		7 -49 3			4 ,87	3	3 315° 1+ 3	+ 4,4			-2,6	235	- 5
2295 3410	ð Hydrae 2001	32 ,4	4 + 6	3 A0	2°,5 YG¹	4 ,18 4 ,37	- 74 - 46	4 261° 6+ 58	Var +10,3	20 20		0,7 3,5		+27
_	- 2166 2167 Prob-	abbi a s		1- 1111 or		nm 2141 2141		intel mem	-1114 -4 [					40 lm 1

Bom 2166, 2167 Probably a physical pair 41", 220" — Bom 2168, 2169. The total magnitude of \$ Canori is 4%,71 and 4%,80 in t two systems until here

12.34

 $8^{\rm h}$ 

1	2	3	1	5	6	7	8	9	10	H	12	13	14	15
2299	e² ( amae	33 <sup>m</sup> ,0	-57° 40′	Kο	1	4 <sup>10</sup> ,80	31	71°	+ 23,6				241°	10°
3414	1591					4 ,91	22	- 22	· • • • • • • • • • • • • • • • • • • •			2,3		T-04
2302 3418	σ Hydrae 2026	33 5	F 3 42	K()	6°,5	1 ,54 4 ,55	27	222°	+25.9	14	(6)	0,1	190	+26
2307	e Velorum	34 ,2	-12 38	Ā 5		4 ,13	- 15	247°	-20,0	17	(ā)		230	1
3126	4451					4 29	-l_ b	- 13				0,0		
2318	β Pyxidis 5128	36 ,2	-34 57	65		4,04 4,11	20	165°	-118	14	(1)	-0,2	224	+ 5
3138	9 Hydrae	37 ,1	15 35	Řо <sup>-</sup>	5°,3	4 ,11	99	182	1,8	31	(2) <sup>-</sup>	$-\frac{0}{2,5}$	209	+16
3111	2551				$Y^2$	4 ,97	+ 83	+ 53		32	`'	5,0		
2324	b Velorum	37 ,3	-46 18	1.5p		4 ,06	15	2085	Vai			0.0	233	- 2
3415 2325	4438 Velorum	37 ,4	-52 34	133		3 ,88	20	1 4 307°	+25.3	12	(1)	0,0	238	- 7
3447	1583	,,,,,	1,22, 34	,		3 ,82	- 6	F 19	١٠/	12		0,2		
2327	y Cancii	37 .5	<b>+21</b> 50	Ao	2°,3	4 ,73	113	243	Var	12	(3)	-0,1	172	1 35
3149	n Velotum	,, ,	- 46 57	Α3	W	4 ,91 4 ,85	- 50 29	+ 102 262°	- 36   Vai	11		5,0	234	<u> </u>
2329 3452	4148	מי זי	- 40 5/	23. )		4 ,91	+ 11	- 27	1-17			2,2		
2330	η Hydrae	38 ,0	1 3 46	13.3	2°,()	4 ,32	22	265°	Vai	7	(3)		191	+ 27
3454	2039			110	W	4 ,53	- 14	+ 17	+ 23,8 + 12,9	7	(1)	$\frac{1,0}{-0,4}$	212	- 10
2331 3457	d Carmae 1080	18 ,5	-59 24	132		1,42	25 - 17	256°	7-12,9	11	(1)	1,1	213	10
2335	31 Monocerotis	38 ,7	- 6 52	GŐ	6°,4	1,70	7	1170	1 31,6	5	(1)		202	22
3459	2708			15	Ya Ya	4 179	6	3		5	16)	1,0		1 35
2336 3461	δ ( anc. 1 2027	39 ,0	1 18 31	Ko	5°,5	4,17	240  +134	1816	十17,1	18	(6)	- 0,5 6,1	1/3	135
2342	a Pyxidis	39 ,0	32 50	132	i	3,70	13	2990	F-16,5	6	(1)		223	F 7
3468	5651					3 ,88	8	1 10		6		-0,8		1 ( 20)
2348	1824	40 ,0	-29 8	A 5	() <sup>a</sup> , 1	6 ,61						2,2	164	1 38
3474 2348	t Cancii	10 ,6	29 8	(r 5	50,4	4 .20	54	202	+15,2	15	(5)	- 0,3	164	1-38
3175	1821				Y	4 ,14	13	52		13_		2,9		
2349	d Velotum	40 ,8	3 42 17	(x 5		4 ,12	18	341"	- 1,0	11	(1)	- 0,2	230	1
$-\frac{3477}{2354}$	4569 8 Hydrae	41.	5 1 6 17	J-8	5,3	4 ,20	196	254 0	[- 36,8	36	(7)		189	+30
3482	2036	1. "	, , , ,		Ay	3 ,58	- 98	1171	_	32		4,0		<u> </u>
2355	12 Hydrac	41 7	7 -13 11	(, 5	() <sup>0</sup> ,()	4 ,44	31	127 °	Vai	4	(2)	3.2	207	120
- 3484 2356	2673 δ Velorum	41,	-54 21	Λ0	Y'5	2 ,01	1- 29	- 11 166°	- 8,5  - 2	30	(a)	2,1	240	-6
3485	1788	[,,,	34 21	1, ,	, ,,,	2 ,25	1 77	- 58		"	, ,	1,9	)	_
2358	a Velorum	42 ,	6 -45 40	Λ 0		4 ,09	21	231 °	+23,6			0,7	233	- 1
3487	4517	43 ,	1 + 6 13	A 0	20,4	4 .42	+ 16	1080	1 33,4	111	(3)		190	-F 30
2361 3492	g Hydrac 2040	43 ,	1   6 13	70	w	4 ,63	1 15	1 37	3311	9	10"	2,		_ ' '
2363	f Carmae	44 ,	1 -56 25	133		4 ,63	5	259°	- -27				241	- 8
3498	1865					4 .72	1 - 3	1 4	1.24.7	- 17	100	- 1,0	220	12
2375 3518	γ Pyxidis 5986	46 ,	3 27 21	K2	$X_3$ $Q_a$	4 ,19	159	1	1-24,7	17	(1)	2,8		7-12
2382	f Velorum	47 ,	2 -46 10	30		4 .89	23	211	Vai				231	- 1
3527	4661					5 ,27	1 21	1- 8	1-00		143	1,7		- 1 21
2393	\$ Hydrae	50 7	1 + 6 20	Ko	5°,5	3,30	- 81		22,7	18 17	(4)	3,4		-  31
-3547 2399	_ 2060 δ Pyxidis	51 ,	3 -27 18	A 2	20-30	4 .87	127		+ 4,6				220	- 12
3556	6072	1	1		Y1	5 ,04	123	30			100	_5,4	1	1 15
2404	t Ursao maj	52 ,	4 +48 26	A 5	3°,4 Y15	3,12	502	240°	+13	62 59	(8)	6,	0 139	1 42
3569	1707	1	ial magnitude	1			1 - 200	17-45/	ı	119	1	1 (1)	** 4	

Boss 2318 A binary, the total magnitude of which is 1m,20 (RHP)

1400 Appendices to Chap 4. K.Lundmark Luminosities, Colours, Diameters, etc of the Stars

8h to 9h.

						w b								
1	2	3	4	5	6	7		9	10	H	12	13	14	15
2406 3571	o Carinao 1243	527,8	-60° 16′	ВВ		3*,98 4 ,10	62 - 40	+ 48	+24,9	22 22	(1)	0,7 2,9	245°	-10°
2407 3572	α Cancri 1948	53 ,0	+12 15	A 3	3°,3 W	4 ,27 4 ,50	+ 54 + 54		-13,6	30 30	(3)	1,7	185	+35
2408 3574	H Volorum 1788	53 .3	-52 21	B5		4 .77 4 ,86	+ 11	195	Var +22,2	3	(1)	-2,8 0 0	239	- 4
2411 3576	g Ursae maj	53 .5	+68 1	Ma	7 1 OY	4 ,99 4 ,93	21 - 21	315°	+ 4,8	9	(4)	-0,2 1,6	113	+38
2413 3579	10 Urane maj 1956	54 ,2	+42 11	F5	4*.1 Y.5	4 ,09	504 - 186	239° + 469	+27,1	69	(4)	3,3 7,6	147	+42
2421 3591	w Velorum 4810	56 ,3	-40 52	F8		4 ,42 4 ,54	68 - 32	299° + 60	Var 65	28	(B)	1,6 3,6		+ 4
2424 3594	# Ureac maj 1633		+47 33	A0	2',9 YG	3 ,68 3 ,87	73 + 16	204° + 71	+ 5	23 23	(2)	0,5 3.0	139	+43
2437 3612	Uraso maj 2900	0 ,2	+38 51	G5	5*,9 Y	4 ,71 4 ,76	43 - 12	234 <sup>8</sup> + 41	+17.4	5	(4)	-1,8 2,9	151	+43
2438 3614	c Velorum 4883		-46 42	Ko		3 ,69 3 ,83	+ 33	+ 66	+24,2	22 22	(t)	3,0		Ŧ 0
2440 3615	a Volentia 1088		<b>-66</b> 0	A 5		4 ,18 4 ,29	103 + 96	•	+ 7.7	27 27	(2)	4,2	250	-13
2441 3616	o Urane maj		+67 32	F8	4°,2	4 ,87 5 ,00	70 + 40	+ 57	- 1,8	53 52	(4)	4,1	113	
2443 3619	f Urano maj 1365	1 ,9	+52 0	A3p	3",9 Y'	4 .54	- 132 - 84	+ 102	- 1,0	19	(2)	5,2	133	
2446 3624	r Ursao maj 728	2 ,7		17 5 A 5	4°,2 Y¹	4 ,74 4 ,83	122 + 122	- 9	<b>- 6,5</b>	19 19	(2)	5,2	118	
2450 3628	n Pyzidis 6895	3 .7		K5	6°-7°	4 ,82 4 ,80	+ 21	- 34	<b>-44,7</b>	13 12	(2)	2,8	220	+16
2452 3634	1 Velorum 4990	4 ,3		K5	7.3	2,22	_ 26 _ 4	+ 26	+18,5	19 18	(2)	-1,5 -0,7		+ 3
2457 3642	R Carinao 861		<b>-70 8</b>	Взр		4 ,86 4 ,95	_ 1	+ 8	+35			-0,6	253	-15
2458 3643	G Carlono 779	4 ,9	-72 12	P5		4 ,50 4 ,63	+ 20	+ 17	+21,3			1,6	255	-17
2467 3654	Valorum 5206	7 🗚		B5		4 ,96 5 ,11	+ 1	+ 14	+35,4	7 7	(1)	0,7	235	+ 3
2473 3659	a Carinao 1419		-58 33	B3		3 ,56 3 ,70		+ 37	+23,1	20 21	(2)	1,6	246	- 7
2476 3662	o Ursae maj 1285		+54 26	A5	34.2	4 .89 5 ,05	+ 9	- 85	Var 16,9		(3)	4,6	130	+44
2477 3663	l Carinae 1201		-61 54	В3		4 ,18 4 ,29	+ 14	+ 45	+16,6	24	(2)	2,5	248	-10
2479 3665	# Hydrac 2167		+ 2 44	AO	2°,9 Y1	3 ,84 4 ,12	+ 324	+ 98	Var.	22 22	(4)	0,6 6,5		+34
2489 3682	1 Velorum 5408	11 ,7		Ko		4 ,98		+ 78	+ 1,8	14	(1)	0,7 4,4	231	+ 8
2491 3684	k Velorum 8808		-37 0	F5	45.4	4 ,70		- 23	+12			1,5		+ \$
2493 3685	Carinae 1023		-69 18	Ao	45,1	1 ,80		+ 193			120	3,2		
2495 3690	38 Lyncis 1965		+37 14	A2	2°,9 Y¹	3 ,82 4 ,00		+ 119	+ 4	29		4,5	154	+40
2500 3696	g Carinae 1961		-57 7	R5	1.	4 ,18	+ 2	9 + 21	4,7	13	(1)	-0,3 2,0		
2503 3699	1465	14 ,4	-58 51	Bo	4",1	2 ,25 2 ,43	+ 1	0 + 24	+13.2	'		-0,6	246	- ;

911

				-			<del></del>	0		10	11	12	13	11	15
1	2	3	1		5	6	7	8	9					<u>'                                    </u>	
2506 3706	26 Hydrae 2609		-11°		(75	5°,8 Y <sup>3</sup>	4 <sup>m</sup> ,91 4 ,98		+ 16		10	(1)	1,5	212°	+26°
2507 3705	40 Lyncis 1979	15 ,0		49	IC 5	6°,5 OY <sup>3</sup>	3 ,30 3 ,34	216 - 171	-J- 131	]_	24 16	(4)	-0,7 5,0		+46
2511 3709	27 Hydrac 2613	15 ,6	- 9 -	8	(15	5°,4 Ya	4 ,97 5 ,01	+ 10	-l 32	+25,5	15	(1)	2,6	209	+28
2516 3718	θ Pyxidis 7114	17 ,1	-25	32	Ma	7° O³	4 ,93 4 ,91	22 +- 2	+ 22	_	14	(2)	1,6	223	+17
2521 3728	k Carmac 1242	18 ,5	-61	58	Ko		4 ,86 4 ,97	+ 16		+ 50,8			0,9	218	- 9
2524 3731	Leonis 1939	18 ,8	+26	37	Ко	Co, 1	4 ,61 1 ,61	61  - 13	+ 59		15	(5)	-0,2 3,6	169	+46
2525 3733	λ Pyxidis 7196	18 ,9	-28	24	KO	. Y2	1,90 4,81	150 64	+ 142	+10,2	39 39	(1)	5,9		+16
2526 3734	y Velorum 2219	19 ,0	-54	35	133	3°,1	2 ,63 2 ,84	S	19		12 12	(3)	2,0 0,8		<b>-</b> 3
2533 3748	a Hydrae 2680	22 ,7			K2	O2 O2	2,16 2,24	3:	5 - 4		28 23	(4)	-1,0 -0,1		- -31
2534 3749	(+ Hydrae 2802	22 ,7	-21		Ko		4 ,91 4 ,89	25 + 22	1 118	'	17 17	(1)	6,9	-	+21
2536 3751	Diaconis 302	22 ,9	- -81	46	К2	6°,6	4 ,58 4 ,49	1			13 13	(3)	0,2		+33
2540 3757	h Ursae maj 845	23 .7		30	l o	3°,8 'Y1	3 ,75 3 ,87	+ 6	7 - 96		36 35	(4)	4,1	~	+42
2541 3759	1 <sup>1</sup> Hydiae 2901	24 ,1	- 2	19	F 5	4°,2 Y'.5	1 ,78 4 ,89	12		+ 9,8	48 48	(1)	5,3		-1-34
2544 3765	s Anthac 5724	25 ,1	-35	30	К2		4 ,61 4 ,65	3: 1:	5 + 30	-	12	(1)	2,2		-1-11
2549 3771	d U15ae maj 565	25 ,0	+70	16	Go	Z1 g	4 ,57 4 ,72	- 8	9 - 9		46	(5)	4,3		-40 
2550 3773	A Leon19 2107	26 ,	+23	25	IC 5	6°,9	4 ,48 4 ,48	+ 2	1 52		15	(4)	3,2		-1 46
2552 3775	9 Ursao maj 1401	26 ,2	+ 52	8	F8p	3°,8 Y2	3 ,26 3 ,43	109 - 33		15,5	73 73		8,5		1 46
2558 3786	ψ Velorum 5580	26 ,8	3 -40	2	I 5		3 ,64 3 ,76	20 7	8 184		65	(1)	5,1	235	1-1-9
2559 3787	t <sup>4</sup> Hydrae 2211		- 0		Λ3	2º,8 Y1	4 ,50 4 ,69	-1-	4 - 25	°+ 7	26 26		1,0		
2565 3799	26 Ursae maj 1402		1-52		ΛO	2°,5 Y1	4 ,65 4 ,82	- 1	2 + 72		18		4,0	1	+-47 49
2566 3800	10 Leonis min 2004		1 -1-36		G 5	5°,3 OY2	4 ,62 4 ,71	+ 2	0 154 18 + 11		19		2,0	0 155 0 246	
2567 3803	N Velorum 2270		2 - 56		K 5	6°,3	3 ,04 3 ,23	+	0 270 5 + 40		39		1,		
2570 3809	Lyncis 2224		8 -1-40			2c,3	4 ,99 4 ,96 Var	2	23 1- 21		16	(4)	2,		
2574 3816	R Carmao 1253		7 -62		Md B5		4,4-10, 4,20	0 - 2	29 -1- 33		8	(1)	-	3 248	
2581 3825	h Carinae 1576		5 58 2 + 5			60,3	4 ,31		7-1- 10		8		0,		
2589 3834	2 Sextantis 2207 M Volorum	33		5 55°		.Xa	4 ,81	<u> -                                    </u>	55 + 16		20	) (3)	6,		
2590 3836	4836	33	7-40	, 55	***3	-	4 ,59		15 + 12				5.	0	

#### 1102 Appendices to Chap 4 K. Lundmark Luminosities, Colours, Diameters, etc of the Stars.

1	2	3	4	5	6	7	8	9	10	11	12	13	14	13
2595	: Hydrae	34 <sup>m</sup> .7	- 0°41'	Ko	6,2	4,10	9.		+24,3	_		-		_
3845	2231	34 ./	- 0 41	L	OY	4,10	+ 85 + 85		+44,3	23 23	(2)	3,8	205	+37
2600	» Hydrao	35 .5	-13 53	B3	2*,3	4 ,96	31		+17	9	(3)	-	217	+29
3849	2917			-	W	5 ,22	+ 2		' ' '	9	\"	2,5		1 29
2602	o Loonia	35 ,8	+10 21	F5	4°,0	3 .76	150	255°	+27,0	18	(4)		194	+43
3852	2044			A 3	Y	3 ,87	- 66			17		4,6		
2604	m Carinao	36 ,6	<b>-60 53</b>	B9		4 ,67	39	299°	+24	17	(1)	0,8	249	- 6
3856	1477	_				4 ,79	- 10	+ 38		17		2,6		
2605 3858	I Hydrao	36 .7	-23 8	B2p		4 ,74	17	295°	+26				224	+22
2015	& Antilan	20.	07.40	Dr.		4 ,95	- 12					0,9		
3871	6881	39 .7	-27 19	F5p	Z.	4 ,98	64 - 40	291°	+24,0	51	(B)		228	+20
2618	a Leonis	40 ,2	+24 14	GOp	4°,5	3 ,12	48	+ 50	1 6 5	- 40		4,0		
3873	2129	٠, م	- - A-T 1-T	GOP	Y	3 ,22	- 10	239° + 47	+ 4.5	18	(5)	-2.1 1,5	175	+49
2627	R Leonia	42 ,2	+11 54	Md	7.9	Ver	33		+10	2	(a)		192	+45
3882	2090				OR.	5.0-10,2	+ 22		1 .0	-	(4)	2,6	192	7.43
2628	1 Carlnao	42 ,5	-62 3	Go		Var	31	314°	+ 4,0	1	(a)		250	- 7
3884	1888					3,6~5,0	- 15	+ 27			(-)	1,1		'
2632	v Uraco maj	43 ,9	+59 31	Fo	3*,8	3 ,89	330	241°	+32	35	(4)	1,5	120	+46
3888	1268				YG1	4 ,02	- 79			33		6,5		
2635 3 <b>8</b> 90	v Caringo	44 .6	<b>-64</b> 36			3 .15	21	287°	+13,8				253	- 9
	v Carinao			Fo		3 ,23	<u> </u>	+ 21				-0,2		_
2635 3891	1084	44 ,6	-64 36			ნ ,03							253	- 9
2637	φ Ursao maj.	45 4	+54 32	Λ2	20,8	4 54			45.5		1.00	2,6		
3894	1331	73 .7	T-34-34	AZ	YI YI	4 ,54	- 9	_ 0°	-12,7	15	(6)		127	1 48
2645	v Hydrae	46 .7	-14 23	Ko	5*,8	4 ,29	30	154°	-14.5	11	(1)	-0,7 -0,5	220	17.00
3903	2963	"	.,		Y	4 ,25	+ 30		- 14,3	11	(1)	1.7	200	+31
2648	μ Leonia	47 ,1	+26 29	Ко	54,9	4 ,10	227		+14,3	22	(6)	_	173	+52
3905	2019				Y	4 ,08		+ 202	, - 1,,	21	(0)	5.9	.,,	, ,,,
2651	ın Velorum	47 .9	-46 5	GS		4 ,56	39	226°	Var				242	+ 6
3912	5808					4 ,70	+ 26	+ 29	十10,8			2,5		
2657	Hydrao	49 ,6	-25 28	ко		5,00	212	285°	+51,9	13	(1)	0,6	228	+23
3919	7585			-		4 ,99		+ 174		13		6,6		
2674 3940	9 Volorum 8078	53 ,4	<b>~54</b> 6	B5		3 .70	23	255°	+14,1	10	(2)	-1.3	247	0
2680	# Leonis	54 ,9	+ 8 31	Ma	74.3	3 ,85	+ 8		107.0	10	745	0,5	100	1 15
3950	2301	24 13	A 0 31	шь	0	4 ,82	_	231° + 43	+23,2	8	(4)	-0,6 3,1	198	+47
2690	v Hydrao	0,3	-12 35	B8	3*,8	4 ,72	38	289°	+24	13	(1)	0,3	221	+34
3970	3073				YG1	4 .89	- 28	+ 25	1	13	1-7	2,6		1.2.
2692	21 Loonis min	1,6	+35 44	A5	2,9	4 ,47	54	96°	-12	26	(5)	1,6	156	+55
3974 2694	2110	1			W	4 ,68	+ 40	<b>–</b> 36		26		3,1		
3975	y Leonis 2171	1 ,9	+17 15	Yob	2°,2	3 ,58	12		+ 2,1	8	(1)	-1,9		+52
2696	A Leonis	2.6	+10 30	K2	64,9	4 ,58	117	+ 8	+40,2	15	/a\	-1,0		1 60
3980	2112	- /9	110 00		0	4 ,53		+ 117	T 40,4	15	(2)	4,9	197	+50
2697	15 Sextontie	2.9	+ 0 7	Αo	2*,5	4 ,50	30		+ 9,8	14	(2)		210	+43
3981	2615				W	4 ,69	- 6	+ 29		14	\-/	1,9		1
2698	a Leonia	3 ,0	+12 27	B8	1*,5	1 ,34	247	269*	+ 7.	64	(3)			+50
3982	2149		- 14 - 75	12	W	1, 61		+ 198		63		3,3		
2706 3994	λ Hydrae 2820	2 ,7	-11 52	Ko	5 .5 Y	3 ,83	221	245	+19,9	18	(3)		220	+36
2723	q Velorum	10 E	-41 38	A2	1-	3 ,87 4 ,09	160	+ 221	+ 8	17	74	5,5	0.45	1 15
1023	5713	1 . 0 . 13	T1 30	T.A		ליטו ד	100	401	+ 8	36	(1)	1,8	447	+12

Boss 2627. Long period vertisble 50,0 to 100,2 is 310 days. — Boss 2628. Capheld vertisble: period 35,5 days. — Boss 2635. A binary 5", 128" — Boss 2637 ADS 7545. A well observed visual binary with a period of 113 years.

The said of the said

10h.

		-						1	1		***	1.0		
1	2	3	4	5	6	7	8	9	10	11	12	13	13	15
2730 4031	ζ Leonis 2209	11 <sup>m</sup> ,1	1 23° 55′	$1^{\circ}0$	3°,1 Y2	3 <sup>m</sup> ,65	27 + 26	- 125°	i f	23 20	(6)	0,1 0,8	178°	4 56°
2729 4033	7 Ursae maj 2005	11 ,1	F43 25	A 2	2°,3	3 ,52 3 ,70	16h	255  - 153	+ 18	18	( <del>4</del> )	-1,1 4,6	143	-1 56
2733 4037	ω C 11111AC 1178	11,4	-69 32	138	_ "	3,56	28	266°	1 1	- 11 11	(2)	-1,2 0,8	258	- 12
2739	q Carmac	13 ,7	-60 50	K 5	~~	$\frac{3}{3}$ ,70	F 8		  -  δ,1	12	_( <u>1</u> )_	-1,2	253	4
4050 2741	1817 40 I con15	14 3	- 19 <u>-</u> 59	- <sub>I</sub> , 5	- 4'.4	3 ,62 1 ,97	+ 11	+ 45	  - - <b>5</b> ,8	12 47	(4)	-1,7	185	- <del> -</del> 55
4054	2166			T. 3	Yı	5 ,08	+ 329	1 326	,	47		7,6	_	_
2742 4057	η <sup>t</sup> Leonis 2467	14 ,5	+20 21		5°,2	2,30	338 + 308		-36,0	30 25	(8)	-0.3	185	+55
2743	y <sup>a</sup> I coms	14,5	- 20 21	Kο	Y3 YG2	3 ,80	353	1210	36,0			1,2	185	F 55
4058 2747	V Velorum	15.8	-54 32	$\bar{\mathbf{K}}_0$		- 3 ,89 - 1 ,58	328		-  13,0	11	(1)	6,6 0,2	250	  - <del> </del> - 1
4063	3474					4 ,70	1 18	1 12		11		1,3		
2751 4069	μ U19ac maj 2115	16 4	+42 ()	IC 5	6°,8 O1	3,21	84 67		Vai 20 3	33 32	(4)	4,7	145	- <del>1</del> -57
2754 4072	Uisac maj 664	ī6 ,9	166 1	Αυ	2°,3	4 ,92 5 ,15	25 i 12	1	- i,4	15 15	(3)	0,8	110	-46
2755 4074	J Velorum 3286	17 ,2	- 55 33	B5p		4 ,65 4 ,74	18	'	+10			1,0	251	+ 1
2758 4080	ı Velorum 5809	18 ,1	-41 9	К5		1,99	62 - 58	328	1 20,9	6	(n)	-1,0	243	-  13
2768	30 I conis min	20 ,2	134 18	10	31,5 Y1	4 ,83	107	217	1 13.7	31	(3)		160	-1-59
4090 2771	2128 μ Hydrae	21,3	-16 20	IC 5	6°,3	-4 ,06	153	236°	F39.7	23	(2)	5,0	228	-+-34
4094	3052  B Leonis min	22 1	- 37 13	Ko	_O <sup>3</sup>	$-\frac{4}{4},09$	161		-1 6,8	23	(5)	- 5,0 0,0	154	- <del>-</del> 60
4100	2080				Y,	4 ,36	1 14	F 161		20	(5)	5,4		
2778 4102	1 Carmac 733	22 ,4	-73 32	J+ 5		4,08	28		- 1,3			1,3	261	15
2779 4104	a Anthae 8465	22 ,6	-30 34	1K 5	_	4,42	68	270°	-15,2	10	(1)	-0,6	239	+22
2783	Carmae	23 .7	-57 8	1 5p		4 .94	7	196	- 1,2	• ``			252	<u>-</u> - 0
2785	3256 36 U19ae maj	24 ,2	L 2 36 30	1.5	46.5	5,06	182	1 '	1-9,60	70	(4)	-0,8 2,4	1	-+ 52
4112	s Carmae		2 58 14	~ <sub>F0</sub>	X 3	5,01	7.5	1	10,0	69	~	6,1	Ž53	
4114	2227	44 ,2	50 14			1,20	11 8	3 - 16				0,4		
2792 4119	30 Sextantis 2663	25 ,2	0 8	135	1°,9 W	4 ,95	- 54	238	1 1	8 8	(3)	3,6		1-1-48
2802 4132	Ursae maj	27 .5	F40 57	A 5	3°,5	4 ,84 5 ,04	141	267 0 1 1 1 6	15	25 25	(4)	1,8		4 60
2804	g Leonis	27 ,	-1 9 49	Вор	20,0	3 ,85	9	229	°-1 37,6	11	(4)	-1.9	204	-1 54
4133	k Carmao	27 .8	71 29	Λ2	W	4 ,03	+ 39	1 + 9	° -Ī~ 7,6	_7	ļ	-1.4	260	-12
4138	1034		5 - 61 11	135p		5 ,03	1 28	.1				2,9	254	- 3
2811 4140	p Carmao 1704	40 ,	-01 11			3 ,72	(	i - 25	1			_0,7		
2812 4142	Carmae 981	28 ,	7 - 72 43	15.5		4 ,90 5 ,01	-1	207	+11,2	10	(2)	-0.1	261	13
2823	ı Carınae	31 ,8	3 -57 3	IC 5	- ~-	4,54	2	237	°1-1- 9,8		(1)	(),5	253	1
4159 2827	U Hydrae	32 ,0	5 - 12 52	_Np		Var	± -13	110	18,8			1,4	229	1-39
4163	3218					4,8-5,6		2 - 24		1		1		
130	ss 2712 A well obs	erred b	mary with a	period at	onna 400	years (AD)	0 //41)							

Boss 2712 A well observed binary with a period around 400 years (ADS 7721)

10ª to 11h.

	10° to 11°.														
1	1	3	4		5	đ	7	8	9	10	11	12	13	14	15
2829 4166	37 Leonis min 2061	33*,1	+32°	30'	Go	5*,3 Y*	4 <sup>m</sup> ,77 4 ,87	+ 6	- 3	- 6,9	13	(3)	0,2 1,0	162°	+62°
2830 4167	p Velorum 6042	33 ,1	-47	42	F2 A3		4 ,06	167 + 5	259° +167	+19,2	26 26	(1)	1,1 5,2	249	+ 9
2837 4174	y Chamaeleont	34 .3	-78	6	Ma		4 ,10 4 ,23	45	291	-22,8	7	(e)	-1.7 2,4	263	-18
2840	t Carinse 2460	34 .9	-58	40	K5 A		4 .73	14	159°	+11,0	14	(a)	0,4	255	- 1
4177 2842	z Velorum	35 .3	-55	5	Go		4 .37	28	226	+20,7			'	253	+ 3
4180 2862	3915 # Caringo	39 .4	-63	52	Во	3°,8	3 ,03	+ 18	293°	Var	7	(3)	-2.7	257	- 5
4199 2863	w Carinae	39 .7	60	3	155	-	3 ,20 4 ,49	- 9 38	259°	+24,0	-7 16	(a)	0,5	256	- 1
4200 2871	7 Carinae	41 ,2	-59	10	Pec		4 ,60 Ver	+ 7	+ 37 478	-25,0	2	<b>(1)</b>	-9,5	255	+ 0
4210 2875	μ Valorum	42 ,5	-48	54	Nova G5	5*,5	-1,0 to 8,5	- 4 78	<u>- 6</u>	+ 7,3	30	(2)	-6,8 0,2	251	+ 9
4216 2888	5913 • Hydrae	44 .7	-15	40	Кo	5°,8	3 ,01	+ 66		- 1,2	30 33	(3)	0,9	234	+ 38
4232 2889	3138	44 .8		1	Вз	Y	3 ,31	- 128 48	-171	+21,7	33		5,0	265	-19
4234	658 46 Leonis min			45	Ko	4°,9	4 .72	+ 14	+ 46	+16,2	37	(7)	3,0	157	+65
4247	2172		-	_	Ao	Y.	3 ,92	+ 289	+ 94	,	_35	, ,	6,3		+62
2900 4248	2058			43		2°,4 Y¹	4 ,84 4 ,96		+ 18		12	(3)	3,6		
2908 4257	u Carinac 2834		-59		Ko		3 ,88	- 19	- 62	+ 8,4	30 30	(1)	2,9	256	+ 1
2909 4259	54 Leonie 2314	50 ,2	+25	17	Ao	2°,9 W	4 ,51 4 ,49	- 77 - 28		+ 6	20 20	(3)	3,9	160	+64
2909 4260	54 Leonia 2314	50 ,2	+25	17		Δ,	6 ,30						2,8 5,7	180	+64
2919 4273	Antileo 6808	52 ,1	-36	36	Ko		4 ,70 4 ,71	164 + 159		- 0,2	14	(1)	0,4 5,8	247	+21
2925 4287	a Crateria 3273	54 ,9	-17	46	Ko	5°,3	4 ,20 4 ,23	481 - 312	284 +361	+47,6	15	(2)	0,1 7,6	239	+38
2929 4293	i Velorum 6276	55 .5	-41	41	A2		4 ,56 4 ,71	+ 14	107°	- 5,1			1,6	250	+16
2930 4295	β Ursae maj. 1808	55 ,8	+56	55	ΨO	1°,9	2,44	+ 17	71°	-11,4	45	(7)		115	+55
2931 4299	p <sup>2</sup> Loonis 2471	56 ,8	- 1	57	Ma	71,3	4 .97	+ 41	154	-13	9	(3)	-0,5	226	+51
2932 4300	b Leonis 2547	57 .0	+20	43	Αo	21,7 W	4,42	- 2l	328°	-10,6	15	(4)		191	+65
2933	a Urma maj.	57 .6	+62	17	Ko	5*,0 Y <sup>0</sup>	1 ,95	139	237	- 9	55	(4)		110	+52
4301 2942	Z Leonis	59 ,9	+ 7	53	Fo	3°,9	4 ,66	350	1 139 262	+ 6,1				216	+- 59
4310 2952	a Carinas	2,4	-61	53	Кo	7-	4 ,83	2		- 2,0		(1)		259	- 2
4325 2958	y Urase maj.	4 ,0	+45	2	Ko	5°,1	3 ,15	- 1	237	- 4,2		(4)		132	+64
4335 2960	x Carinso	4 ,4	-58	26	Fap	X	3 ,21	+ 2	2+ 69 264°		44		2,3	258	+ 2
1337 964	β Craterta	6 ,	-22	17	A2	4	4 .15		+ 19	+ 7.3	-		0,4		+35
141	3095	ı				W	4 ,69	+ 9		+ 6,4	1		4.5	[	1

42909. Hossyi ADS 7979. 6",3, 108",4 (1923,6). Dynamic parallex 0",025,

30: 45

11h.

						L1 •								
1	2	3	1	5	6	7	8	9	10	11	12	13	14	15
2966 4352	y Carinae 3190	8m,3	59° 46′	F5p		4 <sup>ta</sup> ,73 4,85_	+ 6	9	- 8,4		707 dT	-0,1	259°	
2972 4357	δ Leonis 2298	8,8	+21 4	A3	2°,8 Y1	2,58	207 + 203		-23,2	66 64	(7)	1,6 4,2	194	+-68
2974 4359	artheta Leonis $2234$	9,0	+15 59	A0	2°,5 W	3,41	106		+ 7,2	26 26	(6)	0,5	204	+65
2976 4362	72 Leonis 2322	9,9	+23 39	Ma	6°,8	4 ,87	18	236°	+15,8	8	(3)		185	- <del> -</del> 68
2982 4368	φ Leonis 3315	11 ,6	- 3 6	A 5 -	3°,5	4 58	120	,	- 7	29 29	<b>(1)</b>		232	+52
2984	L Uisae maj	12,9	+32 6	_G0_	4° Y <sup>8</sup>	4 ,87	732	215°	-15,5		(7)		163	- <del> -</del> 70
4374 2984	& Ursae maj	12,9	+32 6	Go	4°,0 Y2	4,41	732	215°		ردعا			163	+73
4375 2985	v Ursae maj	13 ,1	+33 38	Кo	5°,9 OY8	3 ,71	27	304°	-15,9 $-9,1$	16	(3)	-0,6	157	+70
4377 2987	2098 55 Ursac maj	13 ,7	+38 44	A2	2°,8	3 ,67 4 ,78	102	214°	_	14	(5)		143	-1-68
4380 2989	2225 δ Crateris	14 ,3	-14 14	Ko	5°,4	3 ,82	+_ 43 230	328°	- 3 - 5,1	20	(4)		240	+43
4382 2990	- 3346 σ Leonis	16 ,0	+ 6 35	Ao	Y8 2°,8	3 ,81 4 ,13	<u>- 230</u>	261°		16	(4)		222	+61
4386 2992	2437 π Centamı	16 ,4	-53 56	-B5	_XC1_	4 ,34	- 37 39	243	- 5,3 +16.	16	(2)	1	258	+ 6
4390 2999	4498 Leonis	18 ,7	+11 5	IF 5	3°,7	4 ,38	176	119	10,0	51	(3)		218	+65
4399 3005	2348	19 ,9	-17 8	A 5	Y1 4°,0	4 .16	+ 153	268	-+ 4	31	(2)		244	-1-41
4405 3031	3214 λ Draconis	25 ,5	+69 53	Ma	6°,9	4 ,33	45	238	+ 7.0		(5)	4,3 -0,1	99	-1-47
1434 3035	665 o <sup>1</sup> Centauri	27 ,1	-58 53	F8p		_3 <u>,98</u> _4 ,96	18	174	-20	15		2,3	261	+ 2
4441 3036	3692 o <sup>2</sup> Centaum	27 ,1	-58 58	А2р		5,09	29		-16,8			1,3	261	+ 2
4442 3042	3693 <i>ξ</i> Hydrae	28 ,1	-31 18	G5		5 <u>.33</u> .72	210		- 4,3	16	(1)		252	+29
_4450_ 3048	A Centaun	30 ,0	-53 42	138		3 ,80 4 ,82	65		+ 4	16	(2)		260	+ 7
3054	4637 l Centauri	31 ,2	-62 28	B9	-	4 ,91	- 12 48	2 - 64 3 242	+ 8	18	(3)	3,9 -0,4		- 1
_4467 3055	2127 v Crateris	31 ,6	9 15	139	20,4	3 ,51 4 ,81	+ 15	5	· 1·	18	(4)	0,5	244	+50
4468 3058	3202 v Leonis		- 0 16	- Ko	W 5°,4	4,98	- 32 3:		1,2	14	-(4)	3,7	237	+58
4471 3073	2458 o Hydrao	35 ,2	2 -34 11	138	Ya	4 ,47	- 30 30		6	17	(1)	-0,0	255	+26
4494 3076	7610 Centauri		-61 32	Go	~*	4 ,98	1;			8		2,3	263	_ 1
4499 3087	2514 ζ Ciateris		-17 <del>48</del>	G 5	40,8	5 ,01 4 ,90	1	1 5	+14,2 - 4,6	17	(1)	-1,0		+42
4514 3089	3460 v Virginis	1	+ 7 5	Ma	OY2 60,7	4 .93	+ 50	0,- 11	° + 50,6	17		3,5	233	
4517	2479			Ko	Oa	4,18	15:	2 + 111	° - 8,7	13		5.0		
3090 4518	χ Ursac maj 1966		+48 20		5°,5 OY8	3 ,85		9 + 119		24	1	4,5	5	
3092 4520	λ Muscae 1640	40 ,9	-66 10	A 5		3 ,80	- 4	2 286 3 + 93	+16			3,8	264	- 5

Boss 2984 Wellknown visual binary. Period 60 years.

11h to 12h.

11" to 12".														
1	2	3	4	5	h	y	H	y	10 1	11	1,1	11	14	15
3094 4522	Contauri 3325	41",7	<b>60"3</b>	7' (+0		47,23	1 22	1 17 577.	45	411	(1)	2.11		7- 0.
309R 4527	93 Leonia 2353	42 ,5	-1 20 4	1.8	41,4 Y	4 .54	155	702'	Vat u,0	tH	(a)	2,4 5 5	207	1 73
3099 4530	<i>н</i> Минско 1649	43 ,4	~-66 4	5 K 5		4 ,71	1 30	168"	1 17.4	!		3,1	414	- 5
3101 4534	# Launds 2383	44 ,11	15	A A2	2'.5 Y'	2 ,24 2 ,52	511 148	250 1491	" 1	R4 ¦	(1-)	1 1) 5 H	121	F71
3103 4537	j Centauri 1988	44 ,H	63 1·	1 115		4 .63	1 11	235" 1 17	1 17 1	1 1		14		- 2
3104 4538	Mumato 1595	45 ,2	60 4	(+5		4 ,00	11	201K	1 18.2	4	(1)	11,1		~ 9
3105 4540	// Virginia 2489	45 ,5	1 2 2	1-8	4',2 Yi	1 ,80	794 1 626	111" 494	1 4.9	94	(4)	1.7 H, 1		+60_
3109 4546	13 Contauri 7614	46 ,1	_	7 Ko		4 ,71	- 15	470"   91	F 3.4	j		4.7	l l	+16
3115 4552	# Hydrae Bull		-11 2			4 .40	56 EN	1 51	1,	14	(1)	1.1	, 1	+28
3117 4554	y Urene maj. 1475	48 ,6			1",9 W	2 .54	1 31	. Ky	11	(M)	(r.)	4.4	1	1-62
3139 4589	a Virginia 2502	55 .7			2",5 Yi	4 .57	1 26	187"	24.0	24	(4)	22		+66
3146 4599	#1 Crncis 2543	1	-02 4			4 ,48	146	267"	2,5	14	(4)	5.3	265	- 1
3151 4603	2501	59 ,2			ŀ	5 10%	- 1	2HH	1 3/4.1			~ 10		- 1
3153 4605	or Chammologast. 777		<b>-75</b> 5			5 (0)	14	1 74 1 24 1 2807	"			4,8	1	-14
3155 4608	o Virginia 2583 y Cruch	0,1			5°.1	4 ,21	1- 111	1 170	29,0	19	(4)	о,о 6,0	ί	+69 
3160 4616 3162	WIAA Contanti )	1 .7		3 F()		4 ,42	1 44	180°   12   261°	1 94		. 4	2,6		
4618 3165	0#13			n 135	47,0	4 ,90	- 6	1 240"	1 10	8	(4)	2,2 - 1,2		+12
4621 3166	6697	3,2	50 1 24 1			3,07	1 01	+ 41	Var.	15	(3)	1,1		
1623 3172	10174 Corvi			4 Ko	Y	4 ,28	+ 81	~ 45 276*	,T 100	43	(6)	4.0		+ 37
4630	Sear p Centauri	5,0			Y.0	3 ,26	- 37 49	14 55 243*	+ 21	28	(2)	, 3'3	!	+39 +10
1638	6455 8 Crucia	9,8		2 B3	37,0	4,32	+ 5	+ 49	+ 20	15		2,7		+ 4
4656 3190	4189 A Urano maj.	10 ,5			21.7	3 ,25	+ 3	4 48	1	45		1.5		+59
4660 3191	1363 7 Corvi		-16 3		Y1 3',0	3 .58 2 .78		107	Var.	40	(1)	3.7		+44
4662	3424		-67 2		W	4 ,16	- 90 237	+ 133	- 4,2	42	(=)	1,8		- 5
4671	1931 # Chamnelsont		-78 4			4 ,29	- 21	+237	,	16	(1)	6,0	1	-17
4674 3200	741 ¢ Crucis		-63 2			4 ,40	- 20	+ 45		16	(2)	2,8		-1
_4079 3203	# Centauri		-54 3			4 .98	+ 4	+ 50 241	- 6.9	16		2,6	266	+ 7
4682	5113	1	ļ			5 ,00	+ 11	+ 93	i	1 }		4,9		

Ross 3162, 3165. Probably a wide double.

	j#1					12".							,	
1	2	3	1	5	6	7	8	9	10	11	12	13	11	15
3210 4689	η Virginis 2926	14 <sup>m</sup> ,8	- 0° 7′	Αo	3°,0 W	4 <sup>tn</sup> ,00 4 ,21	67 - 11	248° + 66	Var + 7	25 24	(2)	0,9 3,1		+61°
3216 4697	11 Comae Bei 2592	15 ,6	+18 21	Κo	5°,5	4 ,91 4 ,87	139 -122	303° + 65	+42,4	15 14	(4)	0,6 5,6	242	+78
3218 4700	ε Crucis 4188	15 ,9	59 51	К2	7,0	3 ,57 3 ,73	199 133	292°	- 4,8			5,1	267	+ 2
3224 4707	12 Comae Bu 2337	17 ,5	+26 24	F5	4°,1 Y <sup>2</sup>	4 ,78 4 ,92	13	205° 11	Vai + 1,9	36 36	(1)		200	+84
3230 4716	5 Canum Ven 1626	19 ,2	+52 7	Ko	4°,3 Y2	4 ,97 4 ,96	11 - 4	52°	-13,4	11	(3)	0,2	97	<del>-</del> -65
3237 4730	α <sup>1</sup> Crucis 2745	21 ,0	-62 33	B1		1 ,58	47 + 17	228°	Vai ?	18	(5)		268	- 1
3238 4731	2745	21 ,Ĩ	-62 32	_B1	2,3	2,09 2,37	49	251° + 49	Var ? + 0,3	1,		- 1,6 +0,5	268	- 1
3242 4737	y Comae Ber 2288	22 ,0	+28 49	ΚÕ	5',2 Y <sup>3</sup>	4 ,56 4 ,52	122 + 40	225°	+ 4,0	13 10	(6)	0,4 5,0	163	+85
3245 4743	σ Centauri 7115	22,6	$-49 \ 40$	В3		4 ,16 4 ,27	47	233°	+12	14	(2)	-0,1 2,5	267	+12
3256 4757	δ 01 δ <sup>2</sup> Corvi 3482	24 .7	-15 58	Ao -	3°,5 YG1	3,11	251 + 18	235° +251	- 4.	22 18	(2)		264	-+46
3263 4763	γ Crucis 5272	25 ,6	<b>-</b> 56 33	Mb	6°,9	1,61	273 +259	176° 90	+21,4	~ 10		3,8	268	+ 5
3263 4764	γ Ci ucis 5272	25 ,6	<b>−</b> 56 33	^A2	-	6 ,68 6 ,84	1,22,7	1 70				-5,0	268	-1- 5
3269 4773	γ Muscae 1336	26 ,5	-71 35	B 5		4,04 4,14	46	253° + 46	+14	15 15	(2)	-0,1 2,3	269	10
3272 4775	η Co1 v1 3489	26 ,9	-15 38	Fo	5°,2 Y1	4 ,42 4 ,54	444 164	261° +413	- 5	45 45	(3)	-	266	<del>+</del> 46
3279 4785	β Canum Ven 2321	29 ,0	+41 54	Go	5°,0	4 ,32 4 ,43	758 -508	292° 561	+ 6,1	109 110	(4)	4,5 8,7	99	<del>+</del> 75
3280 4786	β Co. v. 3401	29 ,1	-22 51	G 5	4°,8 Y <sup>2</sup>	2,84	61	180° 32	- 7,1	26 26	(3)		266	+39
3281 4787	z Dracoms	29 ,2	70 20	B5p	2°,2 W	3 ,88 4 ,08	60	276° 59	Var. -11.4	7	(4)	-2,2 2,8	92	-1-48
3283 4789	23 Comao Ber, 2475	29 ,9	+23 11	AO	2°,7 W	4 ,78 5 ,03	- 72 - 39	276° + 60	-23.	12 12	(5)	arram.	244	+83
	24 <sup>1</sup> ComacBer.)	30 ,1	+18 56	A 3	BV <sup>2</sup>	6 ,72	- 19 19	325° 2	+ 3,7	9	(2)	-0,3	257	+80
	24 <sup>9</sup> Comae Ber. 2584	3Ō ,1	+18 56	K o	5°,9	5 ,18 4 ,98	16 - 12	14° 11		11	(1)	0,4	257	+80
3289 4798	α Muscae 1702	31 ,2	-68 35	B 3	2°,8	2,94	42 8	240° + 41	- -18	13	(4)	-1,5 1,0	269	- 7
3292 4802	τ Centauri 7745	32 ,3	47 59	Λ2	-	4 ,02 4 ,15	27	228° + 26	+ 5:	9	(1)	-1,2 1,2	269	+14
3298 4813	χ Viiginis 3452	34 ,1		Кo~	6°,0 Y2	4 ,78 4 ,74	85	+ 84	-19.7	14	(2)		267	+55
3300 4817	1 Centauri 7748	34 ,4	-39 26	B8		4 ,79 4 ,94	63	227° + 61	+15			3,8		+23
3302 4819	γ Contauri 7597		-48 25	ΛO	30,8	2,38 2,59	200 - 82	266° +182	- 8	17	(2)	-1,5 0,9	269	-+-14
3307 4825	y Virginis 2601	36 ,6		Fo	3º,6 Y1	3 ,65 3 ,92	564 -299	271° +479	-19,8	_			268	<b>+61</b>
3307 4826	y Virginis 2601	36,6	1	Fo	3°,3	3 ,68 3 ,95	564 -299	271° +479	-20,0	67 65	(8)		268	+-61
3309 4828	Q Virginis 2486	36 ,8	+10 47	AO	2°,5 W	4 ,95	135 +132	138° - 28	0:	13 13	(5)		267	+73
BAR	4 2263 Rinnru?	Dogg 22	04 200r A	Manney Ir	adudad a	n hasle of I	ta total	magnitude	4 06 (D)	(da)	Bor	n 2302	1740100	hinary

Boss 3263 Binary? — Boss 3284, 3285 A binary included on basis of its total magnitude 4,95 (RIIP) — Boss 3307 Visual binary rith a period of about \$180 years

12h to 18h.

						12h	to 18	4.								
1	2	1	•		5 1	6	1	- [	Ħ	11	[11)	11	11	11	11	14
3311 4831	w Configuri 760H	37".1	-48°	16′	Ko		4''',1	16	129	1448 1471	11.7	11	(1)	0 2 5 2	ļ69	1 14"
1319   4842	/ ( Tuch) 4273	30 .7	(4)	26	Ko			'N' '	1111	129"	i I sto	21 24	(1)	14	2719	1 1
3320 4844	# Minerao	40 ,1	-67	34	111		_	16) 1-1	1 10	1 1H	142	11	(5)	1 a 1a1	2311	41
3322 4846	Y Camma Von	40 ,4	145	59	Nh Viu		1,640	(1,66	h	55*	114	11			*#*	) 7Å
J324 4648	5215	40 ,0	- 55	50	11.3			H1 15	1 19	1 27	1 16.7	16	(2)	4 (1	1711	į ų
332H 4853	# Critical 1451	41 3	- 59	y	351	¥.7	1 1 4	77	510	210° 1 50	( 40,0	11	(5)	, <u>, , , , , , , , , , , , , , , , , , </u>	1/1	3 1
3351 48HR	o Centauri	47 .4	- 48	24	K2		4.	15 I	[10] [1,	454" 1 101	0.7	18	(1)	1010	475	1 H
3352	n tentauri 780 j	47 .	-39	18	Λ5		4 .	14 511	17	1.40 *	٠,			1 1 16	17.1	1-24
4889 3357	A Criu.b	48 .:	- 5H	36	113		4.8	H4	51	1 46	1 10	15	(4)	1	171	1 1
4897 3358	# Crucia	48 ,1	- 56	38	113		4 1	16	iro	248"   10	1 11.9		(4)	4.1	171	F \$
48y8 335y	54H7 μ <sup>e</sup> Crus Is	44 4	-50	37	333)			(6	47	4 41"	LIA.			•	471	4 5
4899 3362	5487 J	49 ,	1 ~ 9	()	Mb	7'.I	4 .	<b>91</b>	1.1	1219	4 17,0	19	(1)	0.4	371	+ 53
4902 3363	# Urnen nun)	40 .	  - 56	30	Aup	1".U	10	iji Iji	115	1 (2	8,0		(7)	9,4	nğ	+61
1905 3367	1627 Virginia	511 ,6	5 F 3	56	Ma	07.6	. 3 .	nă Nă	479	117	17.9	18	(3)		277	4 65
4910 3370	al Cunum Von	51 0	+38	52	Aup	OK1		65 39	187	1 441	~ ,5 M	17		7.1 U,2	75	+ 78
4914 3371	a Canum Von	51 ,4	+311	52	Aup	27.9 Y1		70 05	437	2H1"	- 18	31 29	(5)	4.7 0.3	78	+ 78
4915 3374	36 Commo Her	54 .	+17	57	Mn	67.7	1 4 1	96	- 114 ' ,4te	(02"	~ 1,7	11	(4)		180	+79
3377	у Минско Винско	55 .	4, -71	1	Ka	}	3 .	6.J	364	, U)^	1 16.1	20	(1)	27	271	- 9
4923 3382	75 Ursan maj.	36 .	5 + 56	55	Fu	5.4	1 4 .	74 89	4 147 101	117	- 9	35	(2)	2,6	_	+61
4931 3383	1408 Virginis	57 .	2 +11	30	Ko	5.0	1 2 /	08 95	+ 14	271	- 13.5	35	(4)		284	+73
4932 3390	i Contauri	0,	4 -47	56	E Z	Y*	4.	96 96	- 145 59		+ 9	16	(2)		27.1	<b>414</b>
4940 3393	# Cantauri	1 .	0 -49	23	Bj		4 ,	40	+ 17	14 57 235°	Var.	11	(2)		471	+13
4942 3401	7644 41 Comas Bar	. 2,	4 +28	10	K5	64	4 .	52 90	4 ,		-4 14,3 16.3	13	(3)	0,1	3	+16
4954 3409	8 Virginia	Ĭ 4 .	8 - 5	u	Au	7.7	1 4 .	91	+ HH	223*	. 0		(5)		181	+ 54
4963 3412	a Comes Ber.	) 5 .	1 + 18	4		W	5 ,	23	450		,-17.5	15			294	+78
4968 3412	a Comeo Ber.	5 .	+18	4	P 5	A.	1 5 .	30	- 101	+333	1	77 77	(1)	4.5	296	,¥75
4969 3419	2697 Contauri	6 ,	0 -59	23	BS		4 .	30 70	61		Var.	18	, (2)		271	j+ <b>3</b>
4975 3421	4B15 Centauri	6,	5 -37	16	05		14	15 50	+ 4		- 13.8	34	(1)		275	+11
4979	} 8437 = 1358, 1356, λ b	1	100 40		Ton order	1		94	- 742 == , ==		) 3452 W	24	,	7,1		} 

Dom 3358, 3359. A binary: 36", 17" — Dom 3370, 3371. A binary: 20", 206" — Bom 3412. Wellington binary with a pusit Algo years, 11s total respected to 4",67 (RHP).

13h.

						19								
	2	3	1	5	- 6	7	8	9	10	11	12	13	14	15
24 83	β Comae Ber 2193	7 <sup>111</sup> ,2	+28° 23'	Go	3,'8	4 <sup>111</sup> ,32 4 ,44	1184 1101	+ 126		112 109	(4)	4,5 9,7	3°	+84°
29	η Muscae	8 ,5	<b>-67</b> 22	138		4 ,95	32		Vai	9	(2)	-0,3 2,5	273	- 5
93	2224 Muscae	10 .5	66 15	Ko		5,04	1-1- 4	193°	+ 5 -10,3	- "			273	_ 4
102	2142					4,90	+ 26	+ 23			77	2,5		
46	σ Vngmis 2722	12 ,6	+ 6 0	Ma	6°,9 OY3	5 ,01 4 ,93	16	-1- 7	-26,7	5	(1)	-1.7		+66
47		13 ,1	- -41 6	Fo	3",5	4 ,66 4 ,87	125		+ 8,7	10	(4)	-0,6 5,1	66	- <b> </b> -75
148	61 Virginis	13 ,2	-17 45	G 5	4°,6 Y2	4 ,80 4 ,84	1529		- 8,0		(4)	~ ~	280	+43
)19  49	3813 γ Hydiae	13 ,5	-22 39	G-5	5',0	3 ,33	83	128°	- 5,6	28 26	(5)	-	280	+38
)20 152	3554 (Contauri	15 .0	-36 11	_Ā2	OY2 4°,5	2,91	+ 353		0			_	278	+25
)28	8497				_	3,13	127	+ 328				_5,7	044	
15G 234	Centaum 4627	16 ,1	-60 27	B3		6,51	_ 20		7			3,6	274	+ 2
157	J Centauri	16 ,2	-60 28	B5		4 ,62 4 ,72	39	241	+26	11 11	(2)	0,5	274	+ 2
23.5_ 164	4627 J m Centauri	17 ,2	-64 1	Go		4,50	50	142	+12,1				274	- 2
341	2732	47 2	-74 22	Ko-	_ '	4 ,62	+ 50 203		  - -28,8	14	(a)	3,0	273	-12
463 042	1057			_		5,06	7:	189		_		6,5		
474 054	ζ¹ Ursae maj 1598	19 ,9	+55 27	Aop	10,9	2,40	130	6 - 125	Var 9,9	44	(12)	0,6		+62
475	ζ <sup>a</sup> Uısae maj	19 ,9	+55 20	AO	G <sup>3</sup>	3 ,96	130	6 105	11			2,2		+62
055 476	4 598 J a Viiginis	19,9	-10 38	B2	1°,6	4 ,20	5	5 229		23	(4)	-2,2	285	<del>+</del> 50
056	3672 ω Contauri		46 47		3°,5	1,52	-	6 + 54	1,6	0,14	(1)	-0.8	277	- <del> </del> -15
					30,2	4 ,02	12	3 <sup>1</sup> 102	°-12	37	(7)	1,8	78	+61
480 062	g Ursae maj	21 ,2	- <del>1</del> -55 30		OYı	4 ,19	+ 3	2- 119		36		4,5		
1482 1068	69 Vitginia 3668	22 ,1	-15 2	Ko	5",6 Y2	4 ,89 4 ,85	- 12	5 + 94	-13,7			5,4	+	+46
1491	R Hydrae	24 ,2	-22 4	Md	7°,6 OR8	Vai 3,9-10	7	3 273 7 + 56	° - 4,0				283	+ 38
1080 1496	d Centaur	25 ,2	-38 5	Ko	O.K.	3 ,96	2	9 211	° - 3,1			Ì	279	+22
,089	8592				70,3	4 ,01		2 243	+ 18.	11	(4)	1,3	3   3  291	+ 54
3499 5095	1 Virginis 3714	26 ,8	3 5 4	) IATER	Oa	4 ,79	- 1	3 111		11		5.	1	
3506	o Vugmis	29 ,	1 + 4 1	0 A2p	2º,4 W	4 ,93		$\frac{32}{18}$ - $\frac{127}{19}$		18	(7)	3.	298	+ 63
5105 3508	ζ Virginis	29 ,	6 - 0	5 A2	3º,4	3 ,44	28	38 277	· - 13	36 36	(3)		2 295	+ 60
5107 3511		30 ,	3 + 37 4	2 F0	3°.7	3 ,62	8.		Var	33		2,	5 46	+75
51 LC	2426		4 +49 3		3',3	5 ,11	-	38 - 76 18 277	7°-18	32	(4)	4,		+66
3512 5112				1	W	4 ,88	3 - 2	26 + 114	1	17		5,	0	1 _
3518 5127		33 ,	0 +36 4	8 Fo	3°,4 Y1	4 ,92		04 278 41 + 90		27		5,	0	_
3521	P Centauri	33 ,	5 - 52 5	7 B1	2,8	2 ,50	5   4		°+ 6	11		-2,   0,		+ 8
5132 3530		36 ,	9 -1-55	2 Ma	70,0	4 .7	5 :	28 24:	20 16,	9 10	(3)	0	3 73	3 <del> ∓</del> 61
5150	1625	1,	0 -32		Oa	4 ,6		13'+ 2 89' 25	5 2° - 23	61		. '	28	+ +27
3544 5168	9603	1				4 ,4	7 - 1	76+ 45	5	61		7	,8	1
	Boss 3456, 3457 Bir	.new 60	" 2429	Boss 3474.	3125 Bli	narvi id".	150°, mc	ember of t	Irsa Majo	r Cluste	er	Boss 3 1	91 L	ong per

Boss 3456, 3457 Binary: 60", 343° — Boss 3474, 3475 Binary: 14", 150°, member of Ursa Major Cluster — Boss 3491 Long period ariable, period 144 days

## 4410 Appendices to Chap.4 K.Lunnmann Luminosities, Colours, Diameters, etc of the Stars

18h to 14h.

						18h	to 14".								
1	2	3	4		5	6	7	8	9	10	11	12	13	14	15
547	M Contract 8017	40=,4	-50°	56'	K0		4*,68 4 ,79	32 + 27	176° + 18	Var. - 5,8	14	(1)	2,2		+10*
558 185	7 Bootle	42 .5	+17	57	F5	3°,8 Y¹	4 ,51 4 ,65	487 -229	273° +429	-15.7	71 67	(6)	3.7 7.9	328	+73
564 190	y Centruri 8171	43 .5	-41	11	B2		3 ,53 3 ,71	- <sup>42</sup>	234° + 42	+ 8,8	9	(4)	-1,9 1,6		+19
566 191	η Umao maj. 2027	43 ,6	+49	49	В3	1°,3 W	1, 91	- 119 - 57	260° +104	-16	16 10	(4)	-3,1 2,3		+65
567 192	g Centaurl 9358	43 ,6	-33	58	Мь		4 ,40 4 ,43	72 + 12	220° + 71	+40,8	54	(a)	3,7	285	+26
565 193	μ Contauri 8172	43 .6	-41	59	Вар		3 ,32 3 ,51	28 0	230° + 28	+12,6	7 7	(1)	0,5	282	+18
572 200	บ Bootie 2564	44 ,6	+16	17	K5	6',4 0Y	4 ,28 4 ,18	106 - 73	288° + 76	<del>- 6,3</del>	46 31	(3)	4,4	324	+70
577 210	k Centauri 9676		-32	30	Bs		4 ,72 4 ,86	- 66 - 0	230° + 60	+13,8	15 15	(2)	3.5		+27
578 211	k Centauri 9676	46 ,0	-32	30			6,17	+ 4	80° 16	+ 1,2			0,3 0,6	285	+27
584 219	Canum Ven		+34	57	Ma	61,9	4 ,96 4 ,91	+ 30	+ 32	<b>-43,6</b>	10 10	(4)	0,0 3,2		+73
586 221	h Centenri 10729			26	B5		4 ,76 4 ,91	+ 4	221 + 28	+ 5,2			2,0	287	+29
589 226	Dracomis 963		+65	13	Ма	7'2 0Y	4 ,77	+ 2	- 135° - 3	- 10,7	8	(6)	-0,7 -2,2	78	+51
593 231	¢ Centauri 8949			48	В2р	34,2	3 ,06 3 ,01	82	230 + 82	Var	16 15	(4)	-0,5 2,6		+13
596 235	# Bootla 1788		+18	54	Go	Ar.	2,80 3,00	373 +306	190 +213	Var. - 0,2		(4)	5.7	334	+72
599 241	Contauri 3070		-63	11	Ko		4 ,68	+ 18	215° + 60		15 15	(1)	3,7	278	- 2
602 248	φ Centauri 8329		-41	36	B3		4 ,05 4 ,21	- 34 - 2	233° + 34		9	(1)	1.7	284	+18
603 249	9010			19	B3		4 ,17 4 ,18	+ 2	+ 46		12 12	(2)	-0,4 2,5	283	+16
610 260	9040		-45	7	I 5		4 ,39 4 ,57	+ 21	198° + 35	- 1:			2,5	283	+14
612 264	r Virginia 2761		+ 2	2	A2	A <sub>1</sub>	4 ,34 4 ,51	+ 32	- 141°	- 5	20 18	(5)	1,9		+58
615 267	β Centauri 5365		-59	53	B1	27,6	0 ,86 1 ,14	+ 8	219° + 40	-12	18 16	(5)	-1,1	279	+ 1
621 285	χ Centauri 8405		-40	42	В3		4 ,54 4 ,69	+ 13	+ 36	+12,1	9	(2)	-0,7 2,4		+19
622 287	π Hydrae 10095	0 ,7		12	Ko	A. 6.	3 ,48 3 ,54	166 +149	165° + 73	+27.1	38 37	(3)	3,6		+33
623 288	# Centauri 9260		-35	53	Ko	6°,5	2 ,26 2 ,32	750 + 38	225° +750	+ 1,8	59	(4)	6,6		+23
626 291	or Draconis		+64			2*,1 W	3 ,64 3 ,84	- 54 - 3	286° + 54	Var 16,0	22	(3)	2,3		+51
628 297	Centeuri 7028		-52		Ko		4 ,78 4 ,90	189 - 23	235° +187	1	18 18	(1)	1,1 6,2		+ 7
633 303	η Apodia 706		-80		A2p		4 ,97 5 ,06	+ 39		- 9			4,7	273	-20
635 304	d Bootis 2737		+25		F3	3°,8 Y1	4 ,82 5 ,00	76 + 60		Var + 9,8	27 27	(3)	4,2		+70
3639 5313	Virginia 8867	7.2	+ 2	53	Aop	2*,4 W	4 ,90 5 ,18	- 60 - 3		Ver + 3	12		0,3	314	+57
Bo	■ 3577, 3578. A 1d	mary 8",	109											1	

14h.

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
3642 5315	× Vugnis 3878	7 <sup>111</sup> ,6	- 9°48′	Ko	6°,5 Y <sup>8</sup>	4 <sup>111</sup> ,31 4 30	130 96		- 4,0	35 31	(4)	1,8 4,9	30 <b>2°</b>	+46°
3649 5321	4 Ursae min 478	9 ,2	+78 1	Кo	6°,3 OY2	5,00	38	313°	+10	17	(4)	1,0	84	+39
3652 5328	*1 Bootis 1782	9 ,9	+52 16		30,5	6,61	67	140°	-23,2	-10		3.7 5.7	62	+61
3654 5329	* <sup>3</sup> Bootis	9,9	+52 16	A 5	ΥG1	4,60 4,81	+ 11	103°	- 14,9	26 26	(6)	1,5 3,6	62	+61
3660 5338	Virginia 3843	10 ,8	- 5 31	F5	4°,3 YG2	4 ,16 4 ,26	427 - 320	183°	+11,5	37 36	(3)		307	+49
3661 5339	δ Octantis 557	10 ,9	-83 13	K2		4 ,14 4 ,28	93 - 44	262° 82	+ 5,0	19 19	(1)		273	-22
3662 5340	α Bootis 2777		+19 42	K0	4°.7 OY3	0 ,24 0 ,14	2282 +1369	209° +1826	- 5,4	138 115	(5)	0,5	344	+68
3667 5350	1300tis 1784		+51 50	A 5	3°,9 Y1	4 ,78 4 ,98	169 - 74	+ 152	-17	26 26	(1)	1,9 5,9		+60
3666 5351	λ Bootis 1949	12 ,6	+-46 33	A0	2°,6 W	4 ,26 4 ,43	- 152	+ 183	- 5	31 29	(4)	1,5 6,1		+63
3668 5354	2084		-45 36	В3		4 ,10 3 ,99	- 1	+ 12	+22	3	(1)	-0,5		+13
3670 5358	v Centaum 5984		-55 56	В5		4,41	- 22	+ 32	+ 4,6	8	(2)	-1,1 -4,0		+ 4
3672 5359	λ Virginis 4018		-12 55	A.2	3°,2 W	4,60	32 32	+ 2	Vai - 7,2		(1)	0,9	302	+43
3673 5361	A Bootis		4-35 58	KO	Y1,5	4 ,83 4 ,87	+ 10	+ 16	Var. -25.6	24 23	(3)	1,6 0,9	28	+68
3680 5367	y Contauri 9336		37 26	Ao	50.0	4 ,17 4 ,34	- 38	+ 61	- 4	40	(0)	3,5		+22  +65
3681 5370	20 Bootis 2637	1	+16 46	Ko Go	6°,0 Y3	4 .97	- 110 - 110	+ 110	- 7,3 + 18,4	18	(2)	1,3 5,9	339 282	+ 2
3682 5371	Centauri 6619		5 58 0	B5		5,06	- 39 49	+ 32	+ 8,7	1		3,4	290	+19
3688 5378 3689	a Centauri 9329 k Hydiao		3 - 39  3 $1 - 27  18$	K2	6°7°	4 ,55 4 ,70 4 ,93		8 -1- 48	+19.9		(3)	3,0	295	+30
5381	9803 Bootis	' '			Ya	4 ,91	- 4º	9 + 226	Var	13	(2)	6,7	324	+60
3692 5385	2882 Bootis		5 - - 8 54	Ao	2°,3 V2	6,82		4 + 71		13	-	6,1	324	+60
3692 5386 3699	2882 r <sup>1</sup> Lupi	18 ,			W	5 ,29	- 3	0 197°	-17,7		-	5,8	288	+14
5395	9322 7 <sup>4</sup> Lupi		8 -44 56	F8		4 ,77	+ 1	4 + 26		1	(1)	1,9		+14
5396 3704	9323		8 + 52 19	F8	4°,4	4 ,64	+ 1	6+ 12		7		3,3		+ 59
5404 3707	1804 1 Hydrao		4 -29 3	138	- Y1	4 ,25	+ 43	3 + 184 2 217°		68		7,4		+28
5407 3710	10712		0 - 1 47	Kō	W 5°,0	5 ,18	+ 13	6 + 42 4 266°			(1)	3,1	314	
5409 3716	2957		9 50 1	B2	Y2	4 ,98	<del>- 7</del>	2+ 113 4 256°		36 12	(1)	5,6	287	+ 9
5425 3717	8831 g Bootis		5 +30 49	Ko	5°,4 Ya	4 ,69	+ 1	8 + 50 9 318°			(4)	0,8	14	+66
$\frac{5429}{3718}$	2628 5 Ursae min		7 +76 8	K2	60,4	3 ,77	<u>- 13</u>	1 + 70 1 35°	+10,		(2)	0,7	82	+40
5430 3722	527 γ Bootis	28		Fo	Y3 20,9	3,00	18	$\frac{1}{32}$ $\frac{2}{323}$	-35	63	(4)	1,0	34	+65
5435	2565 oss 3652, 3654 Is d				YG1	3 ,23	- 15	8 + 91	 021 → B	) 60 oss 36		4,3 nary, <i>1</i>		i 47 6",4,

Boss 3652, 3654 Is doubtless a physical system (ADS 9173) The dynamic parallax is 0",021 — Boss 3692 Binary, ADS 9247 6", 1925). The fainter star is itself a binary, 0",2, 283° (1926). The close pair has a period of 40,5 years

						144.			ara I	11 14		11
-	2	3	4	5	ħ	7		11	100			
724	y Contouri	294,2	- 41°43′	143p	3",1	27,05 3 ,85	40	324.	13	14 (1)	1 to 2015 1,1	) 16°
720	a Hootis	10 . 1	4 30 41	10	150	4 .48	224	58"	1.02	41 (4)	. 25 12	1 441
417	2536	31. 11	1 300 11		γı	1 titi	71	217		40	11,1	•
3732	e land	11 ,2	49 0	145		4 ,14	51	221"	F14	13 (2)	U, 4 ZBB	1 9
5453	9198					1 ,15	74 140	1 51	!!!	111	2,7	
3735   5459	74 (antauri ) 5483	32 .H	¬(n) 25	(10)		0,21	112H			773 (6) 780	4,5 484	•
3735	a Contauri	32 ,8	~60 25	165	50,0	1 ,70	1680	2H1"	- 22.2		0,2,284	- 1
5460	5483	J= ,	5			1 ,61	HAR				9.6	
3739	a Circini	34 ,4	-04 12	10		1 (41	2 17	1854	1 7.1		a, Lana	f.
5463	2977					1,50	1 152	1 181	'	tal .	5, 4	
3745 5469	a Lapl 9501	75 .3	46 5H	112	3,5	2,80	1 15	1 35	1 7	9 (4) 9	4, (490). 1 (17)	F 11
3746	or Alkalia	35 ,4	-7X 17	165		1 .81	34		0.4	17: (1)	140 276	~ 1H
5470	803	55	7			1 .97	1 6		,-	17	1.4	
3747	b Contouri	35 .7	- 37 21	113		4 ,09	44	"HH"	1 4	11 (2)		4 30
5471	9018	24 4		A 45	- A	1,20	1- 14	1 -		11.	1 1 1 144	1464
3749 5475	2 1 100 th 1	30 10	+10 51	ΑU	7,4 W	1 4 ,94 5 ,0H	1 5		- 4	10   (4)   15	, ILN 544	4 61
3750	a Booth	36 .0	+16 31	Ao	12	18, 7			i	1 1		4 61
5476	8768				Kı	5 .95				'	1	
3752	( Bootle )	36 ,4	+14 9			4 ,84	61		- 3.	201 (7)		1 50
5477	2770	2/ 4		A2	2°,5	4 44	1 50	15	!	19	1,8	4 an
3752   5478	2770	36 .4	+14 V		1.	4 .43	1				מונד איני	+ 39
3757	o' Centauri	37 .5	34 44	Ko		4 .11	2017	201"	- 1H,7		1 296	1 21
5485	BORG					4 .10	1 75	1 191			4.7	1
3758	μ Virginia	37 .8	- 5 13	1'5	4.0	3 .05	139		4 4	44 (4)		1 47
5467	3936 c* Contauri	40 .	74 46	1 40	YI	4 (1)	' F 315		!	44	(i ft	) .1.94
3759 5489	9888	30 10	-34 46	Vo.		5 .15		, ju	~ 5	İ	(,(1)	+21
3761	34 Booth	39 ,0	1 -26 57	Ma	6,6	1 4 .91	20	i luna	+ 5.2	7 (3)		+63
5490	2413			1	()1	4 ,91		1 11		7	1.8	
3770	a Bootis	40 1	+17 23	Ko	5,0	4 ,69	83		- 9,6	17 (2)		+ 60
5502 3771	2780 # Hootle 1	40 .	+27 30	AO	OY	4 .75	T 31	1 77	- 18,8	1 17	1.81 7	+63
3505	2417	۱۳۳ "	T-/ 30	1,10	4",3	3			10,0	1	1410;	703
3771	a Brootis	40 ,0	+27 30	Ro	OX.	2 .70	45	260	- 16,4	23 (6)	-06 7	+61
5506	2417					2 .65	- 22	1 -		22	1 1.1	
3772	109 Virginia 2862	41 /	+ 2 19	VO	27.7 W	3 .76	120		- 9	24 (3)		+ 51
3781	38 Hydrao	44 .	-27 32	K2	,	3 .98	250	1	- 0.9		4,2 1,2 '301	+ 27
5526	10073	" "	7 -/	1	O	4 .62	- 13			33	66	
3783	e Lapi	45 .	1 -43 9	1 B5		4 .49	, 51		+ 7,0	13 (2		+14
5528	9391	1		!	-	4 .64		1+ 50		13	10	
3784 5530	41 Libras 3965	45 1	-15 35	1.5	3,	5 .43	131	1 235"	- 24,1	100 (1)		4 37
3787	a Librae	45 .	3 -15 36	EA I	3,0	2 .00	12		Var	47 (1)	1.3 308	+ 37
5531	3966	1		1	YG	3 ,10		+ 127	10	47	34	,
3798	# Bootis	46 ,	+19 31	G 5	5.3	4 ,80			+ 4.2	118 (8		+60
5344	2870		J		OY	4 .72				104	5.7	1)
3809 3563	# Ursaa min, 595	51 ,	0 +74 34	K5	67,Î	2 ,34	31		+16,9	34 (4		+40
3514	16 Librao	52 .	0 - 3 56	Fo	3,3	4 .59	-	2+ 27 2 211	+24	32, (3	2.1 130	445
5570	3696	"- '	3 30	1	Y	4 .74		4 184	7.04	32	6,0	4.43

14h to 15h.

							10 10.							44 1	
1	2	3	1		5	6	7	8	9	10	11	12	13	11	15
3815 5571	β Lupi 9853	52 <sup>:</sup> ,0	-42°4	4' 1	B2p		2 <sup>m</sup> ,81 3 ,02	- 69 - 5	223° + 69	0	14 14	(4)	2,0	_	+13°
3818 5576	2 Centau11 9342		-41	2	В3	4°,5	3 .35 3 .55	36 - 7	208° + 35	+ 9,1	9	(4)	-1,9 1,2		+14
3825 5586	d Librae 3938	55 ,6			Λo		4,84 5,1—6,3		261° + 57	Vai 45,0	14 11	(1)	0,6 4,0		
3827 5589	Uisae min 878		+66 2		Mb	7°,1	4,86	+ 82	293° + 81	Var  + 6,8	8	(4)	-0,6 4,4		+46
3834 5600	ω Bootis 2861		+25			6°,4 OY3	4 ,93 5 ,09	58 52	187° + 26	+13.5	13	(1)	3,8		1-59
3835 5601	110 Virginia 2905				KO	5°,8	4 ,62 4 ,64	- 30	268° + 40	-16.7	16	(1)	_ 3,1	327	+48
3836 5602	# Bootis 2840		+40	_	G5	4°,9 Y <sup>2</sup>	3 ,63	63 + 43	227° + 46	-19.9	21 20	(4)	2,6		+59 +28
3837 5603	o Libiao 11834	58 ,2			Mb	O.8	3 ,41 3 ,50	- 23	234° + 91	- 4,0	25 24	(2)	3,3		+ 9
3838 5605	7 Lupi 9773	58 ,3			В5		4 ,72	1 2	215° + 40	+16	10	(2)	2,7	293 293	+ 9
3838 5606	π Lupi 9773		-46		Ko	F0.0	4 ,82 4 ,95	+ 19	118° - 3 264°	- 3,1	10	(2)	1,2		+59
3842 5616	1/2 Bootis 2447		+27		Ko	7º,5 Yº,5	4 ,67 4 ,63 4 ,86	178 - 30	+ 174 274°	-25,6	16	(5) (6)	5,9		+56
3847 5618	1 Bootis		-+48	3	G0 B3	5°,1 Y2	4,86	387 + 39	-1-383		75	(2)	7.9		+10
3852 5626	) Lupi 9889	2,	1 -44 0 -48	-	139		4 ,39	- 7 121			7 29	(1)	1,8		+ 7
3862 5646	я <sup>1</sup> Lup1 9704 я <sup>2</sup> Lup1		0 -48	21	AO	-	4 ,25	- 44 116	+113	1	29		4,3		+ 7
3863 5647	9705	l	1 -51	43	Ko		3 ,50	- 58 127	+- 100		17	(1)	6,3		4- 4
3864 5649 3865	ξ Lupi 8830 e Lupi	6.		8	Вз		3 ,66	- 46 51	- -118		17	,	4,0		_
5651 3866	9932	6,		25	Aop	2° 3°	5 ,06	- 12 61	+ 49	- - 1 i	13	(3)	3,		+-31
5652 3871	4047		5 -31	9	FO	YGi	4 ,82	+ 3	+ 61		13		3,0	304	+21
5660 3876	11 813 8 Cu cini		2 -63		ко		5 ,07	+ 14	12				1,:	286	- 6
5666 3880	3544 B Circini		6 - 58	i	Λ3	1	4 ,95	+ 4	1-1- 8				-0,	289	- 1
5670 3879	5875				A0	   4",3	4 ,28		5 178			-	5,	283	-10
5671 3887	2383		5 + 33		Ko	40,6	3 ,23	- 30	5 56					4 20	+ 57
5681 3888	2561 μ Lupi		5 -47		В8	Ys	3,60	+130	6 - 73		15	(2)		2 295	+ 7
5683 3890	9860 β Librae	11		1	B8	2°,4	4 ,46	-1-	3 + 59	o Vai	15	(1)	1-0	2 320	+38
5685 3891	3935 f Lupi		,7 -29		Ro	G1	2 ,96	- 4	9 90	-37 - 3,	3 1	5	2	,8) ,4 30;	1
5686	11630 81 upi		.8 -40		В2	3°,5	4 ,46	i	5 4- 26		1		1 -1	,6 ,8 300	
3896 5695	9538 7 Circuit	- 15			B5-F8	-	3 ,61 4 ,54	1 1- 1				9 ]	) -0	,0 ,3  28	
3901 5704	5908	15			IC 5		4 ,64	+ + 1	5 + 40		8 2	1 5 (1	)   2	,6 30	
3903 5705	1	1,3	,3		1	47 3/60	3 ,6;	5 - 2	6 -135	1	12	5	4	,3 l	38. 245

Boss 3838 Doubtful if a physical pair — Boss 3847 Visual binary (ADS 9494), period 205 years The companion 6m,1, 3",38, 245°,3 (1926) is Boss 3846 and has very near the same p m as the principal The dynamic parallex is 0",082

						10"•	_							
1	2	3	4	3	6	7	H	ŋ	ļu	11	IJ	111	14	1 15
3905 5708	# Lupl 10066	15'n,9	-44° 20'		3°.5	1".74 1 .76	28 1	471¢	Var	H	(4)	1,7	711 <b>7</b> '	1 100
3910 5712	φ <sup>1</sup> l upl 10103	16 ,8	-36 TO	113		4 ,(4)	11	#14"    -	'	13	(2)	0,5	1111	1 15
3021 5724	k Lupi 10289	18 ,8	-3H 22	Ao		4 ,68	61	141"	* *			· inte	(r)1	1 14
3926 5733	μ* Booth   2036	20 ,7	1 37 44	10	3',0 Y'	4 ,47	109	1974 1150	- H,11	4:	(4)	A,A,	47	1 55
3027 5734	1100th 2637	211 .7	1 37 42	Ko	Alta 1.	6 ,66	174	104*	9.4			7,8	47	1 55
3928 5735	7 Ursno min 679	20 ,9	F72 11	A2	27,2 W	4 ,14	17	115"	Var J.y	41	(4)	1.1,	75	4 41
3936 5744	1 Druconis 1654	22 ,7	1 59 19	Ku	5°.5	3 .47	111	111"	1044	- 11	(4)	-0,7	59	1 48
3940 5747	# Coronno Hor.	23 .7	+29 27	Fop	7.1	1,72	190	404"	43	12	(11)	1,5	12	4 54
3947	2670 a Friang, Aust	27 ,6	-65 59	Ko	Att	11, 1	75	164"	14,4		(1)		2116	- 9
5771 3949	ra Hooth	28 ,2	F41 14	Λ2	F.5	1,24	27	230°	24	27	(4)	1,4	12	1151
5774 3950	2611 γ Lupi	28 ,5	- 40 50	Н3	Y(1)	2 ,95	1 1H	******   ****	F 0	19	(3)	1,E 7,1-	jos	   <del> </del>
5770 3952	9760 37 Libruo	28 .7	~ 9 43	1¢n	5".7	4 ,83	180	130*	+46,5	42	(3)	- 69°	ردر	+ 34
5777 3953	#171 # Coronao Hor	28 ,9	+31 42	115	Y 2.7	4 .81	13Ky	224°	   10	12	(1)	7,8	17	+ 53
5778 3954	d Lapt	29 ,0	-44 37	113	W	4 ,40	33	1 30 189*	, ×	12	(1)	3.09 11.4	100	+ #
5781 3959	y Libruo	ر. <b>29</b>	- 14 27	Ko	57	4 ,87	1 15	1 16	- <b>ሕን</b> (11	20	(2)	2,8	•	(+ 12
5787 3960	4237 8 Serpentin Ni	30 ,0	1 10 53	Fo	ήχ. r	4 (0)	+ 52	49 255°	~ (4	30	1,	1,1		h 47
378B 3960	3891 J Berpuntis N	30 ,0	F10 53	Fo	Y(;1	5 10	Or.	262*	~ JR	ا 27	(12)	4 11	_	1+47
3789 3961	a Coronno Bor	30 ,5	+27 3	ΑU	W 2".1	4 .43	- 46 13H	1 40	+ 0,4	20	(9)	3 4		1
5793 3962	2512 r Librar	30 .0	-27 48	K2	W	2 .53 3 .78	+131	BH		47		1.3	-	+33
3794 3964	10464 10 Lupi	31 ,3	-42 14	K5	ÓY!	3 .80	- 4	1 9	~24,7	31,	(2)	0,7 1,2		+20
5797 3973	10601 r Librao	32 .6		03		4 .35	-16H	4 12	7.7	21		5.5		+10
5812 3978	- 11817 -	33 .5			M 1,	3 ,811	- 1	41 + 41	Var	101		1,2,		+20
5820 3980	10831 g Lapi			Ko		4 ,61	F 15	+ 1	~21,8	18	(1)	0,9		+16
5825	10310	34 ,3		F5		4 ,69	- 124 29	4 324	7	}		7.2	300	+ 8
5833	Coronacillor 2006			138	Br	81, 6	+ 21	- 149°	~23	9	(1)	3,1	15	+ 52
5834	Coronae Bor, 9888		十36 58		2',4 W	5 .07			-28,6			~0,2	_	+ 52
3990 5838	и Librae 4188		-19 21	K	0.7	4 ,96	459 - 55	318* +454	Var. - 4.9	10	(2)	8,3	317	+27
3991 5839	y Lupi 10494		-34 25	B5		4 ,82	- 40	121 4 + 48	Var. + 8.5	12	(1)		307	+15
3994 5842	r Berpentia 3138	37 .1	+20 0	A2	27.4 W	4 ,49	91 + 19	232	Var	13		4.3	359	+49

Boss 9927 A wide physical pair (ADS 9826). The fabrier star is itself a binary dw.,1—7w.], 1".41, 41".1 (1935.6). Pariet 234 years. T dynamic parallex of Bu is 1".025. — Boss 3960 — ADS 9701 Dynamic parallex 0".026—0".041 — Boss 3961 Estipates binary Pariet 1.735 day

15h.

						,	(D"								
1	2	3	4		5	6	7	8	9	10	11	12	13	11	15
,998 ,849	γ Coronae Bor 2722		- -26°	37'	Λo	2°,6 YG1	3 <sup>ra</sup> ,93 4,05	105 59		Vai 10,4	22 22	(6)	0,6 4,0		+∙51°
854	α Serpentis 3088	39 ,3	+ 6	44	Ко	5°,3 Y8	2 ,75 2 ,84	46 12		+ 3,0	49	(5)	1,2	342	+42
1009	β Serpentis	41 ,6	+ 15	44	Λ2	2°,6 Y1	3 ,74	91	127°	- 7 <sup>-</sup>	25	(6)	0,7	354	+47
867 1010	2911 7 Serpentis	41,6	+ 7	40	Go	4',4	3 ,89_ 4 ,42	+ _86 244		<b>−</b> 66,1	25 97	(4)	3,6	344	_ +43
868 1015	3023 ≈ Serpentis	44 ,2	+18	27	K 5	Y15	4,57	- 100 110		-39,3	98	(4)	6,4 0,0	357	+47
1879	3074					O <sub>8</sub>	4,19	68	+ 87		14		4,5_		
1016 1881	μ Serpentis	44 ,4	- 3	7	A0	2º,8 W	3 .63 3 .80	- 48		-11	29 29	(3)	0,9 3,4	333	+36
1018	μ Lupi 10754	44,6	-33	19	В9		4 ,11 4 ,27	+ 29		Var	7	(1)	-1,7 1,4	309	+ 15
1019	b Scorpu	45 ,0	-25	27	В3	2 <sup>d</sup> W	4 .77	42	213°	-10	10	(3)	-0,2 2,9	314	+21
5885 1024	11131 δ Coronae Bor	45 ,4	+26	23	-G5	5°,0	$-\frac{4}{4},93$	110	222	-19,3	25	(4)	1,5	8	<del>1</del> -49
5889 1026	2737 ε Serpentis	45,8	+ 4	47	A2	Y <sup>2</sup> 3°,2	4 .77 3 .75	+ 57 136	+_95 66°	- 9,8	23 37	(4)	4,9	341	+41
892	3069			7	Fo	W		-1- 46 538	<b>-128</b>	+ 1.	37	(1)	4,4 2,8	289	- 8
1030 5897	βTriang. Aust 3723	46 ,3		_		5", 1	3,18	(	+538		90		6,7	_	
1031 5899	ρ Serpentis 2829	46 ,9	- -21	17	K5	0.'Q	4 ,88 4 ,87	- 49 - 21	1	-62,6	13	(3)	0,5	1	1-47
1032 5901	x Cotonae Bot	47 ,5	+35	59	Ko	5°,9	4 .77 4 .88	+ 364		-25,0	28 27	(5)	1,9	24	+49
4035	ζ Uısac mm	47 ,6	+78	6	A2	20,4	4,34	25	97	Var	25	(2)	1,3	79	+36
5903 1034	527 A Scorpu	47 ,6	-25	2	-B3	3° -	4 ,53	18	1 .	-12	25	(2)	1,3 -0,6	315	+20
5904_ 4039	12 352 1 Libiae	48 ,1	-16	27	Ko	Y1 5°,2	4 ,83	+ (		+ 3,4	9		2,3	322	+27
5908	4174					$X_B$	4 ,32	+ 10	-154	-55,8	24	(5)	5,3	34	+49
4042 5914	χ Herculis 2648	49 ,2	+42	44	Go	4°,4 'Y <sup>2</sup>	4,61	760 - 707	-274		77	(3)	9,0		_
4049 5925	51 Lupi 10826	50 ,5	-33	40	ĀO		5,37	4		-10	04	(0)	2,2 4,1	309	+14
4050	Lupi Lupi	50 ,5	33	40	AO		5 ,73	-l- 50	145	-12	24	(a)	2,6 4,5	309	+14
5926 4052	10826 J η Scorpi	50 ,7	-28	55	133	4º	4 ,02	33	203	+ 2,8	9	(3)	-1,2	313	+17
5928 4055	y Serpentis	51 .8	- -15	59	F5	4°,4	3 ,86	133	+ 33 2 167	+ 6,9	9	(5)	1,6 3,8	355	44
5933	2849 48 Libiae				Взр	Y2	3,99		+829	P <sub>1</sub> 14	96	(1)	9,5	324	-1-27
4059 5941	4302		-13				4 ,88	+ :	1- 34		9		2,3		
4062 5944	π Scorpit 11228	52 ,8			132	20-30 YG1	3,00	39	203	Var. - 3,0	11	(4)	1,0	315	+19
4063 5947	ε Coronae Bor 2558	53 ,4	+-27	10	Ko	5°,6 OY3	4 ,22 4 ,23	109	231 5 + 99	-31,8	23 23	(3)	1,0 4,4	10	+48
4064	η Lupi	53 ,4	-38	6			3 ,61	4	1 207	+ 7	11	(2)	-1,2	307	+10
5948 4066	δ Scorpii	54 ,4	-22	20	Во	20-30	3 ,80 2 ,54	4		-19,2		(3)	$-\frac{1.8}{2.3}$	318	+-22
5953	4068 Γ̃ Coronae Boi.		+26	_	мБ	G1	2,7 <u>7</u> 2,0 to	- <del>-</del>	9 + 40 3 32	- 5	11	(3)	0,6	10	+47
40	2765				Nova	26.2	10,3		7 - 10		28	_	-2,4 2,1	52	
4072 5960	Draconis 1793	55 ,4	+55	2	A 5	3°,3 Y¹	4 ,96 5 ,18	+ 19	4+193	- 5.7		(2)	6,4	1 32	7.40

Boss 4049, 4050 Binary: 11", 49° Certainly a physical system

15h to 16h.

					15 <sup>n</sup>	to 16 <sup>11</sup> .								
1	2	3	4	5	6	7	8	9	10	11	12	11	14	11
4071	1 Normae	55",4	-57°29′	Λ2		4 <sup>11</sup> ,87	147	229°	18:	1			294°	, , , , , n
5961	7500					4,96	- 57	-1-135			}	5.7		
4073	η Normae	55 ,8	-48 57	G 5		4 .74	30	106°	··· 0,3	16	(1)			-}·
5962	10512		* 30 40	-77.4	1	4 ,86	· · 29	~ 5		16	4-1	2,1		
4076 5967	Lupi 10832	50 ,8	-38 19	13 5		4 ,97 5 ,13	7	217°	0:	11	(2)	3,2		+ 111
4080	Coronae Bor,	57 .4	+30 7	Ao	2",3	4 ,91	45	238	Var.	14	(4)	1 '		- -47
5971	2738		100 7		W	5 ,20	1. 17	1. 42	1	14	(1)	3,2		
4081	π Serpentia	57 .9	+23 4	Å2	2",4	4 ,82	17	250	Var.	18	(3)	1.1		4 46
5972	2886				W	5,06	12	12	30,1	18		1.0		
4082 5977	\$1 Scorpii 4237	58 .9	-11 6		4°5° Y <sup>9</sup>	5 .07						3.2	328	+ 28
4083	& Scorpli	58 ,9	-11 6	F8	5°,0	5 .16 4 .77	71	241°	22.6	42	(5)	2.0	  บาน	
5978	4237	34 19			Y2	4 .86	- 32	1. 63	-33,6	12	(3)	4,0	340	4.24
4084	o Normae	59 .5	-44 54	Азр		4 ,84	17	3 0	15,5	14	(a)	0,6	303	+ 4
5980	10625		~			4,98	7	- 16	- 570		, ,	0,9	1	,
4089 5982	v Horculis	59 ,6	-1-46 19	B9	20,3	4,64	89	140°	-l· 5.5	11	(2)	(),2	39	4 47
4086	2142   / <sup>1</sup> Scorpii )	50 6	-19 32		W 1"-2"	4 ,91	40	79		11	4.1	4.4		
5984	4307	29 ,0	-19 32		$G^1$	2,90	31	201°	Var. 4.3	8 8	(4)	2,6	321	+33
4087	8º Scorpli	59 ,6	-19 32	131	10	5,06	34	223°	4,3	"	1	() <sub>1</sub> } (-() <sub>4</sub> 4	121	+ 22
5985	4307				Va	5 ,29	- 7	1- 33	1,3			2.7		1
4090	# Draconis	0,0	+58 50	F8	4º,3	4 ,11	458	318°	8,5	77	(4)			+ 44
5986 4091	1608		ac aa	-	Y1.5	4 ,22	- 72	452		75		7.4		
5987	<b>⊕</b> Lupi 10642	0,0	-36 32	133		4 ,33	41	2110	-1.15	10	(2)	~ 0.7	308	d 10
,4093	ω¹ Scorpil	1.0	-20 24	B2	2°,8	4 ,48	34	- - 41 192°	- 8	10	(2)	2.4	221	. ~
5993	4405				YG1	4 ,29	+ 11	+ 32	- 0	9	(2)	1,1 1,8	341	4.21
4095	o• Scorpil	1,6	-20 36	G <sub>0</sub>	5",1	4,58	70	143°	- 5,2	12	(1)	0,0	320	+21
5997 4108	4408				Y	4,67	+ 64	+ 27		12	, ,	3,8		
6018	r Coronae Bor. 2699	5 ,3	+36 45	IC O	5,4 Y <sup>2</sup>	4 ,94	325	349	17,0	43	(6)	2.7	26	+46
4109	δ¹ Apodis	5.4	-78 27	"Mb	1-	4 ,78	-312 42	1-1- 94 207°	10.0	36		7.5	- T.	
6020	1092		10 21	1111		4 ,90	1	1- 42	-12,0			2,9	280	-20
4110	გ₃ Apodla	5 ,5	-78 25	K 5		5 ,22	32	175°	~- 10,2				280	<b>2</b> 0
6021	1093	-, ,				5 ,32	+ 16	+ 27				2.7		,_
4112 6023	φ Herculia 2376	5 ,6	+45 12	В9р	2",5	4 ,26	32	221°	-15.4	16	(3)	0,3	37	+46
4116	" Scorpii	6 3	-19 12	Λ	W 3ª	4 ,46	- 48	+165		15		1.8		
6026	4332	,,_	19 12	A	BVs	6,49	12	189° + 12				1.7		+ 22
4117	" Scorpil	6,2	-19 12	В3	30	4 ,29	34	200	Var.	12	(3)	1.0 0.5		.1. 77
6027	4333 J				Yı	4 .34	+ 5	+ 34	- 6,5	11	(3)	1,9		-F & #
4115 6028	c <sup>a</sup> Scorpii 10841	6,1	-27 40	B3	3 <sup>n</sup>	4,70	47	216°	H- 9:	10	(3)	-0,3		+16
4118	o Triang, Aust.	6 4	-63 26	Go	W	4,85	8	47		10		3,1		
6030	3854	0 ,4	-03 20	00		4 ,03 4 ,16	18 十 10	171°	5,1			F. 19	291	- 10
4119	y Scorpii	6,6	- 9 48	Λ2	2",8	4 ,91	27		7,9	18	1 (4)	0.3	770	
6031	4324				W	5,11	+ 11	-l· 25	1,9	18	(1)	2,1	270	+ 37
4134	d Ophiuchi	9,1	<b>- 3 26</b>	Ma	6,9	3,03	161	198°	19,9	,	(5)	0.5	337	+31
6056 4135	3903 yl Normao			han	O*	3 ,05	+ 47	-l-155		31		4.1		
6058	10474	טי א	-49 49	F8p		5 ,00	7	236°	18,5	- 1	(1)		300	- 1
4143	d Scorpil	12 ,1	-28 22	Λo	3" ·	5 ,12 4 ,87	114	197°	-12,4		 	0.7		
6070	12037				w	5,08	+ 16	+113	- 12,4			5.2	317	+14
4145	ya Normae	12 ,4	<b>-49</b> 55	Ĩĸo-	1	4 ,14	182	253°	-28,8		· -	المدور ا	301	_ ~ i '°
6072	10 536	• • •		1	1	4 ,27	-140					5,4		•
13043	4082. ADS 9000.	WALL OF	wormed black	- A.L.			_							

Boss 4082. ADS 9909. Well observed binery with a period of 45 years. Dynamic parallax 0",045. — Boss 4066, 4067. Doubtices a physical system. ADS 9913. — Boss 4093, 4095. Forms possibly a physical pair in spite of the differences in p. m., rad. vel. and parallax. — parallax 0",007.

Period of 45 years. Dynamic parallax of the differences in p. m., rad. vel. and parallax. — parallax 0",007.

							16"								
1	2	3	4		5	6	7	8	9	10	11	12	13	11	15
147	# Ophiuchi 4086	13 <sup>m</sup> ,0			ΙζΟ	5',1 Y <sup>3</sup>	3 <sup>111</sup> , 34 3_, 39	86 -  48	- 68°	- 9,8	31 30	(3)	3,0		+30°
155 5081	o Scorpii 12849	1	-23		A3	$A_1$	4,76 4,92	1 5	199° + 42	- 8,5	16	(2)	2,9	320	+16
11 58 5084	σ Scorpn 11485	15 ,1	-25	21	134	3° W	3 ,08 3 ,28	34	200° -⊦ 34	V 11 - 3,2	9	(4)	-2,2 0,7	320	+16
1162 5092	τ Herculis 2169	16 ,7	-1-46	33	B5	2º,4 W	3 ,91	- 32 - 20	338° + 25	-13,8	13	(1)	-0,5 1,4	40	44
1163 5093	σ Sei pentis 3215	17,0	+ 1	16	Fo	3°,7 Y1	4 ,80 4 ,96	172 159	285° + 64	-46	29 29	(5)	2,1 6,0	342	+32
1165 5095	7 Herculis 3086	17 .5	+19	23	FO	3°,7 Y1	3,79 3,95	- 62 59	309° + 20	-43	29 28	(5)	1,0 2,8	2	+40
1166 5098	ζ Triang Aust 2558	17 ,6	-69	52	GŌ		4 ,93 5 ,05	228	63°	Va. + 8,5			6,7	287	-15
1168 5102	y Apodis	18 ,1	-78	40	Ιζο	-	3 ,90 4 ,05	141 - 79	237° +117	+ 5,1	20	(i)	0,4	280	-21
1169 5103		18 ,2	- <del>-</del> -31	7	IÇ O	5°,4 Y2	4 ,72 4 ,84	132 102	314° 84	-29.7	17 17	(5)	0,9 5,3		+-43
1170 5104	ψ Ophiuchi 4365	18 ,3	19	49	KO	5°,4 Y <sup>2</sup>	4 .59 4 .58	66 + 11	196°	+ 0,2	13 13	(1)		323	+19
1173 5107	v <sup>1</sup> Coronae Bor 2773	18 ,6	+34	2	Ma	7 <sup>1</sup> ,1 OY3	5 ,36 5 ,35	49 49	174°	-13,6	11	(1)	0,6		+43
1175 5108	v <sup>a</sup> Coronae Bor 2771	18 ,7	+-33	56	IC 5	7°,0 ()Y <sup>3</sup>	5 ,28 5 ,39	55 - 55	_ 4°	-39,8	12 12	(1)	0,7	22	+43
1180 5115	8 Normae 10765	19 ,8	-47	20	B 5		4 ,71	10 - 3	217°	Vai.	2 2	(1)	-3.8 $-0.3$	304	# 0
1182 5117	ω Herculis 3049	20 ,8	+14	16	Aop	2°,9 W	4 ,53 4 ,76	79 + 78	146° + 9	- 7	20	(3)	1,0	357	+37
4183 6118	χ Ophluchi 4282	21 ,2	-18	14	Взр	3° W	4 ,85 5 ,01	31 + 10	188°	Vai 8,1	8	(3)	-0,6 2,4	326	+20
4189 6129	v Ophruchi 4243	22 ,4	- 8	9	A2	2',8 W	4 ,68	84 - 76	276°	-30,8	23	(1)	-	334	-1-26
4 1 92 61 32	η Diaconis 1591	22 ,6	+61	44	G 5	5°,1 Y2	2 ,89	62	343°	-14,2	40	(5)	0,9		+40
4193 6134	α Scorpπ 11359	23 ,3	-26	13	Ma A3	7°,2 OR3	1 ,22	+ 6	192°	Var - 3,0	15	(5)	-3.4	320	- -14
4198 6141	22 Scorpu 12695	24 ,1	-24	54	<b>I</b> 33	20 Y	4 ,87 5 ,02	+ 7	188°	- 5	7 7	(3)	-0,9 2,	321	+14
4200 6143	N Scorpir 11 044	24 ,8	-34	29	133	-	4 ,33 4 ,49	+ 1	200°	Vat	1 6	(2)	1,5 1,4	3   3   4	8
4201 6146	g Herculis 2714	25 ,4	+42	6	Mb	7°,4 O8	5,02 4,7-5,5	28	130°	+ 3,3		(1)	1, 2,		+43
4202 6147	φ Ophiuchi 4298	25 7	-16	23	"IKO	5°,1 Y <sup>8</sup>	4 ,40 4 ,42	66 - 34	236°	- 34,4	-1 -	(3)	-0,: 3,	2 328 5	1-20
4204 6148	β Herculis 2934		+21		Ko	5°,1		107	257°	-25,8	27 25	(4)	- 0,: 3,	2 7	1
4203 6149		25 ,	9 + 2	12	Ao	2º,6 W	3 ,85		210°	Var 15,9	20	(5)		3 344	-l-31
4206 6153	ω Ophiuchi 4381	26 ,	2 -21	15	Fo	2º Y1	4 ,57	- 33 + 9	39°			(3)		5 324	+17
4212 6159	h Herculis 3008	27 ,	9 +11	42	K5	6°,9	4 ,92	204 - 75	245°	+ 3,1		(4)		9 355	+-35
4213 6161	A Draconis	28 .	+68	59	B8p		4 ,98	42	325	Var - 9,1	11	(4)		2 68	+37
4215 6163	β Apodis	28 ,	8 -77	18	Ko		4 ,16	451						282 5	-20
C 103		1	1		1	1	, , ,-,	1 - 57	1 1 1-14	•	,		. ,	-,	

Boss 4173, 4175. Seem not to form a physical pair Have been included on basis of equally large parallaxes — Boss 4193 Antares

radial velocity undergoes slight changes which seem to be real. No variations in the light of this star have been discovered so far —

>BS 4203 Well known binary = ADS 10087 The period seems to be around 150 years. The dynamic parallax is 0",022—0",038

18h to 17h.

					16"	to 17".						
	а	3	4	3	()	7		Ų	10	11 14	11 15	13
4218 u165	7 Scorpil 11018	20°.7	2H°	1' 110	a, k	2",91 1 .11	39	197"	1 14	[0 (3) ]0	21 40g 000	1 12*
4219 6166	H Scorpil	29 .8	35	3 Mn		4 , 10	1 41	124"	1,2	19 (1)	0.7 114	17
1220 6168	o Herculia 2724	30 ,9	F42 3	19 A0	25,6 W	4 .45	37 27	144"   25	1 "			141
1225 0175	¿ Ophluchi 4350	31 ,7	-10 2	2   110	2',8 W	2,70	21	45" 21	20 '	H (4)		1 22
4246	& Horoulis	37 .5	1 31 4	7 60	4°,4 Y	3 ,00	1#14	310"	- 71	91 (6) 88	A 14	1 39
6212 4250	a Triang Aust,	38 ,1	68 5	1 K2	67.8	1 ,88	3H8	148"	3.4	ju (4)	11,7 270)	16
6217 4255	y Hercolls	39 .5	+39	7 Ko	5.1	3,61	101	100	J- 8,0		1,0 49	F40
6220 4250	g Draconis	40 ,2	-1 64 4	7 Ko	6',0	3 ,66	176	167	1 0,3			+ 18
6223 4265	1145 4 Arao	41 .1	5R 5	2 K5	Am	4 ,01 3 ,68	57	14.4*	1 9.7	29 (1)		~ 10
6229 4270	6906 Druconb	43 ,4	<b>⊢56</b> 5	8 Fo	4",0	7 ,H4 4 ,HH	F 46	14 26°	0 1	1 - 1-1		  -  Jy
6237 4272	1702 2 Scorpii	43 .7	-34	7   K0	Y1 5",0	5 ,04 2 ,30	— 54 667	(0) 248°	2,3	31: 40, (2)	0,7 317	,
6241 4273	11 285 20 Ophluchi	44 .3	-10 3	6 F5	450	4 ,73	520 133	1420 141°	0,5	46 41 (3)	6.5 4.8 335	4 19
6243	4394 µ¹ Scorpii	45 .1	<b>→37</b> 5	1 111p	2°,0	4 ,81 3 ,09	-1- 110 31	194ª	VAL	41 9' (4)	4.1	+ 3
6247 4281	11 033 #* Scorpii	45 ,6				3 ,46	F 2	4 31	1 2	- 61 7 (4)	n,5	1
6252 4284	11 037 52 Horonia	46 ,3		0 A2p	2".8	3 ,92	- 10   - 76	163	1 0.8	at (3)	1,1	+ 10
6254 4287	2220 Li Scorpii	47 .0			w	5 ,05	1- 44	- 64 163"	20	14 17	4.3	_
6262 4292	11633 (* Scorpii	47 ,0				5 .02	1 11	+ 17		181	1 14	Ü
6271	11616				- Art 4	3 ,82	- 51	4 201	- 18,8	17 (1)	5,9	0
6281	- 3092 - £ Aras	49 ,3			27,1 W	4 ,29	- 19	+ 71	Var. -21	19 (3)	3,6	+29
6285	7766	50 ,3		0 K5	7".5	3 ,06 3 ,25	- 47	+ 40	- 6,1	21 (2)	1.4	- 9
4313 6295	10 878	51 ,6		0 K2		4 ,15	- 4	284	+24,4	19 (1)	0,3 303	- 8
4315 6299	a Ophluchi 3298	52 ,9		2 Ko	¥7	3 ,42 3 ,41	295 -236	267* + 177	- 56,2	39 (3) 37	1.3 356 5.8	+28
4322 6315	h Draconis 1157	35 .4		7 F 5	3.7	4 ,82	252 -244	- 79°	Var. 22,6	64 (4)	3.9 62 6.8	+36
4323 6318	30 Ophlachi 4215	55 ,8		4 Ko	0 .7 Y	5 ,00 4 ,06	103 - 16	211" + 102	- 6,7	14 (3)	0,7,343	+21
4327 6322	≢Urace min, 498	56 ,2		2 G5	5,6 Y	4 ,40	- 15	94.	Var.	7 (2)	1.4 82	+31
4328 6324	# Morenite 2947	56 ,5		4 A0	27.7 W	3 ,92 4 ,14	- 31 - 24	295° + 45	Vat. 25,1	24 (3)		+35
4334 6334	k Scorpill 11 700	58 ,2	<b>-33</b> 5	9 Btp		4 ,87 5 ,03	+ 7	82	+10		316	+ 3
4346 6355	60 Horonila 3142	0 ,7	+12	3 Å3	2",6 YG1	4 ,91	56 + 54	108* - 16	- 3,2	19 (3)		+28
4360 6378	a Ophiuchi 4467	4 ,6	-15 3	6 A2	3".3 W	2 ,63	93	23° - 92	- 1,2	30 (3) 28		+12
	ANA Walthmann		T			_ ,00	. 13	- 94	1	40	2,5	

Dans 4246. Well'inown binary — Boss 4277, 4281. Certainly a physical pair — Boss 4287, 4298. Doos suct summ to be a physical pair, — Boss 4315 Variable 4m, 1— 5m,0 photographic.

				1			17"•								
1	2	3			5	6	7	8	9	10	11	12	13	14	15
4361 6380	η Scorpπ 11485		-43°	6'	F2		3 <sup>m</sup> ,44 3 ,56		+ 283	-28,4			5,8	312°	- 3°
4368 6396	ζ Diaconis	8,5	+65	50	B5	2°,2   W	3 ,22 3 3 ,45	- 2; + 6	327°	14,5	18 16	<b>(</b> 4)	-0,8 0,1	63	十35
4370	36 Ophruchi 12 026	9,2	-26	27		ر <sub>ا</sub> –	5,33	1235	202°	- 0,2	158	(1)	6,3	326	<del>+</del> 6
_ 6401 4371	36 Ophuchi	9,2	-26	27	Kol	Х3 б	5 ,32 5 ,29	$\frac{-198}{1224}$	+ 1223 203°	- 0.6	158		6,3	326	<del>+</del> 6
6402 4373	12026 J	40 4	+14	30	Mb	Ya 7°,0	5 ,28 3 ,32		+1200	22.6	9	/m\	10,7		
6406	3207		_	30		Oa	3,52	30  - 25	<b>— 17</b>	- 32,6	7	(7)	-2,5	3	+-27
4374	α <sup>2</sup> Herculis 3207	10 ,1	14	30	G	5° BG2	5 .39 5 .43	- 32 - 22	- 23	38,0			0,1 2,8	3	+27
4376 6410	δ Herculis 3221	10 ,9	+24	57	A2	2°,5	3,16 3,41	165 127		Vai 39	38 38	(5)	1,1 4,3	14	+30
4379 6415	41 Ophiuchi 3255	11 ,5	- 0	20	K 5	5°,7	4 ,82 4 ,82	65	204	Vai - 2,6	17	(4)		<del>3</del> 48	+19
4380 6417	ζ Apodis 3310	11 ,5	67	40	К2	-	4 .74	38	290°	+ 12,6	.,		_	291	18
4.381	τ Herculis	11 ,6	+36	55	K 5	6°,0 Y <sup>3</sup>	4 ,85 3 ,36	- 37 25	265°	~-25,7	22	_ (4)	- 2,6 0,1	28	+33
6418 4388	2844 68 u Herculis	ī3 <sup>-</sup> ,6	+33	12	133	1°,9	-3 ,32 Vai	24		Var	22	(a)	0,3	23	+32
_ 6431 4391	2864 c Herculis	14 ,2	+37	24	Λ2	2°,2	5,01 — 5,5 4 ,80	+ 17 60	7 -1 17 323°	-21,2 -10	19	(2)	1,2	28	-1-33
<b>643</b> 6 <b>- 4</b> 394	2864 § Ophuch	15 .0	-21	1	F 5	G1 4º	4 ,89	- 22 315		- 9,2	19 65	(a)	_3,9	331	+ 7
6445 4395	4731 Serpentis		-12		Ao	Y1 3°,7	4 ,55	+ 274	1-1- 151				7,0		
6446	4722		-			YG1	4 ,51	+ 3	5 - 10	+ 7	21	(2)	2,2	338	+12
4399 6453	# Ophruchi 13292		-24	-	133	2º W	3 ,37		5  - 31	- 1	7	(3)	-2,4 0,9		+ 5
4406 6461	β Λιαο 8100		-55		K2	7°,0	2 ,80 3 ,01	- 36	9 + 35	- 0,8	17	(2)	-1,1 0,6		12
4405 6462	y Atae 8225	17 ,0	-56	17	<b>1</b> B 1	2°,5	3,51	1	0 -1- 13	- 4	4	(2)	-3,5 -0,9	302	-12
4419 6484	Q ITerculis 2878	20 ,2	+37	14		36 R1	5 ,47	34		20			0,0	28	-+31~
4419 6485	Q Herculis 2878	20 ,2	+37	14	AO	2°,2 G1	4 ,52	3	8 264°	-21	12	(4)	-1,0	28	+31
4420	b Ophuchi	20 ,3	-24	-5	Fo	3°	4 ,28	13:		-37.2	33	(2)		330	+ 5
6486 4421	d Ophiuchi	21 ,0	-29	47	F 5	$A_n$	$-\frac{4}{4},\frac{41}{37}$	15		+ 37,8	33		4.9	324	+ 2
6492 4423	43 557 Ophruchi	21 ,3	- 5	0	Fo	4°,0	4 ,47	10	4 151 4 242°	Var	21	(3)	5,4	346	+15
6493 4425	d275 o Ophwchi		5 + 4	-	1¢o	Y1,6	4 .73	- 7	7 + 70 4 45°	+0.4 $-27.3$	19		4,7	354	
6498	3422					Ya	4 ,40	+ :	2 4		16	(2)	-2,6		
4426 6500	8 Arae 6842		-60				3 ,79 3 ,94		3 + 93	+12	27 27	(1)	3,8		
4429 6508	v Scorpii 11 638	24 ,0	-37		В3	2°,3	2 ,80 3 ,01	+ 4	2 183° 4+ 42	Vai.	10	(3)	-2,2 0,9		- 3
4431 6510	α Λιαο 11511	24 ,1	-49	48	Взр	3°.7	2,97	9	And a state of the	Var. - 2,2	21 20	(3)		308	-10
	Nov Ophiuchi	24 .0	-21	24	Nov		-4 to 15						-,,	333	+ 6
6595 4434	c <sup>2</sup> Ophluchi	25 ,3	-23	53	A.0	3°	4 ,89	3		-12	38	(a)		330	+ 4
6519	13412		[			W	5 ,04		7 + 37				2,8		1

Boss 4370, 4371 Certainly a binary system with a very long period of revolution Dynamic parallax 0",054 — Boss 4373, 4371 Fibreulls is probably an irregular variable between 3m,1 and 3m,9 The dynamic parallax is 0',006—0',022 — Boss 4388 A visual binary — Boss 4419 Zinner has derived a combined magnitude of 4m,33 for this pair The RHP value is 4m,14 Tor p in see the Appendix of the PGC 174.

							17".									ł
1	2	3	4		3	Ú	Y	U	9	10	11	11	13	14	13	
4438 6526	1 Herculis 3034	26°.7	4 26°	11'	Ко	(7,3 () <sup>u</sup>	4",48 4 ,51	- 21 - 4	45° 21	- 26,8	21	(5)	1,1	176	1 27°	
4439 6527	λ ScorpH 11 6/3	26 ,H	37	2	H2	37,0	1 1 .71	36	186°	Var	12	( 4)	1,5	120	· 1	
4443 6536	# Diagonia 2065	28 ,3	4 52	23	(+0)	\$",0	2 .99 3 .08	16	297"   11	~ 20,9	7	(1)	3,8	40	1 32	
4445 6537	o Arno 11661	28 .3	- 46	26	Λυ		4 .01	561 35	326"	1 4	,		4,4	112	9	
4450 6546	Q Scorpil 12044	29 ,6	-38	34 (	Ko		4 .17	210	185"	49,2	2±1 <sub>1</sub> 2±11 <sub>1</sub>	(1)	6,0	118	•	
4457 6553	# Hearph 12312	30 ,1	~42	56	Po	41.7	2,04	12	160°	1 1,4			2,6	114	7	
4458 6554	rt Draconia 1944	30 ,2	-} 55	15	Λ5	27.9 Y1	4 ,98	158	73"	14,2	3H	(5)	6,0	51)	1 13	
4400	≠ 1)raconts 1945	30 ,3	<b>⊹-55</b>	14	Λs	27.0 YI	5 ,16	165 - 165	7.1"  - 5	Var 17	i		0.1	\$1) .	F33	1
4459 6556	a Ophlachi 3252	30 ,3	+12	38	Λ5	27,5 W	2,14	+ 180	153"   181	Var  -15	53	(4)	4.3	4 1	1 22	
4462 6561	# Surpontia 4621	31 ,9	-15	20	Λ5	4°,0 Y1	3 ,64 3 ,83	- 34	312"   76	-42,H	50	(1)	3,1	139	+ 7	
4465 0567	µ Ophluold 4472	32 ,4	8	3	រាទ	3",6 \V	4 .65	25	1H9*	18	9	(2)	1,7	345	+11	
4466 6569	λ Arao 11616	32 ,6	-49	21	175		4 .84	4 123	149*	+ 3.7			6.4		-11	
4474 6580	и Всогра 12137	35 .0	-3B	59	B2	27,5	2,51	_ 28	201*	Var. -10	8	(2)	~3.3 ~0.1	319	~ G	
1475 6581	o Sorpontla 4808		-12	49	A2	1',2 Y(+1	4 ,39	- 62	231°	30	20	(1)	4.2	341	+ 8	
4476 6582	y Pavenis 3662		-64	41	Ko		3 .58	- 50g	188*	B₁1	18	(1)	2,1	205	-19	
4479 6588	a Horculla 2349	36 ,6	+46	1	133	27.1 W	3 .79	1- K	+ 1	- IH,6	1		-3.H -1.7	39	<b>小3</b> 0	
4481 6595	58 Ophluchi 4712		-21	38	1/5	3,	4 ,89	- B3	4- 62	LI,0			, 5,0	333	+ 3	
4483 6596	m Draconia		+68	48	175	A.'4	4 ,87	327 - 52	-1-324	VAF - 14,0	36	(4)	7.4	66	+31	
4487 6603	# Ophluchi 3489	38 .5		37	Ko	3°.5	2 ,94 3 ,01	- 60	344° -137	- 12,2	33 32	(4)	3.0	357	+16	
4492 6615	4 Scorpit		-40	5	Y5p	47,4	3 .14	+ 3	- 50°	- 20,7	7	(1)	-1.6 -3.9	316	- 7	
4493 6616	X Bagittarii 11930		-27	48	F8	As A	Var. 4.4-5.0	_	+ 23	-13,5	6	(1)		32Å	- 1	
6023	μ Horculis 2888		+27	47	Gs	Y.	3 .48	- 517 - 90		- 16,1	102	(5)	3,5	20	+25	
4498 6628	Secret 14 609		-31	40	B8		4 ,83	+ 5	173°	- 13	6	(1)	1.7		- 4	
4500 6629	y Ophiuold 3403	42 ,9		45	A0	2*,2 W	3 ,74	- 18	+ 81	Var.	17	(3)	-0,7 3.3	356	+14	
4501 6030	O Scorpil 11 907		-37	1	K2	6.3	3 ,25	+ 64	- 23	1-24,6	25 28	(2)	2,4		- 6	
4503 6631	1 Scorpit 11886		-40	4	A2p		5 ,03				j		0,8	319	- 8	
4504 6636	y Draconia 804	43 .7			FS	4°.1 Y	4 ,90		167	-10,2	39	(6)	7.0	70	+31	
4505	P Draconia 805	43 .7	+72	12	- ,	٧٠	6,07	- 5	163° -274	-10,3			8,3	70	+31	
Then	a 2460 Cambald our	4.44	and a large													

Bess 4493. Copheid variable; period 7,0 days.

17h to 18h.

					17	" to 18".								
1	2	3	1	5	6	7	8	9	10	ii	12	13	11	15
4519 6675	Scorpu 12201	49™,5	-44° 1	y Ko		4 <sup>m</sup> ,98 5 ,02	- 28 - 22	232°   18	+44,9			2,2	315°	-11°
4525 6682	Scorpu 12231	50 ,7	-41 4:	2   Ma		4 ,89	- 33, - 16 -		4,4			2,5	318	-10
4531 6688	\$ Diaconis 2033	51 ,8	+56 5	K0	Xa 2, '0	3,90 3,93	123 <sub> </sub>  - 101 -	52°   70	-25,2	29 29	(5)	0,9	52	+29
1535 6695	# Herculis 2982	52 ,8	37 1	Ko Ko	5°,6	3 ,99	- 6, - 51-	45°	-28,1	11 8	(7)	1,5	30	- -25
1536 6698	1 Ophiuchi 1632	53 .5	- 9 4	Ko	5',1 Y2	3,50	118	186° - 118	+12,7	22 20	(3)	0,2	345	+ 6
4537 6700	4 Sagittarii 13731	53 ,7	-23 4	A O	2' Y1	4 ,76 4 ,90	58 + 2-	179° - 58	-22	8	(a)	-0,7 3,6	333	- 1
4538 6703	z Herenha 3156	53 ,9	+29 1	Ko Ko	5".4 Y3	3 ,82 3 ,86	90	107° - 14	- 1,8	26 26	(5)	0,7 3,6	22	+23
1541 6705	y Diaconis 2282	54 ,3	+51 31	K5	6',5 OY3	2,42	+ 9-	197° - 26	-27,2	33 30	(3)	0,2 -0,4	47	-l-29
4542 6707	p Herculis 3093	54 ,7	+30 1	I to	3',8 Y1	4 ,48	6		-22,1	<b>12</b>	(3)	-4,0 -2,5	23	+22
1544 6710	ζ Scrpentis 1217	55 ,2	- 3 4	Ĭ Ō	3',9 Y1	4 ,60	153		-43	31 31	(2)	2,1 5,5	351	+ 8
4545 6712	66 Ophiuchi 3570	55 ,3	+ 4 2	B3	2',5 Y2	4 ,81	- 19 - 7-		Vai	8 8	(3)	-0.7	358	+12
4547 6713	93 Herculis 3335		+16 46		5°,9 W	4 ,71 4 ,69	 → 6 -1		-23,0	11 11	(4)	-0,1 0,1	10	+17
4548 6714	67 Ophiuchi 3458	55 ,6	+ 2 50	B51	W	3 ,92 4 ,14	+ 2-	of Months	- 4,4	5	(4)	-3,1 -0,4	357	+11
4552 6723	68 Ophruchi 3560	56 ,7	+ 1 1		3°,3 W	4 ,44 4 ,60	+ 9		Vai	20	(3)	0,9	356	+10
4556 6729	95 Herculia 3280	57 ,3	+21 30	G 5	3',9 R1	5 ,21 5 ,28	30	27° - 48	-30,9	8	(1)	-0,3 2,6	15	+19
4557 6730	95 Herculis 3280	57 ,2	+21 30	A3	G1	5 ,13 5 ,20	30	- 48	-27	14	(a)	0,8	15	+19
4559 6733	τ Ophiuchi 4549	57 ,6	<b>→</b> 8 11	Fo	4°,3 Y1	6,04	+ 21 -	152° - 40	Var	18 18	(1)	2,3 4,3		+ б
4559 6734	τ Ophwchi 4549	57 ,6	- 8 1		4°,2 Y1	5 ,34 5 ,49						1,6		+ 6
4564 6742	W Sagitlarıı 14447	58 ,6	-29 3		X5	Vai 4,3-5,1	+ 9-1		-25,0				329	- 6
4565 6743	θ Aine 11720	58 ,8	-50	B11		3 ,90 4 ,04	- 30 - 12-		+ 3	8	(2)	-1,6 1,3		15
4566 6745	π Pavonis 4292	58 ,9	63 40			4 ,44 4 ,54	192 17	175° - 192	-14,9	29	(a)	1.7 5.9	~ ***	21
4568 6746	y Sagittarii 15215		-30 20		54,3	3 ,07 3 ,31	_	197° - 195	+21,5	34 32	(3)	4.6	329	- 6
4571	70 Ophluchi	0 ,4	+ 2 3	Ko	5°,3	4 ,07	1131	1678	- 7,2	136	(8)	4,0	358	+10
6752 4577	3482 Sagittarii	1 ,8	-28 28	Ko	Q0	4 ,10	+ 238 + 37	153°	- 4,5	96			331	- 6
6766 4580	14174 71 Ophwchi	2,5	+ 8 43	G 5	5°,6	4 ,64	+ 16 + 25	0 0	— 3,5	12	(2)	$-\frac{2.5}{0.1}$	4~	+12
6770 4581	3582 72 Ophuchi	2,6			2°,8	4 ,78	103	- 25 323°	-25	12 43	(3)	1,7	5	+13
6771 4584	3564 o Horculis		+28 4		Y1 2°,2	3 ,95	- 58	- 85 56°	-27	43	(2)	3,8	23	+-20
6779 4588	2925 s Telescopii	3 ,8			w	4 ,05	+ 4-	1 205°-	-26,5	24	(1)	-3.2 $-0.2$		-14
6783	12251	,,0	- TO 34	1150		4 ,71	- 18-		20,3	11		2,7	2.2	

Boss 4559. ADS 11005 Wellknown visual binary the period of which is around 224 years. The dynamic parallax is 0",028 — Boss 4564. Cepheld variable, period 7,6 days — Boss 4571. The components are 4m,28 and 5m,98 — Boss 4581. Light possibly variable.

						10								
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4590 6787	102 Herculis 3674	4 <sup>m</sup> ,4	+20°48′	В3	2º,0 W	4 <sup>11</sup> ,32 4,56	- 17 - 3	183° + 17	-13,5	5	(1)	-2,2 0,5	15°	
4591 6789	d Ursae min. 269	4 .5	+86 37	Λo	2°,3 W	4 ,44 4 ,66	52 19	22° + 48	- 8:	17	(2)	0,6 3,0	87	+28
4604 6812	μ Sagittarii 4908	7 ,8	-21 5	В8р	3°,7	4 ,01 4 ,20	+ 4	141° + 5	Var. + 9,2	12	(a)	-0,6 -2,0	338	- 3
4617 6832	η Sagittarli	10 ,9	-36 47	Mb	50,2	3 ,16	216	219°	+ 9,2	20	(2)	-0.7	324	-11
4619	Sngittarii	11 ,8	-27 5	K 5	80	3 ,24 4 ,69	<del>-145</del>	+160 53°	-16,9	11	(1)	4,8 -0,1	333	- 7
6842 4625	12684 § Pavonis	14 ,0	-6i 33	K2	Og	4 ,66	+ 8	5 319°	Var.	23	(1)		300	-21
6855 4628	å Sagittarii	14 ,6	-29 52	Ko	60-70	4 ,38	<u> 7</u> 51	135	-20,0	23	(3)	-0.5	331	~ 9
6859 4635	14834 74 Ophiuchi	15 ,8	+ 3 20	G 5	ΟΥ <sup>8</sup> 5°,4	4 ,92	+ 34	+ 38 259°	+ 5,1	28	(2)	1,4 -0,3	ō	+ 7
6866 4636	3680 106 Herculls		+21 55	IC 5	Yº 6°,1	4 ,90	- 15 62	+ 1	-32,0	11	(3)	0,8		+15
6868 4638	3390 y Serpentis		- 2 55	Ko	Y <sup>8</sup>	4 ,97	- 15 898	+ 60 219°	+ 8,9	11	(3) (š)	3,9	355	+ 4
6869 4639	4599 k Lyrae	16 ,4		KO	Y8 5°.7	3 ,52	-647	+620		56		8,2	1	
6872	3094				Y1,5	4 ,34 4 ,41	38 + 36	325° + 12	-22,7	17	(4)	0,4 2,2		+20
6879	& Sngittarli 12784		-34 26	Ao	4°,5	1 ,95 2 ,20	- 51	198° +129	-11			2,7	327	-11
4650 6884	& Scuti 4712	18 ,2		G5	5°,4 Y <sup>8</sup>	4 ,83 4 ,89	62 + 47	44° - 40	Var. - 4,7	16 16	(4)	0,9 3,8	349	+ 1
4656 6895	109 Herculis 3411	19 ,4	+21 43	Ko	5°,4 Ya	3 ,92 3 ,98	324 + 55	144° +318	-58,2	35 31	(5)	1,4 6,5	18	+14
4655 6896	21 Sagittarii 5134	19 ,4	-20 35	Ko Ao	6°,2 OY <sup>9</sup>	4 ,96 4 ,92	+ 7	158° + 22	-11,5	10	(a)		339	- 6
4657 6897	α Telescopii 12379	19 ,6	<b>-46</b> 1	В3		3 ,76 3 ,88	53 15	191° 51	- 0,8	12 11	(3)		316	-17
4662 6905	Telescopii 12153	21 ,1	-49 7	Ko		4 ,14 4 ,28	294 +121	151° +268	-30,5	22	(1)		313	-18
4665 6913	l Sagittarli 13149	21 ,8	-25 29	Ko	6°	2,94	197 - 67	194° + 185	-43,2	58	(5)	0,4	335	- 7
4666 6916	v Pavonis 5879	22 ,6	<del>-62 20</del>	В8		4 ,81	34	192°	+59	_31		4.4	300	-22
4670 6920	φ Draconia	22 ,2	+71 17	Aop	20,2	4 ,90	$\frac{-10}{32}$	+ 33 353°	Var,	12	(3)	2,5 -0,8	68	- -28
4671	b Draconis	22 ,5	+58 45	A2	W 2°,7	4 ,46	+ 8	+ 31 329°	-16,8 Var.	26	(3)	1,8 1,8	55	+26
6923 4672	χ Draconis	22 ,9	+72 41	F8	4°,7	5 ,14	+ 43	+ 47 125°	-12 + 32,1	25 121	(4)	3,9 4,1	71	+28
6927 4674	839 γ Scuti	23 .5	-14 38	A 3	Y <sup>2</sup>	4 .73	- 568 9	+287	— 51	120	(1)	7.7	345	- 4
6930 4686	5071 42 Draconis	25 ,7	+65 30	Ko	Y <sup>1</sup> 5°,6	4 ,92	+ 2	+ 9 105°	+33,2	19		-0.5		+27
6945 4689	1271 D Coronas Aust			G 5	Ya	4 ,96	-104 47	- 9 125°		18		5,1		
6951 4705	13378 & Scuti		- 8 19	Ko	60.4	4,76	+ 36	+ 30	-0,5	8	(1)	-0,8 3,0		-16 
6973 4707	4638 d Draconis				6°,1 Y8	4 ,06 4 ,03	318 - 83	184° +308	+35,6	21	(4)	6,6	352	- 1
6978	2113		+56 58	F8p	4º,8 Yi.6	4 ,95 5 ,03	+ 1	202° - 11	-11,3	3	(1)	-2,7 0,2		+24
4709 6982	ζ Pavonis 2553	31 ,4	-71 31	Кo		4,10	155 - 29	184° +152	-16,9	35 35	(1)	1,8 5,1	290	26

		<del></del>				18".								
1	2	3	4	3	6	7	8	9	10	11	12	13	14	15
4722 7001	a Lyiac 3238	33 <sup>m</sup> ,6			1°,3 131	0 <sup>m</sup> ,14 0 ,31	346 + 48	36° +343	-14,2	115	(4)	0,4	35°	+19°
4725 7012	Pavonis 3948	35 ,7	-64 5	8 A2		4 ,90 4 ,98	114	182°	+- 5				298	-25
4731 7020	δ Scuti 4796	36 ,8	9	9 F0	4º,0 Y¹	4 ,98 4 ,74 4 ,83	14 + 12	+ 141 107° + 7	-Vai -47.9	14	(2)	5.7 0.1 0.4	352	- 3
4734 7029	Sagittarii 12876	37 ,6	-35 4	5 B3		4 ,82 4 ,98	53	180° + 52	+ 2,8	14	(ī) <sup>-</sup>	1	327	-15
4739 7039	φ Sagittarii 13170	39 ,4	-27	6 338	3' YG1	3,30	48 + 47	91° + 12	Va1 	16	(1)	1	336	-12
4747 7051	3509	41,0	+39 3	4	2°,8	5,06 5,30	52 + 32	10° 41	31,2	18		1,3	37	+18
1748 7052	ε <sup>1</sup> Lyrae 3509	41 ,0	+39 3	4 A3	OR1	6,02	57 + 42	1° + 39	33.5	18	(1)	2,3 4,8	37	+18
4749 7053	<sup>8</sup> Lyrae 3510	41 ,1	-1-39 3		2°,9	5,14			-15			,,-	37	<del>-1</del> 18
4749 7054	ε <sup>2</sup> Ly1ae 3510	41 ,1	+39 3		Y1	5 ,37, 5 ,69	64 + 36	14° 53	-16		-	4,4	37	-+-18
4752 7056	ζ¹ Lyıae 3222 ]	41 ,3	+ 37 3	0 A3	3°,6	4 ,29	31	56°	Var	30 30	(6)	1,7	35	+17
4752 7057	ζ <sup>8</sup> Ly1ac 3223	_	-1 37 3		3°,0	5 ,87	31	56° + 31				3,3	35	+17
4753 7061	110 Herculis 3926	41 ,4			4°,0 Y16	4 ,26	345 -238	183° +248	+22,2	65 65	(4)	3,3 6,9	18	-F 9
4756 7063	β Scut1 4582	41 ,9			5°,9 ¥8	4 ,47	25 16	205° + 19	Vat -20,9	10	(3)	-0,8 1,5	356	- 2
4758 7064	Ly1ae 3349	42 ,0			5',7 Y <sup>8</sup>	4 ,92 5 ,11	29 - 29	27°	-16,9	19 19	(2)	1,3 2,2	25	+11
4759 7066	R Scuti 4760	42 ,2		9 150	O2	Vai 4,7-8,0	- 70	243° + 15	Var  -38,3	-3	(a)	4,0	356	- 3
4761 7069	411 Herculis 3823		·	4 A3	2°,7	4 ,37	123 +113	- 48	Vat -46,7	38 36	(5)	2,2 4,8	16	+ 7
4762 7074	λ Pavoms 5983		-62 1			4 ,42	- 17	235°	+20			0,8	301	-25
_	Aquilae	43 ,8	- - 0 2	Nov		-0,2 to	- 18	194° 16	13	3,1	(3)	-8,3 $-3,9$	0	- 1
4776 7106	β¹ Lyrao 3223	46 ,4	+33 1	1321	Y15	Vai 3,4-4,1	8 8	152° + 3		8	(1)		30	+14
4778 7107	и Pavoms 3603	46 ,6	-67 2	1 F51		Vai 3,8-5,2	- <sup>17</sup>	- 335°	+36,3	3	(a)		296	-26
4781 7116	v <sup>1</sup> Sagittarii 4907	48 ,1		2 65	5",6 OY <sup>2</sup>	4 ,96 4 ,99	+ 3	158° 18	11,6	8	(a)	(), 5 1, 3		-12
4784 7121	o Sagitlarii 13595	49 ,1		5 33	1°-2°	2,14	- 66 - 7	173°	-10,7	16 16	(2)	-1,8 1,2	337	-13
4790 7125	o Draconis 1925		-1-59 1	o IX o	6",1 Y8	4 ,78	- 68 - 68	74° -1 53	Vai 19,5	12 12	(5)	0,2 4,4		+23
4797 7133	113 Herculis 3524			2 G0 A3	4,9 Ya	4,56	5 2	- 325°	-23,8	14	(5)	0,3 1,9		+ 9
4799 7137	Dinconis 2686		-1-50 3		4°,9 Y <sup>g</sup>	4 ,97 5 ,08	33 - 16	178° - 29	+ 8,2	10 10	(1)	0,0 2,6	48	+20
4800 7139	δ <sup>2</sup> Ly1ae 3319		- -36 4		7°,0 Os	4,52	+ 9	4	-26,6	7	(3)	-1,3 $-0,5$		+14
4802 7141	91 Serpentis 3916	51 ,2		4 A5	3°,0	4 ,50 4 ,89	53 52	- 59°	-41	22 22	(2)	1,2 3,1		- 1
4803 7142	θ <sup>a</sup> Serpentis 3917	51 ,2	+ 4	4 A5	3°,0 Y1	5 ,37	48 + 48	68°	-42			2,1 3,8	5	- 1
17.	es 4700 Tion o non	1-1-1	Ale Levelant			1 111.4	The steet				1-3	87 1 . 6	ttt	

Boss 4722 Has a variable radial velocity and might also vary in light Photoelectric methods have revealed a slight variation in the light (Gurinnen) — Boss 4752 71nnan gives the combined magnitude 120,60 for this pair — Boss 4759 Irregular variable 420,5 to 910 — Boss 4778 Copheld variable, period 9,1 days

					181	to 19h.								
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4808 7149	η Scuti. 4976	51 <sup>th</sup> ,;	— 5° 58	Ko	5°,9	5 <sup>10</sup> ,04 5,00	71 + 50	117° + 50	-93.1				356	_
4809 7150	E Sogittarii 5201		-21 14	Ko	5°,7	3,61	37	120° + 26	-20,1	23 24	(4)	0,5	342	-12
4810 7152	s Coronae Aust	52 ,0	-37 14	15		4 .87	161 -148	235° + 63	+53	-4-		1,5	327	-19
4814 7157	R Lyrae 3117	52 ,3	+43 49	МЬ	6°,6	4,32	77	21° + 70	-27	8	(5)	5.9 1,2	41	+17
4823 7176	s Aquilao 3736	55 ,1	+14 56	Ko	5',6	4 ,21	100	220°	-51,6		(5)	0,8	15	+40
4824 7178	у <b>Lyreo</b> 3286	35 ,2	+32 33	AOp	2°,9	3 .30	8 7	203 <sup>8</sup>	Var20	18	(5)	-0,5	31	+12
4825 7180	v Draconks 915	55 ,6		Ko	6°,1	4 ,91	66 - 37	+ 55	Var - 7,2	13	(1)	0,5	69	+25
4830 7188	Coronae Aust 13855			A0		4 ,85 5 ,00	82 + 44	134	- 7	13	-	4.0	323	-21
7189	Sagitharii	56 ,2		Peo. Nova		4.7-157		, ,,				_4,4	350	-10
4834 7193	i Aquilao 4840	56 ,3		Kō_	5',9 OY	4 ,15	4B - 41	220° + 25	-44,3	28 28	(5)	1,4	357	<b>–</b> 6
4832 7194 4847	\$ Sagittarii 16575	56 ,3		AZ	3,0	2,71	- 18	270°	+22	43 40	(2)		334	-17
7217	o Sagittarii 5237	58 ,7		Кo	4 .7 Y	3 ,90 3 ,86	98 + 51	133° + 84	+25,8	29 28	(3)		342	-14
7226 4857	y Coronae Aust.		-37 12	I/B	4*,0	4 ,26 4 ,37	301 + 27	161° +301	-51,0	65	(a)	3.3 6.7	328	-20
7234 4858	r Sagittarii 13 564	0 ,7		Ko	OA.	3,42	267 125	193* +235	Var -45,7	40 39	(3)		337	-17
7235 4859	Aquilae 3899 A Aquilae		+13 43	Ao	2°,7 YG1	3 ,02 3 ,26	102	186° + 74	Var -26	35 35	(5)	0.7		+ 2
7236	4876 Corongo Aust		- 5 2	Во	2*,8 W	3 ,55 3 ,72	93 - 55	195° + 75	-13	28 27	(2)		358	- 7
7242	13061 «Coronao Aust.		-40 39	Ko		4 ,66 4 ,69	49 + 24	136* + 43	+21,7			3,1	324	-21
7254	13350 Coronno Aust.	2 .7		A2		4 ,t2 4 ,35	136 + 56	141° +124	-18	19 19	(1)		327	-21
7259 4874	13146		-39 30	GS		4 ,16 4 ,29	36 - 15	184° + 33	+ 2,9	9	(1)	-1,1 2,0	325	-22
7264 4891	5275 y Sagittarii	3 ,6		F2	(4°,6)	3,02	40 - 18	189° + 36	-10,2	17	(3)	-0,8 1,0	344	-15
7292 4897	13866 7 Lyrao		-25 26	P5	3° Y1		53 + 28	131° + 46	Ver -33.7			3,5	340	-17
7298 4906	3490 1 Vulpeculae	11 ,9	+38 58	В3	21,1 W	4 ,46	- 3	180° - 1	- 8.7	5	(3)	-2,1 -3,2	38	+12
7306	3713			B5	2°,1 W	4 ,60 4 ,89	<b>-</b> 3	180° + 2	-17,4	8	(2)	-0,3 -2,4		+ 3
7310	1129	_	+67 29	Ko	5°,1	3 ,24 3 ,29	133 - 49	+124	+25,9	35 35	(4)	0,9		+23
7314	3398		+37 57 +53 11	Ko	6°,0	4 ,46 4 ,48	+ 0	253° - 10	-30,5	9	(6)	-1,0 -0,5	37	+11
7328 4929	2216	15 ,4		Ko	5°,2 Y•			30° +130	-29,2	29 28	(5)	1,2 4,6		+17
7337 4932	13277	15 ,9		B8	40 4	4 ,24		183° + 18	- 8	4.	(1)	-2,8 0,6	321	-25
7340 4934	5322	16 ,0		A5	YG1	3 ,95	- 15	- 27	+ 2	43 43	(4)	2,1 1,4		-16
7342	5283 4814. Verdable 4m.0			Bap Pap	YG1	4 ,58	- 4	+ 3	+11,9			1,9	350	-15

Boss 4814. Verdable 4m,0 to 4m,5 in the RHP-system — Boss 4851 Binary, the components of which are each 5m,0 in the RHP-system.

						10".	-		7.5		1.0	4.5		
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4933 7343	/} <sup>2</sup> Sagittarn 	16",0	-44° 59′	FO		1",51 4 ,52	125 -  84	+ 92		28	(a)	5,0	321°	-25°
4936 7348	a Sagittain 13215	17,0	-40 48	138		1,11 4,27	129 13	128	1 1	26 25	(2)	1,1	325	24
4940 7352	7 Diaconis 857	17 .5	+73 10	Ko	ნ',0 OY²	4 ,63 4 ,53	176 + 171	309	Vai 30, 1	16	(2)	0,7 5,8	72	-1-24
4942	3 Vulpeculae 3811	18 ,7	- -26	В5	2',1 W	4 ,92 5 ,23	15		-13,2	8	(3)	-0,6 0,8	27	+- 4
7358 4948	π Draconis	20 ,2	+65 31	Λ2	2°,7 W	4 ,63	45	25	-27,7	19	(3)	1,0	65	- -21
7371 4949	1345 2 Cygni	20 ,2	+29 26	133	1',9	4 ,82	13	42	-23	4	<b>(1)</b>	2,9 -2,1	30	-l- 5
1372 4953	3584 δ Aquilae	20 ,5	+ 2 55	Fo	3°,9	5 ,08	265		-25	59	(6)	2,3	7	- 7
7377 4962	3879 Aquilae	21 ,4	+09	Fo	Y',5	3 ,65 4 ,86	+ 254	297	0,4	58 32	(1)	5,6 2,4	_ 5	— 9 <sup>-</sup>
7387   4976	4206 & Vulpeculae	24,5	+24 28	Ma	Q, '0	4 ,93	( 170	227	-85,5	13	(5)	0,1	27	+ 3
7405 4986	3759 β <sup>1</sup> Cygni	26 ,7	+27 45	ко	OY8 5",4	1 .52	1	198		13	(5)	5,5 1,0	30	- <del>1</del> 3
7417 4987	3410 β <sup>a</sup> Cygni	26 ,7	+27 45	B9	OY3 154	3 ,19 5 ,36		0 4 234	° - 23	14	-	2,0 1,1	30	+ 3
7 118 4988	3411 J	27 ,2	+51 31	Λ2	$\frac{B^3}{3^{\tilde{o}},0}$	5,65	- 1 12	6 9	o 18	24	(4)	+1,1 0,3	52	  - -15
7420 4992	2605 8 Cygni		   +34 14	133	YG1 2°,4	4,07		8 <u>+ 100</u>	-21,8	19	(2)	4,4	35	  - - 6
7426 4995	3590 μ Aquilae	29 ,2	1	Ko	W 6°.3	4 ,97	26	3 - 2 2 126		22	(5)	-2,1	12	- 7
7429 4998	4132 9 Vulpeculae		+19 33	В8	Y8 2°,0	4 .59	+ 6	8 + 254 4 117		11	(2)	6.7	23	_ 1
7437 4999	4063 h <sup>2</sup> Sagittarii		-25 6	-139	4.	5 ,14 4 ,66	+	0 -1 4		12	_	2,1	342	-22
7440	14 184			B5	W 3°,1	4 ,82	+ 5	6 + 51		8	(2)	4,1	4	12
5004 7447	3782		- 1 31		$\mathbf{A}_{\mathbf{I}}$	4 ,59	- 1	2 1 12		8		-0,4	68	+22
5009 7462	a Diaconis 1053		+69 29	Ko	5°,2 Y2	4 ,78	184 138	0-1214		163 163	(5)	5,8		
5014 7469			8 -1-49 59	F5	3°,9	4 ,64 4 ,68	+ 21	4 + 129		61	(4)	3,5	50	+13
5021 7478	q <sup>2</sup> Cygn1 3684		1-29 56	KO	Z8	4 ,79	-H 3	355	3	15	1	2,5	33	+ 3
5023 _7479		35 ,	6 -1-17 47	Go	5°,1	4 ,37	1	16 153 7-1 32	2	6	, ,	2,1	22	- 3
5027 7488	\$ Sagittae 4048	36 ,	6 +-17 15	Ko	5",7 Ya	4 ,45		8 178 80 - 24	1	15		0,2 2,3	22	
5047 7525	y Aquilae	41 ,	5 +10 22	K2	6°,2 ΟΥ <sup>3</sup>	2 ,80		6 + 13	2	28	,-,	-1,5	16	8
5048 7528	d Cygni	41 ,	9 +44 53	A0	2°,4 Y1	2 ,97	(			37		0,8		+10
5052 7536	δ Sagitlao	42 ,	9 +-18 17	Ma A0	6°,7	3 ,78 3 ,83		9	6° Var	12	(5)		23	- 5
7539	11 Vulpecula	0 43 ,	5 +27 4			3,0-12		_					31	0
5058 7546	ζ Sagittao	44	5 -+ 18 53	A2	2°,3 YG¹		+		6° — 17	20		1,9		- 4
7540 5062 7557	α Aquilao	45	9 + 8 30	A.5	2º,4 Y1	0 ,89	6	55 5	40 -26,1		5 (4)	-	16	-10
155/	1 4230	. 1	1	1	1 4	1 * 1**	1 0	10 1	- 1	1	- 1	ب وي	1	,

Boss 5048 Visual binary ADS 12880 Has a period of some 500 years The dynamic parallax is 0",026-0",036.

19h to 20h.

					19	to zu".								
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
5067	χ Cygni	46 <sup>თ</sup> .7	+32°40′	Md	7°,5	Var.	91	233°	- 0,5				37°	+ 2°
7564	3593		ļ		ORB	13 <sup>m</sup> ,2	- 67	_				4,0		
5068 7565	12 Vulpeculae 3833	46 ,8	+22 21	В3	1°,5 W	4 ,91 5 ,12	- 29 - 8		-28:	7	(2)	-0,9 2,2	27	~ 4
5071 7570	η Aquilae 4337	47 .4	+ 0 45	Gop	5°,1 Y³	3,5-4,7 3,8-4,5	12		-14,8	5	(3)		9	-14
5078	: Sagittaril	48 ,4	-42 8	KO		4 ,21	53	10°	+36,2	20	(a)	0,7	325	-30
7581 5079	8 Draconls	48 ,5	+70 1	Ko	-5°,1	4 ,26	+ 30 87		+ 3.1	18	(F)	2,8		1.54
7582	1070				Y2	_3,99	<b>—</b> 47	+ 73		14	(5)	-0,3 3,7	70	+21
5084 7590	s Pavonis 2086	49 .0	<b>-73 10</b>	Ao		4 ,10	+ 10		0:			5,0	289	-32
5086 7592	13 Vulpeculae 3820	49 ,2	+23 50	A <sub>0</sub>	2º,6 Y¹	4 ,50 4 ,73	40 + 36	46° + 16	-33	15 15	(2)	0,4	29	- 3
5089 7595	\$ Aquilae 4261	49 .4	+ 8 12	ΙζΟ	5°,5	4 ,86 4 ,83	126	131	-41,9	20	(5)	0,9	15	-11
5091 7597	ω Sagittarii 14637	49 .7	-26 34	G 5	3° OY2	4 ,81 4 ,84	225	68°	-21,3	40	(1)	2,8	342	-26
5093	β Aquileo	50 ,4	+ 6 9	Κo	50,1	3 ,90	+ 225 484	176°	-40,0	40 81	(5)	6,6 3,4	14	-12
7602 5095	4357 b Sagittarii	50 ,8	-27 26	K2	OY <sup>2</sup>	3 ,86	<u> 305</u>		Var.	80	(2)	7,3	342	-27
7604	14 399 22 Cygni	52 2	+38 13	В3	OY2 10,8	4 ,61	- 4 12		-16.2 $-36.3$	12	(4)	$\frac{1,0}{-1,2}$	41	+ 4
7613	3817				w	5 ,11	- 9	- 8		6		0,3	41	
5103 7615	η Cygni 3798	52 ,6	+34 49	Ko	5°,1 Y³	4 ,03 4 ,03	- 38	→ 35	-26,3	33 30	(5)	1,4 2,6	39	+ 3
5104 7618	A Sagittarii 14682	52 ,8	<b>-2</b> 6 28	G 5	5° O'Y2	4 ,95 4 ,99	38 + 35		Var. -48,6	8	(1)	-0,5 2,8	343	-27
5105 7619	ψ Cygni 2572	53 ,0	+52 10	A 3	2°,5 W	4 ,80 5 ,06	- 51 - 3	_	-17:	13 12	(5)	0,2	53	+12
5108 7623	# Sagittarii 13831	53 ,2	-35 33	В3		4 .39 4 ,55	47 5	160°	+ 0,9	12	(1)	-0,2 2,7	332	<del>-3</del> 0
5118 7635	γ Sagittae 4229	54 ,3	+19 13	K5	6°,5 OY8	3 ,71	62	-	-34,1	20	(5)	0,1	25	- 6
1 - 2 - 2	Cygni	55 ,9	+53 21	Nova	Var.	1,5 to 16,5?	· · · ·		-17	.,		~1/	55	+12
5129	c Sagittarii	56 .5	-27 59	Mb	6°,7	4 ,60	37	74	+11.5	13	(2)	0,2	341	-28
7650 5131	16355 Sagittarii	56 .0	-38 13	K5	OA:	4 ,59	+ 36	+ 7	-38,3	13	(1)	2,4	330	-31
7652	13828					4 ,80	+ 29	+ 115		14		5,2		
5132 7653	15 Vulpeculae 3587	57 ,0		A 5	3°,2 Y¹	4 ,74 4 ,92	+ 19	+ 48		26 26	(3)	1,8 3,3	33	- 2
5138 7665	ð Pavonis 3474	58 ,9	-66 26	G 5	7°,0	3,64	1625 + 536	+1544		60 43	(3)		297	-33
5147 7673	& Telescopii 9794	59 .7	-53 10	Ma.		4 ,86 4 ,97	24 - 22	268	+36,9			1,8	313	-34
5153 7685	e Draconis	2 ,3	+67 35	Ko	6°,5	4 ,66 4 ,66	51		- 9,4	18	(2)	1,1		+18
5170 7708	b Cygni 3907	5 .7	+36 33	B2p	2°,4 Y1	4 ,82 5 ,13	+ 9	331		6	(2)	1,3 -0,2		+ 2
5171 7710	Ø Aquilao 3911	6,1	- 1 7	AO	2°,8 W	3 ,37	32	85		17	(3)	-0,5	370	-18
5182	Q Aquilae	9.7	+14 54	Ao	2°,8	3 ,59 4 ,96	73		Var.	19	(2)	1,3		-11
- 7724 5186	o <sup>1</sup> Cygni	10 .2	+46 31	A2	2°,5	5 ,15	+ 72	+ 15	-24.5	19	(4)	0,7	50	+ 6
7730	2881	,-			YG*	5 ,07		+ 10		14		1,1	55	, ,

Boss 5071. Cophold variable; period 7,2 days.

							20°•								
1	2	3	1		5	6	7	8	9	10	11	12	13	11	15
5187 7735	o² Cygnı 2882	10''',5			Ko B8	6°,5 O <sup>2</sup>	3 <sup>m</sup> ,95 3 ,93	2	63° + 2	Var - 3,0	8 5	(4)	2,6 4,6	50°	+ 6°
5188 7736	h <sup>a</sup> Cygni 3955	10 ,8	+-36	30	A0	2°,7	4 ,98 5 ,17	94 65	44° + 68	-22	16 15	(4)	0,9	43	0
5190 7739	Vulpeculae 4165	11,0	+25	17	_В3	1°,9	4 ,82 5 ,04	4 3	236°	Vai - 1	6	(2)	-1.3 $-2.2$	33	— б
5191 7740	33 Cygn1 2376	11,1	+56	16	А3	3°,3	4 ,32 4 ,52	102 + 34	- 37° -⊢ 97	28,6	32 32	(1)	1,9	58	- - 11
5195 7744	23 Vulpeculae 3666	11 ,7	<del>- </del> 27	30	K 5	6',5 Y8	4 ,73 4 ,69	43 - 34	278° - 27	+ 2,6	12	(1)	0,1	35	- 5
5197 7747	a <sup>1</sup> Capticorni 5683	12 ,1	-12	49	Gop	5º,6	4 ,55	15 + 15	67°	-25,9	~3 1	(3)		359	
7750	ж Cephei 764	12,3	-1-77	25	Во	2°,4 Y1	4 ,40 4 ,61		25° + 28	-22,6	14	(3)	0,1	77	+22
5200 7751	o <sup>2</sup> Cygn1 3059	12 ,3	-1-47	24	-Ко Аз	6°,9	4 ,16 4 ,15	5 0	68°	Vai	3	(2)	$-\frac{17}{1,3}$ -2,3	51	+ 6
5202 7754	δ <sup>2</sup> Capi icoini 5685	12 ,5	12	51	G 5	5°,5	3 ,77	58 50	+ 5 + 30	+ 0,1	25 17	¯ (6)	-0,1 2,6	359	-26
5208 7763	P Cygni 3871	14 ,1	+37	43	B1p Nova	4°,1 Y2	4 ,88	16 - 10	227° - 12	- 7.9	-9 1	(2)	-5,1 0,9	44	- <del> -</del> 1
5214 7773	y Capricorni 5642	15 .1	-13	4	Λο	2°,5 W	4 ,84 5 ,00	18	158° + 17	- 2,8	18 18	(1)		359	-27
5215 7775	β <sup>1</sup> Capi (coini) 5626	15 ,2	15	6	B9	-1 <sup>0</sup> B2	6,16	45 + 36	87° + 22	-	17	(a)		357	-28
5216 7776	β <sup>2</sup> Capι ι co ι n 1 5629	15,4	-15	б	G0 A0	5°,5 Y8	3 ,25 3 ,37	35 + 29	88° + 19	Vai 19,0	20	(3)	0,7	357	-28
5223 7790	a Pavonis	17 .7	-57	3	.B3	10,8	2,12	86 - 38	177°	1,8	13	(2)	-2,3 1,8	308	—3б
5229 7796	γ Cygni 4159	18 ,6	+39	56	F8p	4°,5 Y2	2 ,32	3 - 3	162°	- 5,4	6	(4)	-4,2 2,0	46	+ 1
5235 7806	39 Cygni 4062	19 ,9	+31	52	К2	6°, 1	4,60	41	93° + 41	- 13,9	15	(4)	0,5	40	- 4
5244 7822	ρ Capricorni 5689	23 ,2	-18	9	Fo	3° Y1	4,96	26 - 24	213° + 9	+ 19	20 18	(4)		355	31
5255 7834	41 Cygni 7	25 ,3	+30	2	1.5	4°,2 Y1	4,09	10	1140	- 18,6	2 5	(4)	-2,4 -0,9		- 6
5265 7844	ω <sup>2</sup> Cygn1 3142	27 ,0	-1-48	37	133	1º,8 W	4 ,89 5 ,10	10	66°	-14.	5 5	(2)	-1,6 -0,1	318	-38
5268 7848	q Pavonis	27 ,3	-60	55	Fo		4 ,84 4 ,95	176	163° +171	-19			6,1	303	-37
5270 7850	θ Cepher 1821	27 ,9	+62	39	A.5	3°,3 W	4 ,28 4 ,42	49 - 42	112°	Vai - 4,9	26 26	(2)	1,4	65	+14
5272 7852	8 Delphini 4321	28 ,/	- -10	58	135	2º,5 W	3 ,98 4 ,25	28 - 16	161° + 23	-18	7 5	(3)	-2,5 1,2	24	-18
5279 7866	47 Cygni 4079	30 ,0	+34	54	K5 A3	6°,8	4 ,85 4 ,81	14	188°	- 4,4	-	(2)		43	- 4
5281 7869	α Indi 13477	30 ,	-47	38	Ko	40,3	3 ,21	72 + 66	33°	- 1,8		(2)		319	-38
5282 7871	C Delphini 4353	30 ,	Š +-14	20	^A2	3°,0	4 ,69 4 ,83	38 + 24	84°	-24	21 20	(4)	1,2	27	-17
5291 7882	β Delphini 4369	32 ,	+14	15	F5	4°,0 Y2	3 ,72 3 ,93	113	109° +110	Var 22,9	41	(6)	1,7	27	-17
5294 7884	l Aquilae 4016	33 ,	2 - 1	27	~Ko	5°,1 Y2	4 ,51 4 ,50	28 - 10	154°	Var - 5,8	11	(3)		373	25
5301 7891	29 Vulpeculae 4658	34 ,	1 +20	51	Λo	2°,4 W	4 ,78	58 - - 24	91°	16	12			32	-13

Boss 5215, 5216 A wide pair. The bright star is a spectroscopic binary

20h to 21h.

					20 <sup>b</sup>	to 21 <sup>h</sup> .								
1	2	3	4	3	6	7	8	9	10	11	12	13	14	15
5310 7906	a Delphini 4222	35 <sup>m</sup> ,0	+15°34′	138	3°.3	3**,86 4 ,10	65	97°	- 9	17	(3)	0,0	29°	16°
5315 7913	/ Pavonia 3501	36 ,0	-66 34	A 5	4",9	3 ,60 3 ,75	49 - 31		+ 9,8	29	(a)	0,9	295	-37
5318 7920	η Indi 11752	36 ,7	-52 17	Fo		4 ,70	148 + 92		- 2	34	(B)	_	314	-40
5320 7924	a Cygni 3541	38 ,0	+44 55	A2p	2',1 Y1	1 ,33 1 ,55	1 1	180°	Ver - 4	8	(2)	-4.1 -8.7	52	+ 2
5323 7928	d Delphini 4403	38 ,8	+14 43	Δ5	4',0 Y1	4 ,53 4 ,63	56 - 55	204	+ 8,3	20	(2)	0,8	28	-18
5328 7936	ψ Capricorni 15018	40 ,2	-25 38	F8	4° Y1	4 ,26 4 ,35	169 142	200° + 91	+26,0	50 50	(1)		347	-37
5331 7942	52 Cygni 4167	41 ,6	+30 21	Ko	5',6 Y	4 ,34 4 ,40	27 + 20	329° - 18	- 1,0	24	(6)	1,1	41	- 8
5334 7947	7 Delphini   4255	42 ,0	+15 46	G5	3°,5 BG	5 ,47 5 ,84			- 7,4				30	-18
5335 7948	7 Delphini 4255		+15 46	G 5	5*,4 OY*	4 ,49 4 ,86	207 -193	189° + 75		36 36	(5)	2,3 6,1	30	-18
5336 79 <del>19</del>	# Cygnl 4018		+33 36	Ko	5°.5	2,69	483 +362	+319	-10	47 46	(6)	0,9	44	7
5337 7950	Aquarii ABOO		- 9 52	Ao	3°,0	3 ,83 4 ,01	- 44 - 3	141	-15	28 28	(4)	1,1 3,0	6	- 32
5338 7951	k Aquaril 5378		- 5 24	Ma	7.1	4 ,60 4 ,60	39 — 32	189°		15	(2)	0,5 2,6		-29
5340 7952	( Indi 13718		-46 36	K5		4 ,90	+ 39	73° + 13	- 5,2			3,0	321	-41
5344 7955	Cephel 2240		+57 13	Go	5',0 Y	4 ,63 4 ,71	241 -178	196° 161		57 56	(4)	3,4 6,5		+ 8
5346 7957	# Cephel 2050		+61 27	Кo	5',3 Y	3 ,59 3 ,58	826 +653	7° +512	-87,0	87 85	(4)	3,2 8,2		711
5350 7963	1 Cygnl 4967		+36 7	B5	2*,4 W	4 ,47	- 11	160° + 5	-25	19 18	(4)	0,8 -0,1		- 5
5352 7965	a Microscopii 14660		<b>−34</b> 9	Ko		5 ,00 5 ,01	- 39 - 21	177' + 33	-14.5	11	(1)	0,2 3,0		-40
5361 7977	55 Cygnl 3291		+45 45	B2	3°,0 Y1	4 ,89 5 ,03	- 5 - 4	143	- 3.9	3	(2)	-2,7 -1,6		+ 1
5363 7980	ω Capricorni 15082		-27 18	Ma	7° OY³	4 ,24	- 16	213° + 6		13	(1)	0,4		-38
5367 7986	β Indi 7788		-58 50	Ko		3 ,72 3 ,88	_ 29 _ 5	155 + 28		18 18	(1)	1,0		-40
5371 7990	μ Aquarli 5598	47 ,3		A3	4°,2	4 ,80 4 ,97	+ 4	133 + 51		28 27	(2)	2,0 3,4	L	-32
5373 7995	31 Vulpeculas 4017		+26 43	G5	5°,4 Y	4 .76 4 .79		227 - 52		11	(4)	0,0	L	-12
5375 8001	57 Cygni 8768	49 .7	+44 0		1°,9 W	4 ,68 4 ,91	+ 3	+ 18	-16,2	8	(2)	-0,8		0
5393 8028	v Cygni 4364		+40 47		21,8 YG1	4,04	- 25 - 24	+ 4		12	(2)	-1,4 1,0	L.	- 3
5402 B039	7 Microscopii 16353		-32 39			4 ,71	+ 9	+ 63		10	(1)	-0,5		
5410 8047	S188		+47 8		1.7 W	4 ,86 5 ,01	+ 2	+ 8	Yer + 1	4	(2)	-2,1 -0,6		
5417 8060	7 Capricorni 6115		-20 15		3°,1 W	4 ,93 5 ,10	- 60 - 60	+ 5	+24	21	(2)	3,8		
5427 8075	6174 6174 5170. Domb As		3 - 17 38		2',0 W	4 ,19		+104		21	(1)	4,3	•	

Box 5320. Doneb As the radial velocity is variable in a very segmenting polantions this star should be tested for an eventual variability in its light. — Box 5334, 5335. ADS 14 279. Doubtless a physical pair. The dynamic paralles is 0",042.

 $21^{\rm h}$ 

1	2	3 4	5	6	7	8	9	10	11	12	13	11	15
5431	ξ ( ygnı	1 <sup>th</sup> ,3 +43°		6,6	311,92	7	117°	Var	6	(3)	-2,2		
8079	3800	1		O <sub>3</sub>	3 ,88	- 4	6	- 19,9	6		- 1,9		
5130 8080	A C upricorni 15235	1 ,3 -25	24 Ma	6"-7'	4 ,60 4 ,56	- 56	, 210° -  19	+32,4	14	(2)	3,5	ა50	41
5436	f2 Cygni	3 ,2 +47	15 K5	6',3	4 ,88	14	126°	-26,5	9	(3)	-0,4	57	1
_8089   5441	3292 r Aquam	4 ,1 11	47 Ko	Y <sup>3</sup>     5',8	4 .75 4 .52	- 10 94	+ 10   98°	11,8	29	(2)	0,6	6	37
8093	5538			Y	4 .50		162°	47.4	30		4,4	28	-2 <del>5</del>
5443 8097	γ Isquulci 4732	5,5+9	44 1 top	3',4 Y1	4 ,76 4 .77	169 106	132	-17.1	21 18	(6)	1,0 5,9		
5452 8115	Հ Cygm 4348	8 ,7 -1-29	49 Ix0	5',1 Ya	3,40	59 - 58	183°	+17,0	17	(4)	0,6	45	13
5455 8123	δ Equulei 4746	9 .6 -1- 9	36 1 5	4",5 Y <sup>2</sup>	4 ,61 4 ,69	306 230	172° +202	-15.4	62 62	(7)	3,6 7,0	29	-26
5460	τ Cygnι	10 ,8 -1-37	37 Fo	4',0 Y2	3 ,82	455 441	20°	Var -22,0	48 48	(6)	2,2 7,1	51	<b>—</b> 8
8130 5461	4240 n Equulei	10 ,8 + 4	50 F8	4",6	3,93	101	117°	Vai	31	(5)	1,6	25	30
8131	4635 F Microscopii		Λ3	Y1	4 ,18 4 ,79	- 37 66	+ 97   121°	15,9   1	31		4,2	340	45
5464 8135	16498	11 ,9 -32	35 AO		4 ,92	- 20	-1 63	1			3,9	340	
5467 8140	<b>∌</b> Indi 10037	12 ,7 53	52 A 5		4 ,60 4 ,69	136 + 39	123°	-14			5,3	310	44
5469 8143	o Cygni 4431	13 ,5 +38	59 Aop	3',1 Y1	4,28	- 8 - 6	220°	Var 3,8	-1 0	(1)	4,3 -1,2	52	- 7
5471	v Cygni 4371	13 ,8 +34	29   133p	2',5 W	4 ,42 4 ,61	29 17	136° + 23	+ 6	12 12	(2)	-0,2 1,7	48	-11
$-\frac{8146}{5473}$	v Microscopu	14 ,4 -41	14 A2p	,,,	4 ,92	85	90 0	- 2	1.2	-	i	329	-46
8151 5480	44475 & Cupher	16 ,2 +62	10 A 5	20,8	2,60	+ 64 160	-  56   72°	- 8	73	(5)	4,0 1,9	68	+ 9
8162	2111			YG1	2 81	11	1-160		73		3,6	_ <u>_</u>	42
5484 8167	Capilcoini	16 ,7 -17	16 Ko	5°,4 Y8	4 ,30	32  - 27	79° 18	+11,2	16 16	(1)	0,3 6,3	2	42
5489 8173	1 Pegasi 4691	17 ,5 +19	23 Ko	5°,9 Y8	4 ,24 4 ,23	118	60° + 70	-76,3	28 28	(5)	1,5 4,6	38	22
5493	γ Pavonis	18 ,2 -65	49 F8		4,30	815 -1-603	60	30 1	129 129	(1)	8,9	295	-41
8181 5507	3918 Capilcoini	21 ,0 -22	51 G5p	50	3 ,86	23	00	+ 2	4	(2)	-3,1	354	45
8204 5513	b Capricoini	23 ,0 -22	15 G5	Y25	3 .92	+ 16		-22,0	18	(2)	0,7	356	45
8213	5692			Y 2,5	4 ,61	+ 88	+ 98 103°	18,9	18	(5)	5,2		-20
5522 8225	2 Pegasi 4325	25 ,5 +23		7°,1	4 ,68	F 2	1-1- 17		12		0,9		-
5527 8232	β Aquarn 5770	26 .3 - 6	1 G0	4°,6 Y2	3 ,07	+ 4	+ 16	6,8	5 5	(4)	-3,4 -0,7		-39
5532 8238	β Cepher 1173	27 ,4 70	7 B1	2°,4	3 ,32	12	+ 12	- 7,2	6	(5)	-2,8 -1,3		- -14
5543 8252	υ Cygnı 3866	30 ,2 +45	9 K0	5°,1	4 ,22	99 + 95		+ 6,9	23	(4)	0,7		- 5
5544 8254	r Octantis 1510	30 ,4 -77	50 K0		3 ,74 3 ,91	234 140	169°	Var - -32,1	31 31	(1)	1,2 5,0	281	-36
5546	72 Cygni 4359	30 ,7 +38	5 K0	6°,0	4 ,98 4 ,97	148 + 105	52°			(5)	0,7	54	-11
8255 5549	P Capucorni	31 .5 -19	54 B5p			8 + 4	104°	-25	7	(2)	-1,C	0	-47
8260 5551	6251 § Aquarii	32 ,4 8	18 A5	30,2	4 ,78	114	102	-20	24	(1)	1,7	15	-41
8264	5701			W	4 .93	+ 54	- <b> - -1</b> 00	1	24		5,1	1	

Boss 5460 Wellknown binary = ADS 11787 The period is 49,2 years The bright star is a very short-period spectroscopic binary

215 to 225.

						to 222"		,						
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
5562 8278	7 Capricorni 6340	34=,6		Fop	3',9	3 <sup>m</sup> ,80 3 ,93	188 + 111	+ 152	Var -31,2	15 15	(2)	-0,9 5,2		-46
5563 8279	9 Cephol 2169		+61 38	B2p	Αı	4 ,87 5 ,07	5		-14,7	3	(3)	-4,7 -1,6		+ 7
5570 8288	и Capricorni 61 52	37 .1		G 5	5,6 O <b>Y</b>	4 ,82 4 ,86	+ 91	+ 109	- 3,1	6	(2)	-1,3 5,6		-47
8296	Q Cygni		+42 23	Pec. Nove		3,0-15,4	+ 3	+ 2	_		L	4,0	57	- 8
5580 8301	≠¹ Cygnl 3410		+50 44	В3	2',2 W	4 ,78	_ 6 _ 2	+ 6	Var.	5	(3)	-1.7	64	- 2
5582 8305	Fiecis Aust. 15734		-33 29	A0		4 ,35 4 ,50	93 - 34		+ 2			4,2	341	51
5584 8308	s Pognal 4891	-,	+ 9 25	Ko	6°,1 Y•	2 ,54 2 ,68	+ 12		+ 4.7	21 15	(5)	-1,6 -0,5		- 33
5587 8309	μ¹ Cygnl 4169	39 ,6		F5	4",1 Y1	4 ,73 4 ,91	350 - 12		+18,5	58 59	(5)	3,6 7,4		19
5588 8310	μ Cygnl 4169	39 ,6			Åι	6 ,08 6 ,26	325 ~ 10	130° + 309	+16,3			4,9 8,6		- 19
5590 8313	9 Poguai 4582		+16 54	G 5	5*,8 Y*	4 ,52 4 ,49	— 13		_ <b>22,</b> 3	11	(3)	-0,3 1,8	40	-27
5592 8315	n Pogani 4463	40 ,1		F5	4°,0 Y■	4 ,27 4 ,32	33 + 14		-10,3	42 38	(8)	1,9		-22
5593 8316	μ Cephei 2316	40 ,4		Ma	7'.9 OR	3.92-4.53 3.7-4.7	_ 2 _ 2	207° - 1	Var +20,5	2 2	(1)		68	+ 4
5594 8317	11 Cephol 1193	40 ,5		Ko	7°,8	4 ,85 4 ,76	159 + 43	51 + 147	-37.3	13 13	(5)	0,4 5,8		+14
5600 8322	6 Capricorni 5943	41 .5		A 5	3°.7 Y1	2 ,98 3 ,18	392 - 55	+ 388	Var. - 6,4	78 76	(4)	2,4 6,0		-47
5608 8334	r Cephri 2288		+60 40	A2p	4°,1 Y1	4 ,46 4 ,58	+ 0	- 2	-23,7	12 11	(2)	-0,3 4,0	70	+ 6
5609 8335	# Cygn! 3504	43 ,1	+48 51	В3	2',3 W	4 ,26 4 ,44	- 5 - 3	127° + 4	<b>−19.</b>	5	(3)	-2,2 2,2	63	4
5617 8343	14 Pognal 4525			Δo	2°,6	5 ,00 5 ,30	- 18		-22	10 9	(3)	-0,2 3,0	51	<b>— 18</b>
5624 8353	y Gruta 14536	47 ,9		B8	34,7	3 ,16 3 ,37	+ 65	98 + 90	- 2	18	(a)	-0,5 3,4	333	53
5635 8368	9733	51 ,1	-55 28	Po		4 ,56 4 ,63	59 + 19		+15			3,4	306	-49
5650 8383	VV Coplied 8007	53 ,8		Мар		4,9 to 5,6	9 + 7	- 311°	Ver,	5	(a)		73	+- 7
5654 8387 5663	# Indi 10015	55 .7		K5		4 .74 4 .85	4696 + 657		-40,4	267 265	(2)	6,8 13,0	303	- 49
8402	o Aquarii 5681	58 ,1	- 2 38	Bsp	2°,5 W	4 ,66 4 ,86	_ 18	+ 18	+16.	13 13	(1)	0,2	25	<b>—4</b> 3
5672 8411	1 Grule 14639	0 ,1	-40 2	K2		4 ,60 4 ,62	124 - 110	195° + 56	+40,0	17	(1)	0,7 5,1	329	<u> </u>
5674 8413	* Pegasi 4800			K5	7.0 OY	4 ,90 4 ,97	144 + 138	50° + 42		13		0,5 5,7	34	- 39
5676 8414	a Aquarii		- 0 48	Go	4*,8 Y*	3 ,19 3 ,32	+ 15	113° + 15	+ 7,6	8	(3)	-2,3 -0,9		-43
5677 8417	1809		+64 8	G	5°,0 Y1	6 ,47	225	66*				4,8 8,2		+ 7
5679 8417	E Cophel 1802		+64 8	¥3	31,9 V1	4 ,57	226 + 43	68° + 221	- 6,0	53 47	(5)	2,9 6,3	73	+ 7
5680 8418	6209		-14 21	B8	3°,0	4 ,35 4 ,54	70 24		Var.	15 15	(1)	0,2 3,6		— <b>5</b> 0
5684 8425	a Gruls 14063		-47 27	B5	20,4	2 ,16 2 ,23		145° + 194		31 30	(2)	-0,5 3,7	318	
Boss (Zuman)	5677, 5679. Doubl	Som A	physical pair	The	dynamic	al parallex			n benide	e de la constant	ude le	48.40	(BEP)	. 410.6

						44			-					
1	2	3	1 1	5	0	7	8	9	10	11	12	13	11	15
5688 8430	ι Pegası 4533	2 <sup>10</sup> ,4	+21°51'	F5	3°,9 Y2	3 <sup>111</sup> ,96 4,03	299 -126	86° - -272_	- 4,3	78 78	(5)	3, 1 6,3	51°	_
5689	μ Piscis Aust	2,5	-33 29	A2		4 ,62	82	1190	- <del> </del> -12			4.0	342	- 56
8431	_15922 ∂ l'ogasi	5 2	-1- 5 42	Λ2	20,7	$-\frac{4}{3}, \frac{78}{70}$	+ 17 276	+ 80 83°	Var	26	(3)	4,2 0,7	36	- 39
5703 8450	4961	یشر د	-1- 5 -12	112	W	3 ,96	1-174	1-215	- 7	25	(3/	5,9		
5709	π Pegasi	5 ,5	+-32 41	IF 5	40,1	4 ,38	26	209°	+ 2	22	(5)	0,5	56	-19
8454	4352	١.,,		Ko	Q <sub>0</sub> 'O Ā3	4 ,48	25	- 6 55°	-18,2	21	(1)	$\frac{1.5}{0.2}$	71	+ 2
5714 8465	ζ Cephei 2475	7 ,4	+57 42	IZO	O <sup>2</sup>	3 ,62 3 ,61	+ 6	10	-10,2	21	(1)	-1,0		7 2
5716 8468	24 Cepher 1111	7 ,9	+-71 51	G5	5°,5	4 ,99 4 ,99	28 - 4	82°	- 15,0	9	(3)	-1,5 2,2	79	干13
5732	I accitac	9,6	+39 13	K2	60,2	4 ,64	49	84 6	-10,8	11	(2)	-0.1	60	-14
8485	1711				$\mathbf{Y}^{\mathbf{a}}$	4 ,58	+ 14	47		11	-/-/-	3,1	1705	
5733	μ¹ G1 u15 14810	9,6	-41 51	Go		4 ,86 4 ,97	57  - 55	57°	- 7,2	6	(a)	- 1,2 3,7	325	-56
8486 5742	6 Cephei	11 .3	+56-33	Fo	30,6	4 ,23	452	840	<b>— 1</b>	56	(5)	2,7	71	1
8494	2711			_	Y1 5	1,37	+ 23	+452		50		7,5		
5746 8498	1 I acci tae 4526	11 ,6	+37 15	K.o	X3	4 ,22	+ 1	101°	- 8,5	12	(5)	0,8 0,7		-16
5744 8499	# Aquaru 5845	11 ,6	- 8 17	Ko	Y2	4 ,32	112 + 49	100° + 101	14,7	14	(3)	-0,1 4,6	23	- 50
5747 8502	α Lucanae 7561	11 .7	-60 45	K2	5",4	2 ,91 3 ,12	87 75	249° 45	+45	36 36	(1)	0,7 2,6	297	-49
5761 8518	γ Αquain 5741	16 ,	- 1 53	Λo	2°,6 W	3 ,97	123 + 76	86°	Vai 21	43	(2)	1,9 4,4		-47
5762	31 Pegasi 4784	16 ,6	+11 42	Взр	2°,2 W	4 ,93	6	67°	8	7	(a)	-0.9 -1.2		-37
_8520 5763	32 Pegası	16 ,;	7 -1-27 50	В8	2°,8 W	4 ,88	5 0	112°	+ 7	8 8	(1)	-0.6	55	24
8522 5764	4299 2 Laccitae 3894	16 ,9	-1-46 2	_B 5	26,1 W	4 ,66	20	90°	Vai → 9.0	18	(3)	0,4	66	- 9
8523 5776	B Lacertae	19 ,	5 -+ 51 44	ко	5°,6	4,58	190	184°	-10,6	1	(5)	1,5 6,0	69	4
8538 5777	3358 # Aquand	20 ,	2 + 0 52	вір	2°,9	4 ,64	13	85°	+ 4,4		(1)	- 1,5 - 0,4	35	-46
8539 5778	δ Tucanne	20 ,	2 65 28	В9-	. **	4 ,80	67	810	1-12	١		3,9	291	-47
8540 5779	4044 4 Lacertae	20 ,	4 -1-48 58	-B8p	30,1	4 ,89	+ 46		-26,7				68	- 7
8541 5790	3715 35 Pegasi	22 ,	8 + 4 12	ко	5°,0	4 ,80	325	167°	+54,0		(4)	1,9	39	-44
8551 5791	- 81 Grus	23 ,	3 -44 0	-G5	Ya.	4,90	<del>- 23</del>	88 °	+ 5,0		1 ' '		320	- 58
8556 5793	14931 \$^4 Aquaili	1 23 ,				4 ,19	十 17 173		+28,9	35	(6)	2,0	34	48
8558	4365	II	1	F2	40,5 Y2	4 ,70	+107	-l- 137	1	31		_ 5,8		
5794 8559	ζ <sup>4</sup> Aquarii 4365	]] 23 ,			Ya	4 ,42 4 ,53	212 +151	+151		_		1,9 6,0		
5795 8560		23 ,	8 -44 15	Mb		4 ,31 4 ,42	18	- 16		}		-0,0		
5807 8571	** **	25 ,	4 1-57 54	Go	4°,7 Y20	Var 3,6-4,	14 3 1	+ 14		5		2,	7	+- 1
5804 8572		25 .	4 +47 11	Ko Ao	7°,2	4 ,61	21	239°	1	4	100	-2,	2	
5803 8573	o Aquarii	25	4 11 11	ΛO	2°,7 W	4 ,89 5 ,06	30	180	- - 14	15		0,	6 21	- 54
33/3		l	the Conholds	Police	A dose		1		11", 1029	which	di shor	es its r	m	

Boss 5807 The prototype of the Copheids, period 5,4 days. Has also a companion 7m,5, 11", 192°, which shares its p m

88p

					- 4	<b>2</b> 4								
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
5808 8576	β Pisois Anst 17126	25™,9	-32°52′	A0		4=,36 4 ,51	61	109° + 57	+ 6.3			3,3	342°	-60°
5810 8579	6 Lacertae 4420	26 ,1	+42 36	В3	2°,5	4 .54	13	261 °	Var 10,5	6	(3)	-1,6 0,1	65	-12
5811 8582	7 Tucanac 6348	26 ,2	-62 29	МЬ		4 ,92	39 - 18	151°	- 3,4				294	-49
5813	o Lacortao	27 ,2	+49 46	Λo	2.9	5 ,03	142	+ 35 85	-14	36	(3)	1,6	69	- 7
8585 5824	3875 7 Aquarli	30 ,2	— o 38	B8	Y1 2.6	3 ,99 4 ,13	105	+139 121	- 8	35 17	(1)	4,6 0,3	35	-48
8597	4384 Lacortao	31 7	+52 12	Pec	W	4 ,33 4,5 to	+ 3	+105 0°	ļ	17		4,2	71	- 5
5837	9 Lacertae			Nove		14,5	+ 1	0 210°	7.75-	2.	(4)	-5,5	70	- 6
8613	3770	33 ,2		A 5	3°,4 Y1	4 ,83 4 ,97	116 106	- 49	+19	25 25	(1)	1,8 _5,2		
5844 8622	10 Locortes 4826	34 ,8	+38 32	Oas	2',0 W	4 ,91 5 ,10	- 7	165° + 8	Var			0,3	65	-17
5849 8628	Pisots Aust.	35 .1	-27 34	B8	1 - 2 Y	4 ,22 4 ,41	+ 13	94° + 20	+ 3			1,1	352	-62
5850 8630	# Octantia	35 ,8	-81 54	Fo		4 ,34 4 ,47	63	275° - 59	+25			3,3	275	-35
5852	11 Lacartae	36 ,1	+43 46	Ko	6°,4	4 ,64	97	850	-10,7	17	(4)	0,8	68	-13
8632 5853	4266 Pegasi	36 ,5	+10 19	В8	2.7	4 ,59 3 ,61	+ 27 78	+ 93 99°	+ 4	17	(3)	4,6	47	-42
8634 5854	4797 # Gruis	36 ,7	-47 24	Мъ	6',8	3 .79	+ 27 130	+ 73 99°	+ 1,0	15	(1)	3,1	314	59
8636 5858	o Pogasi	37 ,1		AO	20,4	4 ,85	+ 57	+117 191 °	+ 7,9	15	(3)	1,0	L_	-26
8641 5860	4436 g Gruis			Ko	AC.	5 ,04	- 35	+ 6		17		2,6		-61
8644	18049	37 ,7				4 ,89 4 ,92	- 71	183° + 45	+30,4	14	(1)	4,5		
5864 8649	g Aquarti 6324	38 ,2	-19 21	TC 5	5°,3	4 ,88 4 ,84	- 35 - 35	215°	+21,6	11	(1)	2,6		60
5865 8650	n Pegnal 4741	38 ,3	+29 42	Ģō	₹0 Y	3,10	36 - 29	164°	+ 4,4	24	(3)	-0,2 0,9		-2
5867 8655	η Gross 10123	39 ,5	-54 1	Ko		4 ,86	25 + 24	48°	+27	24	(1)	1,8	302	50
5874	¿ Pegasi	41 ,6	+11 40	F5	4 .8 Y	4 ,31	545	1550	- 4,5	59	(5)	3,1	50	-4
8665 5875	A875	41 ,7	+23 2	Ko	50,1	4 ,32	-322 60	104	- 3,8		(4)		57	-3
8667 5880	# Gruin	42 ,	-51 51	A2	Ă,	3 .69	+ 10 120		0	18	-	3,0	304	-5
8675 5884	13389 r Aquarii	44 .3	-14 7	K5	70,0	3 ,83	+ 2	-	+ 1,2	20	(4)	0,6		-5
8679 5885	6354 # Pegnal		2 +24 4	-	0°	4 ,13	- 38 154	+ 7		19		2,2		
8684	4616				A.	3 .75	+ 18	+152		31		4,6	5	
5891 8694	1814		+65 40		5°,4	3 ,68 3 ,66	-118	<b>— 74</b>	-12,	34		4,4	-	1
5893 8695	7 Plecie Aust 16270		-33 24			4 ,52 4 ,68		- 6	+16	7	(a)	2,7	341	-6
5895 8698	A Aquarii 5968	47 .	4 - 8 7	Ma	OY.	3 ,84	36	6	- 9,	18			32	-5
5899 8702	Cophel 703	47 .	9 +82 37	Ko	6',4 OY'	4 ,97	64	32	-31,	1 19	(3)	1,4	86	+2
5904	J Aquarii	49 ,	3 -16 21	A2	2,8	3 ,51	52	246	+20	39	(2)		19	-6
8709 5910	6173 @ Pagasi	50 ,	2 + 8 17	Ao	2°,8		72	79	-12	12	(4)	-0,	3 49	-5
8717	4961				l W	5 ,12	I+ 48	+ 54		9	1	4,5	2	

22h to 23h.

1	2	3	1	5	6	7	8	9	10	11	12	13	11	15
5911 8720	δ Piscis Aust 16303	50 <sup>m</sup> ,4	-33°	<b>к</b> о		4 <sup>3</sup> 11, 33	36	39°	-11,9		(1)	1,1	311°	-65°
5916 8728	a Piscis Aust 19370	52 ,1	-30	A3	2',6	4 ,35	+ 36	117°	-1 6,5		(2)		348	-66
5926 8747	4 Gaus 10382	55 ,0	-53 1	7 65		1 ,57 4 ,18	-1 51 66	'+361   266°	Vai	111	~ (1)		300	-58
5927 8718	36 Cephei 610	55 ,2	-1-83 4	K 5		4 ,30	- 38 106	- 51   73°	- 3 + 2,9	17	(2)	3,3		-1-23
5933	o Andromedac 4664	57 ,3	+11 4		2,3	4 ,86 3 ,63	+ 7	+106	-15	13	(4)	5.1 -1.6	70	-16
8762 5939 8773	β Piscinm 4818	58 ,8	+ 3 1	A2p B5p	2",4 W	3 ,91 4 ,58	13	- 29   129°	+ 2	10	(1)	1,2 -0,4	48	-51
59 10 8775	β Pegasi 4480	58 ,9	+27 3	2 Ma	6",8 OY4	4 ,75 2 ,61 2 ,66	234	- - 13   55°	+ 8,7	10 23	(5)	0,2	65	29
5942 8780	3 Andromedae 4028	59 ,7	+19 30	Ко	2,'8	1,91 1,81	-199   230  -189	-124   46°	-31,8	14	(5)	4.6 0.1	i	- 9
5911 8781	o Pegasi 4926	59 ,8	1 14 40	0 40	1',8 Y('1	2 .57	71	128° 128° + 73	Vai - 4	32 32	_ (4)	0,1		-41
5919 8787	θ (sturs 15 149	1 ,2	-11	1.5		1,35	57	233°	+ 9,6	10	(a)	1,9 -0,6 3 2		64
5950 8789	61 Aquuu 17 197	1,3	- 21 1	7 (+5	5' 6' OY4	1 .77 4 .81	1 38	90° + 56	+15,2	13	(Ī)	-0,7 3,9	4	67
5952 8795	55 Pegasi 4997	2,0	+ 8 5	Ma	6',8 O <sup>4</sup>	+ ,69 + ,6+	16	153°	- 5.7	9	(5)	-1,1 0,7	53	-46
5954 8796	56 Pegasi 4716	2 ,2	-  24 50	5   Ko	6',4	4 ,98	38	180°	-26,9	16	(4)		63	-32
5955 8797	1 Cassiopeiae 2515	2,4	+58 5.	3 B1	2',6 Y1	\$ .93 5 .07	12	59°	Vai + 8,5	3	(3)	-2.7 0.3	77	- 1 <sup>-</sup>
5960 8812	c <sup>2</sup> Aquarn 6368	4,1	-21 4	3 Ko	5°-6°	3 ,80	59 1 56	51°	+21,1	23 23	(3)	0,6		67 <sup>-</sup>
5963 8817	c <sup>3</sup> Aquain 17771	4 ,5	-23	) (10 A2	2' Y1	4 ,94 5 ,02	+ 3	108°	4,8	9	(2)	-0.3 0.5	7	-67
5966 8819	π Cephei 1006	4 ,7	+71 5	1 65	5',2 Y1	4 ,56 4 ,57	28 26	154°	Vai 19,3	17 12	(7)	0,0		
5965 8820	t Gruis 11947	4 ,7	- 15 4	7 KO		4,10	145 + 38	106° 141	Var - 4,4	17 17	(1)	0.3	310	63
5975 8830	7 Andromedae 3964	8,0	1-48 5	i I o	3,'8	4,62	134	44° + 70	+13	42 41	(4)	2.7 5.3	75	-10
5978 8834	φ Aquani 6170	9,1	- 6 3	5 Ma	7°,0 OY3	4 ,40	193 149	172° +124	- 0,4	14	(4)	0,0 5,8		-59
5981 8841	ψ <sup>1</sup> Aquam 6156	10 ,7	- 9 3	8 Ko	2°,9	4 ,46	367 -1-191	92°	-27,0	21 21	(3)	7.3	37	-62
5985 8848	y Lucanae 8062	11,6	-58 4	7 1.2		4,10	89  - - 57	- 336°	+18			3,8	290	-55
5988 8852	y Piscium 4648	12 ,0			5°,6	3 ,85 3 ,97	753 - -407	88° 633	-14,0	25 25	(4)	0,8 8,2		- 52
5992 8858	ψ <sup>4</sup> Aquarit 6160	12 ,7			2°,6 YG1	4 ,56 4 ,73	13	103° 12	- 3.	10 10	(1)	-0,4 0,2		-62
5993 8860	8 Andromedae 3991	l			7°,1	4 ,99 4 ,95	38 - - 15	+ 35	- 8,3	10 10	(4)	2,9		11
5995 8863	y Sculptoris 16476	1		5 Ko		4 ,51 4 ,53	- 71 - 43	159° + 57	+16,7	15 15	(1)	7,0		- 70
6000 8872	o Cophei 1514		+67 3			4 ,90 4 ,92	66 + 20	75° + 63	- 17,8	22	(7)	1,5 4,0		+ 7
6005 8880	τ Pegası 4810		+23 1		2°,8 Y1	4 ,65 4 ,75	35 - 7	127°	+17	28 27	(2)	1,8 2,4		-35
6012 8892	b1 Aquatii 6587		-20 3		5°-6° Y2	4 .27	153 142	233° - 55	- 5,G	27	(3)	1,4 5,1		69
6024 8905	v Pegasi 4833	20 ,4	+22 5	I Go	4°,7 Y2	4 ,57 4 ,69	191 +107	82° +159	-13	21 21	(4)	1,2 6,0	67	-35

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						23ª.						<u>a</u>		
1	2	3	4	5	6	7	8	9	10	11	12	13	14	13
6026 8906	b <sup>a</sup> Aquarii 6420	20°,8	-21°12	K5	6°,3 Y°	4",52 4 ,53	83 - 81	226° 20	+15,4	24 24	(1)	1,4	16°	-70°
6031 8911	N Piscinm 4998	21 ,8	+ 0 42	A2p	2°,6 W	4 ,94 5 ,17	24 - 32	136° +120	- 4.9	22	(5)	1,6		-56
6037 8916	o Placium 5173	22 ,9	+ 5 50	G5	5 .3 Y	4 ,45	138	252° - 92	+ 6,1	9	(3)	-1,3 5,2	59	-51
6040 8923	q Pegasi 5009	24 ,1	+12 13	K0	5 ,4 Y	4 ,67	62 + 51	64° + 35	-15,0	10	(4)	-0,8 3,0	63	-46
6046 8926	Camiopeina 9748	25 ,4	+58 0	B3	2',5,2' W, V <sup>1</sup>	4 ,89	28	620	Ver	6	(3)	-1,2 2,1	80	- 3
6054 8937	β Sculptoria 15527	27 ,6	-38 22	В9	W, V-	4 ,46	+ 18	+ 22 83	-14,8 + 2				322	-71
6057	ba Aquarli	28 ,0	-21 28	Ao	i° W	4 ,60	+ 54	+ 75	+15	-		4,3	20	-72
8939 6062	6437	29 .7	-43 10	A2p	- W	4 ,92	+ 11	110	+19	-		1,1	309	-69
8949 6068	Phoenicis	32 ,5	<b>-46</b> 3	A2		4 ,94	68	+ 27	+10				303	-67
6071	14720 1 Andromedae	32 ,7	+45 55	Ko	5*,5	4,00	+ 7 449	+ 67 159°	+ 6.7	45	(4)	- 4,0 2,3	78	-14
8961 6073	4283	33 ,2	+42 43	В8	2°,9	3 ,98	-350 26	-283 97*	0,0	45 13	(1)	7,3 -0,2	77	-17
8965	4720	34 ,8	+ 5 5	F8	W 31,9	4 .47	+ 6	+ 25	+ 5.6	13 70	(4)	1,4 3,5	62	-54
8969 6078	5085 7 Cephei	35 ,2		Ko	Y* 5',4	4 ,34	-195 169	+ 540 340	-43,2	69	(4)	8,1	86	+15
8974 6080	928 MAndromedae	35 ,5		Ao	Y 2 .6	3 .45	+157	- 63	- 9,	68	(2)	4,6	78	-17
8976 6083	4522 A Aquerii	36 ,6		Go	W 4*,9	4 ,49	+ 4	+ 83 68°		13		3.9		
8982 6084	6358 2 Piscium	36 ,9		A5	Y.	4 ,95 5 ,05	+ 14	+ 11	+ 4.8	2	(1)	-3,6 1,3	31	-72
8964 6087	6087 ∞ Aquarii				3°.3 Y¹	4 ,61	199 195	223° - 42	+ 8	36 33	(6)	2,2 6,1	59	-57
8988 6094	6476 78 Pegasi		-15 6	<b>A</b> 0	2*,8 W	4 ,62	106 - 7	125° +106	- 3	16 16	(1)	0,6 4.7	39	<b>-70</b>
8997	4627	39 ,0		K0	X.9	4,98	80 - 2	117° + 80	- 6,8	16 16	(5)	1,0	75	-31
6110 9016	d Sculptoria 18353		28 41	A <sub>0</sub>	3°	4 ,64 4 ,81	146 - 35	133° +142	+14.	36	(a)	2,4 5,4	351	-77
6135 9045	3111		+56 57	F8p	6 7 Y	4 ,85	7 + 3	315° - 6	-42,5	8	(5)	-2,1 -0,9	83	- 4
6150 9064	p Pegasi 4865	52 ,7	+24 35	Ma.	7.3 OY	4 .75	56 - 53	228° - 19	- 4,4	12	(3)	-0,1 3,5	77	<b>-36</b>
6155 9071	o Camiopolae 8089	53 ,9	+55 12	B2	2°,8 W	4 ,93 5 ,14	12	115° + 12	- 6.1	4	(3)	-2,1 0,3	83	- 6
6156 9072	O Placinm 5227	54 ,2	+ 6 19	F5	4°,1 Ya	4 ,03 4 ,23	186	126° +186	- 2	31 33	(4)	0,5	70	<b>-54</b>
6160 9076	a Tucanae 3819	54 .7	-66 8	В9		4 .71 4 .80	48	121* + 46	+11	33		5,4	277	<b>-50</b>
6165 9084	Octantia 1596	56 ,4	<b>-77 37</b>	K0		4 ,73	171	204	+23.7	_		3,1	273	-40
6171 9089	30 Placium 6345	56 ,8	- 6 35	МЪ	7,0	4 ,66	-164 53	- 48	-11,8	11	(3)	_5 <u>.9</u> _0,1	61	-66
6173 9091	& Sculptoris	57 ,2	-30 16	B5	<u> </u>	4 ,65	26	94	Var	11	-		345	-80
6179 9098	2 Cett 6417	58 ,6	-17 54	Ao	3° Y1	5 ,15	+ 10	113*	+ 0,3 - 5	16	(1)	0,6	43	-76
	6046. Belipsing bins	 	R Case Park	j   M 6 064 A		4 .77	+ 3	+ 21		16		1,2		

Bom 6046. Relipsing biomry - AR Cass. Pariod 6,066 days. - Bom 6135. Variable star 4m,4 to 5m,1

In the presenting table have been included the two globulers NGC 104 and 5139 m covering in several Uranometrics. To the objects brighter than 5m,00 should also be added several globular clusters and open educions and also the two Magalianic Clouds. The last mantioned objects have, according to the photographic estimates of the present writer, a total magnitude of 0m,8 and 2m,0, respectively.

## II. Catalogue of Stellar Diameters

Explanations to the catalogue Col i gives the Boss number For further details as to the objects the preceding catalogue should be consulted

Col 2 gives the name of the star

Col 3 gives the hypothetical apparent radius according to Herrisprung's determination in Annalen van de Sterrewacht to Leiden XIV, part 1 (1922)

Col 4 the quantity 107,5 x radius (unit 0",001)

(ol 5, 6 and 7 contain the mean ingonometric parallax, the mean spectrographic parallax, and the spectral proper motion parallax, respectively (unit 0",001) By compiling this catalogue the available parallax material up to the beginning of 1929 was used Later on have been added a number of new determinations of trigonometric parallaxes. In a very few cases the dynamic parallax has also been included in the value of  $\pi_1$ . The parallax values have been reduced to absolute values and corrected for systematic errors according to van Maanens tables

Col 8, 9 and 10 contain the linear radii computed by the aid of the three different parallax values  $\pi_1$ ,  $\pi_2$ , and  $\pi_3$  respectively

Col 11 the visual Harvard magnitude (RIIP)

Col. 12 the Harvard spectral class according to the HD Catalogue

Col 13 the quantity  $\hat{H} = m + 5 + 5 \log \mu$  computed on basis of Boss's proper motions When the radius is within parenthesis this indicates that the value is considered to be rather maccinate. In a few cases the radii have not been computed on basis of  $\pi_3$ , because of the fact that the parallax value falls outside the domain within which a fair

	value of $\pi_0$ can	be deriv	ed									
No		Hypothe tical	107.5	filg	Spectro	Spectral proper	Ser	nl diamet	ers	mule	Spectral	
Boss PGC	Namo	radius (unit is 0",0001)	107,5 × radius	parallax T1	parallax	motion parallax π <sub>3</sub>	$\frac{d_1}{2}$	d₃ 2	$\frac{d_3}{2}$	(Hai vard)	Class (Haryard)	H
10	a Andromedae	7	75,2	16	52	59	4,7	1,4	1,3	2,15	AOp	3,8
12	β Cassiopeine	12	129,0	71	71	131	1,8	1,8	0,9	2,42	F5	6,2
27	y L'egasi	4	43,0	3	7	8	_	6,1	5,4	2,87	B2	-1,6
31	χ Pegası	32	344,0	9	11	13	-	31,3	26,5	4,94	Ma	4,8
43	Andromedae	4	43,0	- 2	26	23	_	1,7	1,9	4,44	A2	3,0
50	o Andromedae	2	21,5	14	21	23	1,5	1,0	1,3	4,51	A2	4,0
97	λ Cassiopeiae	1	10,8	9		17	1,2		0,3	4,88	"B8	3,3
103	и Саязгоретае	5	53,8		4	3		13,4	17,9	4,24	Bo	-0,6
122	4 Сазчоренае	3	32,2	-21	5	8	_	6,4	4,0	3,72	B3	0,5
123	π Andromedae	2	21,5	- 8	8	5		2,7	4,3	4,44	В3	1,3
130	a Andromedae	8	86.0	40	27	28	2,1	3,2	3,0	4,52	G5	7,2
132	δ Andromedae	32	344,0	26	30	26	13,2	11,5	13,2	3,49	K2	4,5
135	& Cassiopeine	35	376,3	16	23	33	23,5	16,4	11,4	2,47	Ko	1,4
141	& Cassiopoiae	2	21,5		5	4		4,3	5,4	4,85	B3	1,5
152	о Сазчорење	3	32,2			3			10,7	4,70	B2	1,4
164	& Andromedae	17	182,8	34	22	19	5,4	8,3	9,6	4,30	ко	4,8
168	η Cassiopeiao	11	118,3	182	141	130	0,7	0,8	0,9	3,64	F8	9,1
173	& Piscium	34	365,5	14	16	16	26,1	22,8	22,8	4,55	IX 5	4,4
175	r Andromedae	2	21,5		7	5		3,1	4,3	4,42	B3	1,7
189	Cassiopeiao	6	64,5	65	56	52	1,0	1,2	1,2	4,93	F8	6,3
191	20 Ceti	22	236,5		12	11		19,7	21,5	4,92	Ko	1,1
193	n <sup>1</sup> Cassioperae	15	161,3		13	13		12,4	12,4	4,95	K0	3,6
199	y Cassiopeine	7	75,3	36		129	2,1		0,6	2,25	Bop	-0.4
200	va Cassiopeine	14	150,5	39	16	15	3,9	9,4	10,0	4,83	Ko	4,8
203	μ Andromedae .	4	43,0	33		34	1,3		1,3	3,94	A2	4,9
206	η Andromedao	10	107,5	8	15	15	13,4	7,2	7,2	4,62	G5	3,5
218	2 Ursao minoris	24	258,0		15	16		17,2	16,1	4,52	Ko	4,2
226	s Piscium	13	139,8	25	15	17	5,6	9,3	8,2	4,45	Ko	4,1
257	q Andromedao	3	32,3	10	11	13		2,9	2,5	4,28	B8	-0,7
259	β Andromedae	81	870,7	45	40	39	19,3	21,8	22,3	2,37	Ma	4,0

W.		Hypothe-		74	Spectro-	Speciral- proper	Ве	ni-diame		Myle.	Sportral	
No. Bom PGC	Name	radius (wait is 0",0001)	107.5 × milium	Trig persilen	graphic parallax m	motion parallax	41	4 2	4.	(Har- vard)	(Harvani)	H
264	# Cassiopolas	4	43,0	9	30	34	4,6	1,4	1,3	4,52	A.5	6,3
270	z Piscium .	9	96,7	10	13	12	9.7	7,4	8,1	4,89	Ko	1,5
271	r Pisaiam	13	139,7	38	17	15		8,2	9,3	4,70	Ko	4,2
281	φ Placium .	12	129,0	-8	16	14		8,1	9,2	4,64	Ko	3,0
300	v Piscium	2	21,5	13		16	1,7		1,3	4,67	A2	1,8
304	& Andromedae .	10	107,5		17	12		6,3	9,0	4,99	Ko	3,0
310	w Cassiopoine	16	172,0		14	13		12,3	13,2	4,96	KO	4,6
314	d Camiopeino	8	86,0		68	48		1.3	1,8	2,80	A5	4,2
321	ω Andromodae .	5	53,7	24	38	51	2,2	1,4	1,1	4,96	FS F8	7.7
325	α Uraso minoria	20	215,0	20	11	33	10,7	19,5	6,5	2,12		-0,3
335	$\eta$ Piscium	19	204,2	9	17	16	22,7	12,0	12,8	3.72	G5	1,2
338	z Camiopaina .	9	96.7	17	12	12	5.7	8,1	8,1	4,88	Ko	2,8
350	v Andromedae .	8	86,0	61	84	96	1,4	1,0	0,9	4,18	Go	7.3
357	v Ponsel	31	333,2	17	27	23	19,6	12,3	14,5	3,77	区0 B8	4,3
369	* Andromedae	2	21,5			11			2,0	4,90		2,2
378	Pholum	24	258,0	52	15	12	5,0	17,2	21,5	4,68	Ko	1,3
384	φ Persei	3	32,2	20		12	1,6		2,5	4,19	Hop	1,8
393	o Pincinm	11	118,2	14	15	17	8,4	7.9	7,0	4,50	Ko	4,2
419	« Cassiopeias	4	43,0	12	13	67	3,4	3.3	5,4	3,44	B3	5,4
421	α Trianguli	9,	96.7	51	37		1,9	2,6	1,4			
422	y Ariotis	2	21,5	7		20	3,1		(1,1)	4,04	AOp	4.7
426	E Plecium	10	107,5		19	12		5.7	9,0	4,84	Ko	2,4
428	β Aristia	8	86,0	64	82	57	1,3	1,0	1,5	2,72	A5 A5	3,6
441	A Cassiopeine	3 4	32,2 43,0	25 23	25 37	25 22	1,3	1,3	1,3	4,83	A3	4,7
- 1		1 1		-5			113				_	1
449	50 Camiopelae	4	43,0	08	25	22		1,7	1.9	4,06	A2 B8	2,3
459	g Persel	4	21,5	28	10 22	15	0,8	2,2	1,4	4,99	A2p	3,0
468	21 Andromedae	72	43,0 774,0	13	38	38	59,5	20,4	20,4	3,94	Ko	1,5
477	a Ariotis	50	537,5	33	57	45	16,3	9.4	11,9	2,23	K2	4,1
480		2		-	•	27		7	0,8	4.77	A2	5.7
482	58 Andromedae . β Trianguli .	7	21,5 75,3	14	49	50	5,4	1,5	1.5	3,08	A5	41
505	E <sup>1</sup> CoH	11	118,2	34	7	12	3,5	16,9	9,8	4,54	G 5	1,0
517	7 Trianguil	3	32,2	20	•	23	1,6	,,	1,4	4,07	Ao	3,2
545	65 Andromedae .	37	397.7	4	12	10	99,4	33,1	39,8	4,86	Kg	2.1
550	¿ Camiopaine	4	43.0	24	21	33	1,8	2,0	1.3	4,59	ASD	0,5
560	E Cotl	2	21.5	21	I	17	1.0	_,-,-	1,3	4,34	Ao	2,3
604	d Cetil	2	21,5		3	6	-,-	7,2	3,6	4,04	B2	-+,0
610	12 Porsel	5	53,8	20		12	2,7		4,5	4,99	Go	6,4
617	& Persel	7	75.3	80	94	75	0,9	0,8	1,0	4,22	F8	6,9
620	35 Arietis	1 1	10,8		3	22		2,2	0,5	4,58	B3	0,5
622	7 Cott	6	64,5	38	36	42	1.7	1,8	1,5	3,58	A2	5,2
629	μ Cetl	6	64,5	32		42	2,0		1,5	4,36	FO	6,6
634	39 Ariotta	22	236,5	26	17	19	9,1	13.9	12,4	4,62	KO	6,1
639	η Persel	61	655,7	- 1	15	17	_	43,7	38,6	3,93	Ko	1,7
643	41 Arietis	4	43,0	33	21	29	1,3	2,0	1,5	3,68	138	4.
644	16 Persei	6	64,5	21	35	38	3,1	1,8	1,7	4,27	Fo	5.1
646	17 Persol	38	408,5	9	14	15	45,4	29,2	27,2	4,67	IC5	4.4
653	r Persel	12	129,0	19	26		6,8	5,0	10	4,06	Go, A	
668	# Persel	2	21,5			21	1	1	1,0	4,62	A2	34
670	24 Porael	14	150,5		10	13		15,1	11,6	4,97	Ko	44
674	Arietie ,	3	32,2	10	13	15	3,2	2,5	2,1	4,64	A2	1+0
679	A Ceti	2	21,5		10	7	60.4	2,1	3,1	4,69	B5	-0
691		71	763,2	11	26	22	69,4	29,4	34.7	2,62	F5, A3	1 3
	y Persei	16	172,0	12	40	15	1713	0,0	1 11,5	1 3,00	147 34 44 3	7 7 1

<u> </u>	i			Hypothu			Spectro	Spectral	Sen	d diamete	ers		0 1	
1	11	No Boss PGC	Nami	tical radius (unit is 0",0001)	107,5 > radius	Trig p trailes vi	graphic parallax	proper motion parality	<u>d</u> <sub>1</sub>	$\frac{d_1}{2}$	$\frac{d_3}{2}$	myls (Har vard)	Spectral Class (Haryard)	11
+	6,3	698	ρ Perser ,	62	666,5	38	11	24	17,5	60,6	(27,8)	3,4 to	Mb	4,6
	1.5 4.2 3.0	705 708	Саяморелае В Регвет	2 9	21,5 96,7	29 27	14 45	21	0,7 3,6	1,5 2,1	1,0	4,89 2,2 to	A2 B8	4,6 -3,1
	1,8 3,0	710 713	Persei .	8 21	86,0 225,7	92 29	108 26	113 24	0,9 7,8	0,8 8,7	0,8 9,4	3.7 4.17 4.00	Go Ko	9.7 5.9
	4,6 4,2 7,7 -0,3	717 718 730 741	o Perser δ Arretis ζ Arretis , Camelopardalis	11 16 2 2	118,2 172,0 21,5 21,5	23 47 16 7	15 16 12	12 18 18 22	5,1 3,7 1,3 3,1	7,9 10,8 1,8	9,8 9,6 1,2 1,0	4,82 4,53 4,95 4,76	Ko Ko Ao B3p	1,5 5,4 4,4 0,2
	1,2 2,8 7,3 4,3 2,2	746 752 755 757	Person  # Ceta Arretis 1 Person	31 7 26 2	75.3 279.5 21.5	116	100 100 13 16	61 10 19	30,3 0,6	33,3 0,8 21,5 1,3	33,3 1,2 27,9 1,1	4,92 4,96 4,72 4,98	G5 K5 A2	0,5 7,2 1,9 3,8
כן	1.3	772 778	a Poisei	20 16	215,0 172,0	15	27 20	33 23	14,3 34,4	8,0 8,6	6,5 7,5	1,90 3,80	F5 G5	0,1 3,9
þ	4,2 1,6 5,4 4,7 2,4	780 781 784 786 790	Persei Camelopardalis & Lauri Camelopardalis 34 Persei	33 5 3 6 2	354,7 53,8 32,2 64,5 21,5	13	7 12 7	21 10 26 10 12	1,7	50,7 4,5	16,9 5,4 1,2 6,5 1,8	4,94 4,42 3,75 4,76 4,67	B5 B9p B8 A0p B5	2,5 -2,6 3,0 0,0 2,9
	3,6 4,7 3,5 2,3 3,0	791 795 804 817 825	Camelopaidalis o Persei f Taun  y Persei 10 Taun	2 27 15 4	21,5 290,2 161,2 43,0 75,3	12	14 13 19 76	18 16 15 13	24,2	1,5 22,3 8,5	1,2 18,1 10,7 3,3 0,8	4,98 4,55 4,28 4,26 4,40	A2 K0 K0 B5p G5	2,6 1,4 0,6 2,5 8,0
P	2,1 1,5 4,1 5,7 4,1	838 842 844 847 852	d Person , Camelopardalis o Persel p Persen 17 Lauri	5 9 4 9	53,8 96,7 43,0 96,7 32,2	5 13 17 20	20 12 5 20 18	17 9 6 22 14	10,8 3,3 5,7 1,6	2,7 8,1 8,6 4,8 1,8	3,2 10,8 7,2 4,4 2,3	3.10 4.96 3.94 3.93 3.81	B5 F5, A B1 F5 B5p	1,4 0,7 1,0 -1,3 2,4
) ) )	2,3	856 858 860 861 865	q Lami	2 2 3 45 3	21,5 21,5 32,2 483,7 32,2	9	13 19 14 10	12 16 14 9	2,4	1,7 1,1 2,3 48,4 2,3	1,8 1,3 2,3 53,7 2,3	4,37 4,67 4,02 4,71 4,25	B5 A0 B5 Ma B5	2,8 3.0 2,7 -2,3 3.1
, , , , , , ,	0.3 5,2 6,6	869 877 894 896 901	η Lauri 27 Lauri ζ Persor Camelopardalis w Fridani	5 4 7 3 9	53.8 43.0 75.3 32.2 96.7	- 26 10	28 22 7 13 15	19 24 8 9	7.7 7.5 32,2	1,9 2,0 10,8 2,5 6,4	9,4 3,6	2,91 4,87	B5p B8 B1 B9 A, G5	1,5 2,4 -0,5 -1,6 2,3
0 0	6,1	910 913 920	в Регчет § Регчет λ'Івшт	5 4 5	53.8 43.0 53.8	3	7 5 7	11 5 6	-	7.7 8,6 7.7	8,6	4,05 3,4 to	Oe 5	0,9 0,3 ~0,8
5	5.9	932 936		4	43.t 129.0		29 20		3,3 43,0					-1,8 4,8
2 0 2 5 8	3.6 4.0 -+ 0.8 0.1	938 947 967 970 972	μ Persei f Persei	3 4 16 17 12	32,2 43,0 172,0 182,1	15 28		16 11 11 9	2,9 6,1 16,1		2,0 3,9 15,6 20,3 11,7	4,03 4,28 4,89	B3p G0 G0, A	1,7
	A 3 — 1.9 2⊙		Handbuch der	Astrophysi	k V, 2							72		

1138 Appendices to Chap.4. K.Lundmark; Luminosities, Colours, Diameters, etc. of the Stars.

N'-		Hypothe-		Teir	Spectro-	Spectral-	Sen	ni-diamet	era		Space	
No. Boss PGC	Name	tical radius (unit is 0'',0001)	107,5 x midlus	Trig parallax n <sub>1</sub>	graphic parallax m	proper motion paraliax n	<u>d</u> <sub>1</sub>	$\frac{d_0}{2}$	<u>d</u> , 2	m <sub>vis</sub> (Har- yard)	Spectral Class (Harvard).	H
981	μ Tauri	2	21,5		9	10		2,4	2,2	4,32	В3	2,0
986	b¹ Persei	3	32,2			22			1,5	4,57	A2	4,0
989	ω Tauri	4	43,0	00	28	20		1,5	2,2	4,80	A3	3.9
1000	y Tauri d Persel	16	172,0	29	23	22	5,9	7.5	7,8	3,86	K0	4,3
1003		2	21,5		5	10		4,3	2,2	4,89	В3	3,2
1017	δ¹ Tauri	19	204,2	17 28	26	21	12,0	7,8	9,7	3,93	KO	4,2
1022 1026	7 Tauri	4	21,5 43,0	24	34 30	26 29	0,8	0,6 1,4	0,8	4,84 4,36	A5 A3	5,3 4,6
1020	8 Tauri	3	32,2	25	28	28	1,3	1,2	1,1	4,24	A2	4,4
1033	v <sup>1</sup> Tauri	5	53,8	26	30	30	2,1	1,8	4,8	4,40	A5	4,8
1034	71 Taurl	3	32,2	24	29	27	1,3	1,1	1,2	4,60	A5	5,0
1036	π Tauri	ğ	96,7			12	-,0	-,-	8,0	4,94	Ko	2,7
1044	ε Tauri	22	236,5	31	34	24	7,6	6,9	9,8	3,63	Ιζο	4,0
1045	91 Taurl	20	215,0	37	28	21	5,8	7.7	10,2	4,04	Ko	4,2
1046	Da Tauri	4	43,0	28	42	25	1,5	1,0	1.7	3,62	Fo	3,8
1054	Tauri	3	32,2	28	25	26	1,2	1,3	1,2	4,84	Λ5	5,2
1063	45 Eridani	13	139.7			10		, .	14,0	4,97	KO	-2,6
1067	g Tauri	4	43.0	23	28	26	1,9	1,5	1.7	4,75	A5	4,8
1074 1077	e Persei	25 176	268,7 1892,0	28 57	83	13 60	9,6 33,2	67,2 22,8	20,7	4,46 1,06	K0, A3 K5	1,4 2,6
	3.001				40						1 4 2	
1076 1079	d Tauri	4 2	43,0 21,5		19 4	(2)		2,3	(10,8)	4,38	A3 B2	3,5 -4,4
1087	c¹ Tauri	3	32,2	27	36	29	1,2	0,9	1,1	4,30	A3	4,4
1090	og Tauri	2	21,5	22	28	21	1,0	0,8	1,0	4,85	A3	4,5
1107	r Tauri	2	21,5	8	9	9	2,7	2,4	2,4	4,33	.B5	1,1
1123	μ Eridani	2	21,5		9	10		2,4	2,2	4,18	B5	0,9
1139	9 Camelopardalis	3	32,2	-25	4	3	_	8,1	10,7	4,38	Bo	-0,8
1140	$n^0$ Orionia	10	107,5	136	122	115	0,8	0,9	0,9	3,31	F8	6,7
1141	π² Orionis	3	32,2			16	ا ا	0.0	2,0	4,35	A0	2,0
1147	π <sup>4</sup> Orlonis	3	32,2	2,	4	7	16,1	8,0	4.6	3,78	В3	-2,0
1159	л <sup>в</sup> Orionis, , , ,	2	21,5	3	7	6	7,1	3,1	3,6	3,87	B3	-3,1
1161	7 Camelopardalis	3	32,2	1	20	14		1,6	2,3	4,44	A2	-0,2
1163 1167	π¹ Orionis	60	32,2 645,0	18	18 27	24	35,8	1,8 23,9	1,3	4,74 2,90	A0 K2	5,6
1169	o <sup>2</sup> Orionis	23	247.2	20	19	18	12,3	13,0	13,7	4,28	Ko	4,3
1178	4 Aurigae	2	21,5	27		20	0,8		1,1	4,99	Ao	5,3
1181	# Orlonis	28	301.0	21	15	10	0,0	20,1	30,1	4,73	Ko	-1.4
1185	β Camelopardalis	13	139,7	16	1 4	24	8,6	34,9	5,8-	-4,22	Gop	-0,2
1187	s Aurigae	13	139.7	2	7	11	(69,6)	20,0	12,5	(3,18)	F5p	-1.1
1190	ζ Aurigae	41	440.8	- 3	38	12	-	11,6	36,7	3,94	K0, B1	1:5
1194	'Taurl , , , ,	3	32,2	-19	30	25	-	1,1	1,3	4,70	A 5	4,3
1202	9 Aurigae	5	53.8		34	30	(	1,6	1,8	4,99	Fo	6,2
1203	11 Orionis	2	21,5	16		17	1,4		1,3	4,65	B9	2,7
1204	η Aurigae	3	32,2	14	10	19	2,3	3,2	1,7	3,28	B3	2,8
1227	15 Orionia	4	43,0	-25		14	-		3,1	4,86	Fo	0,1
1236	μ Aurigae	3	32,2	68		22	0,5		1,5	4,78	A 3	4,2
1240	o Orionis	20	215,0	_5	22	12	(43,0)	9,8	17,9	4,64	. Ko	0,5
1246 1258	& Aurigae 16 Aurigae	56	602,0	75	91	91	8,0 16,5	6,6	12,6	0,21	GO KO	3,4 6,2
1259		20	215,0	13 68	13 83	17	1,1	0,9		1.4,85	Go	9,5

No.		Hypothe- tical	107,5	Trig	Spectro-	Spectral- proper	So	mil-diamo	ters	mela	Spectral	
Boss PGC	Name	rndius (unit ls 0",0001)	x radius	parallax n <sub>1</sub>	graphic parallax ar	motion parallax n	<u>d</u> <sub>1</sub>	2	<u>d</u> , <u>2</u>	(Har- vard)	Class (Harvard)	Н
1284 1289 1301 1302 1303	o Orionis m Orionis η Orionis	2 1 3 2 7	21,5 10,8 32,2 21,5 75,3	12	4 5 7 16	6 5 5 7 16	2.7 4.0	5,4 2,2 4,6 4,7	3.6 2,2 6,4 3,1 4,7	4,65 4,99 3,44 4,73 1,70	B3 B3 B4 B3p B2	-0,4 -0,8 -2,7 1,3 -1,8
1304 1315 1314 1327 1331	β Tauri	8 2 1 35 2	86,0 21,5 10,8 376,2 21,5	24 -12 15	37 5 11	67 7 5 9	3.6 - 1.4	2,3 2,2 2,0	1,3 3,1 2,2 41,8 2,1	1,78 4,83 4,66 4,97 4,32	B8 B3 B2 K5 B3	3,1 1,0 0,4 2,2 2,2
1333 1335 1339 1353 1357	χ Aurigae	3 66 5 2 3	32,2 709,5 53,8 21,5 32,2	9 2 6	3 7 6 4	4 8 5 3 4	6,0 10,7 5,4	236,5 7.7 3,6 8,1	8,1 88,7 10,8 7,2 8,1	4,88 4,73 2,48 4,53 3,49	B1 Ma B0 B0 Oc5	1,0 0,3 -4,5 -1,0 -1,3
1364 1370 1373 1375 1389	c¹ Orionis	2 7 18 4 3	21,5 75,3 193,5 43,0 32,2	17 5 27 - 1 - 9	6 12 28 15	4 7 24 13 3	15,1 7,2 —	3,6 6,3 6,9 2,9 8,1	5,4 10,8 8,1 3,3 10,7	4,65 1,75 4,39 3,00 3,78	В3 В0 Ко В3р В0	-3,9 -6,7 6,9 0,2 -6,2
1391 1396 1398	ω Orionis 126 Tauri ζ Orionis	2 2 6	21,5 21,5 64,5	7 -19	4 5 8	5 8 7 3	3,1	5,4 4,3 8,1	4,3 2,7 9,2 21,5	4,54 4,87 2,05 4,21	B3p B3 B0	-1,6 2,3 -2,9
1399 1429	Orlonis	2 10	21,5 107,5	2	7 15	5	53,8	3,1 7,2	4,3 7.7	5.00 4.64	<b>В3</b> Ко	0,7 2,4
1438 1439 1442 1453 1457	134 Tauri	2 33 19 2 3	21,5 354,7 204,2 21,5 32,2	19 -14 16	10 18 20 15	14 10 13 12 13	10,7	35,5 11,3 1,1 2,1	1,5 35,5 15,7 1,8 2,5	4,92 4,99 4,18 4,92 4,54	B9 Ma K0 A2 A0	2,2 3,6 -1,3 0,7 1,3
1461 1468 1472 1475 1478	$\chi$ Orlonis $\alpha$ Orlonis $\delta$ Aurlgao	8 211 18 2 8	86,0 2268,2 193,5 21,5 86,0	104 11 18	94 10 28 4 63	57 39 23 3	0,8 206,2 10,7	0,9 226,8 6,9 5,4 1,4	1,5 58,2 8,4 7,1 2,3	4,62 (0,34) 3,88 4,90 2,07	F8 Ma K0 B2 A0p	6,2 -1,8 4,8 -2,1 0,4
1479 1482 1494 1501 1508	π Aurigae	39 6 14 5 14	419,2 64,5 150,5 53,8 150,5	16 43 28	6 34 30 27 37	8 40 15 19 20	4,0 1,3 5,4	69,9 1,9 5,0 2,0 4,1	52,4 1,6 10,0 2,8 7,5	4,59 2,71 4,68 4,19 4,30	Ma Aop Ko A2 G5	-0,2 2,8 4,3 1,8 4,5
1507 1525 1550 1548 1556	χ <sup>2</sup> Orionis ν Orionis f <sup>1</sup> Orionis ξ Orionis Camelopardalis	5 2 2 2 2	53,8 21,5 21,5 21,5 21,5 21,5	-31 12	4 4 7 13	5 9 7 9 21	- 1,8	13,4 5,4 3,1 1,7	10,8 2,4 3,1 2,4 1,0	4,71 4,40 4,92 4,35 4,73	B2p B2 B3 B3 A0	0,6 2,2 1,8 2,1 4,9
1561 1565 1575 1604 1611	η Geminorum	82 13 2 66 4	881,5 139,7 21,5 709,5 43,0	14 14 34 16 16	12 19 24 15	22 14 23	63,0 10,0 0,6 44,4 2,8	73,4 7,4 0,9 47,3	67,8 6,3 1,5 30,8	(3,2) 4,45 4,42 3,19 4,33	Ma Ko Ao Ma A5	2,3 6,6 1,1 3,7 -0,3

1468.  $\alpha$  Orionis. This is the only star for which actual variations in the diameter have been measured by the interferementer methods. For details about these measurements consult the text. The diameter as computed from the  $\pi_1$ 's ranges from 116,4 (maximum) to 174,4 (minimum). The interferements show also that the diameter is largest at minimum light.

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4		Hypothe		41-3-	Spectro-	Spectral-	Sen	ıl-diamet	егв		Case t-al	_
No. Boss PGC	Name	tical radius (unit is 0",0001)	107,5 ∠ radius	Trig parallax n <sub>1</sub>	graphic parallax	proper motion parallax	$\frac{d_1}{2}$	$\frac{d_{\mathbb{R}}}{2}$	<u>d</u> <sub>0</sub> 2	"tris (Har- vard)	Spectral Class (Harvard)	H
1635	r Geminorum	3	32,2	19	10	9	1,7	3,2	3,6	4,06	135	0,8
1657	13 Monocerotis	3	32,2	-18	13	11	_	2,5	2,9	4,50	AOP	-0,5
1690	y Geminorum	9	96,7	43 8	63	(3)	2,2	1,5 5,4	2,4 (7,1)	1,93 4,68	A O	1,0 0,8
1706 17 <b>16</b>	S Monocerotis . 12 Lyncis	2	21,5 21,5	20	14	14	1,1	1,5	1,5	4,89	Λ2	1,8
1717	# Geminorum	45	483,7	7	11	18	69,1	44,0	26,9	3,18	G 5	-0.3
1721	30 Geminorum	19	204,2	-14	19 49	15	2,2	10,7	13,6	4,65 3,40	ICO ICS	4.0
1725	& Geminorum	10	107,5	48 19	14	12	8,5	11,5	13,4	4,70	Ko	5,2
1740 1758	Camelopardalis	23	247.2	13	13	15	19,0	19,0	16,5	4.75	IK 5	4,4
1763	O Geminorum	4	43,0	19		21	2,3		2,0	3,64	A2	2,3
1776	15 Lyncis	11	118,2	6	19	17	19,7	6,2	7.0	4,54	Go Fo	5.2 4.9
1778	e Geminorum	4 2	43,0 21,5	44	34	15	1,0	1,3	1,6 1,4	4,70 4,80	A2	1.8
1786 1812	19 Monocerotis.	2	21,5		6	4		3,6	5,4	4,89	B3	-0,0
1815	ζ Geminorum	14	150,5	5	3	4	30,1	50,2	37,6	3,6 to 4,5	Gop	-1.5
1840	7 Geminorum	24	258,0	5	18	15	51,6	14,3	17,2	4,48	Ko	3,
1853	3 Monocerotis	3	32,2	20		13	1,6		2,5	4,09	A0	-0,
1879	Lyncis	3	32,2			6			5,4	4,80	A.2	0,
1886	1 Geminorum	5	53,8	38	38	12	1,4	1,4	4,5	3,65	A2	2,
1898	d Geminorum.	8	86,0	60	44	27	1,4	2,0	3,2	3,51	FO	0,
1928	21 Lyncis	18	193,5	25	25	18	7,7	7,7	1,2 8,4	3,89	AO KO	2,
1931 1944	& Canis minoris .	4	43,0	20	30	32	2,1	1,4	1,3	3,09	B8	2,
1952	e Gemlnorum.	6	64,5	52	37	42	1,2	1.7	1,5	4,18	Fo	6,
1953	y Canls minoris .	33	354,7	5	9	15	71,0	39,4	23,6	4,60	Ko	3.
1962	6 Canis minoris .	20	215,0	19	12	11	11,3	17.9	19,5	4,85	Ko	1,
1979	a Geminorum	11	118.2	77	66	39)	1,5	1,8	3,0			3,
1987	v Geminorum	10	440.0	11	18	585	38,1	23,3	2,0]	1,99	K5	1
2001	o Geininorum.	39 4	419,2 43,0	25	19	20 27	1,7	2,3	1,6	4,22 4,92	Fo	5,
2008	α Canis minoris .	31	333,2	312	331	305	1,1	1,0	1,1	0,48	F 5	5.
2010	24 Lyncis	3	32,2		19	19		1,7	1.7	4,96	A 2	4,
2023	σ Geminorum	20	215,0	20	40	22	10,7	5,4	9,8	4,26	Ko	6,
2029	β Geminorum	17 64	182,7 688,0	101	129	83	8,3 6,8	7,3	20,3	3,68	G 5 K 0	2,
2078	φ Gominorum	2	21,5		16	17		1,3	1,3	4,99	A2	3.
2126	1		172,0			15		"	11,5	4,88	Ko	4
2130	13 Canis minoris ,	24	258,0	19	19	17	13,6	13.6	15,2	4,52	Ko	4
2145			21,5		16	18	_	1,3	1,2	4,87	Λ2	3
2155			150,5	- 7	4	10	-	37,6	15,1	4,41		1.
2168			75,3	48	44	25	1,6	1,7	3.0			5 3 4
2195		1 -	408.5	- 2	18	20		22,7	20,4			3
2208 2237			451,5	20	16	18 24	22,6	28,2	25,1	3,95		3
2247			204,2		15	24	3,4	13,6	8,5	3,47		4
2290			182,7	1	19	13	14,1	9,6	14,1			3 3
2295			32,2		20	22		1,6	1,5			3
2302 2327			258,0		14	14	18,4					1
2330			21,5		7	10	3,6	3,1	1,0			5

1815. Cepheid variable. The parallax value derived on basis of the period-luminosity relation is 0",004.

No		Hypothe tical	107,5	Frig	Spectro	Spectral proper	Sen	ni diamet	ers	m, is	Spectral	
Boss PGC	Name	1 adms (unit 1s 0",0001)	\ 1adius	parallax $n_1$	graphic parallax t <sub>a</sub>	inotion parallax	d <sub>1</sub> 2	$\frac{d_3}{2}$	$\frac{d_3}{2}$	(Har yard)	Class (Harvard)	11
2336	δ Cancri	18	193,5	16	19	23	12,1	10,2	8,4	4,17	Kο	6,1
2348	t Cancii	19	204,2	21	10	16	9,7	20,4	12,8	4,20	Cr 5	2,9
2351	e Hydrac	16	172,0	15	54	84	11,5	3,2	2,0	3,48	1.8	4.9
2361 2393	g Hydrae ζ Hydrae	25	21,5	14	13	16 26	(5,4) 19,2	1,6	1,3	4,42 3,30	Ao Ko	2,4 3,4
2404	t Ursae majoris	8	86,0	70								
2407	α Cancii	3	32,2	30	66 30	69 22	1,2	1,3	1,2	3,12	A5	6,6
2411	B Ursae majoris	27	290,2	30	9	8	1,1	1,0 32,2	1,5 36,3	1,27 4,99	A3 Ma	2,9 1,6
2413	10 Ursac majous	6	64,5	70	69	72	0,9	0,9	0,9	4,09	1.5	7.6
2424	& Ursae majoris	4	43,0	17	26	25	2,5	1,7	1,7	3,68	Λo	3,0
2437	Ursae majoris	15	161,2		1	12		40,3	13,4	4,71	G5	2,9
2441	o <sup>2</sup> Ursae majoris	4	43,0	43	54	40	1,0	0,8	1,1	4,87	F8	4,1
2443	f Ursae majoris	5	53,8	- 2	41	28		1,3	1,9	4,54	A3p	5,2
2446	r Ursae majoris	5	53,8		23	39		2,3	1,4	4,74	1.5, A5	5,2
2476	e Ursae majoris	3	32,2		18	24		1,8	1,3	4,89	A 5	4,6
2479	v Hydrae	3	32,3	17	25	41	1,9	1,3	0,9	3,84	Λо	6,5
2495	38 Lyncis 40 Lyncis	4	43,0	32	21	33	1,3	2,0	1,3	3,82	A2	4,5
2507 2524	κ I conis	61 21	655,7	2 7	3 i 20	33	327,8	21,2	19,9	3,30	IC5 ICO	5,0
2536	Diaconis	20	215,0	_ /	15	15	-	11,3	15,0	4,61 4,58	K2	3,6 1,7
2540	h Ursae majoris	7	75,3	29	43	20	2,6	1,8	3,8	3.75	Fo	4,1
2541	τ <sup>1</sup> Hydrae	5	53,8	77	45	37	0,7	1,0	1,5	4,78	F5	5,3
2549	d Uisae majoris	9	96,7	43	42	14	2,2	2,3	6,9	4,57	Go	4,3
2550	λ I coms	39	419,2	21	14	14	20,0	29,9	29,9	4,48	IC 5	3,2
2552	y Uraac majoris	10	107,5	56	79	147	1,9	1,4	0,7	3,26	F8p	8,5
2559	12 Hydrac	3	32,2		0	17		i	1,9	4,50	A.3	1,6
2565	26 Ursae majous	2	21,5		16	20		1,3	1,1	4,65	Ao	4,0
2566	10 Leonis minoris	11	118,2		20	12		5,9	9,8	4,62	G5	2,0
2570 2589	Lyncis 2 Sextantis	11 21	118,2		20	28 18		11,3	4,2 12,5	4,99 4,78	K0	6,0
2595	. Hydrae	28	301,0	19	22	19	15,8	13,7	15,8	4,10	Ko	3,8
2602	o Leonis	8	86,0	26	12	56	3,3	7,2	1,5	3,76	F5, A3	
2618	& I coms	18	193,5	- 1	16	18		12,1	10,8	3,12	Gop	1,5
2632	v Ursae majoris	7	75,3		38	53		2,0	1,4	3,89	Fo	6,5
2637	φ Ursae majous	3	32,2	7	15	12	4.7	2,1	2,7	4,54	A2	-0,7
2648	μ Leonis	24	258,0	19	24	23	13,6	10,7	11,2	4,10	Ko	5.9
2680	7 Leonis	12	451,5		7	10		64.5	45,2	4,89	Ma	3, 1
2692	21 Leonis minoris	3	32,2		28	26		1,2	1,2	4,47	A5	3,1
2694 2696	A I coms	3 37	32,3 397,8		14	10		28,4	3,2 23,4	3,58 4,58	K2	-1,0 4,9
2697	15 Sextantis .	2	21,5			9			2,4	4,50	Ao	1,9
2698	α Leonis	10	107.5	58	66	81	1,9	1,6	1,3	1,34	B8	3.3
2730	ζ Leonis	6	64,5	9	29	28	7,2		2,3	3,67	170	0,8
2729	à Ursae majoris	4	43,0	-10			_			3,52	A2	4,6
2741	40 Leonis	6	64,5	50	46	50	1,3	1,4	1,3	4,97	1.5	7,6
2742	γ <sup>1</sup> and γ <sup>2</sup> Leonis	43	462,2	4	43	43}	(115,5)	10,7	10,7	2,61	Ко	5.31
2751	μ Ursae majoris	71	763,2	34	32	29}	22,4	23,9	15,9] 31,8	3,80	TK 5	6,5
2754		2	21,5		14	12	,	1,5	1,8	4,92	Ao	1,9
2768	30 Leonis minoris	3	32,2		32	26		1,0	1,2	4,83	Fo	5,0
2776	31 Leonis minoris	12	129,0	11	26	20	11,7	5,0	6,4	4,41	Ko	5,4

1142 Appendices to Chap 4 K.Lundmark Luminosities, Colours, Diameters, etc of the Stars.

No.		Hypothe-		7-V-	Specim-	Spectral proper	Sec	d-diamet	m,	e , is	Spectral	
Boss PGC	Namab	radius (unit is 0",0001)	107 <sub>1</sub> 3	Trig parallex #1	graphic paralles #9	motion parallax	41 2	4 2	<u>d,</u> 2	(Har- vani)	Spectral Class (Harvard)	н
2785	36 Uraso majoria	7	75.3	80	67	43	0,9	1,1	1,8	4,84	F5	6,1
2792	30 Sextantia .	1	10,8		8	12		1,3	0,9	4,95	B5	3,6
2802	Urano majoria ,	3	32,2	26	30	27	1,2	1,1	1,2	4,84	A5	5,6
2804	e Leonis .	2	21.5	29	5	4	0,7	4,4	5,4	3,85	Bop	-1,4
2829	37 Leonis minoris	10	107.5	21	8	6	5,1	13,4	17.9	4,77	Go	-1,0
2899	46 Leonis minoris	16	172,0	31	33	27	5.5	5,2	6,4	3,92	Ko	6,3
2900	ω Urace majoris	2	21,5			16			1,3	4,84	A0	3,6
2909	54 Locals	2	21,5		18	21		1,2	1,0	4,32	A0	3,8
2930	β Urase majoris	7	75.3	47	54	41	1,6	1.4	1,8	2,44	AO	2.2
2931	p* Leonis	46	494.5	25	12	9	19,8	41,2	54.9	4.97	Ma	3,0
2932	b Leonia .	3	32,2	10		9	3,2		3,6	4,42	Ao	1,7
2933	α Ureas majoris	47	505,2	21	54	49	24,0	9,4	10,3	1,95	Ko	2,7
2942	z Leonia	5	53,8	10	14	44	5,4	3,8	1,2	4,66	Fo	7.4
2958	w Umas majoris	29	311,7		44	27		7.1	11,5	3,15	Ko	2,3
2972	d Loomis	8	86,0	78	58	60	1,1	1,5	1,4	2,58	A3	4,2
2974	# Loonis	4	43,0	19	32	31	2,3	1,3	1,4	3,41	AO	3,5
2976	72 Leonh	27	290,2		8	8		36,3	36,3	4,87	Ma	1,2
2982	o Leonis . ,	3	32,2			27			1,2	4,58	A5	5,0
2984	è Ursao majoris .	8	86,0	146	126	60	0,6	0,7	1,4	4,87	Go	8,2
2985	r Ursas majoris .	33	354.7	7	21	19	50,7	16,9	18,7	3.71	K0	0,9
2987	55 Ureso majoris	2	21,5	13	16	22	1,7	1,3	1,0	4,78	A2	4,8
2990	o Leonis	3	32,2		15	25		2,1	1,3	4,13	AO	4,0
2999	Leomie	7	75.3	58	51	54	1.3	1,5	1,4	4,03	F5	5.3
3031	λ Draconia	44	473,0	22	14	13	21,5	33,8	36,4	4,06	Ma	2,3
3058	v Leomis ,	11	118,3	12	21	15	9,9	5,6	7.9	4,47	Ko	2,2
3089	* Virginia .	40	430,0	7	15	20	61,4	28,7	21,5	4,20	Ma	5,6
3090	z Uresa majoria .	22	236,5	12	29	22	19,7	8,2	10,8	3,85	Ko	4.5
3098	93 Leonis	6	64,5	29	45	54	2,2	1,4	1,2	4,54	B8	5.5
3101	# Leonis	9	96,7	101	73	86	1,0	1,3	1,1	2,23	A2	5,8
3105	#Virginia	9	96,7	101	90	110	1,0	1,1	0,9	3,80	F8	8,3
3117	y Ursae majoris .	6	64,5	4	48	39	(16,1)	1,3	1,7	2,54	Ao	2,4
3139	# Virginia	3	32,2		22	18		1,5	1,8	4,57	A3	2,2
3155	o Virginis	13	139.7	38	15	25	3.7	9,3	5,6	4,24	G5	6,0
3190	d Urmo majoria ,	4	43,0	45	32	36	1,0	1,3	1,2	3,44	A2	3.7
3210	o Virginia .	3	32,2			23			1,4	4,00	A0	3,1
3216	11 ComaeBerenices	10	107.5		20	16		5,4	6,7	4,91	Ko	5,6
3224 3230	12 Comac Berenices 5 Can Venati-	6	64,5		36	21		1,8	3,1	4,78	F5	0.8
	corrun , ,	8	86,0		11	10		7,8	8,6	4,97	Ko	0,2
3242	y ComacBerenices	14	150,5	1	18	18	(150,5)	8,4	8,4	4,56	K0	5,0
3279	B Can. Vonati-								-			
k 61	oorum	10	107.5	107	110	96	1,0	1,0	1,1	4,32	Go	8,7
3281	и Draconis	2	21,5	- 3	13	17	-	1.7	1,3	3,88	BSp	2,8
3283	23 Comae Berenices		21,5	- 1	14	18	-	1.5	1,2	4,78	AO	4.1
3284 3302	24 Comne Berenices		118,2		10		1	11,8		4,95	Κo	1,14
	y Virginia .	10	107.5	73	64	59	1,5	1.7	1,8		7.1	2.8 4.1 6.7
3309	o Virginia	2	21,5	1	13	22		1,6		4,95		

1144 Appendices to Chap.4. K.Lundmark: Luminosities, Colours, Diameters, etc. of the Stars.

		Hypoths-			C	Spectral-	Sen	nl-dlamot	ers			
No. Boss	Name	tical radius	107,5 × radius	Trig parallax	Spectro- graphic	proper motion				m <sub>vis</sub>	Spectral Class	П
PGC	711112	(unit is 0",000i)	× raunus	$\pi_1$	parallax π <sub>a</sub>	parallax #	<u>d</u> <sub>1</sub>	$\frac{d_1}{2}$	2 2	vard)	(Harvard)	
3770	a Bootis	12	129,0	45		15	2,9		8,6	4,69	Ko	4,3
3771	ε Bootis	23	247,2	16	25	31	15,5	9,9	8,0	2,59	Ko, Ao	1,1
	109 Virginis		43,0	140	440	22	0.6	0.7	2,0	3,76	A0	4,2
3798 3809	β Ursae minoris.	10 82	107,5 881,5	168 11	149 41	20 21	0,6 80,1	0,7 21,5	5,4 42,0	4,64 2,24	G5 K5	5,2 -0,4
3814	16 Librae	3	32,2		32	35					Fo	6,0
3827	Ursac majoris .	33	354,7		7	12		1,0 50,7	0,9 29,6	4,59 4,86	Mb	4,4
3834	ω Bootis	21	225.7			13			17,4	4,93	K5	3.8
3835 3836	110 Virglnis β Bootis	13	139,7	22	39	14	6,3	3,6	10,0	4,62	ICO C5	3,1
			182,7	23	19	20	7,9	9,6	9,1	3,63	G5	2,6
3842 3847	ψ Bootis i Bootis	15	161,2	76	16	19	ا , ا	10,1	8,5	4,67	Ko Co	5.9
3887	d Bootis	17	75,2 182,7	76 24	77 25	68 26	1,0 7,6	1,0 7,3	1,1 7,0	4,86 3,54	Go Ko	7.9 4.5
3926	μ Bootis	4	43,0	34	36	33	1,3	1,2	1,3	4,33	Fo, Ko	
3928	y Ursao minoris .	5	53,8		42	24		1,3	2,2	3,14	Λ2	-0,7
3936	Draconis ,	30	322,5	34	30	17	9,5	10,8	19,0	3,47	Κo	-1,5
3940 3949	β Coronae borealis r <sup>9</sup> Bootis	5 2	53,8		33	45 8		1,6	1,2	3,72	Fop	5,1
3953	# Coronae borealis	3	21,5 32,2			12			2,7 2,7	4,98	A2 B5	2,1 2,0
3960	8 Serpentis	5	53,8	16	30	28	3,4	1,8	1,9	3,85	ro	3,4
3961	α Coronao borealis	6	64,5	53	51	50	1,2	1,3	1,3	2,31	Ao	3,3
3988	Coronae borealis	2	21,5	18	9	7	1,2	2,4	3,1	4,69	В8	0,4
3994 3998	Serpentis	4	21,5 43,0	7 22	20	24 27	3,1 2,0	1,1	0,9	4,49	A2 A0	4,3 4,0
4001	a Serpontis	37	397.8	46	44	35	8,6	1,9	1,6 11,4	- 3,93 2,75	KO	3,5
4009	β Serpentis	4	43,0	32	30	27	1,3	1,4	1,6	3,74	A2	3,5
4010	2 Serpentis	8	86,0	87	101	60	1,0	0,9	1,4	4,42	Go	6,4
4015	* Serpentis	45	483,7	10	14	19	2.0	34,6	25,5	4,28	IC 5	4,5
4016 4024	μ Serpentis	9	43,0 96,7	19	22 28	28 16	6,9	2,0 3,5	6,0	3,63	G5	3,4 4,9
4026												
4031	s Serpentis	25	43,0 268,7	36	13	34 12	1,2	1,0	1,3	3,75 4,88	A2 K5	4,4 3,3
4032	Coronae borealis		172,0	31	28	23	5,5	6,1	7.5	4,77	Ko	7.6
4035	C Ureae minoris .	2	21,5		22	17		1,0	1,3	4,34	A2	1,3
4042	χ Herculis	8	86,0	69	85	72	1,2	1,0	1,2	4,61	Go	9,0
4055	γ Serpentla	8	86,0	78	118	102	1,1	0,7	0,7	3,86	F5	9,5
4063	a Coronao borealis Draconis		225,7		23	19		9,8	11,9	4,22	KO	4,4
4072	Coronae borealis	4 2	43,0 21,5		32 15	28 15		1,3	1,5	4,96	A5 A0	6,4 3,2
4081	π Serpentis	2	21,5		.,	13		117	1,7	4,82	A2	1,0
4089	v Herculis	2	21,5			12			1,8	4,64	Bo	4,4
4090	# Draconis	8	86,0		63	87		1,4	1,0	4,11	F8	7,4
4108 4112	τ Coronae borealis φ Herculis		129,0	30	34	21	4,3	3,8	6,1	4,94	K0	7.5
4134	d Ophluchi	67	21,5 720,2	14 40	30	18 26	1,5	24,0	1,2 27,7	4,26 3,03	B9p Ma	1,8 4,1
4147	s Ophiuchi	22	236,5	46	23	26	5,1	10,3	0.4	2 24	Ko	
4162	r Herculis ,	3	32,2	40	13	11	2,1	2,5	9,1	3,34	B5	3,0
4163	o Serpentis	4	43,0	32	28	31	1,3	1,5	1,4	4,80	Fo	6,0
4165 4169		12	75,3	18	31	32 16	4,2	2,4	2,4	3,79	F0	2,8
4109	1 5 coronac norcans	12	129,0	כו ן	1 17	1 10	8,6	7,6	8,1	4,72	K <sub>0</sub>	5,3

				Ü						-		
		Hypothe-	_		Spectro-	Spectral-	Seir	l-dlamete	г8			
No. Boss PGC	Name	tical radius (unit is 0",0001)	107,5 × radius	Trig parallax n	graphic parallax	proper motion parallax ma	<u>d,</u>	<u>d</u> , 2	$\frac{d_{\mathbf{q}}}{2}$	Her- vard)	Spectral Class (Harvard)	Н
4182 4192 4204 4203 4212	$\omega$ Herculis $\eta$ Draconis $\beta$ Horculis $\lambda$ Ophinchi h Herculis	2 25 26 3 30	21,5 268,7 279,5 32,2 322,5	42 30 0 -11	19 42 26 29 13	20 25 34 27 19	6,4 9,3 —	1,1 6,4 10,7 1,1 24,8	1,1 10,7 8,2 1,2 17,0	4,53 2,89 2,81 3,85 4,92	Aop G5 K0 A0 K5	4,0 1,8 3,0 3,8 6,5
4213 4220 4246 4255 4259	A Draconis σ Herculis ζ Horculis η Horculis g Draconis	2 3 15 18 14	21,5 32,2 161,2 193,5 150,5	31 111 53 19	96 31 21	15 18 132 24 10	0,7 1,5 3,7 7,9	1,6 1,7 6,2 7,2	1,4 1,8 1,2 8,1 15,1	4,98 4,25 3,00 3,61 5,00	B8p A0 G0 K0 K0	3,1 2,1 6,9 3,6 1,1
4270 4284 4302 4315 4322	Draconis 52 Herculis Ophiuchi Ophiuchi	5 2 2 29 4	53,8 21,5 21,5 311,7 43,0	3 61	33 16 39 70	22 20 23 31 36	7,2 0,7	1,5 1,3 8,0 0,6	2,4 1,1 0,9 10,1 1,2	4,88 4,86 4,29 3,42 4,82	F0 A2p B8 K0 F5	3,8 4,3 3,6 5,8 6,8
4323 4327 4328 4346 4368	30 Ophiuchl s Ursae minoris	19 12 3 2 4	204,2 129,0 32,2 21,5 43.0	13 23 19	11 7 25 17 15	14 10 21 18 11	9,9 1,4 2,3	18,6 18,4 1,3 1,3 2,9	14,6 12,9 1,5 1,2 3,9	5,00 4,40 3,92 4,91 3,22	K0 G5 A0 A3 B5	5,1 0,3 2,5 3,6 0,1
4373 4376 4379 4381 4388	α Herculis δ Herculis 41 Ophiuchi π Herculis 68u Herculis	64 6 15 39 1	688,0 64,5 161,2 419,2 10,8	- 2 29 19 -21	6 42 16 24 5	8 44 14 13 9	2,2 22,1	114,8 1,5 10,1 17,5 2,2	86,0 1,5 11,5 32,2 1,2	3,48 3,16 4,82 3,36 4,6 to 5,4	Mb A2 K0 K5 B3	0.7 4,3 3.9 0,3 1,5
4391 4419 4423 4425 4438	o Herculis	2 4 29	21,5 21,5 43,0 311,7 279,5	- 2 19	17 14 19 18 21	19 12 27 15 13	14,7	1,3 1,5 2,3 17,3 13,3	1,1 1,6 1,6 20,8 21,5	4,80 4,14 4,61 4,44 4,48		3,9 2,0 4,7 -2,6 1,1
4443 4458 4460 4459 4479	β Draconis	3 3 10	236,5 32,2 32,2 107,5 32,2	4 23 49 - 3	7 34 40 52 6	14 27 27 78 6	59,1 1,4 2,2	33,8 0,9 0,8 2,1 5,4	16,9 1,2 1,2 1,4 5,4	2,99 4,98 4,95 2,14 3,79	A5 A5 A5	-1,0 6,0 6,1 4,2 -1,7
4483 4487 4497 4500 4504	y Ophiuchi	35 8 3	64,5 376,2 86,0 32,2 53,8	8	36 41 105 21 40	48 34 139 27 45	1,9 15,7 0,8 4,0 1,2	1,8 9,2 8,2 1,5	1,3 11,1 0,6 1,2 1,2		G5 A0	7.4 3.9 8.0 3.3 6.7
4531 4535 4538 4541 4542	# Horoulis	22 17 90	268,7 236,5 182,7 967,5 53,8	0 20 17	29 16 28 41 18	22 13 22 20 12	9,6 - 9,1 56,9 17,9	23,6	48,4	3,99 3,82 2,42	100 K0 K5	4,3 -2,1 3,6 -0,4 -2,5
4544 4545 4547 4548 4552	66 Ophluchi 93 Herculis	17	53,8 21,5 182,7 32,2 32,2	4 2		3t 7 11 8 17	45,6 16,1 2,0	2,7 15,2 5,4	3,1 16,6 4,0	4.8 4.7 3.9	B3 K0 B5p	5,5 1,2 0,1 -0,4 1,5

N-		Hypothe-		t ed=	Spectro	Spectral	Sen	i dinmet	ers	myin	Spectral	
No Boss PGC	Name	radius (unit is 0",0001)	107,5 × radius	l rig parallax -71	praphic parallax	proper motion parallax π <sub>8</sub>	$\frac{d_1}{2}$	<u>d</u> <sub>2</sub> 2	$\frac{d_8}{2}$	(Har vard)	Class (Harvard)	H
4556	95 Herculis	5	53,8	15	8	10	3,6	6,7	5,4	4,42	G5, A3	
4571	70 Ophiuchi .	13	139,7	192	190	251	0,7	0,7	0,6	4,07	K0	9.3
4580	71 Ophruchi	12	129,0	4.0	12	11		10,8	11,8	4,73	G5	1,7
4581 4584	72 Ophtuchi o Herculis	5 4	53,8	40	42	33	1,3 (14,3)	1,3	1,6 6,1	3,73 3,83	A3 A0	-3.8
4304	o Hercuns .	4	43,0	3		7	(14,3)		0,1	2,03		- 3,2
4590	102 Herculis .	2	21,5			9			2,4	4,32	B3	0,5
4591	δ Ursae mmoris	2	21,5	16	18	18	1,3	1,2	1,2	4,44	A O	3,0
4635 4636	74 Ophruchi	10 16	107,5 172,0		8	13		13,4 15,6	11,9 13,2	4,92 4,98	G 5	0,8 3,9
4638	η Serpentis .	23	247,2	65	54	50	3,8	4,6	4,9	3,42	Ko	8,2
4639	z Lyrae	17	1900	12	41	16	15,2	4,5	11,4	4,34	Ko	2,2
4656	109 Herculis	20	182,8	12	40	27	17,9	5,4	8,0	3,92	Ko	6,5
4670	o Draconis	2	21,5	7	19	16	3,1	1,1	1,3	4,24	AOp	1,8
4671	b Draconis	2	21,5	36		31	0,6		0,7	4,85	A2	3,9
4672	¿ Draconis .	10	107,5	118	123	105	0,9	0,9	1,2	3,69	F8	7,7
4686	42 Draconis	12	129,0	24	18	14	5,3	7,2	9,2	4,99	ко	5,1
4707	d Draconis .	7	75.3	6		11	12,5		6,8	4,95	F8p	0,2
4722	α Lyrae .	19	204,2	124	123	129	1,6	1,7	1,6	0,14	AO	2,8
4747 4749	ε <sup>1</sup> Lyrae	3	21.5 32,2	1		16	_		1,4	4,68	A 3	3,7 3,5
4752	ζ¹ Lyiae	6	64,5	28	32	20	2,3	2,0	3,2	4,06	A3, A3	1,5
4753	110 Herculis	6	64,5	54	69	61	1,2	0,9	1,1	4,26	F 5	6,9
4756	β Scut1.	12	129,0	18	9	10	7,2	14,3	12,9	4,47	Go	1,5
4758	Lyrae .	11	118,2		19	12		6,2	9,8	4,92	KO	2,2
4761	111 Herculis	3	32,2	54	33	28	0,6	1,0	1,1	4,37	Λ3	4,8
4776	β¹ Lyrae	.6	64,5	-14						4,96	Bap	2,1
4790 4797	o Draconis	17	182,7	11	13	15	16,6	14,1	12,2	4,78	Ko	4,4
4799	113 Herculis Draconis	9	96,7 118,2	20	22	6 11	4,8	4,4	0,6	4,56	G 5, A 3	-1,9 2,6
4800	δ² Lyrae	35	376,2		7	8		53,8	47,0	4,52	Mb	-0,5
4802	O Serpentis,	4	43,0	24	22	21	1,8	1,9	2,0	4,10	A5, A5	3,1
4814	R Lyrae	25	268,7	6	7	14	44,8	38,4	19,2	4,32	Mb	3,8
4823	s Aquilae	18	193,5	21	20	19	9,2	9,7	10,2	4,21	Ko	4,2
4824	γ Lyrae v Draconis .	5	53,8	11	21	17	4,9	2,6	3,2	3,30	Aop	-2,2
4825		16	172,0	-20		14	_		12,3	4,91	Ko	4,0
4858	ζ Aquilae	6	64.5	40	34	36	1,6	1,9	1,8	3,02	AO	3,1
4859	λ Aquilae	4	43,0	38	1	31	1,1		1,4	3,55	B9	3,4
4897 4906	η Lyrae 1 Vulpeculae .	2 2	21,5		5 7	4 4		4,3	5,4	4.46	B3 B5	-3,2
4909		23	247,2	38	34	28	6,5	7,3	5,4 8,8	4,60 3,24		-2,4 3,9
4912	Δ.Τ.											
4912	ν Lyrae	23 17	247,2 182,7	7 35	11 27	12 22	5,2	22,5 6,8	20,6	4,46 3,98	Ko Ko	-0,5 4,6
4940	r Draconis .	18	193,5	12	16	48	16,1	12,1	4,0	4,63	1	8,0
4942	3 Vulpeculae .	2	21,5		9	6	-0,.	2,4	3,6	4,92	3	0,8
4948	π Draconis	2	21,5	16	22	18	1,3	1,0	1,2	4,63	A2	2,9
4949		1	10,8		4	5		2,7	2,2	4,86		0,4
4953	δ Aquilae .	8	86,0	57	56	54	1,5	1,5	1,6	3,44		5,6
4962 4976		6	64,5	12	32 12	13	24,0	2,0	5,0	4,86	Fo Ma	0,1
4986		29 43	311,7 462,2	13	29	17	(154,1)	26,0 15,9	18,3	4,63 3,24	Ko	5,8 -2,0
	1 , ,,,	13	,,,,,,			17}	1,,	- 317	27.2		AO	1 4,5

		Hypothe		T-2 -	Spectro-	Spectral	840	diamete	13		S-sc-1	
No. Boss PGC	Name	tioni xadina (unit is 0",0001)	107,5 × milins	Trig parallaz #1	graphic parallax	proper motion perallax	41 2	<u>d,</u>	<u>d,</u> 2	(Her vard)	Spectral Class (Harvard)	H
4988	¿ Cygni	5	53,8	5	28	28	10,8	1,9	1,9	3.94	A2	4,4
4992 4995	β Cygni μ Aquilae	1 19	10,8	24	5 21	21	8.5	2,2 9,7	2,7 9,7	4,85	B3 Ko	-2,1 6,7
4998	9 Vulpeculao	2	21,5	41	12	4	6,3	1,8	5,4	4,88	B8	-2.1
5004	Aquilao .	3	32,2		9	10		3,6	3,2	4,28	B5	0,4
5009	a Draconia	10	107,5	181	158	201	0,6	0,7	0,5	4,78	Ko	11,1
5014	& Cygnl	4	43,0	70	57	49	0,6	0,8	0,9	4,64	F5	6,6
5021 5023	φ Cygnl	11	118,2	14	15	13 16	8,4	7.9 9.8	9,1 6,7	4,79	Ko Go	2,5
5027	β Sagittae .	14	150,5	12	15	15	12,6	10,0	10,0	4,45	Ko	2,3
5047	y Aquilac .	63	677.2	18	30	17	37.6	22,6	39,8	2,80	K2	-1,5
5048	o Cygnl	6	64.5	28	42	22	2,3	1,5	2,9	2,97	AO	2,0
5052 5058	δ Sagittae ζ Sagittae	46	494,5	3 24	16	10	(164,8) 0,9	30,9 1,7	1.4	3,78 4,95	Ma, AQ	-1,4 2,4
5062	oaliupA	20	215,0	204	145	152	1,1	1,5	1,4	0,89	A5	5,0
5068	12 Vulpooniae	2	21,5		6	8		3,6	2,7	4,91	Вз	2,2
5071	η Aquilao	14	150,5	6	5	5	25,1	30,0	30,0	3,5 to	G <sub>0</sub> p	-0,9
5079	Druconis	14	150,5	14	26	20	10,7	5.9	7.5	3,99	K0	3.7
5086	13 Vulpoculae	2	21,5	9	16	17	2,4	1,3	1,3	4.50	.▲0	2,5
5089	& Aquilae	12	129,0	38	16	15	3,4	8,1	8,6	4,86	Ko	5,4
5093	β Argulino	14	150,5	78	90	115	1,9	1.7	1,3	3,90	Ko B3	7.3
5102 5103	22 Cygn!	16	172,0	16	42	19	10,7	1,8	9,0	4,87	Ko	0,3 2,6
5105	y Cygni	2	21,5	5	17	19	4.3	1,3	1,2	4,80	A3	3,3
5118	y Sagittae	46	494,5	10	25	18	49,4	19,8	27.5	3,71	IX 5	2,7
5132	15 Vulpooniae	3	32,2	30	20	11	1,1	1,6	2,9	4,74	A.5	3,3
5153	Q Draconis	26	279,5	- 8	16	15	-	17.5	18,6	4,66	K0	3,2
3170	b Cygni	2 4	21,5 43,0	15	19	13	2,9	2,3	3.3	4,82 3,37	B2p	0,9
5171 5182	Q Aquilao	2	21,5	1.3	22	17	4,7	1,0	1,3	4,96	A0	4,3
5186	nt Cygni	2	21,5	9	15	7	2,4	1,4	3,1	4,96	A2	1,1
5187	o <sup>a</sup> Cygnl	32	344,0	- 2	8	11	-	43,0	31,3	3,95	K0, B8	
5188	ba Cygni Vulnoculao	2	21,5	1	18	18		1,2	2,7	4,98	B3	4,8
5190 5191	33 Cygnl	4	43,0	42	6	28	1,0	7,2	1.5	4,32	A3	4,4
5195	23 Vulpeculae		322,5	15		12	21,5		26,9	4.73	K5	2,9
3199	# Cophel	2	21,5	11	16	16	2,0	1.3	1,3	4,40	H9 K0. A3	1.7
5200	32 Cygnl   P Cygni		354.7 53.8	- 2 -21	8 6	4		9,0	13.5	4,16	Bip	-2,3 0,9
5208 5229	7 Cygnl	4.0	247,2	- 2	8	7	-	30,9	1313	2,32	F8p	-5.3
5235	39 Cygnl		279.5	16	15	13	17.5	18,6	21,5	4,60	K2	2,7
5255	41 Cygn!	6	64,5	-19	9	11	-	7,2	5.9	4,09	Г5р	-0,9
5265	e Cygnl		10,8		30	24	1	1,8	2,1	4,89	B3	2,7
5270 5272	# Caphei		53,8 32,2	1	10	111	(32,2)		2,9	3,98	B5	1,2
5279	47 Cygni	1	483.7	6	5	8	(80,6)		60,5	4,85	K 5, A	
1282	Dolphini		32,2	15	23	16	2,1		2,0	4,69	F5	4,0
5291	# Delphini		86,0	24	45	52	3.6 (26,9)		7.7	3,72 4,51	Ko	1,8
5294 8304		10	107,5		17	17	(21,5)			4.78		3,6
μ, . <b>.</b>	071 Copheid variable, 7		t value (re									

		Hypothe		nt	Spectro	Spectral	Sem	i diamete	rs	773 (n	Spectral	
No Boss PGC	Name	radius (unit is 0 ',0001)	107,5 × 13dius	frig parallax n	graphic parallax	proper motion parallax $\pi_4$	$\frac{d_1}{2}$	d <sub>3</sub>	$\frac{d_3}{2}$	(Har yard)	Class (Harvard)	11
5310 5320 5323 5331 5334	α Delphini α Cygni δ Delphini 52 Cygni y <sup>1</sup> Delphini	4 13 5 17 13	43,0 139,7 53.8 182,7 139,7	21 5 11 13 31	21 29 25 32	24 24 15 26	2,0 27,9 4,9 11,1 4,5	2,0 1,9 7,3 4,4	1,8 2,2 12,2 5,4	3,86 1,33 4,53 4,34 4,12	B8 A2p A5 K0 G5	2,9 8,7 3,3 1,5 5,6
5336 5344 5346 5350 5361	ε Cygnı Cepheı η Cepheι / Cygnı 55 Cygnı	32 8 21 2 7	344,0 86,0 225,7 21,5 75,3	41 41 71 27 18	51 62 92 12	47 57 158 6 3	8,4 2,1 3,2 0,8 4,2	6.7 1.4 2.5 1.8 18,8	7,3 1,5 1,4 3,6 25,1	2,64 4,63 3,59 4,47 4,89	K0 G0 K0 B5 B2	6,1 6,5 8,2 -0,1 -1,6
5373 5375 5393 5410 5431	31 Vulpeculae 57 Cygni v Cygni f <sup>1</sup> Cygni £ Cygni	3 3 51	118,2 21,5 32,2 32,2 548,2	27 7 6	9 8 17 3 6	16 7 10 3 8	4,4 4,6 91,4	13,1 2,7 1,9 10,7 91,4	7,4 3,1 2,0 10,7 68,5	4,76 4,68 4,04 4,86 3,92	G5 B3 A0 B0p K5	4,8 1,0 1,0 -0,6 -1,9
5436 5443 5452 5455 5460	f <sup>2</sup> Cygnı γ Equuleı ζ Cygnı δ Equuleı τ Cygnı	26 4 19 6 8	279,5 43,0 204,2 64,5 86,0	13 23 24 60 50	8 19 15 59 46	7 32 9 52 63	21,5 1,9 8,5 1,1 1,7	34,9 2,3 13,6 1,1 1,9	39,9 1,3 22,7 1,2 1,4	4,88 4,76 3,40 4,61 3,82	K5 Fop K0 F5 Fo	0,6 5,9 -3,2 7,0 7,1
5461 5469 5471 5480 5489	α Equules σ Cygns υ Cygns α Cephes 1 Pegass	8 4 2 8 20	86,0 43,0 21,5 86,0 215,0	35 1 16 83 25	30 61 30	22 7 9 60 20	2,5 - 1,3 1,0 8,6	2,9 1,4 7,2	3,9 6,1 2,4 1,4 10,7	4,14 4,28 4,42 2,60 4,24	F8, A3 Aop B3p A5 K0	4,2 -1,2 1,7 3,6 4,6
5522 5532 5543 5546 5563	2 Pegası  \$\beta\$ Cephei  \$\textit{g}\$ Cygni  72 Cygni  9 Cephei	34 3 12 19 4	365,5 32,2 129,0 204,2 43,0	10 7 6 12	13 6 29 15 4	8 6 19 15 3	36,6 4,6 21,5 17,0	28,1 5,4 4,4 13,6 10,7	45.7 5.4 6,8 13,6 14,3	4,76 3,32 4,22 4,98 4,87	K5 B1 K0 K0 B2	0,9 -1,3 4,2 5,8 -1,6
5580 5584 5587 5590 5592		1 64 6 17 7	10,8 688,0 64,5 182,7 75,3	2 45 10	26 57 11 34	4 29 54 12 32	(344,0 1,4 18,3 2,9	1,1	2,7 23,7 1,2 15,2 2,4	4,78 2,54 4,45 4,52 4,27	Ko Ko	-1,3 -0,5 7,1 1,8 1,9
5593	μ Cepher	73	784,7	11	7	5	71,3		156,8	3,92-1 4,53	Ma	-4,0
5594 5608 5609 5617	ν Cephei π² Cygni	13 6 2 2	139.7 64.5 21,5 21,5	11	15 19 5 12	3	8,2  5,4	3,4	7,1	4,85 4,46 4,26 5,00	A2p B3	5,8 -4,0 -2,2 3,0
5663 5674 5676 5677 5688	ν Pegası α Aquarıı ξ¹ Cephei	2 32 18 6 7	21,5 344,0 193,5 64,9 75,3	15 9 5 39	30	13	22,9 21,9 1,7	24,2	1,8	4,90 3,19 4,40	GO A3, G	5,7 -0,9
5703 5709 5714 5716 5733	π Pegasi 4 ζ Cephei 5 24 Cephei	4 6 35 9 24		5 5 2 26 7 0	126	28 7 12 3 10	14,	2,5 5 22,1 12,1 18,4	2,3 31,3 9,7	4,38 3,63 4,9 4,6	F 5 2 K0 9 G5 4 K2	5,9 1,5 1,0 2,2 3,1

5532 Cepheid variable The partillar value from the period luminosity curve is 0",022 This attributes an astonishing small diameter (2,9 O) to the star

No.		Hypotho-		Tyles	Spectro-	Spectral	Be	احصعتاه-ان	ers.		0	
PGC	Namo	radies (unit in 0",0001)	× 107,3	Trig parallax **1	graphic parallax #4	proper two lon persites	41	4 2	4 2	(Har- vard)	Spectral Class (Harvard)	H
5742	· Cophol .	5	53,8	46	37	55	1,2	1,5	1,0	4,23	Po	7.5
5746	1 Lecartae	29	311,7	2	15	15	155,8	20,8	20,8	4,22	CO	0,7
5761	y Aquarii	3	32,2	64		28	0,5		1,1	3,97	Λo	4,4
5762 5763	31 Pognal 32 Pognal	1 2	10,8 21,5			9			2,7	4.93 4.88	B3, p B8	-1,2 -1,6
5764	2 Lacortac .	2	21,5	37	11	8	0,6	2,0	2,7	4,66	B5	1,2
5776	# Lacortac	14	150,5	17	26	19	8,9	5,8	7,9	4,58	Ko	6,0
5777	★ Aquarii ,     4 Lacertae	3	32,2			3			10,7	4,64	Bip	-0,4
5779 5790	35 Pogasi	10	32,2 107,5	33	23	12 21	3.3	4.7	2,7 5,1	4,64	B8p Ko	7,5
5793	ζ <sup>τ</sup> Aquarii	9	96,7	13	28	26	7.4	3,5	3,7	4.59	F2	5,8
5805	d Caphal	13	139.7				.,.			(3,7)	F5, G0	-0.9
5804	5 Lacertae ,	44	473,0	5	3	13	94,6	157,6	36,4	4.61	Ko, A	1,2
5810	6 Lacertno .	2	21,5		7	6		3,0	3,6	4,54	<b>B</b> 3	0,1
5813	7 Lacortao	4	43,0	34	ł	31	1,3		1,4	3,85	A0	4,6
5824	η Aquarii .	2	21,5		1	27			0,8	4,13	B8	4,2
5837 5844	9 Lacortao .	3	32,2	20	1	26	1,6	1	1,2	4,83	A.S	5,2
5852	10 Lacortac	24	10,8		١	3			3,6	4,91	Oo 5	-0.3
5853	Pegasi .	4	43,0	- 2	20	16 28	-	15,2	16,1	4,64 3,61	B8	4,6 3,1
5858	o Pognal	2	21,5		19	16		1.1	1,3	4,85	AO	2.6
5865	p Pogasi	21	225,7	- 1	23	17	-	9,8	13,3	3,10	Go	0,9
5874	Pegari	7	75.3	51	61	69	1.5	1,2	1,1	4,31	P5	8,0
5875 5885	λ Pogasi	15	161,2	37 31	15 32	18 24	6,2	10,7	9,0	4,14 3,67	K <sub>Q</sub> K <sub>Q</sub>	3.0 4.6
5891	Cophel .	18	193.5	40	34	24	4.8	5.7	8,1	3,68	Ko	4.4
5899	Cophel		204,2	-	19	13	1,0	10,7	15.7	4.97	Ko	4,0
5910	e Pognal	2	21,5	2	14	17	(10,7)	1.6	1,3	4,95	AO	4,2
5927	Cophei .	22	236,5		13	15	,,	18,2	15,8	4,96	K5	5.1
5933	o Andromodno .	4	43,0	3	16	12	(14,3)	2,7	3,6	3,63	B5, A2p	1,2
5939 5940	β Piscium β Pognal	90	21,5	16	25	6 34	60,5	38,7	3,6	4,58	B5p Ma	0,2 4,6
5942	3 Andromodae		129,0	- 4	19	18	00,5	6.8	28,5	4,91	Ko	6,7
3944	a Pognal .	6	64,5	38	37	36	1,7	1.7	1,8	2,57	AO	1,9
5952	S5 Pograsi	36	387,0	- 3	12	8	-"	32,2	48,4	4,69	Ma.	0,7
5954	56 Pognal	17	182,7	- 5	16	12		11,4	15,2	4,98	Ko	2,9
5955 5966	1 Cassiopojao .	1 2	21,5	0	3	4		7.2	5.4	4.93	Bi	0,3
5975	7 Andromedae	11	118,2	48	19	12		6,2	9,8	4,56	G5 Fo	1,8
5988	y Pisolum	17	182,7	28	24	41	6,5	7,0	4,5	4,62 3,85	K0	6,3 8,2
5993	8 Andromodae	28	301,0		10	9		30,1	33,4	4,99	Ma.	2,9
6000	o Cophal	9	96,7	26	16	14	3.7	6,0	6,9	4.90	G 5	4,0
6005	r Pogani , ,	2	21.5	34		10	0,6	-	2,2	4,65	A 5	2,4
6024 6031	v Pogasi * Piscium .	8 2	86,0	25 41	16	20 29	3,4	4,3	4,3	4.57	G <sub>0</sub>	6,0 5,4
6037	& Pisclum	12	129,0	- 2	16	20		8,1	6,5	4,45	G 5	
6040	q Pognai		139,7	- 8	16	15	_	8,7	9,3	4,67	Ko	5,2 3,6
6016	Cassiopoleo .		21,5	_ 3	10	13		4,3	2,7	4,89	B3	2,1
6071	2 Andromodae		182,7	39	47	32	4,7	3,9	5.7	4,00		7.3
6073	Andromodae .	3	32,2			16		,	,	4,28	B8	1,4

5805. Copheki variable. The period luminosity relation attributes a parallex value of 0",006 to this star.

No Boss PGC	Nume	Hypothe tical radius (unit is 0 ',0001)	107,5 > radius	Trig parallax	Spectro graphic parallax	Spectral proper motion parallax	4 <sub>1</sub> 2	nt diamet	$\frac{d_3}{2}$	m <sub>vis</sub> (Har- vard)	Spectial Glass (Harvard)	н
6077	t Piscium	6	64,5	73	70	87	0,9	0,9	0,7	4,28	F8	8,1
6078	y Cephei	26	279,5	69	69	27	4,1	4,3	10,4	3,42	Ko	4,6
6080	* Andromedae	2	21,5	8		21	2,7		1,0	4,33	A <sub>0</sub>	3,9
6084	? Piscium	3	32,2	30	32	34	1,1	1,0	0,9	4,61	A 5	6,1
6094	78 Pegası	13	139.7	18	17	13	7.7	8,2	10,7	4,98	K0	4,5
6135	g Cassiopejae	18	193,5	29	2	10	6,7	96,7	19,3	4,85	1·8p	0,9
6150	ψ Pegasi	36	387,0		12	11	.,	32,3	35,2	4,75	Ma	3,5
6155	σ Cassiopejae	2	21,5	12	4	5	1,8	5,4	4,3	4,93	132	0,3
6156	ω Piscium	8	86,0	11	37	57	7,8	2,3	1,5	4,03	F 5	5,4

When a scrutiny is made as to the average size and distribution of linear diameters in the pieceding table it will be noted that the mean values for the diameters computed with aid of the trigonometric, spectrographic and spectral-proper motion parallaxes respectively, will on an average agree very well. This is to be expected because the two latter parallax methods are founded upon the trigonometric method and possibly existing systematic errors in  $\pi_1$  are to a certain extent taken over by the series  $\pi_2$  and  $\pi_3$ . But what is remarkable as to the linear diameters is the good agreement in individual cases. Any justified discussion of the material will show that our knowledge of parallaxes evidently has advanced in such a way, that we now can compute the linear diameters of the stars with a high, may, unexpected degree of accuracy. It also seems that the material as to  $\pi_1$  added since 1929 has in the majority of cases increased the agreement between the three series of linear stellar diameters.

A recent investigation by Jesse Greenstein [Haiv Bull 876, p 32 (1930)] reveals the existence of systematic errors in IIlrtzsprung's colour equivalent  $c_2/I$  Greenstein computes the quantity  $c_2/T - c_2/T_1$ , where  $T_2$  is the mean temperature for a cortain spectral class S These quantities show a seasonal variation, which indicates a reddening of the winter stars, probably due to elimatological phenomena. Errors of that kind affect the diameter values to a certain extent and it seems that a rovision of the derivation of the stellar diameters is warranted. On that account an extensive statistical treatment of the data in the preceding catalogue is postponed until such a revision has been undertaken During the mean time the preceding table will represent a summary of our present knowledge as to the distribution of the stellar diameters

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